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1 **A cascading risk model for the failure of the concrete spillway of the**
2 **Toddbrook dam, England during the August 2019 flooding**

3
4 Mohammad Heidarzadeh ^{*1}, Siamak Feizi²

5
6 ¹ Department of Architecture and Civil Engineering, University of Bath, Bath BA2 7AY, UK

7 ² Norwegian Geotechnical Institute, Oslo, Norway
8
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12 * **Correspondence to:**

13 Mohammad Heidarzadeh, PhD

14 Associate Professor

15 Department of Architecture and Civil Engineering,

16 University of Bath,

17 Bath BA2 7AY, UK.

18 Email: mhk58@bath.ac.uk

19 ORCID: <https://orcid.org/0000-0002-1112-1276>
20

21 **Abstract** (250 words)

22 Dam break is considered as a major catastrophe with significant negative economic, social, and
23 environmental consequences, and thus must be prevented at any cost. Here, we report and analyze a near-
24 miss dam break incident in Toddbrook dam, England during the August 2019 flooding, where the spillway of
25 the dam failed putting the entire dam at the risk of failure. A combination of field surveys, desk studies and
26 numerical modelling is applied to analyze the incident and to develop a cascading risk model for the first
27 time. Our hydraulic modelling showed that the spillway was under fast-flowing water having a speed of up
28 to 15.0 m/s. Such a high-speed flow played a major role in the failure of the spillway through facilitating
29 water injection beneath the spillway slabs. The spillway suffered from poor maintenance and was densely
30 vegetated, which most likely undermined the foundation. The spillway was poorly designed as the concrete
31 slabs were relatively thin and unreinforced, the profile of the spillway was not fit for purpose, and the
32 spillway lacked a stilling basin. Due to rapid drawdown, a landslide was generated on the upstream slope of
33 the dam, which was reconstructed through our geotechnical modelling, indicating that a slower pace must
34 have been taken during the process of emptying the reservoir. We developed a cascading risk model which
35 begins with three primary causes of insufficient maintenance, design shortcomings, and the torrential rainfall
36 leading to flooding. Our risk model, which is among the first of its type, would help in preventing future dam
37 failures.

38

39 **Keywords:** Dam Engineering; Hydraulic Engineering; Cascading Risks; Numerical Modelling; Spillway;
40 Flooding.

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42

43 **1. Introduction**

44 Dams are among the oldest structures that have been built since thousands of years ago for different
45 purposes such as supplying water for domestic and non-domestic uses, controlling floods, hydropower
46 generation, supplying water for navigation through waterways, and recreation. These mega infrastructures,
47 that hold back millions to billions of meter-cubed of water in their reservoirs, require continuous monitoring
48 and maintenance to prevent them from potential failures and consequent catastrophes (e.g., Heidarzadeh et
49 al., 2015, 2019). A dam break can be both highly costly and deadly as the large and fast-moving currents,
50 generated by the release of the reservoir water, can wash away communities at the downstream. For instance,
51 the Malpasset Dam Break (France) in 1959, which was a concrete dam with a height of 66.5 m and a
52 reservoir volume of 55 million m³, caused flooding with wave heights of up to 40 m and killed 421 people
53 (Valiani et al., 2002). An example of the failure of an earth dam is the Machchu-2 dam break in India in 1979
54 whose death toll was reported to be as high as 25,000 (Proske, 2018; Kumar and Setia, 2017).

55 Dam failures can occur due to several reasons including overtopping from excessive flooding, technical
56 problems in different dam elements (such as spillways, foundation, slopes), poor management, and natural
57 disasters such as earthquakes (e.g., ICOLD, 1973; Evans et al., 2000; Deangeli et al., 2009; Zhang et al.,
58 2009; Zhou et al., 2015, 2020; Baecher, 2016; Aureli et al., 2021). By analyzing data from historical dam
59 failures, it is established that majority of dam failure incidents belong to earth-fill dams (e.g., Zhang et al.,
60 2009; Aureli et al., 2021). Among various factors contributing to dam failures, an important reason has been
61 the failure of spillways, which can occur due to several reasons including insufficient spillway capacity,

62 blockage of spillways by flood debris, and technical failures of spillway structure such as water injection
63 below the spillway slabs and consequent erosion and scouring (e.g., ICOLD, 1973; Demissie et al., 1988;
64 Koskinas et al., 2019).

65 The Toddbrook earth-fill dam, England, Figure 1, was on the brink of failure in 1-3 August 2019
66 following the failure of the dam's auxiliary spillway (spillway-2 in Figure 1a, b, d) while the reservoir was at
67 the maximum water level due to torrential rainfall and flooding in the area. As seen in Figure 1b,d, part of the
68 left side of the concrete spillway was washed away by the water flow. The dam eventually survived, and the
69 overtopping of the embankment was prevented through rapidly decreasing the reservoir water level by hiring
70 multiple powerful pumps. Figure 1d shows that tens of aggregate bags were employed during the incident
71 and were placed on the damaged part of the spillway in order to prevent progressive erosion of the dam body.
72 The aggregate bags were placed on the spillway using a helicopter (Balmforth, 2020; Hughes, 2020). [Several](#)
73 [authors have studied the incident including Heidarzadeh \(2019\), Balmforth \(2020\), Hughes \(2020\), Mason](#)
74 [\(2020\), Mehta et al. \(2020\), Allman et al. \(2020\), and Lewis et al. \(2020\)](#). This incident was a wake-up call
75 for the safety of dam and reservoir infrastructure in the UK, which highlighted the urgency for reassessment
76 of the structural integrity of these aged infrastructures (Heidarzadeh, 2019).

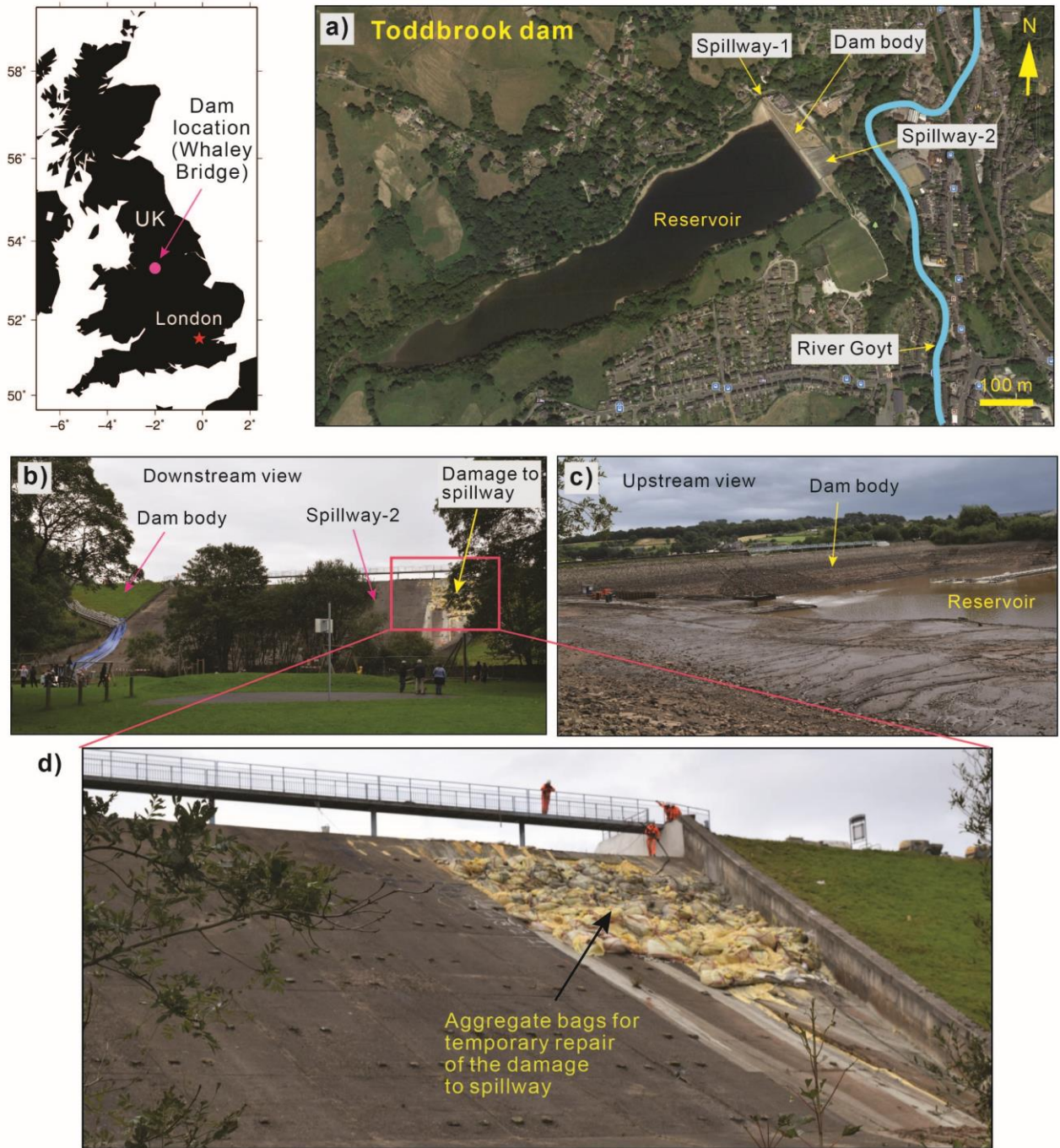
77 Aiming at developing a risk model for the failure of the Toddbrook dam spillway and to prevent future
78 incidents, here we analyze the failure of the spillway through a combination of field surveys, desk studies,
79 and numerical modelling. A one-day field survey was conducted in the dam and reservoir area 10 days after
80 the incident (on 12th August 2019) to observe the situation and to record the impacts of the incident. Here, we

81 report the results of the field survey along with our hydraulic and geotechnical modelling as well as analysis
82 of satellite images to explain the primary causes of this incident. A novel risk model is proposed for the
83 failure of the Toddbrook dam's spillway by benefiting from the concept of cascading risks (Alexander, 2018;
84 Pescaroli and Alexander, 2015; Pescaroli et al., 2018; Kappes et al., 2012; Delmonaco et al., 2006;
85 Carpignano et al., 2009). Such a risk model would be an important tool for planning maintenance works for
86 dam and reservoir infrastructure and preventing potential similar incidents in the future.

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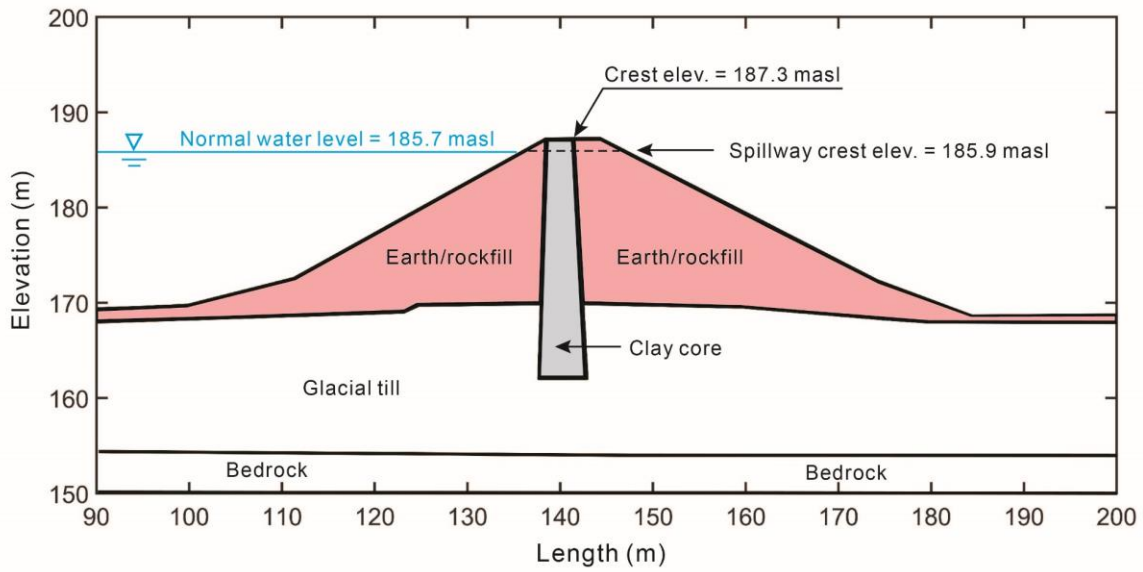
91 **Figure 1.** Location of the Toddbrook dam in the UK and its dam body and two spillways. The damaged part
 92 of the spillway is shown in panels “b” and “d”. The yellow aggregate bags, shown in panel “d”, were
 93 placed at the damaged part of the spillway to stop the spread of the damage as a temporary measure.
 94 Photos in “b”, “c” and “d” are taken during our field survey in August 2019 while panel “a” is from
 95 Google-Earth (<https://earth.google.com>). The pink box in panel “b” is enlarged in panel “d”.

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98 **2. The Toddbrook dam structure, and its spillways**

99 The Toddbrook dam is a zoned earth-fill dam with a clay core acting as its water sealing element (Figure
100 2). The height of the dam is approximately 24 m, its crest length is 310 m, the reservoir capacity is 1.29
101 million m³, and the slope of the upper part of its embankment is 2 (horizontal):1 (vertical), (Balmforth,
102 2020). The dam construction was completed in 1840 and its purpose was to supply water to a nearby
103 navigation canal (Hughes, 2020). The dam was originally equipped with a side channel as its spillway, which
104 is called spillway-1 throughout this report (Figure 3). These types of spillways usually have limited discharge
105 capacities and are susceptible to blockage by flood debris as they are located at a side of the dam and are
106 usually narrow. Therefore, it was concluded that the original spillway does not have enough capacity and a
107 new spillway, called as spillway-2 hereafter (Figure 3), was built in 1970. The new spillway is of chute type
108 with an entrance width of 76 m that extends from the dam crest to the downstream channel connected to
109 spillway-1 (Figure 3) and with 15-cm thick concrete slabs (Hughes, 2020). The crest elevation of spillway-2
110 is 1.4 m below the dam crest elevation. With the combined discharge capacities from the two spillways, it is
111 expected that the dam has been provided with sufficient protection during severe flooding in the area.



112

113

114 **Figure 2.** A cross section of the Toddbrook dam showing different soil elements of the embankment. This
 115 section is produced based on a sketch published by Balmforth (2020). “elev.” is the abbreviated form of
 116 elevation. “masl” stands for meter above sea level.

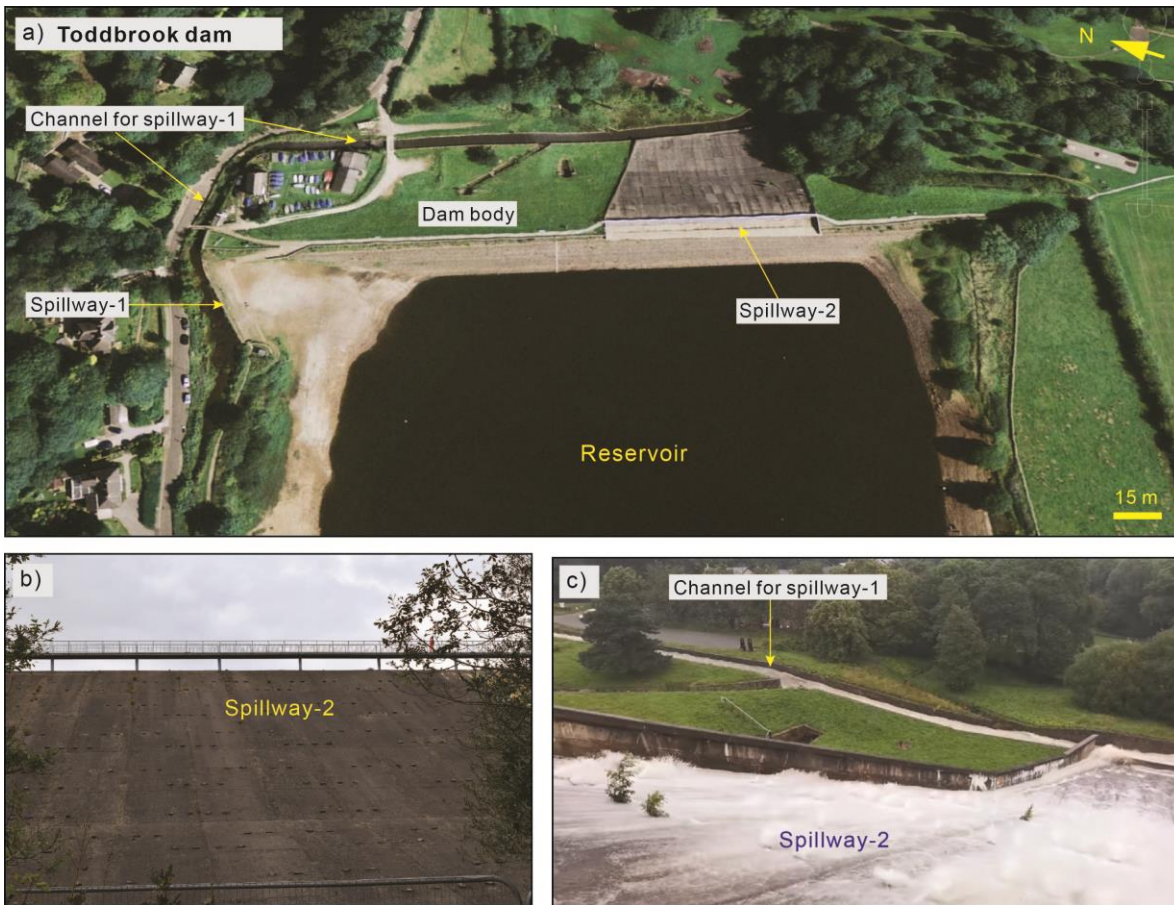
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124 **Figure 3.** The two spillways of the Toddbrook dam named as spillway-1 and spillway-2. Panel “c” is a
 125 snapshot from the video at: www.youtube.com/watch?v=-5I-t7YTkec (YouTube channel of Matthew P.
 126 E. Forrest).

127

128 **3. Discharge capacity of the spillway-2 and the flow velocity distribution**

129 The main risk factor for the safety of spillways is the high flow velocity developed on their surfaces as
 130 spillways release large water volumes during floods. High water velocities could lead to damage to the
 131 concrete surface of spillways through injection of water into the cracks or construction control joints (CCJ)
 132 and by cavitation forces due to objects and obstacles along flow paths. Normally, the concrete surfaces of
 133 spillways are maintained very well through ensuring that they are crack free, obstacle free, and the CCJs are
 134 filled with appropriate elastic materials. These efforts would help to prevent water injection into the joints

135 and cracks and to protect the structure against damaging forces from cavitation.

136 The first step towards protection and maintenance of a spillway is to calculate the discharge rate and flow
137 velocities on the spillway surface under various flow scenarios. The flow discharge over a spillway depends
138 on the reservoir water level and the height of water above the crest level of the spillway (H in Figure 4) and
139 the discharge coefficient of the spillway (C_d). Here, we apply the following equation for calculating the
140 discharge rate (Haan et al., 1994):

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$$142 \quad Q = \frac{2}{3} b C_d \sqrt{2g} H^{3/2} \quad (1)$$

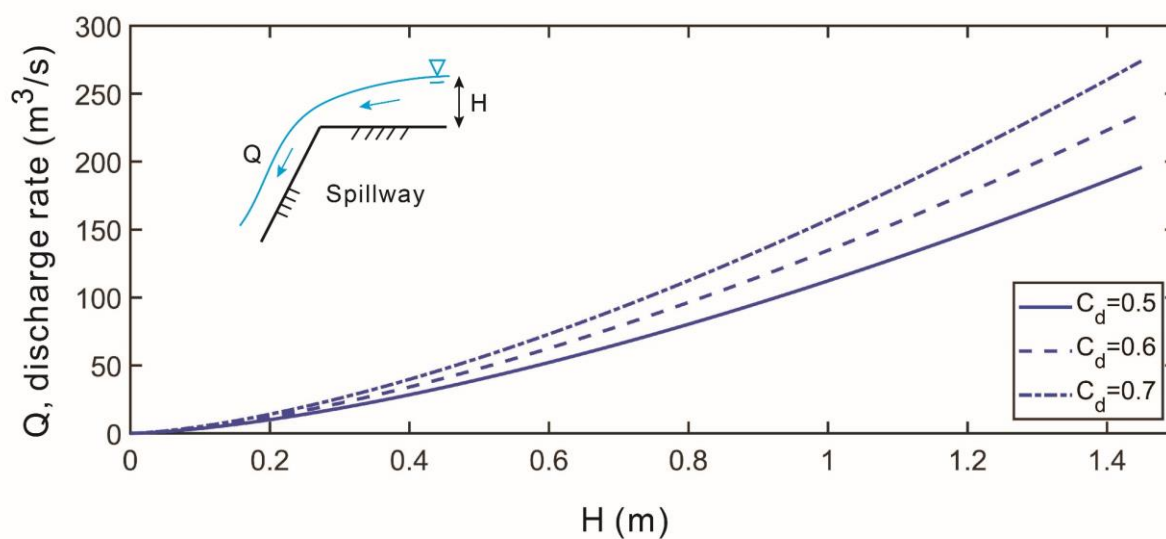
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144 where, Q is discharge in m^3/s , C_d is discharge coefficient, which is assumed to be in the range of 0.5 – 0.7
145 in this study, g ($= 9.81 \text{ m/s}^2$) is gravitational acceleration, b is spillway width ($b = 76 \text{ m}$), and H is water
146 elevation difference between water surface in the reservoir and the crest elevation of the spillway (Figure 4).
147 The result of discharge calculations is shown in Figure 4 indicating that the spillway-2's discharge rates are
148 $177.0 \text{ m}^3/\text{s}$, $134.7 \text{ m}^3/\text{s}$, and $96.4 \text{ m}^3/\text{s}$ for the H values of 1.2 m, 1.0 m and 0.8 m, respectively (assuming
149 $C_d = 0.6$ in Figure 4). The Probable Maximum Flood (PMF) for the design of the Toddbrook dam is reported
150 as being $164.0 \text{ m}^3/\text{s}$ at the reservoir level of 187.1 m (equivalent to $H = 1.2 \text{ m}$) (Hughes, 2020). We note
151 that Equation (1) results in a discharge rate of $177.0 \text{ m}^3/\text{s}$ for $H = 1.2 \text{ m}$; therefore, we assume a PMF of
152 $Q_{PMF} = 177.0 \text{ m}^3/\text{s}$ in this study, which is slightly higher than the PMF reported by Hughes (2020).

153 We calculate the distribution of flow velocity over the spillway-2 for the case of PMF ($Q_{PMF} = 177.0$

154 m^3/s) and another discharge rate of $134.7 \text{ m}^3/\text{s}$. For flow velocity calculations, we use the software
 155 SpillwayPro developed by the US Bureau of Reclamation (USBR, 2019). This program is inputted by the
 156 geometry of the spillway, and the flow characteristics such as discharge rate, and the Manning's roughness
 157 coefficient. The outputs are the flow velocity, pressure, and other flow parameters along the spillway surface.
 158 The outcomes of simulations are shown in Figure 5 for the two discharge rates of $177.0 \text{ m}^3/\text{s}$ (Q_{PMF}) and
 159 $134.7 \text{ m}^3/\text{s}$. The maximum flow velocity developed over the surface of the spillway-2 is approximately 15.0
 160 m/s during the PMF. However, the flow velocity is $7.0 - 10.0 \text{ m/s}$ around the damaged part of the spillway-2
 161 (distance mark of 155 m in Figure 5) for the PMF (Figure 5).

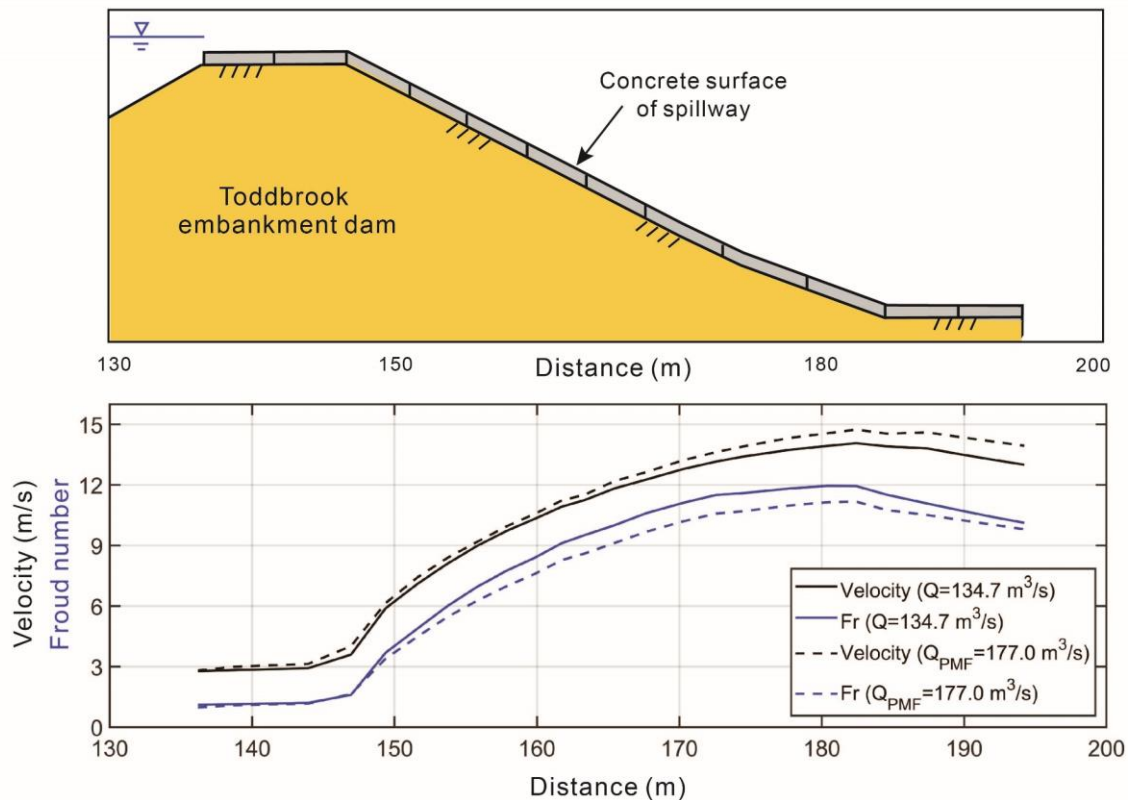
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164 **Figure 4.** The discharge capacity of the Toddbrook dam spillway-2 at different water heights above the
 165 spillway crest level (H) as a function of C_d (discharge coefficient).

166



167
 168 **Figure 5.** Results of water velocity (black) and Froude number (blue) analyses along the concrete surface of
 169 the Toddbrook dam spillway-2 at two water discharges of $134.7 \text{ m}^3/\text{s}$ and $Q_{PMF} = 177.0 \text{ m}^3/\text{s}$.

170

171 4. The causes of the failure of the spillway

172 The causes of the failure of spillway-2 were previously discussed by Heidarzadeh (2019), Balmforth
 173 (2020), and Hughes (2020). In this study, our analysis shows that three factors played roles in the failure of
 174 the Toddbrook dam's spillway-2, which are: insufficient maintenance, design shortcomings and the torrential
 175 rainfall. We call these three factors as primary causes. Each of these primary causes cascaded to a series of
 176 secondary causes, which are discussed in the following sections. A combination of these primary and
 177 secondary causes resulted in the failure of spillway-2. It is known that the cascading mechanisms of hazards
 178 and their interactions play important roles in creating catastrophic events (Pescaroli and Alexander, 2015;
 179 Alexander, 2018; Pescaroli et al., 2018; Heidarzadeh et al., 2021; Adams and Heidarzadeh, 2021). Therefore,

180 such cascading mechanisms and hazard interactions are needed to be discovered. In the following, each of
181 the contributing factors to the Toddbrook dam incident and their cascading effects are discussed in detail.

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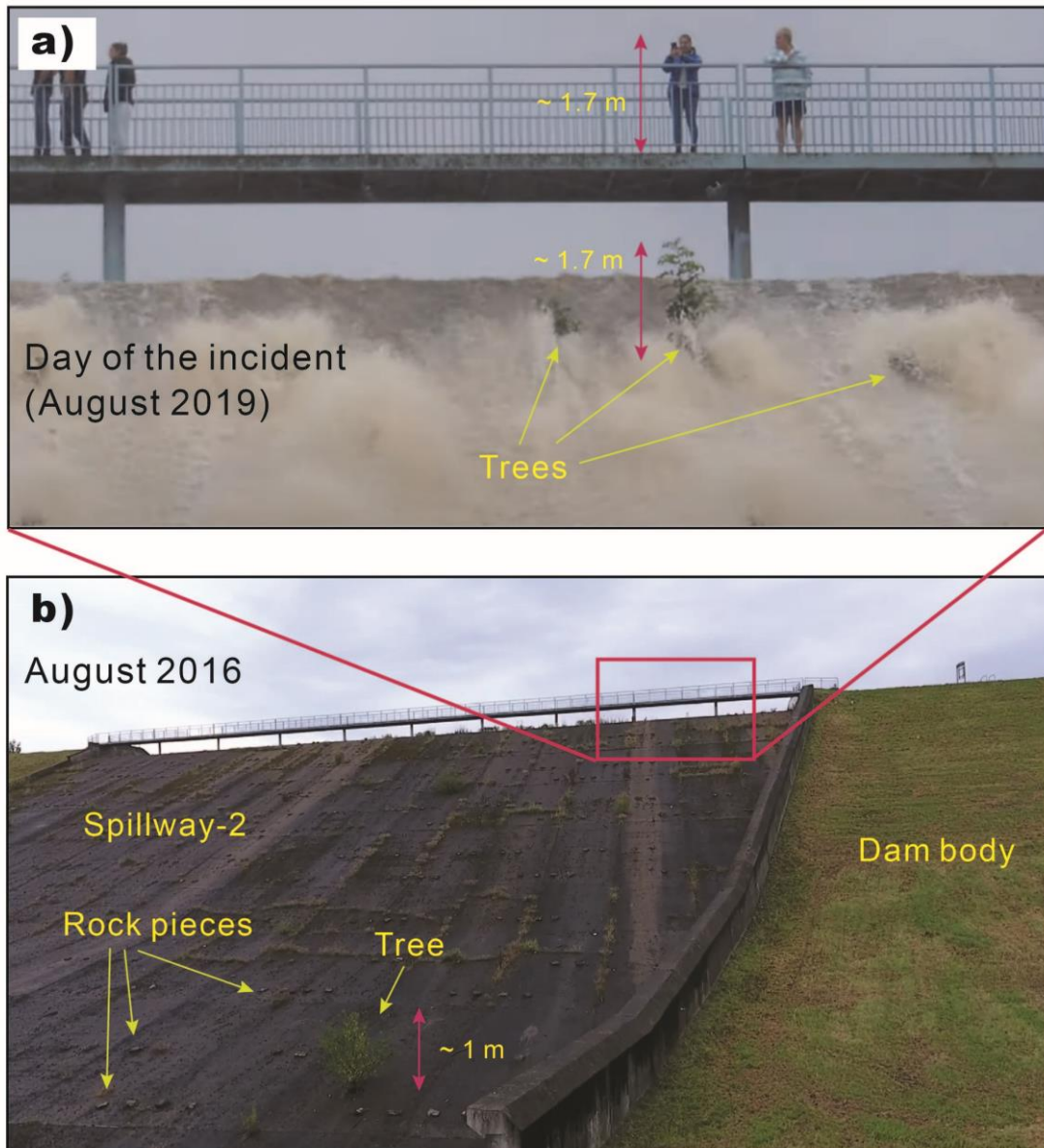
183 **4.1 Insufficient maintenance**

184 The basic and essential design consideration for chute-type spillways (such as spillway-2 of the
185 Toddbrook dam) is that the concrete surface must be smooth, crack free and obstacle free in order to prevent
186 potential damage due to cavitation or water injection beneath the slabs. Sometimes large concrete blocks,
187 known as chute or baffle blocks, are placed on the surface of spillways or at the downstream part of
188 spillways within the stilling basins to reduce the speed of the flow and to help decreasing the length of the
189 stilling basins (USBR, 1987). However, installation of chute and baffle blocks is subject to special design
190 procedures regarding their dimensions, weights, and spacings. The baffle blocks are usually very large, of the
191 height and width of at least a meter or larger (USBR, 1987; Novak et al., 2017).

192 Analysis of photos and videos from the Toddbrook dam incident reveals that the concrete surface of the
193 spillway-2 was in a poor condition at the time of the incident. Dense vegetation including a few trees were
194 present on the surface of spillway-2 when high-speed flow was passing over it during the incident (Figure
195 6a). It is noted that at least three trees, one of them approximately 1.7 m tall, are seen at the damaged part of
196 the spillway during the incident. A review of satellite images of spillway-2 over the period of 1999 – 2020
197 (Figure 7) reveals that the spillway surface was cleaned up of vegetations and trees from time to time. For
198 example, the surface appears to be in a good condition in December 1999 (Figure 7f) and December 2005

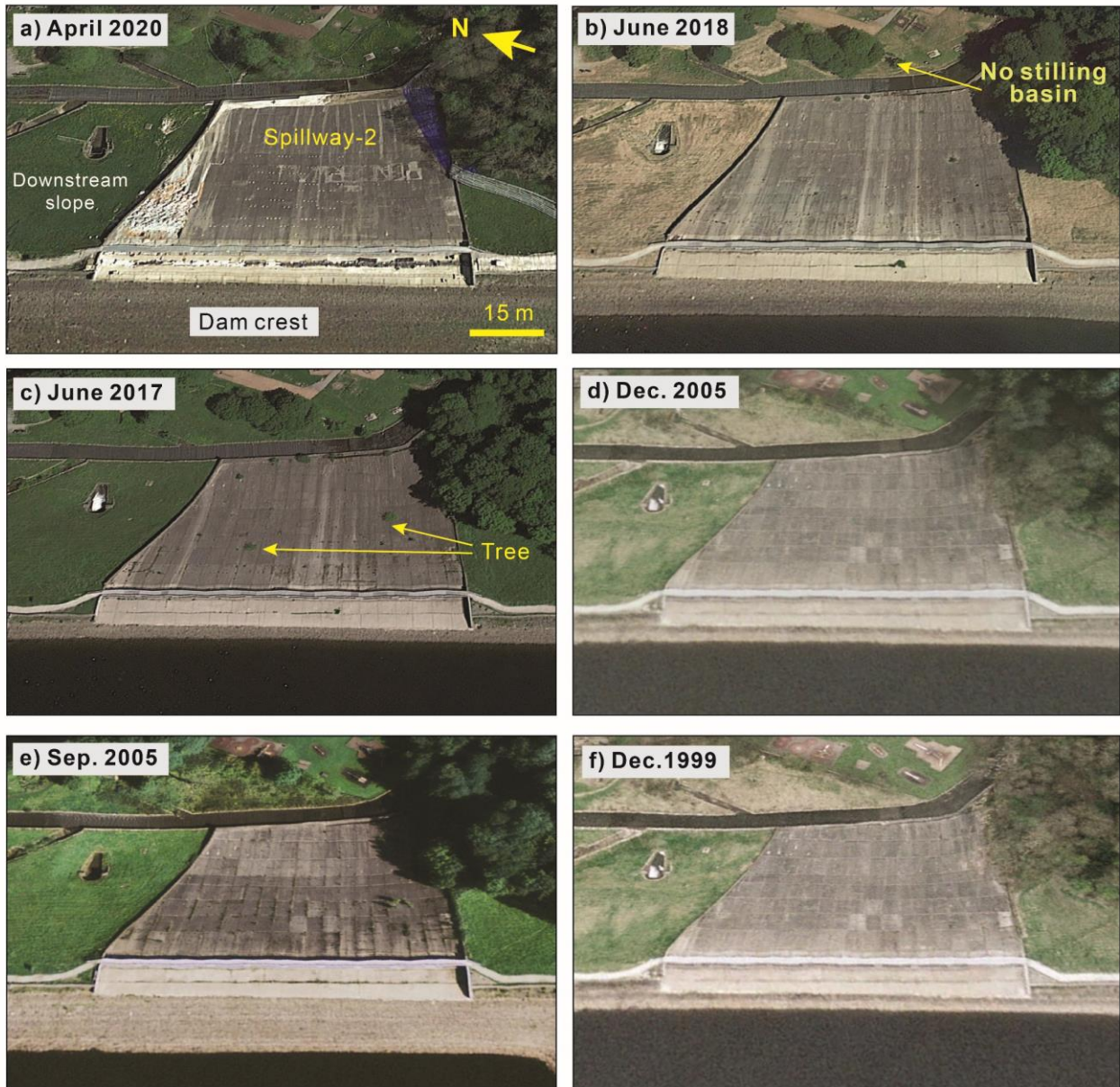
199 (Figure 7b), but it is covered with vegetation and trees in other times (Figure 7b,c,e). It is most likely that the
200 foundation of spillway-2 has been seriously undermined due to the extensive growth of vegetation and trees
201 over years; therefore, the concrete slabs were not resting on a solid foundation. As a result, any water
202 injection beneath the slabs could lead to erosion of the foundation and settlements of the slabs (Figure 8).

203 In addition, the concrete surface of spillway-2 is embedded with numerous rock pieces (Figure 6b) at
204 certain intervals whose dimensions are approximately 22 cm (length) × 22 cm (width) × 22 cm (height)
205 (Heidarzadeh, 2019; Hughes, 2020; Balmforth, 2020) and some of them were removed before or during the
206 incident. It is not clear as why such rock pieces are placed on the spillway surface, but certainly they cannot
207 yield the hydraulic performance of chute blocks due to their small sizes and poor connection to the main
208 slabs. Rather, these small rock pieces could cause cavitation and damaging forces on the main slabs during
209 the passage of high-velocity flows. In addition, removal of some of these rock pieces could lead to increased
210 water injections beneath the slabs (Heidarzadeh, 2019; Hughes, 2020; Balmforth, 2020).



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Figure 6. Photos of the Toddbrook dam’s spillway-2 from the day of the incident in August 2019 (a) and August 2016 (b) showing the growth of vegetation and several trees over the spillway. Photo in “a” is a snapshot from the video at: https://www.youtube.com/watch?v=_pOu5AHJ1U8&t=3s whereas the photo in “b” is from <https://www.youtube.com/watch?v=qQNh2lhYXBM>.



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225 **Figure 7.** Satellite images of the Toddbrook dam spillway-2 at different times before and after the incident
 226 (August 2019) based on GoogleEarth data (<https://earth.google.com/>).

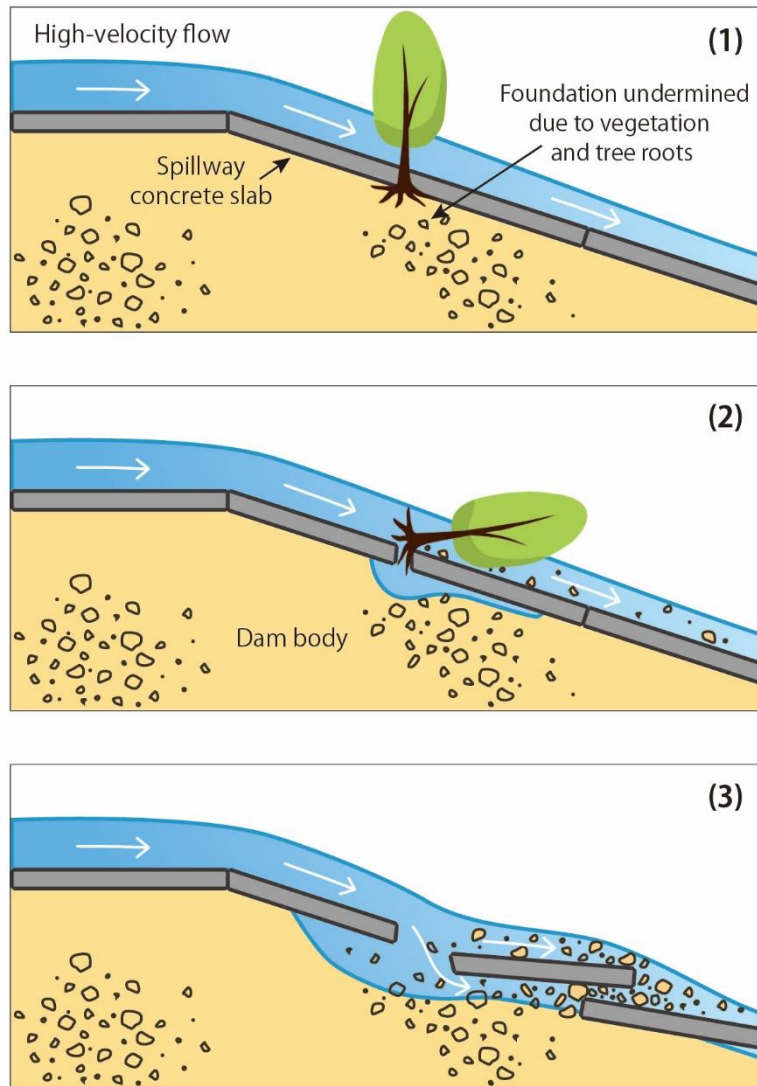
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233 **Figure 8.** Sketch showing the sequence of events leading to the damage to the Toddbrook dam spillway-2 in
 234 August 2019.

235

236 **4.2 Dam design shortcomings**

237 The design and construction of spillway-2 occurred more than half a century ago (in 1970), when the
 238 existing standards and guidelines were not as established as they are today. Our analysis reveals that the
 239 design of spillway-2 is associated with some shortcomings. Modern spillways are made of thick concrete
 240 slabs (a thickness of up to a meter or more) as they are subject to high water velocities (up to 40 m/s for large

241 dams) and negative pressures and forces from cavitation. To minimize the risks of destructive cavitation
242 forces, the profile of spillways is generally made of a multi-slope shape starting with an ogee profile,
243 followed by a combination of mild and steep slopes depending on the specific circumstances of each project.
244 Furthermore, modern spillways are usually equipped with a stilling basin at the foot of the spillway (USBR,
245 1987). It is noted that there is no typical design for spillways, and it may change from one project to another
246 depending on the specifications of each project. The shape of a spillway profile is subject to various design
247 procedures, which includes numerical and physical modelling, to ensure that the structure can discharge the
248 flood water safely without sustaining damage.

249 For the case of the Toddbrook dam, our modelling revealed that spillway-2 experiences a maximum flow
250 velocity of approximately 15.0 m/s at the PMF (Figure 5). The spillway-2 is made of 15-cm thick concrete
251 slabs, which are not reinforced with rebars. Such relatively thin slabs appear to be insufficient; in particular,
252 as they are not reinforced as well. Another potential shortcoming is the profile of the spillway itself. It
253 appears that the profile of the spillway follows that of the downstream slope of the embankment rather than
254 being specifically designed for water flow with large volumetric rates and high speeds. On top of these
255 shortcomings, the spillway lacks any stilling basin (Figure 7b); as a result, severe scouring was observed at
256 the toe of the spillway during the August 2019 incident. We acknowledge that the design and construction of
257 spillway-2 was limited by the slope and shape of the dam body, but this does not justify the design of a
258 spillway that is not fit for purpose. It is because of such restrictions that most of the spillways are moved to
259 dam abutments, which offer adequate space for the construction of a properly-designed structure.

260 **4.3 Torrential rainfall**

261 It is clear that the previous two factors (i.e., insufficient maintenance and design shortcomings) would not
262 come to light given there was no torrential rainfall and flooding in the area. The flooding resulted in the
263 filling of the reservoir to its maximum capacity and consequently in discharge of the excessive water through
264 spillway-1 and later through spillway-2. Although such discharge of flood water through spillway-2 must
265 have been a regular and routine process, it led to the failure of spillway-2 due to its insufficient maintenance
266 and design shortcomings.

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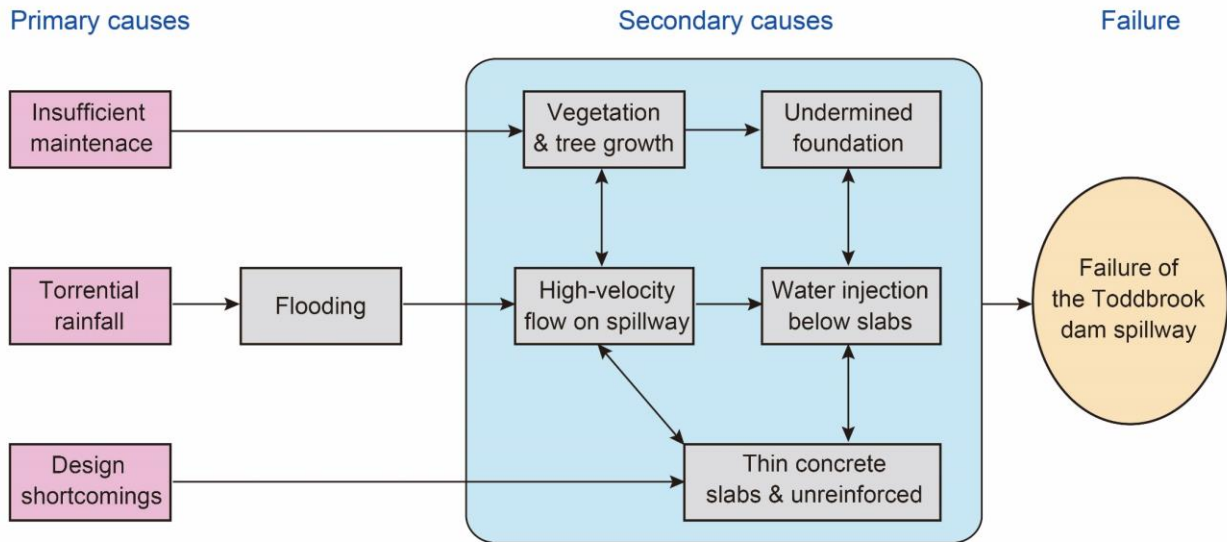
268 **4.4. A cascading risk model for the causes of the damage**

269 We note that any water injection beneath the spillway slabs may not necessarily lead to scouring and slab
270 settlements because such water injections appear to be inevitable, at least at part of spillways during high-
271 speed flows. In fact, the damage or failure of spillways occurs when water injection is combined with an
272 undermined foundation as well as under-designed concrete slabs.

273 In summary, we attribute the failure of the Toddbrook dam spillway to a combination of three primary
274 factors comprising insufficient maintenance, design shortcomings and the torrential rainfall (Figure 9). Each
275 of these factors interacted with each other and cascaded to other causes to produce the failure of the spillway
276 (Figure 9). The construction joints and cracks, generated by vegetation and tree growth, largely facilitated
277 water injection beneath the spillway slabs. In addition, the foundation was significantly undermined over
278 years by extensive vegetation and the concrete slabs were relatively thin and under-designed (only 15 cm

279 thick and unreinforced). It is hard to exactly determine the contribution of each factor in creating the failure,
 280 but it is very likely that the failure was the outcome of a combination and cascade of different factors (Figure
 281 9).

282



283
 284 **Figure 9.** The cascading risk model showing a flowchart of events and various primary and secondary causes
 285 leading to the damage to the Toddbrook dam spillway-2 in August 2019.

286

287 5. Stability analysis of the dam during the incident

288 5.1 Rapid drawdown and landslides

289 As a response to the failure of spillway-2, a rapid drawdown of the Toddbrook reservoir was conducted
 290 during the August 2019 incident as authorities rushed to empty the reservoir by employing multiple powerful
 291 pumps (Table 1, Figure 10b). According to Table 1, the reservoir water level was dropped more than 9.0 m,
 292 and the reservoir water volume was decreased to 17 % of its maximum volume in six days. As a result of
 293 such a rapid drawdown, several minor landslides occurred; the most critical landslide occurred on the

294 upstream slope of the embankment, which has a height of approximately 7.0 m (Figure 10a). Other
295 landslides occurred on the reservoir banks (Figure 10b). These landslides are evidence that the process of
296 decreasing reservoir water level occurred at a high speed, which posed a risk for the safety of the dam.
297 Although the landslides are minor and they did not create major risks, larger movements of the landslide on
298 the downstream slope of the dam could result in a major damage. In addition, large landslides on the banks
299 of the reservoir can generate large waves in the reservoir, which could overtop the dam.

300 However, it is hard to criticize the dam authorities for this rapid drawdown as otherwise the entire dam
301 could fail due to the pressure of a full reservoir, which itself could flood the entire downstream town (i.e.,
302 Whaley Bridge) with potential large deaths and loss of properties. Apparently, it was a difficult choice
303 between accepting the risks of a rapid drawdown and saving the lives and properties of downstream people.
304 At least, it can be said that the process of emptying the reservoir could be done in a safer pace, and through
305 following the existing industry best practices including monitoring the dam and reservoir banks during the
306 process. As per industry best practices, before starting the drawdown, normally the rapid drawdown process
307 is modeled at different paces and a safe pace with an acceptable factor of safety is implemented using which
308 the risks of failure or damage are avoided. Apparently dam authorities did not have enough time to conduct
309 such analyses.

310 To develop a better understanding of risk posed by rapid drawdown, here we model the situation using a
311 modelling package called PLAXIS (Plane strain and axial symmetry; PLAXIS, 2019), which is widely used
312 in Geotechnical Engineering (<https://www.bentley.com/en>). PLAXIS is based on Finite Element Method with

313 an implicit numerical scheme. For our modelling, we use a 2D section of the dam body with fine meshing
314 having approximately 44,000 nodes (Figure 11). In order to find an optimum mesh size for modelling the
315 dam, a few sensitivity analyses were carried out prior to the main analyses. Such sensitivity analyses resulted
316 in a computational mesh with varying grid sizes at different parts of the dam. The mesh sizes are in the range
317 of 0.2 – 5.0 m with an average element size of 1.7 m (Figure 11). Soil properties for different layers of the
318 dam (Figure 2) are presented in Table 2. It is noted that the material properties in Table 2 are based on our
319 geotechnical engineering judgments as there are no available documents for the dam's soil properties. The
320 water is modeled at the level 186.0 masl based on the observations of the dam's water level before the
321 incident.

322 Figure 12 shows the results of dam stability analysis under the rapid drawdown situation. In case of rapid
323 drawdown from water level of 186.0 masl to a water level of 176.0 masl, the failure mechanics is observed at
324 the upstream side of the dam and many local failures and holes are generated resulting in a safety factor of
325 marginally below 1.0 (Figure 12). At the water level of 176.0 masl, however the factor of safety of the entire
326 dam is above 1.0 indicating that the failure of the entire dam is not likely, but parts of the upstream slope of
327 the dam are damaged (Figure 12). This means that the dam operator will need to introduce measures to repair
328 the damaged surfaces. The results of our PLAXIS modelling of the rapid drawdown are consistent with field
329 observations of the dam site following the incident, which identified a landslide on the upstream side of the
330 dam (Figure 10a).

331

332

333 **Table 1.** The timetable of emptying the Toddbrook dam’s reservoir based on data from the dam owner, which
 334 is the Canal and River Trust (Source of data: [https://canalrivertrust.org.uk/news-and-](https://canalrivertrust.org.uk/news-and-views/news/toddbrook-reservoir-update)
 335 [views/news/toddbrook-reservoir-update](https://canalrivertrust.org.uk/news-and-views/news/toddbrook-reservoir-update)). N/A indicates “Not Applicable”.

| Date and time | Reservoir volume based on % of full reservoir | Amount of water level drawdown (m) |
|---------------------------|---|------------------------------------|
| 1 August 2019 | 100 % | 0 |
| 3 August 2019 at 04:00 PM | 83 % | N/A |
| 4 August 2019 at 12:00 PM | 64 % | N/A |
| 4 August 2019 at 08:00 PM | Below 55 % | More than 4 m |
| 5 August 2019 at 11:00 AM | 46 % | 5.7 m |
| 5 August 2019 at 05:00 PM | 38 % | 6.1 m |
| 6 August 2019 at 11:00 AM | 25 % | 8.4 m |
| 6 August 2019 at 07:00 PM | 17 % | More than 9 m |
| 9 August 2019 at 11:30 AM | Below 10 % | N/A |

337

338

339 **Table 2.** Soil properties for different layers of the dam body for modelling the Toddbrook dam. See Figure 2
 340 for different soil layers of the dam. N/A indicates “Not Applicable”.

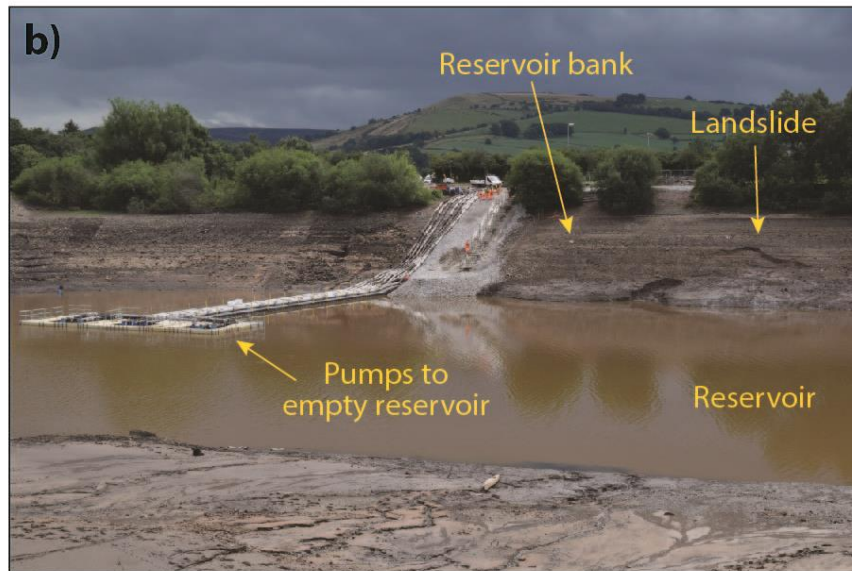
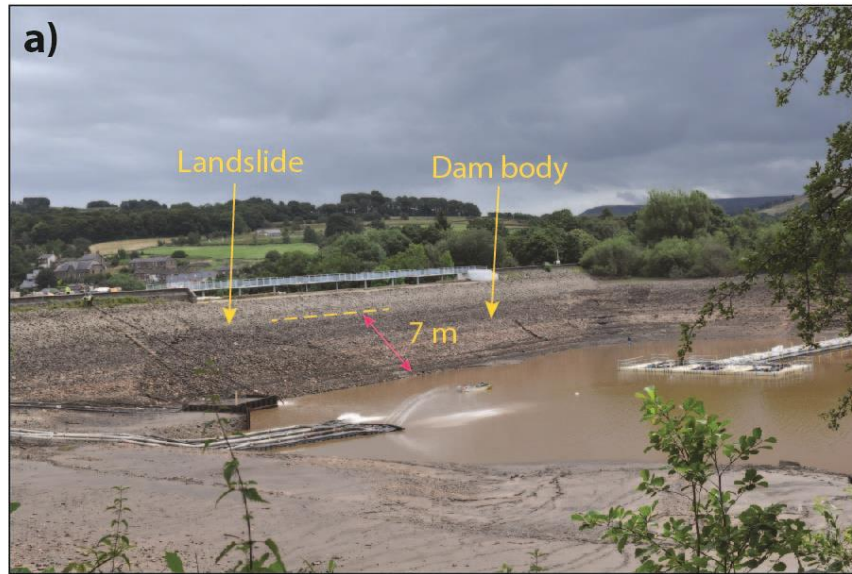
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| Material name/type | Model type | Elastic stiffness (MPa) | Shear strength (KPa) | Friction angle (°) | Material behavior |
|--------------------|----------------------|-------------------------|----------------------|--------------------|-------------------|
| Shell/rockfill | Hardening soil model | 60 | 1 | 42 | Drained |
| Til | Mohr-Columb | 35 | 20 | 37 | Drained |
| Core | Mohr-Columb | 40 | 100 | N/A | Un-Drained |
| Bedrock | Elastic | 1000 | N/A | N/A | Non-porous |

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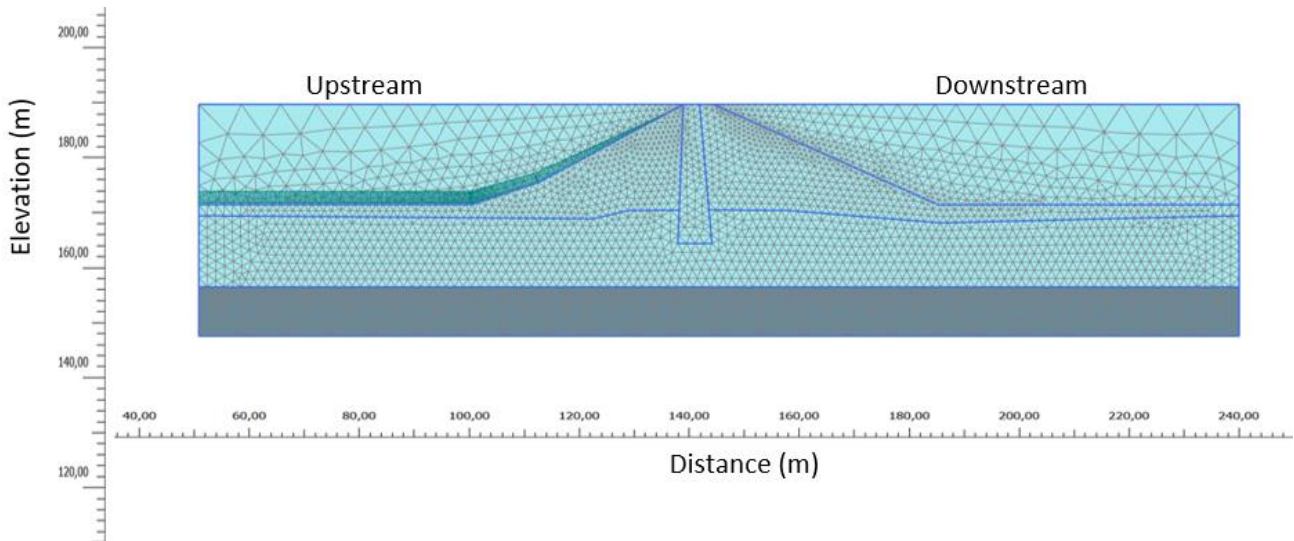
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Figure 10. Several landslides observed following the rapid drawdown of the Toddbrook reservoir in August 2019. a) Photo showing a landslide on the upstream side of the embankment. b) Photo of a landslide in the banks of the reservoir.

358



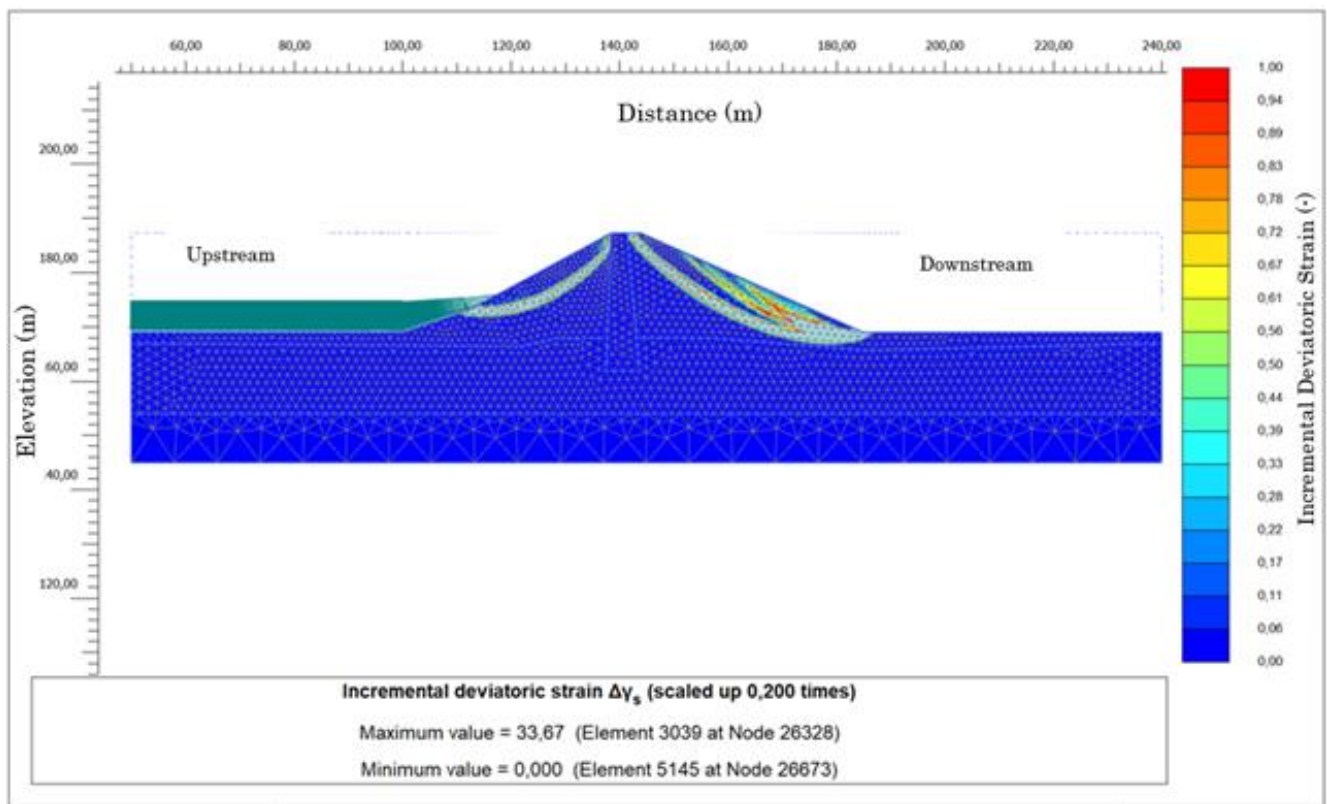
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361 **Figure 11.** An overview of the meshing system with varying grid sizes at different parts of the dam used for
362 modelling the Toddbrook dam using the PLAXIS modelling package.

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367 **Figure 12.** The result of reservoir rapid drawdown analysis of the Toddbrook dam using the PLAXIS
368 modelling package during the August 2019 incident.

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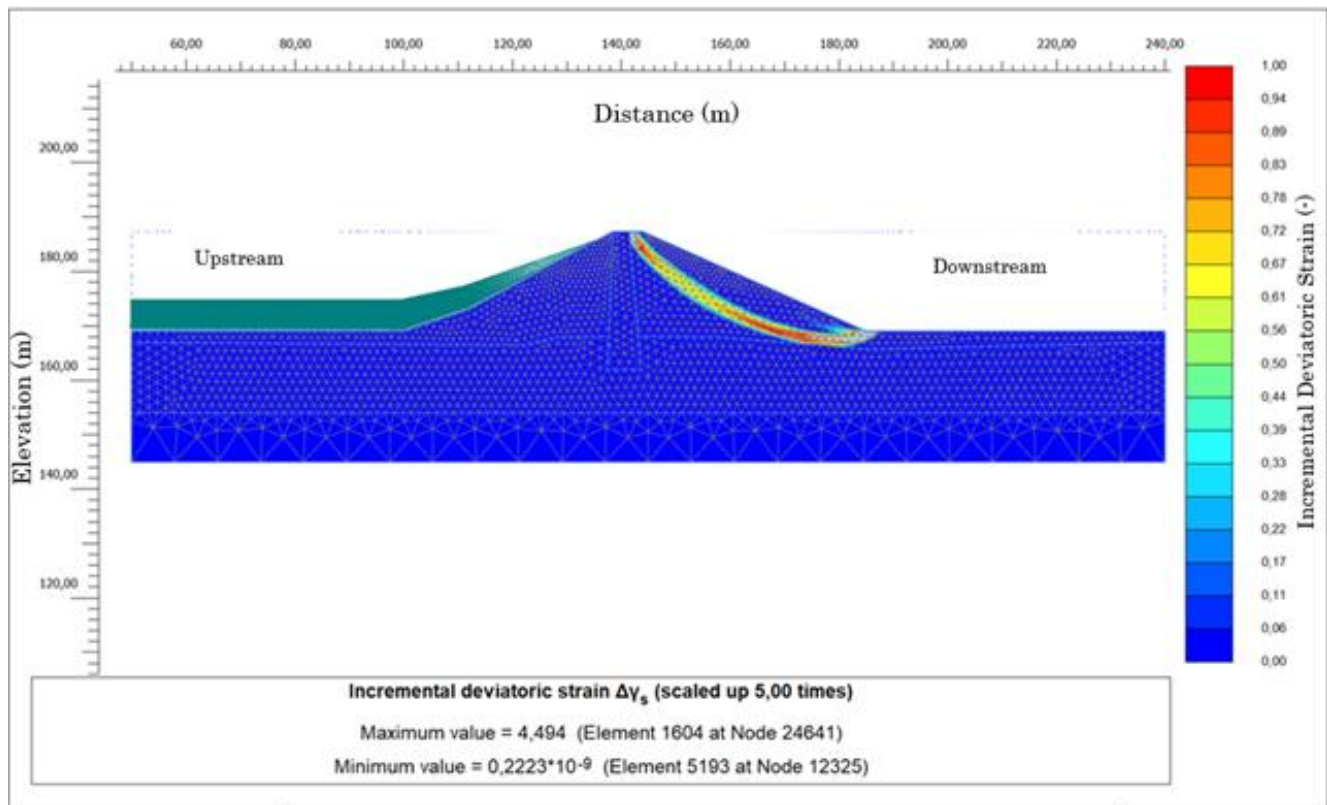
370 **5.2 General stability of the embankment**

371 A major concern during the August 2019 incident was the stability of the dam itself. As the reservoir was
372 near the maximum water level and considering that the dam was approximately 180 years old at the time of
373 the incident, there were concerns about the overall safety of the embankment. Here, we use the PLAXIS
374 modelling package to study the safety factor of the dam under a full reservoir (water level of 186.0 masl).

375 Figure 13 shows the results of the overall dam stability when the water level is at 186.0 masl. Results
376 indicate that, at such a high water level (i.e., 186 masl), the water pressure makes the upstream slope of the
377 dam more stable; therefore, the probability of occurring a failure at the upstream side of dam is low as long
378 as overtopping of the embankment does not occur. It is needless to say that, in case of overtopping, the entire
379 dam could be washed away in a few hours as soil embankments are very vulnerable to flowing water.

380 Analysis shows that the factor of safety at this water level (i.e., 186.0 masl) is marginally above 1.0 and the
381 main failure surface occurs at the downstream side of the dam (Figure 13).

382



383

384 **Figure 13.** General stability analysis of the Toddbrook dam slopes using the PLAXIS software during the
 385 August 2019 incident.

386

387 6. Conclusions

388 We analyzed the failure of the auxiliary spillway (named as spillway-2 in this study) of the Toddbrook
 389 dam during the August 2019 flooding and developed a novel cascading risk model, which explains this
 390 failure. Our study was based on a combination of field surveys, desk studies and numerical modelling. Main
 391 findings are:

- 392 • We calculated a maximum flow velocity of approximately 15.0 m/s over the surface of spillway-2.
 393 Such a high-velocity flow played a major role in the failure of spillway-2 through facilitating water
 394 injection beneath the spillway slabs and cavitation forces.
- 395 • Our analysis showed that spillway-2 was in a poor condition at the time of the incident as dense

396 vegetation and tree growth were present on the spillway surface during the incident. These extensive
397 vegetation and tree growth over years have most likely undermined the foundation of the spillway.

398 • We observed design shortcomings for spillway-2: the concrete slabs were relatively thin and were
399 not reinforced, the profile of the spillway was not fit for purpose, and the spillway lacks a stilling
400 basin.

401 • We identified the primary causes of spillway-2 failure as: insufficient maintenance, design
402 shortcomings and the torrential rainfall. These primary causes cascaded to other causes and resulted
403 in the failure of the spillway through their interactions and combinations.

404 • As the three primary causes of the failure are interconnected, it is not possible to state whether the
405 failure could be prevented given the spillway had a better maintenance because the spillway was also
406 under-designed. However, we may conclude that dam spillways must be designed properly and be
407 maintained adequately and regularly to ensure such failures are prevented.

408 • We observed a landslide on the upstream slope of the dam as a result of the rapid drawdown, which
409 was reconstructed through our geotechnical modelling. This implies that a slower pace must have
410 been taken during the process of emptying the reservoir.

411

412 **Acknowledgements**

413 A number of figures were drafted using the GMT software (Wessel and Smith, 1998). The software
414 PLAXIS (Plane Strain and Axial Symmetry) (<https://www.bentley.com/en/products/brands/plaxis>), used in
415 this study, is licensed to the Norwegian Geotechnical Institute (Norway), where the second co-author is

416 based. We acknowledge University of Bath Institutional Open Access Fund.

417

418 **Data Availability**

419 All data used in this research are provided in the body of the article.

420

421 **Declaration of competing interest:**

422 The authors declare that they have no competing interests regarding the work presented in this paper.

423

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457 [bridge-dam-collapse-is-a-wake-up-call-concrete-infrastructure-will-not-last-forever-without-care-](https://theconversation.com/whaley-bridge-dam-collapse-is-a-wake-up-call-concrete-infrastructure-will-not-last-forever-without-care-121423)

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507

508 **List of Table Captions:**

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510 **Table 1.** The timetable of emptying the Toddbrook dam’s reservoir based on data from the dam owner, which
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513

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515 for different soil layers of the dam. N/A indicates “Not Applicable”.

516

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518 ***** End of Table captions *****

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520

521 **List of Figure Captions:**

522

523 **Figure 1.** Location of the Toddbrook dam in the UK and its dam body and two spillways. The damaged part
524 of the spillway is shown in panels “b” and “d”. The yellow aggregate bags, shown in panel “d”, were
525 placed at the damaged part of the spillway to stop the spread of the damage as a temporary measure.
526 Photos in “b”, “c” and “d” are taken during our field survey in August 2019 while panel “a” is from
527 Google-Earth (<https://earth.google.com>). The pink box in panel “b” is enlarged in panel “d”.

528

529 **Figure 2.** A cross section of the Toddbrook dam showing different soil elements of the embankment. This
530 section is produced based on a sketch published by Balmforth (2020). “elev.” is the abbreviated form of
531 elevation. “masl” stands for meter above sea level.

532

533 **Figure 3.** The two spillways of the Toddbrook dam named as spillway-1 and spillway-2. Panel “c” is a
534 snapshot from the video at: www.youtube.com/watch?v=-5I-t7YTkec (YouTube channel of Matthew P.
535 E. Forrest).

536

537 **Figure 4.** The discharge capacity of the Toddbrook dam spillway-2 at different water heights above the
538 spillway crest level (H) as a function of C_d (discharge coefficient).

539

540 **Figure 5.** Results of water velocity (black) and Froud number (blue) analyses along the concrete surface of
541 the Toddbrook dam spillway-2 at two water discharges of $134.7 \text{ m}^3/\text{s}$ and $Q_{PMF} = 177.0 \text{ m}^3/\text{s}$.

542

543 **Figure 6.** Photos of the Toddbrook dam’s spillway-2 from the day of the incident in August 2019 (a) and
544 August 2016 (b) showing the growth of vegetation and several trees over the spillway. Photo in “a” is a
545 snapshot from the video at: https://www.youtube.com/watch?v=_pOu5AHJ1U8&t=3s whereas the
546 photo in “b” is from <https://www.youtube.com/watch?v=qQNh2lhYXBM>.

547

548 **Figure 7.** Satellite images of the Toddbrook dam spillway-2 at different times before and after the incident
549 (August 2019) based on GoogleEarth data (<https://earth.google.com/>).

550

551 **Figure 8.** Sketch showing the sequence of events leading to the damage to the Toddbrook dam spillway-2 in
552 August 2019.

553

554 **Figure 9.** The cascading risk model showing a flowchart of events and various primary and secondary causes
555 leading to the damage to the Toddbrook dam spillway-2 in August 2019.

556

557 **Figure 10.** Several landslides observed following the rapid drawdown of the Toddbrook reservoir in August
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567 **Figure 13.** General stability analysis of the Toddbrook dam slopes using the PLAXIS software during the
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