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## Impact of bandwidth on antenna-array noise matching

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This letter expands the treatments of wideband noise analysis of antenna arrays by including bandwidth effects on beam-equivalent receiver noise temperature,  $T_{rec}$ , and the active reflection coefficient,  $\Gamma_{act}$ . The particular focus of the letter is on receiver noise decorrelation in wideband systems having noise bandwidth  $f_{\rm B} \gg 1$  Hz. The new analysis and simulations show increase in  $T_{rec}$  and the departure of  $\Gamma_{act}$  from that obtained using contemporary analyses for  $f_{\rm B} = 1$  Hz. Although the paper also shows that for many applications over moderate bandwidths and close connection between the receiver and array the influence of  $f_{\rm B}$ on  $T_{rec}$  is not significant, the simulations of a 71-element array demonstrate that the noise decorrelation due to wide  $f_{\rm B}$  can result in tens of percent (as much as 45.5% in simulations described in this letter) increase in T<sub>rec</sub> above the low-noise amplifier minimum noise temperature, which should be taken into account at the design stage of ultrawide band systems, such as those under investigation by, for example, the Defense Advanced Research Project Agency (DARPA) in its wideband adaptive RF protection (WARP) program and ultra-sensitive active electronically scanned array (AESA) radars for tracking stealth objects.

Introduction: Antenna arrays see ever-expanding application in communications (e.g. emerging 5G and 6G systems, massive, and holographic MIMO systems), radar, radio astronomy, magnetic resonance imaging, remote sensing, signal intelligence, and spectrum sensing [1-11]. Past research showed that minimizing the noise of a receiving antenna array requires the optimum reflection coefficient for minimum noise,  $\Gamma_{opt} \in \mathbb{C}$ , of the receiver front-end low-noise amplifier (LNA) to equal the 'active' reflection coefficient,  $\Gamma_{act} \in \mathbb{C}$ , of the antenna array [12–16]. The determination of  $\Gamma_{act}$  requires the knowledge of beamforming coefficients and the electrical parameters, for example, S-parameters, of the antenna array. However, typically focusing on narrow-band applications, prior analyses did not consider the effects of noise bandwidth on  $\Gamma_{act}$ . As such, a typical noise analysis was performed at a single frequency for a 1-Hz bandwidth and simply extended to wideband by multiplying the resultant noise power by the desired bandwidth.

For each frequency of array operation, the conventional noise analysis proceeds as follows: (a) S-parameters of an antenna array and the LNA are simulated or measured in a 1-Hz bandwidth,  $f_{B0}$ ; (b) noise parameters (NPs) of the LNA are simulated in a 1-Hz bandwidth or measured over a  $\sim$ 1-MHz bandwidth,  $f_{\rm B,np}$ , and the NPs are assumed to be invariant of  $f_{B,np}$ ; (c) noise power at the array output, beam-equivalent receiver noise temperature,  $T_{rec}$ , and  $\Gamma_{act}$  are calculated in a 1-Hz bandwidth based on the results in (a) and (b) and the knowledge of the beamformer coefficients [12, 14–16]; and, if needed, (d)  $T_{rec}$  and  $\Gamma_{act}$  are assumed unchanged over operating noise bandwidth  $f_{\rm B}$ , and the output noise power for  $f_{\rm B}$  is calculated by multiplying the result in (c) by  $f_{\rm B}$ .

Three observations are made: (a) measured S-parameters manifest any propagation delays through the array as phases at each frequency; (b) while wide  $f_{B,np}$  increases the LNA output noise power and accelerates measurements, the assumption of LNA NP invariance on  $f_{B,np}$  is not accurate as it ignores bandwidth-dependent decorrelation of LNA noise sources [17]; and (c) the linear scaling of the output noise power by

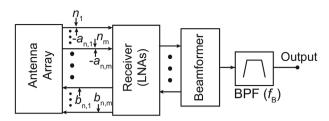


Fig. 1 Block diagram of the network

 $f_B$  may also be inaccurate due to noise decorrelation problem akin discussions in [17]. This last observation has not been investigated in the past for compact arrays, while for physically large antenna arrays, such as single-pixel aperture-synthesis radio telescopes, it is well known that even bandwidths of a few kHz result in noise decorrelation [18]. Therefore, this work investigates  $f_{\rm B}$  impact of noise decorrelation on  $T_{\rm rec}$  and  $\Gamma_{act}$  of wideband compact arrays. Note that as  $f_{\rm B}$  is the noise bandwidth, it may be much narrower than the RF system bandwidth; therefore, in this work "wideband" refers to wide noise bandwidths.

 $T_{rec}$  and  $\Gamma_{act}$  dependence on bandwidth: As already stated above, prior works analyzed array noise temperatures in a 1-Hz bandwidth. While 1-Hz bandwidth is conventional, in practice most array receivers operate with  $f_{\rm B} \gg 1$  Hz. To investigate the impact of  $f_B$  on  $T_{\rm rec}$  and  $\Gamma_{\rm act}$ , we start by considering an *m*-element array representation in Figure 1. The formulations from (31) of [15] describes  $T_{\rm rec}$  as

$$T_{\rm rec} = T_0 \frac{\mathbf{w}^{\dagger} \mathbf{G} \mathbf{R}_{\rm rec} \mathbf{G}^{\dagger} \mathbf{w}}{\mathbf{w}^{\dagger} \mathbf{G} \mathbf{R}_{\rm t} \mathbf{G}^{\dagger} \mathbf{w}},\tag{1}$$

where  $(\cdot)^{\dagger}$  denotes Hermitian conjugate,  $T_0 = 290$  K is the reference temperature,  $\mathbf{w} \in \mathbb{C}^m$  is the vector of *m* beamformer coefficients,

$$\mathbf{G} = \sqrt{R_0} \left( \mathbf{I} + \mathbf{S}_A \right) \left( \mathbf{I} - \mathbf{S}_R \mathbf{S}_A \right)^{-1}$$
(2)

relates the forward waves of the noise emanating from the array ports to the receiver output,  $\mathbf{S}_R \in \mathbb{C}^{m \times m}$  is a matrix of receiver reflection coefficients,  $R_0 \in \mathbb{R}$  is the characteristic impedance, **I** is the identify matrix,  $\mathbf{R}_{rec} \in \mathbb{C}^{m \times m}$  is the receiver noise correlation matrix, and  $\mathbf{R}_{t} \in \mathbb{C}^{m \times m}$  is the array noise correlation matrix. White-thermal-noise waves, which are identified by a vector  $\mathbf{n} = [n_1 \dots n_m]$  in Figure 1 and emanate from the ports of each element of the array, are uncorrelated [19]. On the other hand, the corresponding terms of the two noise wave vectors  $\mathbf{a}_{n} = [a_{n,1} \dots a_{n,m}]$  and  $\mathbf{b}_{n} = [b_{n,1} \dots b_{n,m}]$  that are emanating from each LNA are correlated. This correlation is advantageous and is used for minimizing the receiver noise by appropriately scaling and phasing  $\mathbf{b}_n$ so that when combined with  $\mathbf{a}_n$  in the receiver their correlated portion destructively interfered [20]. This minimization is accomplished by reflecting  $\mathbf{b}_n$  either off an antenna with a reflection coefficient  $\Gamma_s=\Gamma_{opt}$  in a single-antenna system or off an effective reflection coefficient, known as  $\Gamma_{act}$ , when  $\Gamma_{act} = \Gamma_{opt}$  in a multi-element array. To have  $\Gamma_{act} = \Gamma_{opt}$ irrespective of the beamformer coefficients, the array antennas should be fully decoupled. In practical arrays, mutual coupling exists, which results in  $b_{n,1}$  to  $b_{n,m}$  coupling to all antennas in an array and propagating to the system output via multiple paths thereby making the total output power beamformer dependent, and the required destructive interference of  $\mathbf{a}_n$  with  $\mathbf{b}_n$  is beamformer specific and influences  $\Gamma_{act}$ .

As noise waves  $b_{n,1}$  to  $b_{n,m}$  propagate among the *m* elements of the array, they experience delays  $\tau_{delay}$  that consist of the following:  $\tau_{i,j}$ , where  $i, j = 1 \dots m$  and  $i \neq j$ , due to the physical distance between antenna elements;  $\tau_d$  due to the length of the antenna-feed network; and  $\tau_{tx}$  due to any transmission lines that may be used between antenna output ports and the receiver inputs. When delayed,  $\mathbf{b}_n$  correlation with  $\mathbf{a}_n$  becomes dependent on the receiver bandwidth,  $f_{\rm B}$ . Intuitively then, one would expect that the combination of the receiver bandwidth and delays should increase  $T_{\rm rec}$ , since destructive interference requires correlation. It is also expected that in this case  $\Gamma_{act}$  should move closer to the center of the Smith chart, since  $\Gamma_{act} = 0$  is optimum when  $\mathbf{b}_n$  and  $\mathbf{a}_n$  are uncorrelated. An *m*-element antenna array S-parameter matrix,  $\mathbf{S}_{A} \in \mathbb{C}^{m \times m}$ ,

consists of complex elements for each measured frequency that are

determined over a bandwidth  $f_{\rm B0} = 1$  Hz, thereby representing the effects of delays experienced by signals by their associated phases. The effect of the delays,  $\tau_{\rm delay}$ , on  $S_{\rm A}$  at each operating frequency can be represented by the Fourier transforms of delay terms as

$$\mathbf{S}_{A} = \begin{bmatrix} S_{11}e^{-j\omega(2\tau_{d}+2\tau_{tx})} & \cdots & S_{1m}e^{-j\omega(2\tau_{d}+\tau_{1m}+2\tau_{tx})} \\ \vdots & \ddots & \vdots \\ S_{m1}e^{-j\omega(2\tau_{d}+\tau_{m1}+2\tau_{tx})} & \cdots & S_{mm}e^{-j\omega(2\tau_{d}+2\tau_{tx})} \end{bmatrix}.$$
 (3)

We next represent  $\mathbf{R}_{rec}$  in terms of travelling-wave NPs [21, p. 54]  $\mathbf{T}_{\alpha} = E\{\mathbf{a}_{n}\mathbf{a}_{n}^{\dagger}\}/2k_{b}f_{B0}, \mathbf{T}_{\beta} = E\{\mathbf{b}_{n}\mathbf{b}_{n}^{\dagger}\}/2k_{b}f_{B0}, \text{ and } \mathbf{T}_{\gamma} = E\{\mathbf{b}_{n}\mathbf{a}_{n}^{\dagger}\}/2k_{b}f_{B0},$ where  $E\{\cdot\}$  denotes expectation, as [14]

$$\mathbf{R}_{\rm rec} = 2k_{\rm b}f_{\rm B0} \Big( \mathbf{T}_{\alpha} + \mathbf{S}_{\rm A}\mathbf{T}_{\beta}\mathbf{S}_{\rm A}^{\dagger} - \mathbf{S}_{A}\mathbf{T}_{\gamma} - \mathbf{T}_{\gamma}^{\dagger}\mathbf{S}_{\rm A}^{\dagger} \Big).$$
(4)

To determine  $T_{\rm rec}$  for a receiver operating over a bandwidth  $f_{\rm B}$ , the numerator and the denominator of (1) are integrated over  $f_{\rm B} = f_{\rm H} - f_{\rm L}$  to obtain

$$T_{\rm rec} = \frac{\mathbf{w}^{\dagger} \Big[ \int_{f_{\rm L}}^{f_{\rm H}} \mathbf{G} \Big( \mathbf{T}_{\alpha} + \mathbf{S}_{\rm A} \mathbf{T}_{\beta} \mathbf{S}_{\rm A}^{\dagger} - 2 \Re \{ \mathbf{S}_{\rm A} \mathbf{T}_{\gamma} \} \Big) \mathbf{G}^{\dagger} \mathrm{d}f \Big] \mathbf{w}}{\mathbf{w}^{\dagger} \Big[ \int_{f_{\rm L}}^{f_{\rm H}} \mathbf{G} \Big( \mathbf{I} - \mathbf{S}_{\rm A} \mathbf{S}_{\rm A}^{\dagger} \Big) \mathbf{G}^{\dagger} \mathrm{d}f \Big] \mathbf{w}},$$
(5)

where in general each term under the integrals is frequency dependent, and Bosma's theorem [19] was used to expand  $\mathbf{R}_t$  in terms of  $\mathbf{S}_A$ . It is important to highlight here that prior works assumed that over  $f_B$  all terms are independent of frequency and ignored decorrelation between  $\mathbf{b}_n$  and  $\mathbf{a}_n$  thus simply leading to (1).

While previous works [12, 15] have demonstrated that for each LNA #*i* ( $1 \le i \le m$ ) there is a unique  $\Gamma_{act}$ , found from

$$\Gamma_{\text{act},i} = \frac{1}{w_{\text{f},i}^*} \sum_{j=1}^m w_{\text{f},j}^* S_{\text{A},ji},$$
(6)

where  $w_{f,j}^*$  are conjugated elements of  $\mathbf{w}_f \equiv \mathbf{G}^{\dagger}\mathbf{w}$  [15], to limit the number of *m* different LNA designs, in practice all LNAs are designed the same. Therefore, this work also assumes identical LNAs. We then identify the optimum  $\Gamma_{opt}$ , denoted as  $\Gamma_{act}$ , of the LNA that minimizes  $T_{rec}$  in (5) for a given set of beamformer coefficients  $\mathbf{w}$ .

To do this, we first express travelling-wave NPs in terms of conventional NPs,  $T_{min}$  (minimum noise temperature),  $Y_{opt} = G_{opt} + jB_{opt}$  (the optimum admittance for minimum noise), and N (Lange invariant), to obtain [21]

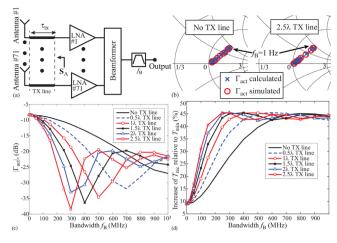
$$\begin{cases} T_{\alpha} = T_{\min} + T_0 \frac{N}{G_{opt}R_0} \left| 1 - R_0 Y_{opt} \right|^2, \\ T_{\beta} = -T_{\min} + T_0 \frac{N}{G_{opt}R_0} \left| 1 + R_0 Y_{opt} \right|^2, \\ T_{\gamma} = T_0 \frac{N}{G_{opt}R_0} \left( 1 + R_0 Y_{opt} \right) \left( 1 - R_0 Y_{opt}^* \right), \end{cases}$$
(7)

where *N* is preferred over another NP  $R_n \equiv N/G_{opt}$  (the noise equivalent resistance) due to its invariance under lossless transformations. Then, in contrast to prior works of assuming *m* different LNAs [14], to minimize  $T_{rec}$ , we find one optimum  $Y_{opt} = R_0^{-1}(1 - \Gamma_{opt})/(1 + \Gamma_{opt})$ , denoted as  $Y_{act} \equiv R_0^{-1}(1 - \Gamma_{act})/(1 + \Gamma_{act})$ , that minimizes  $T_{rec}$  via  $\partial T_{rec}/\partial Y_{opt} = 0$ by first solving for  $B_{act}$  from  $\partial T_{rec}/\partial B_{opt} = 0$  and then for  $G_{act}$  from  $\partial T_{rec}/\partial G_{opt} = 0$  to obtain

$$B_{\text{act}} = \frac{-2\mathbf{w}^{\dagger} \Big[ \int_{f_{\text{L}}}^{f_{\text{H}}} \mathbf{G} \Im \{ \mathbf{S}_{\text{A}} \} \mathbf{G}^{\dagger} df \Big] \mathbf{w}}{R_{0} \mathbf{w}^{\dagger} \Big[ \int_{f_{\text{L}}}^{f_{\text{H}}} \mathbf{G} \Big[ \mathbf{I} + \mathbf{S}_{\text{A}} \mathbf{S}_{\text{A}}^{\dagger} + 2 \Re \{ \mathbf{S}_{\text{A}} \} \Big] \mathbf{G}^{\dagger} df \Big] \mathbf{w}},$$
(8)

$$G_{\rm act}^{2} = \frac{\mathbf{w}^{\dagger} \left[ \int_{f_{\rm L}}^{f_{\rm H}} \mathbf{G} \left[ \left( 1 + R_{0}^{2} B_{\rm act}^{2} \right) \left( \mathbf{I} + \mathbf{S}_{\rm A} \mathbf{S}_{\rm A}^{\dagger} \right) \right) \right]}{R_{0}^{2} \mathbf{w}^{\dagger} \left[ \int_{f_{\rm L}}^{f_{\rm H}} \mathbf{G} \left[ \mathbf{I} + \mathbf{S}_{\rm A} \mathbf{S}_{\rm A}^{\dagger} + 2 \Re \left\{ \mathbf{S}_{\rm A} \right\} \right] \mathbf{G}^{\dagger} \mathrm{d}f \right] \mathbf{w}}$$
(9)

$$-\frac{\left(\left(2\Re\left\{\left(1+j2R_{0}B_{\mathrm{act}}-R_{0}^{2}B_{\mathrm{act}}^{2}\right)\mathbf{S}_{\mathrm{A}}\right\}\right]\mathbf{G}^{\dagger}\mathrm{d}f\right]\mathbf{w}}{R_{0}^{2}\mathbf{w}^{\dagger}\left[\int_{f_{\mathrm{L}}}^{f_{\mathrm{H}}}\mathbf{G}\left[\mathbf{I}+\mathbf{S}_{\mathrm{A}}\mathbf{S}_{\mathrm{A}}^{\dagger}+2\Re\left\{\mathbf{S}_{\mathrm{A}}\right\}\right]\mathbf{G}^{\dagger}\mathrm{d}f\right]\mathbf{w}}.$$
(9)



**Fig. 2** Simulated  $\Gamma_{act}$  and  $T_{rec}$  as a function of  $f_B$  of a 71-element Vivaldi antenna array operating at 1.4 GHz: (a) Block diagram with TX lines; (b)  $\Gamma_{act}$  as function of  $f_B$ ; (c)  $\Gamma_{act}$  [dB] as function of  $f_B$ ; and (d)  $T_{rec}$  as function of  $f_B$ 

Since real and imaginary parts of  $Y_{act}$  in (9) and (8) are functions of delays through  $\mathbf{S}_A$  and bandwidth through the integration, the anticipated dependence of  $\Gamma_{act}$  on the receiver bandwidth is identified. In addition to the bandwidth-dependent decorrelation of  $\mathbf{a}_n$  and  $\mathbf{b}_n$ , the expressions in (5), (8), and (9) also allow us to incorporate frequency variations of  $\mathbf{S}_A$ ,  $\mathbf{G}$ , and NPs that naturally exist in practice and to analyze the effect of bandwidth on  $T_{rec}$  and  $\Gamma_{act}$ .

Simulation results with a 71-element array: We next illustrate the dependence of  $\Gamma_{act}$  and  $T_{rec}$  on bandwidth  $f_B$  using simulations. The simulations were simplified by setting the LNA NPs and the magnitude of  $\mathbf{S}_A$  constant over bandwidth. This simplification was made intentionally to focus strictly on the effects of  $\mathbf{a}_n$  and  $\mathbf{b}_n$  decorrelation on  $\Gamma_{act}$  and  $T_{rec}$ , which is the unique focus of this work. However, the LNA NPs and  $\mathbf{S}_A$  frequency dependence can be readily accommodated by accounting for them in  $\mathbf{T}_{\alpha}$ ,  $\mathbf{T}_{\beta}$ ,  $\mathbf{T}_{\gamma}$ ,  $\mathbf{S}_A$ , and  $\mathbf{G}$  under integrals in (5), (8), and (9). This additional frequency dependence would further exacerbate the impact  $f_B$  on  $T_{rec}$  and  $\Gamma_{act}$ , but would obscure the intended demonstration of the noise decorrelation impact.

In these simulations, a 1.4-GHz EM model of a 71-element dualpolarized Vivaldi focal-plane array for a Square Kilometer Array demonstrator was taken from [22]. Since each polarization has its own beamforming network, the beamformer coefficients associated with the 36 vertically polarized antennas were assigned unity value whereas the 35 coefficients associated with horizontal polarized antennas were set to zero. We introduced delays to the S-parameters by first calculating physical distances between each antenna element and the length of each antenna and then assuming that signals propagate across antennas at approximately the speed of light to calculate the delays. These delays are approximate but sufficient to demonstrate the dependence of  $\Gamma_{act}$ and  $T_{rec}$  on  $f_B$ . Once delays were found, we adjusted the phases of the S-parameters by the phase associated with the calculated delays at 1.4 GHz. By doing so, the combined phase of each element of  $S_A$  at 1.4 GHz remains unaltered.

The receiver was implemented with LNAs from [23] having  $T_{\rm min} = 15$  K and N = 0.024. Note that in this and the previous sections, we make use of noise parameter N [24], which, like  $T_{\rm min}$ , is invariant under lossless transformations and is independent of  $\Gamma_{\rm opt}$ . Therefore, the search for  $\Gamma_{\rm act}$  can proceed by setting LNA  $\Gamma_{\rm opt}$  to each value in a set of 18141 values spread over an entire Smith chart and monitoring  $T_{\rm rec}$  until minimum  $T_{\rm rec}$  is identified. This process of modifying  $\Gamma_{\rm opt}$  is equivalent to employing a lossless matching network between the antenna array and LNAs. The block diagram of the simulated system is shown in Figure 2a, where TX line represents some length of transmission lines, if any, connecting the receiver LNAs to the array. In our simulations, we have used TX lines that are multiple of half of the wavelength,  $\lambda$ , at 1.4 GHz. Such transmission lines do not affect the array S-parameters at the band center but they do introduce delays experienced by noise waves travelling

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through the network. These delays exacerbate the effect of  $f_{\rm B}$  on  $T_{\rm rec}$  and  $\Gamma_{\rm act}$  even though the S-parameters at 1.4 GHz are identical for all such transmission lines.

Once  $\Gamma_{act}$  is found with simulations, it is compared to  $\Gamma_{act}$  found via  $Y_{act}$  from (8) and (9). Figure 2b, demonstrates the results for two different TX lines. As shown,  $\Gamma_{act}$  follow the same trajectory in both cases, but for the longer TX line the rate of change in  $\Gamma_{act}$  position is more rapid as can be deduced from Figure 2c that shows another representation of the results in Figure 2b and for four other TX lines. As expected, the starting points, when  $f_{\rm B} = 1$  Hz, are the same regardless of TX lines, but longer TX lines accelerate the change of  $\Gamma_{act}$  with  $f_{\rm B}$ .

Figure 2d shows the impact of  $f_{\rm B}$  on  $T_{\rm rec}$ . For the array,  $T_{\rm rec}$  is 9% higher than the LNA  $T_{\rm min}$  when  $f_{\rm B} = 1$  Hz, mainly due to array noisematching efficiency [15]. However,  $f_{\rm B} = 200$  MHz results in ~20% increase even when no TX lines between the array and the LNA are inserted. Figure 2d also shows that for a 1 $\lambda$  TX line, there is nearly 20% increase in  $T_{\rm rec}$  over  $T_{\rm min}$  for  $f_{\rm B} = 100$  MHz. This increases to ~31% for a 2.5 $\lambda$  transmission line. It is also observed that for lower  $f_{\rm B}$ , the impact of the TX-line lengths on increase in  $T_{\rm rec}$  is proportional to  $f_{\rm B} \times \tau_{\rm delay}$ as expected [17] until  $\mathbf{a}_{\rm n}$  and  $\mathbf{b}_{\rm n}$  become uncorrelated, and  $T_{\rm rec}$  comes near its maximum. The delay-bandwidth product  $f_{\rm B} \times \tau_{\rm delay}$  is therefore seen as a convenient estimate to the severity of the noise decorrelation problem when scaling systems to wider bandwidths.

Discussion and conclusions: The impact of noise bandwidth on array  $\Gamma_{act}$  and  $T_{rec}$  is investigated. It is shown that as bandwidth increases,  $T_{rec}$  increases to as much as 45.5% of LNA  $T_{min}$  for the 71-element array used in this work. While the increase in  $T_{rec}$  may be insignificant for some applications that operate over a modest noise bandwidth, for ultra-wideband systems, such as a WiGig radio ( $f_B = 2$  GHz), DARPA's WARP radios ( $f_B = 16$  GHz), and ultra-sensitive military AESA radars, full decorrelation of LNA noise waves is very possible, particularly if even short TX lines in an order of 1 cm are used to connect antenna arrays to receivers, resulting in increase of  $T_{rec}$  much higher than would be calculated using prior methods.

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