A TESS Search for Distant Solar System Planets: A Feasibility Study

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TESS (Ricker et al. 2015) monitors the sky through four cameras, each imaging $24^{\circ} \times 24^{\circ}$, with $21''_{11}$ pixels. During its two-year mission, TESS observes most of the sky, omitting within $\sim \pm 6^{\circ}$ of the ecliptic. Each 'sector' is observed for two 13.7 day TESS orbits. In its approved extended mission, TESS will re-observe most of the sky, including two-thirds of the ecliptic, increasing sky coverage to $\sim 94\%$.

The TESS cameras operate in shutter-less mode, taking 2 s exposures. These are combined into pre-selected regions recorded at 2-min cadence and full-frame images (FFIs) recorded at 30-min cadence. Cosmic ray rejection reduces the effective FFI integration time to 1440 s.

Faint objects can be detected by combining FFIs. With TESS, the signal from a solar-color source with magnitude I_C is $S = t_{\exp} A s_0 \times 10^{-0.4I_C}$, where t_{\exp} is the exposure time, $A = 69 \text{ cm}^2$ is the effective area, $s_0 = 1.45 \times 10^6 \text{ ph s}^{-1} \text{ cm}^{-2}$, and the bandpass is 600-1000 nm (Sullivan et al. 2015).

We estimate the noise as $N = \left[S + n_{\text{pix}} Z_L t_{\text{exp}} + n_{\text{pix}} n_r R_N^2\right]^{1/2}$, where n_{pix} is the number of aperture pixels, the zodiacal light is $Z_L \sim 47 - 135 \,\text{ph}\,\text{pix}^{-1}\,s^{-1}$, the number of readouts is n_r , and the read noise is $R_N \sim 10 \,\text{e}^-/\text{pix}$ (Sullivan et al. 2015). At faint magnitudes, zodiacal light is the dominant noise source. The aperture is dictated by the pixel response function (PRF), with 90% ensquared energy within 4 pixels (Ricker et al. 2015).

Figure 1 displays the resulting detection efficiency curves. Combining ~1,300 exposures from a TESS sector, gives a 50% detection threshold of $I_C \sim 22.0 \pm 0.5$. TESS will observe portions of the sky for $\gg 27$ days, increasing the depth.

DIGITAL TRACKING

The curves in Figure 1 also apply to moving objects. Given a *known* orbit, one can predict an object's location in a series of background-subtracted TESS FFIs and sum the flux. Figure 1 demonstrates this for three TNOs.

To discover new objects, with unknown trajectories, we can try *all possible orbits*! Previous searches have demonstrated the power of 'digital tracking' to detect solar system bodies significantly fainter than single exposure limits (Gladman et al. 1998, 2001; Holman et al. 2004; Bernstein et al. 2004).

One can shift a series of images to compensate for the parallax. The remaining proper motion then yields straight line trajectories. By shifting the parallax-compensated images along all plausible linear velocities, one can sum the flux and search for significant peaks in the signal. One only needs an *approximate* orbit. In the case of TESS, the size of the PRF sets the precision with which the signal in the images must be aligned.

The basis of Bernstein & Khushalani (2000) simplifies an exhaustive orbit search. Bernstein et al. (2004) demonstrated this with an HST survey for extremely faint TNOs. The key parameters are the parallax constant $\gamma = 1/d$ for distance d, scaled radial velocity $\dot{\gamma} = \dot{d}/d$, and transverse angular velocities $\dot{\alpha}$ and $\dot{\beta}$. For short time spans, $\dot{\gamma} \approx 0$.

The sky-plane resolution, P, is similar to the pixel scale. The number of angular velocity bins required is

$$N_{\dot{\alpha}} = N_{\dot{\beta}} = 2\dot{\alpha}_{\max} / \Delta \dot{\alpha} \approx 100 \left(\frac{T}{27 \,\mathrm{day}}\right) \left(\frac{d}{25 \,\mathrm{au}}\right)^{-1.5} \left(\frac{P}{21''}\right)^{-1},$$

where α_{max} is the maximum bound angular velocity, T is the span of the observations, and the angular velocity resolution is $\Delta \dot{\alpha} \lesssim P/T$. The number of distance bins is small for TESS (Bernstein & Khushalani 2000; Holman et al.

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Figure 1. Top: Predicted detection efficiency $f = \frac{1}{2} [1.0 - \operatorname{erf}(X/2)]$, where $X = n_{\sigma} - S/N$, and $n_{\sigma} = 5$. The curves correspond to zodiacal light values of 47 ph pix⁻¹ s⁻¹, 135 ph pix⁻¹ s⁻¹, and 270 ph pix⁻¹ s⁻¹. The third value doubles the maximum estimated zodiacal light value, to account for unmodeled noise. We assume $n_{pix} = 4$. Bottom: Differential TESS data stacked around the predicted locations of (90377) Sedna ($I_C \sim 20.2$), 2015 BP519 ($I_C \sim 21.6$), and 2015 BM518 ($I_C \sim 21.6$), left to right. Their S/N values are 11.1, 8, 7, and 7.3, respectively. Images created and processed using FITSH (Pál 2012).

2018):

$$N_{\gamma} = \gamma / \Delta \gamma \sim \left(\frac{T}{27 \text{ day}}\right) \left(\frac{P}{21''}\right)^{-1} \left(\frac{d}{25 \text{ au}}\right)^{-1} \sim 1.$$

The total number of operations is

$$N_{\rm op} = N_{\rm sec} N_{\dot{\alpha}} N_{\dot{\beta}} N_{\gamma} N_{\rm pix} N_{\rm exp} \sim 5 \times 10^{15} \left(\frac{N_{\rm sec}}{26 \, \rm sectors}\right) \left(\frac{T}{27 \, \rm day}\right)^3 \left(\frac{P}{21^{\prime\prime}}\right)^{-3} \left(\frac{d}{25 \, \rm au}\right)^{-4} \left(\frac{N_{\rm exp}}{1,300}\right) \left(\frac{N_{\rm pix}}{16 \, \rm Mpix}\right),$$

where $N_{\rm sec}$ is the number of sectors, $N_{\rm pix} \propto P^{-2}$ is the number of pixels, and $N_{\rm exp}$ the number of exposures. The Bernstein et al. (2004) search required $N_{\rm op} \sim 10^{16}$ operations.

TESS can detect objects at $d \leq 900 \left(\frac{5 \text{ pix}}{n_p}\right)$ au, assuming a minimum $n_p \sim 5$ pixel displacement. The hypothesized Planet Nine (Trujillo & Sheppard 2014; Brown & Batygin 2016), has an expected magnitude of 19 < V < 24 (Fortney et al. 2016; Batygin et al. 2019), raising the possibility that TESS could discover it!

The expected yield of a TESS search for TNOs and Centaurs will be the subject of a future investigation.

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