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Wind Turbine Pitch Actuator Regulation for Efficient and Reliable Energy Conversion: A Fault-Tolerant Constrained Control Solution

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Abstract: Motivated for improving the efficiency and reliability of wind turbine energy conversion, this paper presents an advanced control design that enhances the power regulation efficiency and reliability. The constrained behavior of the wind turbine is taken into account, by using the barrier Lyapunov function in the analysis of the Lyapunov direct method. This, consequently, guarantees that the generated power remains within the desired bounds to satisfy the grid power demand. Moreover, a Nussbaum-type function is utilized in the control scheme, to cope with the unpredictable wind speed. This eliminates the need for accurate wind speed measurement or estimation. Furthermore, via properly designed adaptive laws, a robust actuator fault-tolerant capability is integrated into the scheme, handling the model uncertainty. Numerical simulations are performed on a high-fidelity wind turbine benchmark model, under different fault scenarios, to verify the effectiveness of the developed design. Furthermore, a Monte-Carlo analysis is exploited for the evaluation of the reliability and robustness characteristics against the model-reality mismatch, measurement errors and disturbance effects.

Keywords: Adaptive Constrained Control; barrier lyapunov function; fault-tolerant control; Nussbaumtype function; power regulation; wind turbine benchmark



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1. Introduction

Horizontal Axis Wind Turbines (HAWTs) have dominated the Wind Energy Conversion (WEC) industry over the last few decades [1,2]. Modern HAWTs are designed larger and are located in remote places, e.g., offshore sites, to increase the WEC capacity. The HAWT is a complex highly nonlinear dynamic system [3]. So, in the presence of high wind speed variation, it is challenging to retain HAWT operation with the prescribed WEC efficiency [4]. The high wind speed may cause HAWT out-of-control operation with catastrophic overspeeding of the rotor. In this case, either the HAWT is stalled to stop, or the mechanical brake is engaged. As a result, only a conservative WEC is achieved and the efficiency is cumulatively less than that desired [1].

The HAWT efficiency is a trade-off between capturing the maximum energy and satisfying the structural/operational safety [1]. In this regard, modern HAWT manufacturers define the so-called ideal power curve, which characterizes the HAWT operation with optimal efficiency. The key solution for the enhancement of the HAWT efficiency relies on the development of proper control strategies to retain the operation on the ideal power curve [4]. Accordingly, in high wind speed conditions, the generated power is regulated at its nominal value to maintain safe operation and to avoid overspeeding. This region of operation is known as the full load region, where power regulation represents the main objective. In the HAWT, the power regulation is fulfilled by adjusting the pitch angle of the blades, which leads to regulating the rotor speed [5]. Therefore, it is crucial to control

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the pitch angle such that the rotor speed is kept within the predefined safe-to-operate bound around the nominal value and, consequently, to avoid conservative WEC control solutions [1].

The long-term operation of HAWTs may increase the incidence of pitch actuator faults [1]. The fault occurrence reduces the availability of the plant and increases the WEC cost. Pitch actuator bias, effectiveness loss and dynamic change are the most commonly reported pitch actuator fault types [1,6]. In WTs with hydraulic actuators, the dynamic change is caused by a pressure drop due to hydraulic oil leak, high air content in the oil and pump wear, for those installations using hydraulic actuation. In the case of electric actuators, dynamic change is due, for example, to the wear or ageing of the electric motor, whose response becomes slower due to the friction increase [1,6]. This, in turn, leads to a slower response of the pitch actuator, and, consequently, inefficient power regulation. The pitch actuator bias can be caused when blades are installed to the pitch actuator, and small misalignments can be thus generated. This problem can be present in both electric and hydraulic actuators. The effectiveness loss can be derived from a mechanical fault affecting the electric motor actuating the blades, e.g., some deflection angles (for the complete range of motion) are no longer available due to the wear out of the bearings. The same issue arises also in hydraulic actuators, where the increased friction of the mechanical parts is due to the aging of the hydraulic cylinders. On the other hand, debris build-up and blade erosion are inevitable, which leads to the Blade Aerodynamic Profile Change (BAPC) [1]. These issues motivate the need for maintenance procedures. However, the increased maintenance downtime leads to reduce the power generation rate at a higher cost, especially for offshore installations, due to the reachability difficulties of harsh environments [5]. Therefore, the pitch angle control should integrate fault-tolerance capabilities to compensate possible fault effects [6].

The power regulation control design has gained significant attention and viable solutions are proposed (see, e.g., [7] and the references therein). However, most of the available solutions fail to operate satisfactorily in the presence of pitch actuator faults. Consequently, Fault-Tolerant Control (FTC) has emerged recently and different schemes have been designed, such as robust linear parameter varying control [6], adaptive sliding mode control [5], and fuzzy control [8,9]. Nevertheless, in all the aforementioned works, the constrained rotor speed has not been considered. The constrained HAWT performance may be tackled using Model Predictive Control (MPC) approaches [10–13]. However, as mentioned in [12], if the constraints are selected inadequately the optimization problem is difficult or even impossible to solve, or the closed-loop system may become unstable. Furthermore, most MPC approaches may suffer from the heavy online computation burden as the solution should be obtained between every two sampling times [14]. The pitch angle control design for efficient power regulation represents a long-lasting challenge, i.e., the mathematical relationship between aerodynamic torque and the pitch angle is not completely known as it is a function of the uncertain wind speed variation [1,15]. This is considered as the unknown control gain problem [16]. It is worth noting that wind speed can be roughly measured on-site by an anemometer, placed on the rotor hub, or by Light Detection and Ranging (LiDAR) devices. However, the accurate measurement of the effective wind speed over the blades is impossible, due to spatial/temporal distribution of the effective wind speed over the blade plane, turbulence, wind shear and tower shadow effects, which is even more important for large rotor installations [1,4]. On the other hand, different numerical approaches have been proposed for wind speed estimation (see, e.g., [17] and references therein), though they remain complicated for practical implementation and, thus, ineffective. Finally, BAPC can be tackled by feeding the measured power into a controller with an integral action [18,19]. However, constructing the pitch angle control on the measured power basis requires the design of generator torque control simultaneously, which is mainly reserved for the low wind speed region [1]. Furthermore, in the mentioned works other pitch actuator faults, and consequent unknown control gain are not considered. Actuators 2022, 11, 102 3 of 23

Moreover, the control integral action might be dangerous in the presence of faults, caused by the integration of the error, which can be due to a fault.

Motivated by these considerations, in this paper, a pitch angle control is designed for the safe and reliable power regulation purpose, constraining the rotor speed and the generated power within the safe-to-operate bounds. This is a resolution to the overspeeding and the conservative WEC problems. In the proposed controller the unknown control gain is resolved. Furthermore, the designed control tolerates the pitch angle faults, without the need for complex wind estimation schemes. The main features of the proposed controller are summarized in Figure 1.

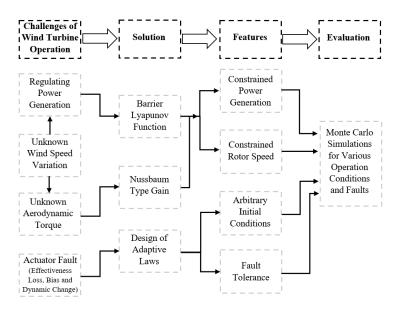


Figure 1. The proposed solution qualitative features.

To highlight the main contributions, the following comments can be drawn.

The unknown control gain problem, due to uncertain wind speed variation, is tackled by utilizing the Nussbaum-type function. In contrast to the available solutions, e.g., [15,17,20], no computationally expensive and complicated algorithm for the wind speed estimation is required. Therefore, this paper presents an industrially viable scheme.

The constrained power generation is achieved in the control design by the development of a Barrier Lyapunov Function (BLF) to constrain the rotor speed and the generated power, with guaranteed stability and no online optimization burden, in contrast to MPC approaches [10–13]. Furthermore, the assumption of bounded initial conditions is relaxed. The control parameter selection is formulated as an offline optimization problem.

The fault tolerance capability is inherently included in the proposed solution. By that means, contrary to [15,21,22], the designed control automatically and systematically compensates for the pitch actuator faults. In this manner, neither fault detection nor control reconfiguration schemes are needed. In contrast to the robust solutions, e.g., H_{∞} optimization [1], in which the worst-case scenario is presumed, the conservatism is avoided.

The rest of this paper is organized as follows. Section 2 briefly recalls the HAWT model with some technical preliminaries. In Section 3, a baseline Nonlinear Adaptive Constrained Control (NACC) approach is constructed, with the assumption of known control gain. This restrictive assumption is relaxed in Section 4 and the Modified NACC (MNACC) approach is proposed. In Section 5, asymmetric time variable constraints are constructed to handle arbitrary initial conditions. The fault tolerance characteristics of the proposed MNACC are analysed in Section 6. In Section 7, the feasibility of the proposed solution is studied. The numerical evaluation is addressed in Section 8, and the results are discussed. Furthermore, a Monte-Carlo analysis is exploited for the evaluation of the reliability and robustness features against the model-reality mismatch and measurement errors. The Monte-Carlo

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analysis represents an effective tool for the preliminary validation of the proposed solution prior to application to real systems. Finally, some concluding remarks and future research issues are summarized in Section 9.

2. HAWT Operational Model and Preliminaries

In this section, the HAWT operational model is briefly introduced with the pitch actuator faults. Furthermore, BAPC is also considered. Finally, some technical preliminaries are given. Hereafter, to simplify the subsequent notation if there is no confusion, function arguments are omitted.

2.1. HAWT Operational Model

The wind energy is converted into the rotor kinetic energy by the blades. The effective wind speed $V_r(t)$ induces the aerodynamic torque $T_a(t)$, thrust $F_t(t)$, and power $P_a(t)$ modelled as [1]:

$$T_{a}(t) = 0.5\rho_{a}\pi R^{3}V_{r}^{2}(t)C_{q}(\beta(t),\lambda(t))$$

$$F_{t}(t) = 0.5\rho_{a}\pi R^{2}V_{r}^{2}(t)C_{t}(\beta(t),\lambda(t))$$

$$P_{a}(t) = 0.5\rho_{a}\pi R^{2}V_{r}^{3}(t)C_{p}(\beta(t),\lambda(t))$$
(1)

where ρ_a and R are the air density and the rotor radius, respectively. Additionally, $C_q(\bullet)$, $C_p(\bullet)$ and $C_t(\bullet)$ are torque, power and thrust coefficients, respectively. These factors are functions of the blade pitch angle, $\beta(t)$, and the tip speed ratio, $\lambda(t)$, defined as $\lambda(t) = R\omega_r(t)/V_r(t)$ [1]. $\omega_r(t)$ is the rotor angular speed. Furthermore, the aerodynamic power is as $P_a(t) = T_a(t)\omega_r(t)$, which leads to the relation $C_p(\bullet) = C_q(\bullet)\lambda(t)$. The effect of $F_t(t)$ on the tower causes a bending oscillation [6]. The displacement of the nacelle is represented by $x_t(t)$, measured from its equilibrium position. The effective wind speed at the rotor plane is then obtained as $V_r(t) = V_w(t) - \dot{x}_t(t)$, where $V_w(t)$ is the free wind speed, i.e., the wind speed before the blades [23].

The kinetic energy of the rotor shaft is transferred into the generator shaft, via the drivetrain, with efficiency η_{dt} and speed ratio N_g . The rotor and generator shafts inertia are represented by J_r and J_g , respectively. Furthermore, the rotor and the generator speeds are denoted by $\omega_r(t)$ and $\omega_g(t)$, respectively. Moreover, the drivetrain is modelled as a two-mass system, including the torsion stiffness K_{dt} and the torsion damping B_{dt} . Therefore, a torsion angle $\theta_\Delta(t) = \theta_r(t) - \theta_g(t)/N_g$ is considered, where $\theta_r(t)$ and $\theta_g(t)$ are the rotation angle of the rotor and generator shafts, respectively. On the other hand, the bearings of the rotor and generator shafts impose the viscous friction, modelled by the coefficients B_r and B_g , respectively. The generator converts kinetic energy into electrical energy. Additionally, between the generator and the electrical grid, a converter is placed, regulating the power frequency [6]. The internal electronic controller of the generator is much faster than the HAWT mechanical dynamic behaviour. So, it is reasonable to assume that the generator torque $T_g(t)$ is adjusted according to the generator reference torque fast enough to ignore the generator dynamic response. As a result, the electrical power $P_g(t)$ can be approximated by the following static function [6]:

$$P_{g}(t) = \eta_{g}\omega_{g}(t)T_{g}(t) \tag{2}$$

where η_g is the generator efficiency. The power regulation objective can be stated as the generation of the nominal power $P_{g,N}$ under uncertain wind speed variation, while avoiding overspeeding and consequent brake engagement. Accordingly, taking Equation (2) into account, this objective is achieved by the following operation requirements: (i) setting $T_g(t)$ at its nominal value $T_{g,N}$; (ii) regulating $\omega_g(t)$ at its nominal value $\omega_{g,N}$.

The nominal power generation is then achieved as $P_g(t) = P_{g,N}$, where $P_{g,N} = \eta_g T_{g,N} \omega_{g,N}$ [6]. The operation requirement (i) can be simply fulfilled by setting the generator reference torque at $T_{g,N}$. The operation requirement (ii) can be fulfilled by the pitch angle control. In this manner, the induced aerodynamic torque is controlled.

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Consequently, the rotor and the generator angular speeds are regulated [5]. Therefore, the main objective of this paper is to satisfy the requirement (ii).

In order to reduce drivetrain stress, the drivetrain torsion angle variation $\theta_{\Delta}(t)$ is to be kept as small as possible. In this regard, the ideal case can be stated as $N_g \omega_r(t) = \omega_g(t)$, i.e., keeping the rotor and generator speeds at the drivetrain ratio [24]. As the generator speed is kept at $\omega_{g,N}$, then the rotor speed is maintained at $\omega_{r,N} = \omega_{g,N}/N_g$. This represents the reduced drivetrain stress trajectory. Accordingly, the HAWT operational model is given by [16]:

$$\ddot{\omega}_r(t) = c_1 \omega_r(t) + c_2 \omega_g(t) + c_3 T_a(t) + c_4 T_g(t) + a_3 \dot{T}_a(t)$$
(3)

where,
$$c_1 = a_1^2 + a_2b_1$$
, $c_2 = a_1a_2 + a_2b_2$, $c_3 = a_1a_3$, $c_4 = a_2b_3$, $a_1 = -(B_{dt} + B_r)/J_r$, $a_2 = B_{dt}/N_gJ_r$, $a_3 = 1/J_r$, $b_1 = \eta_{dt}B_{dt}/N_gJ_g$, $b_2 = (-\eta_{dt}B_{dt}/N_g^2 - B_g)/J_g$ and $b_3 = -1/J_g$.

Considering Equations (1) and (3), the pitch angle control leads to the adjustment of $C_q(\beta(t),\lambda(t))$, and consequently, the aerodynamic torque. This, in turn, regulates the rotor speed. The aerodynamic torque is not a singular function in the operational range of HAWT [16]. By that means, in the presence of wind speed variation, there always exists a given pitch angle $\beta^*(t)$, and by setting the reference pitch angle $\beta_{ref}(t)$ at $\beta^*(t)$, the consequent aerodynamic torque leads to the nominal power generation [23]. Therefore, the pitch angle controller has to maintain the reference pitch angle $\beta_{ref}(t)$ at $\beta^*(t)$, which retains ω_r at nominal values $\omega_{r,N}$. This, consequently, regulates $\omega_g(t)$ at $\omega_{g,N}$, which meets the operation requirement (ii). However, due to uncertain wind speed variation, retaining ω_r exactly at $\omega_{r,N}$ is impossible and there is always an error [1]. Therefore, the main aim of this paper is to retain the tracking error as close as possible to zero within the safe-to-operate bounds, i.e., to avoid hazardous overspeeding.

As this work considers a hydraulic pitch actuator, it moves the blades to regulate $\beta(t)$ at the actuated angle $\beta_u(t)$. The pitch actuator is modelled as [5]:

$$\ddot{\beta}(t) = -\omega_n^2 \beta(t) - 2\omega_n \xi \dot{\beta}(t) + \omega_n^2 \beta_u(t) \tag{4}$$

with the natural frequency ω_n and the damping ratio ξ . The pitch actuator operational ranges are limited as $\dot{\beta}_{min} \leq \dot{\beta}(t) \leq \dot{\beta}_{max}$ and $\beta_{min} \leq \beta(t) \leq \beta_{max}$. In this paper X_{max} and X_{min} indicate the maximum and minimum allowable value of the variable X, respectively. Note that HAWT operation in a harsh environment may lead to pitch actuator dynamic change, which reduces the power regulation efficiency. This causes the variation in the natural frequency and the damping ratio of the pitch actuator, which in turn leads to a slower pitch actuator response [6]. The dynamic change is modelled by the additive signal $f_{\beta}(t)$ in the pitch actuator model, defined later [5]. Moreover, the pitch actuator may suffer from bias, and effectiveness loss. These lead to the deviation of the actuated pitch angle $\beta_u(t)$ from the reference one $\beta_{ref}(t)$, defined by the pitch angle controller [16], modelled as:

$$\beta_u(t) = \rho(t)\beta_{ref}(t) + \Phi(t) \tag{5}$$

with the unknown pitch actuator bias $\Phi(t)$ and the unknown effectiveness $\rho(t)$ [9]. Note that $0 < \rho \le \rho(t) \le 1$, where $\rho(t) = 1$ represents full effectiveness and $\rho(t) = 0$ is total loss [9,25]. More importantly, ρ is an unknown lower bound of the actuator effectiveness, below which the actuator is unable to keep controlling the system and it practically becomes uncontrollable [26]. The signal $\beta_{ref}(t)$ is the reference pitch angle, which is generated by the pitch angle controller. Clearly, in the case of full effectiveness and no bias, $\beta_u(t) = \beta_{ref}(t)$. Associating the pitch actuator dynamic behaviour of Equation (4), with the pitch actuator dynamic change, bias and effectiveness loss, yields:

$$\ddot{\beta}(t) = -\omega_n^2 \beta(t) - 2\omega_n \xi \dot{\beta}(t) + \omega_n^2 \rho(t) \beta_{ref}(t) + \omega_n^2 \Phi(t) + f_{\beta}(t)$$
(6)

Environmental situations, such as rain, snow and dirt, lead to erosion or debris buildup on blades. This, in turn, causes BAPC. As a result, the captured aerodynamic power is Actuators 2022, 11, 102 6 of 23

reduced [15]. Consequently, the power regulation is not efficiently achieved. BAPC can be modelled as an aerodynamic torque change $f_{T_a}(t)$, due to a change in the power coefficient described as $\widetilde{C}_p(t) = C_p(\beta(t), \lambda(t)) + \Delta C_p(t)$ [18]. These changes are challenging to detect due to their slow-developing (incipient) characteristics. Therefore, it is difficult to determine if the decreased generated power is due to BAPC or reduced wind speed. However, as BAPC occurs slowly, this change is mostly assumed to be solved by the planned annual maintenance, when the blades are cleaned or replaced. Therefore, this paper aims to design a pitch angle controller that is insensitive to BAPC, thus guaranteeing nominal power generation up to the next planned maintenance.

Considering Equations (1) and (3), the rotor dynamic relation is represented by a non-affine function of the pitch angle [23]. As stated earlier, $T_a(t)$ is not a singular function. Accordingly, this problem is resolved by using the mean value theorem [15], i.e., for any given pair of $(V_r(t), \omega_r(t))$, there exists $\Xi \in (0, 1)$ such that $T_a(t) = T_a(t)|_{\beta^*(t)} + (\beta(t) - \beta^*(t)) T_{a,\beta}(t)|_{\beta_k(t)}$, where $T_{a,\beta}(t) = \partial T_a(t)/\partial \beta(t)$ and $\beta_k(t) = \Xi \beta(t) + (1 - \Xi)\beta^*(t)$. It is worth noting that $-L \le T_{a,\beta}(t) \le -U < 0$, with constants 0 < U < L. It can be seen that as effective wind speed V_r increases, by increasing pitch angle, the aerodynamic torque decreases. Therefore, by taking the time derivative of $T_a(t)$, the following relation is obtained:

$$\dot{T}_a(t) = \dot{\beta}(t)T_{a,\beta}(t) + f_{T_a}(t) \tag{7}$$

where $f_{T_a}(t)$ is an aerodynamic torque change due to BAPC [18]. Moreover, it is worth noting that, as the wind speed is not accurately measurable, $T_{a,\beta}(t)$ in Equation (7) is an unknown variable. Now, by using Equations (6) and (7) in Equation (3), one can obtain:

$$\ddot{\omega}_{r}(t) = c_{1}\omega_{r}(t) + c_{2}\omega_{g}(t) + c_{3}T_{a}(t) + c_{4}T_{g}(t) + a_{3}f_{T_{a}}(t) - \frac{a_{3}\omega_{n}T_{a,\beta}(t)}{2\xi}\beta(t) + \frac{a_{3}\omega_{n}T_{a,\beta}(t)}{2\xi}\beta(t) + \frac{a_{3}\omega_{n}T_{a,\beta}(t)}{2\xi}\rho(t)\beta_{ref}(t) + \frac{a_{3}\omega_{n}T_{a,\beta}(t)}{2\xi}\Phi(t) + \frac{a_{3}T_{a,\beta}(t)}{2\xi\omega_{n}}f_{\beta}(t),$$
(8)

This describes the HAWT rotor dynamic response, which takes into account possible pitch actuator dynamic change, bias, effectiveness loss and BAPC. It is worth noting that the HAWT sensor is affected by measurement error, modelled by stochastic processes. For the sake of notation, the measured variable X is represented by the signal X_s , with $X_s = X + \nu_X$, where ν_X represents a Gaussian white noise process [1,27]. Considering this measurement error, the computable expression of the rotor dynamic of Equation (8) has the following form:

Assumption 1. The bounded achievable values of pitch angle, i.e., $\beta(t)$ and $\beta(t)$, are limited which leads to the boundedness of $\Phi(t)$ as $|\Phi(t)| \leq \overline{\Phi}$ [28]. As $f_{\beta}(t)$ varies due to the variation in $\beta(t)$ and $\dot{\beta}(t)$, the signal $f_{\beta}(t)$ is bounded as $|f_{\beta}(t)| \leq \overline{f}_{\beta}$ [5,16]. The debris build-up and erosion occur very slowly when compared to the scheduled maintenance of the blades. Therefore, it is reasonable to assume that $f_{T_a}(t)$ is bounded as $|f_{T_a}(t)| \leq \overline{f}_{T_a}$ [18]. It should be noted that $\overline{\Phi}, \overline{f}_{\beta}$ and \overline{f}_{T_a} are unknown positive constants. Moreover, it is assumed that the noise processes used to represent the measurements errors have a limited bandwidth [1,24]. By considering the bounded variation in $T_{a,\beta}(t)$, i.e., $-L \leq T_{a,\beta}(t) \leq -U < 0$, $f_2(t)$ is bounded as $|f_2(t)| \leq \overline{f}_2$, where \overline{f}_2 is a positive unknown constant. It can be shown that G(x(t)) in Equation (9) is unknown yet bounded,

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due to the presence of $T_{a,\beta}(t)$ as well as $\rho(t)$ [15]. More importantly, it is assumed that there is always a pitch actuator effort, i.e., $\rho(t) \neq 0$, the control gain G(x(t)) never becomes zero. Finally, considering the limited generator torque and drivetrain dynamic response of the industrial HAWTs with limited operation range, it can be shown that the induced aerodynamic torque is bounded as $|T_a(t)| \leq N_g T_{g,max}/\eta_{dt}$ [16].

Considering Assumption 1, based on the information extraction technique from the system nonlinearities [16], there is an unknown non-negative constant θ_F and a computable non-negative function $\varphi_F(\mathbf{x}(t))$, i.e., a core function, such that the following inequality is satisfied:

$$|F(\mathbf{x}(t))| \le \vartheta_F \varphi_F(\mathbf{x}(t))$$
 (10)

where
$$\vartheta_F = \max\{1, \overline{f}_2\}$$
 and $\varphi_F(t) = |c_1\omega_{r,s}(t)| + |c_2\omega_{g,s}(t)| + |c_3N_gT_{g,max}/\eta_{dt}| + |c_4T_{g,s}(t)| + L|f_1(t)| + 1$.

2.2. Technical Preliminaries

The following definitions and lemmas are introduced, which are used for the stability analysis.

The BLF function is defined as follows, which is used for the design of the constrained control.

Definition 1 [29]. Let's assume that V(x(t)) is positive definite continuous with respect to the solution of the system $\dot{x}(t) = f(x(t))$ on an open region \mathcal{D} . If V(x(t)) approaches to infinity, as x(t) approaches to the boundary of the region \mathcal{D} , then V(x(t)) is a BLF with continuous first order partial derivatives within all \mathcal{D} . Consequently, the inequality $V(x(t)) \leq \mathcal{W}$, $\forall t \geq 0$ holds along with the solution of $\dot{x}(t) = f(x(t))$ for $x(0) \in \mathcal{D}$, and some positive constant \mathcal{W} .

The following definition is given, thus demonstrating the boundedness of the closed-loop system.

Definition 2 [30]. x(t) is Uniformly Ultimately Bounded (UUB) if there exists a number $T(K, x(t_0))$, and a K > 0 such that for any compact set S and all $x(t_0) \in S$, $||x(t)|| \leq K$, for all $t \geq t_0 + T$.

Definition 3 [16]. Any continuous function $N(s) \in \mathbb{R}$ is a Nussbaum-type function of $s \in \mathbb{R}$, satisfying $\lim_{s \to \infty} \sup \int_{s_0}^s N(\tau) d\tau = +\infty$ and $\lim_{s \to \infty} \inf \int_{s_0}^s N(\tau) d\tau = -\infty$, for $s_0 \in \mathbb{R}$.

Lemma 1 [16]. Let's assume that V(t) > 0 and $\mathcal{F}(t)$ are smooth functions for any $t \in [0 \ t_f]$. Then, if

$$V(t) < c_0 + exp(-c_1t) \int_0^t (g(\tau)N(\mathcal{F}(\tau)) + 1)\dot{\mathcal{F}}(\tau)exp(c_1\tau)d\tau,$$

where c_0 and c_1 are positive constants, and the function $g(\tau)$ takes values in the unknown closed intervals $L \in [l^+, l^-]$ with $0 \notin L$. Then V(t), $\mathcal{F}(t)$ and $\int_0^t g(\tau)N(\mathcal{F}(\tau))\dot{\mathcal{F}}(\tau)exp(c_1\tau)d\tau$ must be bounded on $\left[0\ t_f\right)$.

Lemma 2 [15]. For a real variable ψ in $|\psi| < 1$, the inequality $tan(\pi\psi^2/2) < \pi\psi^2sec^2(\pi\psi^2/2)$ holds true.

3. Baseline NACC Design

In this section, the baseline NACC of the pitch actuator is designed to achieve the control operation requirement (ii), as described in Section 2. Furthermore, the constrained rotor speed and generated power requirements are guaranteed, with the closed-loop stability analysis. In this section the control gain is assumed to be known, i.e., the aerodynamic

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torque variation with respect to pitch angle is available. This assumption will be relaxed in Section 4 and the NCCA is modified. Moreover, in this section, the design procedure is developed on the fault-free case, i.e., $\rho(t)=1$, $\Phi(t)=0$, $f_{T_a}(t)=0$, and $f_{\beta}(t)=0$. The fault-tolerance capability is discussed in Section 6.

The baseline NACC is designed based on the rotor speed tracking error e_1 and its time derivative e_2 , defined as:

$$e_1(t) = \omega_{r,s}(t) - \omega_{r,d}$$

 $e_2(t) = \dot{\omega}_r(t) - \alpha_1(t)$ (11)

where $\omega_{r,d}$ is the desired rotor speed. The measured rotor speed $\omega_{r,s}$ is affected by noise. So, its differentiation might lead to noise amplification. Therefore, the rotor acceleration $\dot{\omega}_r(t)$ is obtained via a Gaussian regression of $\omega_{r,s}$ [31–33]. As stated earlier, $\omega_{r,d}$ in the full load region is $\omega_{r,N}$. The function $\alpha_1(t)$ corresponds to a virtual control, designed as:

$$\alpha_1(t) = -\kappa_1 e_1(t) - \frac{1}{2} e_1(t) sec^2(Y_1(t))$$
(12)

where κ_1 is a positive design parameter and $Y_1(t) = \pi \chi_1^2(t)/2$, with $\chi_1(t) = e_1(t)/\delta_1$ is the modified tracking error and δ_1 is a constraint on $e_1(t)$. A BLF is chosen as:

$$V_1(t) = \frac{\delta_1^2}{\pi} tan(Y_1(t)) \tag{13}$$

which is positive definite and continuous in the set $C_1 = \{e_1(t) : |e_1(t)| < \delta_1\}$. This imposes the constrained characteristic on $\chi_1(t)$, according to Definition 1. Taking the first-time derivative of $\chi_1(t)$, the following expression is obtained:

$$\dot{\chi}_1(t) = \frac{e_2(t) + \alpha_1(t)}{\delta_1} \tag{14}$$

On the other hand, the first-time derivative of $V_1(t)$ has the following form:

$$\dot{V}_1(t) = e_1(t)e_2(t)sec^2(Y_1(t)) + e_1(t)\alpha_1(t)sec^2(Y_1(t))$$
(15)

By replacing Equation (12) into Equation (15), the following relation is obtained:

$$\dot{V}_1(t) = e_1(t)e_2(t)sec^2(Y_1(t)) - \kappa_1 e_1^2(t)sec^2(Y_1(t)) - \frac{1}{2}e_1^2(t)sec^4(Y_1(t))$$
 (16)

Based on Young's inequality, it is easy to show that

$$e_1(t)e_2(t)sec^2(Y_1(t)) \le 0.5e_1^2(t)sec^4(Y_1(t)) + 0.5e_2^2(t).$$

Considering Lemma 2, the inequality $-\kappa_1 e_1^2(t) sec^2(Y_1(t)) < -\kappa_1 \delta_1^2 tan(Y_1(t))/\pi$ holds. Consequently, Equation (16) is rewritten as:

$$\dot{V}_1(t) < -\kappa_1 V_1(t) + \frac{1}{2} e_2^2(t) \tag{17}$$

Now, the baseline NACC is designed as:

$$\beta_{ref}(t) = H(\mathbf{x}(t))\alpha_2(t) \tag{18}$$

with the control gain defined as:

$$H(x(t)) = -\frac{1}{G(x(t))} \tag{19}$$

and $\alpha_2(t)$ is a virtual control designed as:

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$$\alpha_2(t) = \hat{\vartheta}_F(t)e_2(t)sec^2(Y_2(t))\varphi_F^2(x(t)) + \kappa_2 e_2(t) - \dot{\alpha}_1(t)$$
(20)

where $Y_2(t) = \pi \chi_2^2(t)/2$, with $\chi_2(t) = e_2(t)/\delta_2$ is the modified tracking error and δ_2 is a constraint on $e_2(t)$. κ_2 is a positive design parameter. The signal $\hat{\vartheta}_F(t)$ represents the estimation of ϑ_F , updated by the following adaption law:

$$\dot{\hat{\theta}}_F(t) = \sigma_{F1} \varphi_F^2(x(t)) e_2^2(t) sec^4(Y_2(t)) - \sigma_{F2} \hat{\theta}_F(t)$$
(21)

where σ_{F1} and σ_{F2} are positive design parameters. A Lyapunov function is chosen as:

$$V_2(t) = \frac{\delta_2^2}{\pi} tan(Y_2(t)) + \frac{1}{2\sigma_{F1}} \widetilde{\vartheta}_F^2(t)$$
(22)

where $\tilde{\vartheta}_F(t)$ is the estimation error of ϑ_F , defined as $\tilde{\vartheta}_F(t) = \vartheta_F - \hat{\vartheta}_F(t)$. The Lyapunov function $V_2(t)$ is positive definite and continuous in the set $C_2 = \{e_2(t) : |e_2(t)| < \delta_2\}$. This imposes the constrained characteristic on $\chi_2(t)$, according to Definition 1. The first-time derivative of $V_2(t)$ is obtained as:

$$\dot{V}_2(t) = e_2(t)sec^2(Y_2(t))\left(F(\mathbf{x}(t)) + G(\mathbf{x}(t))\beta_{ref}(t) - \dot{\alpha}_1(t)\right) - \frac{1}{\sigma_{F1}}\widetilde{\vartheta}_F(t)\dot{\widehat{\vartheta}}_F(t)$$
(23)

By replacing the baseline NACC of Equation (18) and the adaption law of Equation (21) into Equation (23), the following expression is obtained:

$$\dot{V}_{2}(t) = e_{2}(t)F(\mathbf{x}(t))sec^{2}(Y_{2}(t)) - \vartheta_{F}e_{2}^{2}(t)sec^{4}(Y_{2}(t))\varphi_{F}^{2}(\mathbf{x}(t))
- \kappa_{2}e_{2}^{2}(t)sec^{2}(Y_{2}(t)) + \frac{\sigma_{F2}}{\sigma_{F1}}\hat{\vartheta}_{F}(t)\tilde{\vartheta}_{F}(t)$$
(24)

Considering the trivial inequality $a(2b-1)^2 \ge 0$, $\forall a \ge 0$, and Equation (10), it can be shown that $e_2(t)F(x(t))sec^2(Y_2(t)) \le \vartheta_F e_2^2(t)\varphi_F^2(x(t))sec^4(Y_2(t)) + \vartheta_F/4$.

Additionally, considering Lemma 2, the inequality $-\kappa_2 e_2^2(t) sec^2(Y_2(t)) < -\kappa_2 \delta_2^2 tan(Y_2(t))$ / π holds. Finally, it is easy to show that $\sigma_{F2} \hat{\vartheta}_F(t) \tilde{\vartheta}_F(t) / \sigma_{F1} \leq -\sigma_{F2} \tilde{\vartheta}_F^2(t) / 2\sigma_{F1} + \sigma_{F2} \vartheta_F^2 / 2\sigma_{F1}$. Consequently, Equation (24) is rewritten as:

$$\dot{V}_2(t) \le -c_{2,1}V_2(t) + c_{2,2} \tag{25}$$

where $c_{2,1} = \min\{\kappa_2, \sigma_{F2}\}$ and $c_{2,2} = \sigma_{F2}\vartheta_F^2/2\sigma_{F1} + \vartheta_F/4$, which are positive constants. The main properties of the baseline NACC are stated in Theorem 1.

Theorem 1. Consider the HAWT dynamic model of Equation (8) for the fault-free case, i.e., $\rho(t) = 1$, $\Phi(t) = 0$, $f_{T_a}(t) = 0$, and $f_{\beta}(t) = 0$. If the initial conditions belong to set $e_i(0) \in C_i$ for i = 1, 2, by using the pitch angle control of Equation (18), with the gain of Equation (19), the virtual controls of Equations (12) and (20), together with the adaption law of Equation (21), then the following propositions hold:

- P1. All the closed-loop system states are bounded;
- P2. For i = 1, 2, the constraint sets C_i are not violated;
- P3. By the proper choice of the design parameters, the tracking error $e_1(t)$ can be made arbitrarily small.

Proof. Multiplying Equation (25) by $exp(c_{2,1}t)$, the following inequality is obtained:

$$d(V_2(t)e^{c_{2,1}t})/dt \le c_{2,2}e^{c_{2,1}t} \tag{26}$$

The integration of Equation (26) over [0, t] yields the expression:

$$V_2(t) \le \mathfrak{D}_2(t) \tag{27}$$

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where $\mathfrak{D}_2(t) = c_{2,2}/c_{2,1} + (V_2(0) - c_{2,2}/c_{2,1})exp(-c_{2,1}t)$. It should be noted that $c_{2,2}/c_{2,1} > 0$ and $\lim_{t \to \infty} exp(-c_{2,1}t) = 0$. Therefore, Equation (27) can be rewritten as:

$$V_2(t) \le \Delta_2 \tag{28}$$

where $\Delta_2 = c_{2,2}/c_{2,1} + V_2(0)$ is an unknown positive constant. Accordingly, it can be stated that the Lyapunov function $V_2(t)$ is bounded. Consequently, $tan(Y_2(t))$ and $\tilde{\theta}_F(t)$ are bounded. Therefore, it can be inferred that $e_2(t)$ belongs to C_2 , hence, it is bounded. In this sense, Equation (17) can be rewritten as:

$$\dot{V}_1(t) < -\kappa_1 V_1(t) + c_{1,2} \tag{29}$$

where $c_{1,2} = 0.5 \max_{\tau \in [0,t]} e_2^2(\tau)$ is an unknown positive constant. Multiplying both sides of Equation (29) by $exp(\kappa_1 t)$ the following inequality is obtained:

$$d(V_1(t)e^{\kappa_1 t})/dt < c_{1,2}e^{\kappa_1 t} \tag{30}$$

The integration of Equation (30) over [0, t] yields to:

$$V_1(t) < \mathfrak{D}_1(t) \tag{31}$$

where $\mathfrak{D}_1(t)=c_{1,2}/\kappa_1+(V_1(0)-c_{1,2}/\kappa_1)exp(-\kappa_1 t)$. It should be noted that $c_{1,2}/\kappa_1>0$ and $\lim_{t\to\infty}exp(-\kappa_1 t)=0$. Therefore, Equation (31) can be rewritten as:

$$V_1(t) < \Delta_1 \tag{32}$$

where $\Delta_1 = V_1(0) + c_{1,2}/\kappa_1$ is an unknown positive constant. Accordingly, it can be stated that the Lyapunov function $V_1(t)$ is bounded. Consequently, $tan(Y_1(t))$ is bounded. Therefore, it can be inferred that $e_1(t)$ belongs to C_1 , and hence it is bounded. In the light of the above-mentioned analysis, Propositions P1, P2 and P3, stated in Theorem 1, are proven as follows.

P1. Consider the boundedness of $V_1(t)$, $V_2(t)$, $e_1(t)$ and $e_2(t)$. Therefore, $Y_1(t)$ and $Y_2(t)$ are bounded. Hence, Equation (12) implies the boundedness of $\alpha_1(t)$. This, in turn, leads to the boundedness of $\omega_r(t)$ and $\dot{\omega}_r(t)$, considering Equation (11) and the assumptions on the error processes affecting the measured signals. Provided the boundedness of $\tilde{\theta}_F(t)$, the boundedness of $\hat{\theta}_F(t)$ is inferred. Therefore, considering Equation (20), $\alpha_2(t)$ is bounded. Consequently, $\beta_{ref}(t)$ is bounded.

P2. The tracking errors $e_1(t)$ and $e_2(t)$ belong to the sets $C_1 = \{e_1(t) : |e_1(t)| < \delta_1\}$ and $C_2 = \{e_2(t) : |e_2(t)| < \delta_2\}$, respectively, for t > 0.

P3. Considering Equations (13) and (31), it can be shown that $|e_1(t)| < \delta_1 \sqrt{2tan^{-1}(\pi\mathfrak{D}_1(t)/\delta_1^2)/\pi}$. Given $\mathfrak{D}_1(t) = c_{1,2}/\kappa_1 + (V_1(0) - c_{1,2}/\kappa_1)exp(-\kappa_1 t)$, if $V_1(0) = c_{1,2}/\kappa_1$, then, it holds that $\mathfrak{D}_1(t) = c_{1,2}/\kappa_1$. If $V_1(0) \neq c_{1,2}/\kappa_1$, since $\kappa_1 > 0$, then it can be concluded that for any given $\mathfrak{D}_1(t) > c_{1,2}/\kappa_1$, there exists T such that $exp(-\kappa_1 t) \approx 0$, for any t > T. Therefore, the expression $\mathfrak{D}_1(t) = c_{1,2}/\kappa_1$ holds for any t > T. Since $tan^{-1}(\bullet)$ is an increasing function of its argument, it can be concluded that $|e_1(t)| < \delta_1 \sqrt{2tan^{-1}(\pi c_{1,2}/\kappa_1 \delta_1^2)/\pi}$. As κ_1 is a design parameter, this implies that $e_1(t)$ can be made arbitrarily small by an appropriate selection of the design parameter. This guarantees that the closed-loop system is UUB based on Definition 2. \square

4. MNACC Design with Unknown Control Gain

The control gain H(x(t)) in Equation (19) is unknown as it is a function of the pitch actuator effectiveness, i.e., $\rho(t)$, and the aerodynamic torque variation with respect to pitch angle, i.e., $T_{a,\beta}(t)$. The former is represented by an unknown time-dependent variable. The latter depends on the wind speed and the aerodynamic blade profile. Some studies,

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e.g., [15,17,20], suggest estimating the effective wind speed and the blade aerodynamic profile. Besides the computational expensiveness of solutions, the estimation error is unavoidable, especially with high wind speed variations. This, in turn, leads to the degraded performance of the HAWT. On the other hand, some works, e.g., [6], use a look-up table to compute the $T_{a,\beta}(t)$, based on the in-site measurements by a linear interpolation. This has led to computationally-practical solutions. However, a small amount of measurement data and the linear interpolation approach cannot capture the nonlinear dynamic response of HAWTs accurately. More importantly, both approaches fail to operate desirably in the case of pitch actuator effectiveness loss and BAPC.

The aforementioned unknown control gain problem is resolved in this section, by the adoption of a Nussbaum-type function for the control gain. The MNACC is designed for the fault-free pitch actuator, i.e., $\rho(t)=1$ and $\Phi(t)=0$. The fault tolerance capability of the proposed MNACC is discussed in Section 6. The structure of MNACC is given by Equation (18), with the control gain, defined as follows:

$$H(\zeta_1(t)) = N(\zeta_1(t)) \tag{33}$$

where $N(\bullet)$ is a Nussbaum-type function, which satisfies Definition 3. Furthermore, $\zeta_1(t)$ is obtained via the following adaption laws:

$$\dot{\zeta}_1(t) = e_2(t)sec^2(Y_2(t))\alpha_2(t)$$
 (34)

Now, the main properties of the MNACC are stated in Theorem 2.

Theorem 2. Consider the HAWT dynamic model of Equation (8) for the fault-free case, i.e., $\rho(t) = 1$, $\Phi(t) = 0$, $f_{T_a}(t) = 0$, and $f_{\beta}(t) = 0$. If the initial conditions belong to set $e_i(0) \in C_i$ for i = 1, 2, by using the pitch angle control law of Equation (18), with the gain of Equation (33), the virtual controls of Equations (12) and (20), and the adaption law of Equations (21) and (34), then Propositions P1, P2 and P3, stated in Theorem 1, hold.

Proof. Consider the Lyapunov functions $V_1(t)$ and $V_2(t)$, described by Equations (13) and (22), respectively. By substituting the control law of Equation (18) with the gain of Equation (33) and the adaption laws of Equations (21) and (34) into the first-time derivative of $V_2(t)$, given in Equation (23), one can obtain:

$$\dot{V}_{2}(t) = e_{2}(t)F(\mathbf{x}(t))sec^{2}(Y_{2}(t)) + G(\mathbf{x}(t))N(\zeta_{1}(t))\dot{\zeta}_{1}(t)
- \vartheta_{F}\varphi_{F}^{2}(\mathbf{x}(t))e_{2}^{2}(t)sec^{4}(Y_{2}(t)) + \frac{\sigma_{F2}}{\sigma_{F1}}\tilde{\vartheta}_{F}(t)\hat{\vartheta}_{F}(t) + \dot{\zeta}_{1}(t)
- \kappa_{2}e_{2}^{2}(t)sec^{2}(Y_{2}(t))$$
(35)

It is readily shown that:

$$\begin{split} e_{2}(t)F(x(t))sec^{2}(Y_{2}(t)) &\leq \vartheta_{F}e_{2}^{2}(t)\varphi_{F}^{2}(x(t))sec^{4}(Y_{2}(t)) + \vartheta_{F}/4, \\ &- \kappa_{2}e_{2}^{2}(t)sec^{2}(Y_{2}(t)) < -\kappa_{2}\delta_{2}^{2}tan(Y_{2}(t))/\pi, \\ &\sigma_{F2}\hat{\vartheta}_{F}(t)\tilde{\vartheta}_{F}(t)/\sigma_{F1} \leq -\sigma_{F2}\tilde{\vartheta}_{F}^{2}(t)/2\sigma_{F1} + \sigma_{F2}\vartheta_{F}^{2}/2\sigma_{F1}. \end{split}$$

Therefore, from Equation (35) the following inequality can be derived:

$$\dot{V}_2(t) \le -c_{2,1}V_2(t) + c_{2,2} + G(x(t))N(\zeta_1(t))\dot{\zeta}_1(t) + \dot{\zeta}_1(t) \tag{36}$$

The multiplication of Equation (36) by $exp(c_{2,1}t)$, yields the following inequality:

$$d(V_2(t)e^{c_{2,1}t})/dt \le c_{2,2}e^{c_{2,1}t} + \left(G(\mathbf{x}(t))N(\zeta_1(t))\dot{\zeta}_1(t) + \dot{\zeta}_1(t)\right)e^{c_{2,1}t} \tag{37}$$

Therefore, the integration of Equation (37) over [0, t] yields to:

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$$V_2(t) \le \mathfrak{D}_2(t) + e^{-c_{2,1}t} \int_0^t (G(\mathbf{x}(\tau))N(\zeta_1(\tau)) + 1)\dot{\zeta}_1(\tau)e^{c_{2,1}\tau}d\tau \tag{38}$$

It should be noted that $c_{2,2}/c_{2,1}>0$ and $\lim_{t\to\infty}exp(-c_{2,1}t)=0$. Therefore, Equation (38) can be rewritten as:

$$V_2(t) \le \Delta_2 + e^{-c_{2,1}t} \int_0^t (G(\mathbf{x}(\tau))N(\zeta_1(\tau)) + 1)\dot{\zeta}_1(\tau)e^{c_{2,1}\tau}d\tau \tag{39}$$

Moreover, the variable G(x(t)) in Equation (39) satisfies the conditions stated for $g(\tau)$ in Lemma 1. Furthermore, Δ_2 and $c_{2,1}$ are unknown positive constants. Therefore, considering Equation (39), it can be shown that $V_2(t)$ and $\zeta_1(t)$ are bounded. The rest of the proof is similar to that of Theorem 1 and is thus omitted here (see from Equation (29) to the end of the proof). \square

Remark 1. Regarding the MNACC of Equation (18) with the gain of Equation (33), it is worth noting that in the design procedure of the pitch angle control, there is no need to estimate the aerodynamic torque variation with respect to pitch angle, i.e., $T_{a,\beta}$, and Propositions P1–P3 are still satisfied. This represents one significant key of the proposed MNACC.

5. MNACC Control with Arbitrary Initial Conditions

The initial conditions of HAWT are not necessarily close to the desired trajectory, i.e., $e_i(0) \notin C_i$ for i = 1, 2. In this section, the case of arbitrary initial condition is handled.

If the initial conditions do not belong to the constraint sets, the stability analysis given in Theorem 2, is no longer valid. This might lead to HAWT over speeding or, even to more dangerous catastrophic consequences. This requires the initial conditions to be manually set within the constraint sets, which is not a practical approach. As an example, in [34–37] the authors adopted too large and conservative constraints to include the initial conditions. Nevertheless, such a constraint may be ineffective in practice. Instead, it is beneficial to have a systematic and automatic approach to handle arbitrary initial conditions. To relax this requirement, the constraints are initially enlarged based on the assigned initial conditions. Then, the constraints converge exponentially to the intended bounds, in which the desired performance is achieved. In this manner, the arbitrary initial condition is systematically handled. The exponential convergence of the constraints to the given bounds offers more degrees of freedom that can be exploited in the control design. To this end, the constraint δ_i for i=1,2, are designed according to the following relation:

$$\delta_i(t) = \begin{cases} \overline{\delta}_i(t), & \text{if } e_i(t) \ge 0\\ \delta_i(t), & \text{if } e_i(t) < 0 \end{cases}$$
(40)

where

$$\overline{\delta}_i(t) = \overline{a}_i exp(-\phi_i t) + \overline{b}_i(t),$$

$$\underline{\delta}_i(t) = \underline{a}_i exp(-\phi_i t) - \underline{b}_i(t).$$

Furthermore, if $e_i(0) \geq 0$, then $\overline{a}_i = e_i(0)$ and $\underline{a}_i = 0$, otherwise $\overline{a}_i = 0$ and $\underline{a}_i = e_i(0)$. The term ϕ_i is a positive design parameter. The terms $\overline{b}_i(t)$ and $\underline{b}_i(t)$ represent positive upper and lower thresholds, respectively, between the desired trajectory and constraints, which can be constant or variable. The terms \overline{a}_i and \underline{a}_i are defined based on the initial condition values. Accordingly, the constraint is initially enlarged to cover the arbitrary initial condition. On the other hand, $exp(-\phi_i t)$ approaches to zero as time increases. This provides further degrees of freedom in the design, i.e., the rate of the distance vanishes. For example, for large inertia and slow dynamic systems the term $\phi_i < 1$ is selected in order to have a suitable convergence time and avoid a large control effort. Finally, \overline{b}_i and \underline{b}_i define a small bound, within which desirable performance is achieved.

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The constraint $\delta_i(t)$, defined in Equation (40), is obviously a time variable and thus $\dot{\delta}_i(t)$ affects the closed-loop performance. This effect leads to extra terms contributing to the time derivative of $V_1(t)$ and $V_2(t)$. These functions are represented by the expression:

$$2\delta_i(t)\dot{\delta}_i(t)tan(Y_i(t))/\pi - e_i^2(t)\dot{\delta}_i(t)sec^2(Y_i(t))/\delta_i(t)$$

for i = 1, 2, which is added to Equations (15) and (23), respectively. Accordingly, in order to remove their effects, the virtual control $\alpha_1(t)$ in Equation (12) and $\alpha_2(t)$ in Equation (20) are modified as follows:

$$\alpha_1(t) = -\kappa_1 e_1(t) - \frac{1}{2} e_1(t) sec^2(Y_1(t)) - \overline{\alpha}_1(t)$$
(41)

$$\alpha_2(t) = \hat{\vartheta}_F(t)e_2(t)sec^2(Y_2(t))\varphi_F^2(x(t)) + \kappa_2 e_2(t) - \dot{\alpha}_1(t) + \overline{\alpha}_2(t), \tag{42}$$

where

$$\overline{\alpha}_i(t) = \delta_i(t)\dot{\delta}_i(t)\sin(2Y_i(t))/e_i(t)\pi - e_i(t)\dot{\delta}_i(t)/\delta_i(t),$$

for i = 1, 2. It is worth noting that $\dot{\delta}_i(t)$ can be defined by the following relation:

$$\dot{\delta}_i(t) = \begin{cases} \frac{\dot{\delta}}{\dot{\delta}_i}(t), & \text{if } e_i(t) \ge 0\\ \frac{\dot{\delta}_i}{\dot{\delta}_i}(t), & \text{if } e_i(t) < 0 \end{cases}$$

where

$$\dot{\overline{\delta}}_i(t) = -\overline{a}_i \phi_i exp(-\phi_i t) + \dot{\overline{b}}_i(t),$$

$$\dot{\underline{\delta}}_i(t) = -\underline{a}_i \phi_i exp(-\phi_i t) - \dot{\underline{b}}_i(t).$$

The achieved results valid for the arbitrary initial condition are summarized as follows.

Theorem 3. Consider the HAWT dynamic model of Equation (8) for the fault-free case, i.e., $\rho(t) = 1$, $\Phi(t) = 0$, $f_{T_a}(t) = 0$, and $f_{\beta}(t) = 0$. The pitch angle control law of Equation (18) is designed with the gain of Equation (33) and the virtual controls of Equations (41) and (42), the adaption laws of Equations (21) and (34), and the constraints defined by Equation (40). For any initial conditions Propositions P1, P2 and P3, stated in Theorem 1, hold.

Proof. The proof is straightforward (similar to that of Theorem 2), and thus omitted here. \Box

Remark 2. Considering the definition of $\bar{\alpha}_i(t)$ in Equations (41) and (42) for i=1,2, when $e_i(t)$ approaches to zero, the term $\delta_i(t)\dot{\delta}_i(t)sin(2Y_i(t))/e_i(t)\pi$ approaches to zero, by using L'Hospital's rule. Therefore, the singularity does not occur. However, since digital processors are not able to evaluate indeterminate form 0/0, the Maclaurin series with the first term is used in the implementation step to solve this problem. Accordingly, in $\bar{\alpha}_i(t)$ the term $\delta_i(t)\dot{\delta}_i(t)sin(2Y_i(t))/e_i(t)\pi$ is replaced with $\dot{\delta}_i(t)e_i(t)/\delta_i(t)$, when $|e_i(t)| < \varepsilon_i$, where ε_i is a small positive design constant.

6. Fault-Tolerance Capability of MNACC

The pitch actuator might suffer from effectiveness loss, bias and dynamic change. On the other hand, the long-term operation might lead to BAPC. This section aims to analyse the fault-tolerant capability of the proposed controller. It is proven that the control law of Equation (18), integrated with the gain of Equation (33), is able to compensate for the fault effects from the closed-loop performance automatically, and no control modification is required. This represents a key feature of the proposed pitch angle control, i.e., the constrained power generation is guaranteed, while no redundant hardware components are required. Furthermore, an extra computationally expensive scheme to detect, isolate and identify the faults is not needed. This is an important advantage in general for HAWTs,

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especially for offshore deployments. To this end, the main results on the fault tolerance capability of the proposed MNACC are summarized in the following theorem.

Theorem 4. Consider the HAWT dynamic model of Equation (8) under pitch actuator effectiveness loss $\rho(t)$, bias $\Phi(t)$, dynamic change $f_{\beta}(t)$ and the BAPC $f_{T_a}(t)$. The pitch angle control exploits Equation (18), with the gain of Equation (33) and, the virtual controls of Equations (41) and (42), the adaption law of Equations (21) and (34), and the constraints defined by Equation (40). For any initial conditions, Propositions P1, P2 and P3, stated in Theorem 1, hold.

Proof. Consider the Lyapunov functions $V_1(t)$ and $V_2(t)$, given in Equations (13) and (22), respectively. By using the control of Equation (18) with the gain of Equation (33) and the adaption laws of Equations (21) and (34), and the virtual control of Equations (41) and (42), the first-time derivative of $V_2(t)$ satisfies the following inequality:

$$\dot{V}_2(t) \le -c_{2,1}V_2(t) + c_{2,2} + W(t)N(\zeta_1(t))\dot{\zeta}_1(t) + \dot{\zeta}_1(t) \tag{43}$$

where $W(t) = \rho(t)G(x(t))$. Therefore, the integration of Equation (43) over [0, t] leads to the following inequality:

$$V_2(t) \le \mathfrak{D}_2(t) + e^{-c_{2,1}t} \int_0^t (W(\tau)N(\zeta_1(\tau)) + 1)\dot{\zeta}_1(\tau)e^{c_{2,1}\tau}d\tau \tag{44}$$

It should be noted that $c_{2,2}/c_{2,1}>0$ and $\lim_{t\to\infty} exp(-c_{2,1}t)=0$. Therefore, Equation (44) can be rewritten as:

$$V_2(t) \le \Delta_2 + e^{-c_{2,1}t} \int_0^t (W(\tau)N(\zeta_1(\tau)) + 1)\dot{\zeta}_1(\tau)e^{c_{2,1}\tau}d\tau \tag{45}$$

Moreover, as $\rho(t) \neq 0$, then the term W(t) satisfies the conditions on $g(\tau)$ in Lemma 1. Furthermore, Δ_2 and $c_{2,1}$ are unknown positive constants. Therefore, considering Equation (45), it can be shown that $V_2(t)$ and $\zeta_1(t)$ are bounded. The rest of the proof is similar to that of Theorem 1 and is, thus, omitted here (see from Equation (29) to the end of the proof). \square

Remark 3. In Theorem 4, Proposition P1 implies that the closed-loop HAWT including the MNACC controller is stable. Proposition P2 guarantees the fulfilment of the constraints on the rotor speed and its acceleration. Consequently, the generator speed and the generated power are kept within the prescribed bounds. Considering Section 3, the efficient power regulation requirements are also met, hence, the required power grid demand is satisfied. Moreover, both the rotor overspeeding and the mechanical brake engagement is avoided. Proposition P3 indicates the expert's knowledge in the implementation stage, to satisfactorily make the tracking error small. These objectives are also satisfied in the presence of uncertain wind speed variation, pitch actuator effectiveness loss, bias, dynamic change, and BAPC, for any initial conditions. So, efficient power regulation is satisfied without the need for unplanned maintenance. Accordingly, the reliability and availability properties are improved. Furthermore, downtime and maintenance costs are reduced.

Remark 4. It should be noted that in [27], different faults, either sensor or actuator, mechanical or electrical, were introduced. In the current study, the pitch actuator dynamic change, bias and effectiveness loss are considered. This is mainly motivated by considering the severity of these faults [1]. Meanwhile, the effects of BAPC and drivetrain efficiency reduction are evaluated. However, the rest of the mentioned faults [27] are not included. This stems from two reasons. In the full load region, the generator control is not active, and the generator torque load is just set at the nominal value. Therefore, the faults on the generator are not considered. More importantly, the proposed controller can be used in parallel to the available solutions, which are designed to compensate, for instance, for the sensor faults (for the other faults see the suggested strategies in [38]).

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7. Feasibility Check and Design Algorithm

In the proposed controller, the constraints are imposed on the tracking error. However, from a practical point of view, the state constraints are given directly on the HAWT rotor speed and its derivative, rather than the tracking error. In that sense, the operational requirements are defined as $|\omega_r(t)| < \delta_{\omega_r}$ and $|\dot{\omega}_r(t)| < \delta_{\omega_r}$. In practice, it is assumed that $|\omega_{r,d}| < \delta_{\omega_{r,d}} < \delta_{\omega_r}$. From Equation (41), it can be stated that if the virtual control $\alpha_1(t)$ is bounded with respect to the specified constrained $\dot{\omega}_r(t)$, the inequality $|\dot{\omega}_r(t)| < \delta_{\dot{\omega}_r}$ is guaranteed. As $|\dot{\omega}_r(t)| < \delta_{\omega_r}$, and also since $|e_2(t) + \alpha_1(t)| = |\dot{\omega}_{r,s}(t)|$, it can be verified that $|\alpha_1(t)| < \delta_{\dot{\omega}_r}$. An important issue is that the feasibility condition $|\alpha_1(t)| < \delta_{\dot{\omega}_r}$ may be violated when the $\omega_r(t)$ approaches the constraint δ_{ω_r} [30]. Therefore, $|\alpha_1(t)| < \delta_{\omega_r}$ must be satisfied by choosing the appropriate design parameter κ_1 [29]. On the other hand, considering effect of $\dot{\alpha}_1(t)$ as in Equation (42), $\alpha_2(t)$ may become very large when $e_1(t)$ gets very close to $\delta_1(t)$ [29]. Therefore, the state constraints cannot be arbitrarily selected, and a given feasibility constraint has to be satisfied, which is based on $\alpha_1(t)$. The feasibility condition depends on the existence of the design parameters to satisfy the state constraints. To this end, if the constraints are too small, such a control may not exist. In this regard, the feasibility condition is formulated as a static optimization and solved prior to the implementation of the controller. Let us assume there exists an upper bound $A_1(\kappa_1)$, such that:

$$A_1(\kappa_1) = \sup_{\Omega} (\alpha_1(\omega_r(t), e_1(t), \omega_{r,d}; \kappa_1))$$
(46)

where $\Omega = \left\{ \omega_r(t), e_1(t), \omega_{r,d} : |\omega_r(t)| < \delta_1 + \delta_{\omega_{r,d}}, |e_1(t)| < \delta_1, \; |\omega_{r,d}| < \delta_{\omega_{r,d}} \right\}$. From Proposition P3 in Theorem 3, it is evident that the design parameters are to be selected large enough to achieve good tracking performance. However, this increases $\alpha_1(t)$ in Equation (41), and consequently, $\alpha_2(t)$. This may violate the state constraint $|\dot{\omega}_r(t)| < \delta_{\dot{\omega}_r}$. Accordingly, a tradeoff has to be defined, which is formulated as a feasibility condition. Specifically, it checks if there exists a solution κ_1^* for the following static Optimization Problem (OP).

OP : Given
$$\delta_{\omega_r}$$
 and $\delta_{\dot{\omega}_r}$,

Maximize (κ_1) ,

 $\kappa_1 > 0$ (47)

Subject to $\delta_{\dot{\omega}_r} > A_1(\kappa_1)$.

It should be noted that this is a sufficient condition. In such a case, with $\kappa_1 = \kappa_1^*$ the state constraints are not violated. The design procedure is summarized in Algorithm 1. It should be noted that this algorithm can be solved by using, e.g., the fmincon routine in MATLAB [39]. Additionally, the design structure is summarized in Figure 2.

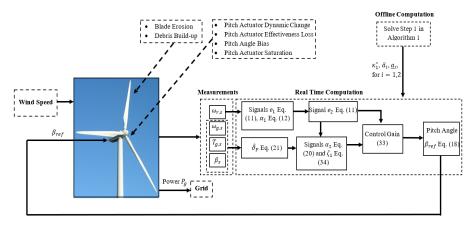


Figure 2. Block diagram of the design procedure.

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Algorithm 1 Proposed controller design procedure

- 1. Offline computation:
- 1.1. For the given δ_{ω_r} and $\dot{\omega}_r$, solve OP to obtain κ_1^* . Select κ_2 , σ_{F1} , σ_{F2} and ε_i , for i = 1,2, in accordance with Remark 2.
 - 1.2. For the given initial condition, compute \bar{a}_i and \underline{a}_i , then select \bar{b}_i , \underline{b}_i and ϕ_i , for i = 1,2.
- 2. Online computation:
 - 2.1. Integrate the virtual controls Equations (41) and (42), the adaptive laws Equations (21) and (34).
 - 2.2. Compute the control gain Equation (33) and then the control signal Equation (18).

8. Simulations and Discussion

This section presents and discusses the numerical simulations conducted on the high-fidelity 4.8 MW HAWT benchmark to evaluate the effectiveness of the MANCC [6,27]. Different fault scenarios are applied to the benchmark, i.e., single and simultaneous faults. It is shown that in both cases the considered constraints are not violated, satisfying the operation requirement (ii). Uncertainties represent the key point in the case of offshore HAWTs. Indeed, in remote harsh locations, BAPC and drivetrain efficiency reduction are unavoidable. This issue is important, as this may lead to less captured power. Accordingly, to assess the robustness of the proposed MANCC, a Monte-Carlo analysis is performed with different measurement errors, modelled as Gaussian processes, and the model-reality mismatch. To numerically evaluate the nominal power generation the following normalized Power Metric (PM) is defined as follows:

$$PM(\%) = \frac{100|P_g(t) - P_{g,N}|}{P_{g,N}} \tag{48}$$

8.1. Control Parameters

The constraints on the rotor speed and its time derivative are selected as $\delta_{\omega_r}=1.736\ rad/s$ and $\delta_{\dot{\omega}_r}=0.07\ rad/s^2$. Accordingly, by solving OP, the parameters of the MANCC are $\kappa_1=0.1,\ \kappa_2=4,\ \sigma_{F1}=\sigma_{F2}=10$. Furthermore, the initial conditions vector is $\mathbf{x}(0)=[1.7355,\ 164.87,\ 3,\ 32107]$. Consequently, the parameters of the tracking error constraints in Equation (40) are $\bar{a}_1=0.025,\ \bar{b}_1=0.02,\ \underline{a}_1=0,\ \underline{b}_1=0.02,\ \phi_1=0.02,$ $\bar{a}_2=0.055,\ \bar{b}_2=0.05,\ \underline{a}_2=0,\ \underline{b}_2=0.05$ and $\phi_2=0.02$. The Nussbaum-type function $N(\zeta_1(t))=\zeta_1^2(t)cos(\zeta_1(t))$ is used, according to Definition 3. Finally, considering Remark 2, $\varepsilon_1=\varepsilon_2=0.001$ is selected.

8.2. Fault Model

The fault $f_{\beta}(t)$ in Equation (6) is due to the pitch actuator dynamic change, which in turn causes the variation in the natural frequency ω_n and the damping ratio ξ . As described in [1], the fault $f_{\beta}(t)$ can be modelled as a convex functions depending on the nominal values of the natural frequency and the damping ratio, as described by the following relation [1,6]:

$$f_{\beta}(t) = -\alpha_{f_1} \Delta(\widetilde{\omega}_n^2) \beta(t) - 2\alpha_{f_2} \Delta(\widetilde{\omega}_n \widetilde{\xi}) \dot{\beta}(t) + \alpha_{f_1} \Delta(\widetilde{\omega}_n^2) \beta_{ref}(t)$$
(49)

where $\Delta(\widetilde{\omega}_n^2) = \omega_{n,HL}^2 - \omega_{n,N}^2$, $\Delta(\widetilde{\omega}_n\widetilde{\xi}) = \omega_{n,HAC}\xi_{HAC} - \omega_{n,N}\xi_N$, α_{f_1} and α_{f_2} are fault indicators, $\omega_{n,X}$ and ξ_X are the natural frequency and the damping ratio, respectively, in the condition X. Additionally, the acronyms N, HL, PW, and HAC stand for normal, hydraulic leaks, pump wear, and high air content conditions, respectively. The parameters of these conditions are summarized in Table 1. On the other hand, to precisely investigate the effects of faults and the performance of the proposed controller, different fault types, sizes and periods are considered.

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Table 1. Pitch actuator dynamic change parameters [1,6].

Pitch Actuator Condition	Parameters	Indicator		
Normal (N))	$\omega_{n,N} = 11.11, \xi_N = 0.6$	$\alpha_{f_1} = \alpha_{f_2} = 0$		
Pump Wear (PW)	$\omega_{n,PW} = 7.27, \xi_{PW} = 0.75$	$\alpha_{f_1} = 0.63, \alpha_{f_2} = 0.30$		

Furthermore, single faults occurring once per time are simulated, as well as simultaneous ones. To summarize, two fault scenarios, including single and simultaneous fault conditions with different sizes and types are implemented, as described in Table 2 and Table 3, respectively. Additionally, it should be noted that $f_{Ta}(t)$ can be implemented as a reduction in the power coefficient. BAPC is described as a 10% reduction in the power coefficient in the simulations. On the other hand, the drivetrain friction may lead to decreased efficiency. This is modelled by a 5% reduction in drivetrain efficiency.

Table 2. Single fault scenario.

Pitch Actuator Condition	Parameters	Indicator		
Bias	$\Phi(t)=10^{\circ}$	$200(s) \le t \le 300(s)$		
Effectiveness loss	$\rho(t) = 0.7$	$400(s) \le t \le 500(s)$		
Pump wear	$\alpha_{f_1} = 0.63, \alpha_{f_2} = 0.30$	$600(s) \le t \le 700(s)$		
Hydraulic oil leak	$\alpha_{f_1} = 1, \alpha_{f_2} = 0.88$	$800(s) \le t \le 900(s)$		
High air content in oil	$\alpha_{f_1} = 0.81, \alpha_{f_2} = 1$	$900(s) \le t \le 1000(s)$		

Table 3. Simultaneous fault scenario.

Pitch Actuator Fault Type	Fault Effect	Fault Period	
Bias Pump wear	$\Phi(t) = 15^{\circ}$ $\alpha_{f_1} = 0.63, \alpha_{f_2} = 0.30$	$100(s) \le t \le 400(s)$	
Effectiveness loss High air content in oil	$ ho(t) = 0.5 \ lpha_{f_1} = 0.81, lpha_{f_2} = 1$	$500(s) \le t \le 800(s)$	
Hydraulic oil leak	$\alpha_{f_1}=1, \alpha_{f_2}=0.88$	$900(s) \le t \le 1000(s)$	

8.3. Parameters of Measurement Errors

To have a realistic simulation analysis, the sensor measurements are affected by measurement errors, modelled as Gaussian processes, which is a common assumption in many works [27]. The measurement error parameters are described by the variables of *Set* 1 in Table 4. It is worth noting that the measurement error of the sensors may be variable over a long period of operation. These effects are investigated through the evaluation of the robustness feature via the Monte-Carlo tool. Accordingly, three sets of measurement errors with different standard deviations are considered, which are reported in Table 4, i.e., *Set* 1, *Set* 2 and *Set* 3. It should be pointed out that, as the paper focuses on the pitch angle control, larger variations in pitch angle standard deviation are considered.

Table 4. Parameters of the different measurement error conditions.

	Sensor	Mean	Noise Standard Deviation	Error Compared to Nominal Values (%)
	Rotor speed	0	$\sigma_{\omega_r}=0.002$	0.12
7	Generator speed	0	$\sigma_{\omega_g} = 0.5$	0.31
Set 1	Generator torque	0	$\sigma_{\omega_g} = 0.5$ $\sigma_{T_g} = 90$	0.28
	Pitch angle	0	$\sigma_{eta}^{\circ}=0.2$	1.16

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	Sensor	Mean	Noise Standard Deviation	Error Compared to Nominal Values (%)
	Rotor speed	0	$\sigma_{\omega_r} = 0.004$	0.24
2	Generator speed	0	$\sigma_{\omega_g} = 1$	0.62
Set	Generator torque	0	$\sigma_{T_g} = 100$	0.31
	Pitch angle	0	$\mathring{\sigma_eta}=1$	5.8
	Rotor speed	0	$\sigma_{\omega_r} = 0.008$	0.48
3	Generator speed	0	$\sigma_{\omega_{\hat{g}}} = 3$	1.84
Set	Generator torque	0	$\sigma_{T_{\sigma}} = 120$	0.37
	Pitch angle	0	$\sigma_{T_g} = 120$ $\sigma_{eta} = 2$	11.6

8.4. Simulation Results and Discussion

The considered wind speed sequence is shown in Figure 3, with the mean $17.84 \, (m/s)$ and the standard deviation of $1.94 \, (m/s)$. It is worth noting that other wind sequences can be used to study the robustness of the performance. In this work, however, the robustness is analysed via the Monte-Carlo tool in the presence of measurement errors. Therefore, for the sake of brevity, the wind speed sequence depicted in Figure 3 is only used. Under single and simultaneous fault scenarios, the results are shown in Figures 4-10.

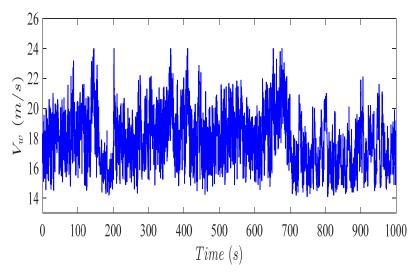


Figure 3. Free wind speed profile.

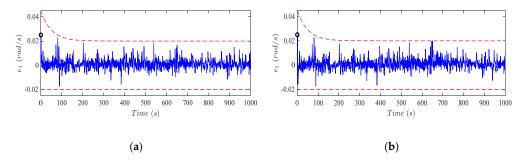


Figure 4. Tacking error e_1 (blue line) with constructed constraints (red dashed lines), under single (a) and simultaneous faults (b). The circle represents the initial value.

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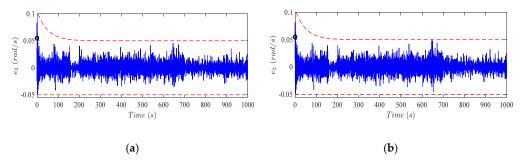


Figure 5. Tacking error e_2 (blue line) with constructed constraints (red dashed lines), under single (a) and simultaneous faults (b). The circle represents the initial value.

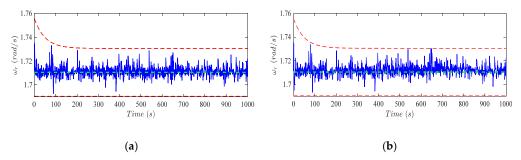


Figure 6. Rotor speed ω_r (blue line) with constructed constraints (red dashed lines) and nominal value (green dashed line), under single (**a**) and simultaneous faults (**b**).

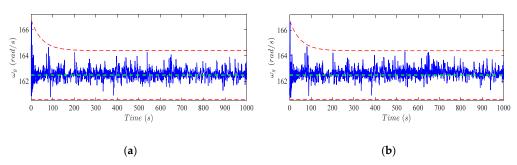


Figure 7. Generator speed ω_g (blue line) with constructed constraints (red dashed lines) and nominal value (green dashed line), under single (**a**) and simultaneous faults (**b**).

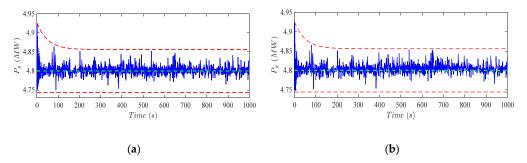


Figure 8. Generated power P_g (blue line) with constructed constraints (red dashed lines) and nominal value (green dashed line), under single (**a**) and simultaneous faults (**b**).

It can be seen that the tracking errors $e_1(t)$ and $e_2(t)$ are within the considered constraints, considering Figures 4 and 5. Accordingly, both the rotor and the generator speed signals, illustrated in Figures 6 and 7, are quite close to the corresponding nominal values despite the wind speed variation and faults. As a result, the generated power is regulated at the nominal value, as shown in Figure 8. These results imply that the wind turbine is successfully controlled by pitch angle regulation, i.e., the nominal power is generated, despite the wind speed high variation and the faults. Furthermore, the given operation

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bounds are not violated. This enables safe operation and avoids conservative WEC. Especially, considering the bounded rotor speed, the engagement of the mechanical brake on the rotor shaft can be avoided. On the other hand, as indicated in Figures 4 and 5, the proposed scheme is able to construct the bounds to handle the initial conditions outside of these bounds, as discussed in Section 5.

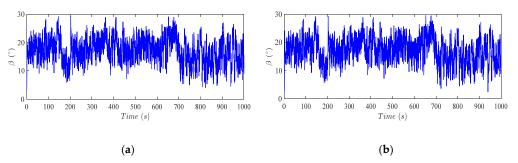


Figure 9. Reference pitch angle under single (a) and simultaneous faults (b).

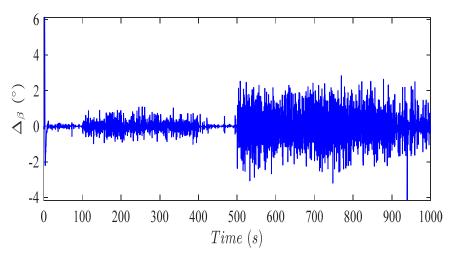


Figure 10. Profile of Δ_{β} .

The reference pitch angle computed by the proposed controller is shown in Figure 9. The pitch angles in Figure 9 are very similar to each other. Therefore, to accurately investigate the performance of the proposed controller, the difference between these two pitch angles, defined as $\Delta_{\beta}(t) = \beta(t)_{single\ faults} - \beta(t)_{simultaneous\ faults}$, is reported in Figure 10. Considering Tables 1 and 2, and Figure 10, it is clear that the main difference is in the periods that the pitch actuator bias and effectiveness loss commence, i.e., $100\ (s) \le t \le 400\ (s)$ and $500\ (s) \le t \le 800\ (s)$. Considering Figure 10 and Tables 2 and 3, the effects of the pitch actuator dynamic change have led to more variations, compared to bias and effectiveness loss. Indeed, the dynamic change causes the slower pitch actuator dynamic response. In this case, the controller has to vary the pitch angle faster with larger values to retain the rotor speed within the bounds.

Now to extensively evaluate the performance, the Monte-Carlo analysis is performed to assess the robustness and reliability of the proposed controller, in terms of nominal power generation, considering different measurement errors and the PM(%) index. Additionally, BAPC is included as a 10% reduction in the power coefficient. On the other hand, the drivetrain decreased efficiency is considered by a 5% reduction in this parameter. Accordingly, two cases with and without BAPC and drivetrain efficiency reduction are represented by Case 1 (C1) and Case 2 (C2), respectively. The Monte-Carlo analysis is performed under a single fault scenario. For each case, 100 simulations are performed. For each simulation, the PM(%) is computed over the simulation time. Then, the maximum, minimum, standard deviation and mean values of each PM(%) index for each simulation

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are computed. Accordingly, for the sake of brevity, the Worst (W), the Average (A) and the Best (B) values over 100 simulations are considered, as indicated in Table 5. It is worth noting that the PM(%) index, as defined in Equation (48), is ideally close to zero. Therefore, the worst, the average and the best values represent the largest, average and smallest values, respectively. The rationale behind this is that the largest PM(%) represents the largest deviation from the nominal power generation. Therefore, this is selected as the worst performance index. Similar justifications can be given for average and the best values. All Monte-Carlo simulation results reported in Table 5 highlight that the proposed control scheme is robust with respect to the model efficiency reduction, measurement errors, wind speed variations as well as faults. Indeed, in terms of nominal power generation, which is the main operational objective of the wind turbine in the full load region, the proposed pitch angle controller is able to keep the generated power very close to the nominal value.

Table 5. Monte-Carlo simulation results in terms of PM% index. Letters B, A and W stand for best, average and worst values, respectively.

		PM (%)						
		Maximum			Minimum			
		В	A	W	В	A	W	
Set 1	C1 C2	1.038 1.142	1.151 1.268	1.422 1.531	$6.14 \times 10^{-8} $ 7.51×10^{-8}	3.73×10^{-4} 6.14×10^{-6}	$0.016 \\ 2.37 \times 10^{-4}$	
Set 2	C1 C2	1.033 1.131	1.230 1.359	1.641 1.813	1.13×10^{-8} 2.77×10^{-10}	5.53×10^{-4} 1.14×10^{-5}	$0.014 \\ 1.48 \times 10^{-4}$	
Set 3	C1 C2	1.042 1.136	1.419 1.446	2.428 2.482	$7.65 \times 10^{-9} \\ 0.21 \times 10^{-8}$	$0.006 \\ 2.72 \times 10^{-5}$	$0.349 \\ 5.39 \times 10^{-4}$	
			Mean		St	tandard Deviatio	on	
		В	A	W	В	A	W	
Set 1	C1 C2	0.155 0.169	0.186 0.197	0.277 0.334	0.141 0.158	0.157 0.168	0.198 0.207	
Set 2	C1 C2	0.155 0.117	0.249 0.268	0.576 0.629	0.144 0.158	0.167 0.182	0.209 0.228	
Set 3	C1 C2	0.155 0.171	0.413 0.353	1.374 1.285	0.143 0.158	0.182 0.191	0.214 0.234	

Table 5 summarises the Monte-Carlo analysis results. As these simulations are performed under random noise processes 600 times, cumulatively, it can be concluded that the achievement of this objective is guaranteed by using the proposed controller. This highlights the robustness and reliability of the developed solution, in terms of nominal power generation. This is verified considering the PM(%) in Table 5. The deviation of the generated power from the nominal value is negligible for all the simulations with different measurement errors and faults. Even the worst cases, i.e., the largest PM(%), have led to small deviations.

9. Conclusions

This paper proposed a novel pitch actuator controller to improve the power regulation efficiency of the horizontal axis wind turbine. It also guaranteed safe operation with efficient wind energy conversion. The constrained control was designed, using the barrier Lyapunov function, to retain the rotor speed and the generated power within the safe-to-operate bounds. Therefore, the rotor overspeeding, the mechanical brake engagement, and the conservative energy conversion are avoided. The proposed controller was able to handle the uncertain wind speed variation effects without requiring accurate wind speed measurement, using the Nussbaum-type function. It was also able to compensate

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for pitch actuator faults and aerodynamic characteristic change. Accordingly, unplanned maintenance and consequent cost are reduced. Numerical simulations were performed to validate the effectiveness of the proposed controller under various faults. The Monte-Carlo tool was exploited for the evaluation of reliability and robustness against the model uncertainty and measurement noise.

This paper suggests some future research issues that need to be investigated. One of the most crucial issues is the experimental analysis of the proposed scheme, which needs to be conducted before industrial applications. However, the development of the proposed solution for real wind turbines is promising. Furthermore, the numerical calculation of the captured wind energy can be evaluated, considering the reduced downtime, operation and maintenance costs. This can further highlight the economic benefits of the proposed controller.

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