



Universiteit  
Leiden  
The Netherlands

## Density profile of the ambient circumnuclear medium in Seyfert 1 galaxies

Wang, Y.; He, Z.; Mao, J.; Kaastra, J.S.; Xue, Y.; Mehdipour, M.

### Citation

Wang, Y., He, Z., Mao, J., Kaastra, J. S., Xue, Y., & Mehdipour, M. (2022). Density profile of the ambient circumnuclear medium in Seyfert 1 galaxies. *The Astrophysical Journal*, 928(1). doi:10.3847/1538-4357/ac524d

Version: Publisher's Version  
License: [Creative Commons CC BY 4.0 license](https://creativecommons.org/licenses/by/4.0/)  
Downloaded from: <https://hdl.handle.net/1887/3515504>

**Note:** To cite this publication please use the final published version (if applicable).



# Density Profile of the Ambient Circumnuclear Medium in Seyfert 1 Galaxies

Yijun Wang (王倚君)<sup>1,2,3,4</sup> , Zhicheng He (何志成)<sup>3,4</sup> , Junjie Mao (毛俊捷)<sup>5,6</sup>, Jelle Kaastra<sup>6,7</sup>,Yongquan Xue (薛永泉)<sup>3,4</sup> , and Missagh Mehdipour<sup>8</sup> <sup>1</sup> Department of Astronomy, Nanjing University, Nanjing 210093, People's Republic of China<sup>2</sup> Key Laboratory of Modern Astronomy and Astrophysics (Nanjing University), Ministry of Education, Nanjing 210093, People's Republic of China<sup>3</sup> CAS Key Laboratory for Research in Galaxies and Cosmology, Department of Astronomy, University of Science and Technology of China, Hefei 230026, People's Republic of China; [zcho@ustc.edu.cn](mailto:zcho@ustc.edu.cn)<sup>4</sup> School of Astronomy and Space Science, University of Science and Technology of China, Hefei 230026, People's Republic of China<sup>5</sup> Department of Physical, Hiroshima University, 1-3-1 Kagamiyama, Higashi Hiroshima, Hiroshima 739-8526, Japan<sup>6</sup> SRON Netherlands Institute for Space Research, Niels Bohrweg 4, 2333 CA Leiden, The Netherlands<sup>7</sup> Leiden Observatory, Leiden University, Niels Bohrweg 2, 2300 RA Leiden, The Netherlands<sup>8</sup> Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA

Received 2021 September 8; revised 2022 January 12; accepted 2022 February 3; published 2022 March 22

## Abstract

The shape of the ambient circumnuclear medium (ACM) density profile can probe the history of accretion onto the central supermassive black holes in galaxies and the circumnuclear environment. However, due to the limitations of instrument resolution, the density profiles of the ACM for most galaxies remain largely unknown. In this work, we propose a novel method to measure the ACM density profile of active galactic nuclei (AGNs) by the equilibrium between the radiation pressure on the warm absorbers (WAs, a type of AGN outflow) and the drag pressure from the ACM. We study the correlation between the outflow velocity and ionization parameter of WAs in each of the five Seyfert 1 galaxies (NGC 3227, NGC 3783, NGC 4051, NGC 4593, and NGC 5548), inferring that the density profile of the ACM is between  $n \propto r^{-1.7}$  and  $n \propto r^{-2.15}$  ( $n$  is number density and  $r$  is distance) from 0.01 pc to parsec scales in these five AGNs. Our results indicate that the ACM density profile in Seyfert 1 galaxies is steeper than the prediction by the spherically symmetric Bondi accretion model and the simulated results of the hot accretion flow, but more in line with the prediction by the standard thin-disk model.

*Unified Astronomy Thesaurus concepts:* Active galactic nuclei (16); Accretion (14); Seyfert galaxies (1447); Galaxy nuclei (609); Interstellar medium (847)

## 1. Introduction

The ambient circumnuclear medium (ACM) in the center of galaxies can probe the accretion history of the central supermassive black holes (SMBHs) in galaxies. Different accretion models correspond to different density profiles of the ACM. The classical Bondi accretion (spherically symmetrical accretion; Bondi 1952) predicts that the density profile of the accretion flow is  $n \propto r^{-1.5}$  ( $n$  is number density and  $r$  is distance) within the Bondi radius, and is a constant at larger radii (Frank et al. 2002). The density profile of the hot accretion flow, such as advection-dominated accretion flows (see Narayan & Yi 1994 and Yuan & Narayan 2014 for reviews), is between  $n \propto r^{-0.5}$  and  $n \propto r^{-1}$  according to simulations (Yuan et al. 2012). The theory of the standard cold, thin accretion disk (Shakura & Sunyaev 1973) predicts that the density profile of the accretion flow is  $n \propto r^{-15/8}$  (Frank et al. 2002). The multi-wavelength observations toward the center of the Milky Way indicated that the density profile of the ACM is  $n \propto r^{-1}$  at several hundred Schwarzschild radii (Gillessen et al. 2019), and  $n \propto r^{-1.5}$  in the hot gas halo at the kiloparsec scale (Miller & Bregman 2015). Chandra X-ray observations toward the center of M87 and NGC 3115 show that the density profiles of their ACM are  $n \propto r^{-1}$  within the Bondi radius (Wong et al. 2011; Russell et al. 2015). However, due to the limitations of the instrument resolution, the density profiles of the ACM for most galaxies are still unknown. One way to infer the density profile of the ACM is

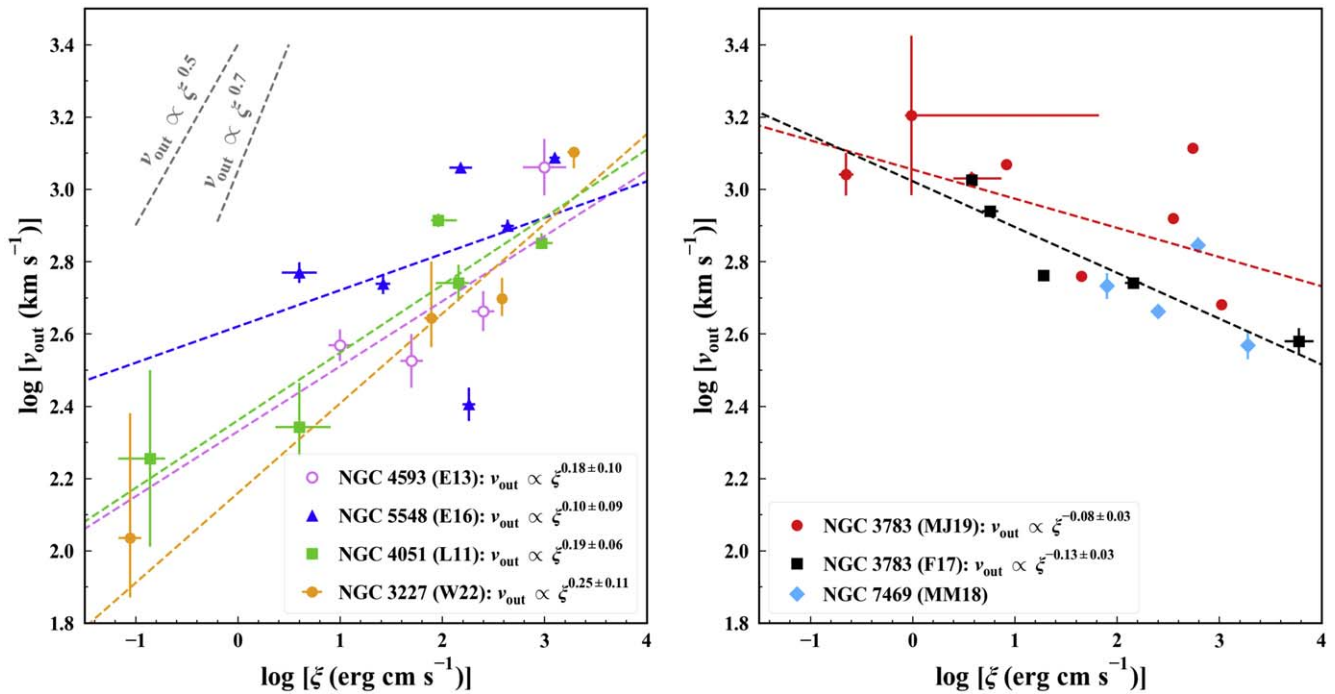
through fitting the spectral energy distribution of tidal disruption events (TDEs; a star disrupted by the tidal forces from the SMBH), which can trace the interaction process between the outflows from TDEs and the ACM (Alexander et al. 2016; Eftekhari et al. 2018; Alexander et al. 2020; Anderson et al. 2020). However, TDEs are only detected in a small number of galaxies and are difficult to identify in active galactic nuclei (AGNs; Gezari 2021). Besides, for AGNs, the emission from the accretion disk or jet will overshadow the emission from the interaction between outflows and ACM at small scales. In this work, we propose a novel way to estimate the density profile of the ACM in AGNs.

AGNs usually play an important role in forming and driving outflows that might further affect the star formation of their host galaxies (see King & Pounds 2015; He et al. 2019, 2022, and Chen et al. 2022 for reviews). These outflows might interact with the ACM. Warm absorbers (WAs) are part of AGN ionized outflows (e.g., Laha et al. 2014), which are detected in roughly half of nearby AGNs (e.g., Reynolds 1997; Kaastra et al. 2000; Tombesi et al. 2013). WAs usually consist of several ionization phases (e.g., Laha et al. 2014) and are located from the accretion disk to the narrow-line region (e.g., Reynolds & Fabian 1995; Elvis 2000; Blustin et al. 2005). WAs have outflowing velocities up to a few thousand kilometers per second (e.g., Kaastra et al. 2000; Ebrero et al. 2013), and are considered to be driven by radiation pressure (e.g., Proga & Kallman 2004), magnetic forces (e.g., Blandford & Payne 1982; Fukumura et al. 2010; Li & Cao 2019), or thermal pressure (e.g., Begelman et al. 1983; Mizumoto et al. 2019).

For the radiatively driven outflowing mechanism, the outflow momentum rate  $\dot{P}_{\text{out}} (\propto n_{\text{H}} r^2 v_{\text{out}}^2)$  approximates to the momentum flux of the radiation field  $\dot{P}_{\text{rad}} (\equiv L_{\text{bol}}/c)$  (Gofford et al. 2015),



Original content from this work may be used under the terms of the [Creative Commons Attribution 4.0 licence](https://creativecommons.org/licenses/by/4.0/). Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.



**Figure 1.** The correlation between the outflow velocity ( $v_{\text{out}}$ ) and ionization parameter ( $\xi$ ) for the following six Seyfert 1 galaxies: NGC 3227 (orange solid circles in the left panel), NGC 3783 (red solid circles and black squares in the right panel), NGC 4051 (green squares in the left panel), NGC 4593 (pink hollow circles in the left panel), NGC 5548 (blue triangles in the left panel), and NGC 7469 (sky-blue diamonds in the right panel). The observational data are from the previously published papers: Wang et al. (2022; W22), Fu et al. (2017; F17), Mao et al. (2019; MJ19), Lobban et al. (2011; L11), Ebrero et al. (2013; E13), Ebrero et al. (2016; E16), and Mehdipour et al. (2018; MM18). The dashed lines represent the best-fit linear models. The gray dashed lines represent the predicted correlations of radiation-driven and MHD-driven outflowing mechanisms, so only the observational data are shown here.

which can produce a simple scaling relation of  $v_{\text{out}} \propto \xi^{0.5}$  (Tombesi et al. 2013). For the magnetohydrodynamically (MHD) driven outflowing mechanism, Fukumura et al. (2010) suggested a few scaling relations between  $v_{\text{out}}$ ,  $r$ , and  $\xi$ :  $v_{\text{out}} \propto r^{-\frac{1}{2}} \propto \xi^{\frac{1}{2(2q-1)}}$ . Behar (2009) indicated that the parameter  $q$  is between  $\frac{6}{7}$  and 1 for WA-outflowing winds in Seyfert galaxies. Therefore, the scaling relation between  $v_{\text{out}}$  and  $\xi$  in the MHD scenario is estimated to be between  $v_{\text{out}} \propto \xi^{0.5}$  and  $v_{\text{out}} \propto \xi^{0.7}$  (see Figure 1). However, the observational results show that the index of the  $v_{\text{out}}-\xi$  relation is usually smaller than 0.5 (e.g., Tombesi et al. 2013; Laha et al. 2014) or see Figure 1 in this work, which cannot be explained by the above models.

In this work, we consider that WAs are in a pressure equilibrium state, which means that the radiation pressure on the WAs is comparable to the drag pressure from the ACM. With that, we will use the fitting results for the  $v_{\text{out}}-\xi$  relation of WAs to infer the shape of the density profile of the ACM in AGNs. The structure of this work is shown as follows. The method that is applied to infer the density profile of the ACM in AGNs is described in Section 2. In Section 3, we introduce the historical data that are used in this work. In Section 4, we show the fitting results of the observational data, which are further used to infer the density profile of the ACM in AGNs. In Section 5, we discuss the scope of application of our method. Finally, we summarize our conclusions in Section 6.

## 2. Method

The outflows in AGNs might be driven by multiple mechanisms but, for simplicity, we only consider the radiatively driven outflowing mechanism in this work. The radiation pressure from the AGN radiation on the WA gas

**Table 1**  
Basic Properties of Each Object for the Six Seyfert Galaxies and Previously Published X-Ray Data Used in This Work

| Source   | Seyfert Type | Redshift | WA References   |
|----------|--------------|----------|---|
| NGC 3227 | Sy1.5        | 0.004    | Wang et al. (2022) <sup>a</sup>                                   |
| NGC 3783 | Sy1          | 0.010    | Fu et al. (2017) <sup>a</sup><br>Mao et al. (2019) <sup>a,b</sup> |
| NGC 4051 | Sy1.5        | 0.002    | Lobban et al. (2011) <sup>b</sup>                                 |
| NGC 4593 | Sy1          | 0.008    | Ebrero et al. (2013) <sup>a,b</sup>                               |
| NGC 5548 | Sy1.5        | 0.017    | Ebrero et al. (2016) <sup>a,b</sup>                               |
| NGC 7469 | Sy1.2        | 0.016    | Mehdipour et al. (2018) <sup>b</sup>                              |

**Notes.** Seyfert type and redshift of each object are obtained from the NASA/IPAC Extragalactic Database (NED; <https://ned.ipac.caltech.edu/>).

<sup>a</sup> XMM-Newton X-ray data.

<sup>b</sup> Chandra X-ray data.

(Mo et al. 2010) is

$$P_{\text{rad}} = \frac{L_{\text{ion}}}{4\pi r^2 c}, \quad (1)$$

where  $L_{\text{ion}}$  is the ionizing luminosity over 1–1000 Ryd,  $r$  is the radial distance of the absorbing gas to the central engine, and  $c$  is the speed of light. The drag pressure (Batchelor 2000) produced by the ACM on the WAs is

$$P_{\text{D}} = \frac{1}{2} C_{\text{D}} n_{\text{ACM}} m_{\text{p}} v_{\text{out}}^2, \quad (2)$$

where  $C_{\text{D}}$  is the drag coefficient which is probably equal to 1 for compressible gas or clouds,  $n_{\text{ACM}}$  is the number density of the ACM, and  $m_{\text{p}}$  is the proton mass. The outflowing velocities

**Table 2**Best-fit Parameters of  $\log[v_{\text{out}} (\text{km s}^{-1})] = a \times \log[\xi (\text{erg cm s}^{-1})] + b$  using LINMIX, ODR, and BCES Methods, and Index  $k$  of the Density Profile of the ACM

| Sources           | Data      | Parameter | $\log[v_{\text{out}} (\text{km s}^{-1})] = a \times \log[\xi (\text{erg cm s}^{-1})] + b$ |                         |                         | $k = 2a(m - 2) + 2$       |
|-------------------|-----------|-----------|---|-------------------------|-------------------------|---------------------------|
|                   |           |           | Fitting Method  |                         |                         | $k (m = 1.42)^{\text{a}}$ |
|                   |           |           | LINMIX  | ODR                     | BCES                    |                           |
| Individual Source |           |           |   |                         |                         |                           |
| NGC 3227          | W22       | $a$       | $\lesssim 0.24$   | $0.25 \pm 0.11^{\star}$ | $0.35 \pm 0.10$         | $1.71 \pm 0.13$           |
|                   |           | $b$       | $\lesssim 2.15$   | $2.16 \pm 0.29$         | $1.93 \pm 0.32$         |                           |
| NGC 4051          | L11       | $a$       | $0.19 \pm 0.06^{\star}$   | $0.20 \pm 0.10$         | $0.03 \pm 0.09$         | $1.78 \pm 0.07$           |
|                   |           | $b$       | $2.36 \pm 0.13$   | $2.35 \pm 0.20$         | $2.79 \pm 0.23$         |                           |
| NGC 4593          | E13       | $a$       | $\lesssim 0.18$   | $0.27 \pm 0.24$         | $0.18 \pm 0.10^{\star}$ | $1.79 \pm 0.11$           |
|                   |           | $b$       | $\lesssim 2.06$   | $2.09 \pm 0.58$         | $2.33 \pm 0.19$         |                           |
| NGC 5548          | E16       | $a$       | $0.10 \pm 0.09^{\star}$   | $0.13 \pm 0.18$         | $0.24 \pm 0.12$         | $1.88 \pm 0.10$           |
|                   |           | $b$       | $2.62 \pm 0.19$   | $2.54 \pm 0.42$         | $2.34 \pm 0.34$         |                           |
| NGC 3783          | F17       | $a$       | $-0.13 \pm 0.03^{\star}$  | $-0.16 \pm 0.12$        | $-0.31 \pm 0.10$        | $2.15 \pm 0.03$           |
|                   |           | $b$       | $3.02 \pm 0.06$   | $3.04 \pm 0.11$         | $3.17 \pm 0.12$         |                           |
|                   | MJ19      | $a$       | $-0.08 \pm 0.03^{\star}$  | $-0.10 \pm 0.07$        | $-0.08 \pm 0.09$        | $2.09 \pm 0.03$           |
|                   |           | $b$       | $3.05 \pm 0.06$   | $3.09 \pm 0.08$         | $3.04 \pm 0.21$         |                           |
| NGC 7469          | MM18      | $a$       | $\lesssim 0.64$   | $-0.06 \pm 0.20$        | $0.06 \pm 0.19$         | ...                       |
|                   |           | $b$       | $\lesssim -0.56$  | $2.88 \pm 0.55$         | $2.54 \pm 0.47$         |                           |
| Total             |           |           |   |                         |                         |                           |
| NGC 3227, 4051,   | W22, L11, | $a$       | $0.19 \pm 0.02^{\star}$   | $0.20 \pm 0.03$         | $0.26 \pm 0.06$         | $1.78 \pm 0.02$           |
| 4593, 5548        | E13, E16  | $b$       | $2.37 \pm 0.05$   | $2.36 \pm 0.07$         | $2.25 \pm 0.16$         |                           |

**Notes.** The fitting results followed by “ $\star$ ” are used to calculate the index  $k$  and are plotted in Figure 1. The observational data are from the previously published papers: Wang et al. (2022; W22), Fu et al. (2017; F17), Mao et al. (2019; MJ19), Lobban et al. (2011; L11), Ebrero et al. (2013; E13), Ebrero et al. (2016; E16), and Mehdipour et al. (2018; MM18). The data of NGC 3227, NGC 4051, NGC 4593, and NGC 5548 are also fitted together as a reference (see “NGC 3227, 4051, 4593, and 5548” in the “Total”).

<sup>a</sup>  $m = 1.42$  is obtained for a sample of 35 Seyfert 1 galaxies from Tombesi et al. (2013) using the absorption measure distribution.

of WAs are nearly constant over several years (e.g., Silva et al. 2018). In this work we assume that WAs are in a pressure equilibrium state where the radiation pressure on the WAs is comparable to the drag pressure from the ACM:

$$P_{\text{rad}} \simeq P_{\text{D}}. \quad (3)$$

According to Tarter et al. (1969), the ionization parameter of WAs can be defined by

$$\xi = \frac{L_{\text{ion}}}{n_{\text{e}} r^2}, \quad (4)$$

where  $n_{\text{e}}$  is the electron number density of the WA gas. We assume that the electron number densities of the WA gas and the ACM follow the power-law distributions:

$$\begin{aligned} n_{\text{e}} &= n_{\text{e},0} \left( \frac{r}{r_0} \right)^{-m}, \\ n_{\text{ACM}} &= n_{\text{ACM},0} \left( \frac{r}{r_0} \right)^{-k}, \end{aligned} \quad (5)$$

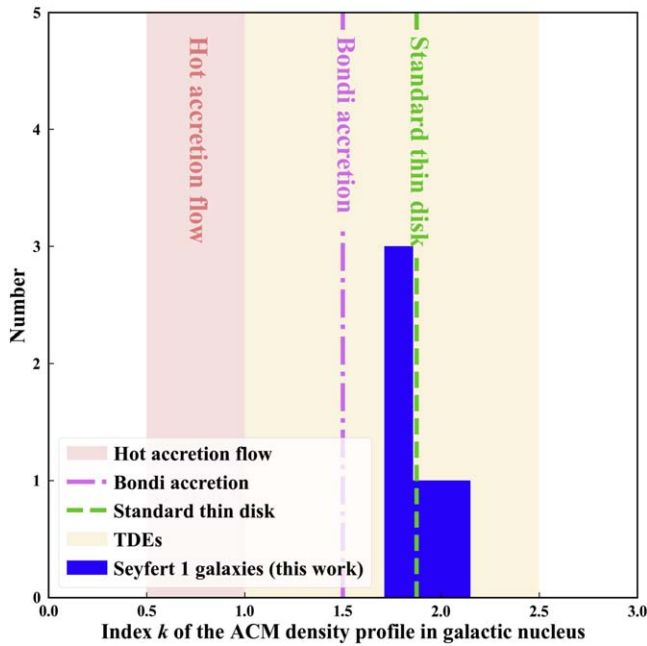
where  $r_0$  is the launching radius of the WA cloud,  $n_{\text{e},0}$  is the number density of WA cloud at  $r_0$ , and  $n_{\text{ACM},0}$  is the number density of the ACM at  $r_0$ . Therefore, combining Equations (4) and (5), we can obtain a correlation between  $\xi$  and  $v_{\text{out}}$ :

$$v_{\text{out}} = \left[ \frac{L_{\text{ion}}^{\frac{m-k}{m-2}}}{2\pi m_p c} \cdot \frac{n_{\text{e},0}^{\frac{k-2}{m-2}}}{n_{\text{ACM},0}} \cdot r_0^{\frac{2(k-m)}{m-2}} \right]^{1/2} \xi^{\frac{k-2}{2(m-2)}}. \quad (6)$$

### 3. Data and Fitting

In order to describe the correlation between  $v_{\text{out}}$  and  $\xi$  of WAs for the observational data in individual AGN (see Equation (6)), high-resolution X-ray spectra and at least four WA components are required. Finally, we collect the parameters of WAs from the previously published papers for the following six Seyfert 1 galaxies (see Table 1):

1. NGC 3227: Wang et al. (2022) found four WA components using the XMM-Newton spectra data.
2. NGC 3783: Fu et al. (2017) found five WA components through fitting the XMM-Newton spectra, while



**Figure 2.** The distribution of the ACM density profile index  $k$  for the five Seyfert 1 galaxies (NGC 3227, NGC 4051, NGC 4593, NGC 5548, and NGC 3783) in this work (blue histogram). The green dashed line represents the predicted index by the standard thin-disk model (Frank et al. 2002). The purple dashed-dotted line represents the predicted index by the Bondi accretion model (Frank et al. 2002). The red region represents the predicted range of the index by the hot accretion flow simulations (Yuan et al. 2012). The yellow region represents the observational range of the index in TDEs (Alexander et al. 2020).

Mao et al. (2019) found nine WA components using both the XMM-Newton and Chandra data.

3. *NGC 4051*: Lobban et al. (2011) found five WA components using the Chandra spectral data.
4. *NGC 4593*: Ebrero et al. (2013) found four WA components through fitting the spectra of XMM-Newton and Chandra.
5. *NGC 5548*: Ebrero et al. (2016) found six WA components through fitting the spectra of XMM-Newton and Chandra (H02 data in Ebrero et al. 2016).
6. *NGC 7469*: Mehdipour et al. (2018) found four WA components through fitting the spectra of Chandra.

Then we fit the correlation between  $\xi$  and  $v_{\text{out}}$  in each source using the following linear model:

$$\log[v_{\text{out}} (\text{km s}^{-1})] = a \times \log[\xi (\text{erg cm s}^{-1})] + b, \quad (7)$$

where  $a$  corresponds to the theoretical index  $(k-2)/[2(m-2)]$  in Equation (6), i.e.,  $a = (k-2)/[2(m-2)]$ . Therefore, the index of the density profile of the ACM can be calculated by

$$k = 2a(m-2) + 2. \quad (8)$$

We mainly use the LINMIX<sup>9</sup> method (Kelly 2007) to fit the observational data. The LINMIX method performs the linear regression based on a Bayesian approach, which runs a Markov Chain Monte Carlo algorithm to calculate the posterior distribution and can account for measurement errors on both variables in the fit. However, for NGC 3227 and NGC 4593, this method can only give an upper limit for the parameters (see

Table 2). Therefore, we also use the following two methods as supplements: Orthogonal Distance Regression<sup>10</sup> (ODR; Boggs et al. 1989), and bivariate correlated errors and intrinsic scatter<sup>11</sup> (BCES; Akritas & Bershady 1996; Nemmen et al. 2012). Both of these two methods can also deal with measurement errors on both variables. The BCES method is a weighted least-squares estimator, and the ODR method uses the least-squares method to minimize the weighed orthogonal distance from the data to the fitted curve. The LINMIX method can provide a consistent fitting result to at least one of the other two methods (see Table 2).

## 4. Results

As Figure 1 shows, there is a positive correlation between  $v_{\text{out}}$  and  $\xi$  for NGC 3227, NGC 4051, NGC 4593, and NGC 5548 (the coefficient  $a$  of Equation (7) ranges from 0.10 to 0.25; also see Table 2), while NGC 3783 shows a negative correlation. For NGC 3783,  $a$  is  $-0.13 \pm 0.03$  for the data from Fu et al. (2017), and is  $-0.08 \pm 0.03$  for the data from Mao et al. (2019). However, the error bar of coefficient  $a$  is large, so we fit the data of NGC 3227, NGC 4051, NGC 4593, and NGC 5548 together as a reference, resulting in  $a = 0.19 \pm 0.02$ . The fitting result in an individual source is consistent with the total fitting result in the sample. As mentioned in Section 1, the power-law indexes  $a$  for these Seyfert 1 galaxies are smaller than the predicted values by the theories: 0.5 for the radiatively driven outflowing mechanism, and larger than 0.5 for the MHD-driven outflowing mechanism. The  $v_{\text{out}}-\xi$  relation of NGC 7469 cannot be constrained, so its ACM density profile will not be discussed further (see Table 2), and its observational data are shown in Figure 1 as a reference.

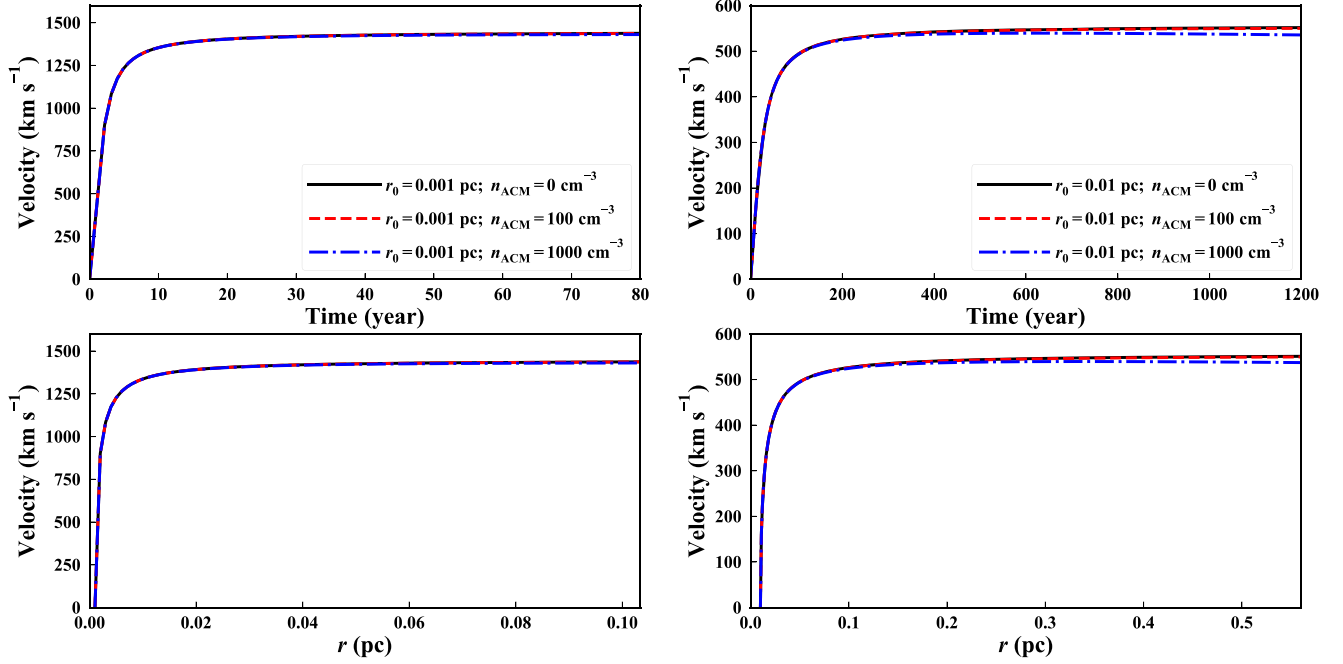
The number density distribution of WAs can be estimated by the absorption measure distribution (Holczer et al. 2007; Behar 2009). Tombesi et al. (2013) estimated that  $m = 1.42$  for WAs in a sample of 35 Seyfert 1 galaxies. Combining Equation (8) and  $m = 1.42$  (Tombesi et al. 2013), the density profiles of the ACM in these Seyfert 1 galaxies are estimated to be between  $n \propto r^{-1.7}$  and  $n \propto r^{-2.15}$  (see Table 2) from 0.01 pc to parsec scales, or even larger scales (the distance range of WAs). Both Tombesi et al. (2013) and Laha et al. (2014) investigated the correlation between  $v_{\text{out}}$  and  $\xi$  for WAs in a large AGN sample, which obtained  $a = 0.31$  and  $a = 0.12$ , respectively. Therefore, the index of  $k$  is 1.64 and 1.82 for Tombesi et al. (2013) and Laha et al. (2014), respectively. Our results are similar to those in AGN samples. The density profile indexes  $k$  of the ACM in the five Seyfert 1 galaxies of our sample (NGC 3227, NGC 3783, NGC 4051, NGC 4593, and NGC 5548) are within the range of  $k$  for the ACM in TDEs (between  $-1$  and  $-2.5$ ; Alexander et al. 2020; see Figure 2).

The density profile of the ACM within the Bondi radius might be connected to the accretion models. The Bondi radius can be expressed by  $r_{\text{B}} = 2GM_{\text{BH}}/c_{\text{s},\infty}^2$ , where  $M_{\text{BH}}$  is the SMBH mass and  $c_{\text{s},\infty}$  is the sound speed at infinity Bondi 1952. For simplicity, we assume that the sound speeds at infinity of our sample are similar to that of M87 ( $r_{\text{B}} = 0.11-0.22$  kpc with  $M_{\text{BH}} = 3.5 \times 10^9 M_{\odot}$ ; Russell et al. 2015) and Sgr A\* ( $r_{\text{B}} = 0.4$  pc with  $M_{\text{BH}} = 4 \times 10^6 M_{\odot}$ ; Li et al. 2015). Thus, according to the average  $M_{\text{BH}}$  of our sample ( $\sim 10^7 M_{\odot}$ ; Bentz &

<sup>9</sup> <https://linmix.readthedocs.io/en/latest/src/linmix.html>

<sup>10</sup> <https://docs.scipy.org/doc/scipy/reference/odr.html>

<sup>11</sup> <https://github.com/rsnemmen/BCES>



**Figure 3.** Estimating the acceleration timescale of WA outflows. The left two panels show the case of a launching radius ( $r_0$ ) of 0.001 pc and the right two panels show the case of a launching radius of 0.01 pc. The black solid, red dashed, and blue dashed–dotted lines represent the calculation of the ACM number density ( $n_{\text{ACM}}$ ) of 0, 100, and 1000  $\text{cm}^{-3}$ , respectively. It is obvious that the acceleration timescale is much shorter than the lifetime of WA.

Katz 2015), the Bondi radii of our sample might be between 0.5 pc and 1 pc. Warm absorbers can exist from the scale within the Bondi radius (e.g., Ebrero et al. 2016; Wang et al. 2022) to the kpc scale Laha et al. 2021. Although the large scale might not be associated with the accretion flow, given that most of the WAs in our sample might be located within or around the Bondi radius (e.g., Ebrero et al. 2016; Wang et al. 2022), we can briefly compare the density profiles between the ACM and the accretion flow here. The indexes  $k$  of the five Seyfert 1 galaxies are larger than the predicted value by the spherically symmetrical Bondi accretion model ( $-1.5$ ; Frank et al. 2002) and the simulated results of the hot accretion flow (between  $-0.5$  and  $-1.0$ ; Yuan et al. 2012), but relatively consistent with the prediction by the standard thin disk model ( $-15/8$ ; Frank et al. 2002) (see Figure 2).

## 5. Discussions

### 5.1. Acceleration Timescale Required before Equilibrium

To verify whether the assumption about the pressure equilibrium is feasible, we first estimate the acceleration timescale before reaching equilibrium of WA outflows. Under the action of the radiation pressure and drag pressure, the motion equation of the WA clouds is

$$\frac{vdv}{dr} = \frac{f_L L_{\text{ion}}}{4\pi c N_{\text{H}} m_p r^2} - \frac{C_D n_{\text{ACM}}}{2N_{\text{H}}} v^2, \quad (9)$$

where  $f_L$  is the fraction of the ionizing luminosity being absorbed or scattered by the WA cloud, which is about 2% according to Grafton-Waters et al. (2020) and Wang et al. (2022), and  $m_p$  is the mass of protons. The average ionizing luminosity of the sources in our sample is  $5 \times 10^{43} \text{ erg s}^{-1}$ . We simply set a constant column density to be  $N_{\text{H}} = 10^{22.5} \text{ cm}^{-2}$ , which is the maximum  $N_{\text{H}}$  for WAs obtained in AGN samples

(Tombsi et al. 2013; Laha et al. 2014). As shown in Figure 3, we calculate the acceleration timescale for the launching radii  $r_0$  of 0.001 and 0.01 pc, with  $n_{\text{ACM}}$  being 0, 100, and 1000  $\text{cm}^{-3}$ . For the WA component that is close to the SMBH, the typical acceleration distance might be about 0.01 pc and the typical acceleration timescale might be about 10 yr (see the left two panels of Figure 3), while the existence distance of this WA component might be larger than 0.01 pc (Laha et al. 2021), which means that its existence timescale might be longer than its acceleration timescale. For the WA component that is relatively farther away, the typical acceleration distance might be about 0.05 pc and the typical acceleration timescale might be about 100 yr (see the right two panels of Figure 3), while the existence distance of this WA component is larger than 0.05 pc (e.g., Ebrero et al. 2016; Wang et al. 2022), which indicates that its acceleration timescale might be shorter than the existence timescale. These imply that the lifetimes of WAs are much larger than the acceleration timescales. These results indicate that WAs can stay in an equilibrium state during most periods of their lives.

### 5.2. Imbalance Caused by AGN Variabilities

The AGN variabilities can break the equilibrium state of WAs. Assuming the central luminosity changes from  $L$  to  $L'$  with  $L' = (1 + f)L$ , the radiation pressure acting on each component of WAs along the line of sight will become  $P'_{\text{rad}} = (1 + f)P_{\text{rad}}$  one by one. According to Equations (1) and (2), we can then easily find that  $P'_{\text{rad}} = (1 + f)P_{\text{D}}$  for each WA component. This means that the variability only has an impact on the estimation for the coefficient of Equation (6) rather than the index. That is to say, even if the AGN variabilities are considered, the estimation for the index of the ACM density profile will not be affected.

## 6. Summary

In this work, we propose a novel method to measure the ACM density profile by the equilibrium between the radiation pressure on the WA outflows and the drag pressure from the ACM for the following six Seyfert 1 galaxies: NGC 3227, NGC 3783, NGC 4051, NGC 4593, NGC 5548, and NGC 7469.

We study the correlation between outflow velocity and ionization parameter of the WAs in five Seyfert 1 galaxies of our sample (NGC 3227, NGC 3783, NGC 4051, NGC 4593, and NGC 5548). According to the fitting results of the  $v_{\text{out}}-\xi$  relation, we infer that the density profile of the ACM is between  $n \propto r^{-1.7}$  and  $n \propto r^{-2.15}$  from 0.01 pc to parsec scales in these five AGNs. The indexes of the ACM density profiles in these five Seyfert galaxies are within the range of the indexes in TDEs. Our results indicate that the ACM density profile in Seyfert 1 galaxies is steeper than the prediction by the spherically symmetric Bondi accretion model and the simulation results of the hot accretion flow, but more in line with the prediction by the standard thin-disk model.

We thank the referee for constructive comments that improved this paper. Y.J.W. acknowledges support from the start-up research fund of the School of Astronomy and Space Science of Nanjing University. Y.J.W. and Y.Q.X. acknowledge support from NSFC-12025303, 11890693, the CAS Frontier Science Key Research Program (QYZDJ-SSW-SLH006), and the K.C. Wong Education Foundation. Z.-C.H. is supported by NSFC-11903031, 12192220, 12192221, and USTC Research Funds of the Double First-Class Initiative YD 3440002001. This research has made use of the NASA/IPAC Extragalactic Database (NED), which is funded by the National Aeronautics and Space Administration and operated by the California Institute of Technology.

## ORCID iDs

Yijun Wang (王倚君)  <https://orcid.org/0000-0002-1010-7763>  
 Zhicheng He (何志成)  <https://orcid.org/0000-0003-3667-1060>  
 Yongquan Xue (薛永泉)  <https://orcid.org/0000-0002-1935-8104>  
 Missagh Mehdipour  <https://orcid.org/0000-0002-4992-4664>

## References

Akritas, M. G., & Bershad, M. A. 1996, *ApJ*, 470, 706  
 Alexander, K. D., Berger, E., Guillochon, J., Zauderer, B. A., & Williams, P. K. G. 2016, *ApJL*, 819, L25  
 Alexander, K. D., van Velzen, S., Horesh, A., & Zauderer, B. A. 2020, *SSRv*, 216, 81  
 Anderson, M. M., Mooley, K. P., Hallinan, G., et al. 2020, *ApJ*, 903, 116  
 Batchelor, G. K. 2000, *An Introduction to Fluid Dynamics* (Cambridge: Cambridge Univ. Press)  
 Begelman, M. C., McKee, C. F., & Shields, G. A. 1983, *ApJ*, 271, 70  
 Behar, E. 2009, *ApJ*, 703, 1346

Bentz, M. C., & Katz, S. 2015, *PASP*, 127, 67  
 Blandford, R. D., & Payne, D. G. 1982, *MNRAS*, 199, 883  
 Blustin, A. J., Page, M. J., Fuerst, S. V., Branduardi-Raymont, G., & Ashton, C. E. 2005, *A&A*, 431, 111  
 Boggs, P. T., Donaldson, J. R., Byrd, R. H., & Schnabel, R. B. 1989, *ACM Trans. Math. Softw.*, 15, 348  
 Bondi, H. 1952, *MNRAS*, 112, 195  
 Chen, Z., He, Z., & Ho, L. S. 2022, *NatAs*, in press  
 Ebrero, J., Kaastra, J. S., Kriss, G. A., et al. 2016, *A&A*, 587, A129  
 Ebrero, J., Kaastra, J. S., Kriss, G. A., de Vries, C. P., & Costantini, E. 2013, *MNRAS*, 435, 3028  
 Eftekhari, T., Berger, E., Zauderer, B. A., Margutti, R., & Alexander, K. D. 2018, *ApJ*, 854, 86  
 Elvis, M. 2000, *ApJ*, 545, 63  
 Frank, J., King, A., & Raine, D. J. 2002, *Accretion Power in Astrophysics: Third Edition* (Cambridge: Cambridge Univ. Press)  
 Fu, X.-D., Zhang, S.-N., Sun, W., Niu, S., & Ji, L. 2017, *RAA*, 17, 095  
 Fukumura, K., Kazanas, D., Contopoulos, I., & Behar, E. 2010, *ApJ*, 715, 636  
 Gezari, S. 2021, *ARA&A*, 59, 21  
 Gillessen, S., Plewa, P. M., Widmann, F., et al. 2019, *ApJ*, 871, 126  
 Gofford, J., Reeves, J. N., McLaughlin, D. E., et al. 2015, *MNRAS*, 451, 4169  
 Grafton-Waters, S., Branduardi-Raymont, G., Mehdipour, M., et al. 2020, *A&A*, 633, A62  
 He, Z., Wang, T., Liu, G., et al. 2019, *NatAs*, 3, 265  
 He, Z., Liu, G., Wang, T., et al. 2022, *SciAdv*, 8, eabk3291  
 Holczer, T., Behar, E., & Kaspi, S. 2007, *ApJ*, 663, 799  
 Kaastra, J. S., Mewe, R., Liedahl, D. A., Komossa, S., & Brinkman, A. C. 2000, *A&A*, 354, L83  
 Kelly, B. C. 2007, *ApJ*, 665, 1489  
 King, A., & Pounds, K. 2015, *ARA&A*, 53, 115  
 Laha, S., Guainazzi, M., Dewangan, G. C., Chakravorty, S., & Kembhavi, A. K. 2014, *MNRAS*, 441, 2613  
 Laha, S., Reynolds, C. S., Reeves, J., et al. 2021, *NatAs*, 5, 13  
 Li, J., & Cao, X. 2019, *ApJ*, 872, 149  
 Li, Y.-P., Yuan, F., & Wang, Q. D. 2015, *ApJ*, 798, 22  
 Lobban, A. P., Reeves, J. N., Miller, L., et al. 2011, *MNRAS*, 414, 1965  
 Mao, J., Mehdipour, M., Kaastra, J. S., et al. 2019, *A&A*, 621, A99  
 Mehdipour, M., Kaastra, J. S., Costantini, E., et al. 2018, *A&A*, 615, A72  
 Miller, M. J., & Bregman, J. N. 2015, *ApJ*, 800, 14  
 Mizumoto, M., Done, C., Tomaru, R., & Edwards, I. 2019, *MNRAS*, 489, 1152  
 Mo, H., van den Bosch, F. C., & White, S. 2010, *Galaxy Formation and Evolution* (Cambridge: Cambridge Univ. Press)  
 Narayan, R., & Yi, I. 1994, *ApJL*, 428, L13  
 Nemmen, R. S., Georganopoulos, M., Guirrec, S., et al. 2012, *Sci*, 338, 1445  
 Proga, D., & Kallman, T. R. 2004, *ApJ*, 616, 688  
 Reynolds, C. S. 1997, *MNRAS*, 286, 513  
 Reynolds, C. S., & Fabian, A. C. 1995, *MNRAS*, 273, 1167  
 Russell, H. R., Fabian, A. C., McNamara, B. R., & Broderick, A. E. 2015, *MNRAS*, 451, 588  
 Shakura, N. I., & Sunyaev, R. A. 1973, *A&A*, 500, 33  
 Silva, C. V., Costantini, E., Giustini, M., et al. 2018, *MNRAS*, 480, 2334  
 Tarter, C. B., Tucker, W. H., & Salpeter, E. E. 1969, *ApJ*, 156, 943  
 Tombesi, F., Cappi, M., Reeves, J. N., et al. 2013, *MNRAS*, 430, 1102  
 Wang, Y., Kaastra, J., Mehdipour, M., et al. 2022, *A&A*, 657, A77  
 Wong, K.-W., Irwin, J. A., Yukita, M., et al. 2011, *ApJL*, 736, L23  
 Yuan, F., & Narayan, R. 2014, *ARA&A*, 52, 529  
 Yuan, F., Wu, M., & Bu, D. 2012, *ApJ*, 761, 129