

1 **Modelling changes in soil structure caused by**  
2 **livestock treading**

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14 **HIGHLIGHTS**

15 • Soil compaction increases bulk density and reduces saturated hydraulic conductivity

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17 • A soil rheology and animal movement models estimate changes in these properties

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19 • The model predicts changes in macroporosity and saturated hydraulic conductivity

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21 • Compaction-induced changes in these soil properties depend on the soil water  
22 content

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24 • Predicted temporal changes in soil properties are validated with literature data

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31 **KEYWORDS**

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33 soil compaction - animal treading - soil structure - hydraulic conductivity - bulk density -

34 macroporosity

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## 39 **Abstract**

40 Increased soil compaction resulting from livestock treading and use of heavy machinery is a  
41 major environmental hazard often linked to degradation of the soil ecosystem and  
42 economic services. However, there is a weak quantitative understanding of the spatial and  
43 temporal extent of soil compaction and how it modifies soil properties and associated  
44 functions. To address this challenge, we developed a framework for systematic modelling  
45 soil compaction caused by grazing animals. We considered random movement of livestock  
46 in a confined field to describe the spatial variation in the soil that is discretized in square  
47 cells with given properties. We then used a rheology model based on Bingham's law to infer  
48 compaction-induced changes in soil bulk density and porosity. An associated reduction of  
49 saturated hydraulic conductivity is obtained from soil porosity predictions by empirically  
50 accounting for macroporosity reduction using a dual-porosity permeability model. This  
51 model is coupled with an empirical model of soil structure recovery to account for biological  
52 activity (i.e., earthworms and roots). The modelling framework effectively captures primary  
53 effects of soil compaction on key soil properties despite lack of explicit consideration of  
54 complex effects of compaction such as redistribution of pore sizes and changes in pore  
55 connectivity. We tested the model using bulk density, macroporosity and saturated  
56 hydraulic conductivity data from a grazing study at the Tussock Creek experimental platform  
57 in New Zealand. Data were successfully reproduced by the model. Compaction and recovery  
58 trends can be interpreted in terms of model properties associated with management, soil  
59 texture and environmental conditions. If data are available for calibration of such  
60 properties, the model could be used in agro-ecosystem modelling applications to assess the

61 environmental impacts (such as surface runoff and green-house gas emissions) of livestock-

62 grazing systems and inform management strategies for ameliorating these.

63

## 64 **1 Introduction**

65

66 Soil compaction is a major environmental hazard. It is produced by stresses on or within the  
67 soil due to agricultural operations, usage of military, forestry and construction vehicles and  
68 animal treading under vulnerable soil conditions (Hamza and Anderson, 2005). Soil  
69 compaction adversely impacts soil mechanical and hydraulic properties (Keller et al., 2017,  
70 Rabot et al., 2018) and it is often linked with soil erosion (Nawaz et al., 2013), increased  
71 greenhouse gas (GHG) emissions (Oertel et al., 2016) and reduction of crop and pasture  
72 productivity (Håkansson and Reeder, 1994, Houlbrooke et al., 2009). These responses can  
73 have a strong effect on soil ecosystem services (Conrad, 1996, Aitkenhead et al., 2016, Foster  
74 et al., 2017) and economy (Graves et al., 2015).

75

76 Quantifying large scale environmental effects of soil compaction remains challenging due to  
77 fragmentary data on how soil processes and properties are affected by soil compaction across  
78 temporal and spatial scales. Early estimates by Oldeman (1992) suggested that 68 Mha of  
79 arable lands were compacted globally and recent estimates indicate that about 25-40% of all  
80 arable land is compacted in the United Kingdom (Graves et al., 2015), Denmark (Schjønning  
81 et al., 2015) and the Netherlands (Brus and Van Den Akker, 2018). Similarly, estimations by  
82 Steinfeld et al. (2006) suggest that 20% of the world's grasslands are degraded, mostly  
83 through overgrazing, compaction, and erosion caused by livestock treading.

84

85 Soil properties respond to soil compaction differently, presenting different relative post-  
86 compaction changes and recovery rates (Keller et al., 2021). Transport properties are often

87 strongly reduced by compaction, diminishing the capacity of the soil to provide water and  
88 oxygen to plant roots due to a reduction and disruption of the soil pore system (primarily  
89 macropores), further leading to changes in soil evaporation (Assouline et al.,2014; Romero-  
90 Ruiz et al., 2022; Yi et al., 2022). In addition, the impact of compaction on soil mechanical  
91 properties limits the ability of plant roots to reach larger soil volumes and extract water  
92 (Bengough et al., 2011). All these interacting processes ultimately determine how water is  
93 partitioned through processes such as drainage, evaporation, root water uptake and surface  
94 runoff (Oades, 1993, Gregory et al., 2009, Or et al., 2021). Such limitations on water flow and  
95 gas diffusion can lead to anaerobic conditions favoured by the microorganisms responsible  
96 for denitrification (reduction of nitrate to produce nitric oxide, NO; nitrous oxide, N<sub>2</sub>O; and  
97 nitrogen gas, N<sub>2</sub>) in soil (Khalil et al., 2005). Our limited ability to qualitatively describe these  
98 processes is one barrier that constrains our understanding of environmental processes (e.g.,  
99 water flow, carbon cycling, GHG emissions) from agriculture, especially in (but not limited to)  
100 livestock-grazing systems (Bilotta et al., 2007). Developing strategies for livestock-grassland  
101 management to ameliorate the animal's environmental impact will then largely rely on  
102 improving our qualitative and quantitative understanding of the underlying mechanisms  
103 affecting soil functioning at relevant spatial and temporal scales under real-world conditions.  
104 Integrative mechanistic modelling considering animal movement under different grazing  
105 strategies and how they modify key soil properties is currently lacking and may offer a crucial  
106 first step towards developing a more complete understanding of the environmental and  
107 economic consequences of soil degradation under grassland-livestock systems (Vereecken et  
108 al., 2016, Baveye et al., 2021).

109

110 The aim of this work is to develop a mechanistic model for predicting spatio-temporal changes  
111 of soil bulk density, porosity, macroporosity, and saturated hydraulic conductivity explicitly  
112 considering soil compaction due to animal grazing. Rates of natural soil recovery are also  
113 considered. To achieve this, we (1) developed a model of animal movement for a given soil  
114 area, (2) used a soil rheology model to calculate soil viscous deformation in response to  
115 animal treading, and (3) used the results from the rheology model along with commonly used  
116 soil physics models to calculate changes in soil properties in response to compaction. The  
117 modelling tool developed here was used to reproduce data from the literature showing  
118 changes in soil properties due to animal treading.

119

## 120 **2 Soil compaction model**

### 121 **2.1 Soil structure: Conceptual model and definitions**

122

123 In order to have a consistent representation of the various soil properties predicted by our  
124 soil compaction model (Figure 1) and to facilitate their computation, we first provide a  
125 definition of soil structure. This definition is used exclusively for this work, and may differ  
126 from other definitions found in the literature (Dexter, 1988). We consider the soil to be  
127 formed by two domains: (1) a soil matrix that is represented as an assembly of soil aggregates  
128 that encompass intra-aggregate porosity and (2) a soil macroporous region that can be  
129 conceptualized as inter-aggregate porosity (see Figures 2a, 2b and 2c). Similar  
130 conceptualizations have been successfully used to compute electrical (Day-Lewis et al., 2017,  
131 Romero-Ruiz et al., 2022), seismic (Dvorkin et al., 1999, Romero-Ruiz et al., 2021) and  
132 dielectric (Blonquist Jr et al., 2006) properties of structured porous media. Here, the total

133 porosity ( $\phi_T$ ) is expressed as a function of the soil matrix porosity ( $\phi_{sm}$ , pore radius  $r_p < 30 \mu m$ )  
134 and the macroporous region ( $\phi_{mac} = 1$ ,  $r_p > 30 \mu m$ ) together with the volumetric fraction  
135 occupied by the soil macropores ( $w_{mac}$ ) and the soil matrix ( $1 - w_{mac}$ ):

136

$$137 \quad \phi_T = (1 - w_{mac}) \phi_{sm} + w_{mac} \phi_{mac}.$$

138 *1*

139

## 140 **2.2 Bingham model of soil rheology applied to animal treading**

141

142 For simplicity, the time-dependent signature stress applied on the soil by a walking animal  
143 (Scholefield and Hall, 1986) is represented here by a half-sine cycle. This is similar to the more  
144 widely used representation of the transient stress produced by the passage of vehicles (Or  
145 and Ghezzehei, 2002). Moreover, this simple representation allows modelling soil  
146 deformation due to animal treading using the Bingham rheology model (Ghezzehei and Or,  
147 2001). The application of a transient load by a walking animal will then result in an elastic  
148 (temporary) and a viscous (permanent) deformation of the soil frame producing an axial strain  
149  $\epsilon = \epsilon_e + \epsilon_v$  (see Figure 2, Ghezzehei and Or, 2003), where  $\epsilon_e$  and  $\epsilon_v$  are the elastic and viscous  
150 strains, respectively. The lasting effect of one treading event produces an irreversible  
151 deformation,  $\epsilon_v$ , which can be modelled using information about the initial (prior to  
152 compaction) strain  $\epsilon_0$ , the axial load and duration of stress application and the soil rheological  
153 properties as:

154

155 
$$\epsilon_v(t) = [\epsilon_B^2 S_{sm}(t)^{N_v} (1 - \cos(\omega t)) + \epsilon_0^2]^{\frac{1}{2}},$$

156 2

157 where  $t$  is the time,  $\omega$  is the angular frequency,  $\epsilon_B$  comprises information of the soil  
158 rheological properties and the characteristics of the compaction event (e.g., weight of animal  
159 and walking speed),  $S_{sm} = \theta_{sm}/\phi_{sm}$  is the water saturation in the soil matrix, where  $\theta_{sm}$  is  
160 the water content in the soil matrix and  $N_v$  is an empirical exponent. Note that deformation  
161 is assumed to occur in aggregate contacts forming the soil matrix; equation 2 thus takes the  
162 properties and states of the soil matrix.

163

164 The extent of soil compaction damage produced by animal treading is strongly dependent on  
165 soil water content. As described by Drewry et al., (2008), the main effects of water content-  
166 dependent soil responses to treading are: (i) little soil compaction damage and elastic  
167 recovery for treading events when soil water contents are low, (ii) viscous deformation and  
168 greater soil compaction damage for higher soil water contents (e.g., in the vicinity of field  
169 capacity) and (iii) high risk of pugging for water contents near full water saturation. The effects  
170 (i) and (ii) are accounted for in Equation 2, where the product  $\epsilon_B^2 S_{sm}(t)^{N_v}$  is a function of the  
171 soil complex viscosity (Vyalov, 1986). For simplicity, we propose using the time- and water  
172 content-dependent term  $S_{sm}(t)^{N_v} = (\theta_{sm}(t)/\phi_{sm})^{N_v}$  for modelling the effect of water  
173 saturation on the complex viscosity and resulting viscous strain. This function is similar to  
174 other models of soil properties, for example, accounting for effects of water saturation in soil  
175 electrical resistivity (Archie, 1980) or the effective stress parameter (Nuth and Laloui, 2008)  
176 for calculating suction stresses. The viscous strain  $\epsilon_v$  can thus be used to model soil properties  
177 by means of geometrical approximations as shown in the following sections. Similarly,  $\epsilon_v$  for



178 transient loads (i.e., a walking animal or a passing vehicle), can be derived from an expression  
179 for viscous strain for static loads. However, for simplicity, in this study we only focus on  
180 transient loads (equation 2).

181

## 182 **2.3 Spatio-temporal evolution of compaction patterns**

183

184 We incorporate spatial and temporal dynamics of compaction patterns by simulating animal  
185 movement within a defined area that is further discretized in cells. For simplicity, a random  
186 walk algorithm is used to simulate animal movement within the delimited area by setting the  
187 stock density ( $D$ ) and the number of steps per day per animal ( $N_{steps}$ ). We then count the  
188 number of steps per day per cell, simulating full spatial dynamics of animal movement in a  
189 field. To translate this information to soil deformation, Equation 2 is used recursively making  
190 a daily update of the strain associated with each cell. This process can be further constrained  
191 using GPS data from animals.

192

## 193 **2.4 Bulk density, total porosity and microporosity**

194

195 Having the strain as a function of time and assuming deformation in all axes, as proposed by  
196 Ghezzehei and Or (2001), we can calculate the bulk density of compacted soils ( $\rho_c$ ) as a  
197 function of the compacted strain ( $\epsilon_c$ ), the initial strain ( $\epsilon_0$ ), and the initial bulk density ( $\rho_0$ ) as:

198

199 
$$\rho_c = \rho_0 \left( \frac{1 - \epsilon_0}{1 - \epsilon_c} \right)^3.$$

200 3

201

202 Similarly, the total porosity ( $\phi_{T_c}$ ) can be calculated as:

203

204 
$$\phi_{T_c} = 1 - \frac{\rho_c}{\rho_p},$$

205 4

206

207 where  $\rho_p$  is the bulk density of soil particles ( $\sim 2.7 \text{ g/cm}^3$ ). It has been extensively shown that  
208 soil compaction impacts primarily soil macroporosity while the microporous domain remains  
209 largely unaffected (see Or and Ghezzehei, 2002, Berli et al., 2008). For this reason, we  
210 attribute changes in total porosity due to compaction completely. Reductions of  
211 macroporosity after a treading event are calculated as (for  $\Delta\phi_T > 0$ ):

212

213 
$$\Delta w_{mac} = \Delta\phi_T,$$

214 
$$w_{mac_c} = w_{mac_0} - \Delta\phi_T,$$

215 5

216 where  $w_{mac}$ ,  $w_{mac_c}$ , and  $w_{mac_0}$  are macroporosity, macroporosity after compaction and initial  
217 macroporosity, respectively.

218

219

## 220 **2.5 Water retention and hydraulic properties**

221

222 We account for soil structure and macropore water flow using the water retention and  
 223 hydraulic model proposed by Durner (1994). This model is consistent with our conceptual  
 224 description of soil structure dividing the soil porosity into two overlapping domains  
 225 representing (1) the pore system in the soil matrix and (2) the macropore system. In this  
 226 parametrization, the water retention and the hydraulic conductivity function of the soil are  
 227 expressed as a combination of the functions ascribed to the two considered domains:

228

$$229 \quad S_e = \frac{\theta - \theta_r}{\phi_T - \theta_r} = w_{sm} [1 + (\alpha_{sm} h)^{n_{sm}}]^{1 - \frac{1}{n_{sm}}} + w_{mac} [1 + (\alpha_{mac} h)^{n_{mac}}]^{1 - \frac{1}{n_{mac}}},$$

230 6

231 and

232

$$233 \quad K_{soil} = r_k K_{sm} \frac{(w_{sm} S_{e_{sm}} + w_{mac} S_{e_{mac}})^{0.5}}{(w_{sm} \alpha_{sm} + w_{mac} \alpha_{mac})^2} \left( w_{sm} \alpha_{sm} \left[ 1 - \left( 1 - S_{e_{sm}}^{\frac{n_{sm}}{n_{sm}-1}} \right)^{1 - \frac{1}{n_{sm}}} \right] \right. \\ 234 \quad \left. + w_{mac} \alpha_{mac} \left[ 1 - \left( 1 - S_{e_{mac}}^{\frac{n_{mac}}{n_{mac}-1}} \right)^{1 - \frac{1}{n_{mac}}} \right] \right)^2,$$

235 7

236

237 where  $h$  is the pressure head,  $S_e$  is the effective saturation of the soil,  $\theta_r$  is the residual water  
 238 content,  $n_i$  is the van Genuchten exponent (which is related to soil texture) and  $\alpha_i$  is related  
 239 to the inverse of the air-entry pressure. The saturated hydraulic conductivity of the soil  $K_{sat} =$   
 240  $r_k K_{sm}$  is defined as the product of the saturated hydraulic conductivity of the soil matrix  $K_{sm}$   
 241 and the ratio  $r_k = K_{sat}/K_{sm}$  which is a function of the soil macroporosity. The indices  $sm$  and

242 *mac* represent the soil matrix and the macroporous region, respectively. Equation 7 is used  
243 to calculate the hydraulic conductivity as a function of water content (or pressure head). Such  
244 parametrization can be approximated by a linear combination of the hydraulic conductivity  
245 functions of the two domains as (see Fatichi et al., 2020, Romero-Ruiz et al., 2022):

246

$$247 \quad K_{soil}(h, z) = (1 - w_{mac_c}(z))K_{matrix}(h, z) + w_{mac_c}(z)K_{macropore}(h, z),$$

248 8

249

250 where  $z$  is the vertical spatial coordinate. This allows representing the  $K_{sat}$  as a function of  
251 the macroporosity  $w_{mac}$ . Thus, a reduction of saturated hydraulic conductivity can be  
252 calculated using equation 8 and updating the compaction induced change in  $w_{mac}$  resulting  
253 from equation 5 as:

254

255

$$256 \quad K_{sat_c}(z) = (1 - w_{mac_c}(z))K_{matrix_{sat}}(z) + w_{mac_c}(z)K_{macropore_{sat}}(z).$$

257

258 9

259

260 Equation 9 is simplified and implies that changes in unsaturated flow (occurring in the soil  
261 matrix) is the same for compacted and non-compacted soils (Fatichi et al., 2020) which may  
262 not be always the case (Berli et al., 2008). Where macroporosity is absent (e.g., in non-  
263 structured soils or where compaction has removed macroporosity), the saturated hydraulic

264 conductivity can be calculated using the expression proposed by Or et al. (2000) based on the  
265 Kozeny-Carman relationship:

266

$$267 \quad K_{sat_c} = K_{sat_0} \frac{\phi_{T_c}(1 - \phi_{T_0})^2}{\phi_{T_0}(1 - \phi_{T_c})^2}$$

268 10

269

270 where the  $K_{sat_0}$  is the initial saturated hydraulic conductivity (i.e., non-compacted). If  
271 necessary, vertical changes of saturated hydraulic conductivity of the soil  $K_{sat}$  can be  
272 approximated with a function that decays exponentially with soil depth, similarly to decay of  
273 soil organic matter and macroporosity with depth (Araya and Ghezzehei, 2019, Kramer and  
274 Gleixner, 2008, Hobley and Wilson, 2016).

275

## 276 2.6 Soil structure recovery

277

278 It is expected that soil macro and micro-porosities change dynamically as a function of time  
279 in response to biological activity (earthworm movement and root decay), seasonal climatic  
280 cycles and management. Meurer et al. (2020) showed that macroporosity ( $w_{mac}$ ) recovers at  
281 an exponential rate asymptotically to a maximum macroporosity ( $w_{mac_0}$ ). Similarly, we  
282 empirically account for soil structure recovery in the viscous strain as:

283

$$284 \quad \epsilon_v = \epsilon_0 - (\epsilon_0 - \epsilon_i)e^{-d_r/\lambda_{tr}},$$

285 11

286

287 where  $\epsilon_i$  is the soil strain, representing the strain resulting after the grazing season,  $d_r$  is the  
288 number of days after the last grazing season, and  $\lambda_{tr}$  determines the recovery rate. In this  
289 work, we did not consider recovery by wetting and drying cycles. However, the model by  
290 Stewart et al. (2016) could be used to predict changes in soil porosity resulting from swelling  
291 events. The changes in pore-spaces described in this section generate soil structure recovery  
292 and produce concurrent changes in soil bulk density and saturated hydraulic conductivity  
293 which are updated using the models described in the previous section.

294

295

### 296 **3 Case study: Tussock Creek, New Zealand**

#### 297 **3.1 Soil compaction experiment**

298

299 We make use of data from the Tussock Creek experimental platform (-46.2 N, 168.4 E) in New  
300 Zealand reported by Houlbrooke et al. (2009). The soil (Pukemutu silt loam) has a texture of  
301 32% clay (< 2  $\mu m$ ), 65% silt (2-60  $\mu m$ ), and 3% sand (60-2000  $\mu m$ ). Pasture at the experimental  
302 site was predominantly a mix of ryegrass (*Lolium perenne* L.) and white cover (*Trifolium*  
303 *repens* L.). Soil fertility levels were optimal for pasture production, with pH at 5.9, Olsen P at  
304 40  $\mu g/ml$ , sulphate-S at 6.6  $\mu g/g$  and organic carbon content of 4.5%. This study investigated  
305 the ability of grazing practices to prevent soil degradation by livestock treading. As per  
306 common practice for the region, the site was rotationally grazed (stocking density of 65  
307 animals/ha) on 10 – 12 occasions throughout spring, summer and autumn and remained  
308 ungrazed over winter. Specific treatments were: (1) normal (rotational) grazing of undrained

309 land, (2) normal grazing, (3) normal grazing then restricted to 3-hour grazing periods during  
310 autumn, (4) normal grazing, but restricted to 3 hours grazing when the soil was wet, (5)  
311 strategic grazing to avoid soil pugging damage when conditions were wet, and (6) never  
312 grazed. With the exception of treatment 1, treatment plots were artificially drained by a mole-  
313 pipe drainage system, as is common practice for the naturally poorly drained Pokemutu soil.  
314 Grazing scheduling for treatments 4 and 5 was guided by the use of a cone penetrometer;  
315 further details can be found in Houlbrooke et al. (2009). Treatment responses were observed  
316 using measurements of bulk density, macroporosity and saturated hydraulic conductivity for  
317 the 0-5 cm soil layer at the end of winter and spring in three consecutive years from 2000 to  
318 2002. These sampling times were scheduled to coincide with occasions when soil physical  
319 condition was expected to reflect winter recovery or maximum damage due to cow treading  
320 during spring, respectively. Grazing periods, water contents and temperatures at the Tussock  
321 Creek experimental station are presented in Figure 3.

322

### 323 **3.2 Modelling considerations**

324

325 We aimed to systematically capture and reproduce primary signatures of soil compaction due  
326 to animal treading in key soil properties and how they recover after the grazing season. For  
327 this, we set the model to reproduce the soil compaction experiment by Houlbrooke et al.  
328 (2009). For all treatments, there was a drop in macroporosity during the spring grazing season  
329 followed by a period of significant recovery (returning to pre-grazing conditions in most cases;  
330 see averaged macroporosities in Figure 4). As discussed by the authors, the grazing strategies  
331 that were used to prevent structural damage within the top 10 cm of the soil were not

332 strikingly different to conventional grazing practices (see statistical analysis in Houlbrooke et  
333 al., 2009). For this reason, we compared two basic treatments: (1) grazed vs (2) non-grazed.  
334 Data from the nil grazed treatments were used for non-grazed. Grazed treatment data were  
335 obtained by averaging measurements from all the grazing treatments described in section  
336 3.1. As shown in Figure 4, we used data from the first two grazing seasons (2000 and 2001) to  
337 calibrate key model properties (data used for inverse modelling, data I) and evaluated the  
338 ability of the model to predict data from the third grazing season (2002) (data predicted for  
339 validation, data P). The calibrated properties were:  $\epsilon_B$  containing information about the  
340 compaction event, the initial bulk density  $\rho_0$ , the rate of recovery  $\lambda_{tr}$ , the porosity of the soil  
341 matrix  $\phi_{sm}$ , the hydraulic conductivity of the soil matrix  $K_{sm}$  and the exponent  $N_v$ .

342

343 For simplicity, we assumed that compaction occurred during spring and recovery occurred in  
344 all other seasons (see also Drewry et al., 2004). To simulate the treading events, we did not  
345 report the spatial variation of soil properties but instead focused on the median value for  
346 each treatment and its temporal variations utilizing a daily time step in the model. We  
347 simulated random animal movement in a 100 x 100 m square field using the characteristics  
348 of the grazing experiments (about 12 grazing days per season using c. 65 cows per hectare on  
349 each occasion), considering information about the grazing dates (Figure 3a) and assuming  
350 5000 steps per animal per day. We then selected the median of the numbers of steps counted  
351 per cell (see Figure 5) to be representative of the treading event. This resulted in 97 steps per  
352 grazing day. For each of the grazing days, Equation 2 is then used recursively 97 times to  
353 obtain the associated compaction-induced viscous strain. We considered that soil structure  
354 recovery is dominated by bioturbation. The recovery of soil strain was simulated outside  
355 spring using Equation 11. Bulk density, macroporosity and saturated hydraulic conductivity



356 were then updated daily using equations 3-5 and 7-8 reflecting changes induced by  
 357 compaction and recovery agents. We used the three data sets of Houlbrooke et al. (2009)  
 358 (bulk densities, macroporosities and saturated hydraulic conductivities) for inverting the key  
 359 model properties representing compaction and recovery. Such model properties ( $\mathbf{P} =$   
 360  $[\epsilon_B, \lambda_{tr}, \rho_0, \phi_{sm}, K_{sm}, N^v]$ ) are inferred using the Markov-chain Monte Carlo (MCMC) method  
 361 of Laloy and Vrugt (2012) (the so-called differential evolution adaptive Metropolis,  
 362 DREAM(zs)). The posterior probability density functions of the model properties were inferred  
 363 using the following likelihood function:

364

$$365 \quad L(\mathbf{P}|\mathbf{d}) = (\sqrt{2\pi\sigma_d})^{-N_d} \exp \left[ -\frac{1}{2} \sum_{d_i=1}^{N_d} \left( \frac{F_i(\mathbf{P}) - d_i}{\sigma_{d_i}} \right)^2 \right],$$

366 11

367

368 where  $F(\mathbf{P})$  and  $\mathbf{d}$  are the simulated and measured data (simultaneously containing bulk  
 369 densities, macroporosities and saturated hydraulic conductivities), respectively,  $\sigma_{d_i}$  is the  
 370 data error of the i-th datum (considered here as 5% of each datum) and  $N_d$  is the number of  
 371 data points. We used uniform probability distributions as priors of all inverted properties.

372

## 373 4 Results

374

375 After burn-in for 10000 iterations, the mean values inferred from the posterior distributions  
 376 were  $\epsilon_B = 0.31\%$ ,  $\lambda_{tr} = 52.17$  days,  $\rho_0 = 0.91 \text{ g/cm}^3$ ,  $K_{sm} = 0.04 \text{ cm/h}$  and  $N_v = 3.44$ . The model

377 succeeded in reproducing the data used for inversion (first two grazing seasons) resulting in  
378 a weighted root-mean square error (WRMSE) of 1.25. A reasonable fit was obtained for data  
379 not included in the inversion (third grazing season) with a WRMSE of 2.8. For the grazed  
380 treatment the bulk density increased as a result of grazing, but then recovered to a level  
381 similar to pre-grazing (Figure 6a). The bulk density of the non-grazed treatment was variable:  
382 increasing on occasions during the spring and decreasing during the summer, fall and winter  
383 seasons. The bulk density of the non-grazed treatment was less for all measurement  
384 occasions after the first grazing season. The final bulk density of the grazed treatments was  
385 14% higher than in the non-grazed treatment. The post-spring grazing bulk density was 27%  
386 higher than the pre-grazing bulk density for the last grazing season.

387

388 We present (Figure 6a) the modelled bulk densities as a function of time resulting from the  
389 MCMC inversion considering chains after 10000 iterations. The modelled bulk densities  
390 reflect changes due to compaction and recovery and reproduced the patterns of the observed  
391 bulk densities from the first two grazing seasons reasonably well. The bulk densities  
392 corresponding to the third grazing season, not considered in the inverted data vector, were  
393 slightly overestimated by the model. This can be partly explained by the considerably lower  
394 values of bulk density measured in 2002 compared to values from 2000 and 2001. Similar to  
395 the bulk density measurements, the saturated hydraulic conductivity decreased in response  
396 to compaction during spring grazing periods and increased during the recovery periods  
397 (Figures 6c). We observed typically higher values in the non-grazed treatment. However, the  
398 variations in saturated hydraulic conductivities were substantially larger when comparing  
399 grazed vs non-grazed treatments (78% drop at the last measurement occasion) and pre- vs  
400 post-grazing (95% drop at the last occasion). Despite such large variations, the model

401 provided a reasonable description of compaction and recovery cycles and captured measured  
402 values quantitatively. By considering a dual-domain conceptual model of soils that explicitly  
403 takes account of the effects of macropores on soil hydraulic properties, it is possible to  
404 simultaneously reproduce large changes in hydraulic properties alongside relatively small  
405 changes in bulk density (see Figure 7a).

406

407 Saturated hydraulic conductivity (Figure 6c) was strongly dependent on soil macroporosity  
408 (see Figure 7b) and thus followed similar trends (refer to Figures 6b and 6c). The final  
409 macroporosity was 45% less for the grazed than for the non-grazed treatments. As seen for  
410 the bulk density and macroporosity data (Figures 6a and 6b) changes induced during the  
411 spring 2001 were less marked than those induced in the springs of 2000 and 2002. By  
412 considering the effects of water saturation on the potential damage to soil compaction  
413 (Equation 2), this effect was reasonably well reproduced by the model that predicts a smaller  
414 impact on soil properties for the drier spring of 2001 compared to the wetter springs of 2000  
415 and 2002. Overall, the macroporosity data and tendencies responding to compaction and  
416 recovery are reasonably well reproduced by the model for both data I and data P.

417

## 418 **5 Discussion**

419 The modelling framework presented in this work predicts compaction-induced changes in  
420 soil properties due to animal treading. We intentionally only sought to represent primary  
421 features of soil compaction in order to provide a model that is relatively easy to implement  
422 and helps assessing impacts of management on soil properties and functions. As  
423 demonstrated in the Results section, the model does a reasonable job of reproducing not

424 only data from grazing seasons in 2000 and 2001 (i.e., those used for property calibration),  
425 but also for data from grazing in 2002. However, it is important to stress that changes in soil  
426 properties and functions due to compaction are very complex and some limitations in the  
427 model remain as described below.

428

429 The model uses a very simple approach to calculate bulk densities, macroporosities and  
430 saturated hydraulic conductivities (equations 3, 5, 7 and 9). Despite this simplicity, the  
431 macroporosity and saturated hydraulic conductivity data were particularly well reproduced.  
432 This is partly explained by the ability of the model to represent the dependency of saturated  
433 hydraulic conductivity on macroporosity (Figure 7), employing a linear superposition of the  
434 two porosity domains using Equations 7 and 10. Such larger variations are difficult to capture  
435 when using more common approaches that obviate macroporosity effects (e.g., Equation 11).  
436 The variability in bulk density in response to compaction is much less, but is consistent with  
437 values observed in the literature of about 15% decrease (Keller et al., 2017). The model was  
438 able to reproduce variations in bulk density successfully, but bulk densities from the non-  
439 grazed treatment did not show a clear baseline (i.e., a constant value as a function of time)  
440 characteristic of non-grazed soils. In contrast, we did observe a less variable baseline for  
441 macroporosity and saturated hydraulic conductivity values in the non-grazed treatment.  
442 These variations in baselines may be attributed to the natural spatial variability of soil  
443 properties in grasslands and, for simplicity, possible effects related to them (e.g., swelling-  
444 induced compaction) were not considered in the model. Having a highly variable baseline of  
445 bulk density and a less variable baseline for macroporosity is to be expected if we  
446 acknowledge that bulk soil properties such as bulk density and total porosity only offer an  
447 incomplete representation of soil structure (Romero-Ruiz et al., 2018, Rabot et al., 2018, Or

448 et al., 2021). As shown in Figure 7, this means that saturated hydraulic conductivity, which is  
449 a property that is more representative of soil structure, can vary substantially for the same  
450 value of porosity (or bulk density) in response to redistributions of pore sizes and  
451 connectivities, such as those resulting from compaction and shear deformation (Whalley et  
452 al., 2012) which were not explicitly considered in this study.

453

454 The model considers porosity ( $\phi_{sm}$ ) and hydraulic conductivity of the soil matrix ( $K_{sm}$ ) to be  
455 constant as function of time. This assumption was based on evidence suggesting that soil  
456 compaction primarily impacts inter-aggregate pore spaces (macropores) and aggregate  
457 contacts (Berli et al., 2008; Eggers et al., 2006; Ghezzehei & Or, 2001). However, other  
458 studies have shown that soil compaction may increase both the porosity of the soil  
459 matrix and the unsaturated hydraulic conductivity due to redistributions of pore spaces  
460 and their connectivity (Richard et al., 2001). If necessary, such changes can be  
461 incorporated in the water saturation and hydraulic conductivity functions (equations 6  
462 and 7). Similarly, we did not consider changes in pore connectivity of the macroporous  
463 region which has been demonstrated to have a large influence on soil hydraulic  
464 properties (e.g., Fu et al., 2020; Müller et al., 2018). This may help explain some of the  
465 mismatch between measured and modelled hydraulic conductivities and  
466 macroporosities presented in Figure 7b.

467

468 We modelled three grazing periods considering the dates of grazing (Figure 3a), the stock  
469 density (65 animals per hectare) and the water content measured on the grazing dates (Figure  
470 3a). The strain  $\epsilon_B$  (which helps determining the susceptibility of the soil to compaction) was  
471 set constant in space and time in the model, reflecting that all soil compaction events (i.e.,

472 animal trampling) occurred under the same soil texture and animal weight. We proposed to  
473 model the susceptibility to compaction as a function of the water content by using the term  
474  $S^{N_v}$  in Equation 2. This function has the ability of assigning a dependency of the soil  
475 compaction damage with the corresponding soil wetness conditions during the compaction  
476 event. It is difficult and outside the scope of this work to properly determine the parameter  
477  $\epsilon_B$  and function  $S^{N_v}$  as a function of time and for different soil textures. They mainly depend on:  
478 Poisson's ratio and complex viscosity of the soil, the hoof pressure and velocity of the walking  
479 animals and the size of aggregates conceptualized as forming the soil (Ghezzehei and Or,  
480 2001). For practical reasons, we opted for calibrating only  $\epsilon_B$  and  $N_v$ . Despite lacking a  
481 complete explicit consideration of the various soil physical properties, environmental  
482 conditions and characteristics of the compacting stresses, the model remains valid and could  
483 be further used for comparing different grazing strategies (e.g., involving livestock animals  
484 with different weights such as sheep). Moreover, the model simultaneously reproduced  
485 compaction-induced variations of some soil physical properties. The model predicted changes  
486 in soil properties to be larger during the springs of 2000 and 2002 than changes in properties  
487 after the drier spring of 2001 (see Figures 6b and 6c). The predicted compaction-induced  
488 reductions in macroporosity during the spring were 65%, 46%, and 80% for 2000, 2001, and  
489 2002, respectively; corresponding measured reductions were 53%, 46%, and 80%,  
490 respectively. Similarly, the model predicted saturated hydraulic conductivity reductions of  
491 90%, 76%, and 96% for 2000, 2001, and 2002, respectively; which were consistent with their  
492 corresponding measured reductions (compared with the non-grazed control treatment) of  
493 93%, 62%, and 95%. The data confirmed that soil water content largely controls the  
494 susceptibility of the soil to compaction (see discussions by Drewry et al., 2008) and the results  
495 suggested that the representation of water content effects in the model is sufficient to

496 capture such influence. Further field and laboratory research may be performed to explicitly  
497 determine  $\epsilon_B$  and the function  $S^{N_v}$ . This includes applying the modelling framework presented  
498 here to other data-sets, for soil with different textures, different grazing histories and under  
499 different climate.

500

501 Similar to the compaction process, we opted for using a simplified representation of soil  
502 recovery (Equation 11). This model simulated the evolution of soil pore-spaces only in  
503 response to bioturbation by decaying roots and earthworms (Meurer et al.,2020). Effects of  
504 climatic cycles such as wetting-drying and freezing-thawing have been suggested as important  
505 factors playing a role in soil structure evolution and recovery (Kuan et al., 2007, Gregory et  
506 al., 2007). We did not observe major wetting-drying events nor indications of soil freezing in  
507 the water content and temperature data presented in Figure 3. For this reason, these  
508 processes were not considered. The recovery property  $\lambda_{tr}$  was constant with time and the  
509 same for both recovery periods. It is therefore expected that some data might be mis-  
510 predicted. The model predicts a rapid recovery after the grazing periods which is consistent  
511 with the compaction and recovery cycles observed by Drewry et al. (2004). This was difficult  
512 to validate, however, due to the small number of data points measured as a function of time.  
513 Future campaigns dedicated to the study of soil structure recovery may benefit from having  
514 more frequent monitoring of soil properties shortly after compaction.

515

516 We inferred a mean value for  $\lambda_{tr}$  of approximately 52 days, indicating that the soil properties  
517 recover about one third of the relative change during this period. Regardless of the  
518 mechanisms responsible for soil recovery, data presented by Houlbrooke et al. (2009) and  
519 modelled in this work presented an atypically rapid recovery rate for the 0-10 cm soil depth.

520 Soil compaction is often regarded as a process involving very slow recovery rates, yet there is  
521 still some discrepancy in the recovery rates that are site-specific and may dramatically vary  
522 ranging from months to decades depending on soil texture, soil cover, soil depth,  
523 management history, and local climate conditions (Berisso et al., 2012; Schjonning et al.,  
524 2013; Keller et al., 2021).

525

526 Despite offering a relatively broad description of the processes involved in soil structure  
527 dynamics, several simplifications were made in the model. The model does not consider  
528 variations of soil properties with soil depth. This is a reasonable choice for modelling  
529 compaction by animal treading, that mainly affects soil properties of the topsoil (Leitinger et  
530 al., 2010). However, if modelling soil compaction by the passage of heavy agricultural  
531 machinery, stress propagation in the soil profile may be considered to fully capture variations  
532 of soil properties (Keller et al., 2013, Ghezzehei and Or, 2003). Similarly, soil structure  
533 recovery is modelled by only using an exponential function asymptotically approaching a  
534 limiting value of a given property (Meurer et al., 2020). Future modelling work may deal with  
535 assessing recovery as a function of depth by, for example, proposing a depth-dependent  
536 function for  $\lambda_{tr}$ . In addition, we did not consider shear deformation which may be important  
537 when compacting stresses occur under very wet conditions (Whalley et al., 2012).

538

539 The model presented in this work describes the impact of compaction by animal treading on  
540 soil properties that in turn affect soil-water and -nutrient flows. The dynamics of these  
541 processes are commonly incorporated into agroecosystems models (Coleman et al., 2017; Wu  
542 et al., 2007; Dondini et al., 2017). The relative simplicity of our model means that, provided  
543 that properties can be measured or calibrated ( $\epsilon_B$  and  $N_v$ ), it can be readily incorporated into



544 such modelling systems, allowing them to then describe the impact of livestock management  
545 (i.e., stocking rate and length of grazing) on processes involving soil water dynamics, such  
546 infiltration, water flow, evaporation, drainage (Romero-Ruiz et al., 2022) and their  
547 consequences for the environment (e.g., in GHG emissions) and production. The model may  
548 therefore be valuable for informing management strategies for the mitigation of nutrient  
549 losses and emissions.

550

551

552

## 553 **6 Conclusions**

554

555 By considering a physically based model of soil deformation due to compaction, the modelling  
556 framework presented here can systematically incorporate important elements related to soil  
557 management practices in grasslands for evaluation of their impact on soil properties. The  
558 model captures the main effects of soil compaction on key soil properties, it is simple and it  
559 is relatively easy to implement. It does not explicitly take into account some of the more  
560 complex effects that soil compaction has on the soil pore system and hydraulic functions, such  
561 as changes to pore continuity. We tested the model using data from a grazing experiment at  
562 the Tussock Creek experimental platform in New Zealand. Our model successfully reproduced  
563 bulk density, macroporosity and saturated hydraulic conductivity data. By fitting the data with  
564 model properties associated with the soil's susceptibility to compaction and ability to recover,  
565 the model confirmed that drier soils are less prone to compaction and that the overall damage  
566 is less in drier years. In addition, as suggested by the seasonally collected data, the model

567 predicted a rapid recovery after the grazing seasons. This indicates that future campaigns  
568 focusing on monitoring recovery should consider high frequency monitoring for periods  
569 shortly after compaction events. The model presented here is limited by our ability to  
570 measure or calibrate its parameters, yet, if this is achieved, it offers a tool for qualitative and  
571 quantitative assessment of different grazing management strategies by predicting their  
572 impact on key soil properties. The model improves our understanding of the impact of  
573 management factors on soil states and processes and thus may have utility for predicting the  
574 wider environmental impacts of soil compaction, such as water flow, carbon cycling and  
575 greenhouse gas emissions.

576

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584

586 **References**

- 587 Aitkenhead, M., S. D. Allison, S. Assouline, P. Baveye, M. Berli, N. Brüggemann,  
 588 P. Finke, M. Flury, T. Gaiser, G. Govers, T. Ghezzehei, P. Hallett, H. J. H.  
 589 Franssen, J. Heppell, R. Horn, J. A. Huisman, D. Jacques, F. Jonard, S. Kollet,  
 590 F. Lafolie, K. Lamorski, D. Leitner, A. Mcbratney, B. Minasny, C. Montzka,  
 591 W. Nowak, Y. Pachepsky, J. Padarian, N. Romano, K. Roth, Y. Rothfuss, E. C.  
 592 Rowe, A. Schwen, J. ŠimÁrnek, A. Tiktak, J. V. Dam, S. E. A. T. M. V. D. Zee, H. J.  
 593 Vogel, and J. A. Vrugt (2016), Modelling Soil Processes: Review, Key  
 594 Challenges, and New Perspectives Brief History of Soil Modelling, *Vadose Zone*  
 595 *Journal*, 15, doi:10.2136/vzj2015.09.0131.
- 596
- 597 Araya, S. N., and T. A. Ghezzehei (2019), Using machine learning for prediction of  
 598 saturated hydraulic conductivity and its sensitivity to soil structural  
 599 perturbations, *Water Resources Research*, 55(7), 5715–5737,  
 600 doi:<https://doi.org/10.1029/2018WR024357>.
- 601
- 602 Assouline, S., K. Narkis, R. Gherabli, P. Lefort, and M. Prat (2014), Analysis of the  
 603 impact of surface layer properties on evaporation from porous systems using  
 604 column experiments and modified definition of characteristic length, *Water*  
 605 *Resources Research*, 50(5), 3933–3955, doi:10.1002/2013WR014489.
- 606
- 607 Baveye, P. C., E. Dominati, A. Grêt-Regamey, and H.-J. Vogel (2021), Assessment  
 608 and modelling of soil functions or soil-based ecosystem services: Theory and  
 609 applications to practical problems, *Frontiers in Environmental Science*, p. 549.
- 610 Bengough, A. G., B. M. McKenzie, P. D. Hallett, and T. A. Valentine (2011), Root  
 611 elongation, water stress, and mechanical impedance: a review of limiting  
 612 stresses and beneficial root tip traits, *Journal of Experimental Botany*, 62(1), 59–68,  
 613 doi:10.1093/jxb/erq350.
- 614
- 615 Berisso, F. E., et al. "Persistent effects of subsoil compaction on pore size distribution and gas  
 616 transport in a loamy soil." *Soil and Tillage Research* 122 (2012): 42-51.  
 617 <https://doi.org/10.1016/j.still.2012.02.005>
- 618
- 619 Berli, M., A. Carminati, T. A. Ghezzehei, and D. Or (2008), Evolution of  
 620 unsaturated hydraulic conductivity of aggregated soils due to compressive  
 621 forces, *Water Resources Research*, 44(5),  
 622 doi:<https://doi.org/10.1029/2007WR006501>.
- 623
- 624 Bilotta, G., R. Brazier, and P. Haygarth (2007), The impacts of grazing animals on  
 625 the quality of soils, vegetation, and surface waters in intensively managed  
 626 grasslands, pp. 237–280, Academic Press,  
 627 doi:[https://doi.org/10.1016/S0065-2113\(06\)94006-1](https://doi.org/10.1016/S0065-2113(06)94006-1).
- 628
- 629 Blonquist Jr, J., S. B. Jones, I. Lebron, and D. Robinson (2006), Microstructural and  
 630 phase configurational effects determining water content: Dielectric  
 631 relationships of aggregated porous media, *Water Resources Research*, 42(5),

632 doi:10.1029/2005WR004418.

633

634 Brus, D. J., and J. J. Van Den Akker (2018), How serious a problem is subsoil  
635 compaction in the Netherlands? A survey based on probability sampling, *Soil*,  
636 4(1), 37–45, doi:10.5194/soil-4-37-2018.

637

638 Coleman, K., S. E. Muhammed, A. E. Milne, L. C. Todman, A. G. Dailey, M. J.  
639 Glendining, and A. P. Whitmore (2017), The landscape model: A model for  
640 exploring trade-offs between agricultural production and the environment,  
641 *Science of The Total Environment*, 609, 1483–1499,  
642 doi:<https://doi.org/10.1016/j.scitotenv.2017.07.193>.

643

644 Conrad, R. (1996), Soil microorganisms as controllers of atmospheric trace gases  
645 (h<sub>2</sub>, co, ch<sub>4</sub>, ocs, n<sub>2</sub>o, and no)., *Microbiology and Molecular Biology Reviews*, 60(4),  
646 609–640.

647

648 Day-Lewis, F., N. Linde, R. Haggerty, K. Singha, and M. A. Briggs (2017), Pore  
649 network modelling of the electrical signature of solute transport in dual-domain  
650 media, *Geophysical Research Letters*, 44(10), 4908–4916,  
651 doi:10.1002/2017GL073326.

652

653 Dexter, A. (1988), Advances in characterization of soil structure, *Soil and Tillage  
654 Research*, 11(3-4), 199–238, doi:10.1016/0167-1987(88)90002-5.

655

656 Dondini, M., Richards, M., Pogson, M., Jones, E.O., Rowe, R.L., Keith, A.M., McNamara, N.P.,  
657 Smith, J.U. and Smith, P. (2016), Evaluation of the ECOSSE model for simulating soil  
658 organic carbon under *Miscanthus* and short rotation coppice-willow crops in Britain.  
659 *GCB Bioenergy*, 8: 790-804. <https://doi.org/10.1111/gcbb.12286>

660

661 Durner, W. (1994), Hydraulic conductivity estimation for soils with heterogeneous  
662 pore structure, *Water Resources Research*, 30(2), 211–223, doi:10.1029/93WR02676.

663

664 Drewry, J. J., Paton, R. J., & Monaghan, R. M. (2004). Soil compaction and recovery cycle on a  
665 Southland dairy farm: implications for soil monitoring. *Soil Research*, 42(7), 851-856.

666

667 Drewry, J. J., Cameron, K. C., & Buchan, G. D. (2008). Pasture yield and soil physical property  
668 responses to soil compaction from treading and grazing—a review. *Soil Research*, 46(3),  
669 237-256.

670

671 Dvorkin, J., M. Prasad, A. Sakai, and D. Lavoie (1999), Elasticity of marine  
672 sediments: Rock physics modelling, *Geophysical Research Letters*, 26(12),  
673 1781–1784, doi:10.1029/1999GL900332.

674

675 Fatichi, S., D. Or, R. Walko, H. Vereecken, M. H. Young, T. A. Ghezzehei, T. Hengl,  
676 S. Kollet, N. Agam, and R. Avissar (2020), Soil structure is an important  
677 omission in Earth System Models, *Nature Communications*, 11(1), 1–11,  
678 doi:10.1038/s41467-020-14411-z.

679

680 Foster, T., N. Brozovic, and A. P. Butler (2017), Effects of initial aquifer  
681 conditions on economic benefits from groundwater conservation, *Water*  
682 *Resources Research*, 53(1), 744–762, doi:<https://doi.org/10.1002/2016WR019365>.

683

684 Fu, Z., Hu, W., Beare, M., Thomas, S., Carrick, S., Dando, J., Langer, S., Müller, K., Baird, D.  
685 and Lilburne, L., 2021. Land use effects on soil hydraulic properties and the contribution of  
686 soil organic carbon. *Journal of Hydrology*, 602, p.126741.

687 Ghezzehei, T. A., and D. Or (2001), Rheological properties of wet soils and clays  
688 under steady and oscillatory stresses, *Soil Science Society of America Journal*, 65(3),  
689 624–637, doi:10.2136/sssaj2001.653624x.

690

691 Ghezzehei, T. A., and D. Or (2003), Stress-induced volume reduction of isolated  
692 pores in wet soil, *Water Resources Research*, 39(3), doi:10.1029/2001WR001137.

693

694 Graves, A., J. Morris, L. Deeks, R. Rickson, M. Kibblewhite, J. Harris, T. Farewell,  
695 and I. Truckle (2015), The total costs of soil degradation in England and Wales,  
696 *Ecological Economics*, 119, 399–413, doi:10.1016/j.ecolecon.2015.07.026.

697

698 Gregory, A., C. Watts, W. Whalley, H. Kuan, B. Griffiths, P. Hallett, and A. Whitmore (2007),  
699 Physical resilience of soil to field compaction and the  
700 interactions with plant growth and microbial community structure, *European*  
701 *Journal of Soil Science*, 58(6), 1221–1232.

702

703 Gregory, A. S., C. W. Watts, B. S. Griffiths, P. D. Hallett, H. L. Kuan, and A. P.  
704 Whitmore (2009), The effect of long-term soil management on the physical and  
705 biological resilience of a range of arable and grassland soils in England,  
706 *Geoderma*, 153(1-2), 172–185.

707

708 Håkansson, I., and R. C. Reeder (1994), Subsoil compaction by vehicles with high  
709 axle load, persistence and crop response, *Soil and Tillage Research*,  
710 29(2), 277–304, doi:10.1016/0167-1987(94)90065-5.

711

712 Hamza, M. A., and W. K. Anderson (2005), Soil compaction in cropping systems:  
713 A review of the nature, causes and possible solutions, *Soil and Tillage Research*,  
714 82(2), 121–145, doi:10.1016/j.still.2004.08.009.

715

716 Hobley, E. U., and B. Wilson (2016), The depth distribution of organic carbon in  
717 the soils of eastern Australia, *Ecosphere*, 7(1), climate, conditional inference trees,  
718 cropping, datamining, gradient boosting machines, grazing, land use, machine  
719 learning, randomForests, doi:10.1002/ecs2.1214, e01214.

720

721 Houlbrooke, D., J. Drewry, R. Monaghan, R. Paton, L. Smith, and R. Littlejohn  
722 (2009), Grazing strategies to protect soil physical properties and maximise  
723 pasture yield on a southland dairy farm, *New Zealand Journal of Agricultural*  
724 *Research*, 52(3), 323–336.

725

726 Keller, T., M. Carizzoni, F. E. Berisso, M. Stettler, and M. Lamandé (2013),  
727 Measuring the dynamic soil response during repeated wheeling using seismic  
728 methods, *Vadose Zone Journal*, 12(3), 8830, doi:10.2136/vzj2013.01.0033.  
729 Keller, T., T. Colombi, S. Ruiz, M. P. Manalili, J. Rek, V. Stadelmann, H. Wunderli,  
730 D. Breitenstein, R. Reiser, H. Oberholzer, S. Schymanski, A. Romero-Ruiz,  
731 N. Linde, P. Weisskopf, A. Walter, and D. Or (2017), Long-term Soil Structure  
732 Observatory for monitoring post-compaction evolution of soil structure, *Vadose  
733 Zone Journal*, 16(4), doi:10.2136/vzj2016.11.0118.  
734  
735 Keller, T., T. Colombi, S. Ruiz, S. J. Schymanski, P. Weisskopf, J. Koestel,  
736 M. Sommer, V. Stadelmann, D. Breitenstein, N. Kirchgessner, A. Walter, and  
737 D. Or (2021), Soil structure recovery following compaction: Short-term  
738 evolution of soil physical properties in a loamy soil, *Soil Science Society of  
739 America Journal*, 85(4), 1002–1020, doi:https://doi.org/10.1002/saj2.20240.  
740  
741 Khalil, K., P. Renault, and B. Mary (2005), Effects of transient anaerobic conditions  
742 in the presence of acetylene on subsequent aerobic respiration and n<sub>2</sub>o emission  
743 by soil aggregates, *Soil Biology and Biochemistry*, 37(7), 1333–1342.  
744  
745 Kramer, C., and G. Gleixner (2008), Soil organic matter in soil depth profiles:  
746 Distinct carbon preferences of microbial groups during carbon transformation,  
747 *Soil Biology and Biochemistry*, 40(2), 425 – 433, doi:10.1016/j.soilbio.2007.09.016.  
748 Kuan, H., P. Hallett, B. Griffiths, A. Gregory, C. Watts, and A. Whitmore (2007),  
749 The biological and physical stability and resilience of a selection of scottish soils  
750 to stresses, *European Journal of Soil Science*, 58(3), 811–821.  
751  
752 Laloy, E., and J. A. Vrugt (2012), High-dimensional posterior exploration of  
753 hydrologic models using multiple-try DREAM(ZS) and high-performance  
754 computing, *Water Resources Research*, 48(1), W01,526,  
755 doi:10.1029/2011WR010608.  
756  
757 Leitinger, G., E. Tasser, C. Newesely, N. Obojes, and U. Tappeiner (2010), Seasonal  
758 dynamics of surface runoff in mountain grassland ecosystems differing in land  
759 use, *Journal of Hydrology*, 385(1-4), 95–104.  
760  
761 Meurer, K., J. Barron, C. Chenu, E. Coucheney, M. Fielding, P. Hallett, A. M.  
762 Herrmann, T. Keller, J. Koestel, M. Larsbo, E. Lewan, D. Or, D. Parsons,  
763 N. Parvin, A. Taylor, H. Vereecken, and N. Jarvis (2020), A framework for  
764 modelling soil structure dynamics induced by biological activity, *Global Change  
765 Biology*, 26(10), 5382–5403, doi:https://doi.org/10.1111/gcb.15289.  
766  
767 Müller, K., Katuwal, S., Young, I., McLeod, M., Moldrup, P., de Jonge, L. W., & Clothier, B.  
768 (2018). Characterising and linking X-ray CT derived macroporosity parameters to infiltration  
769 in soils with contrasting structures. *Geoderma*, 313, 82-91.  
770 Nawaz, M. F., G. Bourrié, and F. Trolard (2013), Soil compaction impact and  
771 modelling. A review, *Agronomy for Sustainable Development*, 33(2), 291–309,  
772 doi:10.1007/s13593-011-0071-8.

773

774 Oades, J. M. (1993), The role of biology in the formation, stabilization and  
775 degradation of soil structure, *Geoderma*, 56, 377–400,  
776 doi:10.1016/B978-0-444-81490-6.50033-9.

777

778 Oertel, C., J. Matschullat, K. Zurba, F. Zimmermann, and S. Erasmi (2016),  
779 Greenhouse gas emissions from soils - A review, *Chemie der Erde - Geochemistry*,  
780 76(3), 327–352, doi:10.1016/j.chemer.2016.04.002.

781

782 Oldeman, L. R. (1992), Global extent of soil degradation, in *Bi-Annual Report*  
783 1991-1992/ISRIC, pp. 19–36, ISRIC.

784

785 Or, D., and T. A. Ghezzehei (2002), Modelling post-tillage soil structural dynamics:  
786 a review, *Soil and Tillage Research*, 64(1-2), 41–59,  
787 doi:10.1016/S0167-1987(01)00256-2.

788

789 Or, D., F. J. Leij, V. Snyder, and T. a. Ghezzehei (2000), Stochastic model for  
790 posttillage soil pore space evolution, *Water Resources Research*, 36(7), 1641,  
791 doi:10.1029/2000WR900092.

792

793 Or, D., T. Keller, and W. H. Schlesinger (2021), Natural and managed soil structure:  
794 On the fragile scaffolding for soil functioning, *Soil and Tillage Research*, 208,  
795 104,912, doi:https://doi.org/10.1016/j.still.2020.104912.

796

797 Rabot, E., M. Wiesmeier, S. Schlüter, and H. Vogel (2018), Soil structure as an  
798 indicator of soil functions : A review, *Geoderma*, 314, 122–137,  
799 doi:10.1016/j.geoderma.2017.11.009.

800

801 Richard, G., Cousin, I., Sillon, J. F., Bruand, A., & Guérif, J. (2001). Effect of compaction on the  
802 porosity of a silty soil: influence on unsaturated hydraulic properties. *European Journal*  
803 *of Soil Science*, 52(1), 49-58.

804

805 Romero-Ruiz, A. (2021), *Geophysical Methods for Field-Scale Characterization of*  
806 *Soil Structure*, Theses, Université de Lausanne.

807

808 Romero-Ruiz, A., N. Linde, T. Keller, and D. Or (2018), A review of geophysical  
809 methods for soil structure characterization, *Reviews of Geophysics*, 56(4), 672–697,  
810 doi:10.1029/2018RG000611.

811

812 Romero-Ruiz, A., N. Linde, L. Baron, S. G. Solazzi, T. Keller, and D. Or (2021),  
813 Seismic Signatures Reveal Persistence of Soil Compaction, *Vadose Zone Journal*,  
814 p. e20140, doi:https://doi.org/10.1002/vzj2.20140.

815

816 Romero-Ruiz, A., N. Linde, L. Baron, D. Breitenstein, T. Keller, and D. Or (2022),  
817 Lasting effects of soil compaction on soil water regime confirmed by  
818 geoelectrical monitoring, *Water Resources Research*, n/a(n/a), e2021WR030,696,  
819 doi:https://doi.org/10.1029/2021WR030696, e2021WR030696 2021WR030696.

820

821 Schjønning, P., Lamandé, M., Berisso, F. E., Simojoki, A., Alakukku, L., & Andreasen, R. R. (2013).  
822 Gas diffusion, non-Darcy air permeability, and computed tomography images of a clay  
823 subsoil affected by compaction. *Soil Science Society of America Journal*, 77(6), 1977-  
824 1990. <https://doi.org/10.2136/sssaj2013.06.0224>

825

826 Schjønning, P., J. J. H. van den Akker, T. Keller, M. H. Greve, M. Lamandé,  
827 A. Simojoki, M. Stettler, J. Arvidsson, and H. Breuning-Madsen (2015),  
828 Driver-Pressure-State-Impact-Response (DPSIR) analysis and risk assessment  
829 for soil compaction—A European perspective, in *Advances in Agronomy*, vol. 133,  
830 edited by D. Sparks and S. Hallock, chap. Chapter 5, pp. 183–237, Elsevier,  
831 doi:10.1016/bs.agron.2015.06.001.

832

833 Scholefield, D., and D. Hall (1986), A recording penetrometer to measure the  
834 strength of soil in relation to the stresses exerted by a walking cow, *Journal of*  
835 *Soil Science*, 37(1), 165–176.

836

837 Steinfeld, H., P. Gerber, T. D. Wassenaar, V. Castel, M. Rosales, M. Rosales, and  
838 C. de Haan (2006), *Livestock's long shadow: environmental issues and options*, Food  
839 & Agriculture Org.

840

841 Stewart, R. D., D. E. Rupp, M. R. Abou Najm, and J. S. Selker (2016), A Unified  
842 Model for Soil Shrinkage, Subsidence, and Cracking, *Vadose Zone Journal*, 15(3),  
843 doi:10.2136/vzj2015.11.0146.

844

845 Vereecken, H., A. Schnepf, J. Hopmans, M. Javaux, D. Or, T. Roose,  
846 J. Vanderborght, M. Young, W. Amelung, M. Aitkenhead, S. Allison,  
847 S. Assouline, P. Baveye, M. Berli, N. Brüggemann, P. Finke, M. Flury, T. Gaiser,  
848 G. Govers, T. Ghezzehei, P. Hallett, and K. Lamorski (2016), Modelling soil  
849 processes: review, key challenges and new perspectives, *Vadose Zone Journal*,  
850 15(5), doi:10.2136/vzj2015.09.0131.

851

852 Vyalov, S. S. (2013). *Rheological fundamentals of soil mechanics*. Elsevier.

853

854 Whalley, W., G. Matthews, and S. Ferraris (2012), The effect of compaction and  
855 shear deformation of saturated soil on hydraulic conductivity, *Soil and Tillage*  
856 *Research*, 125, 23–29.

857

858

859 Wu, L., McGechan, M. B., McRoberts, N., Baddeley, J. A., & Watson, C. A. (2007). SPACSYS:  
860 integration of a 3D root architecture component to carbon, nitrogen and water  
861 cycling—model description. *Ecological Modelling*, 200(3-4), 343-359.

862

863 Yi, J., Hu, W., Beare, M., Liu, J., Cichota, R., Teixeira, E., & Guo, L. (2022). Treading compaction  
864 during winter grazing can increase subsequent nitrate leaching by enhancing drainage.  
865 *Soil and Tillage Research*, 221, 105424.

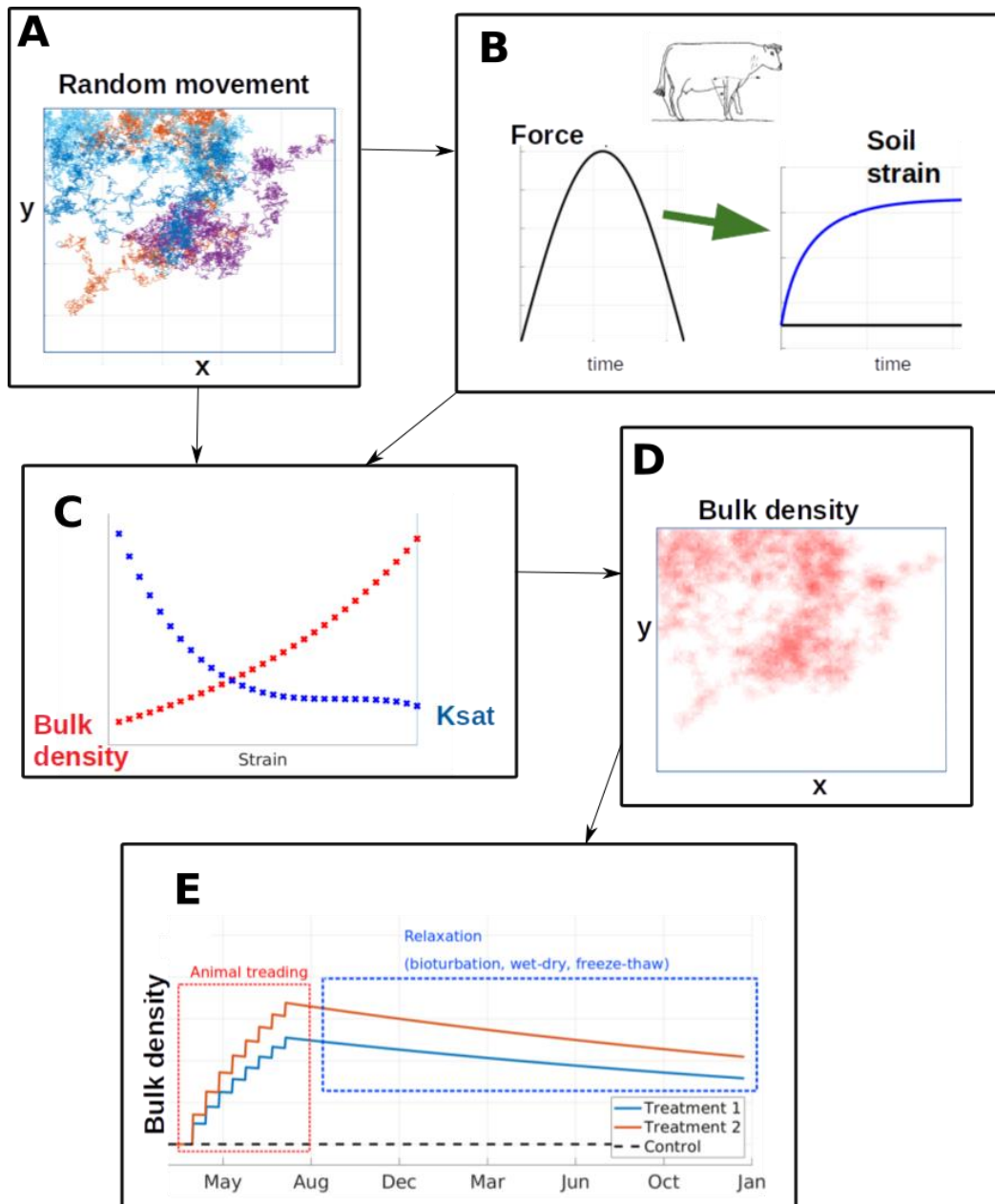
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867 **Figures**

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**Figure 1**

872 Diagram illustrating the main elements of the soil compaction model presented in this work.

873 In A, animal movement in a limited area is simulated obtaining number of steps for a given

874 soil cell. In B, a soil rheology model is used to calculate the soil strain as a function of the

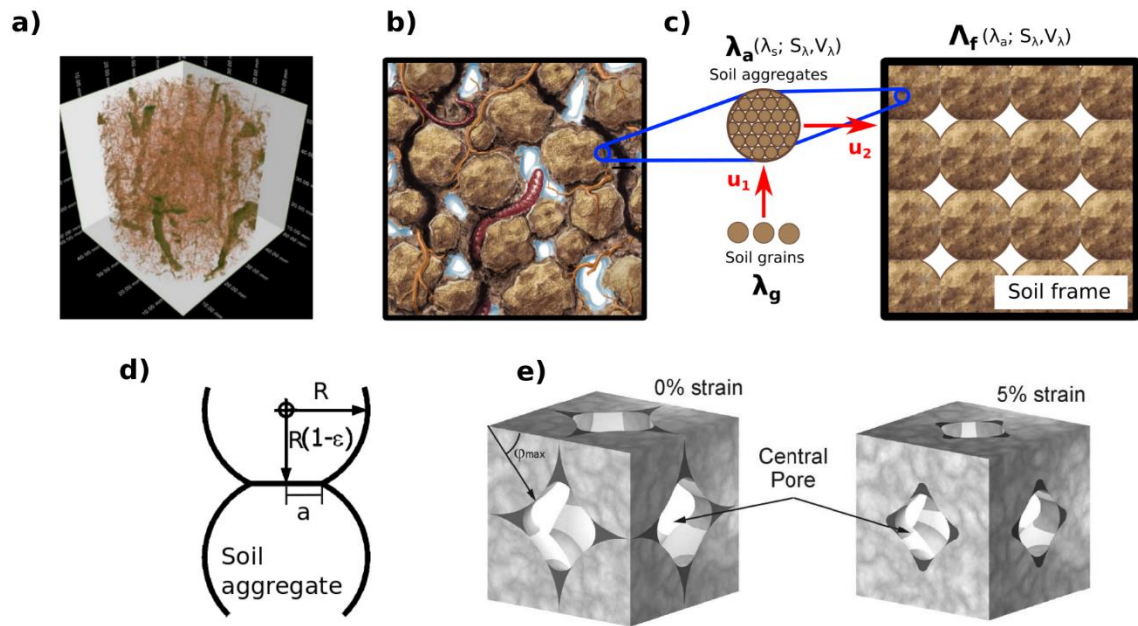
875 steps calculated. In C, soil physics models are used to obtain soil physical properties as a

876 function of the strain. In D, we illustrate that this is done spatially so there is a change in

877 bulk density for all cells in the models. In E, we illustrate how bulk density changes as a

878 function of time for a given cell.

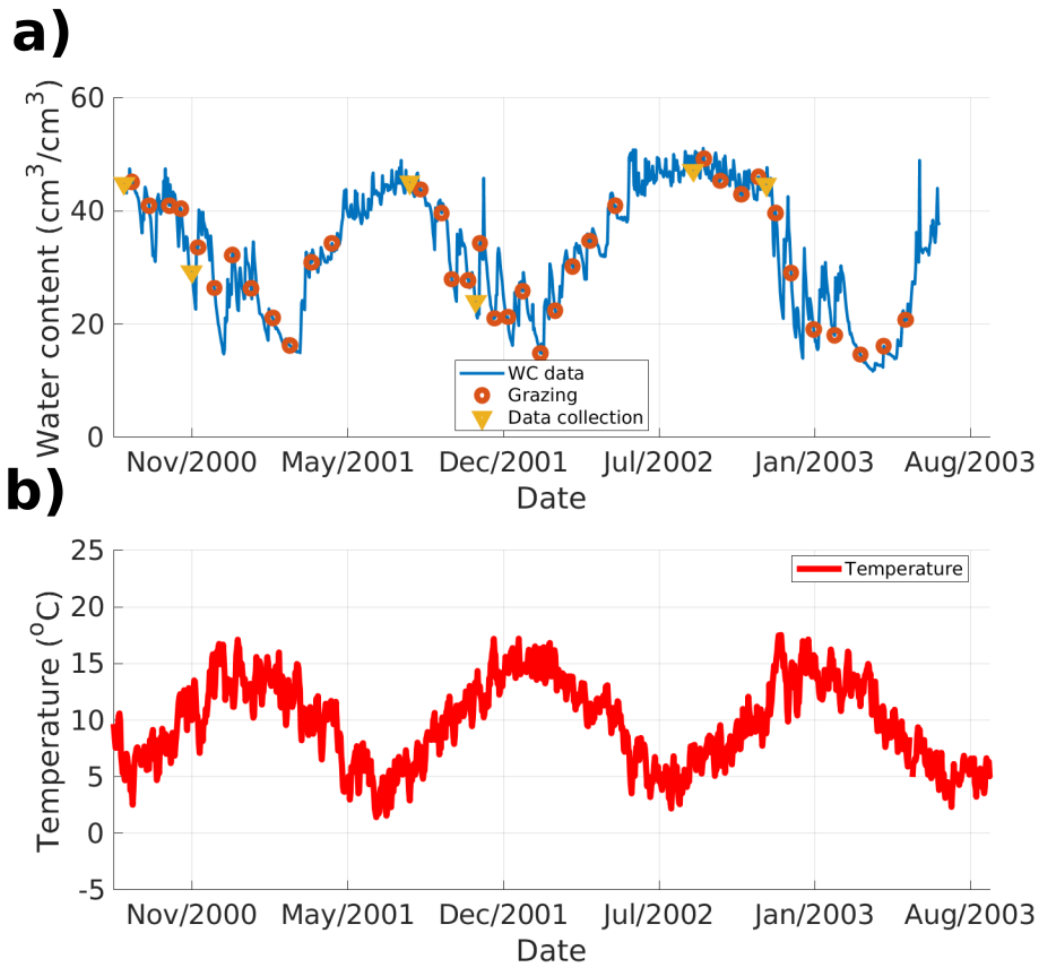
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**Figure 2**

Conceptual model of soil structure. (a) Computer tomography of a  $100 \text{ cm}^3$  soil sample from an agricultural soil (voxel size  $60 \mu\text{m}$ , corresponding to a minimum pore width of  $120 \mu\text{m}$ ) (from Keller et al., 2017). (b) Conceptual illustration of a structured soil including aggregation and macroporosity created by biological activity (from Romero-Ruiz et al., 2018). (c) Schematic representation of the upscaling of soil physical properties of structured soils from soil grains to soil aggregates and ultimately to a soil frame (from Romero-Ruiz, 2021). In these representations the soil is dry. (d) Schematic representation of deformation of contacts between aggregates due to compaction. (e) Illustration of volume reduction and pore closure due to compaction-induced viscous strains.



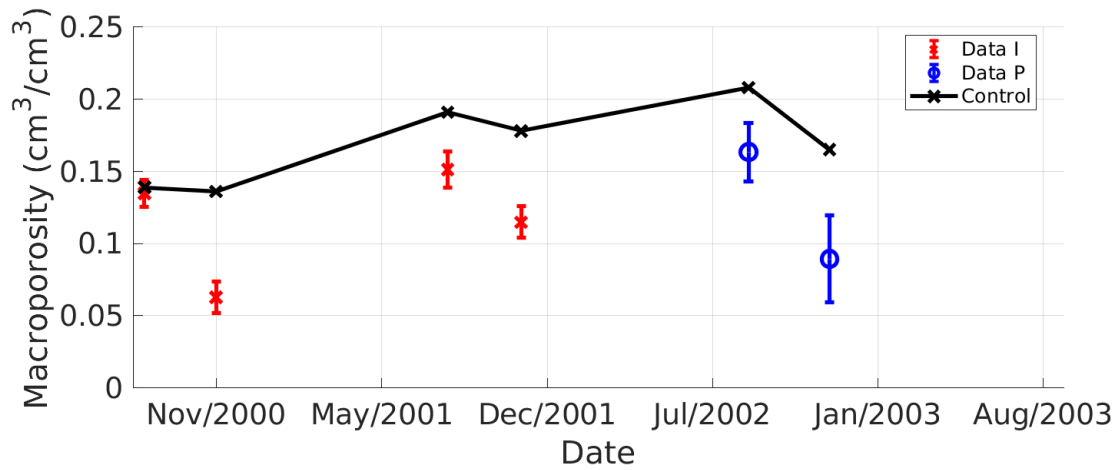
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**Figure 3**

895 (a) Volumetric water content and (b) soil temperature at 10 cm depth measured at the  
 896 Tussock Creek study site. In (a), the grazing dates are marked with circles and the pre- and  
 897 post-spring data collection dates are marked with triangles.

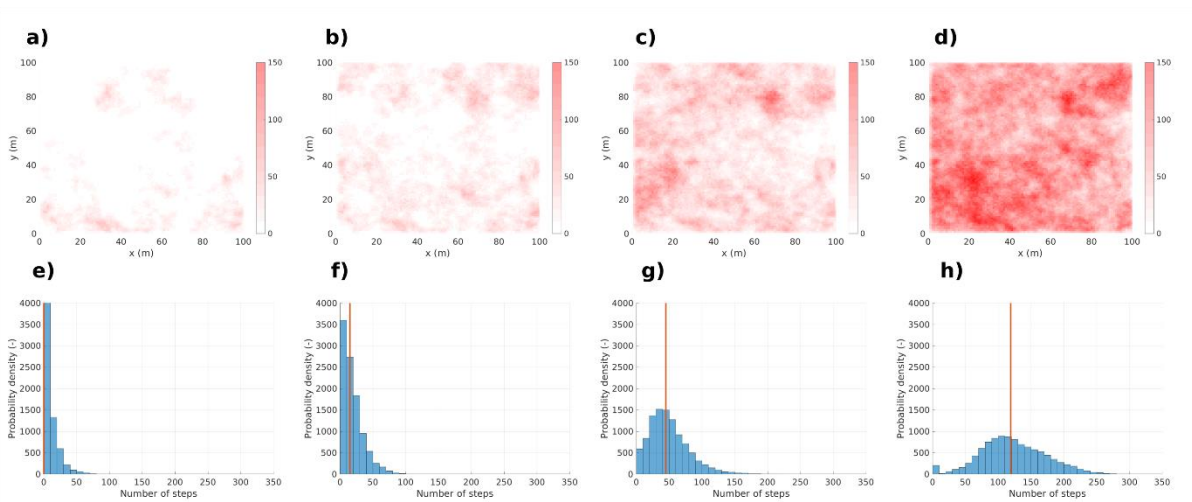
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**Figure 4**

Temporal changes in soil macroporosity values measured at the Tussock Creek study site. The data were averaged for various grazing treatments: normal grazing of undrained land (UND), conventional grazing (CON), conventional grazing, but restricted to 3 hours for grazing events during autumn (AUT), conventional grazing, but restricted to 3 hours grazing when the soil is wet (THR), and conventional grazing, but scheduled to never take place when the soil was wet (NPG).. Error bars correspond to standard deviations. Control (NIL grazed) data are presented for reference. Data were taken from Houlbrooke et al. (2009). Data I corresponds to the data used for parameter calibration and Data P are data predicted for model validation.



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**Figure 5**

913 Maps of simulated number of steps for days (a) 1, (b) 3, (c) 8 and (d) 22 in a grazing period.

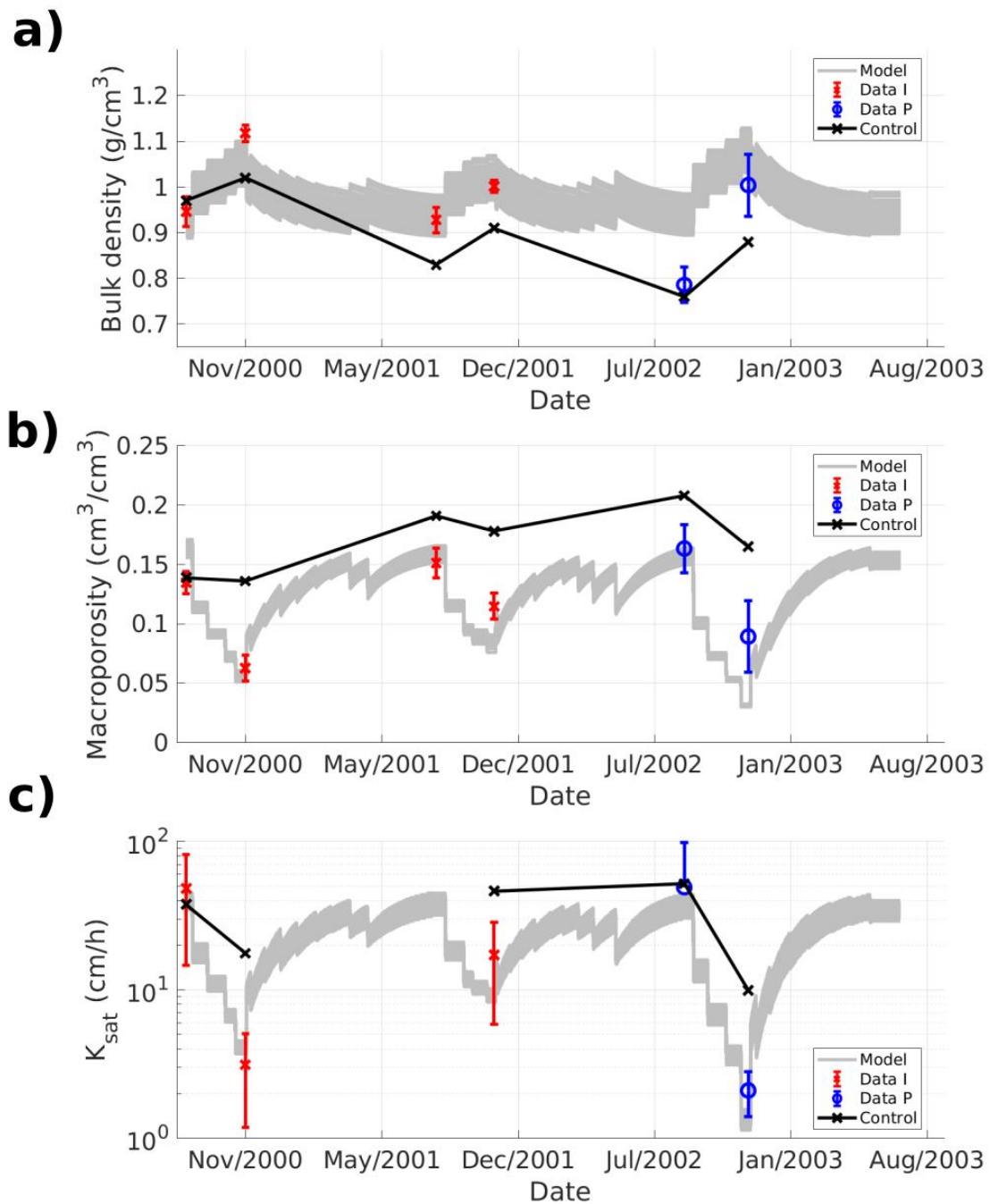
914 For illustration purposes, we chose a stock density of four animals per hectare and

915 considered 5000 steps per animal per day. (e) 1, (f) 3, (g) 8 and (h) 22 present the

916 histograms of the number of steps associated with (a), (b), (c) and (d), respectively. The

917 median value of the obtained distributions is highlighted for each case.

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**Figure 6**

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Modelled and measured (a) bulk density, (b) macroporosity and (c) saturated hydraulic

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conductivity values at 0-5 cm soil depth. Control data (non-grazed) are presented for

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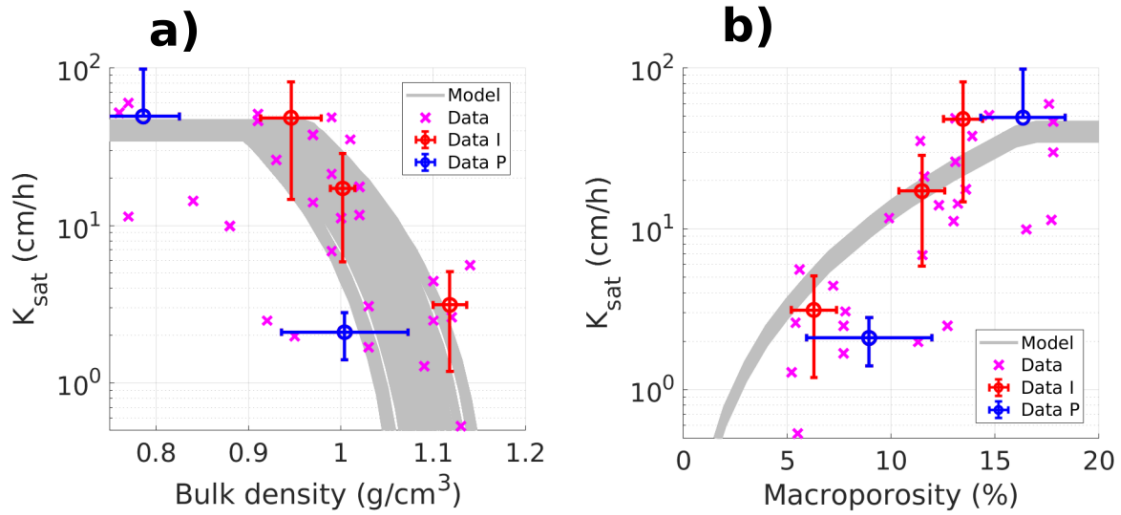
reference. Data I corresponds to the data used for parameter calibration and Data P are

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data predicted for model validation. The curves in grey are all modelled solutions after burn-

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out resulting from the Markov-Chain Monte Carlo inversion.



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**Figure 7**

Modelled and measured saturated hydraulic conductivity as a function of (a) bulk density and (b) macroporosity. The figure contains all data presented by Houlbrooke et al., (2009), data used in this analysis for parameter calibration (Data I) and data predicted for model validation (Data P). The curves in grey are all modelled solutions after burn-out resulting from the Markov-Chain Monte Carlo inversion.