# A New ZCS-PWM Full-Bridge Boost Converter 

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# A New ZCS-PWM Full-Bridge 

## Boost Converter

(Thesis Format: Monograph)
by

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Faculty of Engineering Department of Electrical and Computer Engineering Graduate Program in Engineering Science

A thesis submitted in partial fulfillment of the requirements for the degree of Master of Engineering Science

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## ABSTRACT

The objective of this thesis is to propose, analyze, design, implement, and experimentally confirm the operation of a new Zero-Current-Switching PWM dc-dc fullbridge boost converter that does not have the drawbacks of previously proposed circuits of the same type. In this thesis, the general operating principles of the converter are reviewed, and the converter's operation is discussed in detail and analyzed mathematically. As a result of the mathematical analysis, key voltage and current equations that describes the operation of the auxiliary circuit and other converter devices have been derived. The steady state equations of each mode of operation are used as the basis of a MATLAB program that is used to generate steady-state characteristic curves that shows the effect that individual circuit parameters have on the operation of the auxiliary circuit and the boost converter

Observations as to their steady-state characteristics are made and the curves are used as part of a design procedure to select the components of the converter, especially those of the auxiliary circuit. An experimental full-bridge PWM dc-dc boost converter prototype is built based on the converter design and typical waveforms are presented. The efficiency of the proposed converter operating with the auxiliary circuit is compared to that of a standard PWM dc-dc full-bridge boost converter and the increased efficiency of the proposed converter is confirmed.

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London, Ontario April 2009
Ahmad Mousavi

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## NOMENCLATURE

| AC | Alternative Current |
| :--- | :--- |
| EMI | Electromagnetic Interference |
| ESR | Equivalent Series Resistor |
| DC | Direct Current |
| LC | Inductor and Capacitor |
| MOSFET | Metal Oxide Semiconductor Field Effect Transistor |
| PFC | Power Factor Correction |
| PWM | Pulse Width Modulation |
| SSC | Soft-Switching-Cell |
| UPS | Uninterruptible Power Supply |
| ZCS | Zero Current Switching |
| ZVS | Zero Voltage Switching |
| ZVT | Zero Voltage Transition |

## Chapter 1

### 1.1 General Introduction

### 1.1.1 Power Electronics

It is generally the task of power electronics to convert the electric power available from a power source to the form best suited for the user loads, and some sort of power processor or converter is required to serve as an interface between power source and load. The load may be ac or dc, single-phase or three-phase, and may or may not require transformer isolation from the power source. The power source could be a single-phase or three-phase ac source with line frequency of 50 or 60 Hz ; it can be an electric battery, a solar panel or a commercial power supply. This source feeds the input of the power converter, which converts the power to the required form. The converter can be an ac-dc converter, a dc-dc converter, a dc-ac converter or an ac-ac converter.

Power converters typically consist of semiconductor devices such as transistors and diodes, energy storage elements such as inductors and capacitors, and some sort of controller to regulate the output voltage. Transistor type devices like BJTs (Bipolar Junctions Transistors), MOSFETs (Metal Oxide Silicon Field Effect Transistors) and IGBTs (Insulated Gate Bipolar Transistors) are used as switches in power electronic converters and are made to operate as switches that are either fully on or fully off at any given moment in time. These devices can be operated at higher
switching frequencies than thyristor based devices, which helps reduce converter size. While BJTs and MOSFETs are basic devices, IGBTs are hybrid devices that have an insulated gate like a MOSFET but a conduction region that is the same as a BJT.

BJTs were used as switches in SMPS (Switch Mode Power Supplies) in the late 1970's-early 1980's, but since they are current-controlled devices, they are no longer used in SMPS where switches need to be turned on and off at very high frequencies in the kHz range. The MOSFET, being a charge controlled device, is faster than a BJT. When turned on, a MOSFET is equivalent to a resistance between its source and drain $\left(\mathrm{R}_{\mathrm{DS} \text {,on }}\right)$, while the BJT when fully on is equivalent to a voltage source equal to the saturation voltage between collector and emitter ( $\mathrm{V}_{\mathrm{CE}, \text { sat }}$ ).Thus the conduction losses in MOSFETs are proportional to the square of the on-state current that it is conducting while these losses in a BJT is proportional to the on-state current it is conducting.

The IGBT is a hybrid device that incorporates an insulated gate so that it turns on like a MOSFET and conducts like a BJT in saturation, hence the name IGBT. The IGBT undergoes a MOSFET type turn on, faster than a conventional BJT but its turn off is dependant on the minority carriers present in it during its on state (i.e it undergoes a turn off similar to that of a BJT and has a current tail during its turn off). The IGBT is therefore faster than a conventional BJT but slower than a MOSFET.

MOSFETs are used for lower power applications (typically a few kilowatts) and have lower current and lower voltage ratings (typically a few hundreds of volts) but
higher frequency well in a range of hundreds of kHz while the IGBT is used in higher power applications, they have high voltage and current ratings, but operate at lower frequencies (up to 100 kHz ).

IGBTs and MOSFETs are widely used in Power Electronic applications such as high frequency inverters used at the front ends of high efficiency ac motor drives, high and very high frequency dc-dc converters, power factor correction modules etc. Diagrams of a N-P-N IGBT and a N-channel MOSFET are shown in Fig.1.1.

(a)

(b)

Fig.1.1 (a) Schematic diagram of an IGBT.
(b) Schematic diagram of a power MOSFET.

### 1.1.2 High Switching Frequency Operation in Power Electronic Converters

The size of the energy storage components of a power electronic converter, such as inductors ( L ) and capacitors (C), accounts for much of the overall size of the converter. These components are needed to store and transfer energy from the input power supply to the output load in the converter. Their values depend on the frequency that the converter switch is turned on and off. As the switching frequency is increased, the values of the inductors and capacitors decrease and so do their
physical size and weight; therefore the higher the converter switching frequency, the smaller is the converter size.

Higher switching frequency operation, however, results in increased switching losses and Electro Magnetic Interference (EMI) noise emissions, which are described in the next section. Problems associated with switching losses and EMI caused by sudden switching transitions can offset the advantages achieved by operating a converter with a high switching frequency.

### 1.1.3 Losses in Semiconductor Switches

The semiconductor switches used in power converters are not ideal and are a source of energy losses. The main losses that are associated with these switches are conduction losses and switches losses, which will be described in more detail below.

## a) Conduction losses

The conduction losses of MOSFETs are due to their behavior as a resistor when fully on - the resistance being equal to $\mathrm{R}_{\mathrm{DS}, \text { on }}$, the on state drain to source resistance. The conduction losses of an IGBT are related to the amount of current flowing in the device and $\mathrm{V}_{\mathrm{CE}, \text { sat }}$, the saturation voltage between collector and emitter.
b) Switching losses

In a real semiconductor switch, the switch voltage or switch current do not go to zero instantaneously at the instant of turn-on or turn-off. There is a duration of time during any switching transition (i.e. switch turn-on and turn-off) when there is both
voltage across and current through the switch. The corresponding power loss during each switching instant is the overlapped area of the switch current and voltage waveforms at the instant of turn-on or turn-off of the switch. Since the average power is energy divided by the period, higher switching frequencies lead to higher switching losses. Sharp and sudden switching transitions are also sources of electromagnetic interference (EMI) noise that can affect the performance of a converter and/or other surrounding electrical equipment.

Both the IGBT and MOSFET have anti-parallel body diodes. A MOSFET has a much higher output capacitance between its drain and source than that between collector and emitter of an IGBT. This output capacitance charges up to the off state voltage that the MOSFET is subjected to while the IGBT has a current tailing after it is actually turned off.

In a MOSFET, the main switching losses are caused by the charging and discharging of the output capacitance to and from the off state voltage that the MOSFET is subjected to, while the tailing of current is the primary cause of switching losses in IGBTs. Turning on and turning off the power electronic switches with such switching losses is known as "hard switching". Fig. 1.2 shows the hard switching of power electronic switches in a circuit and the power losses associated with doing so.

(a)

(b)

Fig. 1.2 (a) Hard Switching.
(b) Loss of Power during hard switching.

Fig. 1.2(a) shows a power electronic switch $S_{1}$ that conducts current $i_{\text {sw }}$ when turned on; when turned off the voltage across it is $\mathrm{V}_{0}$. Fig. 1.2(b) shows the typical current and voltage graphs of the switch $S_{1}$ during a whole switching cycle. At $t_{0}$, the driving pulse of $S_{1}$ is removed so that it gets turned off. $S_{1}$ takes time $t_{\text {off }}$ to turn off fully. During this time, due to the overlap of the current and voltage waveforms, there occurs a turn off loss represented by the area under the graph $P_{\text {off }}$. At $t_{1}$, the driving pulse is applied to the switch $S_{1}$ so that it gets turned on. The switch $S_{1}$ takes
time $t_{o n}$ to get turned on. During this time $t_{o n}$, due to overlap of the current and voltage waveforms of $\mathrm{S}_{1}$, there occurs a turn-on loss represented in Fig. 1.2(b) by $\mathrm{P}_{\text {on. }}$

### 1.1.4 Diode Reverse-Recovery Current

In addition to semiconductor switches, power electronic converters also contain diodes. A diode is a semiconductor device that allows current to flow in only one direction, from its anode to its cathode, but does not allow current to flow in the negative direction, from its cathode to its anode. An ideal diode will not conduct any negative current, regardless of whatever negative voltage is placed across it, as long as this voltage does not exceed its maximum rated voltage. In reality, however, whenever the current flowing through a diode is decreased to zero, it may momentarily become negative before finally becoming zero, as shown in Fig 1.3.

This negative current is referred to as reverse-recovery current in the power electronics literature since it flows through the device during the time $t_{\pi r}$ needed by the diode to "recover" from its previous current conduction state. The reverserecovery current can lead to power losses in the diode and also creates electromagnetic interference (EMI) noise. Fast-recovery diodes with short reverse recovery times $\left(\mathrm{t}_{\mathrm{r}}\right)$ are therefore widely used in high-frequency converters.


Fig.1.3. Reverse recovery current in a diode.

### 1.1.5 Soft Switching

The problems of switching losses and EMI associated with hard-switching converter operation can be reduced by using soft-switching. The term "softswitching" in the power electronics literature refers to various techniques where the switching transitions are made to be more gradual to force either the voltage or current to be zero while the switching transition is being made. EMI is reduced by soft-switching because the switching transitions from on to off and vice versa is gradual and not sudden. Switching losses are reduced since the power dissipated in a switch while a switching transition made is proportional to the overlap of the voltage across the switch and the current flowing through it.

Soft-switching forces either the voltage or the current to be zero during the time of transition; there is therefore no overlap between voltage and current and therefore (ideally) no switching loss. There are, therefore, two types of soft-switching: zero-
voltage switching (ZVS) and zero-current switching (ZCS). Although there are many ZVS and ZCS techniques, there are general principles associated with each type.

For power converters operating with high switching frequencies, the MOSFET is the semiconductor device that is most commonly used. The circuit symbol for a MOSFET is shown in Fig.1.4, along with an anti-parallel diode (which is the body diode that is internal to the device) and a capacitor $\mathrm{C}_{\mathrm{ds}}$ that is across the device's drain and source. $\mathrm{C}_{\mathrm{ds}}$ usually consists of an internal capacitance associated with the device and an additional external capacitor. The MOSFET can turn on with ZVS if it is somehow ensured that current is flowing through the body diode to clamp the drainsource voltage to zero just before turn-on. The MOSFET can turn off with ZVS because $\mathrm{C}_{\mathrm{ds}}$ prevents the voltage from rising abruptly as the device is turned off.


Fig.1.4 ZVS MOSFET implementation

A MOSFET can be made to operate with ZCS if an inductor is added in series to it as shown in Fig. 1.5. The MOSFET can turn on with ZCS because the inductor limits the rise in current so that the current flowing through the MOSFET is almost zero as the device is being turned on. The MOSFET can turn off with ZCS if a negative voltage is somehow impressed across the inductor-MOSFET combination so that current falls to zero at a gradual rate due to the inductor.


Fig.1.5 ZCS IGBT implementation.

Although both ZVS and ZCS operations can reduce the switching losses of a MOSFET, ZVS is preferred because ZVS can substantially reduce the losses caused by the discharging of $\mathrm{C}_{\mathrm{ds}}$ into the device when it is turned on whereas ZCS cannot.

It should be noted that although soft-switching can reduce switching losses, conduction losses that exist when current flows through a MOSFET/IGBT/ Diode will still exist.

### 1.2 DC-DC Converters

Dc-dc converters convert an available unregulated dc input voltage into a regulated dc output voltage of a different magnitude and/or polarity as required by a particular load. Most dc-dc converters are switch-mode converters that operate with active semiconductor devices like MOSFETs and IGBTs, acting as on-off switches. These switches are required to undergo repetitive and periodic turn on and turn off. The output dc voltage in such converters are dependant on the duty cycle $\mathrm{D}(<1)$
which is defined as the length of time that the switch is on $\left(\mathrm{t}_{\mathrm{on}}\right)$ over the duration of the switching cycle $\left(\mathrm{T}_{\mathrm{sw}}=1 / \mathrm{f}_{\mathrm{sw}}\right)$.

$$
\begin{equation*}
\mathrm{D}=\mathrm{t}_{\mathrm{on}} / \mathrm{T}_{\mathrm{S}} \tag{1-1}
\end{equation*}
$$

The two most basic types of dc-dc converters are the buck converter (Output voltage is a stepped down value of the input voltage) and boost converter (Output voltage is a stepped up value of the input voltage). Other types of dc-dc converters are buckboost, Cuk, Sepic and Zeta etc. The circuit diagram of a boost converter is shown in Fig.1.6 along with the typical voltage and current waveforms in Fig1.7.


Fig.1.6 A dc-dc boost converter

The converter shown has a MOSFET as the power electronic switch since it is best suited for high switching frequency converters. In steady state, after the switches are turned on, the whole input voltage is applied across the input inductor $L_{i n}$ and it stores up energy. When the switches are turned off, a negative voltage equal to ( $\mathrm{V}_{\text {in }}$ $V_{0}$ ) is applied across the inductor and the energy stored in the inductor is delivered to
the output capacitance $\mathrm{C}_{\mathrm{o}}$. The steady state output voltage of the boost inductor must always be greater than the input voltage as the ratio of the output to input voltage is:

$$
\begin{equation*}
\frac{V_{o}}{V_{i n}}=\frac{1}{1-D} \tag{1-2}
\end{equation*}
$$

In order to operate the MOSFET switches in the boost converter, a periodic pulse $\left(\mathrm{V}_{\mathrm{ge}}\right)$ such as shown in Fig.1.7(b) must be applied between the gate $(\mathrm{g})$ and the emitter(E) of the device through a drive circuit. The MOSFET is on when the pulse $\mathrm{V}_{\mathrm{ge}}$ is high and off when it is low. Since $\mathrm{T}_{\mathrm{on}}=\mathrm{DT} \mathrm{T}_{\mathrm{sw}}$, the duty cycle of the converter and hence the ratio of the output to input voltage, is determined by the width of the pulse $\mathrm{V}_{\mathrm{ge}}$ so that it is the pulse width that is ultimately used to control and regulate the output voltage. This method of controlling the converter output, which is frequently used, is known as pulse width modulation control or PWM control.


Fig. 1.7 a)Waveform of the voltage across input inductance $L_{i n}$ of a boost converter.
b) Waveform of the voltage at the gate of the switch in a boost converter.
c) Waveform of current through the input inductance in a boost converter.

### 1.3 Full-Bridge Boost Converters

Full-bridge boost converters like the one shown in Fig.1.8 are very attractive for applications where an output dc voltage that is considerably larger than the input voltage is needed. Such applications include fuel cell power conversion, medical power supplies, and power supplies for electrostatic applications. These converters are essentially boost converters that contain a step-up transformer so that they can do additional voltage "boosting" without the very large duty ratios (D) needed with the boost converter shown in Fig.1.8.

The converter operates like a boost converter as the current in inductor Lin is increased whenever switches from the same leg are on and it is decreased whenever a pair of diagonally opposed switches is on as energy is transferred to the output through the transformer and the output diodes. It should be noted that there must always be a path for the input inductor current to flow through the full bridge switches at all times.


Fig.1.8 Current-fed PWM full-bridge boost converter

A full-bridge boost converter can be implemented with either zero-voltage switching (ZVS) or zero-current switching (ZCS) depending on the application. ZVS is implemented in applications where the input voltage is high, the input current is low or medium, and switch turn-on switching losses are dominant. ZCS is implemented in applications where the input current is high (regardless of what the input voltage is) and conduction losses are dominant. The focus of the thesis will be on ZCS full-bridge boost converters.

### 1.4 Literature Review

The first ZCS full-bridge converters that were proposed were resonant converters [11], [17], [18]. ZCS resonant converters use an inductive - capacitive (L-C) circuit to create oscillatory (usually sinusoidal) switch current waveforms so that ZCS turnon and turn-off conditions can be achieved for the power switches. The converter shown in Fig. 1.9 is the conventional full-bridge boost converter with added L and C component to create the resonant circuit.

Most resonant converters, however, suffer from high peak switch voltage or current stresses in comparison to conventional PWM converters. This leads to higher conduction losses and higher voltage and current ratings for the power switches and other circuit components. Another disadvantage is that most resonant converters operate with variable switching frequency control (the output voltage is controlled by varying the converter switching frequency). If operation over a wide range in input voltage and output load is required, most resonant converters must operate with a wide switching frequency range. This makes it difficult to optimize the design of the converter and its control.

In the circuit proposed in [11] the converter is a fixed frequency resonant ZCS current fed converter (Fig.1.9) or a variable frequency resonant converter in [17]-[18] that generates a considerable amount of circulating current in the full bridge so that the switches can turn off with ZCS. Examples of variable frequency resonant converters are shown in Fig. 1.10 (a),(b). It should be noted that the circulating
current is not transferred to the load and does little but add to the conduction losses of the converter. Although the converter is more efficient than it would be if ZCS was not implemented, the gains in efficiency are not as much as what they could be due to these losses.


Fig.1.9 Fixed frequency resonant ZCS current fed converter proposed in [11]


Fig. 1.10 (a)


Fig.1.10 (b)
Fig. 1.10 (a), (b) Variable frequency resonant ZCS current fed converter

Most recent soft-switched full-bridge boost converters can be classified as being resonant-transition converters, and have the advantages of conventional PWM converters and resonant converters. They use an additional or auxiliary circuitry that is not a part of the main power circuit to help the main converter switch turn on and off with ZCS. This auxiliary circuit typically consists of an active power switch and passive elements such as diodes, inductors, and capacitors. The operation of the auxiliary circuit only occurs during the turn-on and turn-off of the main converter switch and only a very small portion of switching cycle.

To realize ZCS for the main switch, the basic idea behind this type of auxiliary circuit is to activate the circuit by turning on an auxiliary switch placed properly in the circuit for a small fraction of the switching cycle and just before the semiconductor switch has to be turned off. By activating the circuit, a capacitor placed in the circuit is forced to undergo resonance with some inductance properly
placed with the switch so that the capacitor, under resonance, creates a counter voltage across the inductor-switch pair thus forces the current in the switch to be reduced to zero before the pulse at the gate of the switch is removed. Eventually the switch will be turned off with zero current.

Since the auxiliary circuit is active for only a small portion of the switching cycle, the circuit behaves almost exactly like a conventional PWM converter, but with smoother voltage and current waveforms especially during switching transitions. The components in the auxiliary circuit handle a fraction of the power than the main power circuit components must handle, thus allowing small components to be used. This is especially true of the auxiliary switch, which can be a device with ratings smaller than that of the main power switch and therefore operate with fewer switching losses, so that whatever new switching losses that are created by the auxiliary switch are more than offset by the reduction of switching losses in the main switch. Numerous auxiliary circuits for ZCS-PWM full-bridge converters have been proposed in the power electronics literature [12]-[16].

One of the basic and early versions of such a circuit is shown in Fig.1.11. The auxiliary circuit is simple as it incorporates only one extra inductor and a capacitor and one auxiliary switch, but its drawback is the high current peak in main switches. This high current peak in the main switches calls for the need of switches with higher current ratings, and such switch tends to have higher conduction losses. Also high current peaks tend to create additional unwanted conduction losses. Moreover, due to the resonant capacitor charging to as high as twice the output voltage during the
operation of the auxiliary circuit, there is a need for a resonant capacitor with bigger size since a capacitor's physical size is dependant on its voltage ratings.


Fig.1.11 ZCS full-bridge PWM boost converter

In some cases the converter uses an active auxiliary circuit that is connected in parallel to the full-bridge and used to divert current away from the switches in the bridge before they are to be turned off to realize ZCS turn off of devices [13]-[18]. This circuit is activated just before any switches are to be turned off and is deactivated shortly afterwards. Since the circuit is active for only a short length of time, there is less circulating current compared to the fixed frequency resonant converters, but this current is still significant. All the energy from this current is trapped in the primary side of the converter and it contributes to losses. Examples of such converters were proposed in [15] and [16] and are shown in Fig.1.12 (a), (b) respectively. Both converters have an auxiliary circuit connected to the full-bridge in parallel.


Fig.1.12 Current-fed converters with parallel auxiliary circuit (a) [16] (b) [15]

The additional circulating current also contributes to increased peak current stresses in the full-bridge switches as these switches must conduct the current that they are supposed to conduct, to feed the load and the circulating current. Devices that can withstand higher peak current stresses than those found in conventional boost full-bridge converters are needed as the converter switches [13]-[16].

Fig. 1.13 shows the circuit proposed in [13]. In the paper, high rated switches have been used for the experimental results, so the switches can stand the current peak that occurs because of the additional circulating current.


Fig.1.13. Current fed full-bridge converter proposed in [13]

In some other proposed converters, diodes are placed in series with the switches so that current does not flow through the body-diodes of the switches and circulating current is reduced [14]. The circuit proposed in [14] is shown in Fig.1.14. Although conduction losses are increased, they may be smaller than what they would be if the diodes were not added, but this is at the cost of the additional diodes. Some converters avoid using diodes by using reverse blocking IGBTs [12], but they are more expensive than regular IGBTs and not appropriate for low voltage input applications.


Fig.1.14. Full-bridge boost converter with current-blocking diodes proposed in [14]

Other drawbacks that can be found in previously proposed ZCS full-bridge boost converters include the need for a high side driver [15] for the auxiliary circuit switch(es), which makes the driving of this switch(es) more complicated and the appearance of voltage spikes and/or the significant voltage ringing that can appear across the main converter switches [11]-[18]. The later is due to the output capacitances of the switches resonating with the leakage inductance of the main transformer during their turn off. The spikes and ringing will appear across the secondary diodes as well. This creates a need for higher voltage rated devices, which will increase the cost and the losses in the converter.

### 1.5 Thesis Outline

This thesis is organized as follows:
In Chapter 2, a new auxiliary circuit that allows the main power switches in ZCSPWM full-bridge dc-dc boost converters to operate with soft-switching is proposed and its operation is described.

In Chapter 3, the circuit analysis of a ZCS-PWM full-bridge dc-dc boost converter operating with the proposed auxiliary circuit is presented for the various modes of operation that the converter goes through during a switching cycle, as described in Chapter 2. Important mathematical equations describing voltages and currents of different circuit components during the modes of operation are derived.

In Chapter 4, the conditions that ensure the soft switching of the main switches in the converter are derived with the help of the mathematical equations derived in Chapter 3. Also, characteristics curves showing the behavior of the converter with respect to the variation of different passive components are presented. An experimental prototype is designed using these characteristic curves. Converter component values are chosen using a design procedure that will be presented and demonstrated with an example.

In Chapter 5, experimental voltage and current waveforms for the prototype designed in Chapter 4 are presented to validate the concept of the proposed auxiliary circuit. Efficiency graphs for a full-bridge boost converter with and without the proposed auxiliary circuit are presented to demonstrate the effectiveness of the circuit in increasing converter efficiency.

In Chapter 6, the contributions and conclusions of this thesis are presented and suggestions for future work are given.

## Chapter 2

## A New ZCS-PWM Full-Bridge Boost Converter

### 2.1 Introduction

It was seen in Chapter 1 that previously proposed auxiliary circuits applied to ZCS-PWM full bridge converters introduce additional current and voltage stresses on the converter devices. These stresses can cause additional conduction losses in the devices that can reduce the savings of energy realized by the soft-switching of the main switches. For example, the circulating energy that exists when the auxiliary circuit of some ZCS-PWM converters is operating is trapped in the circuit and creates additional losses.

With these issues in consideration, the auxiliary circuit shown in Fig. 2.1 is proposed. The circuit consists of auxiliary diode $\mathrm{D}_{\text {aux }}$, inductor $\mathrm{L}_{\mathrm{r} 2}$, energy feedforward transformer $T_{\text {aux }}$, auxiliary switch $Q_{\text {aux }}$, diodes $D_{S 1}$ and $D_{S 2}$ placed at the secondary and the tertiary windings of the transformer $\mathrm{T}_{\text {aux }}$ and inductor $\mathrm{L}_{\mathrm{rl}}$ placed in series with the main switches $\mathrm{Q}_{1-4}$ (shown in Fig.2.2).

The main concept behind this auxiliary circuit is to add a transformer to create a counter voltage in the circuit to reduce the peak value of the resonating capacitor voltage $\left(\mathrm{V}_{\mathrm{Cr}}\right)$, which is the main cause of the increased peak current in the auxiliary switch. Clamping the primary of the energy feed-forward transformer with a suitable stepped down value of the output voltage imposes this counter voltage. Adding the transformer also creates a path to take out the circulating energy in the auxiliary
circuit and transfer to the output, thus increasing the overall efficiency of the converter. This energy feed-forward is accomplished by suitably connected diodes at the transformer secondary and tertiary windings.


Fig.2.1. The auxiliary circuit used in the proposed converter

The placement of the proposed auxiliary circuit in a ZCS-PWM dc-dc full-bridge boost converter is proposed in this section and shown in Fig. 2.2. The proposed converter is well-suited in low input voltage / high output voltage PWM dc-dc fullbridge boost converters. This auxiliary circuit is the most efficient when compared to several others implemented in a conventional PWM boost converter. Most other auxiliary circuits (i.e. [19]-[24]), however, cannot be adapted for use in ZCS-PWM isolated boost converters (i.e. fuel cell converters) due to their circuit structure or the
fact that they create unwanted current and voltage stresses on the main devices and undergo high circulating current losses


Fig. 2.2. Proposed ZCS full-bridge boost converter

### 2.2 Converter Operation

In this section, the steady state operation of the proposed full-bridge boost converter will be explained in terms of the different modes or phases that the converter undergoes over a steady-state switching cycle. These modes are distinct from each other in terms of flow of current and voltage across different circuit components. By steady state operation of the converter, it is implied that, at the beginning of each switching cycle, the components of the converter are at the same state with respect to their voltages and currents as they were in the previous
switching cycle, or in other words, the voltage and current waveforms of all components of the converter are identical for every switching cycle in steady state.

The voltage and current waveforms of the different components of the converter during each mode over a switching cycle in steady state will be shown to illustrate the operation of the converter. These modes of operation are important for deriving mathematical equations through circuit analysis that will describe the steady state operation of the converter mathematically. These mathematical equations will be needed to derive the characteristics of the converter with respect to different circuit components and help in designing a prototype.

The following assumptions are made regarding different circuit components while analyzing the proposed boost converter topology:

1) Input boost inductor $L_{r 1}$ is large enough to be considered as a constant current source.
2) Output capacitor $C_{o}$ is large enough to be considered as a voltage source equal to the desired output voltage.
3) All semiconductor switches are ideal i.e, they have zero voltage drop across them while they are on and they have no output capacitance across them.
4) The recovery time of each diode is zero.
5) The energy feed-forward transformer is ideal i.e it has infinite magnetizing inductance, zero leakage inductance and no lossy components associated with it.

The boost converter with the proposed auxiliary circuit undergoes nine different modes of operation over one switching cycle at steady state. In the following section, different modes of operation of the boost converter along with the proposed auxiliary circuit are described:

Mode $0\left(t<t_{0}\right)\left(\right.$ Fig.2.4(a)): Input current $\mathrm{I}_{\mathrm{in}}$ flows through switches $\mathrm{Q}_{3}$ and $\mathrm{Q}_{2}$, and energy is transferred to the load through diodes $\mathrm{D}_{2}$ and $\mathrm{D}_{3}$.

Mode $1\left(t_{0}<t<t_{l}\right)$ (Fig.2.4(b)): At time $t=t_{0}$, both $\mathrm{Q}_{1}$ and $\mathrm{Q}_{4}$ are turned on. Due to the primary transformer leakage inductance, the transfer of current to these switches is gradual so that they turn on with ZCS , and some energy continues to be transferred to the output. Eventually, no current flows in the transformer primary except the magnetizing current (which is neglected here), and the dc bus is shorted with half of $\mathrm{I}_{\mathrm{in}}$ flowing through one full-bridge leg and the other half flowing though the other leg. Since the current splits between two legs of the bridge, losses will be half the case where only one leg is shorted.

Mode $2\left(t_{l}<t<t_{2}\right)$ (Fig.2.4(c)): At $\mathrm{t}=\mathrm{t}_{1}$, the auxiliary switch $\mathrm{Q}_{\mathrm{aux}}$ is turned on and $\mathrm{C}_{\mathrm{r}}$ begins to resonate with $\mathrm{L}_{\mathrm{r} 2}$ and discharge. The auxiliary transformer primary voltage is clamped to $V_{x}=V_{0} \frac{N_{1}}{N_{2}}$ from time $t_{2}$ to $t_{4}$ and the secondary diode $D_{s 1}$ is forward biased. Circulating energy from the auxiliary circuit is transferred to the
output during this time through $\mathrm{T}_{\text {aux }}$ and $\mathrm{D}_{\text {sl }}$. This mode ends when the voltage of Cr $\left(\mathrm{V}_{\mathrm{Cr}}\right)$, reaches zero and diode $\mathrm{D}_{\text {aux }}$ turns on.

Mode $3\left(t_{2}<t<t_{3}\right)\left(\right.$ Fig.2.4(d)): At $\mathrm{t}=\mathrm{t}_{2}$, the voltage across $\mathrm{C}_{\mathrm{r}}$ reaches zero and $\mathrm{D}_{\text {aux }}$ starts to conduct as $\mathrm{C}_{\mathrm{r}}$ continues to resonate with $\mathrm{L}_{\mathrm{r} 2}$ and the voltage across it becomes negative. This negative voltage appears across the dc bus and thus current begins to be diverted away from the full-bridge switches.

Mode $4\left(t_{3}<t<t_{4}\right)$ (Fig.2.4(e)): At $t=t_{3}$, the current through the main switches becomes zero and begins reversing direction by flowing through the body diodes of the switches. Switches $Q_{2}$ and $Q_{3}$ can be turned off softly at any time while current is flowing in their body diodes. Current in the auxiliary circuit is positive but decreasing.

Mode $5\left(t_{4}<t<t_{5}\right)$ (Fig.2.4(f)): At $\mathrm{t}=\mathrm{t}_{4}$, the body diode of $\mathrm{Q}_{\text {aux }}$ starts conducting and the switch can be turned off softly after this instant. During this mode, all the body diodes of all converter switches conduct current and the current coming out of the bridge flows through $\mathrm{L}_{\mathrm{rl}}$ and $\mathrm{D}_{\text {aux }}$ while charging $\mathrm{C}_{\mathrm{r}}$. Energy is transferred from the auxiliary circuit to the load through $\mathrm{T}_{\mathrm{aux}}$ and $\mathrm{D}_{\mathrm{s} 2}$.

Mode $6\left(t_{5}<t<t_{6}\right)$ (Fig. 2.4(g)): At $\mathrm{t}=\mathrm{t}_{5}$, the current in the body diode of $\mathrm{Q}_{\text {aux }}$ goes to zero. During this mode, the voltage across $C_{r}$ increases in resonance with $L_{r l}$ while
the current flows through the body diodes of the full-bridge switches. At the end of this mode the voltage across $C_{r}$ reaches $V_{p r i}=V_{0} / N$.

Mode $7\left(t_{6}<t<t_{7}\right)$ (Fig.2.4(h)): At $t=\mathrm{t}_{6}$, the current in the body diodes of the fullbridge switch becomes zero, and some input current starts to flow through $\mathrm{L}_{\mathrm{rl}}, \mathrm{Q}_{1}$ and $Q_{4}$. The remaining input current continues to charge $C_{r}$ and the voltage across it rises. Energy begins to be transferred to the load through $D_{1}$ and $D_{4}$. At the end of this mode the voltage across $\mathrm{C}_{\mathrm{r}}$ charges up to $\mathrm{V}_{\mathrm{Cr} 0}$.

Mode $8\left(t_{7}<t<t_{8}\right)$ (Fig.2.4(i)): At $\mathrm{t}=\mathrm{t}_{7}$, all the input current flows through the bridge and none through $\mathrm{C}_{\mathrm{r}}$. The converter is in an energy transfer mode.

The proposed ZCS-PWM full-bridge boost converter has the following features:
(i) The presence of a transformer in the auxiliary circuit provides a path for energy that would otherwise be trapped in the auxiliary circuit. Energy can be transferred to the output instead of contributing to conduction losses.
(ii) The auxiliary circuit is adaptive as greater the energy that would otherwise be trapped in the circuit, greater the energy that is transferred to the output, since trapped auxiliary circuit energy is a cause of circulating current. This means that the converter can be made to operate with little additional circulating current regardless of whether it is operating with a light load or a heavy load. This property does not exist in most other ZCS-PWM full-bridge boost converters as
they have a considerable amount of circulating current when operating under light load conditions.
(iii) Since the proposed converter has little additional circulating current regardless of load, it does not need additional diodes connected in series with the full bridge switches to prevent current flowing through their body diodes. There are therefore no conduction losses due to series blocking diodes unlike several other ZCS-PWM full-bridge boost converters.
(iv) The peak current stress of the switches is the same as that of a switch in a conventional PWM boost full-bridge converter, as $\mathrm{D}_{\text {aux }}$ blocks any auxiliary circuit current from flowing into the full-bridge.
(v) One of the drawbacks of a conventional current-fed full bridge converter is that it lacks a DC bus capacitor across the full bridge section so that there can be uncontrolled voltage spikes during turn off of the bridge devices owing to resonance between their output capacitance and leakage inductance which can damage the bridge devices. It can be seen from Fig. 2.3 that the full bridge switches do have an additional voltage stress in the form of a controlled voltage hump and not a voltage spike. The rise of this voltage hump is restricted by the size of $C_{r}, L_{r 1}$ and $L_{1 k}$. This allows lower rated devices to be used as the full bridge switches.

Voltage and current waveforms of different converter components are shown in Fig. 2.3 and the flow of currents in the circuit during a whole switching cycle is shown in Fig. 2.4(a) to Fig. 2.4(i).


Fig.2.3 Voltage and current waveforms for different circuit components of a boost converter with proposed auxiliary circuit operating in steady state.

Circuit diagrams showing current flow in different modes of operation:


Fig. 2.4(a) Current flow in Mode 0


Fig. 2.4(b) Current flow in Mode 1


Fig. 2.4(c) Current flow in Mode 2


Fig. 2.4(d) Current flow in Mode 3


Fig. 2.4(e) Current flow in Mode 4


Fig. 2.4(f) Current flow in Mode 5


Fig. 2.4(g) Current flow in Mode 6


Fig. 2.4(h) Current flow in Mode 7


Fig. 2.4(i) Current flow in Mode 8

### 2.3 Conclusion

In this chapter a new auxiliary circuit for ZCS-PWM full-bridge converters was proposed. The basic operation of a full-bridge boost converter with the proposed auxiliary circuit was shown along with the current and voltage waveforms of different circuit components during different stages or modes of operation of the converter in steady state over a switching cycle. From the discussions presented in this chapter it can be seen that the proposed boost converter operates as a PWM DCDC boost converter except for the very small instant of time as compared to the whole switching cycle when the auxiliary switch is on facilitating ZCS turn-off of the main switches.

## Chapter 3

## Circuit Analysis of the Proposed Boost Converter

### 3.1 Introduction

In the previous chapter, the different modes of steady state operation of a fullbridge boost converter implemented with the proposed auxiliary circuit and operating over a switching cycle were described. In this chapter, an analysis of the boost converter is performed and key mathematical equations are derived based on these modes of operation. These equations are important for understanding the characteristic behavior of the converter with respect to the variation of certain key circuit component values and will help in designing a boost converter with the proposed auxiliary circuit.

### 3.2 Circuit Analysis

The following assumptions are made regarding different circuit components while analyzing the proposed boost converter topology for analyzing the boost converter circuit:

1) The input inductor is large enough to be considered as a constant current source.
2) The output capacitor is large enough to be considered as a voltage source
3) All semiconductor switches are ideal i.e while they are on, they have zero voltage drop across them and that they have no output capacitance across them
4) The reverse recovery time for each diode is zero.
5) The energy feedforward Transformer (T) is ideal i.e. it has infinite magnetizing inductance, zero leakage inductance and no lossy components associated with it.

6 ) From time $t_{2}$ to $t_{4}$ the auxiliary transformer primary winding is clamped to $\mathrm{V}_{\mathrm{x}}=\mathrm{V}_{\mathrm{o}}\left(\mathrm{N}_{1} / \mathrm{N}_{2}\right)$ and diode $\mathrm{D}_{\mathrm{S} 1}$ is forward biased, which allows the transfer of the circulating energy from the auxiliary circuit to the output to occur.
7) From time $t_{4}$ to $t_{6}$ the transformer primary is clamped to $-V_{x}=-V_{0}\left(N_{1} / N_{2}\right)$ and the diode $\mathrm{D}_{\mathrm{S} 2}$ is forward biased, which allows the transfer of the circulating energy from the auxiliary circuit to the output to occur.

The description of each mode of operation was presented in Chapter 2, and the reader is referred to this chapter for the detailed description of each mode.

The equivalent circuit for Mode 1 is shown in Fig. 3.1. Based on this circuit, the following equation can be derived:

$$
\begin{equation*}
V_{o} N=L_{i k} \frac{d i_{i n}(t)}{d t} \tag{3-1}
\end{equation*}
$$

$$
\text { where } N=\frac{N_{1}}{N_{2}}
$$



Fig. 3.1 Current flow in mode 1

In this mode, the leakage current $L_{i k}$ drops from $I_{i n}$ to zero. Integrating from time $t_{0}$ to $t_{1}, Q_{1,4}$ switches current can be written as

$$
\begin{equation*}
\mathrm{I}_{\mathrm{Q} 1-4}(\mathrm{t})=\operatorname{Iin}-\frac{V_{o} N}{L_{i k}}\left(\mathrm{t}-\mathrm{t}_{0}\right) \quad \text { for time } \mathrm{t}_{0}<\mathrm{t}<\mathrm{t}_{1} \tag{3-2}
\end{equation*}
$$

The converter enters Mode $2\left(t=t_{1}\right)$ of operation when the auxiliary switch $Q_{\text {aux }}$ is turned on and $\mathrm{C}_{\mathrm{r}}$ begins to resonate with $\mathrm{L}_{\mathrm{r} 2}$ and discharge. The transformer primary voltage is clamped to $V_{x}=V_{0} \frac{N_{1}^{\prime}}{N_{2}^{\prime}}$ from time $t_{2}$ to $t_{4}$ and the secondary diode $D_{s 1}$ is forward biased.

The equivalent circuit diagram for this mode is shown in Fig. 3.2, which can be simplified in Fig 3.4.


Fig.3.2 Current flow in mode2


Fig.3.3 Current flow in active part of auxiliary circuit in mode2


Fig.3.4 Reduced equivalent circuit of the auxiliary circuit in mode2

Voltage $\mathrm{V}_{\mathrm{Cr}}$ and current $\mathrm{I}_{\mathrm{Lr} 2}$ can be expressed according to the following equations:

$$
\begin{gather*}
\mathrm{V}_{\mathrm{Cr}}(\mathrm{t})=\mathrm{L}_{\mathrm{r} 2} \frac{\mathrm{di}_{\mathrm{Lr} 2}(\mathrm{t})}{\mathrm{dt}}+\mathrm{V}_{\mathrm{x}}  \tag{3-3}\\
\mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})=\mathrm{i}_{\mathrm{Cr}}(\mathrm{t})=-\mathrm{C}_{\mathrm{r}} \frac{\mathrm{~d} \mathrm{~V}_{\mathrm{Cr}}(\mathrm{t})}{\mathrm{dt}}  \tag{3-4}\\
\mathrm{~V}_{\mathrm{Cr}}(\mathrm{t})=-\mathrm{L}_{\mathrm{r} 2} \mathrm{C}_{\mathrm{r}} \frac{d^{2}}{d t^{2}} \mathrm{~V}_{\mathrm{Cr}}(\mathrm{t})+\mathrm{V}_{\mathrm{x}} \tag{3-5}
\end{gather*}
$$

The differential equation (3-5) has the following initial conditions: $\mathrm{V}_{\mathrm{cr}}(0)$ is the initial capacitor voltage for this mode and $\mathrm{V}_{\mathrm{cr}}{ }^{\prime}(0)$ is the initial time derivative of the capacitor voltage for this mode. Since the initial current in $\mathrm{L}_{\mathrm{r} 2}$ is zero, therefore equation (3-6) can be written as

$$
\begin{equation*}
\left[\frac{d}{d t} \mathrm{~V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t})\right]_{\mathrm{t}=0}=-\left(1 / \mathrm{C}_{\mathrm{r}}\right)\left[\frac{d}{d t} \mathrm{q}_{\mathrm{Cr}}(\mathrm{t})\right]_{\mathrm{t}=0}=\left(1 / \mathrm{C}_{\mathrm{r}}\right)\left[\mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})\right]_{\mathrm{t}=0}=0 \tag{3-6}
\end{equation*}
$$

and the solution to this equation is

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Cr}}(\mathrm{t})=\mathrm{V}_{\mathrm{x}}+\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \cos \omega_{2} \mathrm{t} \text { for } \mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{3} \tag{3-7}
\end{equation*}
$$

From the initial conditions of Mode 2, $\mathrm{i}_{\mathrm{L}+2}(\mathrm{t})=\mathrm{i}_{\mathrm{Cr}}(\mathrm{t})$ for $\mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{3}$ and

$$
\begin{align*}
\mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t}) & =\mathrm{i}_{\mathrm{Cr}}(\mathrm{t})=-\mathrm{C}_{\mathrm{r}} \frac{d}{d t} \mathrm{~V}_{\mathrm{Cr}}(\mathrm{t})=\mathrm{C}_{\mathrm{r}}\left(\mathrm{~V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \omega_{2} \sin \omega_{2} \mathrm{t} \\
& =\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}\right] \sin \omega_{2} \mathrm{t} \text { for } \mathrm{t}_{1}<\mathrm{t}<\mathrm{t}_{2} \tag{3-8}
\end{align*}
$$

where $\omega_{2}{ }^{2}=1 / L_{r} \mathrm{C}_{\mathrm{r}}$ and $\mathrm{Z}_{2}=\sqrt{L r 2 / C r}$ is characteristic impedance of the auxiliary circuit. Since this mode ends when the voltage across Cr is zero, the duration of this mode can be determined from equ.(3-7) to be

$$
\begin{equation*}
t_{2}-t_{1}=\left[\cos ^{-1}\left(-\mathrm{V}_{\mathrm{x}} /\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right)\right] / \omega_{2}=\gamma\right. \tag{3-9}
\end{equation*}
$$

so that

$$
\begin{equation*}
\mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})=\mathrm{i}_{\mathrm{L} 22}\left(\mathrm{t}_{4}\right)=\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}\right] \sin \omega_{2} \gamma \tag{3-10}
\end{equation*}
$$

At the end of Mode 2 , since $\mathrm{V}_{\mathrm{Cr}}(0) \gg \mathrm{V}_{\mathrm{x}}$, then $\gamma \approx \pi / 2$ according to equation (3-9) and (3-10) can be approximated as:

$$
\begin{equation*}
\mathrm{i}_{\mathrm{Lr} 2}\left(\mathrm{t}_{4}\right) \approx\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2} \tag{3-11}
\end{equation*}
$$

Mode 3 of the operation starts at $t_{2}$ when $D_{\text {aux }}$ starts conducting. The equations that define this mode also define Modes 4 and 5; this can be seen by considering the equivalent circuit diagrams for each mode. Fig 3.5 shows the equivalent circuit diagram of Mode 3 and the reduced equivalent circuit diagram for this mode is shown in Fig. 3.6. Similar diagrams are shown in Figure 3.7 and 3.8 for Modes 4 and 5.


Fig. 3.5 Current flow during mode 3


Fig.3.6 Reduced equivalent circuit of mode 3


Fig. 3.7. Flow of current in mode 4


Fig. 3.8. Current flow in mode 5

It can be seen from Figures 3.5 to 3.8 that the flow of current is not interrupted by any switching action so that it is continuous; therefore Modes 3-5 can be considered as a single mode of operation for the purpose of analysis.

By applying Kirchoff's current law to the equivalent circuit in Fig.3.8, the following relation is found:

$$
\begin{equation*}
I_{s}=i_{L_{r 1}}(t)+i_{L r 2}(t)+i_{C_{r}}(t) \tag{3-12}
\end{equation*}
$$

The initial conditions for the combined modes are $\mathrm{i}_{\mathrm{Lr} 1}\left(\mathrm{t}_{3}\right)=\mathrm{I}_{\mathrm{s}}, \mathrm{V}_{\mathrm{Cr}_{\mathrm{r}}\left(\mathrm{t}_{3}\right)}=0$ and

$$
\begin{equation*}
\mathrm{i}_{\mathrm{L} 22}\left(\mathrm{t}_{3}\right) \approx\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2} \tag{3-13}
\end{equation*}
$$

Since diode $\mathrm{D}_{2}$ is conducting, the following equation can be written:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Lr} 1}=\mathrm{V}_{\mathrm{Cr}}=\mathrm{V}_{\mathrm{Lr} 2}+\mathrm{V}_{\mathrm{x}} \tag{3-14}
\end{equation*}
$$

Differentiating equation (3-12) with respect to time gives the following:

$$
\begin{equation*}
0=\frac{d}{d t} \mathrm{i}_{\mathrm{Lr} 1}(\mathrm{t})+\frac{d}{d t} \mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})+\frac{d}{d t} \mathrm{i}_{\mathrm{Cr}}(\mathrm{t}) \tag{3-15a}
\end{equation*}
$$

The time derivative of $\mathrm{I}_{\mathrm{in}}$ is zero because it is the input current, which is assumed to be constant when the auxiliary circuit is active. Substituting equation (3-14) in equation (3-15a) results in

$$
\begin{equation*}
0=\mathrm{V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t}) / \mathrm{L}_{\mathrm{r} 1}+\left[\mathrm{V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t})-\mathrm{V}_{\mathrm{x}}\right] / \mathrm{L}_{\mathrm{r} 2}+\mathrm{C}_{\mathrm{r}} \frac{d^{2}}{d t^{2}} \mathrm{~V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t}) \tag{3-15b}
\end{equation*}
$$

which can be rewritten as

$$
\begin{equation*}
0=\mathrm{V}_{\mathrm{Cr}}(\mathrm{t}) / \mathrm{L}_{\mathrm{eq}}-\mathrm{V}_{\mathrm{x}} / \mathrm{L}_{\mathrm{r} 2}+\mathrm{C}_{\mathrm{r}} \frac{d^{2}}{d t^{2}} \mathrm{~V}_{\mathrm{Cr}}(\mathrm{t}) \tag{3-15c}
\end{equation*}
$$

where $\mathrm{L}_{\text {eq }}=\mathrm{L}_{\mathrm{r} 1} \mathrm{~L}_{\mathrm{r} 2} /\left(\mathrm{L}_{\mathrm{r} 1}+\mathrm{L}_{\mathrm{r}}\right)$. Equ. (3-15c) can be rearranged to give

$$
\begin{equation*}
-\mathrm{C}_{\mathrm{r}} \frac{d^{2}}{d t^{2}} \mathrm{~V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t})=\mathrm{V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t}) / \mathrm{L}_{\mathrm{eq}}-\mathrm{V}_{\mathrm{x}} / \mathrm{L}_{\mathrm{r} 2} \tag{3-15d}
\end{equation*}
$$

Dividing both sides of (3-15d) by $\mathrm{C}_{\mathrm{r}}$ results in

$$
\begin{equation*}
-\frac{d^{2}}{d t^{2}} \mathrm{~V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t})=\mathrm{V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t}) / \mathrm{L}_{\mathrm{eq}} \mathrm{C}_{\mathrm{r}}-\mathrm{V}_{\mathrm{x}} / \mathrm{L}_{\mathrm{r} 2} \mathrm{C}_{\mathrm{r}} \tag{3-15e}
\end{equation*}
$$

Substituting $\omega_{\mathrm{eq}}{ }^{2}=1 / \mathrm{L}_{\mathrm{eq}} \mathrm{C}_{\mathrm{r}}$ and $\omega_{2}{ }^{2}=1 / L_{\mathrm{r} 2} \mathrm{C}_{\mathrm{r}}$ into this equation gives

$$
\begin{equation*}
-\frac{d^{2}}{d t^{2}} \mathrm{~V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t})=\mathrm{V}_{\mathrm{Cr}}(\mathrm{t}) \omega_{\mathrm{eq}}^{2}-\mathrm{V}_{\mathrm{x}} \omega_{2}^{2} \tag{3-15f}
\end{equation*}
$$

For the combined mode 3-5 of operation, the initial resonance capacitor voltage is

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Cr}}(0)=0 \tag{3-16}
\end{equation*}
$$

and its initial time derivative is

$$
\begin{align*}
{\left[\frac{d}{d t} \mathrm{~V}_{\mathrm{cr}}(\mathrm{t})\right]_{\mathrm{t}=0} } & =-\left(1 / \mathrm{C}_{\mathrm{r}}\right)\left[\frac{d}{d t} \mathrm{q}_{\mathrm{cr}}(\mathrm{t})\right]_{\mathrm{t}=0} \\
& =-\left(1 / \mathrm{C}_{\mathrm{r}}\right)\left[\mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})\right]_{\mathrm{t}=0} \approx-\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2} \mathrm{C}_{\mathrm{r}} \tag{3-17}
\end{align*}
$$

Applying the initial conditions given by (3-16) and (3-17), the solution of the differential equation (3-15f) is given by:

$$
\begin{equation*}
\left.\mathrm{V}_{\mathrm{Cr}}(\mathrm{t})=-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \sqrt{(1+L r 2 / L r 1}\right)\right] \sin \omega_{\mathrm{eq}} \mathrm{t}+\mathrm{V}_{\mathrm{x}} \omega_{2}^{2}\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right] / \omega_{\mathrm{eq}}^{2} \tag{3-18}
\end{equation*}
$$

From the equivalent circuit diagrams shown in Figs. 3.5-3.8 the following equation can be written

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Lr} 1}(\mathrm{t})=\mathrm{V}_{\mathrm{Cr}}(\mathrm{t})=\mathrm{L}_{\mathrm{r} 1} \frac{d}{d t} \mathrm{i}_{\mathrm{Lr} 1}(\mathrm{t})=\mathrm{L}_{\mathrm{r} 2} \frac{d}{d t} \mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})+\mathrm{V}_{\mathrm{x}} \tag{3-19a}
\end{equation*}
$$

which can be rewritten as

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Cr}}(\mathrm{t}) / \mathrm{L}_{\mathrm{rl}}=\frac{d}{d t} \mathrm{i}_{\mathrm{Lrl}}(\mathrm{t}) \tag{3-19b}
\end{equation*}
$$

and simplified to

$$
\begin{equation*}
\left[\mathrm{V}_{\mathrm{Cr}}(\mathrm{t}) / \mathrm{L}_{\mathrm{rl}}\right] \mathrm{dt}=\mathrm{d}\left(\mathrm{i}_{\mathrm{Lr} 1}(\mathrm{t})\right) \tag{3-19c}
\end{equation*}
$$

Integrating from the initial stage $t=0$ for this mode to any intermediate time $t<\mathrm{t}_{6}$, then using the initial value of $\mathrm{i}_{\mathrm{Lr} 1}(\mathrm{t})$ and simplifying results in
$\left.\mathrm{i}_{\mathrm{Lrl}}(\mathrm{t})=\mathrm{I}_{\mathrm{s}}\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{rl}}\right]\left[1-\cos \omega_{\mathrm{eq}}\right]\right]+\mathrm{V}_{\mathrm{x}} \omega_{2}{ }^{2}\left[\mathrm{t}-\sin \omega_{\mathrm{eq}} \mathrm{t} / \omega_{\mathrm{eq}}\right] / \omega_{\mathrm{eq}}{ }^{2} \mathrm{~L}_{\mathrm{rl}}$

$$
\begin{equation*}
\text { for } \mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6} \tag{3-19~d}
\end{equation*}
$$

From equ.(3-19a), it can be written that

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Cr}_{\mathrm{r}}}(\mathrm{t})=\mathrm{L}_{\mathrm{r} 2} \frac{d}{d t} \mathrm{i}_{\mathrm{L} 2}(\mathrm{t})+\mathrm{V}_{\mathrm{x}} \tag{3-20a}
\end{equation*}
$$

Integrating and simplifying this equation with an initial condition of $\mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})$ approximately equals to $\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}$ which results in

$$
\begin{align*}
& \mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})=\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{r} 2}\right]\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right]+\mathrm{V}_{\mathrm{x}} \omega_{2}^{2}\left[\mathrm{t}-\sin \omega_{\mathrm{eq}} \mathrm{t} / \omega_{\mathrm{eq}}\right] / \omega_{\mathrm{eq}}{ }^{2} \mathrm{~L}_{\mathrm{r} 2} \\
&-\mathrm{V}_{\mathrm{x}} \mathrm{t} / \mathrm{L}_{\mathrm{r} 2}  \tag{3-20b}\\
& \text { for } \mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6}
\end{align*}
$$

At $t=t_{6}$, the current in the body diodes of the full-bridge switch becomes zero (as shown in Fig. 3.9), and some input current starts to flow through $L_{r 1}, Q_{1}$ and $Q_{4}$. The remaining input current continues to charge $\mathrm{C}_{\mathrm{r}}$ and the voltage across it rises. Energy begins to be transferred to the load through $D_{1}$ and $D_{4}$. At the end of this mode the voltage across $\mathrm{C}_{\mathrm{r}}$ charges up to $\mathrm{V}_{\mathrm{Cr} 0}$. The differential equations describing this mode are

$$
\begin{gather*}
I_{i n}=C_{r} \frac{d v_{C r}(t)}{d t}+i_{L r 1}  \tag{3-21}\\
V_{C r}(t)=L_{r 1} \frac{d i_{L r 1}(t)}{d t}+\frac{V_{o}}{N} \tag{3-22}
\end{gather*}
$$

which have the following initial conditions: $\mathrm{V}_{\mathrm{Cr}}(0)=\mathrm{Vo} / \mathrm{N}, \mathrm{i}_{\mathrm{Lr}}(0)=0, \mathrm{i}_{\mathrm{Cr}}(0)=\mathrm{I}_{\mathrm{in}}$.


Fig.3.9 Current flow in mode 7

Applying these initial conditions the capacitor voltage in this mode is given by

$$
\begin{align*}
& \mathrm{i}_{\mathrm{Lr} 1}(\mathrm{t})=\mathrm{I}_{\mathrm{in}}\left(1-\cos \omega_{1} t\right)  \tag{3-23}\\
& \mathrm{V}_{\mathrm{Cr}}(\mathrm{t})=\frac{\mathrm{Vo}}{\mathrm{~N}}+\mathrm{I}_{\mathrm{in}} Z_{1} \sin \omega_{1} t  \tag{3-24}\\
& \text { where } \omega_{1}=\frac{1}{\sqrt{\left(\mathrm{~L}_{\mathrm{r} 1}+\mathrm{L}_{\mathrm{ik}}\right) \mathrm{C}_{\mathrm{r}}}}  \tag{3-25}\\
& \text { and } Z_{1}=\sqrt{\frac{L_{r 1}+L_{i k}}{C_{r}}} \tag{3-26}
\end{align*}
$$

where $\mathrm{L}_{\mathrm{ik}}$ is the transformer leakage inductance.
At the end of this mode the capacitor voltage $\mathrm{V}_{\mathrm{Cr}}$ reaches its initial value $\mathrm{V}_{\mathrm{Cr}}(0)$
given by:

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Cr}}(0)=\frac{\mathrm{Vo}}{\mathrm{~N}}+\mathrm{I}_{\mathrm{in}} \mathrm{Z}_{1} \tag{3-27}
\end{equation*}
$$

### 3.3 Summary of Key Equations

In this section the equations describing the current and voltage of different components of the converter during one switching cycle which will prove important for designing circuit components are presented and will be referred while designing a specific boost converter with the proposed auxiliary circuit in Chapter 4.

Initial resonant capacitor voltage $\mathrm{V}_{\mathrm{Cr}}(0)=\frac{\mathrm{Vo}}{\mathrm{N}}+\mathrm{I}_{\text {in }} \mathrm{Z}_{1}$
Resonant capacitor voltage during mode- 2 : $\mathrm{V}_{\mathrm{Cr}}(\mathrm{t})=\mathrm{V}_{\mathrm{x}}+\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \cos \omega_{2} \mathrm{t}$
Resonant Inductor $\mathrm{L}_{\mathrm{r} 2}$ current during mode-2: $\mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})=\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}\right] \sin \omega_{2} \mathrm{t}$

Resonant Inductor $\mathrm{L}_{\mathrm{r} 2}$ current during mode-2 to mode-6:

$$
\begin{aligned}
& \mathrm{i}_{\mathrm{Lr} 2}(\mathrm{t})=\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{r} 2}\right]\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right]+\mathrm{V}_{\mathrm{x}} \omega_{2}^{2}\left[\mathrm{t}-\sin \omega_{\mathrm{eq}} \mathrm{t} / \omega_{\mathrm{eq}}\right] / \omega_{\mathrm{eq}}{ }^{2} \mathrm{~L}_{\mathrm{r} 2} \\
&-\mathrm{V}_{\mathrm{x}} \mathrm{t} / \mathrm{L}_{\mathrm{r} 2} \\
& \text { for } \mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6}
\end{aligned}
$$

Resonant Inductor $\mathrm{L}_{\mathrm{r} 1}$ current during mode-2 to mode-6:
$\mathrm{i}_{\mathrm{Lrl}}(\mathrm{t})=\mathrm{I}_{\mathrm{S}}-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{rl}}\right]\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right]+\mathrm{V}_{\mathrm{x}} \omega_{2}{ }^{2}\left[\mathrm{t}-\sin \omega_{\mathrm{eq}} \mathrm{t} / \omega_{\mathrm{eq}}\right] / \omega_{\mathrm{eq}}{ }^{2} \mathrm{~L}_{\mathrm{r} 1} \quad$ for $\mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6}$

### 3.4 Conclusion

In this chapter, the circuit analysis of a PWM dc-dc boost converter operating with an energy feed-forward auxiliary circuit with reduced conduction losses and switch stresses was presented. The various modes of operation that the converter goes through during a switching cycle were presented, and a mathematical analysis of each mode was performed. The results of the analysis will be used to examine the steady-state characteristics in the next chapter of the thesis that will be needed for designing an experimental prototype of such a converter.

## Chapter 4

## Design Procedure and Example

### 4.1 Introduction

In this chapter, the results of the mathematical analysis performed on the fullbridge PWM dc-dc boost converter with the proposed auxiliary circuit in the previous chapter will be used to determine the steady-state characteristics and properties of the converter. After these have been determined, they will be used as part of a procedure to design the converter by selecting appropriate converter component values. The procedure will be demonstrated with an example in this chapter and can be used to design other PWM converters with the same auxiliary circuit.

### 4.2 Conditions for ZCS Turn-Off in the Proposed Full-Bridge Converter

In this section, the conditions for achieving the ZCS of both the main switch and auxiliary switch of the converter with the proposed auxiliary circuit, shown in Fig. 4.1, are analyzed.

The conditions that must be met to ensure the ZCS turn-off of the main switches can be determined from the equations that define the main and auxiliary switch currents during the time that the converter is operating in Modes 3-5, as shown in Chapter 3. These equations are as follows:


Fig.4.1- PWM DC-DC boost converter with the proposed auxiliary circuit.

$$
\begin{array}{r}
\mathrm{I}_{\mathrm{Ql}}(\mathrm{t})=\mathrm{I}_{\mathrm{s}}-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{r} 1}\right]\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right]+\mathrm{V}_{\mathrm{x}} \omega_{2}^{2}\left[\mathrm{t}-\sin \omega_{\mathrm{eq}} \mathrm{t} / \omega_{\mathrm{eq}}\right] / \omega_{\mathrm{eq}}{ }^{2} \mathrm{~L}_{\mathrm{rl}} \\
\text { for } \mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6} \tag{4-1}
\end{array}
$$

$\mathrm{I}_{\mathrm{Qaux}}(\mathrm{t})=\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{r} 2}\right]\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right]+$

$$
\begin{equation*}
\mathrm{V}_{\mathrm{x}} \omega_{2}^{2}\left[\mathrm{t}-\sin \omega_{\mathrm{eq}} \mathrm{t} / \omega_{\mathrm{eq}}\right] / \omega_{\mathrm{eq}}^{2} \mathrm{~L}_{\mathrm{r} 2}-\mathrm{V}_{\mathrm{x}} \mathrm{t} / \mathrm{L}_{\mathrm{r} 2} \quad \text { for } \mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6} \tag{4-2}
\end{equation*}
$$

According to these equations, the currents in the switches can drop to zero, reverse direction, and become negative. A negative value of $\mathrm{I}_{\mathrm{Q} 1}$ in equ. (4-1) represents a flow of current through the body diode of the main switch $\mathrm{Q}_{1}$ and a negative value of $\mathrm{I}_{\text {Qaux }}$ in equ. (4-2) represents a flow of current through the body diode of the auxiliary switch $\mathrm{Q}_{\text {aux. }}$. Since a switch can be turned off with ZCS while current is flowing through its body diode, the key condition that must be satisfied to ensure that a switch can be turned off with ZCS is that the equation that defines its current is negative. This can be done for both $Q_{1}$ and $Q_{\text {aux }}$ by selecting appropriate values of inductors $L_{r 1}$ and $L_{r 2}$ and capacitor $C_{r}$.

It is evident from equations (4-1) and (4-2) that the instantaneous auxiliary switch current depends mainly on the output voltage, while the instantaneous current of the main switches depends on the output voltage as well as the magnitude of the input current, which can be described by the following equation:

$$
\begin{equation*}
\mathrm{I}_{\mathrm{s}}=\mathrm{P}_{\mathrm{o}} / \eta \mathrm{V}_{\mathrm{in}} \tag{4-3}
\end{equation*}
$$

where $I_{s}=$ Input current,

$$
\begin{aligned}
& \mathrm{P}_{\mathrm{o}}=\text { Output power, } \\
& \eta=\text { Efficiency of the converter, } \\
& V_{\mathrm{in}}=\text { Input Voltage. }
\end{aligned}
$$

For the current of the main full-bridge switches, if the auxiliary circuit components are properly selected to ensure that the current can become negative for a particular value of $\mathrm{I}_{\mathrm{QI}}=\mathrm{I}_{\mathrm{Q} 1, \mathrm{Max}}$ (the input current when the converter is operating with maximum load), then the current can become negative for any lesser value of $\mathrm{I}_{\mathrm{in}}$, for the same value of $V_{0}$. In other words, if a $Z C S$ turn-off for $Q_{1}$ can be ensured when $\mathrm{I}_{\mathrm{Q} 1}=\mathrm{I}_{\mathrm{Q} 1, \mathrm{Max}}$, then it can also be ensured when $\mathrm{I}_{\mathrm{Q} 1}<\mathrm{I}_{\mathrm{Q} 1, \text { max }}$.

To turn off the bridge switches with ZCS under all operating loads, it must be ensured that the auxiliary switch current is greater than the current of the main fullbridge switches during the time that $\mathrm{Q}_{1-4}$ are being turned off, when the converter is operating with maximum load. The peak current of the main switches at maximum load $\mathrm{I}_{\mathrm{Q} 1, \text { max }}$ must be less than the peak auxiliary switch current at maximum load, $\mathrm{I}_{\text {Qaux }}$, which can be defined as

$$
\begin{equation*}
\mathrm{I}_{\mathrm{Qaux}, \max }=\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2} \tag{4-4}
\end{equation*}
$$

where $\mathrm{Z}_{2}=\sqrt{\operatorname{Lr} 2 / C r}$ is the characteristic impedance of the auxiliary circuit and $\mathrm{Vx}=\mathrm{V}_{0} / \mathrm{N}$ where N is the turns ratio of the secondary winding to the primary winding of the auxiliary circuit transformer.

Another criterion can be derived by taking the time derivative of equ. (4-2) for the auxiliary switch from time $\mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6}$. To simplify this analysis, it can be assumed that the auxiliary circuit operates for only a small fraction of the switching cycle. With this assumption, the term

$$
\mathrm{V}_{\mathrm{x}} \omega_{2}^{2}\left[t-\sin \omega_{\mathrm{eq}} t / \omega_{\mathrm{eq}}\right] / \omega_{\mathrm{eq}}{ }^{2} \mathrm{~L}_{\mathrm{r} 2}
$$

can be neglected so that equ. (4-2) can be written as

$$
\begin{equation*}
\mathrm{i}_{\text {Qaux }}(\mathrm{t}) \cong\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{r} 2}\right]\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right]-\mathrm{V}_{\mathrm{x}} \mathrm{t} / \mathrm{L}_{\mathrm{r} 2} \tag{4-5}
\end{equation*}
$$

for time $\mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6}$. If the same assumption is applied to equ. (4-1), then it can be written as

$$
\begin{equation*}
\mathrm{i}_{\mathrm{Q1}}(\mathrm{t})=\mathrm{I}_{\mathrm{s}}-\left[\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{eq}} / \mathrm{Z}_{2} \mathrm{~L}_{\mathrm{r} 1}\right]\left[1-\cos \omega_{\mathrm{eq}} \mathrm{t}\right] \quad \text { for time } \mathrm{t}_{2}<\mathrm{t}<\mathrm{t}_{6} \tag{4-6}
\end{equation*}
$$

The time at which $\mathrm{i}_{\text {Qaux }}$ is at its minimum value, $\mathrm{T}_{\mathrm{ms} 2}$, can be determined by differentiating and simplifying equ. (4-5) with respect to time and equating it to zero

$$
\begin{equation*}
\mathrm{T}_{\mathrm{ms} 2}=\left(1 / \omega_{\mathrm{eq}}\right) \sin ^{-1}\left[-\left\{\mathrm{V}_{\mathrm{x}} /\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right)\right\} \sqrt{(1+L r 2 / L r 1)}\right] \tag{4-7}
\end{equation*}
$$

The currents in all switches at time $\mathrm{T}_{\mathrm{ms} 2}$ given by equ. (4-7) must be less than or equal to zero to achieve ZCS for all switches $Q_{1-4}$ and Qaux. By replacing the value of $T_{m s 2}$ given by equ.(4-7) in the equation for $\mathrm{i}_{\mathrm{Q} 1}$, equ. (4-1), and solving for $\mathrm{i}_{\mathrm{Q} 1}(\mathrm{t})=0$, the following condition for the ZCS turn-off of $\mathrm{Q}_{1}$ can be determined after subsequent simplifications:

$$
\begin{equation*}
\left[\mathrm{I}_{\mathrm{s}} \mathrm{Z}_{2}\left(\mathrm{~L}_{\mathrm{r} 1}+\mathrm{L}_{\mathrm{r} 2}\right) / \mathrm{L}_{\mathrm{r} 2}\right]\left[2\left(\mathrm{~V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right)-\mathrm{I}_{\mathrm{s}} \mathrm{Z}_{2}\left(\mathrm{~L}_{\mathrm{r} 1}+\mathrm{L}_{\mathrm{r} 2}\right) / \mathrm{L}_{\mathrm{r} 2}\right] \geq \mathrm{V}_{\mathrm{x}}^{2}\left(1+\mathrm{L}_{\mathrm{r} 2} / \mathrm{L}_{\mathrm{r} 1}\right) \tag{4-8}
\end{equation*}
$$

This condition can be further simplified so that a ZCS turn-off of $\mathrm{Q}_{\mathrm{I}-4}$ can be ensured if the following two simpler conditions are met

$$
\begin{align*}
& 2\left(\mathrm{~V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) \mathrm{L}_{\mathrm{r} 2} / \mathrm{I}_{\mathrm{s}} \mathrm{Z}_{2}\left(\mathrm{~L}_{\mathrm{r} 1}+\mathrm{L}_{\mathrm{r} 2}\right)>1  \tag{4-9}\\
& 2 \mathrm{I}_{\mathrm{s}} \mathrm{Z}_{2}\left(\mathrm{~V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{V}_{\mathrm{x}}^{2}>1 \tag{4-10}
\end{align*}
$$

These conditions can be met by the proper selection of the appropriate circuit component values. A similar condition for the ZCS turn-off of $\mathrm{Q}_{\mathrm{aux}}$ can be derived by substituting the value of $\mathrm{T}_{\mathrm{ms} 2}$ derived in equ. (4-7) into equ. (4-2)

$$
\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}-\left(\mathrm{V}_{\mathrm{Cr}}(0)-\mathrm{V}_{\mathrm{x}}\right) / \mathrm{Z}_{2}\left[1+\sqrt{1+\left\{V_{x}^{2} /\left(\mathrm{V}_{\mathrm{Cr}}(0)-V_{x}\right)\right\}(1+L r 2 / L r 1)}\right]<\mathrm{V}_{\mathrm{x}} / \mathrm{L}_{\mathrm{r} 2} \omega_{\mathrm{eq}}
$$

Another important factor that must be considered when designing the converter is the peak current in the auxiliary switch. When designing the auxiliary circuit, the peak current in the auxiliary switch should be reduced to decrease the stresses on the devices.

### 4.3 Characteristics of the Proposed Full-Bridge Converter

The equations for the modes of operation that were presented in Chapter 3 for the full-bridge PWM dc-dc boost converter with the proposed auxiliary circuit (Fig. 4.1) can be used to generate graphs of steady-state characteristic curves for this converter.

The graphs can be generated by a computer program such as the MATLAB program presented in Appendix A of this thesis. The key to the program is the fact
that, since it is the steady-state characteristics that are to be determined, the current and voltage of any converter component at the start of a switching cycle must be the same as that at the end of a switching cycle. If the equations derived in the previous chapter are used by the computer program to track component current and voltage values throughout a switching cycle when the converter is operating with a given set of component values, then the program can determine if the converter is operating in steady-state. Once this has been determined, then the appropriate steady-state component voltage and current values can be found. If this is done for a number of component value sets, then characteristic curves and graphs can be generated.

The characteristic graphs that are generated and shown, show the effects that changing a particular component value, such as that of a particular inductor or a capacitor, can have on converter currents and voltages. With these graphs, it then becomes possible to develop a systematic procedure for the design of the converter that would allow appropriate converter component values to be selected.

Graphs of steady-state characteristic curves are shown in Figs. 4.2-4.4. The curves were generated for the following operating condition:

Output Voltage $\mathrm{V}_{0}=300$ Volts
Output Power $P_{0}=600$ Watts
Input Voltage Vin=24Volts
Expected Efficiency $\dot{\eta}=93 \%$
Switching Frequency $=f_{s}=1 / T_{s}=50 \mathrm{kHz}$.

The design procedure that is presented is an iterative one and requires several iterations before the final design can be completed. It should be noted that only the design of the auxiliary circuit components is presented here since that of the main power circuit can be found in any standard power electronics textbook. The design of the main power transformer, however, is dependent on the PWM method used to control this converter and will be discussed in the following steps.

## Step 1: Minimize reverse recovery losses in the auxiliary diode

The duration of Mode 7 in which the input current gets diverted from the auxiliary capacitor $C_{r}$ to the inductance $L_{r l}$ should be greater than $3{ }^{*} t_{\pi}$ (reverse recovery time) for auxiliary diode. The factor $3 * t_{\text {rr }}$ is a typical duration of time needed to gradually transfer away from the diode so that the diode can stop conducting current with little, if no, reverse recovery time; this is typically 7 $3 * 80 \mathrm{~ns}=240 \mathrm{~ns}$. The expression for the commutation time $\mathrm{t}_{\mathrm{c}}$ can be found from eqn. (3-23) as:

$$
\begin{gather*}
t_{c}=\frac{\pi}{2 \omega_{1}}  \tag{4-12}\\
\text { where } \omega_{1}=\frac{1}{\sqrt{\left(L_{r 1}+L_{\mathrm{lk}}\right) C_{r}}} \tag{4-13}
\end{gather*}
$$

by combining eqns. (4-12) and (4-13), eqn. (4-14) can be written as:

$$
\begin{equation*}
\mathrm{t}_{\mathrm{c}}=\frac{\pi}{2} \sqrt{\left(\mathrm{~L}_{\mathrm{r} 1}+\mathrm{L}_{\mathrm{ik}}\right) \mathrm{C}_{\mathrm{r}}} \tag{4-14}
\end{equation*}
$$

The value for the commutation time $t_{c}$ in which the input current gets diverted from the auxiliary capacitor $C_{r}$ to the bridge section, must be greater than the value of 3trr of the auxiliary diode. So from this discussion the following relation can be derived:

$$
\begin{equation*}
3 \mathrm{t}_{\mathrm{r}}=\mathrm{t}_{\mathrm{c}}=\frac{\pi}{2} \sqrt{\left(\mathrm{~L}_{\mathrm{rl}}+\mathrm{L}_{\mathrm{ik}}\right) \mathrm{C}_{\mathrm{r}}}=240 \mathrm{nS} \tag{4-15}
\end{equation*}
$$

Eqn. (4-15) will be used along with equations derived in the following steps to determine values of $\mathrm{C}_{\mathrm{r}}$ and $\mathrm{L}_{\mathrm{r} 1}$.

## Step 2: Determine the values of $\mathrm{C}_{\mathrm{r}}$ and $\mathrm{L}_{\mathrm{r} 1}$

In this step, the values of $\mathrm{C}_{\mathrm{r}}$ and $\mathrm{L}_{\mathrm{r} 1}$ are determined. Referring to Mode7 when switches $\mathrm{Q}_{2}$ and $\mathrm{Q}_{3}$ are turned off and voltage across them builds up due to resonance between the equivalent series inductance of leakage inductance $L_{i k}$ and $L_{r l}$ and capacitor $\mathrm{C}_{\mathrm{r}}$. At the end of this mode the voltage across the switches rises to a certain peak voltage given by eqn. (3-27):

$$
\mathrm{V}_{\mathrm{Cr}}(0)=\frac{\mathrm{Vo}}{\mathrm{~N}}+\mathrm{I}_{\mathrm{in}} \mathrm{Z}_{\mathrm{l}}
$$

The value of this peak voltage across the switches, which is same as the maximum voltage across the resonant capacitor, is plotted for different values of impedance $Z_{1}$ in Fig.4.2. It can be found from this graph that by choosing a larger impedance, the voltage across $C_{r}$ will increase. If a smaller impedance is chosen, then a larger capacitor must be used for $\mathrm{C}_{\mathrm{r}}$ as there must be enough energy stored in the
capacitor at the end of this mode to force the current into the full bridge to reverse direction and create an opportunity for the ZCS turn off of switches.

By choosing a large capacitor, the resonance cycle time will increase in the circuit which in turn will increase the on-time duty ratio in the auxiliary switch and will cause more losses as the device has to be on longer. The energy in the capacitor is $\frac{1}{2} \mathrm{CV}^{2}$, so either a higher voltage can be placed across the capacitor or a bigger capacitor can be chosen. For this design, a value of $Z_{1}=1.5 \Omega$ is chosen. Using eqn. (4-13) determined in Step 2 and $Z_{1}$ given by eqn. (3-26) in this step, values of $L_{r l}$ and $\mathrm{C}_{\mathrm{r}}$ are found to be 240 nH and 360 nF by assuming $\mathrm{L}_{\mathrm{ik}}$ to be typically around 500 nH .


Fig.4.2 Variation of capacitor $C_{r}$ Peak voltage for different values of $Z_{1}$

Step 3: Determine the characteristic impedance of the auxiliary circuit and the value of $L_{r}$.

The characteristic impedance of the auxiliary circuit is defined by:

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{o}}=\sqrt{\frac{\mathrm{L}_{\mathrm{r} 2}}{\mathrm{C}_{\mathrm{r}}}} \tag{4-16}
\end{equation*}
$$

$Z_{0}$ affects the peak current stress of the auxiliary circuit components and the window of time that the main switches can be turned off with ZCS. It should also be considered that the peak current in the auxiliary switch must be greater than the bridge input current so the bridge current starts reversing and eventually reduces to zero and flow in the opposite direction through the body diodes of the bridge switches which can then be turned off with ZCS.

Low values of $Z_{o}$ result in higher values of peak current stress, but result in longer windows of time during which the main switches can be turned off with ZCS. It can be seen in Fig. 4.3 that values of $Z_{o}$ over $1.5 \Omega$ would result in low auxiliary circuit current stresses, but these values of $Z_{o}$ are unsuitable because the time window for the ZCS turn-off of the main switches would be very narrow or nonexistent. Values of $Z_{o}$ below $1.5 \Omega$ will result in very high peak current in the auxiliary switch, which will increase the losses in it. So for this design, $Z_{0}=1.5 \Omega$ is chosen which implies $\mathrm{L}_{\mathrm{r} 2}=0.9 \mu \mathrm{H}$.


Fig.4.3 Variation of Peak current in auxiliary switch for different values of $Z_{0}$

## Step 4: Determine the value of $\mathbf{N}_{\mathbf{x}}$

To determine $\mathrm{N}_{\mathrm{x}}$, the effect of the auxiliary transformer secondary voltage on the soft switching window of both auxiliary switch and bridge switches need to be considered. The primary voltage $\mathrm{V}_{\mathrm{x}}=\mathrm{V}_{0} / \mathrm{N}_{\mathrm{x}}$ across the auxiliary transformer in Modes 2-4 reduces the negative peak voltage across $\mathrm{C}_{\mathrm{r}}$ and also reduces peak current across the auxiliary switch. These two phenomena can have a detrimental effect on the ZCS window, but on the other hand they can help in reducing circulating current in the auxiliary circuit.

The characteristic graphs in Figs.4.4 and 4.5 show the effect that $V_{x}$ has on the duration and amount of negative portion of the bridge switch and auxiliary switch
current for varying values of $\mathrm{V}_{\mathrm{x}}$ with other component values decided in previous steps, during Modes 3-5. These are also the modes in which the currents in all switches reduce to zero and reverse directions following eqns. (3-19d) and (3-20b), thus creating ZCS turn off window for the switches.

From the characteristic graph in Fig.4.4, it can be seen that higher the value of $\mathrm{V}_{\mathrm{x}}$ lower is the magnitude and duration of the negative portion for the current through the bridge switches. This is expected since with higher values of $\mathrm{V}_{\mathrm{x}}$, the negative peak voltage across $C_{r}$ is reduced and thus less negative voltage appears across $\mathrm{L}_{\mathrm{rl}}$ during Modes 3-5, which reduces the duration of its negative current region. On the other hand, it can be seen that the negative part of the auxiliary current is increased with increasing values of $V_{x}$ since increasing values of $V_{x}$ will decrease the peak current in the auxiliary switch from which its current starts decreasing. When trying to choose a suitable value for $\mathrm{V}_{\mathrm{x}}$, it should be considered that greater negative switch currents will increase circulating current losses and also increase the duration of activation of the auxiliary circuit, which will also increase conduction losses in it. $\mathrm{V}_{\mathrm{x}}=24 \mathrm{~V}$ or equivalently $\mathrm{N}_{\mathrm{x}}=1: 12$ is chosen considering all these tradeoffs.


Fig.4.4 Variation of the duration in which bridge switch currents reduce to zero and go negative during Modes 3-5 for different values of $\mathrm{N}_{\mathrm{x}}$.


Fig.4.5 Variation of the duration in which bridge switch currents reduce to zero and go negative during Modes 3-5 for different values of $\mathrm{N}_{\mathrm{x}}$.

### 4.3.1 Design Example

The design of a boost converter operating with the proposed auxiliary circuit is described. For the example, the converter is to be designed according to the following specifications:

Output Voltage $\mathrm{V}_{\mathrm{o}}=300$ Volts
Output Power $\quad P_{0}=600$ Watts
Input Voltage $\mathrm{V}_{\mathrm{in}}=24$ Volts
Expected Efficiency $\dot{\eta}=93 \%$
Switching Frequency $=f_{s}=1 / T_{s}=50 \mathrm{Khz}$.

### 4.3.2 Power Circuit Design

The design procedure consists of two parts - the design of the main power circuit (a full-bridge boost converter) and the design of the auxiliary circuit. The first part of the procedure is presented in this section and the second part is presented in the next section.

### 4.3.3 Designing Input Inductor $\mathbf{L}_{\text {in }}$

For full-bridge PWM dc-dc boost converters, the value of input inductance is generally selected to limit the peak-to-peak ripple of the current flowing through the inductor. A compromise must be made when selecting a value for $\operatorname{Lin}$. If $L_{i n}$ is too large, then the peak current will be small, but the physical size of the inductor will increase significantly, and so will the size and weight of the converter. A $10 \%$ peak-
to-peak ( $\mathrm{p}-\mathrm{p}$ ) ripple to average current ratio of the input current is a compromise that is typically made and will also be made in this example. With this compromise, the boost converter is assumed to have a continuous current.

From the given specifications for the converter, the maximum average input current is

$$
\mathrm{I}_{\mathrm{in}}=\mathrm{P}_{\mathrm{o}} / \mathrm{V}_{\mathrm{in}} \eta \approx 27 \mathrm{Amps}
$$

In this case the p-p ripple of input current is

$$
\Delta \mathrm{I}=0.1 \mathrm{I}_{\mathrm{in}}=2.7 \mathrm{Amps}
$$

Rearranging the conversion ratio for the boost converter given in equation (1-2) to solve for the switch duty ratio D gives

$$
D=\left(V_{0}-V_{\text {in }}\right) / V_{0}=0.91
$$

since

$$
\begin{equation*}
\mathrm{V}_{\mathrm{Lin}}=\mathrm{Lin} \mathrm{di} / \mathrm{dt} \tag{4-17}
\end{equation*}
$$

where $\mathrm{V}_{\mathrm{Lin}}$ is the voltage across $\mathrm{L}_{\mathrm{in}}$ when switches $\mathrm{Q}_{1,4}$ or $\mathrm{Q}_{2,3}$ are on; $d t=D T_{\mathrm{S}}$ is the time for which the switch is on and $d i$ is the change in input current during that time, the value of Lin can therefore be determined by:

$$
\begin{aligned}
\operatorname{Lin} & =\mathrm{V}_{\text {in }} \mathrm{DT}_{\mathrm{S}} / \Delta \mathrm{I}=24 \text { Volts } * 0.91 * 20 \mu \mathrm{~s} / 2.7 \mathrm{Amps} \\
& =1.61 \mathrm{mH}
\end{aligned}
$$

### 4.3.4 Designing Output Capacitor $\mathbf{C o}_{\mathbf{o}}$

The minimum value of the capacitor can be determined from

$$
C_{0}>D / R_{0} f_{s}\left(\Delta V_{0} / V_{o}\right)
$$

given in [MOHAN] where $D$ is the duty ratio determined in equ.(1-1), $R_{0}$ is the output resistance at maximum load $\left(\mathrm{V}_{0}{ }^{2} / \mathrm{P}_{\mathrm{o}, \text { max }}\right)$, fs is the converter switching frequency and $\left(\Delta V_{0} / V_{0}\right)$ is the percentage of peak output voltage ripple. Substituting $\mathrm{D}=0.91, \mathrm{fs}=50 \mathrm{kHz}, \mathrm{Ro}=150 \Omega$ and $\Delta \mathrm{V}_{0} / \mathrm{V}_{0}=0.001$, Co can be found to be

$$
\mathrm{C}_{0}>\mathrm{D} / \mathrm{R}_{0} \mathrm{f}_{\mathrm{s}}\left(\Delta \mathrm{~V}_{0} / \mathrm{V}_{\mathrm{o}}\right)=0.91 /\left(150 * 50^{*} 10^{3}\right)^{*} 0.001=1.22 \mathrm{mF}
$$

In practice, the filter capacitance value is often determined by the holdup requirements of the supply, not by ripple voltage considerations. This means that starting from an initial bus voltage, the capacitor must store enough energy to maintain the output above a specified minimum voltage, $\mathrm{V}_{\min }$, after the input voltage has been absent for a specified time, typically 20 ms for worst case design. Assuming that $\mathrm{V}_{\text {min }}$ is $90 \%$ of $\mathrm{V}_{\mathrm{o}}$ and $\mathrm{T}_{\mathrm{h}}$ is the holdup time, during this holdup time, the energy transferred to the output is $\mathrm{E}=\mathrm{p}_{0}{ }^{*} \mathrm{~T}_{\mathrm{h}}$, which is also equal to the energy discharged by the capacitor is given by:

$$
\begin{equation*}
\mathrm{E}=\mathrm{C}_{0}\left(\mathrm{~V}_{\mathrm{o}}^{2}-\mathrm{V}_{\mathrm{o}, \min }^{2}\right) / 2 \tag{4-17}
\end{equation*}
$$

hence $C_{0}$ is given by:

$$
\mathrm{C}_{0}=2 * \mathrm{P}_{\mathrm{o}} * \mathrm{~T}_{h} /\left(\mathrm{V}_{\mathrm{o}}^{2}-\mathrm{V}_{\mathrm{o}, \min }^{2}\right)=2 * 600 * 0.02 /\left(300^{2}-270^{2}\right)=1.5 \mathrm{mF}
$$

### 4.3.5 Designing Main Switches $\mathbf{Q}_{1-4}$

It can be recalled from Chapterl that MOSFETs are the device of choice for low power applications and high operating frequencies, for their low cost, ruggedness, and for high switching frequencies.

The average current through the main switch is

$$
\mathrm{I}_{\mathrm{in}} * \mathrm{D}=25 * 0.91=22.75 \mathrm{Amps}
$$

The peak current flowing through the bridge is the peak current in the input inductor and it is equal to

$$
\mathrm{I}_{\mathrm{Lin}, \mathrm{pk}}=\mathrm{I}_{\mathrm{Lin}, \mathrm{avg}}+0.5 \Delta \mathrm{I}=25 \mathrm{Amps}+0.5 * 2.7 \mathrm{Amps}=26.35 \mathrm{Amps}
$$

The maximum voltage across the main switches $\mathrm{V}_{\mathrm{Q} 1-4}=75 \mathrm{Volts}$. An "IRF540" device can be selected for the main switches.

### 4.4 Auxiliary Circuit Design

During Mode 5 in which the input current gets diverted from the auxiliary capacitor Cr to the inductance Lr , must be greater than $3 \mathrm{t}_{\mathrm{rr}}$ (reverse recovery time) for auxiliary diode which is $3 * 80 \mathrm{~ns}=240 \mathrm{~ns}$.

The commutation time is calculated as $t_{c}=\frac{\pi}{2} \omega_{1}$ where $\omega_{1}=\frac{1}{\sqrt{L_{r} C_{r}}}$ and as stated $t_{c} \geq 3 t_{r r}$ so $t_{c} \geq 240 \mathrm{~ns}$

$$
\begin{equation*}
V_{c r}=L_{r} \frac{d i_{L r}}{d t}+V_{p} \tag{4-18}
\end{equation*}
$$

by solving equ.(4-18) $\quad i_{c r}(t)=I_{i n} \operatorname{Cos} \omega_{1} t=0$ so $\omega_{1} t=\frac{\pi}{2}$
and for a leakage inductance of $0.5 \mu H, L_{r 1}=0.24 \mu H$

In the design procedure $L_{r 1}=0.3 \mu H$ is taken and the rest of components will be calculated based on this value.

Fig. 4.6 helps to find out the suitable impedance for the circuit in which the minimum circulating current will be gained and ZCS for all the switches is insured.


Fig.4.6 Maximum voltage across the auxiliary capacitor vs. resonance impedance of the circuit for input voltages of 12 and 24 Volts

By choosing a larger impedance, the voltage across $\mathrm{C}_{\mathrm{r}}$ will increase and by choosing a smaller impedance, a bigger capacitor has to be used in the circuit.

By choosing a big capacitor, the resonance cycle time will increase in the circuit which in turn will increase the on-time duty ratio in the auxiliary switch and will cause more losses as the device has to be on longer. The energy in the capacitor is $\frac{1}{2} C_{r} V_{M a x}^{2}$, so there is a tradeoff of going high with the voltage or choosing a bigger capacitor.

$$
\begin{equation*}
Z_{1}=\sqrt{\frac{L_{i k}+L_{r 1}}{C_{r}}} \tag{4-19}
\end{equation*}
$$

and in this particular example $\mathrm{Z}_{1}=1.8 \Omega$ is chosen.
Knowing $\mathrm{Z}_{1}, \mathrm{~L}_{\mathrm{r} 1}$ and $\mathrm{L}_{\mathrm{ik}}$, the value of $\mathrm{C}_{\mathrm{r}}$ can be determined by solving eqn.(4-19) for $C_{r}$ and finding $C_{r}=350 \mathrm{nf}$. (In the practical experience we are using a 0.36 uf standard ac capacitor)

Fig. 4.7 shows the current in the auxiliary switch when the voltage in the capacitor has reduced to zero. To ensure ZCS in the circuit, the peak current in the switches has to be bigger than the current flowing into the bridge, so the current will flow back from the bridge and ZCS is insured.

An impedance value of about 1.5 ohms has been taken from the characteristic graph as it is very important that the peak current always be larger than the current in the bridge ( $25-30 \mathrm{Amps}$ ).


Fig.4.7 Peak current in the auxiliary switch vs. Resonance impedance

Knowing $Z_{2}=1.5 \Omega$ and $\mathrm{C}_{\mathrm{r}}=350 \mathrm{nf}, L_{r 2}$ can be found from the equation below,

$$
Z_{2}=\sqrt{\frac{L_{r 2}}{C_{r}}}=0.88 \mathrm{uH}
$$

There is also another way to confirm the value of $L_{r 2}$ calculated above and it is based on the ratio between $L_{r 2}$ and $L_{r 1}$ which can be determined from Figures 4.8(a) and 4.8(b).


Fig 4.8(a). Current flowing through the main switches for different ratios of $\mathrm{L}_{\mathrm{r} 1} / \mathrm{L}_{\mathrm{r} 2}$


Fig 4.8(b). Current flowing in the auxiliary switch for different ratios of $L_{r 1} / L_{r 2}$

In these graphs, current in the main switches and the auxiliary switch have been shown for different ratio amounts of $L_{r 1} / L_{r 2}$. A curve that ensures ZCS operation has to be chosen, whereas the ones with a huge negative peak should not be considered as this signifies high circulating current, which results in more conduction losses. By analyzing both graphs, $\mathrm{L}_{\mathrm{r} 1} / \mathrm{L}_{\mathrm{r} 2}=0.33$ looks the best choice because it has a proper negative peak current in both graphs that will ensure the ZCS operation while the peak is not so big to cause more conduction losses.

### 4.5 Simulation Results

With the values of resonant inductances, capacitance and the transformer turns ratio the converter circuit was simulated in the circuit simulator PSIM. The following figures show the simulation waveforms generated by the PSIM circuit simulator, and a table of the current and voltage of different circuit components determined by PSIM simulation results are also given. The PSIM results help in verifying the choice of all devices for the specified converter. Key simulation results can be compared with the experimental results in chapter 5.


Fig. 4.9 PSIM simulation of main switches $\mathrm{Q}_{1,4}$ currents


Fig. 4.10 PSIM simulation of Main switches $\mathrm{Q}_{2,3}$ Currents


Fig 4.11 PSIM simulation of the voltage across $\mathrm{Q}_{1}$ and $\mathrm{Q}_{4}$


Fig 4.12 PSIM simulation of the voltage across $\mathrm{Q}_{2}$ and $\mathrm{Q}_{3}$


Fig.4.13 PSIM simulation of resonant capacitor voltage


Fig.4.14 PSIM simulation of auxiliary switch current


Fig.4.15 PSIM simulation of the voltage across $Q_{\text {aux }}$


Fig.4.16 PSIM Simulation of the bridge input current $\mathrm{I}_{\text {Lrı }}$


Fig.4.17 PSIM simulation of auxiliary diode current


Fig.4.18 PSIM simulation of the auxiliary diode voltage


Fig.4.19 PSIM simulation of the auxiliary transformer secondary current


Fig.4.20 Input current in transformer T

### 4.6 Conclusion

In this chapter, the results of the mathematical analysis performed in the previous chapter on the PWM dc-dc boost converter with the proposed auxiliary circuit were used to determine the steady-state characteristics and properties of the converter. This was done by using a MATLAB program that determined steady-state auxiliary circuit voltages and current characteristics over a switching cycle for various sets of component values, and that determined the effect that individual circuit parameters had on converter operation. The results of the MATLAB program and circuit simulator PSIM were plotted as graphs, which were then used as part of a design procedure.

## Chapter 5

## Experimental Results

### 5.1 Introduction

In this chapter, results obtained from an experimental full-bridge PWM dc-dc boost prototype converter operating with the dual auxiliary circuit examined in the previous chapters of this thesis are presented. The converter was implemented with the same parameters as the ones selected in the design example of Chapter 4. Typical converter waveforms are shown as well as efficiency results. Various observations of the experimental results are stated and explanations are given.

### 5.2 Experimental Results

The feasibility of a PWM dc-dc boost converter operating with the example dual auxiliary circuit discussed in Chapters 3 and 4 was verified by an experimental Proto type that was designed according to the following specifications:

Output Power: $\mathrm{P}_{0}=600 \mathrm{~W}$
Output voltage: $\mathrm{V}_{0}=300 \mathrm{~V}$
Input Voltage: $\mathrm{V}_{\mathrm{in}}=24 \mathrm{~V}$
Switching frequency: $\mathrm{f}_{\mathrm{sw}}=50 \mathrm{kHz}$

The prototype was implemented with the parameters from the design example discussed in the previous chapter. A saturable reactor implemented with 5 turns on a Toshiba saturable core $\mathrm{L}_{\mathrm{S}}$ (SA14x8x4.5) was used to reduce possible voltage overshoots and ringing that can be caused by parasitic elements in the circuit.

The following components were used to implement the boost converter prototype with the proposed auxiliary circuit:

1) Input Inductance $\mathrm{L}_{\mathrm{in}}: 500 \mu \mathrm{H} / \mathrm{Mu} 77194 \mathrm{~A} 7$
2) Main Bridge Switches $Q_{1-4}$ : IRF540
3) Output Capacitor: $3 \mathrm{X} 360 \mu \mathrm{~F} 3316(\mathrm{M})$
4) Auxiliary Switch: IRF520IR
5) Auxiliary Diode: FR802
6) Resonant inductor $\mathrm{L}_{\mathrm{r} 1}: 300 \mathrm{nH} / 3$ Turns on 1402D 55894A2 0 core
7) Resonant Inductor $\mathrm{L}_{\mathrm{r} 2}: 900 \mathrm{nH} / 5$ Turns on 1402D 55894A2 0 core
8) Energy Feed Forward Transformer: 1:12 turns on 6832E 7753A7 core
9) Main Bridge Transformer: 1:8 turns on OF47035 core
10) Resonant Capacitor: $\mathrm{C}_{\mathrm{r}}=360 \mathrm{nF} / 222238320333$ BC Components
11) Secondary and tertiary Diodes $D_{S 1}$ and $D_{S 2}$ : GUR5H60
12) Output Diodes: HFA16PA60C


Fig.5.1 Experimental prototype boost converter circuit with the proposed Auxiliary circuit.


Fig.5.2 Main Switches $\mathrm{Q}_{1-4}$ Current and Voltage waveforms:
(V: 30V/div, I: $15 \mathrm{Amps} /$ div, t: $5 \mu \mathrm{~s} / \mathrm{div}$ )


Fig. 5.3 Current and voltage in auxiliary switch over one switching period (V: 30V/div, I: $15 \mathrm{~A} /$ div, t:2 $\mu \mathrm{s} / \mathrm{div}$ )


Fig.5.4 Gate pulses of the main and the auxiliary switches
(V: $10 \mathrm{~V} / \mathrm{div}, \mathrm{t}: 5 \mu \mathrm{~s} / \mathrm{div}$ )


Fig.5.5 Transformer Primary Voltage Waveform (V: 50V.div, t:5 $\mu \mathrm{s} / \mathrm{div}$ )


Fig.5.6 Bridge input current $\mathrm{I}_{\text {Lrl }}$ (I: $10 \mathrm{~A} / \mathrm{div}$, t: $5 \mu \mathrm{~s} /$ div)

### 5.3 Conclusion from the Experimental Results

Fig 5.2 shows typical gating signals for the main switches $\mathrm{Q}_{1-4}$. The auxiliary switch $\mathrm{Q}_{\mathrm{aux}}$ voltage and current waveforms are shown in Fig 5.3. Gate pulses of the main and auxiliary switches are exposed in Fig5.4 and respectively main transformer primary voltage waveform and the bridge input current wave form are presented in Fig. 5.5 and Fig. 5.6 when $P_{o}=600 \mathrm{~W}, V_{\text {in }}=24 \mathrm{~V}$ and $f_{\mathrm{sw}}=50 \mathrm{kHz}$. The following observations can be made from the waveforms and graphs presented in Fig. 5.2-5.6:
(i) It can be seen from Fig 5.2 that the current through main switches $Q_{1-4}$ goes negative before the switches are turned off and the voltage across the switches rises to the output voltage. The negative current that flows through switches $Q_{1-4}$ before they turn off, implies that the current through the main switches is reversed and flows to their body diodes before the switches are turned off, thus showing that the switches undergo ŻS turn off. Also during turn-on, the current through the switches does not rise sharply rather the current through the main switch rises gradually and the voltage across it is zero when the current through it is rising. This shows that the main switches are turned on with ZCS. Also neither voltage nor current of the switches has any sharp high peaks.
(ii) It can be seen from Fig. 5.3 that the current in the auxiliary switch $Q_{a u x}$ also goes negative before it is turned off and voltage develops across it. This proves that the auxiliary circuit current is able to reduce to zero and
commutate the auxiliary switch current to its body diode before the switch is turned off hence ensuring ZCS turn off of the auxiliary switch. Also another point is the gradual rise of current in the auxiliary switch when it is turned on and its voltage drops to zero thus showing almost ZCS turn on of auxiliary switch.
(iii) From the graphs of the gate pulse waveforms in Fig.5.4, it can be seen that the auxiliary switch is activated for a very short duration compared to that of a full switching cycle, before a pair of main switches are turnedoff.
(iv) It can be seen from Fig. 5.5 that the primary voltage waveform is similar to that of a conventional current fed full-bridge converter and from fig.5.6 it can be seen that the negative current flowing in $L_{r 1}$ before it stops conducting altogether is fairly small. Since this small negative current is reverse-recovery current, the fact that it is small confirms that the auxiliary circuit can help minimize it.

### 5.4 Efficiency Results

Fig 5.7 shows the efficiency comparison of the new ZCS-PWM full-bridge boost converter and the conventional hard-switching PWM full-bridge boost converter. It can be seen that the PWM boost converter with the proposed auxiliary circuit (indicated as Efficiency of ZCS converter) has a significantly better efficiency than
the conventional PWM boost converter above $35 \%$ of the full load. The efficiency of the proposed PWM boost converter is consistently about $93 \%$. The efficiency saving in ZCS- PWM in comparison with PWM hard switching is lower in low load than that in high load. The reason is that the sum of switching loss of the auxiliary and conduction loss of the auxiliary circuit is almost fixed. The fixed loss has a higher percentage in lower load than in higher load.

The efficiency improves because there is no turn-on or turn off switching losses of the main switches and also there is energy feed forward from the auxiliary circuit to the output. Normally, those two losses account for most of the switching loss of the conventional hard-switching PWM boost converter. Due to the ZCS turn-on and turn-off of the auxiliary switch, only minimal conduction losses that is introduced by the auxiliary switch is more than overcome by reduced switching losses and energy feed forward from the auxiliary circuit. On the other hand, the reverse recovery current is dramatically reduced by the auxiliary circuit, which also contributes in the efficiency improvement.


Fig.5.7. Efficiency measurements for the proposed converter and the conventional hard switching converter with 24 V input and varying output load.

### 5.5 Conclusion

Experimental results confirming the feasibility of the proposed auxiliary circuit in a PWM full-bridge DC-DC boost converter were presented in this chapter. It was shown that the main converter switches and the auxiliary switch can operate with a ZCS turn-on and turn-off.

The efficiency of the converter operating with the proposed auxiliary circuit was compared to that of converter with no auxiliary circuit, which shows an increase of around $8 \%$ of overall maximum efficiency and hence justifies the use of such an auxiliary circuit in a DC-DC converter.

## Chapter 6

## Conclusion of the Thesis

### 6.1 Introduction

In this chapter, the contents of the thesis are summarized, the conclusions that have been reached as a result of the work performed in thesis are presented, and the main contributions of the thesis are stated. The chapter concludes by suggesting potential future research that can be done based on the thesis work.

### 6.2 Summary

The objective of this thesis was to propose, analyze, design, implement, and experimentally confirm the operation of a new ZCS-PWM dc-dc full-bridge boost converter that does not have the drawbacks of previously proposed circuits of the same type. In this thesis, the general operating principles of the converter were reviewed, and the converter's operation was discussed in detail and then analyzed mathematically. As a result of the mathematical analysis, key voltage and current equations that described the operation of the auxiliary circuit and other converter devices were derived. The steady state equations of each mode of operation were used as the basis of a MATLAB program that was used to generate steady-state characteristic curves that showed the effect that individual circuit parameters had on the operation of proposed auxiliary circuit and the boost converter.

Observations as to their steady-state characteristics were made and the curves were used as part of a design procedure to select the components of the converter, especially those of the auxiliary circuit. An experimental full-bridge PWM dc-dc boost converter prototype was built based on the converter design and typical waveforms were presented. The efficiency of the proposed converter operating with the auxiliary circuit was compared to that of a standard PWM dc-dc full-bridge boost converter and the increased efficiency of the proposed converter was confirmed.

### 6.3 Conclusion

The following conclusions can be made based on the results of this thesis:
(i) The efficiency of a PWM dc-dc full-bridge boost converter can be improved with the implementation of an auxiliary circuit that allows the converter switches to operate with ZCS.
(ii) It is possible to do so with fewer voltage and current component stresses than those found in other previously proposed ZCS dc-dc full-bridge converters.
(iii) The auxiliary circuit has several properties that should be considered when designing it to be implemented in the proposed converter, including the following

- The value of $C_{r}, L_{r l}$ and the maximum input current can be used to fix the maximum voltage across the bridge switches, which is an unique property of the auxiliary circuit.
- Higher the value of $\mathrm{C}_{\mathrm{r}}$, lower will be the peak voltage across the bridge devices for a given value of maximum load current and $L_{r l}$.
- For $\mathrm{L}_{\mathrm{r} 2}$ and the auxiliary turns ratio of the transformer, higher the values of these components, lower will be maximum current stress on the auxiliary circuit.
- Higher values of $C_{r}, L_{r 1}$ and $L_{r 2}$ will increase the total activation time of the auxiliary circuit and the auxiliary switch, which is detrimental as this will increase conduction losses in the auxiliary circuit.

As a result of these properties, a number of trade-offs need to be considered while choosing these components as discussed in the thesis.

### 6.4 Contributions

The principal contributions of this thesis are as follows:
(i) A new ZCS-PWM dc-dc full-bridge boost converter was proposed and its operation was explained.
(ii) The steady-state operation of the new converter was analyzed and a procedure for its design was derived. Based on the analysis and the design procedure, the general properties of the converter were established and were explained.
(iii) The feasibility and the properties of the new converter were experimentally confirmed by the implementation of a prototype. It was also confirmed that the
proposed converter is in fact more efficient that the conventional PWM dc-dc full-bridge boost converter for mid to full load conditions.

### 6.5 Proposal for Future Work

The following suggestions are made for future work:
(i) Single-switch PWM boost converters are widely used as ac-dc converters to improve input power factor. These converters take input ac voltage (usually typically from the utility) and convert it to a dc voltage, while simultaneously shaping the input current so that it is sinusoidal and in phase with the input voltage. Such a current maximizes the use of power from the utility and the act of shaping the current by using a boost converter is called power factor correction (PFC) in the literature. Since the proposed converter is a boost-type converter, it can be used as an ac-dc PFC converter and research can be done to see how well the proposed converter can operate in this particular application.
(ii) The proposed converter is a dc-dc converter with a large inductor connected to its full-bridge. As such, it can be considered to be a current source converter. Another type of current source converter that is widely used is a current source inverter or dc-ac converter. Given that the switches in an inverter operate differently than those of a dc-dc full-bridge converter and with higher voltages and currents, research can be done to see how the proposed converter can be adapted for use as a current source inverter.
(iii)The switches that were used in the proposed converter were low voltage MOSFETs. Research can be done to see how the converter would operate if it were implemented with other semiconductor devices with higher voltage and current ratings as switches such as thyristors, given the different properties of these devices.

## Appendix:

1) MATLAB program for generating Characteristic Graphs in Fig.4.5 and Fig.4.6:
clc
clear all
$\mathrm{V}=40$;
$\mathrm{Lr} 1=0.000013$;
$\mathrm{Lr} 2=0.000009$;
$\mathrm{Z}=17$;
$\mathrm{Cr}=\mathrm{Lr} 2 /\left(\mathrm{Z}^{\wedge} 2\right)$;
$\mathrm{w} 2=\operatorname{sqrt}(1 /(\mathrm{Lr} 2 * \mathrm{Cr})$ );
$\mathrm{L}=\mathrm{Lr} 1 * \mathrm{Lr} 2 /(\mathrm{Lr} 1+\mathrm{Lr} 2)$;
$\mathrm{w}=\mathrm{sqrt}(1 /(\mathrm{L} * \mathrm{Cr}))$;
$\mathrm{Z}=\mathrm{sqrt}(\mathrm{Lr} 2 / \mathrm{Cr})$;
$\mathrm{X}=(\mathrm{w} 2)^{\wedge} 2$;
$\mathrm{Y}=\mathrm{w}^{\wedge} 2$;
$\mathrm{i}=1$;
$t=0: 0.00000005: 0.0000018$;
$\mathrm{Il}=(400-\mathrm{V}) / \mathrm{Z}-((400-\mathrm{V}) / \mathrm{Z}) *(\mathrm{~L} / \mathrm{Lr} 2)^{*}\left(1-\cos \left(\mathrm{w}^{*} \mathrm{t}\right)\right)+\mathrm{V}^{*}\left(\mathrm{X} /\left(\mathrm{Y}^{*} \mathrm{Lr} 2\right)\right)^{*}(\mathrm{t}-$
$\left.\left(\sin \left(\mathrm{w}^{*} \mathrm{t}\right)\right) / \mathrm{w}\right)-\mathrm{V}^{*} \mathrm{t} / \operatorname{Lr} 2$
$\mathrm{L} 2=10.5-((400-\mathrm{V}) / \mathrm{Z})^{*}(\mathrm{~L} / \mathrm{Lr} 1)^{*}\left(1-\cos \left(\mathrm{w}^{*} \mathrm{t}\right)\right)+\mathrm{V}^{*}\left(\mathrm{X} /\left(\mathrm{Y}^{*} \operatorname{Lr} 1\right)\right)^{*}\left(\mathrm{t}-\left(\sin \left(\mathrm{w}^{*} \mathrm{t}\right)\right) / \mathrm{w}\right)$
plot(t , I1,'b-')
hold on
plot(t,I2,'r')
grid on
xlabel('time')
ylabel('Current')
hold on
2) MATLAB program for generating Characteristic Graphs in Fig.4.3:
```
clc
    clear all
    V=80;
    i=1;
    j=1;
    for Lr = 0.000005:0.000001:0.000020
        LR(i)=Lr;
        i=i+1;
    end
    for }\textrm{Cr}=0.000000001:0.000000005:0.0000000
        CR(j)=Cr;
        Zo(j)= sqrt(LR(j)/Cr);
        Ip(j) = (400-V)/sqrt(LR(j)/CR(j));
        j=j+1;
    end
a=[Zo', Ip']
plot(Zo', Ip')
grid on
xlabel('Imp')
ylabel('Current')
hold on
```

3)MATLAB program for generating Characteristic Graphs in Fig.4.2:

```
clc
    clear all
    V=35;
    i=1;
    j=1;
    for Lr2 = 0.000001:0.000001:0.000010
        LR2(i)=Lr2;
        i=i+1;
    end
    for Lr1 = 0.000010:0.000001:0.000020
        LR1(j)=Lr1;
        r(j)= Lr2/Lrl;
        Ip(j)=(400-V)/sqrt(1+r(j))+400-V/(1+r(j));
        j=j+1;
    end
a=[r', Ip']
plot(r', Ip')
grid on
xlabel('Ratio of Lr2 and Lr1')
ylabel('Maximum Voltage across D1')
hold on
```


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