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Extreme structure and spontaneous lift of spin degeneracy in doped perforated bilayer graphenes



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ABSTRACT

Extreme structure and spin states of doped and undoped perforated bigraphenes was studied using DFT simulations. It was found that folded nanopores possess extremely high curvature of 0.34 Å^{-1} . Dramatic structural deformation causes severe changes of the chemical properties of carbon atoms localized at the nanopores converting the folded edges to local oxidative fragments. It was found that asymmetrical coordination of either Li, Ca, or Al to the nanopores is coupled with electron transfer from metal to edge carbon atoms and breakdown of local inversion symmetry. Li-, Ca-, and Al-doped perforated AA bigraphene revealed ferromagnetic spin ordering with magnetic moments of 0.38, 0.14, and 0.32µ_B/unit cell, respectively, and spin polarization energy gain of 0.037eV for Ca-doped superlattice. It was shown that ferromagnetic spin ordering of bigraphene nanopores contradicts to the Nagaoka's theorem, which excludes strong electron correlations as a reason of spin polarization. Spontaneous lift of spin degeneracy was interpreted in terms of perturbing intense local electrostatic fields from extra electron charges localized at the nanopore edges, coupled with breakdown of space inversion and local translation invariances. It was shown that spin energy splitting is proportional to the matrix elements calculated on Bloch states with opposite wavevectors and perturbing electrostatic fields.

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1. Introduction

Lift of spin-degeneracy in low-dimensional crystalline lattices and heterostructures is a fundamental challenge in condensed matter physics [1]. Recent finding of magnetism in atomically thin van der Waals low-dimensional materials and heterostructures [2,3] attracts an increasing interest in the investigation of magnetic phenomena at the nanoscale [4]. Standalone, real-space, interfacelocalized 2D electronic gas superlattice was experimentally observed [5] in a vertically stacked Bi₂Se₃/TMD (TMD = MoS₂, MoSe₂, WS₂, MoSe₂) 2D heterostructures. It was found that regular patterns of the electron gas are driven by interlayer potentials

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determined by Moiré atomic superlattices. A discovery of spinphoton interactions in heterostructures based on InAs quantum dots adjusted with GaNAs spin filter paves the way for remote spin encoding and writing of quantum memory as well as for remote spin control of spin-photon interfaces [6].

At the dawn of the study of magnetism at microscopic scale, Heisenberg [7] concluded that ferromagnetism could not exist in compounds consisting only of light elements. Nevertheless, later a soft ferromagnetism in charge-transfer salt (tetrakisdimethylaminoethylene)C₆₀ [(TDAE)C₆₀] was detected without remanence with atypical behavior of temperature dependence of the magnetization below Curie temperature Tc = 16.1 K ([8] and many other publications). The [(TDAE)C₆₀] lattice merohedral disorder gives rise to a distribution of π -electron exchange interactions between spins on neighboring C₆₀ molecules, originated due to charge transfer of N*p*electrons from TDAE fragments, suggesting a microscopic origin for the observed spinglass behavior of the magnetic state [9]. Ferromagnetism was also discovered in C_{60} polymers like 2D rhombohedral C_{60} polymer [10] which demonstrates typical ferromagnetism with saturation magnetization and large hysteresis. The temperature dependences of its saturation and remanent magnetization indicate a Curie temperature near 500 K. The ferromagnetism of all mentioned materials is realized based on the spin-ordering of regular *p*-derived carbon states.

A challenging 2D material based on superlattices of potential bumps (so-called quantum antidots) driven by folded holes in bilayer graphene (nanoporus bigraphene, NPBG) was theoretically predicted [11,12] and later obtained experimentally by either electron or ion bombardment [13-15] or by fabrication of largearea, sub-10 nm single- and bilayer graphene nanomeshes from block copolymer self-assembly [16]. Nanoporous bigraphene was studied using DFT technique by considering nanomesh lattices with different periodic arrangements [11]. It was found that the nanopores edge types cause specific bonding and hole shape formation, e.g. zig-zag edges form a closed structure with regular threefold coordination. The NPBG electronic properties are determined by the nanopores allowing one to fabricate materials with challenging band structures. Similar twisted NPBG with fused nanopores was recently proposed and theoretically studied as well [17]. It was found that proposed superlattices are stable and demonstrate various challenging electronic properties.

Bigraphene is a very promising material consisting of two graphene sheets stacked to each other either in AA or AB sequences [12]. Like in graphite, in-plane C–C bonding is realized via σ - and π -carbon-carbon bonds while weak van der Waals interactions of neighboring graphene sheets are responsible for out-of-plane bonding [18]. In particular, it was shown [18] that electronic structure of bigraphene is slightly different from the electronic structure of single layered graphene [19] and it can be considered as zero-gap semiconductor even having small band overlap (1.6 meV) [20].

A bigraphene piece of a precisely controlled alignment can be fabricated by "tear and stack" technique [21-24] by exfoliation of graphene flakes with consequent rotation and stacking on each other at arbitrary angles to achieve desirable mutual arrangement. Either electron or ion bombardment [13-15] can be used to create the holes in graphene fragments with consequent fusion of the hole edges to stabilize the lattice by saturation of the dangling bonds at opposite graphene flakes.

Nanoporous materials (NPM) and heterostructures based on NPMs with various atoms adsorbed at the pores are of great interest to design quantum materials, catalysts etc. [25,26]. Pristine and doped nanoporous bigraphene maybe a promising nanomaterial to lift spin degeneracy in 2D quantum materials due to extreme curvature of polarized pores and strong anisotropy of the potential perpendicular to its main plane. One can speculate that making nanopores in bilayer graphene is a promising way to gain extreme local electric fields at the nanoscale through record curvature of the nanopores.

In this study, a novel type of hybrid low-dimensional materials based on AA and AB nanoporous bigraphenes doped by light (Li, Ca, Al) *sp*-metals was theoretically proposed and studied using nonrelativistic Density Functional Theory. It was found that fusion of the dangling bonds at the nanopore edges leads to formation of structural features of extremely high curvature up to 0.34 Å⁻¹ with unique electronegativity properties. Adsorption of *sp*-metal atoms leads to their oxidation by carbon lattice with charge transfer to strongly distorted carbon-carbon bonds of complex nature which form fused edges of the nanopores. The electronic structure calculations revealed spontaneous spin polarization of the carbon atoms at the nanopore edges of Li, Ca, and Al doped nanoporus bigraphene of AA morphology with 0.38, 0.14, and 0.32 μ_B /unit cell, respectively with energy splitting between ferromagnetic and diamagnetic states for Ca-doped AA NPBG equal to 0.037 eV. Relativistic spin-orbital coupling and artificial spin contamination were ruled out as possible sources of spin-polarization by the composition of lattices with only light sp-elements and negligible spin-contamination errors. Using Nagaoka's theorem analysis, it was shown that electron correlation effects cannot be responsible for ferromagnetic spin ordering in doped nanoporous bigraphene lattices for either strong or weak repulsive potentials and all possible numbers of doping electrons. A new non-relativistic mechanism of lift of spin degeneracy by perturbing intense local electrostatic fields coupled with disruption of local space inversion and translation invariances was proposed based on symmetry analysis and perturbation theory. It was shown that combination of extra electronic charge with extremely high curvature of the nanopore edges generates Intense Local Electrostatic Fields (ILEF) inside the pores coupled with breakdown of local space inversion (SII) and translation invariances (TI) due to asymmetrical adsorption of metal ions. It was found that in terms of perturbation theory the spin splitting energy is proportional to the matrix elements of perturbed non-SII and non-TI electric field operator sandwiched by s_u, k and $|-k, s_u$ Bloch states.

The atomistic models of the lattices were developed to rule out the electronic correlation effects and the relativistic spin-orbital coupling from multi-level theoretical consideration. After Computation section, the results of DFT simulations of proposed pristine and doped NPBG lattices are presented coupled with an analysis of possible spin-contamination of spin-polarized electronic wave functions. Using the Nagaoka theorem analysis of the electronic structure of the AA NPBG pore core the strong electron correlations were ruled out as a reason of ferromagnetic spin polarization of *sp*metal doped AA NPBG lattices. Symmetry analysis and perturbation approach were used to introduce the non-relativistic spin-orbital coupling terms and to interpret spin polarization of the lattices in terms of perturbing Intense Local Electrostatic Fields.

2. Computational details

All electronic structure calculations of low-dimensional crystalline lattices were performed using Vienna Ab-initio Simulation Package (VASP) [27-29] within Density Functional Theory (DFT) [30,31] and Periodic Boundary Conditions (PBC) framework. Plane wave basis set with projector augmented wave (PAW) method [32,33], GGA-PBE [34] functional and Grimme correction [35] for van-der-Waals interaction were used in the study. Mönkhorst-Pack Brillouin zone *k*-point sampling was implemented, and the *k*-point mesh contained $3 \times 3 \times 1$ *k*-points along *a*, *b* and *c* directions, respectively, was used for NPBG optimization. For DOS calculations $6 \times 6 \times 1$ *k*-point mesh was used. Non-collinear calculations were carried out using spin-orbital coupling (SOC) to determine electron spin orientation in metal-doped nanoporous bigraphene. A vacuum interval of 20 Å was set normal to the plane to avoid artificial interactions between adjacent unit cell images. In all calculations the cutoff energy was equal to 520 eV. During optimization procedure the maximum force acting on atoms less than 0.001 eV/Å was used as a stopping criterion for structural minimization. The atomic and electronic structure of C₃₆H₂₄ cluster was studied using *ab initio* B3LYP DFT potential [36–38] with 6–31G* basis set [39,40] to analyze the electronic structure of model AA nanoporous bigraphene core.

3. Results and discussion

3.1. Electronic structure of pristine and doped nanoporous bigraphene

The unit cell optimization for both 2D AA and AB bigraphene configurations was performed for perfect hexagonal cells (a = b = 2.45 Å, c = 20.00 Å) and then for bigraphene with double vacancies using $6 \times 6 \times 1$ supercells (Fig. 1 and S1). The pore etching was made by elimination of 6 carbon dimers with further structural optimization (Fig. 2). Energetic and structural characteristics of NPBGs are presented in Table 1. It was found that both AA and AB NPBGs are non-spin-polarized materials with slightly different cell parameters and very large energy difference (35.41eV) between the conformers caused by significant differences in the structure of the nanopores and resulting structural stress.

Both nanopores comprise 6 eight-member rings which share common carbon-carbon bonds either all parallel (AA type) or inclined (AB type) to the main nanopore axis (Fig. 2). The AA and AB nanopore cores are highly symmetrical and belong to either D_{6h} or D_{3d} symmetry groups, respectively. The AA and AB nanopore internal curvatures were estimated by the best fitting of both cross sections (8 points each) by forth order polynomial and it was found that they are equal to 0.336 Å⁻¹ and 0.070 Å⁻¹, respectively.

The mutual graphene layer orientation has a crucial impact on electronic properties of NPBG, i.e. NPBG(AA) possess semiconducting properties with 0.65 eV band gap while NPBG(AB) is a metal (Fig. 3). The pores drastically change the bigraphene DOS completely eliminating electronic density at the Fermi level which is attributed to the Dirac cones of pristine graphene and bigraphene and converting perfect bigraphene from semimetallic either to narrow band gap semiconducting NPBG(AA) or metallic NPBG(AB).

To enhance the polarization effects of NPBG nanopores by extra charges and to ruled out the relativistic spin-orbital coupling which is important for *d*- and *f*-elements, the pores were doped by either Li (Fig. 4a), Ca (Fig. 4b), or Al (Fig. S2) atoms which provide additional 1, 2, or 3 electrons of *s*- $({}^{2}S_{\frac{1}{2}}$ Li, ${}^{1}S_{0}$ Ca) or *s*- and *p*-nature $({}^{2}P_{\frac{1}{2}}$ Al), respectively, to strongly distorted carbon-carbon bonds at the

NPBG(AA) Double pore fragment

NPBG(AB) Double pore fragment



Fig. 1. Top: Three projections of a fragment of 2D AA nanoporus bigraphene with two pores. Two D_{6h} pores are connected through ellipse-shaped channel. Bottom: Three projections of a fragment of 2D AB nanoporus bigraphene with two D_{3d} pores connected through ellipse-shaped channel.



Fig. 2. Left: Three projections of detailed atomic structure of the central core of a pore in AA-stacked bigraphene. The core of AA pore of D_{6h} symmetry consists of 6 equivalent buckled octagonal carbon rings, fused by common carbon-carbon bonds, parallel to the main axis of the nanopore. Right: Three projections of atomic structure of the central core of a pore in AB-stacked bigraphene. The pore of D_{3d} symmetry consists of 6 equivalent deformed octagonal carbon rings, fused by common carbon-carbon bonds with opposite fragments mutually oriented in opposite directions. Fused C–C bonds are inclined in respect to the main axis of AB pore.

Table 1

The energy difference ΔE	(eV), the structural parameters (Å), band gap values (eV)
and edge curvatures (Å-1) of AA and AB NPBGs.

Туре	ΔE, eV	a, Å	Band gap, eV	Edge curvature, Å $^{-1}$
AA	35.41	14.74	0.53	0.336
AB	0.00	14.75	metal	0.070



Fig. 3. Total density of states of NPBG in AA (top) and AB (bottom) stacking sequences.

nanopore edges. It is worth to note that for light elements like Li, C, Ca, and Al, spin is a good quantum number because of negligibly small corresponding spin-orbital coupling constants. The polarization effects in hybrid Me@NPBG (M = Li, Ca, Al) lattices can be enhanced by opposing the extra electronic charges by Li⁺, Ca²⁺, or Al³⁺ counterions as well as combined with possible elimination of local symmetry caused by asymmetrical coordination of metal ions.

Structural parameters, magnetic moments and band gap values of all Me@NPBGs calculated at PBC PAW PBE level of theory are presented in Table 2. Because of relatively small deviation of Li⁺ and Al^{+3} positions from the AA pore centers, the C–Me bond length were averaged as arithmetic mean among the interatomic distances inside the pores. Electronic structure calculations revealed asymmetrical positions of Li⁺, Ca²⁺, or Al³⁺ ions inside the NPBG(AA) pores, which effectively eliminate local symmetry of doped nanopores.

In Me@NPBG(AA) Li⁺ and Al⁺³ ions are localized rather close to the center of the pores with average Li–C and Al–C distances equal to 3.252 and 3.263 Å, respectively (Table 2), which is much longer than corresponding bond length in Li₂C₂ (2.212 and 2.402 Å [41] and Al₄C₃ (1.898, 1.944, 2.170, and 2.223 Å [42]) carbides. In contrast to Li⁺ and Al⁺³, the Ca⁺² (Fig. 4b) occupies very asymmetric position with shortest/longest Ca–C bonds equal to 2.583/3.797 Å, both of each much longer the Ca–C bond in CaC₂ of 2.421 Å [43].

In contrast to ÅA conformers, Li⁺ and Al⁺³ ions inside the pores of Me@NPBG(AB) are localized very asymmetrically with much closer positions to one of external nanopore edge. In fact, both ions are coordinated not to 12 (AA case), but rather to two carbon atoms to the same (Li⁺) or opposite (Al⁺³) nanopore edges. Ca²⁺ ion in NPBG(AB), reveals almost symmetrical coordination rather close to the center the pore with shortest/longest Ca–C bonds equal to 2.825/3.217 Å.

Doping of both NPBG(AA) and NPBG(AB) by either Li, Ca, or Al causes electronic transfer of one, two or three extra electrons from metal 2*s* (Li), 3*s* (Ca, Al) and 3*s*, 3*p* (Al) orbitals to 6 (in case of Li and Al) or just 1 (Ca@NPBG(AA)) π -states localized at C–C bonds which form the inner core of the nanopores (Fig. 5 and S2), making the pores strongly electrically polarized. It is necessary to note that artificial small delocalized charge transfer to the edges of bigraphene unit cell is caused by slight misalignment (0.02 Å, Table 2) of Ca@NPBG(AA) and NPBG(AA) lattices used to calculate charge transfer distribution.

The induced magnetic moments per unit cells (0.38, 0.14, and 0.32 μ_B for Li@NPBG(AA), Ca@NPBG(AA) and Al@NPBG(AA), respectively (Table 2), demonstrate the direct impact of structure and symmetry of the pores on the spin states of the Me@NPBGs. In particular, either highly symmetrical D_{6h} or D_{3d} AA and AB undoped conformers do not reveal any magnetic moments. Distorted atomic structure and extremely high curvature of both types of nanopores leads to oxidation of metal atoms with electron transfer to 6 (Li@NPBG(AA) and Al@NPBG(AA) or 1 (Ca@NPBG(AA) C–C bonds,



Fig. 4. a) Top and side views of Li@NPBG in AA stacking sequence. b) Top and side views of Ca@NPBG in AA stacking sequence. Carbon atoms are denoted in brown, Li⁺, and Ca⁺² ions are denoted in green, and blue. (A colour version of this figure can be viewed online.)

Table 2

C-Me bond lengths (Å), magnetic moments (μ_B) per unit cell, unit cell parameters (Å), and curvature of the nanopore edges (Å⁻¹) of Me@NPBG heterostructures. In the case of AA conformers averaged values are presented. In the case of AB-heterostructures the C-Me bond length for carbon atoms which belong to different carbon layers are separated by slash.

Ion	Туре	C–Me bond length, Å	Magnetic moment, μ_B	Unit cell parameter a, Å	Curvature Å ⁻¹
Li	AA	3.252	0.38	14.74	0.336
	AB	2.417, 2.438-3.010/2.985-3.422	0.00	14.75	0.070
Ca	AA	2.583/3.797	0.14	14.72	0.336
	AB	2.825/3.217	0.00	14.72	0.070
Al	AA	3.263	0.32	14.73	0.336
	AB	2.108-3.583/2.195-3.64	0.00	14.73	0.070



Fig. 5. Charge transfer from Li, and Ca to carbon core of NPBG(AA). Negative charge transfer is depicted in cyan, positive charge transfer is depicted in yellow. Artificial small delocalized charge transfer to the edges of bigraphene unit cell in case of Ca@NPBG(AA) is caused by slight misalignment of Ca@NPBG(AA) and NPBG(AA) lattices. (A colour version of this figure can be viewed online.)

which form the inner pore structures (Fig. 2). Generated intense local electrostatic field at the nanopore is induced by extreme curvature of 0.336 Å⁻¹ of the pores combined with extra electronic charge and opposed Li⁺, Ca²⁺, or Al³⁺ counterions.

Small curvature radii ($R_{AA} = 2.98$ Å and $R_{AB} = 14.29$ Å) of both folded NPBG nanopores is a source of extreme local electric fields:

$$V = ze_{/R} \tag{1}$$

where *ze* is electronic charge, localized at nanopore folded edges and *R* is curvature radius, which promotes enhanced chemi- and physisorption [13,14]. The curvature of sp^2 lattice leads to enhanced electronegativity of the carbon atoms and oxidation of dopant



Fig. 6. Spatial spin density distribution (top and side views) of Li@NPBG(AA) (top); Ca@NPBG(AA) (in the middle); and Al@NPBG(AA) (bottom). Spin-up density is depicted in yellow, and spin-down one is depicted in cyan. Carbon atoms are denoted in brown. (A colour version of this figure can be viewed online.)

metal atoms [44]. Positive and negative charges localized at the nanopores combined with extreme local curvature is a source of intense local electrostatic fields. Combination of ILEF with broken inversion and translation invariances [45] may generate spin energy splitting up to 0.1 eV for light elements like Ne atom [46–48].

To estimate the energy splitting between ferromagnetic and diamagnetic states and to exclude the influence of odd number of electrons per unit cell, the total energies of FM spin-ordered and diamagnetic unpolarized states of Ca@NPBG(AA) were calculated. It was found that Ca@NPBG(AA) diamagnetic state is higher in energy the FM one by 0.037 eV.

Following approximate spin projection (AP) scheme [49-52] the spin contamination error (SCE) is proportional to the energy difference between high- and low-spin states (see, for example [51]). The AP approach was successfully implemented in VASP [27–29] and used for unrestricted PW DFT PBC geometry optimization of correlated crystals like NiO and MnO [52] for which it was found that SCE corrections should be taken into account during structural optimization. In contrast to heavy elements like Mn and Ni, SCEs for the systems composed only by the light elements were found to be negligible [52]. For example, for H₂ dimer the SCE [52]

was found to be 0.027 eV, which is very close to SCE for Ca@N-PBG(AA) (0.037 eV). It is necessary to note that both Li and Al are light atoms which have doublet ground state for which the SCE is equal to 0 by definition since the high- and low-spin states are just equivalent to each other. Summarizing, for all considered Me@NPBG(AA) heterostructures the spin contamination of ferromagnetically ordered states is negligibly small and can be ruled out as a source of artificial spin polarization.

It is clearly seen (Fig. 6) that all Me@NPBG(AA) demonstrate significant spatial lift of spin degeneracy, i.e. the electrons with spin-up (yellow color) are localized differently in comparison with spin-down ones (in cyan). The direction of spin alignment was calculated using SOC and it was found to be parallel to *z*-direction. The Me@NPBG(AB) reveal no magnetic moments which excludes the spin polarization of 2D materials which can be attributed to much smaller AB nanopore curvature equal to 0.070 Å⁻¹ (Table 2).

Densities of states calculated for Me@NPBG(AA) demonstrate dramatic impact of Me electronic states on TDOS at the Fermi level, effectively converting semiconducting NPBG(AA) to metallic state (Fig. 7) by 0.4 eV energy shift. Partial density of states of Li, Ca and Al ions at the vicinity of the Fermi level is almost equal to 0, which



Fig. 7. The densities of states of Li@NPBG(AA) (top), Ca@NPBG(AA) (middle), and Al@NPBG(AA) (bottom). Total densities (TDOS) are depicted in black, and partial densities of Li, Ca, Al (PDOS) are depicted in red. Spin-up DOSes are depicted with positive sign, spin-down DOSes are depicted with negative sign. (A colour version of this figure can be viewed online.)

directly indicate perfect +1, +2, and +3 oxidative states of the ions.

The electronic properties of Me@NPBG(AB) remain the same as for NPBG(AB) and the impact of *sp*-metal doping is not observed, possessing metallic properties with absence of spin-polarization. For all cases Li, Ca, or Al PDOS intensities in the vicinity of Fermi level are close to zero with minor impact on TDOS shape (Fig. S3).

The most reasonable way to synthesize NPBG is ion bombardment followed by treatment of the samples under high pressure, which should lead to formation of irregular fused nanopores. Consequent metal doping of the nanoporous bigraphene should lift spin degeneracy with formation of irregular paramagnetic 2D material rather than ferromagnetic lattice of spin centers due to the stochastic nature of nanopores fabricated by ion treatment.

3.2. Spin ordering and Nagaoka's theorem

Let's consider Nagaoka's theorem [53] to take into account the effect of strong electron correlations on the spin states of hexagonal NPBG(AA) (Figs. 1, 2, S1) and Me@NPBG(AA)s (Fig. 4) lattices. Symmetry analysis and *ab initio* B3LYP/6-31G* calculations of D_{6h} symmetry C₃₆H₂₄ cluster (Fig. 8), which represents the core structure of NPBG(AA), revealed B_{1g} LUMO and E_{2u} LUMO+1 states, with LUMO – LUMO+1 gap $E_b = 0.92$ eV. In total, both two-fold degenerate B_{1g} and four-fold degenerate E_{2u} states provide 6 vacancies to accept doping electrons from metal atoms. To consider half-filled band Nagaoka's model, the NPBG(AA) nanopore is equivalent to 3 vacant double-degenerate states to accept doping electrons, its ground state can be considered as a vacuum state without any correlation effects which may cause spin polarization of the lattice.

According to Nagaoka's theorem, for the case of sufficiently strong repulsive potential *U*, *hcp* lattice, and $N_e > N$, where N_e is a number of electrons and *N* is the number of states to be filled by 2 *N* electrons, the maximum spin state is the ground state of the system, and it is not the ground state for $N_e \le N$. For the case of NPBG(AA) with N = 3 and $N_e = 1, 2$, and 3 for Li-, Ca-, and Al-doped NPBG(AA)s, the ferromagnetically-ordered state cannot be the ground state of either Li@NPBG(AA), Ca@NPBG(AA), or



Atomic and electronic structure of $C_{36}H_{24}$ cluster

Fig. 8. Atomic and electronic structure of $C_{36}H_{24}$ cluster of D_{6h} symmetry. Carbon atoms are presented in black and hydrogen atoms are presented in red. Spin up/spin down electrons are presented by up/down arrows. At B3LYP/6-31G* level of theory the LUMO B_{1g} – LUMO+1 E_{2u} gap E_b = 0.92 eV. The HOMO-LUMO gap Δ HOMO-LUMO = 2.30 eV. (A colour version of this figure can be viewed online.)

Al@NPBG(AA) lattices.

Let's consider the case with $N_e > N$. The trivial case of $N_e = 6$ is equivalent to vacuum state, so it must be diamagnetic. Let's estimate repulsive potential U for $N_e = 4$, and 5. According to Nagaoka's theorem, for *hcp* lattice, and $U < E_b \times N_{/|N - N_e|}$, where E_b is the bandwidth, the ferromagnetically ordered spin state is not the ground state of the system. So, for $E_b = 0.92$ eV and $N_e = 4$ U = 2.8 eV, and for $N_e = 5$ U = 1.4. eV. Both values are of the same order of magnitude the U values for the first transition metal atoms V (3.1 eV), Co (3.3 eV), and Cr (3.5 eV) [54]. It is worth to note that U values for light sp-elements (H, Li, C, Ca, Al) are equal to 0. So, according to Nagaoka's theorem, for either sufficiently strong or weak (U < 1.4 eV) repulsive potentials, for all possible occupation numbers $N_e = 1-5$ electrons, the FM state is not a ground state for doped hcp NPBG(AA) lattice, which unequivocally excludes correlation effects as the main reason of spin polarization of *sp*-metal doped nanoporous bigraphene.

3.3. Symmetry analysis and perturbation theory consideration

Let's consider a low-dimensional crystalline lattice which lacks the SII conditions. Taking into account the spin degree of freedom, the non-perturbed *non*-SII *non*-relativistic Hamiltonian for the lattice can be written

$$\widehat{H} = \frac{\widehat{p}^2}{2m} \widehat{\sigma}_0 + V_0(r) \widehat{\sigma}_0 - e\varphi(r) \widehat{\sigma}_0$$
⁽²⁾

where $V_0(r) = -e\varphi_0(r)$ is SII potential energy of a *non*-relativistic electron with two quantum numbers, the crystal wavevector k and the spin index s_u , which is the eigenvalue of u-component of spin operator \hat{S} , and $\hat{\sigma}_0$ is 2 × 2 identity matrix. The term $\varphi(r)$ is antisymmetric $\hat{I}\varphi(r)\hat{I}^+ = -\varphi(r)$ with respect to inversion symmetry operation and anti-commutes with inversion operator \hat{I} , which effectively lifts the spin degeneracy

$$E_{k,s_u} \neq E_{k,-s_u} \tag{3}$$

Let's consider the spin-rotation operator $\widehat{R}_{u}^{s}(\varphi) = e^{-i\varphi\widehat{S}_{u}}$ for arbitrary axis u which commutes with the Hamiltonian for arbitrary φ : $[\widehat{H}, \widehat{R}_{u}^{s}] = 0$ keeping SU(2) invariance. For unperturbed Hamiltonian the states $|k, s_{u} >$, $|k, -s_{u} >$, $|-k, s_{u} >$, $|-k, -s_{u} >$ span a 4 four-fold degenerate subspace ε_{k}^{0} for the energy $E_{k,s_{u}} = E_{-k,-s_{u}} = E_{-k,s_{u}}$, which directly contradicts with the relation (3) $E_{k,s_{u}} \neq E_{k,-s_{u}}$.

To avoid the paradox, let's consider a small perturbation δV , which consists of *non*-SII electrostatic potential $\varphi(r)$ with anticommutator $\{\varphi(r), \widehat{I}\} = 0$ and introduce two spin-orbit coupling terms: $\widehat{U}_1 = \frac{\hbar}{4m^2c^2}\widehat{\sigma} \cdot (\nabla V_0(r) \times \widehat{p})$ and $\widehat{U}_2 = -\frac{e\hbar}{4m^2c^2}\widehat{\sigma} \cdot (\nabla \varphi(r) \times \widehat{p})$.

With the spin-orbital coupling, the small perturbation can be written as

$$\delta V = -e\varphi(r) + \widehat{U}_1 + \widehat{U}_2 \tag{4}$$

The first-order energy correction $E_k^{(1)}$ can be found from the secular equation $\left[\widehat{P}_k^0 \delta V \widehat{P}_k^0 | 0_k > -E_k^{(1)}\right] = 0$ where \widehat{P}_k^0 is the projector to the subspace ε_k^0 .

The *non*-SII perturbing electrostatic field $\varphi'(r)$ with corresponding energy $V'(r) = -e\varphi'(r)$ does not satisfy both TI and SII conditions: $\widehat{T}_{R_n}V'(r)\widehat{T}_{R_n}^+ \neq V'(r)$; $\widehat{I}V'(r)\widehat{I}^+ \neq V'(r)$. Let's apply Bloch theorem to the matrix element

$$\left\langle s_{u},k|V'(r)|-k,s_{u}\right\rangle \neq e^{2ikR}\left\langle s_{u},k\left|V'(r)\right|-k,s_{u}\right\rangle$$
(5)

and introduce the notation $\beta' = \langle k|V'(r)| - k \rangle = \langle s_u, k|V'(r)| - k, s_u \rangle$. Since the electrostatic field does not contain an operator acting directly on spin degree of freedom, the s_u component maybe skipped in the expression. For any given k and arbitrary translation vector R one can write: $\beta' \neq e^{2ikR}\beta'$, therefore $\beta' \neq 0$. Then, the first-order energy correction can be determined as $E_k^{(1)\pm} = a_1 \pm \Delta E_k^{(1)}/2$ with the spin splitting energy

$$\Delta E_k^{(1)} = 2\sqrt{a_2^2 + |c_2|^2 + |\beta'|^2} \tag{6}$$

For the simplest case of SII system the splitting energy $\Delta E_k^{(1)} = 2|\beta'|$ has contributions only from electrostatic field, since a_2 and c_2 matrix elements are equal to 0, where $a_1 = \langle s_u, k | \hat{U}_1 | k, s_u \rangle$, $a_2 = \langle s_u, k | \hat{U}_2 | k, s_u \rangle$, $c_2 = \langle s_u, k | \hat{U}_2 | k, -s_u \rangle$.

A detailed derivation of spin energy splitting can be found in Supplementary Material (SM) Section.

4. Conclusion

Novel promising class of 2D nanoporous spin-polarized materials constituted only by light sp-elements (Li, C, Ca, Al) with visible lift of spin degeneracy was theorized using GGA PW PBC electronic structure calculations. It was shown that stacking sequence of graphene fragments determines the atomic structure and properties of NPBGs. Folded nanometer size pores in bilayer graphene generate intense local electrostatic perturbing fields caused by extra electron charges localized at the folded edges of extreme curvature up to 0.34 Å⁻¹. It was found that Li-, Ca-, and Al-doped NPBG(AA) lattices have ferromagnetic ground states with 0.38, 0.14, and 0.32 $\mu_{\rm B}$ /unit cell with spin density localized at carbon atoms which form the pore edges. It was shown that spin contamination is negligible for all Me@NPBG(AA) heterostructures and can be ruled out as an artificial source of spin polarization. For the case of even number of doping electrons ($N_e = 2$, Ca@N-PBG(AA)) the relative energy of diamagnetic state is equal to 0.037 eV in respect to ferromagnetic ground state. Based on Nagaoka's theorem analysis, strong electron correlations were excluded as the main course of the lift of spin degeneracy in NPBG hexagonal lattices for all degrees of doping. For proposed heterostructures, relativistic spin-orbital coupling is ruled out as well since the lattices consist only of light elements, for which spin is a good quantum number and all relativistic effects are negligible. Novel mechanism of lift of spin degeneracy by perturbing local intense electrostatic fields in low-dimensional lattices with broken local inversion and translation symmetries was proposed. Using symmetry analysis and perturbation theory, it was found that the energy splitting between the spin channels is proportional to the matrix elements calculated on Bloch states with opposite wavevectors and perturbing electrostatic field with broken inversion and translation invariances. Stochastic lattices of doped irregular nanopores in AA bigraphene formed by ion bombardment with consequent high-pressure treatment and metal doping is expected to reveal 2D paramagnetic properties rather than ferromagnetic regular lattice of spin.

CRediT authorship contribution statement

IuA. Melchakova: DFT calculations, graphics, discussions of the results, Writing — original draft. **T.G. Tenev:** Symmetry analysis and perturbation theory consideration of lift of spin degeneracy by

extreme electric fields. Discussions of the results and manuscript preparation. **N.V. Vitanov:** Symmetry analysis and perturbation theory consideration of lift of spin degeneracy by extreme electric fields. Discussions of the results and manuscript preparation. **O.N. Tchaikovskaya:** Discussions of the results and manuscript preparation. **L.A. Chernozatonskii:** Initial atomistic models, of NPBG, discussions of the results and manuscript preparation. **B.I. Yakobson:** Discussions of the results and manuscript preparation. **P.V. Avramov:** Supervision, of the study, Nagaoka analysis, discussions of the results and manuscript preparation.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.carbon.2022.02.041.

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