Thermal conductivities of solid and molten silicates: Implications for dynamos in mercury-like proto-planets

Thermal conductivities of solid and molten silicates: implications for dynamos in Mercury-like proto-planets

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Abstract

Remanent magnetization and active magnetic fields have been detected for several telluric planetary bodies in the solar system (Earth, Mercury, Moon, Mars) suggesting the presence of core dynamos active at the early stages of the planet formation and variable lifetimes. Among the factors controlling the possibility of core dynamos generation, the dynamics of the surrounding silicate mantle and its associated thermal properties are crucial. The mantle governs the heat evacuation from the core and as a consequence the likeliness of an early thermally driven dynamo. In the case of planets with a thick mantle (associated with supercritical Rayleigh numbers), the core heat is efficiently removed by mantle convection and early thermally-driven dynamos are likely. At the opposite, planets with a thin mantle (associated with subcritical Rayleigh numbers) might evacuate their inner heat by diffusion only, making early thermally-driven dynamos difficult. Within the Solar System, Mercury is a potential example of such a regime. Its small mantle thickness over the planet radius ratio might be inherent to its small orbital semi-axis and hence, might be ubiquitous among the terrestrial objects formed close to their star.

To constrain the likeliness of a thermally driven dynamo on "Mercury-like" planets (i.e. with large Rc/R), we present new thermal diffusivity measurements of various solid, glassy and molten samples. We applied the Angstrom method on cylindrical samples during multi-anvil apparatus experiments at pressures of 2 GPa and temperatures up to 1700 K. Thermal diffusivities and conductivities were estimated for solid and partially molten peridotites, with various melt fractions, and for basaltic and rhyolitic glasses and melts. Our study demonstrates that melts have similar thermal properties despite a broad range of composition investigated. The melts reveal much lower thermal conductivities than the solids with almost an order of magnitude of decrease: 1.70 (±0.19) to 2.29 (±0.26) W/m/K against 0.18 (±0.01) to 0.41 (±0.03) W/m/K for peridotites at high temperatures and various melts respectively. Partially molten samples lie in between and several predictive laws are proposed as a function of the melt fraction and solid/melt texture.

Using our results into forward calculations of heat fluxes for dynamo generation for Mercury-like planets, we quantify the effect of mantle melting on the occurrence of thermally driven dynamos. The presence of a mushy mantle and partial melting could significantly reduce the ability of the mantle to evacuate the heat from the core and can prevent, shut or affect the presence of a planetary magnetic field. The buoyancy and fate of molten material in such bodies can thus influence the magnetic history of the planet. Future observations of Mercury-like planets accreted near their star and the detections of their magnetic signatures could provide constraints on their inner state and partial melting histories.

Keywords: Thermal diffusivity; thermal conductivity; melts; geodynamo; Mercury;

Author contributions:
GM, AM, DA and DF set up the MAA apparatus and heating system for Angström measurements. DF and GM conceived the experiments. DF performed, processed and analyzed the experiments. FS significantly contributed to Raman micro-analyses. NC helped for sample selections, analyses and preparations prior experimental runs. JM, DA, GM and DF realized the modelling and discussion section. DF, JM and DA wrote the manuscript. All of the authors have agreed and contributed to the manuscript.

Introduction

The presence of internally generated magnetic fields is a variable feature among telluric bodies in the inner solar system. While few are currently active, such as for Mercury and Earth, several are now extinct, as observed for the Moon, Venus and Mars. On terrestrial planets currently exhibiting a dynamo, the generated magnetic fields characteristics are very different. Earth's magnetic field is very intense 25-65 μT, originating from the core and present for at least 3.5 Ga (Tarduno et al. 2010). Mercury's field strength is much weaker, representing around a 1% of Earth's one (Kabin et al. 2008; Anderson et al., 2011) and its shape is also unique among the different detection in the solar system (Tian et al., 2015). According to the remnant magnetization measured in the crust, it was proposed that such weak magnetic activity occurred during the last 3.9 Ga (Johnson et al. 2015). The source of such a weak-and-prolonged dynamo is still largely debated (Manthilake et al. 2019). In the meantime, there are several evidences for an intrinsic dynamo during the early stages of both Mars and Moon (Acuña et al., 1999; Hood et al., 2010). Their dynamo seems to cease around 4.1-3.9 Ga ago for Mars (Johnson and Phillips, 2005; Lillis et al., 2008, Lillis et al., 2013) and exhibits a somewhat complicated history for the Moon with a strong dynamo between 4.25 and 3.5 Ga, followed by a weak persistence up to 2.5-2 Ga ago (Tikoo et al. 2014, Lawrence et al. 2008, Garrick-Bethell et al., 2009, Mighani et al. 2020). For Venus, the early presence of a dynamo remains yet unconstrained but may be detectable in future explorations (Nimmo et al. 2002; O'Rourke et al. 2019). More broadly, evidences of paleomagnetic anomalies indicate that the angrite parent bodies, originating from inner regions of the solar system, were subject to an early internally generated dynamo (Weiss et al. 2008). All these elements suggest that transient dynamos might be a somewhat common feature in telluric bodies (Monteux et al. 2011).

The presence of early dynamos is highly conditioned by the internal structure of the planet and its capacity to release the heat accumulated during the accretion processes (accretion, metal/silicate differentiation, core and mantle crystallization) as well as short-lived radiogenic heating. As heat conduction is an inefficient heat transport process in silicates at high temperatures (Hofmeister and Branlund, 2015), the onset of a mantle global convection is a crucial step in planet's thermal history. Convection starts when the Rayleigh number (Ra) of the terrestrial mantle is larger than the critical Rayleigh number (Ra_c). The higher is Ra, the stronger the convection, and the more efficient the heat transport. In contrast, heat is only transported by conduction for a terrestrial mantle with a $Ra<Ra_c$. As Ra scales with mantle thickness (h_{mantle}) as h_{mantle}^3, convection should take place easily in planets with a thick silicate mantle, even after the solidification of the early magma ocean stage. Consequences are efficient evacuation of the inner heat and the possible occurrence of a dynamo. At the opposite, bodies with a thinner mantle lead to smaller Ra values, making convection unlikely and dynamos more difficult to generate.

Mercury is the most interesting planet for our study. Indeed, its mantle is thin 420 ± 30 km (Hauck et al. 2013) and its core occupies almost 55% of planet's volume and 65% of the planet mass (Strom and Spague, 2003; Charlier and Namur, 2019). Hence, the mantle of Mercury is controversially at the limit between conductive and convective regimes (Breuer et al. 2007). Different scenarios could

explain the small h_{mantle}/planet radius (R) ratio on Mercury (Charlier and Namur, 2019): (1) primordial nebular processes, yielding to the enrichment of metal over silicate materials in the inner solar system (Ebel and Grossman, 2000; Wurm et al. 2013; Weidenschilling 1978), (2) highly energetic accretional collisions inducing a major loss of the silicate fraction (Benz et al. 1988, Asphaug and Reufer, 2014), and (3) post–accretion scenarios, with major vaporization of the volatile and silicate elements from the planet during magma ocean stage (Fegley and Cameron 1987; Boujibar et al., 2015). If scenarios (1) and (3) are dominant, then "Mercury-like" planets with small h_{mantle}/R ratio would be ubiquitous within all planetary systems. Moreover, such a small ratio would be prevailing during the whole accretionary processes. Mercury-like bodies could adopt a wide range of possible compositions depending on their history. For example, bodies accreted from reduced enstatite and/or carbonaceous bencubbinite chondrites (Malavergne et al. 2010) could present a mantle composition similar to terrestrial lherzolite, but with a sulfur content potentially as high as 11 wt.% (Namur et al. 2016). Accordingly, the diversity of the silicate samples found on Earth in the forms of rocks, melts and glasses is a good proxy to decipher the properties of a range of mantle-relevant silicate compositions on Mercury-like bodies. Depending on the planet size and the h_{mantle}/R ratio, the internal pressure ranges from a few MPa to several GPa. We note that extensive mantle melting likely occurred at different stages of the history of such Mercury-like bodies. Major energy incomes are expected from the vicinity to the young Sun (2500 to 3500 K according Charlier and Namur, 2019), internal energy release (chemical and gravitational differentiation, core crystallization), and presence of short-period radioactive elements (Al^{26}, K^{40} etc.). The very high temperatures likely induce extensive melting of the thin mantle up to the core-mantle boundary (CMB).

As mentioned above, dynamo generation could be difficult for Mercury-like planets, due to the subcritical value of Ra possibly disabling mantle convection. In such case, heat transfer by conduction would dominate the planet history and the thermal conductivity of the silicate mantle is a key parameter governing the early core heat flow. Silicates thermal conduction properties are now well characterized at ambient conditions (Hofmeister and Branlund, 2015). Among them, the most common geological minerals were characterized in the forms of single crystal and polycrystalline aggregates: olivine (Osako et al. 2004; Xu et al. 2004; Perterman and Hofmeister 2006; Gibert et al. 2005), periclase (Hofmeister and Branlund, 2015), feldspar (Pertermann et al. 2008; Hofmeister et al. 2009; Branlund and Hofmeister, 2012) and pyroxenes (Hofmeister 2012, Hofmeister and Pertermann 2008) as well as peridotite rocks (Gibert et al. 2005; Beck 1978), which have been extensively studied due to their important geological implications. The thermal diffusivities of minerals are linked to the characteristics of their lattice structure and modes of phonon generation and propagation as a function of temperature. For silicates, lattice thermal diffusivities usually decrease with increasing temperature following a 1/T dependence. At the opposite, the diffusivities increase while increasing pressure, however, the temperature dependence is much greater than that of pressure over the considered ranges for small planets. The resulting implication is that mantle rocks and minerals are poor thermal conductors in planetary interiors. Recent measurements of thermal diffusivities of glasses and melts at ambient pressure suggested that the non-crystalline silicates are even more insulating than the minerals (Hofmeister et al. 2009, 2014, Romine et al. 2012).

Measurements of thermal diffusivities at relevant conditions of planetary mantles encompass important difficulties, which were overcome by the use of different techniques (see Hofmeister and Brandlund 2015 for a critical review). Measurements were reported over a wide P and T range for large volume samples of olivine, periclase, bridgmanite using Angström or Pulse method in solid pressure apparatus (Osako et al. 2004; Xu et al. 2004; Manthilake et al. 2011a and 2011b, Zhang et al. 2019). Up to now, accurate measurements of geologically relevant silicate glass, partially molten systems and melts at planetary interior conditions remain scarce if not absent. The available results report a nearly flat evolution of thermal diffusivities with the temperature above 1000 K for silicates, glass and melts (Hofmeister et al. 2014; Hofmeister and Banlund, 2015), suggesting that the

measurements above the melting temperature could be safely extrapolated to planetary P-T conditions.

In this study, we aim at better constraining the thermal properties of Mercury–like protoplanets where convection is unlikely and heat is mostly removed by diffusion. We perform HP-HT *in situ* thermal diffusivities measurements of solid, partially molten and fully molten silicate for various compositions in Multi-anvil apparatus and using Angström method. Then, we constrain the likeliness of a thermally driven dynamo during the early stages of the evolution of a Mercury-like planet. We consider a wide range of planet sizes (1 km < R < $R_{Mercury}$) and thermal states (with solid and partially molten mantles) on the dynamo likeliness.

Experimental and analytical methods

High-pressure assemblies:

High-pressure and high-temperature experiments were performed using a 1500-ton Kawai type Multi-anvil apparatus. All experiments were conducted at 2 GPa, based on a previous press-load vs sample pressure calibration (Boujibar et al. 2014), providing an uncertainty of ~0.1 GPa at pressures <5 GPa. We used octahedral pressure media with full length edges composed of MgO doped with Cr_2O_3 (5 wt. %) in a 25/17 multi-anvil configuration (octahedron edge length / anvil truncation edge length) (Figure 1). Our assembly was designed to accommodate the specific requirements for measurements of thermal conductivity of relatively large samples (4 mm long for 4-3.5 mm diameter). All ceramic parts of the cell assembly, including the pressure media, were fired at 1373 K prior assembling in order to remove the absorbed moisture. Oxygen fugacity of the sample was not controlled during the experiments but is expected to be quite reducing due to the presence of the graphite furnace. The use of a steeped graphite furnace helped reducing thermal gradients. Thermal loss from the sample zone was further reduced by the use of a thick zirconia (ZrO_2) sleeve around the furnace. Thermal gradients in our assembly were computed using the software developed by Hernlund et al. 2006. The models show temperature gradients within the sample volume limited to ~7.5 K/mm vertically and even less radially/horizontally (Figure S1). On the other hand, uncertainties of our thermocouple reading (i.e. where the conductivity measurement is performed, see below) are less than 5 K on absolute and 0.1 K in relative temperatures.

Previous experimental studies described the difficulties to perform a good measurement of thermal diffusivity for a molten sample, due to a potential sample deformation (Hofmeister et al. 2009, 2014; Romine et al. 2012). However, deformation remained minor in our experiments, as evidenced by the good reproducibility of the measurements during the repeated cycles of heating and cooling (Figures 1 and 2) as well as the shape of the recovered samples (Figures S6, S7 and S8).

Two tungsten-rhenium ($W_{95}Re_5$-$W_{74}Re_{26}$) thermocouples of 75 µm of diameter were used to measure temperature oscillations at the center (in 300 and 600 µm drilled holes in solids and glasses, respectively) and at the edge of the cylindrical sample. Special care was given to ensure that the junction points of the two thermocouples were located in the same sample plane perpendicular to the cylinder axis. Measurements of the thermal conductivity of melts and glasses have always been particularly challenging due to the risk of thermocouple short circuit, because melts, even dry, are good electrical conductors (Tyburczy and Waff, 1983; Ni et al. 2011). To prevent this effect, thermocouples were inserted in alumina tubes of 0.6 mm diameter and 170 µm wall thickness. While these tubes show good resistance to cold compression and almost no reaction with the samples, even at very high temperature, some leakages for low viscosity basaltic melts have been identified. Their occurrence was taken in account for thermal diffusivity estimations (see Supplementary Text S1 and Figures S2 and S3).

Angström method for thermal diffusivity measurements

We aim at determining thermal diffusivities of geological samples such as peridotites, mafic and felsic glasses and their melts at high pressure and high temperature using a double contact method: the Angström method. Experimental configurations, assemblies and data treatment are similar to several previous studies (Fujisawa et al. 1968; Kanamori et al. 1969; Katsura 1993; Xu et al. 2004; Manthilake et al. 2011a and 2011b). Briefly, a temperature wave is generated radially in a cylindrical sample by the surrounding heater sleeve of the multi-anvil assembly (Figure 1). Oscillations are generated with controlled frequency and period by modulating the power supply. Periodic temperature signals are recorded by two thermocouples fixed in the center and on the edge of the sample cylinder. At frequencies higher than 1.5 Hz, the signal can get noisier due to a limited time resolution of the recording system.

The recorded signals, for each thermocouple channel, are fitted by a nonlinear least square solver (lsqcurvefit on Matlab© using Levenberg-Marquardt algorithm):

$$\Delta T = A_0 + A_1 t + A_2 sin\left(2\pi A_3 t + \frac{A_4 \pi}{180}\right) \quad (1)$$

Following this method, we obtained the amplitude of the temperature variation (A_2), frequency (A_3), and phase (A_4) of the recorded wave as a function of time (t), for the two thermocouples. Errors are quantified based on the residue on the non-linear curve fitting (the *nlparci* function in Matlab©). To infer thermal diffusivity or conductivity from these parameters, the equation of conductive heat transport has to be solved. Here we consider the sample as an infinite uniform cylinder and assume that the heat flow is negligible in the vertical direction, thanks to a relatively long cylindrical heater. The following equation, expressed in cylindrical coordinates by Carlsaw and Jaegger (1959), has to be inverted in order to retrieve the diffusivity of the sample:

$$\frac{dT}{dt} = D\left(\frac{d^2T}{dr^2} + \frac{1}{r}\frac{dT}{dr}\right) \quad (2)$$

where r is the radial distance from the axis, T the temperature, t the time, and D the thermal diffusivity. The boundary condition of our setup is:

$$\frac{dT}{dr} = 0, at\ r = 0 \quad (3)$$

If we consider harmonic excitation at a distance $r = R$ from the axis in normal or complex form:

$$T_R = B_0 + B_1 \cos wt \ \leftrightarrow\ T_R = b_0 + b_1 \mathrm{Re}\,(\exp iwt) \quad (4)$$

where B_0, B_1, b_0 and b_1 are constants and Re is the real part of the exponential. The solution of the radial flow equation with the boundary conditions developed above can be expressed as:

$$T_R = b_0 + b_1\left[J_0\left(\sqrt{-i} * x\right) * \frac{\exp(iwt)}{J_0\left(\sqrt{-i} * l\right)}\right] \quad (5)$$

where:

$$l = (^{w}/_{\kappa})^{1/2} R\ and\ x = (^{w}/_{\kappa})^{1/2} r \quad (6)$$

for $0 \le r \le R$, where w is the angular frequency and J_0 is the Bessel function of the first kind (integer order $n = 0$). At $r = 0$ and $r = R$ we have:

$$T_0 = b_0 + b_1 \theta \cos(wt - \varphi) \quad (7)$$

$$T_R = b_0 + b_1 \cos wt \quad (8)$$

where:

$$\theta = \frac{1}{\sqrt{bei(u)^2 + ber(u)^2}} \quad (9)$$

$$\varphi = \tan^{-1}\left(\frac{bei(u)}{ber(u)}\right) \quad (10)$$

where θ is the amplitude ratio and φ the phase shift between the two harmonic temperature measurements and *bei* and *ber* are imaginary and real parts of the Bessel function of the first kind, respectively. The solution to the eq. (4) can be written using the dimensionless argument u, from

which thermal diffusivity (D) can be directly estimated knowing angular frequency (w) and sample radius (d).

$$u = d(w/D)^{1/2} \quad (11)$$

Thanks to the Eqs.9, 10, and 11, the diffusivity was then retrieved via forward Monte Carlo simulation and neighborhood algorithm (Sambridge, 2002). In this step, different values of diffusivities are generated and theoretical phase shifts and amplitude ratios are calculated. These values are compared to the values measured in our experiments. When the differences between the computed solution and the experimental determination tend to 0 (minimization step), the correct diffusivity is then obtained if the sample radius (d) and angular frequency (w) are known. We note that mathematical solutions appear every 360° for the phase shift. Such erroneous solutions are checked manually and discarded.

For most of our experiments, we observe a significant variation of the refined raw-diffusivity value as a function of the heat-source frequency. This effect was already reported in the literature. Different equations were proposed to refine a real value of diffusivity, corresponding to the infinite frequency asymptote, based on non-linear equations. While Manthilake et al. (2011b) used:

$$D = D_\infty + A_0 exp(A_1 * f) \quad (12)$$

Xu et al. (2004) used:

$$D = D_\infty + A_0 exp\left(\frac{-f}{f_0}\right) \quad (13)$$

where D is diffusivity, f source frequency, f_0 asymptote frequency and A_0 and A_1 constants. In these equations, D_∞, A_n and f_0 are inverted parameters. For a better fit of our experimental data and to minimize the uncertainties on the parameters, we adopt Eq. 13. On the other hand, for experiments presenting no systematic dependence of the raw-diffusivity with frequency, we consider as real value the average value between the raw-diffusivity values measured at all frequencies (Xu et al. 2004; Manthilake et al. 2011b).

Experimental uncertainties

Experimental measurements of thermal diffusivities and their further transformation into thermal conductivities generate uncertainties originating from the estimations of pressure, temperature, sample dimensions and the data fitting itself. Experimental uncertainties on pressure and temperature are presented above (~0.1 GPa and ~5 K, respectively). Sample lengths prior to the sample loading (d_0) and after the melting experiments were determined with a high precision digital gauge (accuracy of ~1 μm) and using the Scanning Electron Microscope (FEG-SEM), respectively (see Table 1). Then, the sample radius during the experiment at high pressure and temperature was calculated using:

$$d(P,T) = d_0 * \left(1 - \alpha(T - 298) + \frac{P}{K}\right)^{-1/3} \quad (14)$$

where α is the thermal expansion and K the bulk modulus of the sample. For these calculations only samples radii before experiments were considered, as post mortem measurements are affected by decompression cracks (highlighted by the larger values measured after the experiments in Table 1). Moreover, the distance between the two thermocouples could not be measured precisely for a few samples. The values of all experimental parameters are provided in Supplementary Materials (Text S4 and Figure S4). Altogether, final uncertainty on the sample length is between 5 and 10 μm.

There are other uncertainties associated with the procedure of data fitting for the determination of raw thermal diffusivities. Experimental phase shifts and amplitude ratios (Eqs. 9 and 10) are determined with a precision generally better than 1% and majored by 3% in the worst cases. In the course of the Monte Carlo simulation, the differences between experimental and theoretical diffusivities are recorded and used a posteriori to refine uncertainties within 1σ errors.

Then, real thermal diffusivities are refined from the raw-diffusivities using either (i) the asymptotic non-linear fit for experiments presenting a dependence in frequency (Eq. 13, which yields

important uncertainties on the refined parameters) or by averaging (see Methods). The error on average (σ_{AVG}) is:

$$\sigma_{AVG} = \sqrt{\left(\frac{1}{n}\right)^2 * \sum_{1:n} \sigma_D^2} \quad (15)$$

where n is the number of diffusivity measurements performed at different frequencies and σ_D is the error on each diffusivity. Raw diffusivities recovered from Monte Carlo processing have errors of ~1%, similar to those of phase shift and amplitude ratio. If the fitting step is realized with Eq. 13, errors of raw data are used as weights in the inversion. The standard deviations are usually between 1 and 10% of the real asymptotic diffusivity. If the averaging method is selected, the standard deviation, estimated via Eq. 15, is usually about 1% of the final value.

A final source of uncertainties come from other technical issues and apparatus reproducibility, which are inherent to such challenging experiments. We considered that final error must be majored by 5 % of the value. The relative uncertainties become even higher after conversion into thermal conductivities due to uncertainties and simplifications on the sample density and heat capacity at high pressure and temperature (see Supplementary Text S4).

Experimental procedure:

We performed a suite of three heating and cooling cycles to provide an important number of data and maximize the quality of recovered data. A first cycle was run up to 500 °C for moisture removal by 50°C steps (Figure. 2). The second cycle was run up to glass transition temperature (Tg) by 100°C steps. Tg varies according to rock composition and its water content (Giordano et al., 2005). For our dry samples, the temperature of 800°C happened to be above Tg for all our compositions. The temperature was then decreased down to 150°C by 100°C steps. The quality of the measurement is usually better during the cooling cycle once (1) the sample has thermally equilibrated with the assembly, (2) moisture has been removed, and (3) a better contact was achieved between the sample and the thermocouples due to local flow in the solid-state. The redistribution of matter under high temperature cancels most of the potential artifacts associated with the presence of pores/voids between the sample and the thermocouples (Hofmeister et al. 2009). Hence, data recorded during the last cycles were considered for final values.

In the last cycle, we heated the sample up to its melting temperature by 100°C steps or 50°C near the melting point. The sample was maintained above its melting point for less than 1 hour, to avoid sample leakage and chemical reaction with the surrounding parts. The sample was then quenched to 600-550°C. This step produces a glassy sample from which measurements at low temperature are performed.

Temperature oscillations of the two thermocouples were measured at each temperature step for both heating and cooling cycles, at 12 different oscillating frequencies between 0.1 and 1.5 Hz. The measurements were performed after at least 2 min of thermal equilibration to reach a stable regime (the smaller is the frequency, the longer is the required equilibration time). Then, the recording duration was 1 to 2 minutes or at least 10 oscillating periods. The measurement at the 12 frequencies took between 20 to 30 minutes. Thus, the duration of each experiment was more than 12 hours.

Chemical and textural analyses:

Recovered samples were cut parallel and perpendicular to the cylindrical furnace and each section was polished with great care. We could observe the position of the two thermocouples junctions, measure the sample radius and perform the textural and chemical analyses (see Supplementary Figures S6, S7, and S8).

Micro-textures were observed with a Scanning Electron Microscope (SEM) JEOL Jeol JSM-5910 LV using an accelerating voltage of 15 kV and a working distance of 11.4 mm. The 2D phase proportions of our partially molten peridotite samples were obtained from the analyses of qualitative

chemical maps obtained by energy-dispersive X-ray spectroscopy (EDX) in the SEM. The images were binarized and phases were individually separated allowing textural analyses with the FOAMS software (Shea et al., 2010). A more detailed description is given in Freitas et al. (2019). On the other hand, quantitative chemical analyses were performed on both our starting materials and experiment products using the electron probe micro analyzer (EPMA). Chemical and textural analyses of starting materials are reported in the Supplementary Text S2, Figures S6 to S13 and Tables S1, S2, S3 and S4. Analyses of recovered runs are detailed in Supplementary Text S3, supplementary Figures S6 to S7 and Tables S1, S2, S3 and S4.

Water contents were estimated using the ICP-AES for the peridotite starting materials and via Raman spectroscopy for the recovered samples. Raman spectra were collected with a Renishaw InVia confocal Raman micro spectrometer, equipped with a 532 nm diode laser and a Leica DM 2500M optical microscope. Measurements were carried out using a 2400 grooves/mm grating, a 100× microscope objective, a slit aperture set to either 20 µm or 65 µm and a laser power of 8 mW for glasses and 16 or 75 mW for olivine. The resulting lateral and axial resolutions were of ~1 and 3 µm, respectively, and the spectral resolution was better than 1 cm^{-1}. Daily calibration of the spectrometer was performed based on the 520.5 cm^{-1} peak of Si. Spectra were recorded from ~100 to 1300 cm^{-1} (alumino-silicate network domain) and from ~3000 to 3800 cm^{-1} (water domain), with variable acquisition times ranging between 5 and 120 s for silicate bands and 120 and 240 s for water domain depending on the water content (Figures S11 to S17). For water quantification in olivine and glass, we followed the procedures reported by Bolfan-Casanova et al. (2014) and Schiavi et al. (2018). We used both (1) the external calibration procedure, which is based on a set of hydrous olivine standards from (Bolfan-Casanova et al. 2014) and different types of silicate glasses ranging from basaltic to rhyolitic compositions (Schiavi et al., 2018; Médard and Grove, 2008), and (2) the internal calibration procedure, based on the correlation between the water concentration in olivine or glass and the relative areas of the water and silicate Raman bands (OH/Si integrated intensity ratio). The discrepancy between the two methods is small. Water contents in the standard materials were previously determined using the FTIR technique.

Results

We performed a total of 11 thermal diffusivity experiments on various chemical compositions, using the Angström method (details in Table 1). In this section, we first describe phase shifts and amplitude ratios between the two thermocouples and their conversion into thermal diffusivities and conductivities. We detail the post-mortem chemical and textural analyses in the Supplementary Text S3, Tables S1 to S4 and Figures S6 to S13.

Phase shift, amplitude ratio and the refined raw-thermal diffusivities

Signals recorded during the experiments are sinusoidal oscillations with varying frequencies. The thermocouple located at the sample center (labeled TC1 in Figure 3) presents a phase delay and a smaller amplitude compared to the thermocouple located at the sample edge (labeled TC2 in Figure 3). Typical raw signals and their fits are presented in Figure 3, while the refined (absolute) phase shifts and amplitude ratio are reported in Figure 4. Both the magnitude of phase shift and amplitude ratio change significantly with the type of sample and the experimental conditions, including the source frequency. At a constant frequency, the phase shift increases with increasing temperature. At a constant temperature, the phase shift increases with increasing the excitation frequency. The amplitude ratio is decreasing with increasing frequency and temperature.

Globally, the refined thermal diffusivities present a comparable evolution of temperature at all signal frequencies (see an example in Figure 5). When the frequency dependence is larger than the experimental uncertainty (Figure 6), we use Eq. 13 to refine the true asymptotic value of the thermal conductivity. Alternatively, when the temperature dependence is below the experimental uncertainty

or when no clear frequency trends is visible, we average the different raw-diffusivity values (see Methods). In the wide majority of the cases, diffusivity values inferred from phase shifts appear to be more robust and with a lesser degree of uncertainty, compared to values inferred from difference of amplitude, in agreement with previous studies (Kanamori et al. 1969 and Xu et al. 2004). Hence, despite similar values obtained with the two methods, values refined from phase shift were preferred.

Results for peridotite

For peridotite, our two successful experiments present a smooth evolution with temperature, yielding diffusivities values decreasing from $1.7(\pm0.1)e^{-6}$ to $7.5(\pm0.4)e^{-7}$ m²/s for sample M804 and $1.5(\pm0.8)e^{-6}$ to $5.5e^{-7}$ m²/s for sample M847 (Figure 6a), with an uncertainty of about 5 to 10% for each sample. We attribute the relative discrepancy to a difference of sample mineralogy between the two samples, due to the coarse grain size of the core drilled peridotite (see Supplementary Texts S2 and S3 and Figures S8 and S9). Olivine has a higher intrinsic thermal diffusivity than the other phases present in peridotite such as pyroxenes and spinel (Hofmeister and Branlund, 2015). M804 may contain more olivine, inducing higher diffusivities than M847. In this respect, the results for two samples are thus compatible with each other and the differences are representative of the variability of thermal diffusivity that can be expected among the compositional variability of peridotites (from lherzolites to dunites).

Thermal diffusivities of our peridotite samples scale as a function of ~1/T, as expected from the standard equation provided by Hofmeister and Branlund, 2015:

$$D_{lat} = a * T^{-b} + c * T \quad (16)$$

where T is the temperature (K), and a, b and c are adjustable parameters (Table 2). The quality of the fit is excellent up to a temperature of ~1300 K corresponding to the onset of peridotite melting. We therefore exclude the data points above 1300 K to model the thermal properties of solid peridotite.

Results for basalts

For our basaltic samples, the measured diffusivities plot over a broad range of values, from $1.0(\pm0.1)e^{-6}$ to $3.0(\pm0.2)e^{-7}$ m²/s (Figure 6b), with an uncertainty of ~5% for each experiment. The discrepancy is particularly important at low temperatures. Also, a same sample yields thermal diffusivity values significantly different along the different cycles of the experimental procedure (between C2, H3 and the final quench, see Figure S5). Samples with the highest diffusivities at low temperatures present a rapid decrease of diffusivity with increasing temperature. On the other hand, samples with the lowest diffusivities show very small temperature dependence. It yields to a convergence of all diffusivity measurements at ~1000 K. Based on a study of rhyolitic glasses, Romine et al. (2012) reported a moderate temperature dependence, similar to our samples presenting a low diffusivity, and an increase of 0.0192 mm²/s of the glass diffusivity per percent of crystallinity. For our starting materials with less than 5 vol.% of crystals (see Supplementary Text S2 and S3, Figure S7), the effect of microlites could account for ~0.1 mm²/s of variation in our diffusivity values, which correspond to less than ~10% of observed differences. However, the presence of 35 vol.% of crystals in the recovered sample M807 would explain not only its high thermal diffusivity at low temperature, but also its strong temperature dependence that is typical of crystals (see Beck et al., 1978; Romine et al. 2012; Hofmeister and Branlund 2015 and our peridotite trends in Figure 6a). The recrystallization of M807 is not surprising, since the second cycle of annealing was performed above its Tg (Figures 2 and S5). The crystallinity of other samples depends on the applied cycles of annealing at a temperature eventually close to their Tg. Nonetheless, diffusivities of all samples converge at increasing temperatures, because the conductivity of crystals is not much greater than that of the glass at high temperature, especially if microlites are low diffusivity silicates such as pyroxenes, plagioclase or spinels (see Hofmeister and Branlund 2015 for mineral diffusivity compilations). Over the 5 basaltic samples investigated in this study, the diffusivity trends indicate either significant recrystallization of M807 (DR07-MORB) and M662 (EPR-MORB), or negligible

crystallization of M844 and M846 (DR11-MORB) and M836 (synthetic haplobasalt). The sample crystallization is likely to evolve during the thermal diffusivity measurements in step H3 (up to melting point) of the experiments performed at a temperature significantly above the Tg. For this reason, the crystallinity determined on the recovered samples is only a qualitative measurement of the sample properties at high temperatures.

Results for rhyolites

Measured diffusivities of rhyolite samples also plot over a broad range of values from $1.4(\pm0.8)e^{-6}$ to $4.0(\pm0.2)e^{-7}$ m²/s, with an uncertainty of about 5% for each experiment (Figure 6c). The discrepancy appears similar than for the basalt samples, as the sample presenting higher diffusivities also show a major temperature dependence at low temperature. The presence of less than 2 vol.% of crystals in the starting material could account for a diffusivity increase of 0.038 mm²/s at maximum (Romine et al., 2012). Still, the diffusivity trends suggest a major recrystallization at high-temperature for M808 (Güney Dag) and M843 (ATHO), some crystallization for M843 (ATHO), and negligible crystallization for M850 (Güney Dag).

Properties of melts and partially molten samples

In addition to the evolutions described above, a strong decrease of the thermal diffusivity is observed for most of our samples at the highest temperatures (Figure 6). The decrease occurs at temperatures around 1300 K for peridotites, 1200 K for basalts and >1050 K for rhyolites. Such temperatures are in agreement with the melting or glass transition temperatures, depending if the sample is a peridotite or a glass, recrystallized or not. Similar changes were already reported at temperatures above the glass transition (Hofmeister 2009, 2014, Romine et al. 2012).

The amplitude of the decrease is 45-50% in peridotites, which recovered samples present a degree of partial melting (F) up to 23%, 35-70% for basalts and <30% for rhyolites samples. The more pronounced decrease in molten peridotites is probably due to a more contrasted change of the local structure at the melting point, between the minerals and the melt (see discussion). On the other hand, the minor change of diffusivity for rhyolites at Tg could be related to their high SiO_2-content, which preserves a polymerized structure in the melt above the glass transition.

Thermal conductivities

Thermal conductivities (κ) can then be computed from thermal diffusivities following:

$$\kappa\,(P,T) = D(P,T) * \rho(P,T) * C_P(P,T) \quad (17)$$

where $\rho(P,T)$ and $C_P(P,T)$are the sample density and heat capacity, respectively. For our calculations, we considered ρ and Cp values in standard conditions when the P and/or T dependences were not available in the literature (see Supplementary Text S4 and Figure S4).

Conductivities calculated for peridotites evolve from 4.32 (±0.48) to 1.70 (±0.19) W/m/K with increasing the temperature up to the melting point. Values for basalts range from 1.7 ($\pm8.0e^{-2}$) to 0.5 ($\pm4.0e^{-2}$) W/m/K, whereas those for rhyolite lie between 1.1 ($\pm9.0e^{-2}$) and 0.3 ($\pm3.0e^{-2}$) W/m/K for low to high temperatures, respectively. At the melting temperature, our partially molten peridotites display values of 1.19 (±0.16) to 0.93 (±0.10) W/m/K, whereas melts present relatively lower values of 0.34 (±0.2) to 0.18 (±0.1) W/m/K for basaltic and 0.41 (±0.3) to 0.31 (±0.3) for rhyolitic compositions (See Figure 7 and Table 3). We note that the important difference in conductivity between basalts and rhyolites (Figure 7) is predominantly due to differences between their heat capacities and densities, while their thermal diffusivities are found similar (Figure 6).

Interpretation of results

General Temperature dependence

For all compositions investigated in this study, thermal diffusivities decrease with increasing temperature until reaching a plateau at temperatures between 700 and 1000 K. Based on experiments performed at room pressure, it was observed that the plateau occurs at about the Debye temperature of the mantle minerals (Hofmeister et al. 2009, 2014). For this reason, it was proposed that thermal diffusivities vary largely with temperature until the complete activation of the vibration modes (phonons in minerals). The temperature range observed in our study for the occurrence of a plateau is fully compatible with this interpretation.

For basaltic glasses, a comparable but more moderate decrease of thermal diffusivity was reported up to a saturation temperature corresponding well to the glass Tg (Hofmeister et al. 2009, 2014, Romine et al. 2012). In our experiments, the decrease is of ~30% to 60% over the investigated temperature range, depending on the experiment. Such amplitude is compatible with the ~40% decrease observed during the heating of pyroxene glasses (Hofmeister et al. 2009).

For rhyolite samples, the thermal conductivity increases slightly with increasing the temperature (Figure 7). This is due to the heat capacity that increases more with temperature than the density increases and diffusivity decreases (Eq. 17). The increase is, however, smaller than reported in Romine et al. (2012), due to the use of a different Cp (Neuville et al. 1993) (see Supplementary Text S4) and a stronger temperature dependence of thermal diffusivities observed in our experiments because of different crystallizations states.

Effect of radiative conduction

Romine et al. (2012) reported an increase in thermal diffusivities of the melts at very high temperatures at ambient pressure. They attributed this feature to an increased role of the radiative component. Such a component can dominate the thermal diffusivity for a sample transparent to the infrared and visible photons at high temperatures. For thin samples, this effect can become problematic if the mean free path of photons is longer than the sample length (ballistic photons, see Hofmeister and Branlund, 2015). No significant increase in thermal diffusivity and conductivity is observed in our high-pressure experiments, except maybe for the rhyolitic samples (Figures 6 and 7). The difference with the previous work is most probably related to the opacity of our basalts and peridotites samples, hence limiting the radiative transfers.

Effect of glass/melt composition

Overall, our conductivity values are compatible with the values available in the literature (see Figure 8). Differences in absolute values are nonetheless present. Rhyolite melts (0.31-0.41 W/m/K) are found slightly more conductive than basaltic ones (0.18-0.34 W/m/K). Within the same family of glass, thermal conductivity varies by 0.10 to 0.15 W/m/K for rhyolitic and basaltic melts, respectively. This is slightly larger (of at least 10%) than the experimental uncertainty, an effect possibly due to larger uncertainties on the dimensions of the molten sample. No clear trend can be retrieved from the comparison between our different basaltic or rhyolitic compositions. Among the major elements, iron could be of major importance, due to its critical impact on glass/melt density. Indeed, the thermal diffusivity of glasses was reported to decrease with increasing density (Hofmeister 2014). The comparison between our rhyolites and basalts is coherent with such a trend. However, our haplobasalt (M836) presents diffusivity values comparable with natural basalts (M662, M807, M844), as well as Fe-bearing (M843 and M848) and Fe-free (M808 and M850) rhyolites (Figure 6), despite a variation of the Fe-content from 0 to 10 wt.% in these different samples. Other elements could also impact the melt thermal diffusivity, in particular Si and Al, which favor polymerization of the liquid (and alkali elements for the opposite effect) (Ni et al. 2015). Still, within the experimental uncertainty, we observe no clear trend related to these elements, despite a variation of the SiO_2 content by more than 20%. Additionally, water, with a total content smaller than 1.10 wt.%, should have a negligible effect on thermal conductivity (Romine et al. 2012, Ni et al. 2015). It could, however, impact the melt density at a low degree of partial melting (Hofmeister 2014). As the water contents estimated in the

recovered samples are similar to the ones obtained in starting materials (see Supplementary Text S2 and S3), water should not induce any strong diffusivity variation in our data-set. We, therefore, conclude that chemical effects are secondary compared to the structural ones.

Mixing models for thermal conductivities of partially molten peridotite

Our results show that peridotites, and to a lower extent the glasses, present higher thermal diffusivities compared to the melts. This result is not surprising: thermal conductivity is strongly dependent on the local structure and its vibrational properties. The disorder in the atomic structure increases from solid, glasses to molten states (Hofmeister et al. 2014). The composition of the melt appears to be of secondary importance. The final set of thermal diffusivities and conductivities values selected for the applications are given in Tables 3, S5 and Figures 9 and S14.

To propose a predictive law for thermal conductivity of partially molten rocks several mixing equations are now tested. Such equation generally describes the effect of a small amount of conductive phase into an insulating matrix. For thermal conduction, the problem is reversed because the melt is less conductive than the solid. In this section, we explore the different predictive models of thermal conductivity of binary mixtures:

1) Linear mixing model consider parallel thermal resistor:

$$\kappa_{bulk} = \kappa_s * (1 - F) + F\kappa_m \quad (18)$$

Where *s* corresponds to the solid, *m* the melt and *F* the volume fraction of the melt.

2) tube / Ashbie model consider 1/3 of tubes of melt aligned in the heat flow direction (Grant and West, 1965, Schmeling 1986):

$$\kappa_{bulk} = \frac{1}{3} * \kappa_s * (1 - F) + F\kappa_m \quad (19)$$

3) cube model (Waff, 1974) representing cubes of solids into a melt matrix

$$\kappa_{bulk} = \left[1 - F^{2/3}\right] * \kappa_s \quad (20)$$

4) Archie's law, an empirical relation developed for electrical conductivity (Watanabe and Kurita, 1983)

$$\kappa_{bulk} = C * (1 - F)^n * \kappa_s \quad (21)$$

Where *C* and *n* are constants.

5) Thermal resistors in series:

$$\kappa_{bulk} = \kappa_s * \frac{\kappa_m/\kappa_s}{\kappa_m/\kappa_s + F(1 - \kappa_m/\kappa_s)} \quad (22)$$

6) Hashin Shtrikman lower bound (HS^-), representing insulating melt spheres into a conductive solid matrix:

$$\kappa_{bulk} = \kappa_s * \frac{F}{1/(\kappa_m/\kappa_s) + \frac{1 - F}{3\kappa_s}} \quad (23)$$

7) Maxwell-Eucken relation:

$$\kappa_{bulk} = \kappa_s * \frac{\kappa_m + 2\kappa_s + 2F(\kappa_m - \kappa_s)}{\kappa_m + 2\kappa_s - F(\kappa_m - \kappa_s)} \quad (24)$$

8) Landauer relation, based on resistors in series:

$$\kappa_{bulk} = \frac{1}{4} * \left[\kappa_m(3F - 1) + \kappa_s(2 - 3F) + \left\{\left(\kappa_m(3F - 1) + \kappa_s(2 - 3F)\right)^2 + 8\kappa_s\kappa_m\right\}^{\frac{1}{2}}\right] \quad (25)$$

9) Russel-Rayleigh relation:

$$\kappa_{bulk} = \frac{\kappa_s\left[\kappa_s + F^{2/3}(\kappa_m - \kappa_s)\right]}{\kappa_s + (\kappa_m - \kappa_s)(\kappa_m^{\frac{2}{3}} - F)} \quad (26)$$

These equations provide a different evolution of the thermal conductivity with the fraction of melt (F). In Figure S14, we present the results when either fixing κ_{solid} and κ_{melt} to the average value of our measurements, or adjusting their values to minimize the misfit between the mixing models and our results at varying F values (Table S5). Among the variety of fits obtained, it appears that the effect of partial melting is underestimated in most of the cases. Only the thermal resistors in series is capable to reproduce adequately the strong curvature observed experimentally at low F values, as well as the end-member values of solid and melt conductivities. For this reason, we use series model (eq. 22) for further discussions.

We note a lack of data points at high melt fractions, preventing to decipher more precisely the mixing trend. At very high temperatures, the experimental measurements become difficult on natural peridotite melting, in particular due to melt escape and chemical reactions with the experimental cell. Complementary data could be acquired working with analog system such as basalt/olivine mixture and could represent a further research direction.

Thermal conductivity of partially molten peridotite: influence of texture

The 3D solid/melt arrangement is known to influence significantly the geophysical properties of partially molten systems (von Bargen and Waff, 1986; Laporte et al., 1997; Laporte and Provost, 2000, Minarik and Watson, 1995; Yoshino et al., 2005 Maumus et al. 2005; Ten Grotenhuis et al. 2005, Freitas et al. 2019). Their distribution is classically described using dihedral angle value, which translates the ability of a liquid to wet the grain boundaries as a consequence of interfacial energies. The dihedral angle decreases when increasing pressure, temperature, water content and decreasing silica/alumina content of the melt (Yoshino et al. 2007, Mibe et al. 1998, 1999, Laporte et al., 1997, Watson et al 1991). Several studies with similar basaltic or peridotite melts (dry) have shown that basalt-like melts at mantle conditions have dihedral angles significantly lower than the interconnection threshold of 60°, with values between 30-40° at 2 GPa (Laporte et al., 1997, Yoshino et al. 2005, 2007). Our partially molten samples display a coherent texture and dihedral angles with these observations. Dihedral angles of 23.3° and 19.0° were measured from our samples containing 6.4% and 23.3% of melt, respectively (Figure S15), in good agreement with previous data given that these mafic melts are moderately hydrous (Table S3). For each melt fraction, a thin layer of melt surround most of the grains, in particular olivines, which in 3D will result into the insulation of the solid gains from their surroundings (Figure S9). This is very well visible on our low melt fraction sample (F=6.4%) where the layers of melt are few microns thick (M804). Even if melt is more abundant near clinopyroxenes and spinel sites in M847 (F=23.3%), the melt pockets are interconnected with similar thin melt layers (<10 µm) (Figure S9). As a result, thermal conductivity is expected to drop brutally in the first degrees of melting. Still, some grain boundaries should remain un-wetted until the melt fraction rise significantly. For this reason, thermal conductivity should only stabilize at melt fraction corresponding to solid grains completely isolated from each other. This trend is visible in our data and parallel model (Figures 9 and S14) with a strong decrease in the first 10% of melting highlighted by M804, the change of slope seems to occur around 15% and values decease more slowly in the 15-50% range as seen in M847, to stabilize and display near-melt values above 50%. The complete isolation of solids should occur at "packing" threshold, which is a function of the solid shapes and size distribution and is expected to occur between 40 to 60% of melting. Thus, the first degrees of melting are very crucial in the case of a wetting liquid and affecting importantly the thermal properties.

Thermal conductivity of peridotite: effect of the grain size

The modelling of thermal conductivity of peridotites and low F molten peridotites should also take in account the effect of grain boundaries thermal resistances as grain size may vary in the different geological contexts (from 100 µm to >1 cm), as seen in natural meteoritic examples, (Barrat et al. 1999, Busek, 1977, Keil, 2010, Floran et al. 1978). Indeed, grain boundary scattering could be

important when the mean free paths of phonons approach the grain size. This effect, which only concerns solids and low fractions of melt, can be quantified with the following equation (Smith et al. 2003, Smith et al. 2013):

$$\frac{1}{\kappa_{poly}} = \frac{1}{\kappa_{single}} + nR_{boundary} \quad (27)$$

Where κ_{poly} is the thermal conductivity of the polycrystalline sample, κ_{single} the thermal conductivity of a reference single crystal (average from olivine data of Hofmeister et al. 2016, Table 3), *n* represents the surface of grain boundaries along the heat flow direction per unit length, and $R_{boundary}$ the thermal resistance of grain boundary plane. The *n* value should be almost constant with temperature (Smith et al. 2013) and is estimated between $4e^{-4}$ and $7e^{-3}$ m for our two peridotite samples via analyses of SEM images (grain size ranging from 25 to 140 µm, see Table S4 for textural parameters). We calculate $R_{boundary}$ values between $1.9e^{-6}$ and $5.9e^{-6}$ W/m²/K for M804 and $9.3e^{-6}$ and $3.2e^{-5}$ W/m²/K for M847. These values are compatible or slightly higher than hydrous polycrystalline olivine samples (Zhang et al. 2019).

As a result, the thermal conductivities quantified in our experiments are underestimations of natural ones as the grain size is <100 µm, in experiments compared to grain sizes of 100 µm up to >1 cm typical of mantle peridotites and reduced meteorites (which could be relic of bodies interiors, from cumulates (Floran et al. 1978), enstatite chondrite/achondrite (Keil, 2010), diogenite (Barrat et al. 1999) to pallasite (Busek, 1977)). Melts and high F partially molten systems are not affected by such effect, thus the observed decrease of thermal conductivity at the melting temperature is probably smaller in our experiments.

Implications for geodynamos on Mercury-like proto-planets

Suitable conditions for a dynamo

For a thermally driven dynamo to operate in a terrestrial planet, four conditions were found to be necessary (e.g., Monteux et al., 2011): the core heat flow must be at least adiabatic (1), the thermal convection within the core has to supply enough power to compensate the losses due to ohmic dissipation (2), the Reynolds magnetic number must be supercritical (complex turbulent convection) (3) and the mantle heat flow has to overcome the core heat flow needed to induce a dynamo (4). These conditions can be expressed in terms of heat flow balance (See Figure 10 for a schematic representation) and are detailed here:

(1) The metallic core has to convect, meaning that the heat flow out of the core needs to overcome the adiabatic heat flow (Stevenson et al., 1983).

For this, the core thermal conductivity (κ_{core}) is a dominant parameter. A large κ_{core} value increases the heat flux along the core adiabat and reduces the lifetime of a thermally driven dynamo (Breuer et al., 2015). Several laboratory measurements suggested that the thermal conductivity of polycrystalline iron at Mercury's core conditions is 113–125 W/m/K (see Deng et al., 2013 and references therein). However, such values for Mercury are recently challenged with several recent studies proposing a much lower conductivity. In a first one, the conductivity of pure Fe and Fe-Si alloys is reported at 30-40 W/m/K and 35-40 W/m/K, respectively (Sibert et al. 2019). Then, it is proposed that the thermal conductivity of Fe-S at the P-T conditions of Mercury's core is as low as ~4 W/m/K, thus 1-2 orders of magnitude lower than that of pure iron (Pommier et al. 2019, Manthilake et al. 2019).

This first condition can be expressed as:

$$Q_{CMB} > Q_{Ad} = \frac{\kappa_c \alpha_c g_c T_{CMB}}{C_{p,c}} 4\pi R_c^2 \quad (28)$$

To estimate this flux, we assume that T_{CMB} is the melting temperature of pure iron at P_{CMB}. This assumption gives a conservative value of the core heat flow in comparison with considering T_{ICB} since the core liquidus is steeper that the core adiabat. We estimate the relation between the melting temperature of pure iron and the pressure using the following expression obtained by fitting the experimental results from Anzellini et al. 2013 with a Simon and Glatzel equation:

$$T_{m,Fe} = 1800\left(\frac{P_{CMB}}{27.9} + 1\right)^{1/2.08} \quad (29)$$

Such a melting temperature typically lies between the solidus and liquidus of a chondritic mantle for the same pressure conditions (Monteux et al. 2020 and references therein). We also assume that k_c, α_c and $C_{p,c}$ are constant (see values in Table 4) and P_{CMB} is calculated as follows (Monteux and Arkani-Hamed, 2014):

$$P_{CMB} = P(r = R_c) = \frac{2}{3}\pi G\rho_c^2(R_c^2 - r^2) + \frac{2}{3}\pi G\rho_{Si}^2(R^2 - R_c^2) + \frac{4}{3}\pi G\rho_{Si}R_c^3(\rho_c - \rho_{Si})\left(\frac{1}{R_c} - \frac{1}{R}\right) \quad (30)$$

(2) The energy supplied by thermal convection to the geodynamo has to compensate for the loss due to ohmic decay (Buffett, 2002).

This imposes a condition on the core heat flow at the CMB. In fact, core heat flow will need to overcome a critical value. Assuming that dynamo is generated only by thermal convection in the core, we can write:

$$Q_{CMB} > Q_{Ad} + \frac{4\upsilon_c\bar{B}^2C_{p,c}}{0.8\mu_c\alpha_cG\rho_cR_c} \quad (31)$$

This heat flux is estimated by considering that the characteristic magnetic length scale equals the radius of the core. The parameter $\bar{B}$ is the average strength of the magnetic field inside the core and was estimated using a scaling from Christensen and Aubert (2006):

$$\bar{B} = 0.9\mu_c^{\frac{1}{2}}\rho_c^{\frac{1}{6}}\left(\frac{g_cQ_B(R_c - r_i)}{4\pi R_cr_i}\right)^{\frac{1}{3}} \quad (32)$$

With $Q_B = \alpha_cQ_{CMB}/C_{p,c}$ the buoyancy flux and r_i the radius of the inner core. In the scaling from Christensen and Aubert (2006), the inner core size cannot be set to 0. On Mercury the size of the inner core is currently not well constrained even if recent constraints via geodetic analysis (Genova et al. 2018) suggest its presence and a possible important size (r_i/R_c between 0.3 and 0.7). As we focus here on the effect of thermal cooling on dynamo generation (i.e. we do not consider the effect of compositional convection related to inner core growth), we consider a small inner core with $r_i/R_c = 0.01$. The scaling law used to calculate the average strength of the magnetic field inside the core (Eq. 32) is valid for the Earth but overestimates $\bar{B}$ in the case of thin shell dynamos such as the one operating within Mercury (Christensen and Aubert (2006)). Mariner 10 spacecraft measurements showed that Mercury's magnetic field was 100 times weaker than the Earth's one. To account for this discrepancy, we consider that the average strength of the magnetic field is 1%$\bar{B}$ obtained from Eq. 32 when solving Eq. 31. We also consider that υ_c, μ_c and ρ_c are constants (see values in Tab. 4). We note that most of the power needed to overcome the criterion related to Eq. 31 can be supplied by thermal core convection (i.e. criterion related to Eq. 28) especially for large metallic cores.

(3) The magnetic Reynolds number (Re_m) must be supercritical in order to have convective motions, inducing a complex structure needed to carry the magnetic field lines (U. R. Christensen and Aubert, 2006).

Reynolds magnetic number is calculated using Christensen and Aubert, 2006 formulation's and assuming that the characteristic magnetic length scale is the radius of the core:

$$Re_m = \left(\frac{Q_{CMB}G\alpha_c}{3C_{p,c}}\right)^{1/3}\frac{R_c}{\upsilon_c} > 10 - 100 \quad (33)$$

The value of the critical magnetic Reynolds number ($Re_{m,c}$) is usually constrained for models implying a large inner core. For Mercury-like planets, this value is less documented. Here we make the conservative assumption that this value ranges between 10 and 100.

(4) The mantle heat flow has to overcome the core heat flow needed to generate a dynamo.

The mantle's Rayleigh number (Ra) conditions the efficiency of heat evacuation from the mantle:

$$Ra = \frac{\alpha_{Si}\rho_{Si}g\Delta T{\delta_{Si}}^3}{\eta_{Si}\kappa_{Si}} \quad (34)$$

With α_{Si} the mantle thermal expansion coefficient, ρ_{Si} the mantle density, ΔT the temperature difference between the core and the surface of the planet, δ_{Si} the mantle thickness, η_{Si} the mantle viscosity, κ_{Si} the mantle heat diffusivity ($\kappa_{Si} = k_{Si}/(\rho_{Si}C_{p,Si})$), and $C_{p,Si}$ the mantle heat capacity. If Ra is lower than a critical value ($Ra_C \approx 1000$), the heat is evacuated from the mantle by conduction and the mantle heat flow Q_{Si} is:

$$Q_{Si} = \frac{k_{Si}\Delta T}{\delta_{Si}} 4\pi R^2 \quad (35)$$

Alternatively, if the $Ra > Ra_C$, the heat is evacuated from the mantle by convection and Q_{Si} scales with $Ra^{1/3}$ (Solomatov, 2007):

$$Q_{Si} = 0.089 \frac{k_{Si}\Delta T}{\delta_{Si}} 4\pi R^2 Ra^{1/3} \quad (36)$$

In any case, for a thermally-driven dynamo to operate, Q_{Si} has to be larger than the core heat flow Q_{Core}. For these calculations, we consider here that the surface gravity is dominated by the gravity at the CMB ($g = g_c$). On a planet with a core over planet radius ratio (R_c/R) of ~0.5, the mantle is thick enough so that $Ra > Ra_c$ and the heat is efficiently evacuated by convection. On such bodies, the dynamo is generated easily and should appear early in the planet history. If the heat evacuation is very efficient, the planet might cool down rapidly, which can potentially lead to a short-lived dynamo. On a Mercury-like body with a large R_c/R ratio, the mantle is thin compared to the core and its Rayleigh number, critical criterion for thermal convection, hardly overcomes Ra_c. Hence, conduction should be the main heat evacuation process within the mantle of Mercury-like planets, which can limit the occurrence of an early thermally-driven dynamo.

Simulation results

We now compare the core heat flow needed to generate a dynamo within a Mercury-like body (with e.g. $R_c/R_{planets}$) (Figures 11 and 12). To do this, we use a maximum possible range of solid conductivities between κ_{Si} = 4.32 and 1.70 W/m/K. We consider a maximum planet radius R=2440 km with a thin mantle shell to stay in temperature and pressure conditions equivalent to the experimental conditions detailed above (P≤2GPa and T≤1700K). We also report the critical size of the protoplanet (R = 215 km) above which Re_m is larger than 100 (Eq. 33). The Figure 11 shows that a solid conductive mantle is able to evacuate enough heat to induce a thermally driven dynamo if the planet radius is larger than ~215 km, regardless of the value of thermal conductivity in the outer core, at least up to more than 40 W/m/K. In contrast, the change of core conductivities from e.g 40 W/m/K (Sibert et al., 2019) to 4 W/m/K (Manthilake et al. 2019) has a major effect on the maximum size of a planet that can operate a thermally driven dynamo. For a core conductivity κ_{core} = 40 W/m/K, the maximum planet radius evolves from 1220 to 1880 km, for κ_{Si} = 1.70 and 4.32 W/m/K, respectively. When κ_{core} = 4 W/m/K, the maximum planet radius is more than 2500 km.

We now perform the same type of calculation for a mushy mantle using the silicate-melt conductivity refined in this study (Tables 3 and 4). We consider here neither a complete magma ocean that would evacuate the core heat very efficiently by turbulent convection (Monteux et al., 2016) nor a mushy mantle with a large melt fraction (larger than 40-60%) which would imply a strong decrease of the bulk viscosity of the mantle (Picard et al., 2013). We consider here a purely conductive mantle where the melt fraction is smaller than 20%. Hence, if this melt fraction is concentrated at the core

mantle boundary, the molten layer is thin enough to avoid its convection, while if the liquid is equally distributed within the mantle, we can reasonably assume that the bulk viscosity is weakly affected by the liquid phase and close to the viscosity of subsolidus silicate material. Still, the presence of melt may affect mantle properties. An important parameter is the fate of melts, which is primarily controlled by the solid-melt density contrast. The molten material can either be evacuated at the surface during early volcanism or cumulate at the lowermost mantle. For peridotites, negative melt buoyancy is unlikely to happen at pressures lower than 7 GPa (Sakamaki et al. 2006, Matsukage et al. 2005, Freitas et al. 2017). However, the buoyancy of melts generated from the partial melting of a body with composition largely different from peridotite remains uncertain. Molten reservoirs may be trapped at shallow depths at the end of mushy mantle cooling (Monteux et al., 2020) or during the last stages of fractional crystallization within small bodies (e.g. Frossard et al., 2019). On a Moon-like body, a melt layer may be trapped below an anorthositic crust while on a Mercury-like body, anorthite is denser than the melt and then may not float allowing the melt to form a late shallow magma ocean. We consider here that the melt has neutral buoyancy and is equally distributed within the planetary mantle, with the consequence that the mantle viscosity is primarily controlled by the solid fraction of the mantle.

Due to the lower thermal conductivity of the melt compared to the solid mantle, the mushy mantle should limit the heat flow that can be extracted from the core. In our calculation, we consider for simplicity that the entire mantle has the same conductivity as the melt. As a result, the range of planetary radii for which a dynamo is plausible is much narrower than for a fully solid mantle (Figure 12). For a core conductivity of 40 W/m/K, a thermally driven dynamo can only operate for planetary sizes ranging between 215 and 350-570 km, depending on the value of κ_{Si} and for $\kappa_{core} = 40$ W/m/K. The maximum planetary radius becomes 1000-1500 km for a core conductivity of 4 W/m/K. Therefore, the melting of a Mercury-like planetary mantle could limit the establishment of a magnetic field on the planet. This effect could last over different timescales, depending on the size of the planet and of the core, the initial core temperature, the fate of the melt material, etc.

The differences obtained for fully solid (Figure 11) and molten (Figure 12) models show that the presence of melt within a “Mercury-like” planet mantle could result into better thermal insulation of the core, which may prevent the occurrence of a thermally driven dynamo. Of course, planets presenting mantle with supercritical Rayleigh number would not be affected by this effect, because mantle convection could extract enough heat from the core at the CMB. As a consequence, the solid mantle viscosity plays a key role because (1) it controls the planet size above which mantle convection is likely, through the Ra value, and (2) it governs the efficiency of mantle heat evacuation once the critical Rayleigh number is overcome (see Eq. 36). Decreasing the mantle viscosity from 10^{22} to 10^{18} Pa.s decreases the critical planet size for mantle convection by one order of magnitude (from 1600-1900 km to 160-200 km for a solid mantle and from 850-1050 km to 80-110 km for a mushy mantle, see Figures 11 and 12). The figures also show that the lower is mantle viscosity, the easier the planet can meet the criteria for a thermally driven dynamo when the mantle of the planet is convecting. We note here that considering the influence of melt on the bulk mantle viscosity should lead to a decrease of the critical Rayleigh number and as a consequence of the critical planetary size where heat in only evacuated by thermal conduction (i.e. green triangles would move to the left). However, this effect should be negligible for the small melt fraction considered here.

The impact of mantle partial melting crucially depends on the melt quantity and its location within the mantle. Whether it is distributed in a mushy mantle or accumulated as a pond at a given mantle depth affects both, locally and globally, the mantle viscosity and the thermal diffusivity. As a consequence, the dynamic regime can evolve from conduction to convection, changing the thermal outputs at the CMB and making the heat flux enough, or insufficient, to power a thermally-driven dynamo. In this framework, transient phenomena such as mantle overturns (Elkis-Tanton et al. 2003, Ballmer et al. 2017) implying major melt migration will result in a brutal change in the planet magnetic signature. Similarly, the chemical stratification resulting in the production of a crust

(anorthositic, basaltic etc.) may help insulating the planet interior in its early history suggesting weaker but longer sustained dynamos.

Conclusions

In this study, we constrain the thermal diffusivities of silicate melts with a wide range of composition at high pressure and temperature conditions using the multi-anvil apparatus and the Angström method. We observed that melting induces a significant decrease in both thermal diffusivities and conductivities. We measure melt thermal diffusivities ranging from 0.18 (±0.02) W/m/k to 0.41 (±0.04) W/m/K. The composition of the melt does not have a significant impact on diffusivities. We then use our results to address the thermal properties of the molten silicate reservoirs, and the likeliness of a thermally driven dynamo within a Mercury-like planets presenting a large metallic core and a relatively thin silicate mantle (large Rc/Rplanet). The mantle of such bodies is not expected to be convecting easily ($Ra<Ra_c$) leading to an inefficient heat evacuation and difficulty generating a dynamo compared to planets with a thicker mantle (where easily $Ra>Ra_c$). Our results illustrate that the presence of a mushy mantle above the CMB in such a Mercury-like planet can significantly reduce the ability of the mantle to evacuate the heat from the core and limit the likeliness of a thermally-driven dynamo. As a consequence, the fate and the lifetime of such a mushy reservoir can have a profound impact on the thermal history of Mercury-like planets. Future observations of Mercury-like planets accreted in orbits close to their star and the eventual detection of their intrinsic magnetic field would in return constrain the state of the mantle surrounding their metallic core.

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Figure 1: Schematic cross-section of the high-pressure cell assembly used for Angstrom method with multi-anvil apparatus. For glass and melt experiments, thermocouples were inserted in alumina tubes of 0.6 mm diameter and 4.5 mm length in the sample zone.

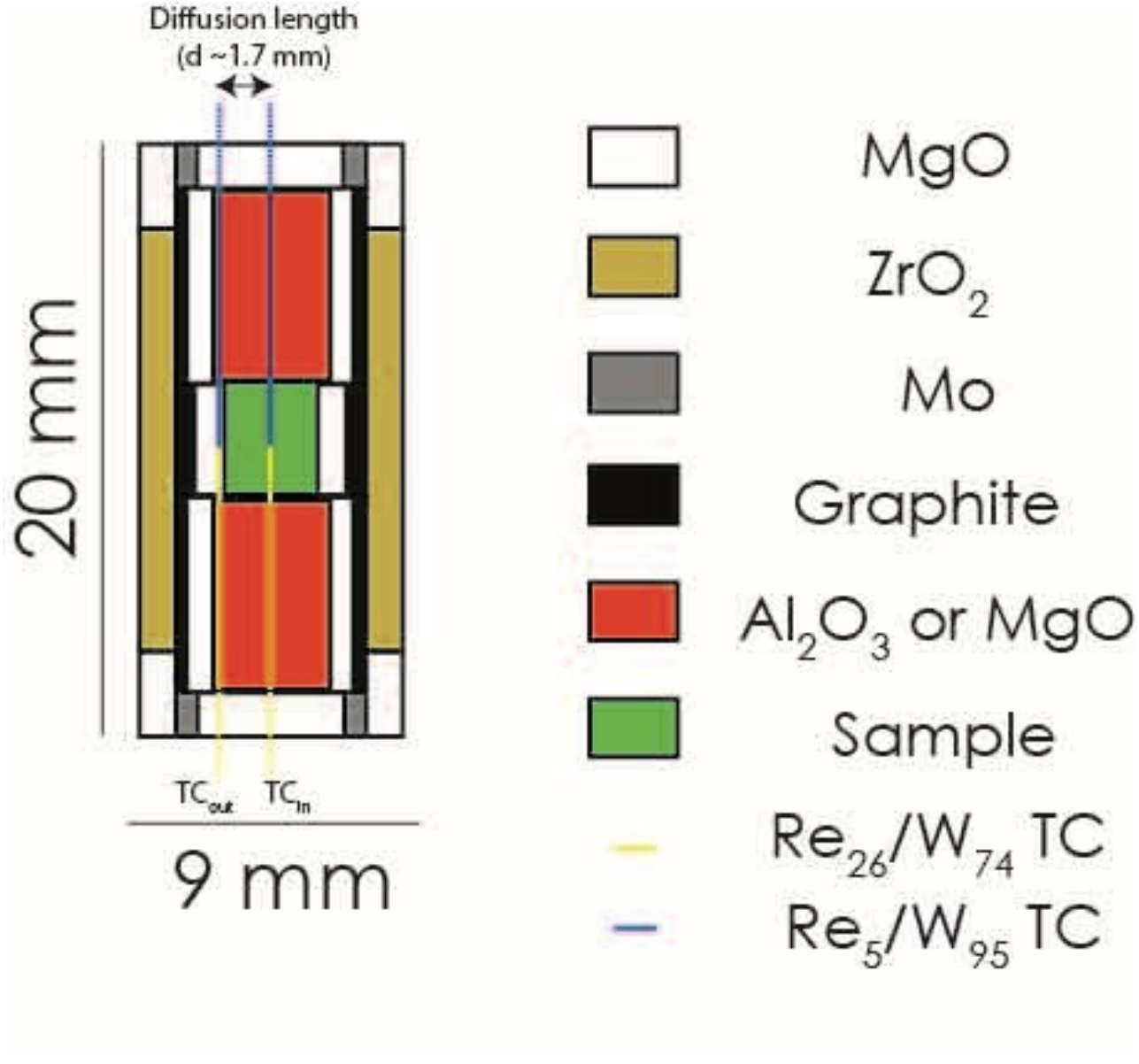

Figure 2: Experimental procedure for the measurement of thermal diffusivity of peridotites, glasses and melts: black, blue and red for cycles 1, 2 and 3 respectively. Heating (H) and cooling (C) parts of the cycles are separated by black dashed lines (for example H1: 1st cycle heating). The expected temperatures for sample dehydration (up to ~500°C), glass transition and melting are illustrated in shaded colors: green, pink and yellow respectively.

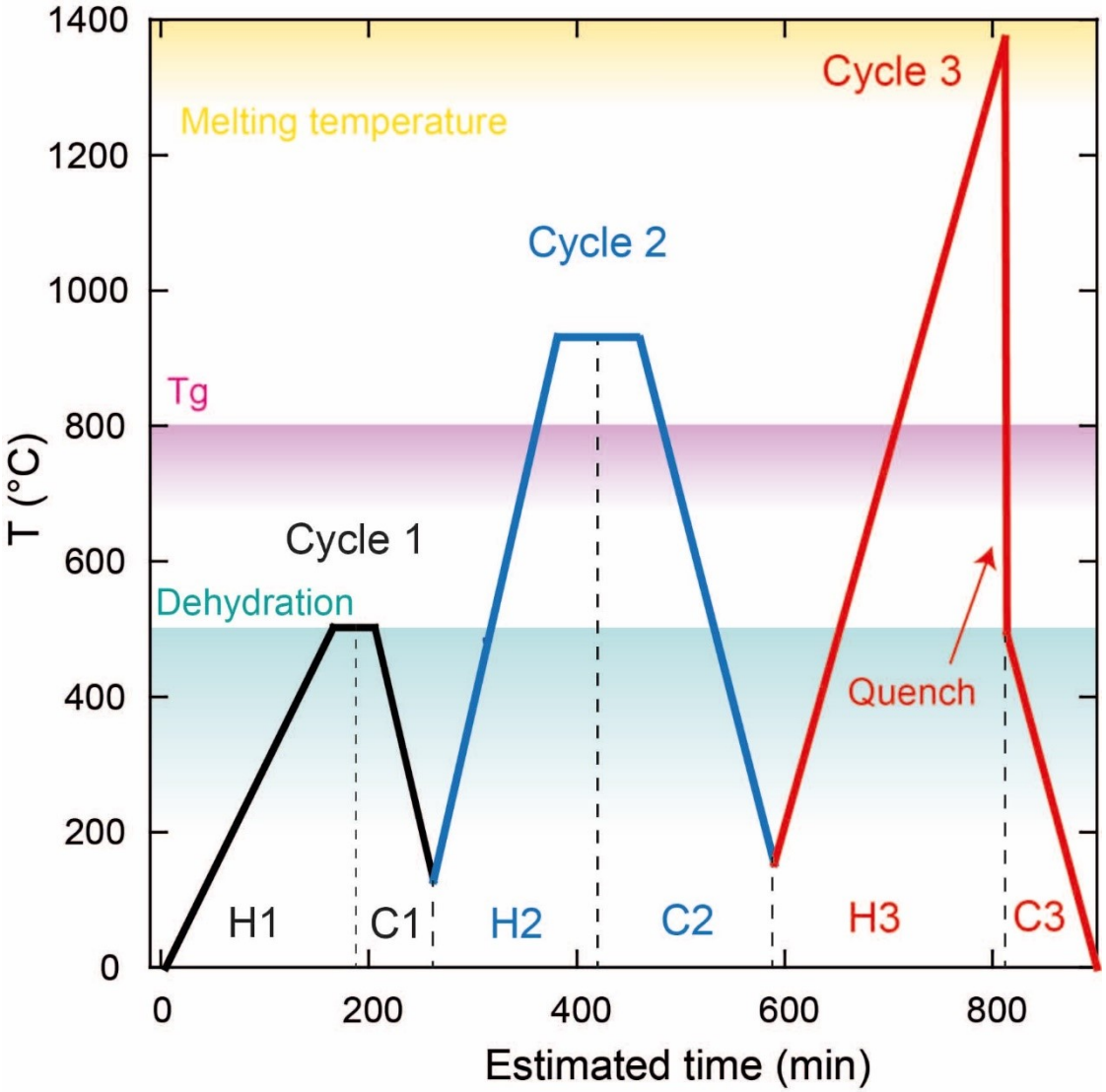

Figure 3: Examples of temperature waves recorded at high temperature during M804 experiments. Such data set is acquired after the sample equilibration at target temperature conditions for a few minutes (here T = 250°C). Acquisitions are performed at an interval ranging from 40 ms to 200 ms. At least 10 periods of the temperature oscillation are recorded to ensure a good extraction of phase shifts and amplitude ratio based on the fitting procedure described in Methods. Upper and lower frames correspond to temperature measurements performed at frequencies of 0.3 and 1 Hz, respectively. Red symbols are measured data and the dash thick lines represent the fitted sine waves.

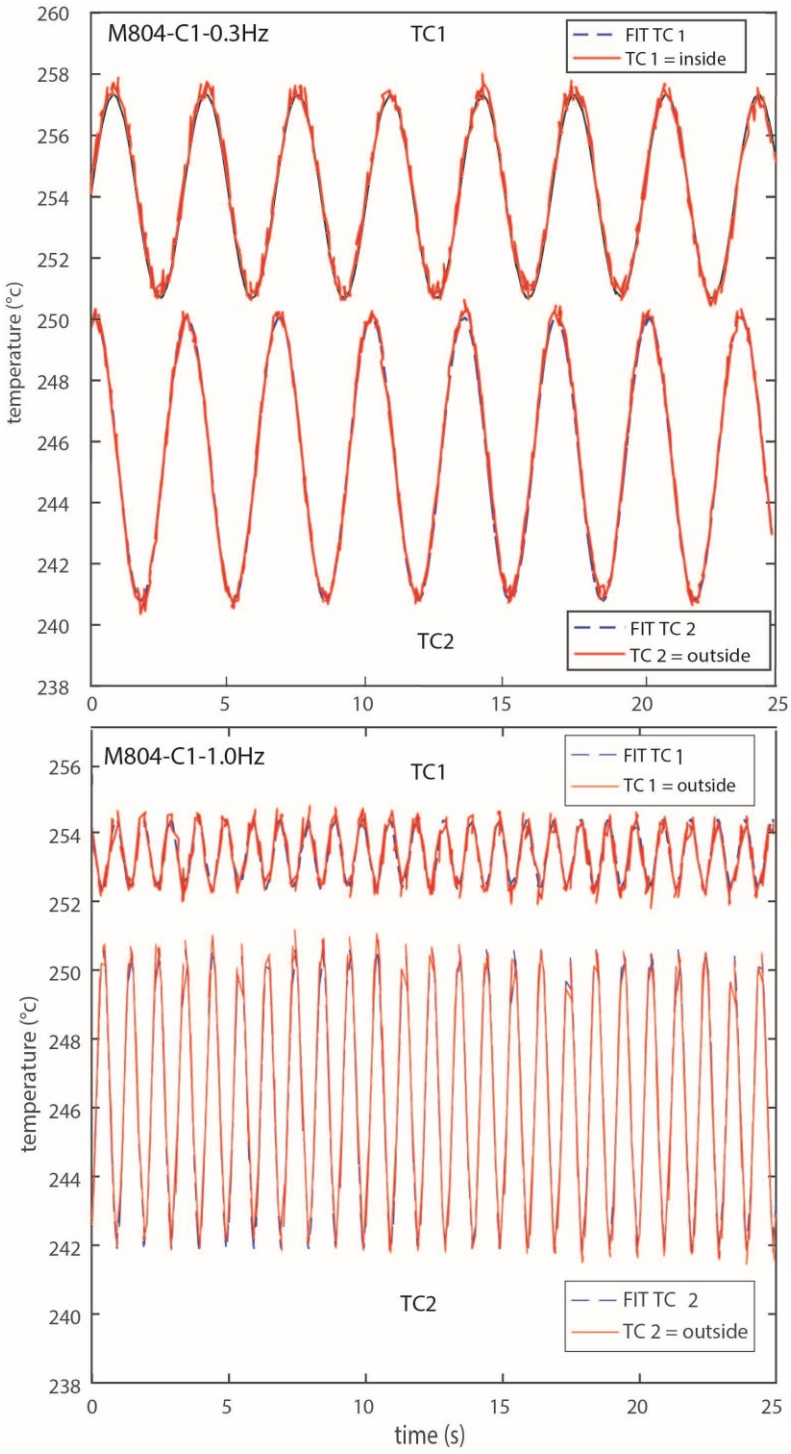

Figure 4: Example of refined phase shifts (top panels) and amplitude ratio (bottom panels) as a function of frequency (from 0.2 to 1.5 Hz, left panels) and temperature (from 428 K to 1191 K, right panels) for sample M844.

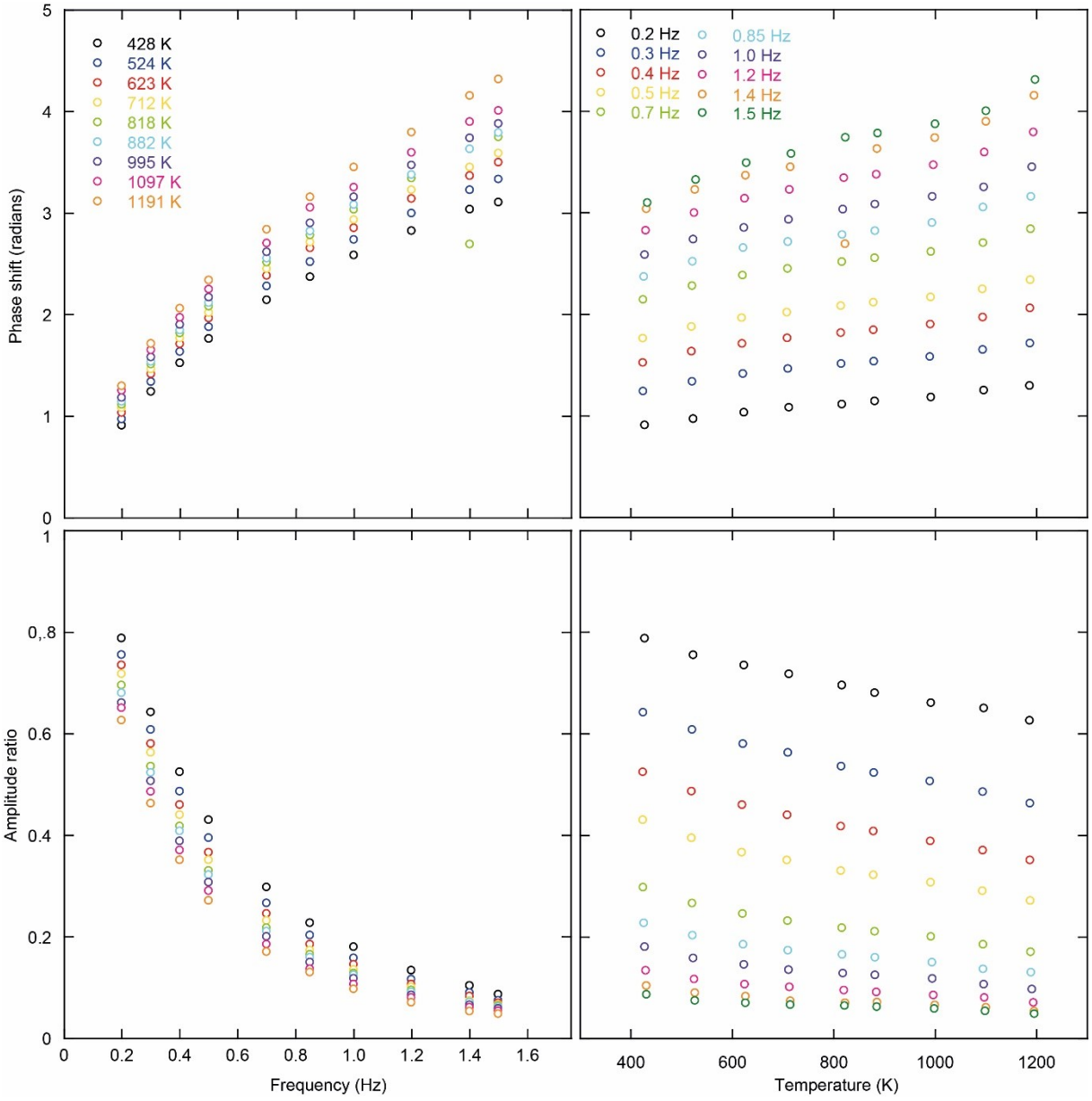

Figure 5: Typical example of a set of raw values of the thermal diffusivity extracted from our measurements for a basaltic glass, presented as a function of the frequency of the heat source. Experimental temperatures range between ~430 and ~1200 K at a pressure of 2GPa (sample M844). Left and right panels correspond to thermal diffusivities calculated from phase shifts and amplitude ratios, respectively. The color code is kept similar in both panels. The fit through the data is made following the equation $D = D_0 + A\,exp(-f/f_0)$ (Xu et al., 2004), were D_0 is the high-frequency asymptote of the diffusivity (see text). Error bars are generally within the size of the symbol.

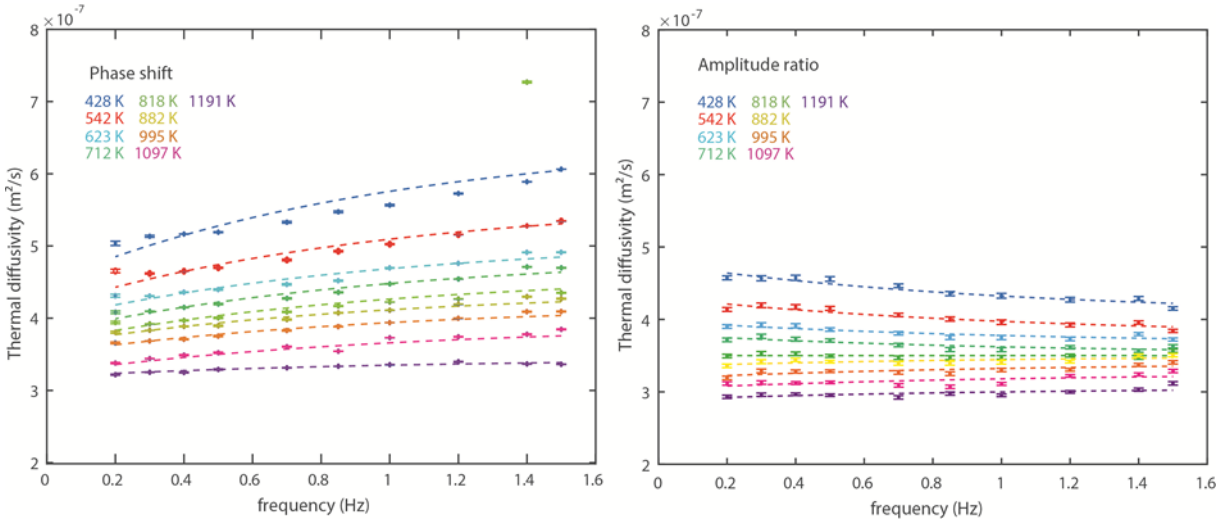

Figure 6: Thermal diffusivities data refined for our peridotites, basalts and rhyolites samples (from top to bottom) as a function of temperature. Associated fits are represented with a solid line of the same color than the symbols. Error bars are shown when larger than the symbol size. Several basaltic (M807, M662) and rhyolite (M848, M808) samples were partially recrystallized during the annealing and dehydration procedures prior to the conductivity measurement, as indicated by their high conductivity values at low temperatures. Thermal diffusivities values converge at high temperatures and melting.

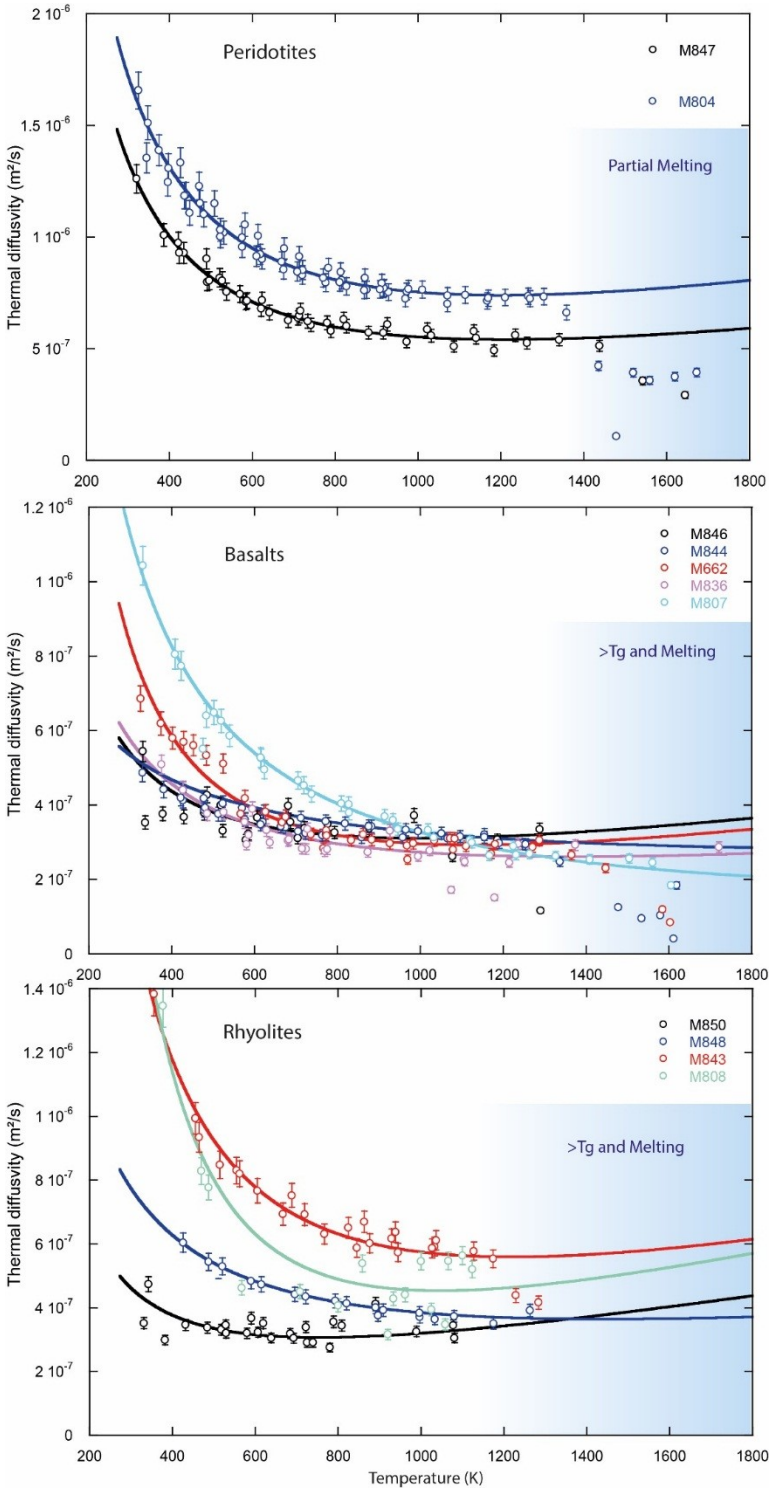

Figure 7: Thermal conductivities inferred from diffusivities (Figure 6), heat capacities and densities (see Figure S4), based on Eq. 17 of the main text.

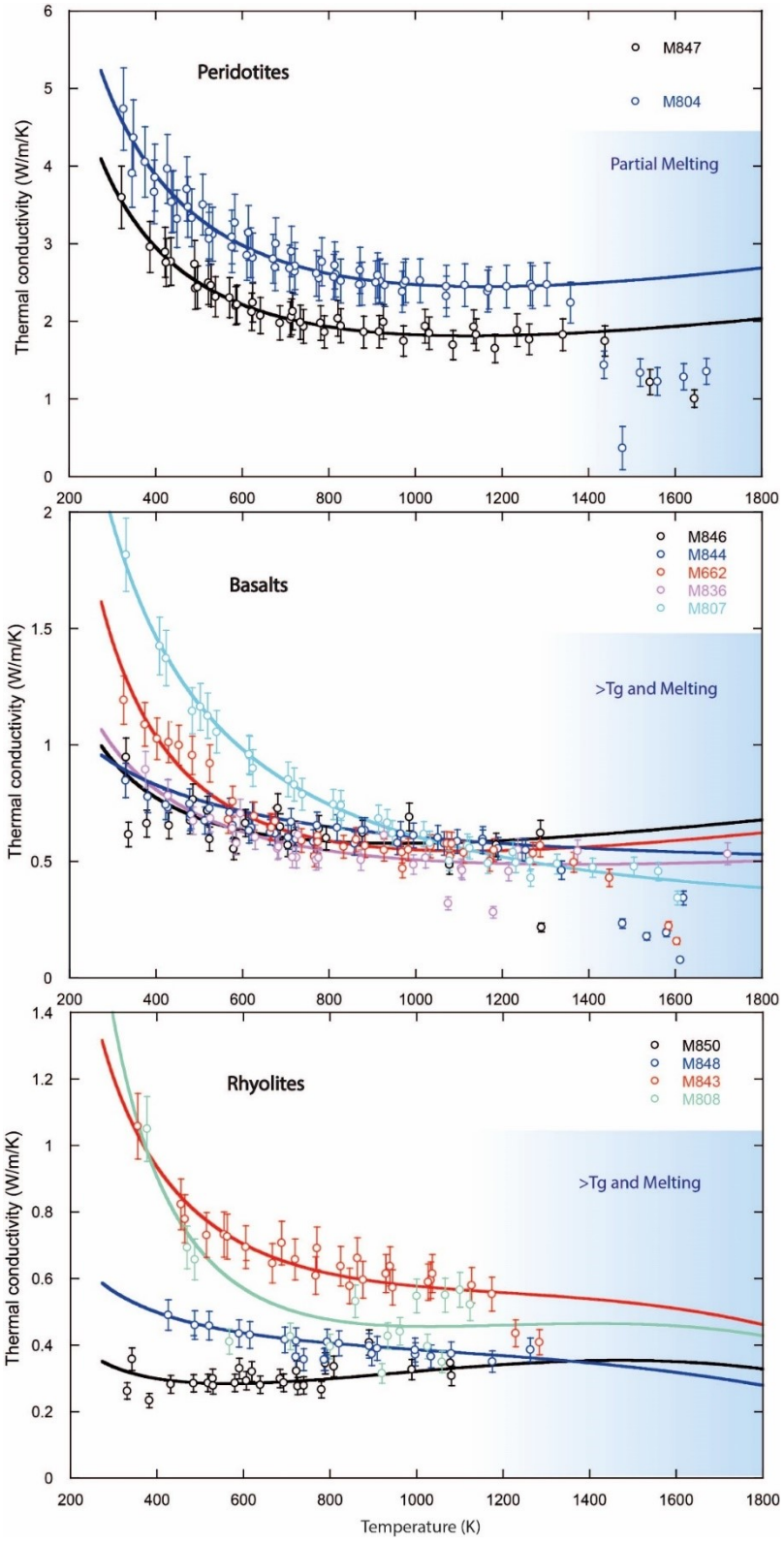

Figure 8: Comparison with the literature of our thermal diffusivities obtained our peridotite (upper panel), basaltic (center panel) and rhyolitic (lower panel) starting materials. Solids (peridotite and glasses) and melts are represented in thick lines and thick dashed line, respectively. Literature data are reported with thinner dashed lines (grey to black). Diopside (Di) glass and melt, $XAlSi_3O_8$ glass, Anorthite melt (An), Albite melt (Ab) and orthose melt (FK) from Hofmeister et al. 2009, NCr Rhyolite from Romine et al. 2012 and Enstatite glass from Hofmeister et al. 2014.

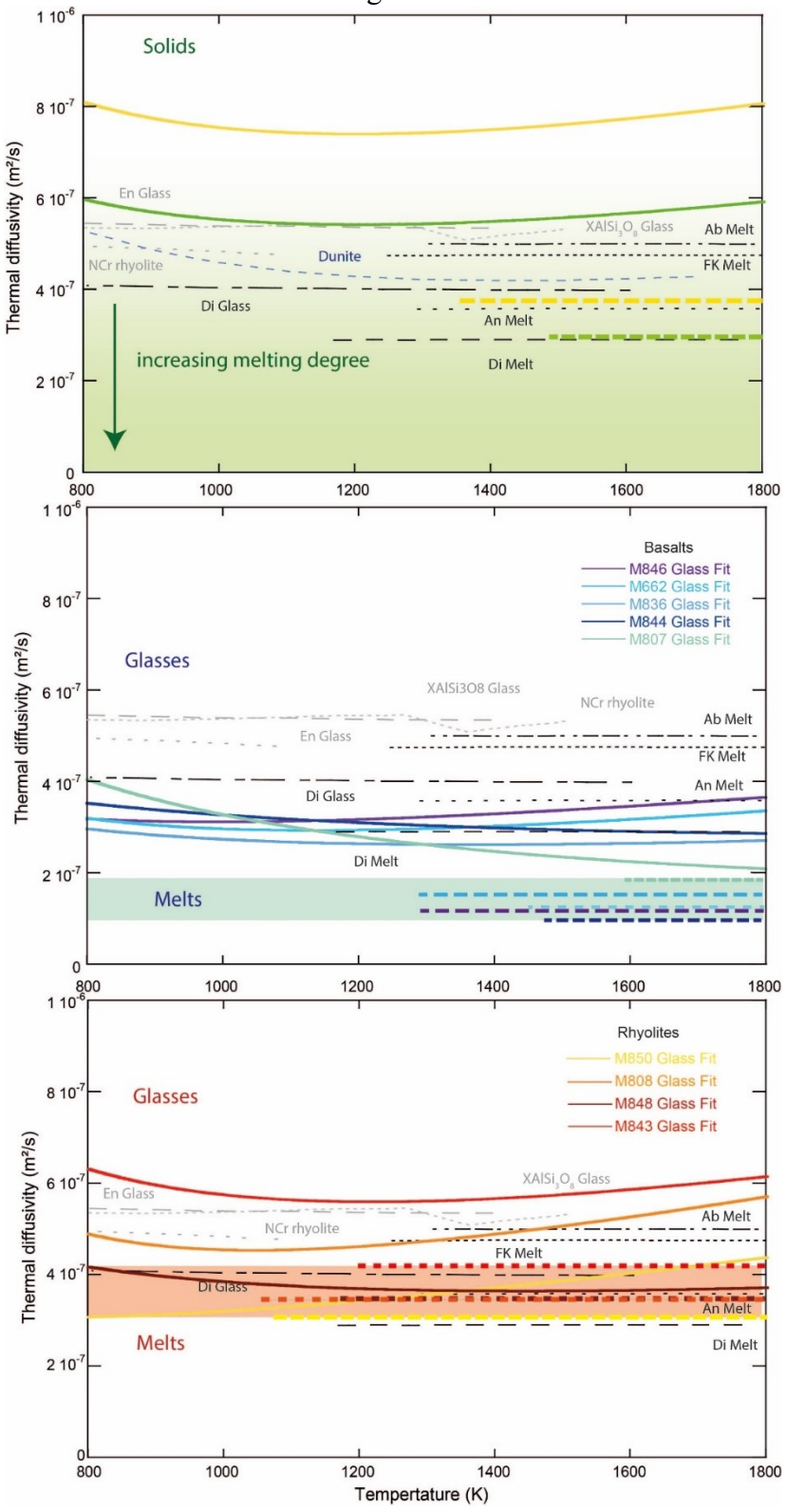

Figure 9: Our best model of the evolution of thermal diffusivity as a function of the melt fraction at high temperature (>1200 K), based on all available data sets. Solid peridotites at low and high temperature are represented with green and blue diamonds, respectively. Partially molten peridotites with 6.4% and 23.3% of melt (see Supplementary Text S3) are represented with red circles and melts (basalts and rhyolites) are represented with blue and pink circles. All the errors represented are 1 standard deviation. The fit represented is using a model of thermal resistors in series (Eq. 22), which fits our data set very well (see Figure S14).

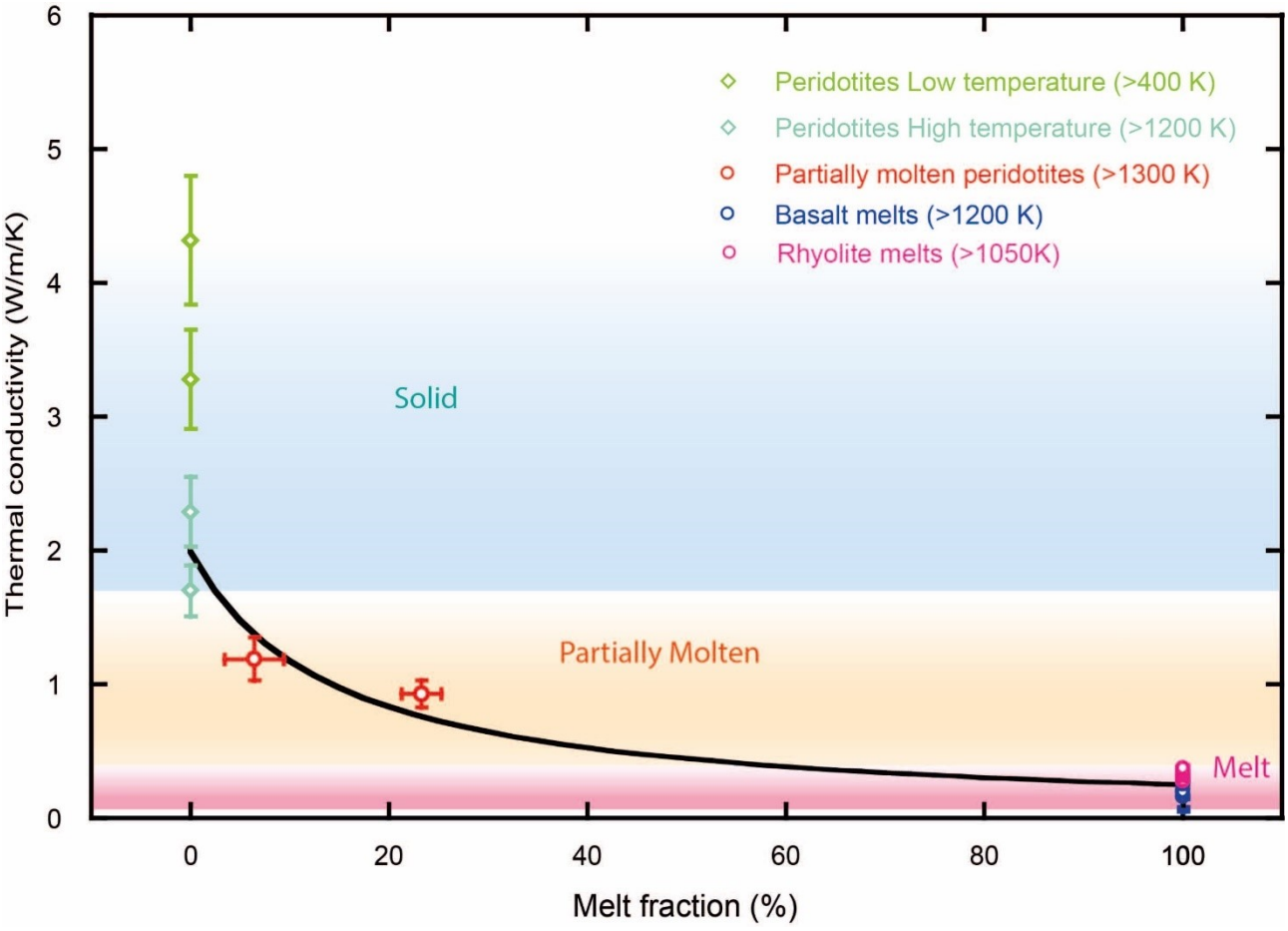

Figure 10: Schematic representation of the geometry and of the heat flows computed in our model.

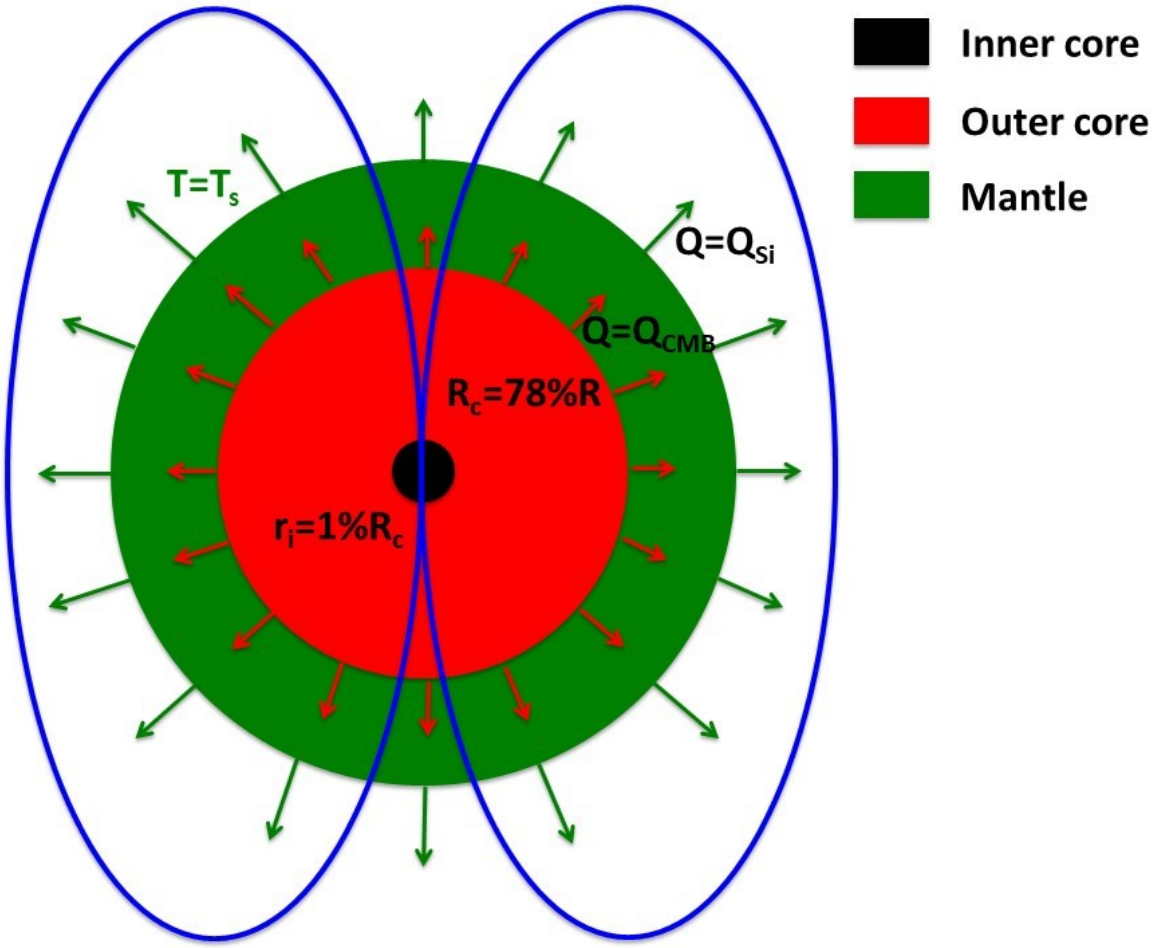

Figure 11: Heat flows as a function of the planetary radius for a fully solid planetary mantle. The black and grey lines represent the critical heat flow needed for a thermally driven dynamo for $k_c = 40$ and 4 W/m/K, respectively (Conditions 1 and 2, Eq. 31). The dark and light green lines represent the mantle heat flow in a conductive regime for $\kappa_{Si} = 4.32$ and 1.70 W/m/K, respectively (Eq. 35). Green triangles represent the critical planet size at which $Ra = Ra_c$, therefore corresponding to the minimum heat flow at the CMB, for mantle viscosity ranging from 10^{18} to 10^{22} Pa.s. Extrapolated values at $R = R_{Mercury} = 2440$ km are also represented with green circles for conductive heat transfers and red and pink squares for convective cases (eq. 36) with mantle viscosities indicated nearby. The red dashed line represents the critical value for Rem = 100 (Condition 3). At the left side of this line, a dynamo is unlikely. The likely zone for a planet radius capable of powering a dynamo is represented by the pink shaded area in case $\kappa_{Si} = 4.32$ W/m/K and $\kappa_{core} = 40$ W/m/K.

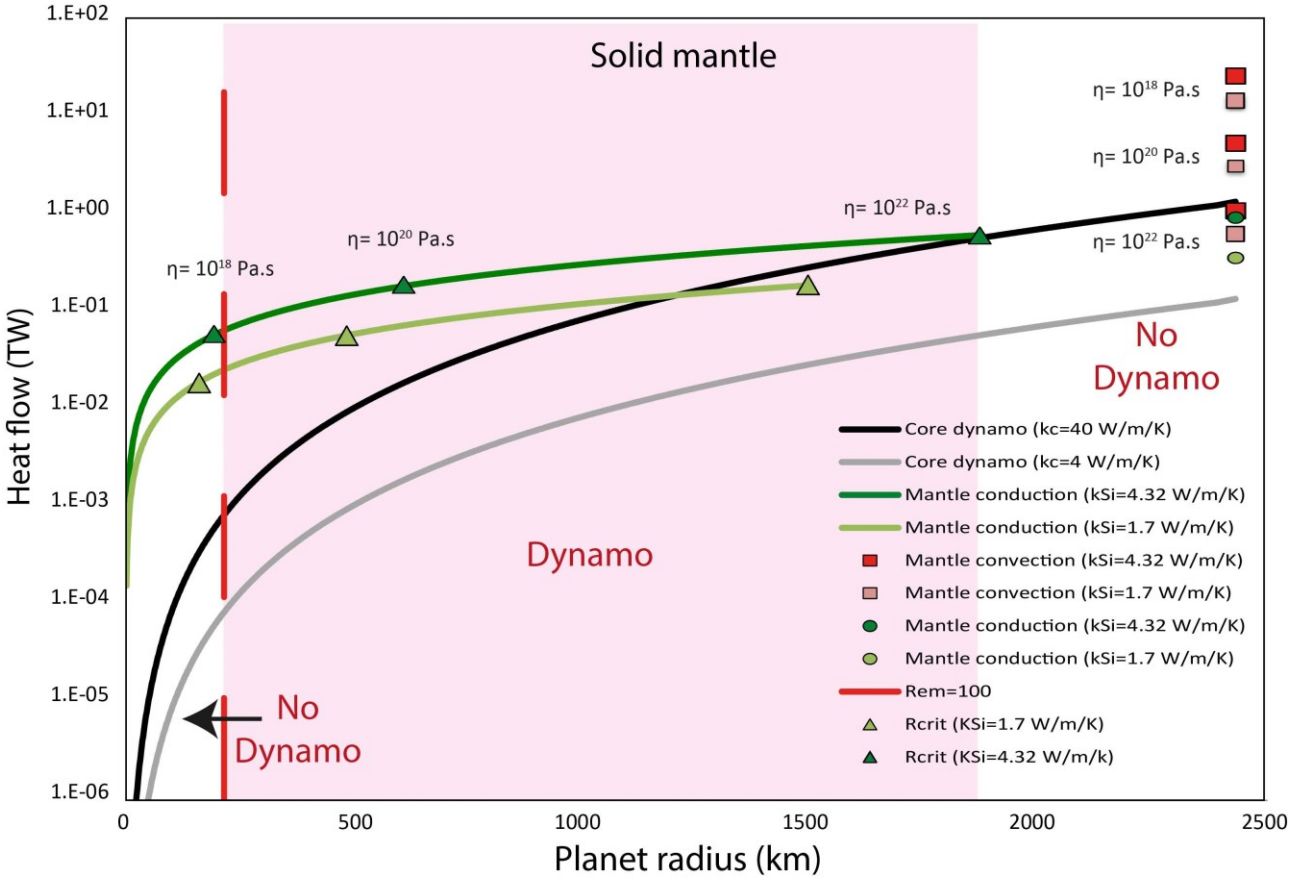

Figure 12.
Heat flows as a function of the planetary radius for a stagnant partially molten planetary mantle. The black and grey lines represent the critical heat flow for a thermally driven dynamo for k_c = 40 and 4 W/m/K, respectively (Conditions 1 and 2, Eq. 31). The dark and light green lines represent the mantle heat flow for κ_{Si} = 0.41 and 0.18 W/m/K, respectively (Eq. 35). Green triangles represent the critical planet size at which Ra = Ra_c, for mantle viscosity ranging from 10^{18} to 10^{22} Pa.s. Extrapolated values at R = $R_{Mercury}$ = 2440 km are also represented with green circles for conductive heat transfers and red and pink squares for convective cases (Eq. 36) with viscosities indicated nearby. The red dashed line represents the critical value for Rem = 100 (Condition 3). At the left side of this line, a dynamo is unlikely. The likely zone for a planet radius capable of powering a dynamo is represented by the pink shaded area in case κ_{Si} = 0.41 W/m/K and κ_{core} = 40 W/m/K.

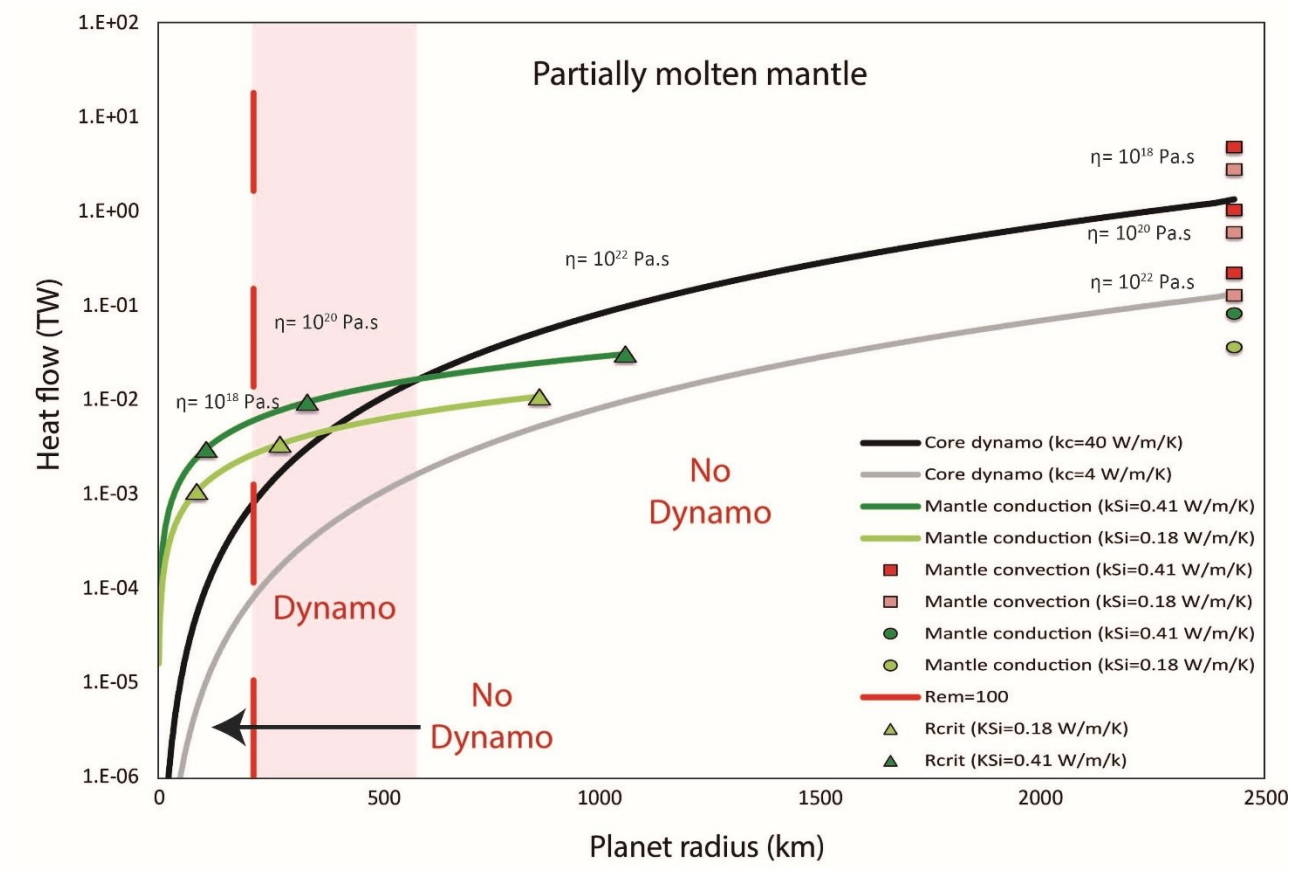

Table 1: Sum up of our Ansgtröm experiments with compositions, P-T ranges and associated parameters.

Run#	M662	M804	M807	M808	M836	M843	M844	M846	M847	M848	M850
Sample name	EPR-MORB	RP4-S2	DR07-S2	GD-S1	Haplo S1	ATHO-S1	DR11-S1	DR11-S2	RP4-S3	ATHO-S2	GD-S2
Composition	MORB	Peridotite	MORB	Rhyolite	haplobasalt	Rhyolite	MORB	MORB	Peridotite	Rhyolite	Rhyolite
Pressure (GPa)	2	2	2	2	2	2	2	2	2	2	2
length before (µm)	1400	1771.2	1061.9	1098.8	1124.6	1541. 9	1141.3	1048.2	1652.9	1045.1	1336.4
length after (µm)	1334.2	1780.0	-	1462.7	1213.2	1666.1	1287.6	1324.9	1643.6	1309.1	1287.4
expected Melting T° (K)	>1600	>1523	>1600	>1173	>1723	>1173	>1600	>1600	>1523	>1173	>1173
Max T (K)	1614	1681	1612	1146	1769	1219	1609	1284	1573	1325	1073
Run duration (min)	544	1089	953	480	832	800	834	439	767	761	610

Table 2: Fitting parameters obtained for the last cycle (C2-H3) of each experiment. Associated errors (1 STD) are given in parenthesis

Run#	a	b	c	R^2	R^2 adj
Peridotites					
M804	7.0e-4 (2.2e-4)	1.06 (0.06)	2.97e-10 (2.8e-11)	0.9659	0.9647
M847	8.8e-4 (7e-4)	1.15 (0.05)	2.37e-10 (1.8e-11)	0.9763	0.9750
Basalts					
M846	8.6e-6 (1.5e-5)	0.5 (0.3)	9.7e-11 (8.4e-11)	0.3933	0.3294
M662	7.2e-4 (1.8e-4)	1.20 (0.04)	1.01e-10 (4.1e-12)	0.9964	0.9962
M836	5.6e-5 (7.6e-5)	0.84 (0.23)	1.03e-10 (3.5e-11)	0.5748	0.5421
M844	1.9e-5 (1.1e-5)	0.63 (0.10)	8.0e-11 (2,3e-11)	0.9608	0.9556
M807	8.1e-4 (1.9e-4)	2.15 (0.04)	4.1e-11 (9e-12)	0.9933	0.9929
Rhyolites					
M850	1.9e-5 (3.5e-5)	0.70 (0.32)	1.7e-10 (7e-11)	0.2788	0.2101
M808	1.8e-2 (7e-2)	1.7 (0.7)	2.3e-10 (1.4e-10)	0.8003	0.7696
M848	1.4e-4 (7e-5)	0.91 (0.09)	1.3e-10 (2.0e-11)	0.9851	0.9826
M843	5.1e-3 (3.3e-3)	1.42 (0.11)	3.18e-10 (3.6e-11)	0.9715	0.9684

Table 3: Thermal diffusivities and conductivities retrieved for our samples at low and high temperatures for solids, above Tg and/or melting temperature (indicated for each group) for melts and partially molten samples. Literature estimates are also provided on the bottom part: "Xu" refers to polycrystalline olivine (dunite) measurements performed at ambient pressure (Xu et al., 2004). "Per06" refers to average values from 3 oriented (100, 010, 001) single crystal measurements at room pressure (Pertermann and Hofmeister, 2006) and some dunite values are also available in the same study. "Beck78" refers to Dunite measurements performed at 2 GPa (Beck et al. 1978). Regarding melts, literature data are taken from Hofmeister et al. (2009), Di: diopside, An : anorthite, Fk : orthose, Ab : albite. Finally, data from a few rhyolites Ncar, NCr and SCE are selected from Romine et al. (2012). When literature data are available in the form of thermal diffusivities, their conductivities are obtained using either the Cp and ρ provided in the source study or from our own parameters if not available (see Supplementary Materials).

SAMPLE NAME	Temperature range	Melt fraction	STD	κ	STD	D	STD
		%	%	W/m/K	W/m/K	m²/s	m²/s
SOLIDS							
M804	LT < 400K	0	0	4.32	0.48	1.66E-06	2.05E-09
M847	LT < 400K	0	0	3.28	0.37	1.26E-06	3.34E-09
M804	HT >1200 K	0	0	2.29	0.26	7.33E-07	1.80E-09
M847	HT >1200 K	0	0	1.70	0.19	5.39E-07	6.13E-10
Partially molten samples							
M804	>1300 K	6.44	2.98	1.19	0.16	3.74E-07	2.55E-08
M847	>1300 K	23.31	2	0.93	0.10	2.92E-07	1.22E-10
MELTS							
BASALTS	MELT >1200K						
M807	>1224 K	100	0	0.34	0.02	1.84E-07	1.51E-09
M844	>1326 K	100	0	0.18	0.01	9.52E-08	2.96E-11
M662	>1450 K	100	0	0.22	0.16	1.20E-07	8.73E-08
M846	>1200 K	100	0	0.22	0.12	1.16E-07	6.47E-08
M836	1180 K	100	0	0.28	0.02	1.51E-07	6.94E-10
rhyolite	Melt >1000 K						
M850	> 1080 K	100	0	0.31	0.03	3.05E-07	2.42E-08
M808	>1060 K	100	0	0.35	0.03	3.47E-07	5.95E-10
M848	>1260 K	100	0	0.39	0.03	3.91E-07	6.21E-10
M843	> 1280 K	100	0	0.41	0.03	4.16E-07	2.36E-10
literature							
SOLIDS							
Olivine Xu 0 GPa LT	294	0	0	4.15	0.42	4.10E-06	2.05E-07
Olivine Xu 0 GPa HT	1377	0	0	1.95	0.19	5.00E-07	2.50E-08
Olivine Hof 16 AVG	300 K	0	0	6.37	0.64	2.37E-06	4.75E-08
Olivine Hof AVG16	>1500 K	0	0	2.76	0.28	7.01E-07	1.40E-08
Dunite Per 06	300 K	0	0	4.22	0.42	1.57E-06	3.15E-08
Dunite 2 Per 06	300 K	0	0	5.35	0.53	1.99E-06	3.99E-08
Dunite Per 06	>1500 K	0	0	1.65	0.17	4.20E-07	8.40E-09
Dunite 2 Per 06	>1500 K	0	0	2.23	0.22	5.65E-07	1.13E-08
Dunite Beck 78 2Gpa	300 K	0	0	4.15	0.42		
Dunite Beck 78 2Gpa	300 K	0	0	5.49	0.55		
Dunite 2 GPa Dry Z19	300 K	0	0	5.21	0.26	1.71E-06	8.55E-08
Dunite 2 GPa 0.08% wt H_2O Z19	300 K	0	0	4.86	0.24	1.59E-06	7.95E-08
Melts							
Di Hof 09	>1140 K	100	0	1.25	0.13	2.89E-07	5.79E-09
An Hof 09	>1290 K	100	0	1.45	0.15	3.58E-07	7.16E-09
Fk Hof 09	>1245 K	100	0	1.45	0.15	4.75E-07	9.50E-09
Ab Hof 09	>1300 K	100	0	1.60	0.16	4.99E-07	9.99E-09
Rhyolite/obsidian							
Ncar Ro 12	1384	100	0	1.53	0.15	5.17E-07	1.03E-08
NCr Ro 12	1365	100	0	1.50	0.15	5.08E-07	1.02E-08
SCE Ro 12	1464	100	0	1.59	0.16	5.31E-07	1.06E-08

1354 **Table 4**: Typical parameter values for heat fluxes calculations displayed in Figures 11 and 12.

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κ_c	Core thermal conductivity	4-40	W m^{-1} K^{-1}
α_c	Core thermal expansion	$7.7x10^{-5}$	K^{-1}
$C_{p,c}$	Core heat capacity	800	J kg^{-1} K^{-1}
υ_c	Core magnetic diffusivity	2	m^2 s^{-1}
μ_c	Core magnetic permeability	4π 10^{-7}	H m^{-1}
ρ_c	Core density	7500	kg m^{-3}
B	Average magnetic field strength	Eq. 3	T
R	Planet radius		m
R_c	Core radius	77% R	m
r_i	Inner core radius	1% R_c	m
G	Gravitational constant	$6.67x10^{-11}$	m^3 kg^{-1} s^{-2}
κ_{Si}	Silicates thermal conductivity	4.32-1.70	W m^{-1} K^{-1}
κ_{Si}	Molten silicates thermal conductivity	0.18-0.41	W m^{-1} K^{-1}
α_{Si}	Silicates thermal expansion	$1x10^{-5}$	K^{-1}
$C_{p,Si}$	Silicates heat capacity	1000	J kg^{-1} K^{-1}
T_s	Surface temperature	500	K
δ_{Si}	Mantle thickness	33% R	m

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