

Ultimate permissible additional hogging of a brick wall during the reconstruction of a historical building

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Abstract. The paper analyzes the possible development of an approach limiting additional deformations of the base of a building during reconstruction. We consider the ultimate permissible value of additional relative hogging in a brickwork wall without reinforcement $(f/L)_{ad,u}$, which is important for the solution of tasks on the reconstruction of historical buildings. The ultimate values of tensile deformations in a wall can serve as a safety criterion for uneven building settlements. The use of this criterion makes it possible to set more precise values $(f/L)_{ad,u}$ for a brick wall as compared with the values used in Construction Regulations SP 22.13330.

1 Introduction

Assessing ultimate permissible deformations of building bases is a common task for specialists in the field of building structures as well as bases and foundations.

Speaking of the historical development of St. Petersburg, the solution of this task is highly relevant for buildings with a wall structural system made of brickwork without reinforcement since it makes it possible to assess permissible additional impacts on buildings, e.g. when they are adapted for modern use.

2 Literature review

A large number of widely known works study and assess ultimate settlements of buildings, including those made of brickwork without reinforcement [1-14]. Ulitsky & Shashkin [15] proposed criteria of “ultimate additional settlements of buildings” with various structural layouts, and categories of technical condition to be used to solve safety tasks during reconstruction. Later, these criteria were adopted in Construction Regulations SP 22.13330. This approach can be further developed by specifying the limits of ultimate additional settlements of buildings taking into account more detailed characteristics of the structural layout.

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3 Materials and methods

When assessing settlements, two types of the combined deformation of the building and the base can be considered: hogging and sagging. The paper is restricted to the analysis of ultimate hogging deformations of a building.

There are various approaches to regulating the deformations of structures and displacements of foundations that are used in different national standards. Their analysis was performed by Paramonov & Popielski [16]. The current version of Construction Regulations SP 22.13330 for high-rise frameless buildings (greenfield development projects) limits three parameters of base deformation, which were described by pioneers in the field of settlement regulation [8]:

- 1) ultimate maximum s_{max} or average settlement of foundations s_u ;
- 2) ultimate relative difference of settlements (rises) of the base under two foundations $(\Delta s/L)_u$ (L is the distance between the foundations) (slope);
- 3) ultimate relative hogging or sagging of buildings $(f/L)_u$ (f is the hog/sag, L is the length of a definitely deflected part of the structure) (relative deflection).

Thus, the only regulated value of deformation along the building wall is the value of relative hogging or sagging. The ultimate value of this parameter for a frameless building (when considering wall hogging in a greenfield facility) is set equal to 50% of the ultimate relative difference of settlements $(\Delta s/L)_u$ and in the case of a brickwork building without reinforcement it will be as follows:

$$(f/L)_u = (\Delta s/L)_u \cdot 50\% = 0.002 \cdot 50\% = 0.001.$$

The value of ultimate additional relative hogging $(f/L)_{ad,u}$ during the reconstruction of a historical building is not regulated in Construction Regulations SP 22.13330 but, similarly to the ultimate value of relative hogging for a greenfield facility, it shall be 50% of $(\Delta s/L)_{ad,u}$. During the reconstruction of a historical building, $(\Delta s/L)_{ad,u}$ amounts to 0.0009 for a building of category 2 and 0.0007 for a building of category 3 (the categories are assigned according to the technical condition).

Thus, for a historical building of category 2:

$$(f/L)_{ad,u} = 0.0009 \cdot 50\% = 0.00045.$$

For a building of category 3:

$$(f/L)_{ad,u} = 0.0007 \cdot 50\% = 0.00035.$$

Let us consider an analytical solution of the problem on the determination of the ultimate value of relative hogging in a brick wall.

An analytical model of a brick wall is represented by a beam with height H and length L , where settlement results in hog f and two types of internal forces: transverse force and bending moment.

According to the general rules of materials resistance under bending:

$$\epsilon_{tensile,max} = (0.5 \cdot H)/R,$$

where $\epsilon_{tensile,max}$ is the relative elongation of the bottom longitudinal fiber of the beam wall if the neutral axis is in the middle of the wall height; H is the wall height; $1/R$ is the curvature of the wall segment under consideration (m⁻¹), where R is the radius of curvature (m). Hence:

$$R_{ult} = 0,5 \cdot H / \epsilon_{tensile,u} \tag{1}$$

where R_u is the ultimate radius of curvature, at which cracks occur in the wall section; H is the wall height; $\epsilon_{tensile,u}$ is the ultimate relative tensile deformation of the brickwork, which, according to different sources, is within 0.03–0.09%.

Upon approximation of settlements in a building base with an arc having the radius of curvature R_{ult} :

$$f_u = R_u - (R_u^2 - (0,5 \cdot L)^2)^{0,5} \tag{2}$$

where f_u is the ultimate wall hogging, at which cracks occur in the most tensile fiber of its section.

The ultimate relative hogging is equal to the following:

$$(f/L)_u = f_u/L \tag{3}$$

According to Burland, for a brick building without reinforcement, at the deformation capacity of walls $L/H > 2$, crack formation caused by brickwork tension due to bending deformations will be a factor determining the ultimate values of the relative building hogging. With more rigid walls, at $L/H < 2$, shear will be the determining factor for a brick building.

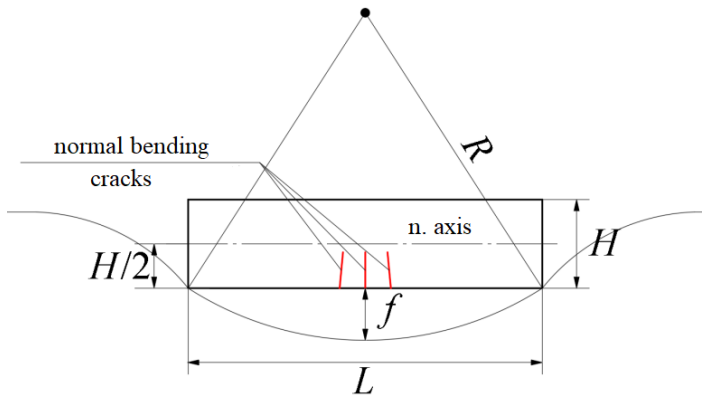


Fig. 1. Analytical model of a brick wall on a base under consideration.

During reconstruction, cracks are usually reinforced with mortar injection. In this case:

$$\epsilon_{tensile,ad,u} = \epsilon_{bt2},$$

where $\epsilon_{tensile,ad,ult}$ is the ultimate additional relative tensile deformation of brickwork after injection; $\epsilon_{bt2} = 0.027\text{--}0.036\%$ is the ultimate relative deformation of concrete at continuous loading pursuant to Construction Regulations SP 63.13330.

Thus, taking into account Eqs. (1), (2), and (3), $\epsilon_{tensile,ad,u}$ determines the ultimate value of additional hogging $f_{ad,u}$ and the ultimate additional relative hogging $(f/L)_{ad,u}$ based on the condition of crack formation in the areas of existing injected cracks.

Let us consider the results of f_u and $(f/L)_u$ calculation for a brick wall without reinforcement at different L/H dimensions using Eqs. (1)–(3) at $\epsilon_{tensile,u} = 0.027\%$ and $\epsilon_{tensile,u} = 0.05\%$, as well as the equations proposed in various literature sources.

The analysis will be restricted to the ultimate values of relative hogging, and tensile deformations at a normal section due to wall deflection will serve as acceptance criteria, i.e. we will consider walls at $L/H > 2$.

4 Results

Figure 2 shows curves $(f/L)u - L/H$.

The diagram also has points representing the data on field measurements $(f/L)u - L/H$ for a number of buildings according to the results of “classic” works [5, 8].

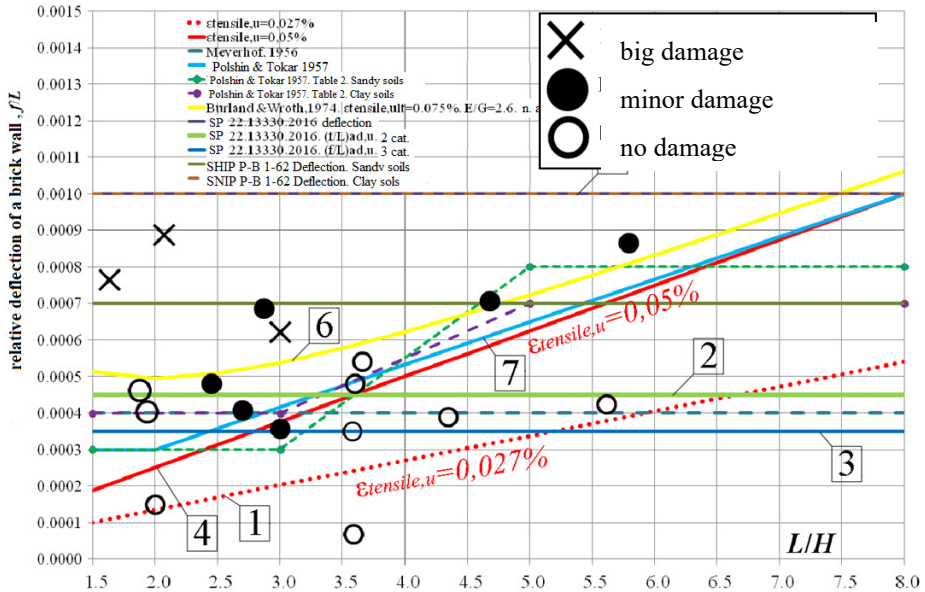


Fig. 2. Diagrams $(f/L)u - L/H$.

For the case of reconstruction, it is interesting to compare curve 1 constructed based on Eqs. (1)–(3) at $\epsilon_{\text{tensile},u} = 0.027\%$ with the values $(f/L)_{ad,u}$ proposed in the current regulations for historical buildings of categories 2 and 3 (curves 2 and 3).

As it can be seen, the values $(f/L)u$, obtained by Eqs. (1)–(3) (curves 4 and 1), as well as by using more complex functions ([4] — curve 6; [8] — curve 7) increase with an increase in L/H . The current version of the regulations uses a more simplified approach and the rigidity of a brick wall is not accounted for — $(f/L)u$ (curve 5) and $(f/L)_{ad,u}$ (curves 2 and 3) are parallel to the X axis.

According to curves 1, 2, 3, the values $(f/L)_{ad,u}$ are less than $(f/L)u$ (curves 4, 5, 6, 7), which is obvious. It can be seen that the use of the regulatory values $(f/L)_{ad,u}$, at $L/B < 5$ according to curve 3 and at $L/B < 6.5$ according to curve 2 will result in the estimated values $\epsilon_{\text{tensile},\text{max}} > 0.027\%$. This means that repeated cracks may occur in the areas of brickwork injection.

Figure 3 shows curves $f_{ad,u} - L2/H$ constructed based on Eqs. (1)–(3) at $\epsilon_{\text{tensile},u} = 0.05\%$ and $\epsilon_{\text{tensile},u} = 0.027\%$. The diagram has points $f_{ad,u}$ (pursuant to Construction Regulations SP 22.13330) for a wall of $L = 30$ m of categories 2 and 3.

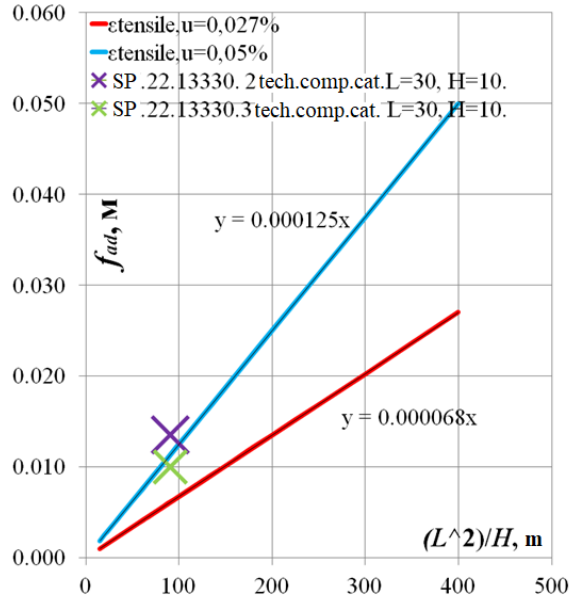


Fig. 3. Diagrams $f_{ad,u}$ – L^2/H according to Eqs. (1)–(3) at $\epsilon_{tensile,u} = 0.05\%$ and $\epsilon_{tensile,u} = 0.027\%$.

Figure 4 shows curves $f_{ad,u}$ – L pursuant to Construction Regulations SP 22.13330 for buildings of categories 2 and 3. The values $f_{ad,u}$ cannot exceed the values of maximum additional settlements $\Delta S_{max,ad,u}$ for buildings of respective categories, which correspond to the horizontal sections of the curves in Figure 4. Figure 4 also has points $f_{ad,u}$ plotted for a wall of $L = 30$ m, $H = 10$ m at $\epsilon_{tensile,u} = 0.027\%$ and $\epsilon_{tensile,u} = 0.05\%$ according to Eqs. (1)–(3).

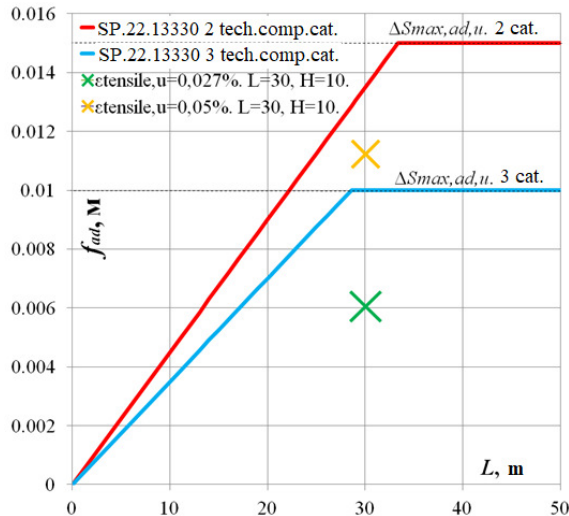


Fig. 4. Diagrams $f_{ad,u}$ – L pursuant to Construction Regulations SP 22.13330 for buildings of categories 2 and 3.

The diagrams show that pursuant to Construction Regulations SP 22.13330 for a building of category 3, $f_{ad,u} = 0.010$ m, and for a building of category 2, $f_{ad,u} = 0.0135$ m. The value $f_{ad,u}$, obtained by Eqs. (1)–(3) at $\epsilon_{tensile,u} = 0.027\%$, equals 0.006 m.

The analysis of these diagrams shows that the limitations for $f_{ad,u}$ and $s_{maxad,u}$ used in the regulations will not make it possible to reliably guarantee the absence of cracks in the wall structure in the case of the building under consideration.

5 Discussion

In the case of rather strict limitations regarding the value of additional settlement of a building during reconstruction $s_{maxad,u}$, the regulatory values of the ultimate additional relative hogging $(f/L)_{ad,u}$ and the ultimate value of additional hogging $f_{ad,u}$ will not always result in “safety margin” of the reconstructed building.

Let us consider the numerical calculation of a reconstructed building with a wall of $L = 30$ m, $H = 10$ m.

Figure 5 shows the results of calculating the values of additional settlement, which do not exceed the regulated values for a building of category 2:

$$\begin{aligned} s_{maxad} &= s_{maxad,u} = 0.015 \text{ m}; \\ f_{ad} &= 0.01 \text{ m}; \\ (f/L)_{ad} &= (0.015 - 0.005) / 30 = 3 \cdot 10^{-4} \leq (f/L)_{ad,u} = 4.5 \cdot 10^{-4}. \end{aligned}$$

The reverse calculation by Eqs. (1)–(3) will result in $\epsilon_{tensile,max} = 0.044\%$. This value is close to the result of the numerical calculation: 0.045% (Fig. 5b) and exceeds ϵ_{bt2} , thus the existing cracks of the injected brickwork may open.

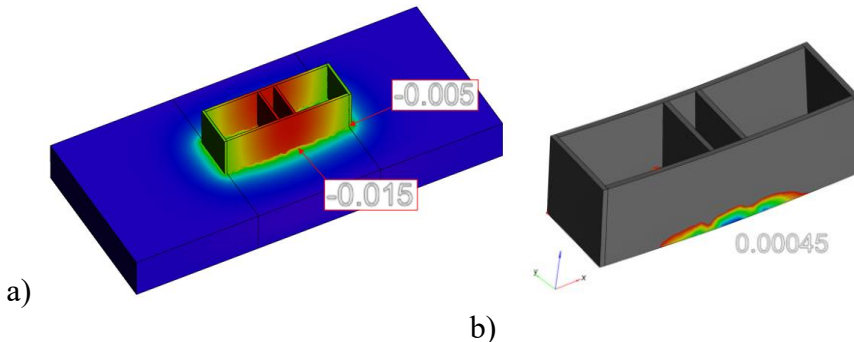


Fig. 5. Building analysis with FEM-models: a) vertical displacements, m; b) normal deformations ex. The area where $\epsilon_x \geq \epsilon_{bt2}$ is marked.

Figure 6 shows the results of calculating the values of additional settlement, which do not exceed $s_{maxad,u}$ for a reconstructed historical building: $s_{maxad} = 0.022$ m.

This results in the following:

$$\begin{aligned} f_{ad} &= 0.01 \text{ m}. \\ (f/L)_{ad} &= (0.022 - 0.016) / 30 = 2 \cdot 10^{-4}. \end{aligned}$$

According to Eqs. (1)–(3) at such values of L, H, and f: $\epsilon_{\text{tensile,max}} = 0.027\%$. This value is close to the result of the numerical calculation: 0.026% (Fig. 6b) and does not exceed ϵ_{bt2} , thus, no cracks shall occur in the injected brickwork and such additional settlements can be considered safe.

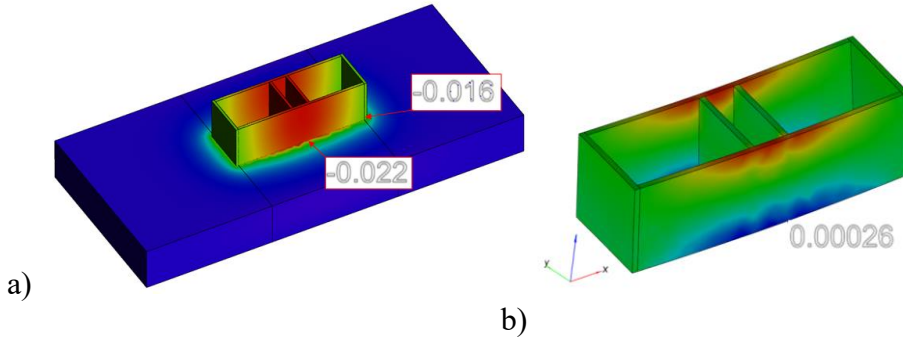


Fig. 6. Building analysis with FEM-models: a) vertical displacements, m; b) normal deformations ϵ_x .

6 Conclusion

In geotechnical analysis during the reconstruction of brick historical buildings, the permissible values of additional settlements shall be established based on the detailed analysis of the stress-strain state of the building. In a number of cases, the use of the ultimate values proposed in Construction Regulations SP 22.13330 may not guarantee the absence of cracks in brickwork. In such an event, ultimate tensile deformations of brickwork can serve as a criterion of safe settlements. The use of this criterion makes it possible to set more precise values $(f/L)_{ad,u}$ depending on the actual structure of the walls according to the results of analytical and numerical calculations.

References

1. L. Bjerrum, *Allowable settlement of structures. Proceedings of the European Conference on Soil Mechanics and Foundation Engineering Wiesbaden*, Deutsche Gesellschaft für Erd und Grundbau (1963).
2. S.J. Boone, *J. of Geotech. and Environm. Eng.* **122(11)**, 886-896 (1996).
3. M.D. Boscardin, E.J. Cording, *J. of Geotech. Eng.* **115(1)**, 1-21 (1989).
4. J.B. Burland, C.P. Wroth, *Settlement of buildings and associated damage. SOA review, Conference on settlement of structures* (Cambridge, 1974).
5. J.B. Burland, B.B. Broms, V.F.B. De Mello, *Behaviour of Foundations and Structures. Ninth International Conference on Soil Mechanics and Foundation Engineering, Tokyo, Japan*, pp. 495-546 (1977).
6. R. Grant, J.T. Christian, E.H. Vanmarcke, *J. of Geotech. Eng. Division* **100(GT 9)**, 973-991 (1974).
7. G.G. Meyerhof, 1953. *Some recent foundation research and its application to design. The structural Engineer* 31(June), pp. 151-167 (1953).
8. D.E. Polshin, R.A. Tokar, *Maximum allowable non-uniform settlement of structures. Proceedings 4th Int. Conference On Soil Mechanics and Foundation Engineering. London, UK, vol.1, Butterworth's scientific* (1957).

9. W.J. Rankin, 1988. Eng. Geology Special publication, Geological Society **5**, 79-92 (1988).
10. A.G. Shashkin, et al., *Analysis of causes of deformations in historic buildings on weak clay soils*, Geotechnics Fundamentals and Applications in Construction: New Materials, Structures, Technologies and Calculations. Proceedings of the International Conference on Geotechnics Fundamentals and Applications in Construction: New Materials, Structures, Technologies and Calculations «GFAC 2019». Saint-Petersburg. Vol. 2. pp. 329-334, (2019).
11. A.W. Skempton, D.H. McDonald, Proceedings Institution of Civil Engineers part III **5(50)**, 727-768 (1956).
12. V.M. Ulitsky, et al., *Soil-structure interaction effects. In: Geotechnical Engineering for Infrastructure and Development*, Proceedings of the XVI European Conference on Soil Mechanics and Geotechnical Engineering, ECSMGE 2015 16, Geotechnical Engineering for Infrastructure and Development, pp. 4191-4196. (2015)
13. V.A. Vasenin, Soil Mechanics and Foundation Eng. **4**, 2–7 (2013).
14. H.E. Wahls, ASCE, J. of Geotechnical Eng. Division **107(GT 11)**, 1489-1505 (1981).
15. V.M. Ulitsky, A.G. Shashkin, Geotechnical support for urban reconstruction (M.: Ed. ACB, 1999).
16. P. Popielski, A. Domska, V.N. Paramonov, Urban development and geotechnical construction. **14**, 215-226 (2012).