SHIFTING CAPSULE NETWORKS FROM THE CLOUD TO THE DEEP EDGE

A PREPRINT

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Abstract

Capsule networks (CapsNets) are an emerging trend in image processing. In contrast to a convolutional neural network, CapsNets are not vulnerable to object deformation, as the relative spatial information of the objects is preserved across the network. However, their complexity is mainly related to the capsule structure and the dynamic routing mechanism, which makes it almost unreasonable to deploy a CapsNet, in its original form, in a resource-constrained device powered by a small microcontroller (MCU). In an era where intelligence is rapidly shifting from the cloud to the edge, this high complexity imposes serious challenges to the adoption of CapsNets at the very edge. To tackle this issue, we present an API for the execution of quantized CapsNets in Arm Cortex-M and RISC-V MCUs. Our software kernels extend the Arm CMSIS-NN and RISC-V PULP-NN to support capsule operations with 8-bit integers as operands. Along with it, we propose a framework to perform post-training quantization of a CapsNet. Results show a reduction in memory footprint of almost 75%, with accuracy loss ranging from 0.07% to 0.18%. In terms of throughput, our Arm Cortex-M API enables the execution of primary capsule and capsule layers with medium-sized kernels in just 119.94 and 90.60 milliseconds (ms), respectively (STM32H755ZIT6U, Cortex-M7 @ 480 MHz). For the GAP-8 SoC (RISC-V RV32IMCXpulp @ 170 MHz), the latency drops to 7.02 and 38.03 ms, respectively.

Keywords capsule networks · capsule network quantization · edge · cloud · CMSIS-NN · PULP-NN

1 Introduction

Convolutional layers have shown an impressive capacity to extract features - edges and shapes - from image pixels [Sabour et al., 2017, Kwabena Patrick et al., 2019, El Alaoui-Elfels, Omaima and Gadi, Taoufiq, 2021]. However, to reduce the dimension of feature maps, and consequently the number of parameters to learn, convolutional layers are typically connected through pooling layers in a convolutional neural network (CNN). Pooling layers take the most important features present in a region of the feature map generated by a convolution and pass those features to the following layer. However, this comes at the cost of decreased capacity to recognize pose and object deformation as the relative spatial information of the features is lost across the network [Sabour et al., 2017, Kwabena Patrick et al., 2019, El Alaoui-Elfels, Omaima and Gadi, Taoufiq, 2021]. Furthermore, CNNs have shown to be vulnerable to adversarial examples, i.e., inputs to a machine learning (ML) model that an attacker intentionally designs to compromise the

integrity of the decision in a process similar to an optical illusion [Su et al., 2019, Sadeghi et al., 2020]. To tackle these issues, Sabour et al. [2017] proposed a new class of deep learning (DL) architectures, named capsule neural networks (CapsNets), to extract and classify features from images, while preserving and learning spatial information.

The core unit of a CapsNet is a capsule, a group of neurons organized as vectors. Each vector dimension represents a different parameter of the same object in the image [Sabour et al., 2017] and the length of the vector represents the probability of the image containing the object. To date, there are four main variants of CapsNet: (i) transforming auto-encoders [Hinton et al., 2011], (ii) routing by agreement between capsules [Sabour et al., 2017], (iii) expectation-maximization routing capsules [Hinton et al., 2018], and (iv) stacked capsule autoencoders [Kosiorek et al., 2019]. However, the most prominent remains the routing by agreement between capsules [Sabour et al., 2017], which is the target on this work. Dynamic routing is used to calculate a series of coefficients that determine the probability of an object in a lower capsule layer, being part of an object represented in a higher capsule layer [Sabour et al., 2017]. In contrast to CNNs, CapsNets are equivariant, learning proportion and pose changing [El Alaoui-Elfels, Omaima and Gadi, Taoufiq, 2021]. CapsNets already outperform CNNs in some healthcare [Toraman et al., 2020] and automation mechanisms [Dinesh Kumar, 2018, Pari S. et al., 2019, Wang et al., 2018, Katebi et al., 2019, Kwabena Patrick et al., 2019, Zhang et al., 2020].

Despite being promoted as the next ground-breaking algorithm in DL [Kwabena Patrick et al., 2019], CapsNets in their original form are computationally intensive in terms of memory requirements (bandwidth and size) and latency [Marchisio et al., 2020a,b, 2021, Zhang et al., 2020, 2021, Park et al., 2020, Kakillioglu et al., 2020]. For the same dataset, the original CapsNet has a ratio of multiply-accumulate (MAC) operations per memory near 100x higher than AlexNet [Marchisio et al., 2020a], which is also a heavy CNN. In an era where concerns with cloud and internet infrastructure are disrupting the shift of AI to the deep edge [Stoica et al., 2017, Lai et al., 2018, Véstias et al., 2020, Li et al., 2018], the feasibility of CapsNets is still mainly confined to powerful cloud servers. To shift AI to the edge, researchers have been developing mechanisms for compressing artificial neural networks (ANNs) and CNNs, discarding floating-point representation, and adopting a lighter fixed-point representation [Lai et al., 2018, Garofalo et al., 2020]. If the potential of fixed-point computation in ANNs and CNNs is already known and ultimately led to the development of APIs tailored for the execution of quantized neural networks in low-end MCUs [Lai et al., 2018, Garofalo et al., 2020] (e.g., Arm Cortex-M and RISC-V), the feasibility of CapsNets under such constraints is still unknown.

To fill this gap, we evaluate the feasibility of CapsNets on resource-constrained platforms, powered by small MCUs targeted for intelligent IoT edge nodes. For this purpose, we extended the software kernels from CMSIS-NN [Lai et al., 2018] and PULP-NN [Garofalo et al., 2020] to support the deployment of CapsNets on Arm Cortex-M and RISC-V MCUs, respectively. We extended these APIs with functions to support capsule operations with int-8 data and evaluated their feasibility in terms of latency, accuracy penalty, and memory footprint reduction. As ML models are typically trained using floating-point precision, we developed a toolchain to perform post-training quantization of CapsNets developed in TensorFlow. Results show that this framework can reduce the memory footprint of a CapsNet by almost 75%, with a maximum accuracy loss of 0.18%. Our API was tested in three different Arm Cortex-M cores, i.e., STM32L4R5ZIT6U (Cortex-M4 @ 120 MHz), STM32H755ZIT6U (Cortex-M7 @ 480 Mhz), and STM32L552ZET6QU (Cortex-M33 @ 110 MHz). For the fastest MCU (STM32L4R5ZIT6U), our API enables the execution of primary capsule and capsule layers with medium-sized kernels in just 119.94 and 90.60 milliseconds, respectively. The API for the RISC-V RV32IMCXpulp architecture was tested on a Gapuino v1 board. For an octa-core setting at 170 MHz, the latency of medium-sized primary capsule and capsule layers dropped to 7.02 and 38.03 milliseconds, respectively. Our work is open-source and available online ¹. We believe our work will open a path in the application space of CapsNets, mainly in areas till now only explored by CNNs [Costa et al., 2019, Lu et al., 2021] and encourage the development of lighter CapsNet architectures.

In summary, we make the following contributions: (i) the first public and open-source software kernels for the execution of CapsNets in Arm Cortex-M and RISC-V (RV32IMCXpulp) MCUs (section 3); (ii) a public and open-source framework to quantize CapsNets from floating-point precision to int-8, compliant with the Qm.n data format, used by Arm CMSIS-NN and RISC-V PULP-NN libraries (section 4); (iii) the first public evaluation of the feasibility of CapsNets in resource-constrained MCUs featuring Arm Cortex-M and RISC-V (RV32IMCXpulp) cores (section 5).

¹https://gitlab.com/ESRGv3/q7-capsnets.git

2 Background

2.1 Capsule Networks (CapsNets): Overview and Evolution

The first concept of capsules applied in DL was introduced in 2011 by Hinton et al. [2011] to tackle the lack of equivariance affecting CNNs and to show how neural networks can be used to recognize pose. Capsules were described as sets of neurons, organized as vectors, and each capsule represented a given object of the input image. In contrast to a CNN, in which layers take as input/output scalars, capsules deal with vectors. They encapsulate posture information (position, direction, etc.) with other instantiation parameters (width, height, etc.) that together represent an object or object part. Each layer in a CapsNet is made up of a series of capsules and CapsNets follow a part-whole hierarchy. Capsules at one layer predict larger objects, represented by capsules at higher layers, via transformation matrices applied to their output vectors. For an object to be detected, capsules at a lower layer must agree in their spatial arrangement. This characteristic is highlighted in Figure 1. As observed, for the CapsNet in green, the pose of the mouth is not spatially aligned with the remaining parts of the face, resulting in a distorted human face to the human eye. As CapsNets learn the spatial relation of object parts, they can easily spot this distortion. In contrast, a traditional CNN would recognize the input image as a human face as CNNs learn the parts but not their spatial arrangement. Researchers have been proposing numerous CapsNet architectures since the proposal of the capsule concept in 2011. Here we review the most relevant architectures developed to date. For an overview of other architectures, we refer to works [Li et al., 2021, El Alaoui-Elfels, Omaima and Gadi, Taoufiq, 2021, Kwabena Patrick et al., 2019, Sun et al., 2022].

Transforming auto-encoders (TAEs) are the first CapsNet architecture [Hinton et al., 2011]. They were designed to encode the input image and regenerate it in the same original pose. TAEs differed from other auto-encoders as they were designed to explicitly learn the transformation matrix that represents the relation of one part of an image (e.g. eyes) to the position of other parts (e.g. nose). A TAE's capsule is composed of two distinct units: (i) recognition units and (ii) generative units. The recognition units were designed to compute the pose parameters and the probability that the object represented by the capsule is present in the input image. The generative units take this data as input to reconstruct the object. The major bottleneck of TAEs is that they require the transformation matrix to be supplied externally.

The previous capsule structure was updated in 2017 for classification tasks. Sabour et al. [2017] succeeded in implementing a CapsNet with state-of-the-art accuracy of 99.75% on MNIST and triggered the hype around CapsNets. This architecture features a convolutional layer, a primary capsule layer, and a class capsule layer. The convolutional layer is intended to extract the most relevant features of the input image, tackling the need to externally provide the pose matrix of the objects of interest. The primary capsule layer is the first capsule layer following the convolutional layer. Primary capsules have a convolutional kernel and encode the instantiation parameters of the lower-level objects of the input image. The last layer is the class capsule layer, which makes the final prediction. Capsules at different layers connect through a dynamic routing algorithm, which computes the probability of the object represented by a capsule in layer L being part of the objects represented by the capsules in layer L + 1. Sabour et al. [2017] updated the capsule structure in this CapsNet architecture. Capsules are still a group of neurons that output a vector with instantiation parameters. However, Sabour et al. [2017] gave meaning to the length of the vector - it represents the probability of the object being present in the input image. This CapsNet architecture is the most supported by the research community and is the focus of this work. Section 2.2 describes it in detail.

In 2018, Hinton et al. [2018] proposed to replace the input and output vectors of capsules with matrices and updated the dynamic routing with an expectation-maximization algorithm. Instead of a pose vector, each capsule comprises a 4x4 pose matrix and an activation parameter that represents the probability of the object is present in the input image. This



Figure 1: Basic intuition behind CapsNets

tackles two of the biggest bottlenecks of the previous CapsNet architecture. Firstly, representing capsules with matrices of n elements instead of vectors reduces the number of parameters in transformation matrices between capsules from n^2 to n. Secondly, it avoids the use of a *squash* function to shrink the vectors to a maximum length of 1, which prevents the existence of any sensible objective function in the network. The new dynamic routing considers every capsule in a higher layer represented by a Gaussian distribution, defined by a mean and a standard deviation, and the capsules in a lower layer as the data points to be mapped to the Gaussian distributions. This algorithm encompasses two phases: (i) the assignment of data points to clusters (expectation) and (ii) the update of the centroids giving the assignments (maximization). This architecture achieved an accuracy of 98.2% on the smallNORB dataset.

The previous CapsNet architecture was updated in 2019 by Kosiorek et al. [2019] for unsupervised learning applications. In addition to the pose matrix and activation parameter, this newer version of capsules (stacked capsule autoencoders) features a vector that represents other properties than pose, such as deformation, velocity, or color. While previous versions of capsules predict the pose of a parent capsule from the pose of the lower-layer capsules, this new architecture works in the opposite direction. A capsule that represents an object at one layer, predicts the pose of the parts represented in the lower layers. Consequently, there is no more need for iterative routing at inference time as every part is explained as a mixture of predictions from different objects. Stacked capsule autoencoders feature two main parts: (i) part capsule autoencoder and (ii) object capsule autoencoder. Stacked capsule autoencoders achieved a state-of-the-art accuracy for unsupervised classification on SVHN (55%) and MNIST (98.7%).

2.2 Capsule Networks (CapsNets) with Dynamic Routing

Dynamic routing between capsules was the first CapsNet architecture proposed for classification tasks. Its successor, matrix capsules with expectation-maximization routing, promised to reduce the number of parameters to learn and to deliver better results in more complex datasets like smallNORB. Nevertheless, at the time of accomplishment of this work, the first version still got the most valuable support from the research community. Furthermore, it is the only version whose original implementation is publicly available ². Figure 2 depicts its general architecture.



Figure 2: General architecture of a CapsNet with dynamic routing between capsules

A CapsNet based on dynamic routing between capsules starts with a convolutional layer, used to extract the most relevant features of the input image. In their model tuned for the MNIST dataset, Sabour et al. [2017] employed 256 convolution kernels with dimensions 9x9 and a stride of 1, followed by a *rectified linear unit (ReLU)* activation. The activated feature map is then sent to every capsule in the primary capsule layer. The primary capsule layer is the first capsule layer of the network and is where the inverse of the rendering process starts. Primary capsules have a convolutional kernel and are designed to refine the objects of interest identified by the previous convolutional layer and to determine the instantiation parameters, including spatial information. Each primary capsule is a vector, where each dimension represents a given parameter of the object. The length of the output vector represents the probability of the object is present in the input image. For this purpose, the output of each capsule is squashed by the non-linear activation detailed in Equation 1. It preserves the original orientation of the output vector but normalizes its length to the range [0-1]. In their model tuned for the MNIST dataset, Sabour et al. [2017] propose a primary capsule layer with 32 convolutional capsules, each one with 8-dimensional features. The convolution relies on a 9x9 kernel and a stride of 2.

$$v_j = \frac{||s_j||^2}{1+||s_j||^2} \frac{s_j}{||s_j||} \tag{1}$$

The primary capsule layer is followed by a single or multiple capsule layer. In the last capsule layer, each capsule represents a different object/class to be recognized by the network. For all but the primary capsules, the input is a weighted sum of the output vectors from the capsules in the layer below. For a given capsule j in layer L + 1, each

²https://github.com/Sarasra/models/tree/master/research/capsules

output vector u_i from layer L is multiplied by the respective weight matrix W_{ij} as detailed in Equation 2. The resulting vector \hat{u}_{ij} (prediction vector) is submitted to the iterative dynamic routing mechanism. This mechanism computes the coupling coefficients c_{ij} between each capsule in layer L and capsules in layer L + 1. Coupling coefficients determine the probability of the object represented by a capsule in layer L being part of a capsule in layer L + 1.

$$s_j = \sum_i c_{ij} * \hat{u}_{ji}, \quad \hat{u}_{ji} = W_{ij} * u_i$$
 (2)

Algorithm 1 details the dynamic routing algorithm [Sabour et al., 2017]. In the first iteration of the routing process, the prediction vector of a capsule *i* in layer *L* is equally routed to every capsule *j* of layer L + 1. This occurs as logits b_{ij} of the coupling coefficients are initialized as zeros. In the next iterations, each coupling coefficient c_{ij} is refined by measuring the agreement between the prediction vector of capsule *i* and the output of capsule *j*. The agreement is calculated as the scalar product between the prediction vector \hat{u}_{ij} and the output vector v_j . This agreement is added to the initial logits b_{ij} . The output of a capsule at a given iteration is computed as the scalar product of the prediction vectors and the respective coupling coefficients. To ensure that the coupling coefficients between capsule of layer *L* and all capsules from layer L + 1 sum to 1, the logits b_{ij} that reflect the level of agreement between capsules are submitted to a *softmax* function before the output vector is calculated. As the output vector is calculated, it is submitted to a *squash* function to ensure that its length belongs to the interval [0, 1]. The routing algorithm is repeated for a given number of iterations, previously defined or hyper-tuned by the neural network designer. In their network specifically tuned for the MNIST dataset, Sabour et al. [2017] uses a unique capsule layer, composed of 10 16-dimensional capsules.

Algorithm 1: Dynamic routing algorithm

1: for all capsule *i* in layer *L* and capsule *j* in layer L + 1: $b_{ij} = 0$ 2: for *r* iterations do 3: for all capsule *i* in layer *L*: $c_i = softmax(b_i)$ 4: for all capsule *j* in layer L + 1: $s_j = \sum_i c_{ij} * \hat{u}_{ji}$ 5: for all capsule *j* in layer L + 1: $v_j = squash(s_j)$ 6: for all capsule *i* in layer *L* and capsule *j* in layer L + 1: $b_{ij} = b_{ij} + \hat{u}_{ji} * v_j$ 7: end for 8: return v_j

2.3 Quantization

Quantization refers to techniques for mapping floating-point tensors to integer tensors, with lower bit-width [Gholami et al., 2021, Wu et al., 2020, Liang et al., 2021, Novac et al., 2021, Wang et al., 2020]. As a consequence, a quantization process involves the encoding of (i) the sign, (ii) the integer part, and (iii) the fractional part of a float in a single integer value. In binary, quantized numbers are typically represented in Qm.n notation, where m specifies the number of bits allocated for the integer part and n the number of bits allocated for the fractional part [Novac et al., 2021]. The main goal of quantization is to improve inference latency and reduce the memory footprint of neural networks. However, the success of a quantization procedure is highly dependent on the memory specification and instruction set architecture (ISA) of the target platform [Gholami et al., 2021, Novac et al., 2021].

Post-training quantization vs. quantization-aware training: Quantization-aware training lowers the impact of the quantization on model accuracy by simulating the low-precision of weights during training. It considers the quantization error as part of the loss returned by the loss function, which the optimization algorithm tries to minimize [Gholami et al., 2021, Wu et al., 2020, Liang et al., 2021, Novac et al., 2021, Wang et al., 2020]. In post-training quantization, the model is quantized without any fine-tuning during training.

Uniform vs. non-uniform quantization: Quantizing floating-point values to lower bit-width integers can return values that are equally (uniform quantization) or non-equally (non-uniform quantization) spaced [Gholami et al., 2021, Novac et al., 2021, Wang et al., 2020]. For a fixed bit-width, non-uniform quantization may return more accurate ML models, as it captures with higher resolution the more important value regions [Gholami et al., 2021, Novac et al., 2021]. The quantization step is tuned to minimize the quantization error [Gholami et al., 2021, Novac et al., 2021]. Wang et al., 2020]. Nevertheless, non-uniform quantization typically introduces non-negligible overhead in the computation of quantized models on general-purpose hardware (GPUs and CPUs), sometimes leading to a latency higher than using the floating-point ML model [Novac et al., 2021, Wang et al., 2020]. As a consequence, uniform quantization is the de-facto method to perform fast computations on resource-constrained devices [Gholami et al., 2021, Novac et al., 2021, Wang et al., 2020].

2021]. Equation 3 represents a typical uniform quantization function, where r is the float to be quantized, S is a scalar, and Z is a zero-point or offset.

$$Q(r) = round(r/S) - Z \tag{3}$$

Scaling and offset: In uniform quantization, the scaling factor and the zero-point are the core of the quantization function [Gholami et al., 2021, Novac et al., 2021, Wu et al., 2020, Jacob et al., 2018]. The scaling factor specifies the step size of the quantizer, dividing a given range of values into equally spaced partitions. The zero-point is an integer offset used to ensure that a zero is quantized with no error when the range of values to be quantized is not centered around 0. To define a scaler (Equation 4), it is required to firstly define the target Qm.n format and the range of floating-point values to be quantized ($[x_{min}, x_{max}]$) [Gholami et al., 2021, Wu et al., 2020]. The clipping range can be symmetric ($|x_{min}| = |x_{max}|$) or asymmetric ($|x_{min}|! = |x_{max}|$)). For an asymmetric setting, the zero-point is calculated as defined in Equation 5 [Wu et al., 2020]. Note that the zero-point is rounded to an integer value. Asymmetric quantization often results in a tight clipping range, which can reduce the impact of quantization on model accuracy [Gholami et al., 2021, Novac et al., 2021]. Nevertheless, symmetric quantization is widely adopted in practice as asymmetric quantization can introduce non-negligible overhead during inference [Gholami et al., 2021].

$$S = \frac{x_{max} - x_{min}}{2^b - 1}$$
(4)

$$z = -round(x_{min} * S) - 2^b - 1 \tag{5}$$

Quantization granularity: Two metrics should be considered when selecting the granularity of quantization: (i) impact on model accuracy and (ii) computational cost [Wu et al., 2020]. The minimum impact on model accuracy is achieved if the scaling factor and the zero-point are calculated for each weight and activation. However, this would result in a tremendous computation overhead and memory consumption as scaling and zero-point factors must be saved for each weight/activation. These factors combined may hamper the main objective of the quantization [Novac et al., 2021], Gholami et al., 2021]. In contrast, the minimum computational cost is achieved if the scaling factor and the zero-point are calculated for the whole neural network [Novac et al., 2021, Gholami et al., 2021]. However, this may result in an accuracy drop that can not be neglected. As a consequence, performing the quantization layer-by-layer or filter-by-filter are the most common strategies [Novac et al., 2021, Wang et al., 2020].

Fixed bit-width vs. mixed bit-width: In a fixed bit-width setting, the same bit-width is used to quantize the whole network [Gholami et al., 2021, Wang et al., 2020]. In a mixed bit-width setting, the bit-width of each layer or filter is tuned for better model accuracy and/or memory footprint reduction [Gholami et al., 2021, Wang et al., 2020]. Activations and weights for layers/filters whose contribution to the final output is smaller get lower bit-width, while layers/filters that contribute the most get higher bit-widths. For the same memory footprint, this strategy has the potential to reduce the degradation of the model accuracy, however at the cost of a more complex quantization scheme and inference-pass software [Gholami et al., 2021, Wang et al., 2020].

Static vs. dynamic quantization: In static quantization, the scaler and the zero-point factors are calculated before inference, using a representative dataset. In dynamic quantization, these parameters are computed dynamically during the inference pass for each input [Gholami et al., 2021, Novac et al., 2021]. In this approach, weights and activations are stored in memory in low-precision bit-width, but the operations (matrix multiplication and convolution) are performed in floating-point arithmetic. In comparison to static quantization, dynamic quantization lowers the impact of quantization on model accuracy; however, it incurs a performance overhead that may be prohibited for low-end MCUs [Gholami et al., 2021, Novac et al., 2021].

2.4 CMSIS-NN

CMSIS-NN [Lai et al., 2018] is a series of open-source software kernels optimized to enable the deployment of neural networks on resource-constrained Arm Cortex-M MCUs. These software kernels are built upon the CMSIS abstraction layer and are optimized for Cortex-M MCUs that support single instruction multiple data (SIMD). This API is organized in two parts: *NNFunctions* and *NNSupportFunctions*. *NNFunctions* include functions for the computation of the most popular layer types, such as convolution and fully-connected. *NNSupportFunctions* include support functions for data precision conversion and activations, which are used in the computation of *NNFunctions*. These kernels support both 8-bit and 16-bit data. The quantization is assumed to be uniform, symmetric, and to return values with fixed bit-width.

The quantization must also be static and conducted layer-by-layer. As the quantization relies on a power-of-two scaling, the scaling of a layer output is implemented as a bitwise shift operation.

For a convolutional layer, input data is assumed to be in Height-Width-Channel (HWC) format, i.e., channel first. In terms of activation functions, CMSIS-NN supports *ReLU*, *sigmoid*, and *tanh* [Dong et al., 2020]. *ReLU* is implemented as a simple clipping function that maps negative values to 0 and maintains the value of positive values. *Sigmoid* and *tanh* are implemented using a lookup table (LUT) approach. These kernels were firstly tested by Lai et al. [2018] on the STM32F746ZG MCU (Arm Cortex-M7) running a CNN featuring three convolutional layers and one fully-connected layer, at 216 MHz. CMSIS-NN was able to classify 10.1 images per second with an accuracy drop of only 0.04%.

2.5 PULP-NN

PULP-NN [Garofalo et al., 2020] is an open-source API optimized for the execution of quantized neural networks in RISC-V RV32IMCXpulp MCUs. As this API is based on CMSIS-NN dataflow, it is also divided into two parts: *NNKernels* and *NNUtils*. *NNKernels* implement matrix multiplication and the standard layer types of neural networks, while *NNUtils* include support functions for data precision conversion and batch normalization. PULP-NN supports 8-bit and sub-byte (4-bit, 2-bit, and 1-bit) data types. However, in terms of activation functions its offering is more limited as it only supports *ReLU*. For the 8-bit setting, the quantization of weights is processed as for CMSIS-NN. Notwithstanding, the quantization of activations follows a different approach, as PULP-NN only supports non-negative activations. Consequently, the quantization must be asymmetric. Similar to CMSIS-NN, data is assumed to be in the HWC layout.

The key innovation of PULP-NN is the support for multi-core processing. For a convolution, the workload can be split along the height, width, or channel dimension of the output feature map. For a fully-connected layer, the workload is split along the output neurons. This library was firstly tested by Garofalo et al. [2020] in a GAP-8 MCU executing a CNN quantized to int-8 data and featuring three convolutional layers and one fully-connected layer. In an octa-core setup at 170 MHz, PULP-NN enables this CNN to run in 30x and 19.6x fewer clock cycles than the CMSIS-NN library, running on STM32L476 (Armv7-M, Cortex-M4) and STM32H743 (Armv7-M, Cortex-M7) MCUs, respectively.

3 Software Kernels

3.1 Matrix Multiplication

Matrix multiplication is a memory-intensive operation. Consequently, reducing memory access by maximizing data reuse at the register file level is a key factor in increasing the throughput of CapsNets. As Armv7E-M, Armv8-M, and RISC-V RV32IMCXpulp are 32-bit computing architectures and our software kernels use 8-bit data as operands, matrix multiplication can strongly benefit from a SIMD to read four operands from memory at once. The maximum throughput would be achieved by combining this SIMD with a SIMD for the simultaneous MAC of two words containing four 8-bit operands (4x8-bit word). Since the ISAs of Armv7E-M and Armv8-M are very distinct from the ISA of RISC-V (RV32IMCXpulp), the matrix multiplication kernel was tuned for each computing architecture.

3.1.1 Arm Cortex-M

CMSIS-NN already provides a function for the multiplication of int-8 matrices: $arm_mat_mult_q7$. However, for all but the latest ARMv8.1-M architecture, this function does not rely on any type of hardware acceleration, including SIMD instructions, to read from memory, and for MAC operations. It simply iterates over the rows of the source matrix A and over the columns of the source matrix B, reading one element at a time and multiplying them. It uses a 32-bit accumulator, which saturates at 8-bit after the proper right shifting determined in the quantization process. $arm_mat_mult_q7$ does not use any loop unrolling technique or parallelism. For a 4x4 sized matrix multiplication kernel, this function requires 8 load operations without sign extension and 4 MACs. As matrix multiplication is a very critical operation within the capsule computation, we tried to optimize the CMSIS-NN baseline function and developed two additional functions for quantized matrix multiplication: (i) $mat_mult_q7_trb$ and (ii) $mat_mult_q7_simd$.

 $mat_mult_q7_trb$ differs from $arm_mat_mult_q7$ as it transposes the source matrix B before entering in the MAC loop. As all matrices are stored in memory in height-width format, the parameters of the source matrix B can not be accessed contiguously. We believe this can reduce the complexity in the calculus of the memory address of the operands during a MAC operation. The general workflow of $mat_mult_q7_trb$ is outlined in Figure 3.

mat_mult_q7_simd uses the SIMD feature of Armv7E-M and Armv8-M to read from memory and for MAC operations. For the signed MAC operation, the ISAs of these architectures do not feature instructions with 4x8-bit operands. However, they still feature instructions with 2x16-bit integers as operands. This means that we have to trade off



Figure 3: Matrix multiplication in Arm Cortex-M MCUs using mat_mult_q7_trb

the additional speedup delivered by SIMD instructions with the additional computation to perform sign extension. $mat_mult_q7_simd$ also transposes the source matrix B prior to the MAC loop; however, it also sign-extends it to 16-bit. This function is also composed of (i) one outer loop over the rows of the source matrix A and (ii) an inner loop over the columns of the transposed and sign-extended matrix B. However, as the SMLAD instruction takes 2x16-bit operands, we applied loop unrolling on the inner loop and compute 2 MACs simultaneously. For a 4x4 sized matrix multiplication kernel, it requires 4 load operations with sign extension and 2 MACs. Algorithm 2 details the $mat_mult_q7_simd$.

Algorithm 2: *mat_mult_q7_simd(a, b, shift, r)* for Arm Cortex-M

1: transpose and sign extend b to 16-bit: $b_trb = matrix_q7_to_q15_transposed(b)$ 2: **for** row *i* in *a* **do** 3: initialize accumulator: sum = 04: read and expand int-8 word from a into two int-16 words: $read_and_pad(i, a1, a2)$ for column j in $num_cols_b >> 2$ do 5: read two int-16 from b_trb : $b1 = read_q15x2_ia(j)$ 6: 7: read two int-16 from b_{trb} : $b2 = read_q 15x2_{ia}(j)$ 8: MAC: $sum = _SMLAD(a1, b1, sum)$ MAC: $sum = _SMLAD(a2, b2, sum)$ 9: 10: end for 11: for column j in $num_cols_b\%4$ do 12: MAC: sum = sum + (i * j)13: end for fix quantization format: $sum = _SSAT(sum >> shift, 8)$ 14: copy accumulator to r: *r + + = sum15: 16: end for

3.1.2 RISC-V

The ISA of RISC-V does not support SIMD instructions. However, in contrast to Arm Cortex-M, the RV32IMCXpulp extension provides SIMD instructions for MAC operations with 4x8-bit words as operands. RISC-V SOCs featuring the RV32IMCXpulp extension are usually provided with a fabric core and a multi-core acceleration cluster tailored for ANN computation [Flamand et al., 2018]. The fabric core is an MCU built around the RISC-V core and extended for efficient digital signal processing. The acceleration cluster is turned on from the fabric controller when the programmer wants to offload computation-intensive kernels. Both the fabric controller and the acceleration cluster feature the RV32IMCXpulp extension. Nevertheless, PULP-NN does not feature any built-in function for the signed and quantized matrix multiplication in int-8 format. As a consequence, we developed three additional functions: (i) mat_mult_q7 , (ii) $mat_mult_q7_simd$. They are based on the Cortex-M implementation, but are tuned to extract the most of the acceleration cluster.

The *mat_mult_q7* does not rely on any SIMD instruction for reading and MAC operations, nor transposes the source matrix *B* prior to the MAC loop. It is the equivalent of the *arm_mat_mult_q7* but re-designed to support parallelization over the rows of the output matrix. The number of cores used in the parallelization must be a power of two (2^n) . Similar to its Arm Cortex-M counterpart, *mat_mult_q7* requires 8 load operations without sign extension and 4 MACs for a 4x4 sized matrix multiplication kernel.

 $mat_mult_q7_trb$ is very similar to the Arm implementation (figure 3) - it was designed to evaluate the advantages of transposing the source matrix B prior to the MAC loop. Notwithstanding, there are two main differences. Firstly, it is

tuned for multi-core processing. The transpose of the source matrix *B* is parallelized on the acceleration cluster over the row dimension and the same applies to the MAC loop. Secondly, the sign saturate is performed via a GCC built-in for the RISC-V RV32IMCXpulp (*__builtin_pulp_clip_r*). For a 4x4 matrix multiplication kernel, this function requires 8 load operations without sign extension and 4 MACs.

When considering the $mat_mult_q7_simd$ function (Algorithm 3), the RISC-V RV32IMCXpulp version is more efficient as the ISA of this architecture features a SIMD instruction for the MAC of 4x8-bit operands. This function also transposes the source matrix *B* prior to the MAC loop. Both the matrix transposing and the MAC loop is performed in the same multi-core fashion as for $mat_mult_q7_trb$. When compared to Arm for a 4x4 matrix multiplication kernel, it requires 2 loads without sign extension and 1 MAC operation instead of 4 loads with sign extension and 2 MACs.

Algorium 5: $mai_mui_q/_sima(a, b, b)$	sniji, r	$^{\prime}$ 101 KISC-V
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1: transpose $b: b_trb = transpose(b)$ 2: for row i in a[start_row, stop_row] do 3: initialize accumulator: sum = 04: read int-8 word from a: a1 = read(i)for column j in $num_cols_b >> 2$ do 5: read int-8 word from b_trb : b1 = read(j)6: 7: MAC: $sum = _builtin_pulp_sdotsp4(a1, b1, sum)$ 8: end for 9: for column j in $num_cols_b\%4$ do 10: MAC: sum = sum + (i * j)11: end for fix quantization format: $sum = _builtin_pulp_clip_r(sum >> shift, 127)$ 12: 13: copy accumulator to r: *r + + = sum14: end for

3.2 Squash Activation and Vector Norm

The *squash* activation function is designed to receive as input a 2D matrix, where each row corresponds to a vector to be squashed. For each row, the computation starts with the calculation of the vector length and ends with the squashing of each vector entry. The calculation of the vector norm uses a 32-bit integer to accumulate the sum of the power of two of each vector entry. As computing the exact value of a square root leads to severe overhead and latency in both architectures, we approximate the square root operation using the Newton-Raphson method [Ram, 2009].

The Newton-Raphson method is one of the most efficient techniques to approximate the zeroes of a mathematical function (f(x) = 0) [Ram, 2009]. It takes as input an initial approximation and then enters into an iterative process that produces successively better approximations. This iterative process is based on the evaluation of the derivative of the zero approximation. The square root calculus can be translated as finding the solution to Equation 6, which determines Equation 7 to find the next optimal solution at each iteration of the Newton-Raphson method [Ram, 2009]. The calculus ends whenever the absolute difference between the current zero-approximation and the zero-approximation projected for the next iteration is below 1 [Ram, 2009]. Algorithm 4 details the implementation of the Newton-Raphson method.

$$f(x_n) = x_n^2 - n \tag{6}$$

$$x_{n+1} = \frac{(x_n + n)/x_n}{2}$$
(7)

Algorithm 4: Newton-Raphson method to calculate the square root of n

- 1: take n/2 as the initial approximate root: $x_0 = n/2$
- 2: calculate the next approximate root according to Equation 7: $x_1 = \frac{(x_n+n)/x_n}{2}$
- 3: while $x_1 < x_0$ do
- 4: update the current approximate root: $x_0 = x_1$
- 5: update the next approximate root: $x_1 = \frac{(x_n+n)/x_n}{2}$
- 6: end while
- 7: return x_0

As the length of a vector is calculated, each vector entry is squashed. In full-precision arithmetic, the output of *squash* is in the range [0, 1]. Therefore, the minimal precision loss is achieved if the output of *squash* is quantized in absolute Q0.7 format, i.e., all bits except for the sign bit represent the fractional part of a number. To comply with this quantization format, we tuned the original *squash* activation (Equation 1) as detailed in Equation 8, where i_{qn} and o_{qn} represent the number of virtual fractional bits in the input and output data, respectively. By extending the scaling granularity to the squared norm and norm parameters, we avoid the accuracy loss when the floating-point norm is below 0. For more details on the absolute and virtual quantization formats, we refer to Section 4. Equation 8 embeds the quantization of the *squash* activation output in the *squash* activation itself, avoiding the use of floating-point division and dynamic quantization, which introduces severe overhead. For the RISC-V implementation, the *squash* kernel can be offloaded to the acceleration cluster and parallelized along the vectors of the input matrix. The number of vectors is equally divided between each core. In case a fair division is not possible, the last core handles the remaining vectors.

$$v_j = \frac{||s_j|| << (o_{qn} - i_{qn})}{1 << i_{qn} + ||s_j||^2 >> i_{qn}} * s_j$$
(8)

3.3 Primary Capsule Layer

A Primary capsule layer is the first capsule layer of a CapsNet. It has a convolutional kernel and can be observed as a convolutional layer with *squash* activation. Nevertheless, we have to consider that a primary capsule layer is 4-dimensional, while CMSIS-NN and PULP-NN only support convolution over 3D data. This characteristic of a primary capsule layer can be observed in Fig. 2 - it is characterized by the (i) height, (ii) width, and (iii) depth of the capsules, as well by the (iv) number of capsules. Instead of implementing a 3D convolutional kernel to perform convolution over 4D data, we borrowed the implementation strategy of Sabour et al. [2017] and implemented primary capsule layers with 2D convolution kernels and then perform reshape. The third dimension of the data submitted to these 2D convolution kernels corresponds to the last two dimensions of the capsule layer (*capsule depth x number of capsules*). The output of the convolution is reshaped as a 2D vector where the first dimension corresponds to *capsule height x capsule width x number of capsules* and the last dimension correspond to *capsule depth.* These 2D vectors get squashed along the last dimension, ensuring that the magnitude of the capsule depth sums to 1. The output feature map of the squash activation is then reshaped to match the original 4D shape of the primary capsule layer. As detailed in section 4, quantized primary capsule layers must scale the output feature map of the convolution prior to the squash activation to minimize the accuracy loss. For this purpose, for both Arm Cortex-M and RISC-V, our software kernel requires the programmer to pass two scaling factors: (i) one for the bias and (ii) another for the outputs.

3.3.1 Arm Cortex-M

In CMSIS-NN, there are two functions for convolutions with 8-bit data: a basic version $arm_convolve_HWC_q7_basic_nonsquare$ and another for reduced latency $- arm_convolve_HWC_q7_fast_nonsquare$. Despite the reduced latency, the later version imposes constraints on the dimension of the input and output channels, which must be multiples of 4 and 2, respectively. Considering that these restrictions are too severe and may not fit all the design scenarios, we decided to provide the API with two functions for the primary capsules: one based on the basic convolution ($pcap_q7_basic$) and another based on the fast convolution ($pcap_q7_fast$). These functions are already designed to leverage most of the SIMD features in Armv7E-M and Armv8-M architectures. Nevertheless, as the remaining CMSIS-NN functions, they are not ready to parallelize the convolution over multi-cores. CMSIS-NN already embeds in their convolution kernels the scaling of the output feature map. The scaling is performed as a bitwise-shift operation for the bias and the outputs. The *squash* activation is detailed in section 3.2. For more details on the convolution kernels implemented by CMSIS-NN, we refer to the work [Lai et al., 2018].

3.3.2 RISC-V

PULP-NN does not provide any function that can be directly used to implement the convolution part of a primary capsule. Convolution functions provided by PULP-NN involve the clipping of negative activations to zero, which is incompatible with the fundamentals of CapsNets. Clipping negative values limit the direction scope and distort the magnitude of the output vector, introducing an additional non-linearity that CapsNets are not designed to support. Nevertheless, RISC-V (RV32IMCXpulp) already features SIMDs and GCC builtin-functions for the dot-product of two vectors with 4x8-bit signed data. Furthermore, it also provides a builtin-function for the saturate operation. Given the background, we borrowed the PULP-NN functions implementing convolutional layers (*pulp_nn_conv_Co_parallel*, *pulp_nn_conv_Ho_parallel*, *pulp_nn_conv_HoWo_parallel*) and adapted them for signed int-8 data. We updated the data type of all arguments and intermediate variables in unsigned integer to signed integer and replaced the GCC built-ins for the dot-product and saturate operations, which are now performed by __builtin_pulp_sdotsp4 and __builtin_pulp_clip_r,

respectively. The batch normalization and relu activation were also updated. The new convolution functions - (i) $pulp_nn_conv_Co_parallel_q7$, (ii) $pulp_nn_conv_Ho_parallel_q7$, (iii) and $pulp_nn_conv_HoWo_parallel_q7$ - maintain the same inner loop of the convolution used by PULP-NN. They are also optimized to run on the acceleration cluster. Consequently, our software kernels feature three different functions for the primary capsule layer, each one devoted to a different parallelization strategy - parallelization can be performed along the channel ($pcap_Co_q7$), height ($pcap_Ho_q7$), or height vs. width ($pcap_HoWo_q7$). Pixels are equally divided by all cores. If a fair division is not possible, the last core handles the remaining. Nevertheless, primary capsule kernels can also run in the fabric controller. For more details on the inner loop of the convolution, we refer to the work [Garofalo et al., 2020]. The squash activation is detailed in section 3.2.

3.4 Capsule Layer

Algorithm 5 details the workflow of the kernel implementing a capsule layer (*capsule_layer_q7*). This workflow is mainly implemented by a series of four support functions, starting with the *calc_inputs_hat* which calculates the prediction vectors, which is then submitted to the dynamic routing. The dynamic routing starts with the *calc_coupling_coefs* which computes the coupling coefficients by applying a softmax function to the logits representing the agreement between capsules in consecutive layers. These coupling coefficients and the prediction vectors are further used as inputs to *calc_caps_output*, which returns the output vectors of the capsule for the current routing iteration. If the dynamic routing is not in the last iteration, the function *calc_agreement_w_prev_caps* calculates the agreement between capsules in layer L + 1 and capsules in layer L. Each one of these support functions is detailed below.

Algorithm 5: *capsule_layer_q7(args)* for Arm Cortex-M and RISC-V

1: initialize logits b_{ij} as zeroes: $memset(b, 0, num_caps * input_num_caps)$

- 2: calculate prediction vectors: *calc_inputs_hat(b,layer_input,shift,pred_vectors)*
- 3: for routing *r* in *num_routings* do
- 4: calculate coupling coefficients c_{ij} : $calc_{coupling_{coefs}}(b, c)$
- 5: calculate output vectors: calc_caps_output(pred_vectors, c, shift, out_vectors)
- 6: **if** $r < num_routings 1$ **then**
- 7: calculate agreement between capsules: calc_agreement_w_prev_caps(pred_vectors, out_vectors, shift, b)
- 8: end if
- 9: end for

3.4.1 calc_inputs_hat

Multiplies the input of the capsule layer by the respective weight matrix. These weights connect each feature of each capsule in layer L to each feature of each capsule in layer L + 1. As a consequence, the original weight matrix is 4D [total capsules in layer L + 1, total capsules in layer L, capsule size in layer L + 1, capsule size in layer L] and not directly supported by our matrix multiplication kernels. Nevertheless, performing a direct 4D matrix multiplication would require the replication of the input feature map for each capsule, increasing the memory footprint. Instead, calc_inputs_hat regards the 2 inner dimensions of the weight matrix as valid matrix multiplication dimensions and the outer dimensions as batch size. calc_inputs_hat has an outer loop that iterates over all capsules of layer L + 1 and an inner loop that iterates over all capsules of layer L. In the inner loop, the weights connecting a capsule i in layer L to a capsule j in layer L + 1 are multiplied by the input features of capsule j (output features of capsule i). The multiplication of these two matrices uses the fastest of the kernels described in section $3.1 - mat_mult_q7_trb$ for Arm and $mat_mult_q7_simd$ for RISC-V. The resulting prediction vector is then submitted to the iterative dynamic routing where the output vector will be iteratively updated.

3.4.2 calc_coupling_coefs

First function of the the dynamic routing and computes the coupling coefficients c_{ij} . More specifically, $calc_coupling_coefs$ applies a softmax function over the logits b_{ij} that measure the agreement between capsules at different layers. Each logit b_{ij} measures the agreement between a capsule *i* in the previous layer (layer *L*) and a capsule *j* of the current layer (layer *L* + 1). Applying a softmax function to these logits ensures that the importance of a capsule *i* in layer *L* for all capsules of the current layer L + 1 sums to 1. For the Armv7E-M and Armv8-M, we make direct use of the *arm_softmax_q7* function provided by CMSIS-NN. In contrast, PULP-NN does not provide any function implementing softmax. We developed a *softmax* function based on the Arm implementation.

3.4.3 calc_caps_output

Multiplies the coupling coefficients with the prediction vectors, returning the output vectors. If coupling coefficients are already expressed in a 2D matrix, the same is not applied to the prediction vector, which is represented by a 3D matrix [total capsules in layer L + 1, total capsules in layer L, capsule size in layer L + 1]. Consequently, calc_caps_output regards the 2 inner dimensions as the valid matrix multiplication dimensions and the outer dimension as batch size. Matrix multiplication is performed using the fastest of the kernels described in section 3.1. When the matrix multiplication loop finishes, the output vectors are squashed using the kernel described in section 3.2.

3.4.4 calc_agreement_w_prev_caps

Determines the degree of agreement between the weighted output of a capsule in layer L (prediction vectors) with the output of capsules (output vectors) in layer L + 1. The agreement is determined as the product of the respective matrices. As the prediction vector is represented by a 3D matrix *[total capsules in layer* L + 1, *total capsules in layer* L, *capsule size in layer* L + 1], *calc_caps_output* consider the inner two dimensions as the valid matrix multiplication dimensions and the outer dimension as batch size. The result is then summed up to the logits b_{ij} . For this purpose, we rely on 2D matrix addition kernels.

4 CapsNet Quantization

The quantization framework is detailed in Algorithm 6. It takes as input a CapsNet developed in TensorFlow and a quantization dataset and returns the quantized weights and bias, as well as the output and bias shifts. Except for primary capsule and capsule layers, this framework considers activation functions as independent layers. Embedding an activation in a dense or convolutional layer may return a faulty quantized model.

As detailed in Algorithm 6, after loading the model and the dataset, the quantization process starts with the quantization of the model's weights. The quantization itself is performed as detailed in Algorithm 7. For each layer, the framework searches for the maximum absolute weight (max_abs) and calculates the number m of integer bits required to represent it. As we are using a power-of-two scaling $(Ax2^n)$, the number of integer bits to represent a value A is calculated as the ceiling of $log_2(max_{abs})$. The remaining n bits are considered for the fractional part. Nevertheless, to increase precision in layers with very small weights (maximum absolute weight lower than 1/127), our framework virtually increases the number of fractional bits, bringing the maximum norm of the quantized weights closer to the saturation barrier without never going over it. In absolute or physical terms, every weight is still in Q0.7 format as it still fits in eight bits, but virtually the quantization format can surpass the eight-bit barrier. It must be noted that the first bit of the eight available is used for the sign. This Qm.n quantization format allows the representation of values comprised in the uniform and symmetric range $[-max_abs, max_abs]$. After getting the quantization Qm.n format, the framework proceeds to the calculus of the quantized weights, where the floating-point number A is multiplied by 2 powered to the number of fractional bits n ($Ax2^n$). The quantization finishes with the clipping of values to the range [-128, 127]. The quantization of the model's bias is performed under the same workflow.

This quantization strategy enables the addition and multiplication of quantized values with minimal overhead. However, the results must be scaled to avoid saturation problems. As we are using a power-of-two-scaling, scaling can be performed as a bitwise shift operation. In the context of CapsNets, scaling takes part of the convolutional, primary capsule, and capsule layers as these layers apply matrix multiplication and/or addition. Convolutional and primary

Algorithm 6: Quantization framework

```
1: load CapsNet from .h5 file
 2: load quantization reference dataset
 3: quantize weights: wq_{ij} = round(w_{ij}/S)
 4: quantize bias: bq_{ij} = round(b_{ij}/S)
 5: calculate amount of output/bias shift:
        for layer l in CapsNet do
 6:
 7:
           for matrix multiplication, matrix addition or convolution k do
 8:
              get Qm.n format of the input, output, and intermediates
              calculate amount of output shift: out\_s = f_{ia} + f_{ib} - f_o
calculate amount of bias shift: bias\_s = f_{ia} + f_{ib} - f_b
 9:
10:
11:
           end for
        end for
12:
13: return wq, bq, s
```

Algorithm 7: O	uantization	algorithm
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1: get Qm.n format: 2: find maximum absolute value max_{abs} 3: find amount m of bits to represent the range $[-max_{abs}, max_{abs}]$: the ceiling of $log_2(max_{abs})$ 4: calculate amount n of bits for the fractional part: 5: n = 7 - mwhile $(max_{abs} >> (n+1)) <= 127$ do 6: 7: n + +8: end while 9٠ convert to quantized integer: 10: multiply floating-point values A by 2 powered to the number of fractional bits: $Ax2^n$

clip quantized integers for the range [-128, 127] 11:

capsule layers only go through a single matrix multiplication process, and therefore only take one scaling factor for the bias and another for the output. However, capsule layers involve at least three distinctive matrix multiplications and one matrix addition. When considering the four support functions of a capsule layer kernel, only *calc_coupling_coefs* does not require any scaling factor. *calc inputs hat* requires one output scaling factor and *calc caps output* requires one for each iteration of the dynamic routing. As *calc_agreement_w_prev_caps* comprises matrix multiplication and addition, it requires two output scaling factors per iteration of the dynamic routing unless for the last one.

The scaling factors are calculated as detailed in Algorithm 6. For each matrix multiplication or addition in each layer of the network, the reference quantization dataset is used to determine the maximum absolute value for the input and output data. Then, it applies Algorithm 7 to get the quantization format (Qm.n) for this data. At this step, the framework is ready to calculate the number of right shifts for every matrix multiplication/addition. Considering f_{ia} as the number of fractional bits for the input matrix A, f_{ib} as the number of fractional bits for the input matrix B, and f_o as the number of fractional bits for the output, the amount of right shifts (output scaling factor) is calculated as detailed in line 9 of Algorithm 6. The same process is carried out to calculate the left bias shift of convolutional and primary capsule layers. The bias shift is calculated as detailed in line 10 of Algorithm 6. f_b represents the number of fractional bits for the bias.

5 **Evaluation**

We evaluated the software kernels and the quantization framework on three imaging datasets: (i) MNIST [Lecun et al., 1998], (ii) smallNORB, and [LeCun et al., 2004] (iii) CIFAR-10 [Krizhevsky, 2009]. MNIST is a large database of handwritten digits between 0 and 9. It contains 60k training images and 10k testing images, both shaped as 28x28x1. smallNORB is a dataset designed to develop applications for 3D object recognition from shape. It contains 5 generic categories of toys - (i) four-legged animals, (ii) human figures, (iii) airplanes, (iv) trucks, and (v) cars - imaged under varying light conditions, elevations, and azimuths. Both training and testing batches are composed of 24.3k images, shaped as 96x96x2. CIFAR-10 consists of 60000 32x32x3 colour images, representing 10 different objects. There are 50k images for training and 10k for testing.

For each dataset, we trained a full-precision and baseline reference CapsNet. We do not intend to build CapsNets with state-of-the-art accuracy on these datasets but rather build a CapsNet that after quantization fits in the limited memory resources of the target low-power MCUs without compromising the accuracy. We have built CapsNets that after quantization take no more than 80% of the RAM available in the least performing target MCU. At the moment of this evaluation, our software kernels do not support tiling. Thus, we have to ensure that both the CapsNet parameters and at least one sampling image can fit in the available RAM without compromising the execution of our software kernels. Table 1 details the architecture and hyper-parameters of the CapsNets used for testing.

The evaluation included three Arm Cortex-M MCUs: STM32L4R5ZIT6U (Cortex-M4 @ 120 MHz, 640 KB RAM), STM32H755ZIT6U (Cortex-M7 @ 480 MHz, 1 MB RAM), and STM32L552ZET6QU (Cortex-M33 @ 110 MHz, 512 KB RAM). Hence, our evaluation encompasses CPUs featuring Armv7-M architecture (Cortex-M4 and Cortex-M7), and the more recent Armv8-M (Cortex-M33). At the time of this evaluation, the market's scarcity of in-silicon MCUs featuring the RISC-V RV32IMCXpulp ISA severely limited the testing setup. For RISC-V, our software kernels were tested on a single development board featuring a GAP-8 MCU (GreenWaves GAPuino v1), with a fabric controller running at 250 MHz and an acceleration cluster with 8 cores running at 170 MHz. All cores share 512 KB of RAM. Although there are several open-source RISC-V cores using RISC-V RV32IMC ISA, using soft-cores deployed in an FPGA to test our software kernels would not enable a fair comparison with the Arm Cortex-M MCUs.

Dataset	Convolut	ional Layers	Primary	Capsule Layers	Capsule Layers		Optimizer	
	Layer #	Configuration	Layer #	Configuration	Layer #	Configuration	Туре	LR
MNIST	1	Filters: 16 Kernel Size: 7 Stride: 1 Activation: ReLU	2	Capsules: 16 Dimension: 4 Kernel Size: 7 Stride: 2	3	Capsules: 10 Dimension: 6 Routings: 3	Adam	0.001
smallNORB	1	Filters: 32 Kernel Size: 7 Stride: 1 Activation: ReLU	2	Capsules: 16 Dimension: 4 Kernel Size: 7 Stride: 2	3	Capsules: 5 Dimension: 6 Routings: 3	Adam	0.00025
CIFAR-10	1-4	Filters: [32, 32, 64, 64] Kernel Size: 4 x [3] Stride: [1, 1, 2, 2] Activation: 4 x [ReLU]	5	Capsules: 16 Dimension: 4 Kernel Size: 3 Stride: 2	6	Capsules: 10 Dimension: 5 Routings: 3	Adam	0.00025

Table 1. Daschille reference Capsivers for evaluatio	Table	1:	Baseline	reference	CapsNets	for	evaluatio
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5.1 Quantization

The quantization framework was evaluated in terms of memory footprint reduction and accuracy loss. As detailed in Section 4, the quantization mechanism returns a series of output and bias shifts that must be performed during inference time. We consider these parameters as part of the memory footprint inherent to the quantized CapsNet. Table 2 details the accuracy and memory footprint of the full precision CapsNets against their quantized counterparts. While a full-precision CapsNet requires 4 bytes per parameter, the quantized version only requires 1 byte. This represents a theoretical memory saving of 75%, which is very near to the memory saving achieved by our quantization framework (74.99%). This demonstrates that the size of the additional parameters required by quantized CapsNets for bias and output shifting is almost negligible. This applies to conventional 3-layered CapsNets but also deeper CapsNets as the one developed for the CIFAR-10 dataset.

In terms of accuracy, the maximum loss was achieved for the MNIST dataset (0.18%) and the minimum for the smallNORB (0.07%). This shows that the accuracy loss resulting from the quantization process does not necessarily grow with the complexity of the dataset. Nevertheless, it is visible that CapsNets do not perform so-well on complex datasets like CIFAR-10. CapsNets like to account for everything in the image so it does better when there is no background noise or the background does not constantly change. As this is not the case with CIFAR-10, CapsNets will perform poorly when compared to other less noisy datasets.

Dataset	Mem	ory Footp	orint (KB)	Accuracy			
	Float-32	Int-8	Int-8 Saving	Float-32	Int-8	Int-8 Loss	
MNIST	1187.20	296.82	74.99%	99.01%	98.83%	0.18%	
smallNORB	1182.34	295.61	74.99%	92.56%	92.49%	0.07%	
CIFAR-10	461.19	115.33	74.99%	78.54%	78.38%	0.16%	

Table 2: Evaluation of the quantization framework

5.2 Software Kernels

5.2.1 Matrix Multiplication

To select the fastest matrix multiplication algorithm for each target architecture, we considered the multiplication of two randomized matrices with dimensions 20x30 and 30x40. The content of each matrix was kept constant during the entire test and the latency was measured in milliseconds and clock cycles. As detailed in Section 3.1.1, for the Arm Cortex-M architecture we tested three different algorithms: (i) *mat_mult_q7_simd*, (ii) *mat_mult_q7_trb*, and (iii) *arm_mat_mult_q7*. The last one is used as a baseline reference as it does not apply any SIMD or matrix transposing operation to simplify memory access during MAC. Results are detailed in Table 3.

Contrary to what was expected, for the Arm Cortex-M implementation, the maximum performance is not observed for the algorithm relying on SIMD instructions. This occurs because the Arm ISA only supports MAC instructions with

	STM32L4R5ZIT6U (Armv7E-M, Cortex-M4)		STM32H7 (Armv7E-M,	755ZIT6U Cortex-M7)	STM32L552ZET6QU (Armv8-M, Cortex-M33)		
	Clock Cycles	Milliseconds	Clock Cycles	Milliseconds	Clock Cycles	Milliseconds	
arm_mat_mult_q7	704395	5.87	790989	1.65	654738	5.96	
mat_mult_q7_trb	655415	5.47	574532	1.20	605769	5.51	
mat_mult_q7_simd	730562	6.09	757482	1.58	697749	6.35	

	Table 3: Evaluation	of the matrix	multiplication	functions for .	Arm Cortex-M MCUs
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16-bit operands, requiring the signal extension of each 8-bit operand. Despite providing SIMD instructions for the sign extension operation, it still introduces too much performance overhead. *mat_mult_q7_simd* is even slower than the *arm_mat_mult_q7*, which does not feature any optimization. The *mat_mult_q7_trb* and *arm_mat_mult_q7* functions are, on average, 1.15x and 1.04x faster than this algorithm, respectively. The maximum performance is registered for the algorithm not based on SIMD instructions but transposes the second input matrix before the matrix multiplication process. By simplifying the calculus of memory addresses during MAC, *mat_mult_q7_trb* is on average 1.15x faster than the approach based on SIMD instructions, and 1.10x faster than the Arm CMSIS implementation.

Regarding the RISC-V implementation, the results are detailed in Table 4. As GAP-8 SoC features an acceleration cluster tailored for neural network computation, we tested our matrix multiplication functions leveraging the cluster. Tests were performed in single-core and octa-core settings. Opposed to Arm Cortex-M, the fastest algorithm here is based on SIMD instructions - $mat_mult_q7_simd$. This happens because the RISC-V RV32IMCXpulp features SIMD instructions for the simultaneous MAC of 8-bit operands, in contrast to Arm Cortex-M that only supports 16-bit operands and requires data expansion. For the octa-core setting, $mat_mult_q7_simd$ is 2.10x faster than $mat_mult_q7_trb$ and 2.05x faster than mat_mult_q7 . In a single-core configuration, the speedup of $mat_mult_q7_simd$ in relation to the other implementations is slightly higher: 2.20x faster than $mat_mult_q7_trb$ and 2.15x faster than mat_mult_q7 . When comparing the performance of the single-core with the octa-core implementation, we notice that the octa-core is 6.32x to 6.63x faster than the single-core. The combination of the RISC-V RV32IMCXpulp SIMD instructions with multi-core processing can outperform the STM32H755ZIT6U even though this Arm MCU runs at a much higher clock frequency than the RISC-V MCU (480 MHz vs. 170 MHz).

	GAP-8 (si RISC-V RV3	ngle-core) 22IMCXpulp	GAP-8 (octa-core) RISC-V RV32IMCXpulp		
	Clock Cycles	Milliseconds	Clock Cycles	Milliseconds	
mat_mult_q7	696951	4.10	105250	0.62	
mat_mult_q7_trb	715602	4.21	107784	0.64	
mat_mult_q7_simd	323844	1.91	51238	0.31	

Table 4: Evaluation of the matrix multiplication functions for RISC-V MCUs

5.2.2 Primary Capsule Layer

We tested the primary capsule kernels in terms of latency on the three previously described CapsNets. For the Armv7E-M and Armv8-M architectures we developed two different functions to implement a primary capsule layer: (i) $pcap_q7_basic$ and (ii) $pcap_q7_fast$. The former is a slower version without constraints on the input and output channel sizes. The latter is a faster version but only supports multiples of 4 and 2 for the input and output channel - a constraint that is met by the three CapsNets used for evaluation. Table 5 details the latency for the three Arm Cortex-M MCUs in the classification of a single image.

As expected, *pcap_q7_fast* outperforms the baseline reference for all datasets - it is at least 1.08x faster. Nevertheless, the most noticeable impact on the latency is caused by the size of the kernel. The biggest kernel, inherent to the smallNORB CapsNet, is 2.73x bigger than the smallest of the kernels, designed for the CIFAR-10 dataset. However, the computation of the smallNORB kernel is 33.32x to 34.23x slower than the computation of the CIFAR-10 kernel. This means that the computation time does not grow linear with the kernel size of the primary capsule layer, but rather exponentially. Given the background, big kernels must be avoided whenever possible.

Dataset		STM32L4R5ZIT6U		STM32H755ZIT6U		STM32L552ZET6QU	
		(Armv7E-M, Cortex-M4)		(Armv7E-M, Cortex-M7)		(Armv8-M, Cortex-M33)	
		Clock Cycles	Milliseconds	Clock Cycles	Milliseconds	Clock Cycles	Milliseconds
MNIST	pcap_q7_basic	65.79M	548.25	63.49M	132.29	51.34M	466.77
7x7x16x64 (M)	pcap_q7_fast	60.12M	500.97	57.57M	119.94	46.65M	424.13
smallNORB	pcap_q7_basic	406.35M	3386.29	389.62M	811.70	316.95M	2881.32
7x7x32x64 (L)	pcap_q7_fast	372.55M	3104.57	355.22M	740.03	289.06M	2627.78
CIFAR-10	pcap_q7_basic	12.09M	100.75	11.40M	23.75	9.26M	84.17
3x3x64x64 (S)	pcap_q7_fast	11.18M	93.19	10.50M	21.87	8.50M	77.30

Table 5: Evaluation of the primary capsule functions for Arm Cortex-M MCUs

For the RISC-V RV32IMCXpulp architecture, we developed three different functions implementing a primary capsule layer. As detailed in Section 3.3, each of them parallelizes a different spatial dimension of the output feature map over the cores of the acceleration cluster. Table 6 details the latency of the three implemented functions on the three reference CapsNets. As expected, it is not possible to mention a function that is the fastest for every dataset or CapsNet architecture. As the latency is directly impacted by the spatial dimension that is parallelized, it all depends on the shape of the input feature map. $pcap_ho_q7$ is simultaneously the fastest function for the MNIST dataset and the slowest for the other two. Similar to Arm, the latency grows exponentially with the kernel size of the primary capsule layer. While the kernel of the smallNORB is only 2.73x bigger than the kernel of the CIFAR-10, the computation of the smallNORB kernel is at least 33.39x slower (single-core). This effect is not attenuated in a multi-core configuration.

Dataset		GAP-8 (si RISC-V RV3	ngle-core) 82IMCXpulp	GAP-8 (octa-core) RISC-V RV32IMCXpulp		
		Clock Cycles	Milliseconds	Clock Cycles	Milliseconds	
MNIST	pcap_co_q7	9.45M	55.59	1.58M	9.27	
7x7x16x64 (M)	pcap_ho_q7	9.40M	55.27	1.19M	7.02	
	pcap_howo_q7	9.49M	55.85	1.18M	6.95	
smallNORB	pcap_co_q7	57.69M	339.35	9.40M	55.32	
7x7x32x64(L)	pcap_ho_q7	58.27M	342.76	11.48M	67.53	
	pcap_howo_q7	57.70M	339.39	11.40M	67.07	
CIFAR-10	pcap_co_q7	1.73M	10.15	0.27M	1.59	
3x3x64x64(S)	pcap_ho_q7	1.74M	10.26	0.43M	2.55	
	pcap_howo_q7	1.72M	10.15	0.22M	1.30	

Table 6: Evaluation of the primary capsule functions for RISC-V MCUs

When compared to Arm, the RISC-V implementation completely outperform by almost two orders of magnitude. As the RISC-V RV32IMCXpulp ISA provides SIMD instructions specifically tailored for the simultaneous MAC of two 4x8-bit operands, it requires far less time for the same matrix multiplication kernel. For a single-core setting on the smallNORB dataset, STM32L552ZET6QU is 5.01x slower than the RISC-V MCU (*pcap_q7_fast vs. pcap_co_q7*).

5.3 Capsule Layer

We tested the function implementing a capsule layer on the three reference datasets. Tables 7 and 8 detail the results for the Arm Cortex-M and RISC-V MCUs, respectively. Considering only the single-core scenario, we observe that the RISC-V implementation outperforms Arm. This arises as a direct consequence of the more efficient matrix multiplication kernel deployed in RISC-V (Section 5.2.1). As detailed in Section 3.4, three of the four support functions composing the capsule layer rely on matrix multiplication. As matrix multiplication is more efficient in RISC-V MCUs, due to the use of appropriate SIMD, the capsule layer function will deliver results with lower latency. When comparing the fastest of the Arm Cortex-M MCUs in terms of clock cycles (STM32L552ZET6QU) against the RISC-V MCU in single-core mode, the latter is on average 3.95x faster. Regarding the octa-core setting of the RISC-V MCU, we can observe that this setting is on average 7.43x faster than the single-core setting. This means that the *cap_parallel_q7* function is very near to the theoretical perfect parallelization over all the cores of the acceleration cluster.

Dataset		STM32L4R5ZIT6U (Armv7E-M, Cortex-M4)		STM32H755ZIT6U (Armv7E-M, Cortex-M7)		STM32L552ZET6QU (Armv8-M, Cortex-M33)	
		Clock Cycles	Milliseconds	Clock Cycles	Milliseconds	Clock Cycles	Milliseconds
MNIST 10x1024x6x4 (L)	cap_q7	40.63M	338.56	49.63M	103.40	23.54	213.97
smallNORB 5x1600x6x4 (M)	cap_q7	32.12M	267.65	43.49M	90.60	20.45	185.90
CIFAR-10 10x64x5x4 (S)	cap_q7	9.55M	79.58	14.22M	29.63	6.91	62.81

Table 7: Evaluation of the capsule functions for Arm Cortex-M MCUs

Table 8: Evaluation of the capsule functions for RISC-V MCUs

Dataset		GAP-8 (si RISC-V RV3	ngle-core) 32IMCXpulp	GAP-8 (octa-core) RISC-V RV32IMCXpulp		
		Clock Cycles	Milliseconds	Clock Cycles	Milliseconds	
MNIST 10x1024x6x4 (L)	cap_parallel_q7	20.32M	119.52	7.96M	46.83	
smallNORB 5x1600x6x4 (M)	cap_parallel_q7	16.26M	95.64	6.46M	38.03	
CIFAR-10 10x64x5x4 (S)	cap_parallel_q7	4.55M	26.77	1.92M	11.28	

6 Related Work

Zhang et al. [2020] proposed a hybrid computing architecture to accelerate the routing procedure of CapsNets during inference in GPU platforms. The authors claim that even in modern GPUs, CapsNets exhibit low efficiency due to their routing procedure. Through runtime profiling, Zhang et al. [2020] showed that the inefficiency of the routing procedure emerges from (i) tremendous data access to off-chip memory and (ii) intensive synchronizations to avoid race conditions on the limited GPU on-chip memory. To tackle this issue, the authors proposed a hybrid computing architecture named PIM-CapsNet. Pim-CapsNet offloads the routing procedure to an in-memory computation solution. Zhang et al. [2020] stated their hybrid computing architecture is 2.44x faster than a GPU-only execution. The previous work was later extended with software optimizations. After profiling, Zhang et al. [2021] stated that (i) nearby capsules have similar coupling coefficients (ii) and not all capsules require the same routing iterations to get stable coupling coefficients. Zhang et al. [2021] proposed then to group capsules in 3x3 groups, where only the central capsule is used in the computation of the coupling coefficients. To address the latter finding, Zhang et al. [2021] grouped capsules in two distinct groups: (i) one containing the capsules whose coupling coefficients are relatively stable and does not require the total routing iterations; (ii) and the other containing the capsules that benefit from the maximum number of iterations. With this software optimization, Zhang et al. [2021] achieved a significantly 3.41x speedup.

To counteract the intensive matrix multiplications and the complexity of the dynamic routing, Marchisio et al. [2021] proposed an RTL-level hardware architecture. At the core of their hardware accelerator, there is a processing element array, which is responsible for all matrix operations. This hardware accelerator also includes units specialized to speed up the *ReLU*, *squash*, and *softmax* activations. Despite only supporting inputs as 8-bit integers, the bit-width of internal operations varies along the pipeline. To thread off the area, delay, and energy consumption of the accelerator, Marchisio et al. [2021] developed a framework that takes as input a given CapsNet model and a general architecture of the CapsNet accelerator and returns a set of optimal parameters for the accelerator. Results showed that the accelerator is 6x faster than a GPU-only solution (Nvidia GTX1070) [Marchisio et al., 2021]. Based on this work, Park et al. [2020] proposed an accelerator enhanced for 3D CapsNets. This newer accelerator relies on a convolution core with 4 arrays of processing elements, each one designed for multiplications with 8-bit operands. For the design of the dynamic routing core, Park et al. [2020] stated that most of the coupling coefficients practically maintain their value between updates. The dynamic routing core was designed to skip the route operation when the variation is less than 0.005%. These optimizations combined resulted in an accelerator that consumes 53.27% less energy than the solution proposed by Marchisio et al. [2021].

In an attempt to reduce the memory footprint of CapsNet, Marchisio et al. [2020a] proposed a quantization framework. This framework explores different layer-wise and operation-wise precisions for obtaining a quantized CapsNet that trades off the classification accuracy and memory footprint. For this purpose, it takes as input a trained CapsNet model, a library of rounding schemes, an accuracy tolerance, and a maximum memory budget. For a CapsNet trained on the CIFAR-10 dataset, the framework reduces the memory footprint by 83% with only 0.15% accuracy loss.

Kakillioglu et al. [2020] proposed a weight pruning technique to reduce the large set of parameters in CapsNets based on dynamic routing, enabling their deployment in resource-constrained devices. Weight pruning techniques work by removing connections between neurons of a trained model. Weights in a tensor are ranked according to their magnitude and then the smallest of them, for a given percentage, are set to zero. The layer-wise pruning technique developed by Kakillioglu et al. [2020] enabled the deployment of CapsNets using 84.93% to 97.01% less memory than the original model proposed by Sabour et al. [2017].

6.1 Gap Analysis

While previous studies accelerate the inference pass of CapsNets on GPUs, ASICs, and FPGA platforms, this paper goes a step further and evaluates the deployment of CapsNets on off-the-shelf Arm and RISC-V MCUs targeted for intelligent IoT nodes. We extended ready-available APIs (CMSIS-NN and PULP-NN) for quantized ANNs to support both primary capsule and capsule layers. As detailed in Table 9, while previous solutions propose hardware accelerators to tackle the heavy computation of CapsNets, we limit the computation spectrum to resource-constrained MCUs ready-available on the market. In addition to the price savings, this approach also has the potential to accelerate the adoption of CapsNets on the edge as it does not require novel and specific hardware solutions to be deployed. As our software kernels only support fixed 8-bit data, we developed a quantization framework. Due to constraints of CMSIS-NN and PULP-NN, our framework does not adopt a mixed bit-width quantization scheme as Marchisio et al. [2020a].

Future work may encompass the tune of our software kernels, along with the required kernels of CMSIS-NN and PULP-NN, to support mixed bit-width. We believe that mixed bit-width quantization can further enhance our software kernels, as it gives more precision to weights with a higher impact on the final decision while reducing the precision of the others. This would be the perfect trade-off between memory footprint reduction and accuracy loss. Following the work from Kakillioglu et al. [2020], we may also use a pruning scheme to enhance our quantization framework. This will also require the tune of our software kernels with techniques to optimize the loading and storing of zeroes in memory. Nevertheless, results detailed in Section 3 show that our software kernels, at this stage of development, already achieve impressive gains in terms of memory footprint and latency, while relying on low-cost platforms available on the market. It is unfeasible to compare the latency speedup, memory footprint reduction, and accuracy loss of our solution with the others on Table 9 as the baseline reference is not the same.

R&D Study	Target Platform	Problems Addressed	Proposal
Zhang et al. [2020]	GPU	Latency	1. Hardware accelerator to offload the computation of the dynamic routing from the GPU
Zhang et al. [2021]	GPU	Latency	1. Software optimization to optimize the dynamic routing on an hardware accelerator coupled to a GPU
Marchisio et al. [2021]	FPGA	Latency Energy	 RTL-level hardware architecture for CapsNet inference Software to optimize the RTL architecture given a CapsNet
Park et al. [2020]	ASIC	Latency Energy	1. RTL-level hardware architecture for 3D CapsNet inference
Marchisio et al. [2020a]	GPU FPGA	Memory	1. CapsNet quantization tool supporting mixed bit-width
Kakillioglu et al. [2020]	GPU CPU	Memory	1. Weight pruning tailored for CapsNets
Costa et. al	MCU	Memory Latency	 CapsNet quantization tool supporting fixed int-8 data API for CapsNets inference in Armv7E-M, Armv8-M MCUs API for CapsNets inference in RISC-V (RV32IMCXpulp) MCUs

Table 9: Functionality of previous research against our approach

7 Conclusion

In this paper, we proposed the first public and open-source software kernels to enable the deployment of CapsNets in Arm Cortex-M and RISC-V MCUs. We extended the CMSIS-NN and PULP-NN to support the inference pass of CapsNets. As CapsNets are typically trained in 32-bit floating-point and low-end MCUs usually do not feature an FPU, we also proposed a framework, built upon TensorFlow, to quantize CapsNets to int-8 data.

Results show that our work succeeds in addressing the latency and memory footprint problems inherent to CapsNets, proving that it is possible to efficiently implement them on the deep edge. Our quantization framework reduces the memory footprint of a CapsNet by about 75% with negligible accuracy loss. Furthermore, the latency induced by our software kernels on the execution of a primary capsule or capsule layer with medium-sized kernels can be lower than a few tenths of a second. To the best of our knowledge, this is the first work evaluating the deployment of quantized CapsNet on resource-constrained MCUs.

References

- Sara Sabour, Nicholas Frosst, and Geoffrey E. Hinton. Dynamic routing between capsules. In *Proceedings of the 31st International Conference on Neural Information Processing Systems*, NIPS'17, page 3859–3869, Red Hook, NY, USA, 2017. Curran Associates Inc. ISBN 9781510860964.
- Mensah Kwabena Patrick, Adebayo Felix Adekoya, Ayidzoe Abra Mighty, and Baagyire Y. Edward. Capsule networks a survey. *Journal of King Saud University Computer and Information Sciences*, 2019. ISSN 1319-1578. doi:https://doi.org/10.1016/j.jksuci.2019.09.014. URL https://www.sciencedirect.com/science/article/pii/S1319157819309322.
- El Alaoui-Elfels, Omaima and Gadi, Taoufiq. From auto-encoders to capsule networks: A survey. *E3S Web Conf.*, 229: 01003, 2021. doi:10.1051/e3sconf/202122901003. URL https://doi.org/10.1051/e3sconf/202122901003.
- Jiawei Su, Danilo Vasconcellos Vargas, and Kouichi Sakurai. One pixel attack for fooling deep neural networks. *IEEE Transactions on Evolutionary Computation*, 23(5):828–841, 2019. doi:10.1109/TEVC.2019.2890858.
- Koosha Sadeghi, Ayan Banerjee, and Sandeep K. S. Gupta. A system-driven taxonomy of attacks and defenses in adversarial machine learning. *IEEE Transactions on Emerging Topics in Computational Intelligence*, 4(4):450–467, 2020. doi:10.1109/TETCI.2020.2968933.
- Geoffrey E. Hinton, Alex Krizhevsky, and Sida D. Wang. Transforming auto-encoders. In *Proceedings of the 21th International Conference on Artificial Neural Networks Volume Part I*, ICANN'11, page 44–51, Berlin, Heidelberg, 2011. Springer-Verlag. ISBN 9783642217340.
- Geoffrey E Hinton, Sara Sabour, and Nicholas Frosst. Matrix capsules with EM routing. In *International Conference* on Learning Representations, 2018. URL https://openreview.net/forum?id=HJWLfGWRb.
- Adam Kosiorek, Sara Sabour, Yee Whye Teh, and Geoffrey E Hinton. Stacked capsule autoencoders. In H. Wallach, H. Larochelle, A. Beygelzimer, F. d'Alché-Buc, E. Fox, and R. Garnett, editors, *Advances in Neural Information Processing Systems*, volume 32. Curran Associates, Inc., 2019.
- Suat Toraman, Talha Burak Alakus, and Ibrahim Turkoglu. Convolutional capsnet: A novel artificial neural network approach to detect covid-19 disease from x-ray images using capsule networks. *Chaos, Solitons & Fractals*, 140:110122, 2020. ISSN 0960-0779. doi:https://doi.org/10.1016/j.chaos.2020.110122. URL https://www.sciencedirect.com/science/article/pii/S0960077920305191.
- Amara Dinesh Kumar. Novel Deep Learning Model for Traffic Sign Detection Using Capsule Networks. *arXiv e-prints*, art. arXiv:1805.04424, May 2018.
- Neelavathy Pari S., T. Mohana, and V. Akshaya. Real-time traffic sign detection using capsule network. In 2019 11th International Conference on Advanced Computing (ICoAC), pages 193–196, 2019. doi:10.1109/ICoAC48765.2019.247140.
- Mingxuan Wang, Jun Xie, Zhixing Tan, Jinsong Su, Deyi Xiong, and Chao Bian. Towards linear time neural machine translation with capsule networks. *CoRR*, abs/1811.00287, 2018. URL http://arxiv.org/abs/1811.00287.
- Reza Katebi, Yadi Zhou, Ryan Chornock, and Razvan Bunescu. Galaxy morphology prediction using Capsule Networks. *Monthly Notices of the Royal Astronomical Society*, 486(2):1539–1547, 04 2019. ISSN 0035-8711. doi:10.1093/mnras/stz915. URL https://doi.org/10.1093/mnras/stz915.
- Xingyao Zhang, Shuaiwen Leon Song, Chenhao Xie, Jing Wang, Weigong Zhang, and Xin Fu. Enabling highly efficient capsule networks processing through a pim-based architecture design. In 2020 IEEE International Symposium on High Performance Computer Architecture (HPCA), pages 542–555, 2020. doi:10.1109/HPCA47549.2020.00051.

- Alberto Marchisio, Beatrice Bussolino, Alessio Colucci, Maurizio Martina, Guido Masera, and Muhammad Shafique. Q-capsnets: A specialized framework for quantizing capsule networks. In 2020 57th ACM/IEEE Design Automation Conference (DAC), pages 1–6, 2020a. doi:10.1109/DAC18072.2020.9218746.
- Alberto Marchisio, Vojtech Mrazek, Muhammad Abdullah Hanif, and Muhammad Shafique. Descnet: Developing efficient scratchpad memories for capsule network hardware. *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, pages 1–1, 2020b. doi:10.1109/TCAD.2020.3030610.
- Alberto Marchisio, Vojtech Mrazek, Muhammad Abdullah Hanif, and Muhammad Shafique. Feeca: Design space exploration for low-latency and energy-efficient capsule network accelerators. *IEEE Transactions on Very Large Scale Integration (VLSI) Systems*, 29(4):716–729, 2021. doi:10.1109/TVLSI.2021.3059518.
- Xingyao Zhang, Xin Fu, Donglin Zhuang, Chenhao Xie, and Shuaiwen Leon Song. Enabling highly efficient capsule networks processing through software-hardware co-design. *IEEE Transactions on Computers*, 70(4):495–510, 2021. doi:10.1109/TC.2021.3056929.
- Gwangtae Park, Dongseok Im, Donghyeon Han, and Hoi-Jun Yoo. A 1.15 tops/w energy-efficient capsule network accelerator for real-time 3d point cloud segmentation in mobile environment. *IEEE Transactions on Circuits and Systems II: Express Briefs*, 67(9):1594–1598, 2020. doi:10.1109/TCSII.2020.3005191.
- Burak Kakillioglu, Ao Ren, Yanzhi Wang, and Senem Velipasalar. 3d capsule networks for object classification with weight pruning. *IEEE Access*, 8:27393–27405, 2020. doi:10.1109/ACCESS.2020.2971950.
- Ion Stoica, Dawn Song, Raluca Ada Popa, David A. Patterson, Michael W. Mahoney, Randy H. Katz, Anthony D. Joseph, Michael I. Jordan, Joseph M. Hellerstein, Joseph E. Gonzalez, Ken Goldberg, Ali Ghodsi, David E. Culler, and Pieter Abbeel. A berkeley view of systems challenges for AI. CoRR, abs/1712.05855, 2017. URL http://arxiv.org/abs/1712.05855.
- Liangzhen Lai, Naveen Suda, and Vikas Chandra. CMSIS-NN: efficient neural network kernels for arm cortex-m cpus. *CoRR*, abs/1801.06601, 2018. URL http://arxiv.org/abs/1801.06601.
- Mário P. Véstias, Rui Policarpo Duarte, José T. de Sousa, and Horácio C. Neto. Moving deep learning to the edge. *Algorithms*, 13(5), 2020. ISSN 1999-4893. doi:10.3390/a13050125. URL https://www.mdpi.com/1999-4893/ 13/5/125.
- He Li, Kaoru Ota, and Mianxiong Dong. Learning iot in edge: Deep learning for the internet of things with edge computing. *IEEE Network*, 32(1):96–101, 2018. doi:10.1109/MNET.2018.1700202.
- Angelo Garofalo, Manuele Rusci, Francesco Conti, Davide Rossi, and Luca Benini. Pulp-nn: accelerating quantized neural networks on parallel ultra-low-power risc-v processors. *Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences*, 378(2164):20190155, 2020. doi:10.1098/rsta.2019.0155. URL https://royalsocietypublishing.org/doi/abs/10.1098/rsta.2019.0155.
- Miguel Costa, Daniel Oliveira, Sandro Pinto, and Adriano Tavares. Detecting driver's fatigue, distraction and activity using a non-intrusive ai-based monitoring system. *Journal of Artificial Intelligence and Soft Computing Research*, 9 (4):247–266, 2019. doi:doi:10.2478/jaiscr-2019-0007. URL https://doi.org/10.2478/jaiscr-2019-0007.
- Jiahao Lu, Dongsheng Liu, Zilong Liu, Xuan Cheng, Lai Wei, Cong Zhang, Xuecheng Zou, and Bo Liu. Efficient hardware architecture of convolutional neural network for ecg classification in wearable healthcare device. *IEEE Transactions on Circuits and Systems I: Regular Papers*, 68(7):2976–2985, 2021. doi:10.1109/TCSI.2021.3072622.
- Jiawei Li, Qichen Zhao, Nan Li, Lin Ma, Xuan Xia, Xiaoguang Zhang, Ning Ding, and Nannan Li. A survey on capsule networks: Evolution, application, and future development. In 2021 International Conference on High Performance Big Data and Intelligent Systems (HPBD IS), pages 177–185, 2021. doi:10.1109/HPBDIS53214.2021.9658349.
- Zengguo Sun, Guodong Zhao, Rafał Scherer, Wei Wei, and Marcin Woźniak. Overview of capsule neural networks. *Journal of Internet Technology*, 23(1):33–44, 2022. ISSN 2079-4029.
- Amir Gholami, Sehoon Kim, Zhen Dong, Zhewei Yao, Michael W. Mahoney, and Kurt Keutzer. A survey of quantization methods for efficient neural network inference. CoRR, abs/2103.13630, 2021. URL https://arxiv.org/abs/ 2103.13630.
- Hao Wu, Patrick Judd, Xiaojie Zhang, Mikhail Isaev, and Paulius Micikevicius. Integer quantization for deep learning inference: Principles and empirical evaluation. *CoRR*, abs/2004.09602, 2020. URL https://arxiv.org/abs/2004.09602.
- Tailin Liang, John Glossner, Lei Wang, and Shaobo Shi. Pruning and quantization for deep neural network acceleration: A survey. *CoRR*, abs/2101.09671, 2021. URL https://arxiv.org/abs/2101.09671.
- Pierre-Emmanuel Novac, Ghouthi Boukli Hacene, Alain Pegatoquet, Benoît Miramond, and Vincent Gripon. Quantization and deployment of deep neural networks on microcontrollers. *Sensors*, 21(9), 2021. ISSN 1424-8220. doi:10.3390/s21092984. URL https://www.mdpi.com/1424-8220/21/9/2984.

- Peisong Wang, Qiang Chen, Xiangyu He, and Jian Cheng. Towards accurate post-training network quantization via bit-split and stitching. In Hal Daumé III and Aarti Singh, editors, *Proceedings of the 37th International Conference* on Machine Learning, volume 119 of Proceedings of Machine Learning Research, pages 9847–9856. PMLR, 13–18 Jul 2020. URL http://proceedings.mlr.press/v119/wang20c.html.
- Benoit Jacob, Skirmantas Kligys, Bo Chen, Menglong Zhu, Matthew Tang, Andrew Howard, Hartwig Adam, and Dmitry Kalenichenko. Quantization and training of neural networks for efficient integer-arithmetic-only inference. In 2018 IEEE/CVF Conference on Computer Vision and Pattern Recognition, pages 2704–2713, 2018. doi:10.1109/CVPR.2018.00286.
- H. Dong, Z. Ding, and S. Zhang. *Deep Reinforcement Learning: Fundamentals, Research and Applications*. Springer Singapore, 2020. ISBN 9789811540950. URL https://books.google.pt/books?id=31juDwAAQBAJ.
- Eric Flamand, Davide Rossi, Francesco Conti, Igor Loi, Antonio Pullini, Florent Rotenberg, and Luca Benini. Gap-8: A risc-v soc for ai at the edge of the iot. In 2018 IEEE 29th International Conference on Application-specific Systems, Architectures and Processors (ASAP), pages 1–4, 2018. doi:10.1109/ASAP.2018.8445101.
- B. Ram. Numerical Methods. Pearson, 2009. ISBN 9788131732212. URL https://books.google.pt/books? id=16cZ2HMo2tUC.
- Y. Lecun, L. Bottou, Y. Bengio, and P. Haffner. Gradient-based learning applied to document recognition. *Proceedings of the IEEE*, 86(11):2278–2324, 1998. doi:10.1109/5.726791.
- Y. LeCun, Fu Jie Huang, and L. Bottou. Learning methods for generic object recognition with invariance to pose and lighting. In *Proceedings of the 2004 IEEE Computer Society Conference on Computer Vision and Pattern Recognition, 2004. CVPR 2004.*, volume 2, pages II–104 Vol.2, 2004. doi:10.1109/CVPR.2004.1315150.

Alex Krizhevsky. Learning multiple layers of features from tiny images. Technical report, 2009.