

Sampling sufficiency for mechanical properties of wood

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ABSTRACT

Based on most recently published studies, there is a large variability in both the mechanical properties of wood and sample sizes selected to evaluate them. This study aims to define sampling sufficiency for some mechanical properties of wood, which were bending strength, bending modulus, compressive strength, compressive modulus, hardness, and shear strength. The mechanical tests were carried out according to the ASTM D143 on wood samples cut from clonal *Eucalyptus* planted in southern Brazil. Sampling sufficiency was determined by an intensive computational method based on resampling of original data using Monte Carlo simulations. The experimental tests data conformed to the normal distribution and most of the obtained sufficient sample sizes determined by Monte Carlo simulation were above those sample sizes used in most already published studies. Furthermore, properties related to wood stiffness presented smaller variabilities than their respective properties associated with wood strength, leading to smaller sample sizes for the former cases.

Keywords: Monte Carlo simulation, resampling, sampling sufficiency, wood stiffness, wood strength.

38 **INTRODUCTION**

39 Efficient use of any material depends on its physical-mechanical properties,
40 including mechanical features related to strength and stiffness. However, a reliable
41 determination of mechanical properties usually implies the destruction of the samples,
42 which may also represent expensive costs, as well as time and effort spent (Bros and
43 Cowell 1987). Therefore, the minimum number of necessary samples to be tested must
44 be determined to ensure a proper characterization of the targeted group of samples,
45 avoiding unnecessary losses, which is called sampling sufficiency (Bros and Cowell
46 1987). However, a suitable sample size may not be simply determined, although this
47 information is not clearly defined by most standards (DePatta Pillar 1998).

48 The distribution of the sample mean (also called “expected value” of M) is a
49 widely used method to determine sample sizes used in experimental studies and it is a
50 valid solution for some properties of many materials (Adcock 1997). However,
51 mechanical properties vary in different ranges depending on the targeted material, this
52 uncertainty affects the number of samples that must be evaluated to ensure reliable results
53 (Bros and Cowell 1987, DePatta Pillar 1998).

54 The multiple variables that influence the mechanical properties in woods generate
55 a complex system of correlations, making the determination of sample sizes extremely
56 difficult, uncertain, and sometimes, even unreliable. Wood is a natural, heterogeneous,
57 and anisotropic material that may display a wide range of mechanical, chemical and
58 hygroscopic properties (Amer *et al.* 2019), which also may depend on wood specie, tree
59 maturity, and density (Amer *et al.* 2021). Moreover, wood characteristics also depend on
60 forest factors (cultivation, location, local climate, etc.) (Hein *et al.* 2016), harvesting
61 factors (overthrow process, different radial position, different axial position, etc.) (Hein
62 *et al.* 2016, Moraisa and Pereira 2007), cutting processes (Svensson and Toratti 2002,

63 Rapp *et al.* 2007) and supply factors (transportation condition, storage condition and
64 wood age) (Bao *et al.* 2001, Dünisch *et al.* 2010).

65 ASTM D143 (ASTM 2021) is a globally known standard procedure devoted to
66 establishing good practices for determining physical and mechanical properties of small
67 and clean wood samples. However, this standard does not specify how many samples
68 should be evaluated for the correct determination of each mechanical property. This
69 uncertainty has been leading to a wide variety of adopted sample sizes in recent studies
70 on physical-mechanical properties of wood. For that, Bao *et al.* (2001) evaluated strength
71 and stiffness of juvenile and mature woods from ten species and 30 samples were selected
72 for each test. Ghorbani-Kookandeh *et al.* (2014) investigated the beech wood
73 impregnated and heat-treated. They carried out static bending, compression strength
74 parallel to grain, and hardness tests by using five samples for each test. Furthermore,
75 Taghiyari (2011) used 60 samples to determine modulus of rupture (MOR) and modulus
76 of elasticity (MOE) in compression parallel to grain tests for the heat-treated *Populus*
77 *nigra* wood. In addition, some studies even did not report the number of samples used for
78 each mechanical test (Santos 2000, Wessels *et al.* 2016).

79 Resampling methods could be an alternative to determine sampling sufficiency
80 and avoid unnecessary large samplings. It estimates the accuracy of means, medians,
81 variances, and percentiles of sampling by using subsets of the available data or randomly
82 generating new samplings by resampling the data set (Edwards *et al.* 2011). The
83 resampling methods such as Bootstrapping (Edwards *et al.* 2011), Jackknifing (Wang and
84 Yu 2020), Permutation (Fieberg *et al.* 2020) and Cross-Validation (Shimodaira 2016)
85 have been used for estimating the sample sizes in many areas, such as ecology (DePatta
86 Pillar 1998), biomedicine (Dwivedi *et al.* 2017), zoology (Dimauro *et al.* 2009), and
87 genetics (Kess and El-Kassaby 2014).

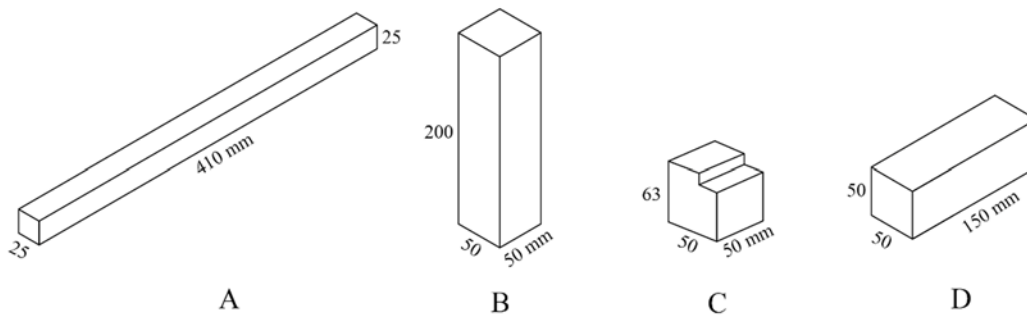
88 The resampling methods based on Monte Carlo simulations have many
89 advantages since this type of method relies upon the use of randomness to solve problems
90 from a deterministic system, encompassing a large number of possible outcomes from the
91 targeted sample (Papadopoulos and Yeung 2001). Taking these facts into account, this
92 study aimed to use Monte Carlo simulations to determine sampling sufficiency for
93 mechanical properties of *Eucalyptus* wood, which were determined according to ASTM
94 D143 (ASTM 2021).

95 **MATERIALS AND METHODS**

96 **Material selection and samples preparation**

97 The studied wood samples were obtained from a clonal test of interspecific
98 hybrids of *Eucalyptus* clones. 29 *Eucalyptus* clones were randomly selected in a planted
99 forest located in southern Brazil following the ASTM D5536 (ASTM 2010). 8 seven-
100 year-old trees by clone were felled, totaling 232 trees. The selected trees had straight
101 trunks, an absence of bifurcation, good phytosanitary conditions and a low presence of
102 defects. Boards were cut from the 1,2 m long baseline logs, which presented a diameter
103 at breast height of around 21 cm.

104 The boards were air dried and their thicknesses were reduced from 8 cm to 6 cm
105 using a thinner plane. For each test, 54 samples were cut according to the requirements
106 of ASTM D143 (ASTM 2021), as shown in Figure 1, avoiding the presence of growth
107 defects, such as knots, splits, etc. Before the mechanical tests, the samples were placed
108 into a climatic chamber (20 °C and 65 % relative humidity) until reaching equilibrium
109 humidity of approximately 12 %. Weight and dimensions (measured in the sample centre)
110 were determined using an analytical scale and a digital calliper, respectively.



111

112 **Figure 1:** Three-point static bending (a), Compression parallel to grain (b), shear parallel
113 to grain (c) and Janka hardness (d) samples geometry for the mechanical tests.

114 Mechanical tests

115 Three points static bending

116 The three points static bending tests were performed according to ASTM D143
117 (ASTM 2021). The wood samples were cut with dimensions of $25 \times 25 \times 410 \text{ mm}^3$ (radial
118 \times tangential \times longitudinal) and a span length of 360 mm was adjusted, keeping a
119 minimum span-to-depth ratio of 14. An Emic DL 30000 universal testing machine was
120 used for applying the load continuously in the centre of the beam throughout the test at a
121 rate of motion of 1,3 mm/min. The load was applied at the tangential plane of the samples
122 and the mid-span deflection was determined by the crosshead position.

123 Flexural strength (σ_f) was calculated using the relationship between the
124 applied load and the measurements of mid-span deflection of the test sample in
125 accordance with Eq. 1. Modulus of elasticity (E_f) was calculated by Eq. 2 using the
126 gradient (∇m) obtained from the ratio of the load vs. deflection curve in the elastic region.
127 These samples presented an equilibrium moisture content mean of 14,05 % with a
128 standard deviation of 0,63 %.

129

130

$$\sigma_f = \frac{3 \cdot F_{\max} (\text{N}) \cdot L (\text{mm})}{2 \cdot b (\text{mm}) \cdot h^2 (\text{mm}^2)} \quad (1)$$

131

$$E_f = \frac{L^3 (\text{mm}^3) \cdot \nabla m (\text{N} \cdot \text{mm}^{-1})}{4 \cdot b (\text{mm}) \cdot h^3 (\text{mm}^3)} \quad (2)$$

132
133 Where: b, h, and L are the width and height of the specimen, and support span length,
134 respectively.

135 **Compression parallel to grain**

136 Compressive modulus and compressive strength were determined using
137 compression parallel to grain tests in samples with dimensions of 50 x 50 x 200 mm³
138 (radial × tangential × longitudinal directions). These samples were cut assuring that the
139 end grain surfaces were parallel to each other and at right angles to the longitudinal axis.
140 A crosshead speed of 0,6 mm/min was applied using an Emic DL 30000 universal testing
141 machine, following ASTM D143 (ASTM 2021).

142 The compressive strength parallel to grain (σ_c) was obtained by the
143 relation of the maximum achieved load (F_{max}) and the cross-sectional dimension at the
144 middle of the specimen (A) according to Eq. 3. Compressive modulus (E_c) was the ratio
145 obtained from the stress (σ_c) vs. deformation (ε_c) curve in the elastic region (Eq. 4). These
146 samples presented an equilibrium moisture content mean of 12,82 % with a standard
147 deviation of 0,75 %.

$$148 \quad \sigma_c = \frac{F_{max} (N)}{A (mm^2)} \quad (3)$$

$$149 \quad E_c = \frac{\sigma_c (MPa)}{\varepsilon_c (\%)} \quad (4)$$

150 **Shear Parallel to Grain**

151 The shear parallel to grain tests were performed to determine shear strength.
152 Specimens with the dimensions of 50 x 50 x 63 mm³ (radial × tangential × longitudinal
153 directions) were cut and tested according to ASTM D143 (ASTM 2021). A shear tool
154 was used to provide a 3 mm offset between the inner edge of the supporting surface and
155 the plane of its adjacent edge. The load was continuously applied at a rate of motion of
156 0,6 mm/min in an Emic DL 30000 universal testing machine. The ultimate shear stress

157 was calculated according to Eq. 5. Using the maximum load (F_{\max}) and the shear cross-
158 section (A). These samples presented an equilibrium moisture content mean of 13,04 %
159 with a standard deviation of 1,22 %.

$$160 \quad \sigma_s = \frac{F_{\max} \text{ (N)}}{A \text{ (mm}^2\text{)}} \quad (5)$$

161

162 **Janka hardness**

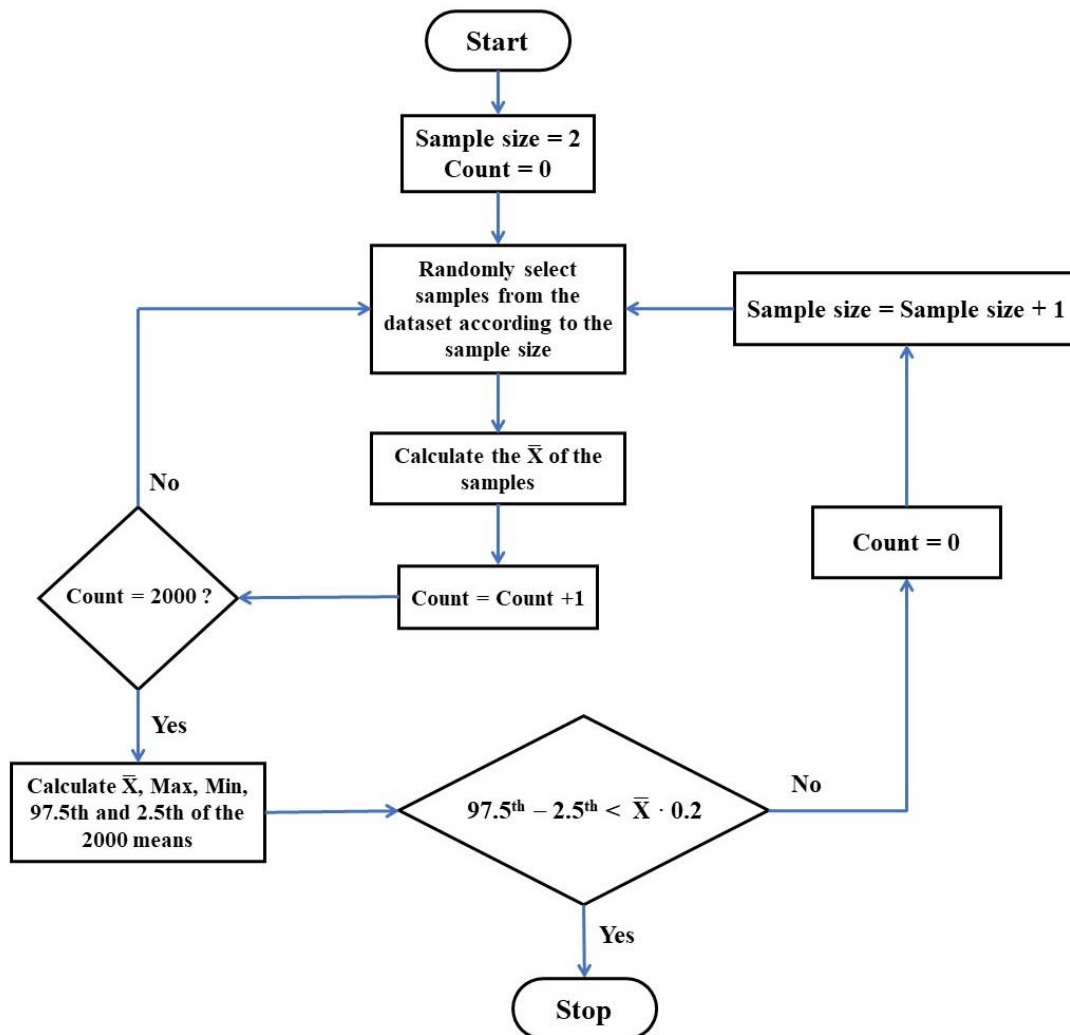
163 Janka hardness was determined on the tangential plane of 50 x 50 x 150 mm³
164 (radial × tangential × longitudinal directions) specimens. A hemisphere with 11,3 mm in
165 diameter penetrated 5,65 mm on the tangential plane of samples. The hardness is
166 considered as the ratio between the maximum load and the indentation area, as shown in
167 Eq. 6. These tests were carried out at a rate of motion of the movable crosshead of 6
168 mm/min in an Emic DL 30000 universal testing machine. Two penetrations were
169 performed for each sample, which were far enough from the sample edges to prevent
170 splitting or chipping, according to ASTM D143 (ASTM 2021). These samples presented
171 an equilibrium moisture content mean of 13,85 % with a standard deviation of 1,33 %.

$$172 \quad \text{Hardness} = \frac{F_{\max} \text{ (N)}}{A \text{ (mm}^2\text{)}} \quad (6)$$

173 **Monte Carlo simulation**

174 Data normality was verified using Shapiro-Wilk tests and sampling sufficiency to infer
175 mechanical properties was performed through confidence intervals. This method was
176 similar to some previous studies on anatomy, ecology, limnology, and phytotechny ,
177 Storck *et al.* 2012). The sample sizes (n= 54) and confidence levels ($1 - \alpha = 0,95$) were
178 fixed in all mechanical tests considered. In the simulation procedure, 30 sample sizes
179 (from 2 to 30) were designed for each property. After that, 2000 resampling with
180 replacements from the pseudo-population of the original 54 data were done for each
181 sample size. Minimum, 2,5th percentile, mean, 97,5th percentile, and maximum were

182 determined and the confidence level of each sample size was equal to the difference
 183 between the 97,5th percentile and 2,5th percentile. Sampling sufficiency was considered
 184 as the lowest sample size in which the amplitude of the confidence interval was lower
 185 than 20 % of its respective mean since this is an adequate variation range based on similar
 186 studies for the determination of mechanical properties of wood. These statistical analyses
 187 were performed using three software packages: Statgraphics 19® (for the descriptive
 188 statistics, R Development Core Team (for the Monte Carlo simulation), and Microsoft
 189 Excel (for graphics). The simplified flowchart of the used Monte Carlo simulation
 190 algorithm is presented in Figure 2.



191 **Figure 2:** Simplified flowchart of the used Monte Carlo simulation algorithm.

192 **RESULTS AND DISCUSSION**

193 **Mechanical test results**

194 Table 1 shows descriptive results of the collected data from mechanical tests. All
 195 the mechanical properties presented small values of standard deviations than those
 196 presented in the literature, which is probably due to the large sample sizes (n= 54) selected
 197 in the present study.

198 **Table 1:** Descriptive statistics of obtained results for the original sample size (n=54).

	Bending modulus	Bending strength	Compressive modulus	Compressive strength	Shear strength	Hardness
Maximum (MPa)	12699,381	90,271	17413,400	52,907	10,560	48,980
97,5 th (MPa)	11803,210	88,840	16786,984	51,396	10,363	47,271
\bar{X} (MPa)	9468,585	72,462	11634,509	41,623	7,508	37,613
sd (MPa)	1197,680	9,560	2509,308	4,695	1,420	4,999
CoV (%)	12,649	13,193	21,568	11,280	18,918	13,292
2,5 th (MPa)	7525,300	56,209	7449,340	33,263	5,043	28,444
Minimum (MPa)	7443,974	53,974	7378,900	32,790	4,350	27,600
Where: \bar{X} = mean; sd= standard deviation; CoV= coefficient of variation.						

199

200 The CoV values are 12,54 % and 13,05 % for bending modulus and bending
 201 strength, respectively. These CoV values are, in general, lower than those obtained for
 202 each of the 14 species studied by Carrillo *et al.* (2011), who used 30 samples for each
 203 species. The variations in the bending test may be attributed to the typical behaviour of
 204 small samples in a bending test, which is marked by an initial yielding on the compression
 205 side, accompanied by the enlargement of the compression zone, and then the neutral
 206 surface shifts toward the tensile side of the sample. As the tensile stress continues to
 207 increase, the ultimate stress is reached when a brittle failure at the tensile side occurs
 208 (Green 2001). However, according to Crespo *et al.* (2020), some specimens submitted to

209 bending tests may present a brittle failure due to small grain deviations without yielding
210 at the compression side.

211 The highest and the lowest CoV values were obtained for the compression parallel
212 to grain results. Compressive modulus and compressive strength reached CoV values of
213 17,91 % and 12,15 %, respectively. This corroborates Crespo *et al.* (2020), who studied
214 an *Eucalyptus globulus* Labill wood by using a 20 samples and reported a higher CoV
215 value for compressive modulus (29 %) compared to that associated with the compressive
216 strength (18 %). According to Mohebbi *et al.* (2014), the anisotropy of the wood
217 ultrastructure is one of the main factors that influences compressive strength (parallel to
218 grain). The crushing is the most common failure in compression tests and is usually
219 characterized by folding of the cellulose microfibrils that may begin in low stress levels
220 (Crespo *et al.* 2020). As the stress levels increase, the folding takes place at the cell wall
221 level and leads to the failure of the specimen (Green 2001).

222 Shear strength presented a variability similar to the other strength properties
223 (bending and compression), with a CoV of 12,97 %. This value is lower than those
224 obtained by authors that used smaller sample sizes than those adopted in this research.
225 Crespo *et. al* (2020) used a sample size of 44 for *Eucalyptus globulus* wood and obtained
226 a CoV of 19 %. Also, Trockenbrodt *et al.* (1999) achieved a 17 % CoV for 9 samples of
227 *Azadirachta excelsa* wood. Moreover, attempts to obtain shear failure perpendicular to
228 the grain according to certain standards, may result in other failure modes, such as
229 compression perpendicular to the grain. According to Kretschmann (1991), that may
230 occur because of the notch used to prevent the rotation of the rectangular prismatic
231 specimens proposed in the ASTM D143 (ASTM 2021), which causes an asymmetry in
232 the application of the force that promotes shear, inducing the appearance of normal tensile
233 stresses and normal compression in wood fibres. Finally, hardness data had a CoV value

234 of 12,67 %, which is smaller than those achieved by Salca and Hiziroglu (2014) for the 4
235 species studied, who used a 5 sample size for each species.

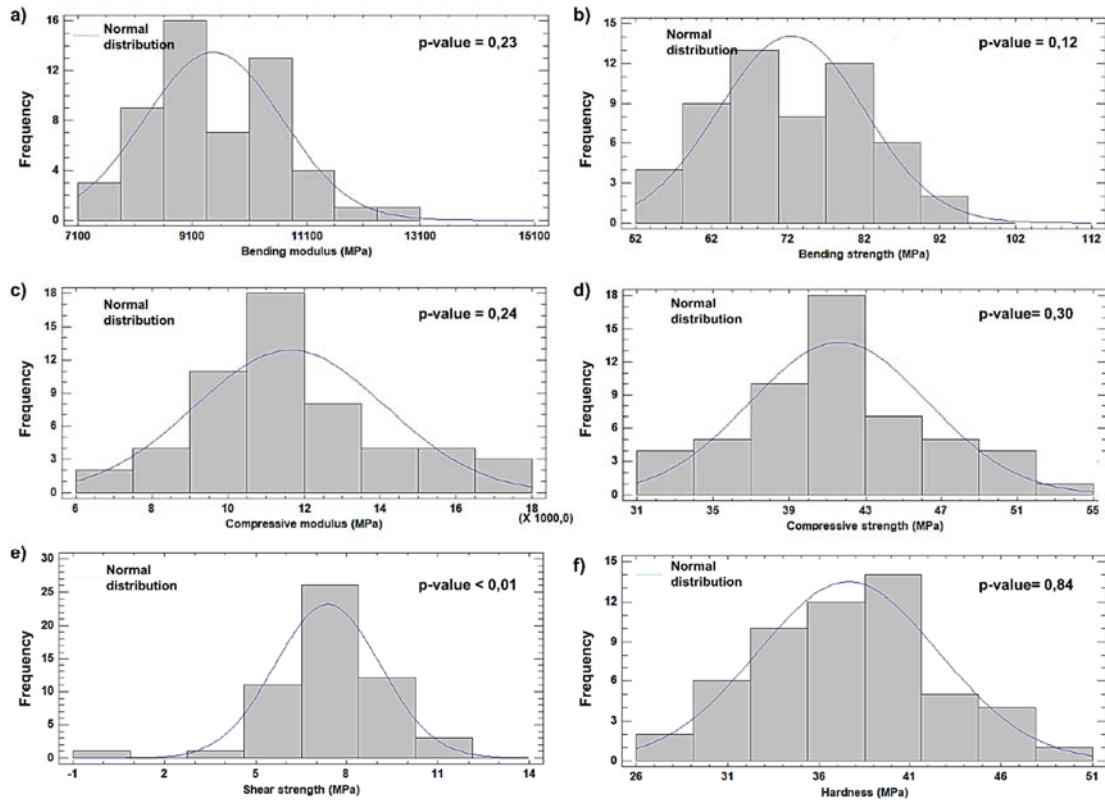
236 **Determination of sample sizes**

237 The results in this section present the sample size for each mechanical test, which
238 were obtained by the Monte Carlo methodology previously described. During the
239 determination of sample sufficiency, increases in small sample sizes cause a large
240 decrease in the standard error, while the same increase in large sample sizes may not
241 greatly affect the standard error (DePatta-Pillar 1998). Based on that, the determination
242 of sample size is crucial to achieve reliable results. Furthermore, this knowledge is
243 extremely necessary since obtaining experimental data is sometimes constrained by the
244 availability of raw materials and time.

245 Figure 1 displays histograms, in which the number of classes (k) was determined
246 according to the empirical rule ($k = \sqrt{n}$), where n is the sample size. Except for the shear
247 strength data, the p -values were above the significance level (0,05), which indicates that
248 all the obtained data conformed to the normal distribution according to the performed
249 Shapiro-Wilk tests. This is a valuable feature since most Monte Carlo simulations may
250 yield inaccurate results for non-parametric data, which also depends on the resampling
251 method.

252 As shown in Figure 3, the data of elasticity modulus in bending and axial
253 compression follow the normal distribution, resulting in small sample sizes for
254 sufficiency (9 and 12 samples, respectively). Despite this, many researchers adopted
255 lower sample sizes than those achieved for sampling sufficiency in this research. For
256 instance, Zhang *et al.* (2015) used 8 specimens of *Eucalyptus regnans* wood, while
257 Kothiyal (2014) used 4 to 6 samples to study intra clonal variations of *Eucalyptus*
258 *tereticornis*. However, it is also possible to find researches with much larger samples sizes

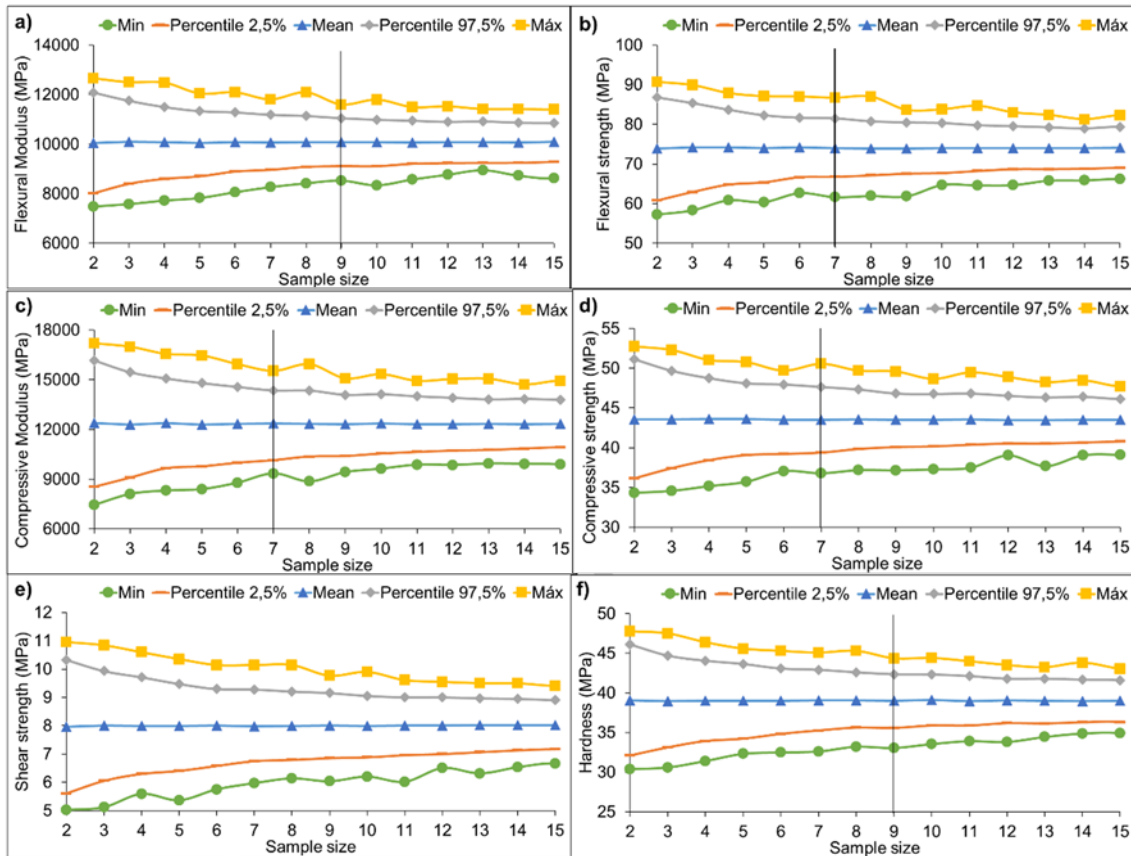
259 than those indicated by Monte Carlo in this study as sample sufficiency. In this sense,
260 Taghiyari (2011) used a 60 sample size of *Populus nigra* wood and Ferreira *et al.* (2019)
261 used 30 specimens of *Eucalyptus* clones.



262 **Figure 3:** Histograms and bell curves for the obtained data.

263 The sampling sufficiency results for the mechanical characteristics of the
264 *Eucalyptus* woods are shown in Figure 4. In general, the sample sufficiency for the test
265 was given in samples size wherein a low convergence rate was still visualized. This can
266 be related to the confidence level set as stop criteria (20 %), in which a lower confidence
267 level, the sample sufficiency would be given at a much higher sample size, where the
268 curves would decrease monotonically. We added this statement in the main text.
269 Regarding the wood stiffness, bending modulus reached sample sufficiency in 9 sample
270 size (Fig. 4a), while compressive modulus obtained sample sufficiency in 12 sample size
271 (Fig. 4c). The larger sampling sufficiency presented by the compressive modulus is
272 attributed to its higher CoV value when compared to the bending modulus.

273 Regarding wood strength, in both bending and compressive strength, the sample
 274 sufficiency reached 7 samples (Figs. 4b, 4d). This sample size is larger than the sizes
 275 adopted in some recent searches, such as Ghorbani Kookandeh *et al.* (2014) ($n = 5$) and
 276 Mohebbi *et al.* (2014) ($n = 6$) and lower than those adopted by Crespo *et al.* (2020) ($n =$
 277 22).



278

279 **Figure 4:** Monte Carlo confidence intervals for means for bending modulus (a), bending
 280 strength (b), compressive modulus (c), compressive strength (d), shear modulus (e), and
 281 hardness (f).

282 A sample sufficiency of 25 was determined for shear strength (Fig. 4e), which can
 283 be attributed to the low normality of the data obtained for this property (Fig. 3). This
 284 probably increased the sample size to this number of specimens, which is unusual based
 285 on recent researches. Although the CoV associated with the shear strength test did not
 286 differ from the other tests (12,97 %), it yielded a much larger sample size than the other
 287 properties, this indicates that the determination of the sampling sufficiency by the applied
 288 resampling method is more related to data normality than that of CoV values. Finally,

289 hardness achieved sampling sufficiency in a 9 sample size, a higher size than those
290 adopted by Salca and Hizirolu (2014), who used 5 specimens per group in their study.

291 Small samples are usually related to methodologies involving the utilization of
292 wood associated with expensive chemicals or laborious treatments, thus is understandable
293 that the utilization of larger samples sizes is sometimes unfeasible (Ghorbani-
Kookandeh 294 *et al.* 2014, Mohebbi *et al.* 2014). However, the variation in the results
could be related 295 to the inherent variation of the wood instead of the studied
treatment is extremely 296 important.

297 CONCLUSIONS

298 The scope of the present study provides for a preliminary elucidation on the
299 sampling sufficiency for some mechanical tests according to the ASTM D143, three
300 points static bending, compression parallel to the fibres, hardness, and shear. Thus,
301 *Eucalyptus* clones were studied regarding those properties and all obtained data
302 conformed to the normal distribution, which enabled the implementation of Monte Carlo
303 simulations. The analysis of the mechanical properties data showed that the wood
304 stiffness presents a smaller variability than its strength, which indicates that the elastic
305 region of the load vs. deformation curve can be studied with fewer samples than the
306 modulus of rupture. Finally, the sampling sufficiency achieved in this research is above
307 those sample sizes used in many recent studies, which indicates that a greater scientific
308 effort should be focused on further conclusive studies for other properties of interest,
309 which are also foreseen in ASTM D143, such as tensile perpendicular and parallel to the
310 fibres and other properties. Finally, the sample sufficiency should also be determined for
311 different species of wood, as the statistical variability strongly depends on this factor.

312

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