

 SpringerWienNewYork

# CISM COURSES AND LECTURES

Series Editors:

The Rectors

Giulio Maier - Milan

Jean Salençon - Palaiseau

Wilhelm Schneider - Wien

The Secretary General

Bernhard Schrefler - Padua

Executive Editor

Paolo Serafini - Udine

The series presents lecture notes, monographs, edited works and proceedings in the field of Mechanics, Engineering, Computer Science and Applied Mathematics.

Purpose of the series is to make known in the international scientific and technical community results obtained in some of the activities organized by CISM, the International Centre for Mechanical Sciences.

INTERNATIONAL CENTRE FOR MECHANICAL SCIENCES

COURSES AND LECTURES - No. 510



ANALYSIS AND CONTROL OF MIXING  
WITH AN APPLICATION TO  
MICRO AND MACRO FLOW PROCESSES

EDITED BY

LUCA CORTELEZZI  
MCGILL UNIVERSITY, MONTREAL, CANADA

IGOR MEZIĆ  
UNIVERSITY OF CALIFORNIA, SANTA BARBARA

SpringerWienNewYork

This volume contains 176 illustrations

This work is subject to copyright.  
All rights are reserved,  
whether the whole or part of the material is concerned  
specifically those of translation, reprinting, re-use of illustrations,  
broadcasting, reproduction by photocopying machine  
or similar means, and storage in data banks.

© 2009 by CISM, Udine

Printed in Italy  
SPIN 12688142

All contributions have been typeset by the authors.

ISBN 978-3-211-99345-3 SpringerWienNewYork

## PREFACE

*The present monograph takes inspiration from the Advanced School on “Analysis and Control of Mixing with Application to Micro and Macro Flow Processes” held in Udine, Italy, (June 1-5, 2005) at the International Center for Mechanical Sciences (CISM). The Advanced School was made possible by the financial and logistic support of CISM and by the financial support of the Marie Curie Program of the European Atelier for Engineering and Computational Sciences (EUA4X). The Advanced School was complemented by a workshop. The workshop provided a fertile environment for discussions where participants in the Advance School, as well as academic and industry experts from fluids, combustion and control disciplines, presented their most recent results. The Advanced School and the workshop attracted a wide range of scientists and practitioners: postgraduates, postdoctoral researchers, mechanical, chemical and aeronautical engineers, and applied mathematicians in universities and industries.*

*The study of mixing two or more fluids with or without chemical reactions is of great practical relevance to both engineering applications and natural phenomena. The analysis and control of mixing at macro and micro scales is receiving great attention because of the potential for optimizing the performance of many flow processes. In modern and futuristic industrial applications, the time allowed to find the appropriate mixing action is becoming increasingly shorter while the demands are increasingly more severe. A better understanding of mixing is crucial for improving old and designing new mixing devices that are able to reduce the residence mixing time, improve mixing homogeneity and allow the process of new materials highly sensitive to the presence of concentration and temperature gradients. In spite of much advancement, the understanding of mixing is still somewhat limited in three-dimensional flows. In particular optimization and feedback control of mixing are still in their infancy. Consequently, mixing continues to represent a rich and appealing research field for both the fundamental and the application oriented scientists.*

*The Advanced School provided an overview of the physics, mathematics and state-of-the-art theoretical/numerical modeling and experimental investigations of mixing in laminar and turbulent flows at macro and micro scales. This monograph follows the footsteps of*

*the Advanced School and contains the following contributions: Anthony Leonard presents an “Overview of Turbulent and Laminar Diffusion and Mixing”, Igor Mezić discusses “Mixing and Dynamical Systems”, Stefano Cerbelli presents the “Hyperbolic Behavior of Laminar Chaotic Flows”, Massimiliano Giona discusses “Advection-diffusion in Chaotic Flows”, Emmanuel Villermaux elaborates on “Random Mixing”, Fotis Sotiropoulos presents an “Experimental Visualization of Lagrangian Coherent Structures Using Eulerian Averaging”, Tatyana Krasnopolskaya discusses “Quality Measures and Transport Properties” of mixing, Tamás Tel discusses some aspects of “Reactions in Chaotic Flows”, Mark A. Stremler elaborates on “Fluid Mixing, Chaotic Advection, and Microarray Analysis”, Jean-Luc Thiffeault presents “The Size of Ghost Rods”, Bartosz Protas discusses the utility of “Nonlinear Preconditioning in Problems of Optimal Control for Fluid Systems” and, finally, Luca Cortelezzi elaborates on the “Sensitivity of Mixing Optimization to the Geometry of the Initial Scalar Field”.*

*We would like to thank all the contributors for their scholarly dedication in making this volume a reality. We would also like to thank all members of CISM for their help in making the Advanced School and this monograph a success. In particular, we would like to thank the Secretary General, Prof. Bernhard A. Schrefler, for encouraging and supporting our Advanced School, Dr. Sara Guttilla, for her dedicated help in all stages of our Advanced School and, finally, the Executive Editor Prof. Paolo Serafini for his precious assistance during the editing of this monograph.*

*Luca Cortelezzi and Igor Mezić*

## CONTENTS

Overview of Turbulent and Laminar Diffusion and Mixing <i>by A. Leonard</i> .....	1
Lectures on Mixing and Dynamical Systems <i>by I. Mezić</i> .....	35
On the Hyperbolic Behavior of Laminar Chaotic Flows <i>by S. Cerbelli</i> .....	109
Advection-diffusion in Chaotic Fows <i>by M. Giona</i> .....	149
On Random Mixing <i>by J. Duplat, C. Innocenti and E. Villermaux</i> .....	219
Experimental Visualization of Lagrangian Coherent Structures Using Eulerian Averaging <i>by F. Sotiropoulos</i> .....	275
Quality Measures and Transport Properties <i>by T. Krasnopolskaya and V. Meleshko</i> .....	291
Reactions in Chaotic Flows <i>by T. Tél and G. Károlyi</i> .....	307
Fluid Mixing, Chaotic Advection, and Microarray Analysis <i>by M. A. Stremler</i> .....	323
The Size of Ghost Rods <i>by J-L. Thiffeault, E. Gouillart and M.D. Finn</i> .....	339
Nonlinear Preconditioning in Problems of Optimal Control for Fluid Systems <i>by B. Protas</i> .....	351
Sensitivity of Mixing Optimization to the Geometry of the Initial Scalar Field <i>by O. Gubanov and L. Cortelezzi</i> .....	369



**Photo Participants**