Strain-Induced Enhancement of the Electron Energy Relaxation in Strongly Correlated Superconductors

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(Received 25 December 2012; published 28 March 2014)

We use femtosecond optical spectroscopy to systematically measure the primary energy relaxation rate Γ_1 of photoexcited carriers in cuprate and pnictide superconductors. We find that Γ_1 increases monotonically with increased negative strain in the crystallographic *a* axis. Generally, the Bardeen-Shockley deformation potential theorem and, specifically, pressure-induced Raman shifts reported in the literature suggest that increased negative strain enhances electron-phonon coupling, which implies that the observed direct correspondence between *a* and Γ_1 is consistent with the canonical assignment of Γ_1 to the electron-phonon interaction. The well-known nonmonotonic dependence of the superconducting critical temperature T_c on the *a*-axis strain is also reflected in a systematic dependence T_c on Γ_1 , with a distinct maximum at intermediate values (~16 ps⁻¹ at room temperature). The empirical nonmonotonic systematic variation of T_c with the strength of the electron-phonon interaction provides us with unique insight into the role of electron-phonon interaction in relation to the mechanism of high- T_c superconductivity as a crossover phenomenon.

DOI: 10.1103/PhysRevX.4.011056

Subject Areas: Condensed Matter Physics, Superconductivity

The deformation potential theorem [1] has been very successful in rationalizing and quantifying the strength of the electron-phonon interaction (EPI) in relation to charge carrier scattering and mobility in semiconductors [2,3], thus rapidly leading to an understanding of charge carrier dynamics and opening the way to modern semiconductor technology. Subsequently, it has been shown that the formalism is not limited to semiconductors, but can be extrapolated to both metals and insulators [4]. Strain on the structure caused by external pressure or doping may result in significant changes of the EPI, leading to changes in

functional properties over and above those caused by the changes of density of doped charges.

In both the cuprate and pnictide families of superconductors, the interatomic distance has been discussed as a quantitative parameter [5-7] in addition to the doping level x that is systematically correlated with the superconducting critical temperature T_c . Although this was pointed out in cuprates long ago and is obviously of primary relevance to the superconducting mechanism, there is not even an elementary understanding of the origin of the peculiar nonmonotonic variation of T_c on the lattice constant that is ubiquitously observed. Here, we present systematic measurements of electron energy relaxation in the normal state of different high- T_c superconductors to show that in both cuprate and pnictide superconductors the primary electron energy relaxation rate Γ_1 is directly correlated with the length *a* of the crystallographic *a* axis, which in turn depends on the structure, the type of dopant atoms, and the doping level x. The dependence of the

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deformation potential on the lattice constant rationalizes how the EPI strength increases with increasing negative strain in the *a* axis. Using established models that relate Γ_1 to the EPI, we make the connection between the EPI and T_c for the first time. From the observed characteristic variation of T_c on the EPI, we can reach important conclusions regarding the relevance of EPI to the superconducting mechanism in the context of strong correlations.

Following the proposal [8] and demonstration [9] of the use of femtosecond optical pump-probe spectroscopy to investigate the EPI in classical superconductors, we use an ultrashort laser pulse (the pump) to create a nonequilibrium electron distribution. The electron energy relaxation is probed by a second, weaker probe pulse, which detects the transient change in the reflectivity $\Delta R/R$. This method has been shown to yield a more reliable measure of the EPI strength [9–14] than the measurement of phonon linewidths by Raman or neutron scattering, which are often compromised by inhomogeneous broadening and probe only a limited selection of phonons.

Although the technique is experimentally well established, some precautions need to be taken to obtain quantitatively accurate data on Γ_1 . In order to disentangle the various relaxation pathways in high- T_c superconductors and determine their time constants $\tau_i = 1/\Gamma_i$, we use several different probe wavelengths. Since the τ_i depend on the sample temperature [see Eq. (1)], and additional processes appear in the presence of low-temperature order [15], we measure all samples at the same temperature— 300 K-well above the temperature where any lowtemperature ordering might take place. We avoid nonlinear, intensity-dependent relaxation processes and sample heating or degradation by keeping the pump pulse fluence below 20 μ J cm⁻². Most importantly, to provide the necessary time resolution and sensitivity, we built a system that gives tunable pump and probe wavelengths ranging from 500 to 700 nm with sub-30-fs overall time resolution. Sub-25-fs pump pulses with a repetition rate of 250 kHz are provided by a noncollinear optical parametric amplifier tuned to a center wavelength of 535 nm (see the Supplemental Material [16] for a detailed description). Probe pulses are provided by a white light continuum generated in 2.5-mm-thick sapphire. Adequate time resolution is ensured via spectral filtering of the chirped probe pulses [17,18]. In several of the samples investigated here, this allowed the identification of previously unresolved relaxation processes.

The sample growth and doping is described elsewhere [19–24]. Samples are glued to a copper support using GE varnish. When needed, samples are cleaved to obtain a reflecting surface with low scattering. The reflectivity and the relative spectral weight of the signal components may vary across the surface, but the relaxation times do not. To eliminate the influence of the sample thickness, we used only samples much thicker than 100 μ m, while our

experiment probes a surface layer typically ~100 nm, depending on the material. The superconducting critical temperature T_c (see Table I) was determined by measuring the temperature dependence of the ac magnetic susceptibility using a superconducting quantum interference device magnetometer.

A representative data set on the transient reflectivity of the selected compounds at room temperature is shown in Fig. 1. (The complete data are reported in the Supplemental Material [16].) To extract the relaxation times, we fit the data using single- or double-exponential decays and a Gaussian function for the instrumental response. (See the Supplemental Material [16] on the time resolution of the used setup and its implications for the accuracy of short τ_1 values.) Oscillatory components are modeled using the same generation term as the main signal, leaving amplitude, frequency, phase, and damping time as the fit parameters. We measure all samples over a range of different wavelengths and in both orthogonal polarizations. Although we let all fit parameters vary freely between different wavelengths, for each sample, the best fits yield the same relaxation times within 10%-20%. From this observation, we conclude that at different wavelengths we are measuring the same relaxation processes but with different spectral weights.

From the fits, we find that the primary (fastest) relaxation rate Γ_1 ranges from 3 to 25 ps⁻¹ (i.e., relaxation time τ_1 between 40 and 330 fs, Table I), independent of probe wavelength and sample orientation with respect to the probe polarization. For the cuprates, we also identify a slower relaxation component τ_2 . Some of the transient reflectivity signals show strong coherent phonon

TABLE I. Stoichiometries, superconducting critical temperatures, and electron-phonon relaxation times and rates of the investigated samples. For each compound family, we calculated error margins (standard deviation over the obtained fit parameters) for the sample with the highest number of measured time traces.

| Sample | $T_{c}(K)$ | $\tau_{e\text{-ph}}$ (fs) | $1/\tau_{e\text{-}\mathrm{ph}}~(\mathrm{ps}^{-1})$ |
|---|------------|---------------------------|--|
| BaFe ₂ As ₂ | 0 | 300 | 3.3 |
| $Ba(Fe_{0.975}Co_{0.025})_2As_2$ | 0 | 330 | 3.0 |
| $Ba(Fe_{0.949}Co_{0.051})_2As_2$ | 20 | 320 | 3.1 |
| $Ba(Fe_{0.93}Co_{0.07})_2As_2$ | 23 | 300 | 3.3 |
| $Ba(Fe_{0.89}Co_{0.11})_2As_2$ | 10 | 300 | 3.3 |
| SmFeAsO _{0.8} F _{0.2} | 49 | 190 | 5.3 |
| YBa ₂ Cu ₃ O ₆₅ | 63 | 72 | 14 |
| YBa ₂ Cu ₃ O _{6.9} | 90 | 77 | 13 |
| HgBa ₂ CuO _{4.1} | 98 | 62 | 16 |
| Bi ₂ Sr ₂ CaCu ₂ O _{8.14} | 80 | 49 | 20 |
| $La_{1.9}Sr_{0.1}CuO_4$ | 30 | 42 | 24 |
| La _{1.85} Sr _{0.15} CuO ₄ | 38 | 45 | 22 |
| | | | |

oscillations [25], which are subtracted in the analysis. The τ_1 values for YBa₂Cu₃O_{6+x}, Bi₂Sr₂CaCu₂O_{8.14}, and the pnictides agree well with room-temperature data from the literature [10–13], while for HgBaCa₂CuO_{4.1}, they are resolved for the first time. For La_{2-x}Sr_xCuO₄, our recent results obtained with much higher pump intensity [14] are confirmed by the present low-intensity data.

In Fig. 2, we plot the primary relaxation rate Γ_1 as a function of the crystallographic *a* axis of pnictides and cuprates. All data points for cuprates, including differently doped samples, fit to a straight line, where Γ_1 decreases with increasing *a*. Defining the *a*-axis strain $\varepsilon_a = \Delta a/a_0$, with the equilibrium value [6] $a_0 = 3.94$ Å, this means that higher negative strain in the Cu-O planes leads to faster



FIG. 1. Transient differential reflection at 295 K for different (near) optimally doped superconducting compounds. Thin solid lines are fits. Please refer to the Supplemental Material ([16], Figs. S8–S19) for different doping levels and sample orientations.

electron energy relaxation. For a given cuprate, *a* is not determined only by the type of compound, but also varies significantly with doping, by 0.1 Å over the whole superconducting range of the phase diagram [5]. This translates into a doping-dependent relaxation rate, as our data for YBa₂Cu₃O_{6+x} and La_{2-x}Sr_xCuO₄ at different doping levels confirm, and is in agreement with previous data [11] on Bi₂Sr₂CaCu₂O_{8+x}. On the other hand [26], *a* in the pnictide Ba(Fe_{1-x}Co_x)₂Se₂ is nearly doping independent, changing by less than 0.002 Å. Remarkably, for all measured Ba(Fe_{1-x}Co_x)₂Se₂ samples, which cover a wide range of doping levels, the measured Γ_1 values show almost no variation. Hence, Γ_1 depends on *a*, but not on the doped carrier density.

Given the consensus in the literature in attributing the ultrafast response Γ_1 to the electron energy relaxation [10–14,27–29], we proceed to discuss the relaxation mechanism. The electron-phonon relaxation rate $1/\tau_{e-\text{ph}}$ can be related to the EPI strength expressed as the second moment $\lambda \langle \omega^2 \rangle$ of the Eliashberg spectral function [8,30]:

$$\frac{1}{\tau_{e-\rm ph}} = B \frac{\lambda \langle \omega^2 \rangle}{T},\tag{1}$$

where T is the temperature and B is a constant. Depending on whether one assumes the electron-electron relaxation to be much faster than the electron-phonon relaxation [8] or not [30], T is either the electronic temperature T_e or the lattice temperature T_L , respectively. In the present experiments, we use a very low laser excitation fluence, in which case $T_e \sim T_L$. The models above assume coupling between two baths: the hot electrons and the phonons whose coupling is characterized by the Eliashberg spectral function. One may also include more specific bosonic excitations in such models to emphasize a particular interaction [11,27–29]. However, this does not have significant bearing in the current discussion, since we are discussing only the dominant relaxation rate. The electron energy relaxes towards the bath that has the largest heat capacity; the lattice is the obvious candidate [31]. Recent microscopic calculations within the driven *t*-*J*-Holstein model suggest that, under certain conditions, rapid energy transfer to spin degrees of freedom can occur [32], but considering the relaxation dynamics, only the relaxation of a highly excited charge carrier through Holstein phonons has been investigated thus far [33]. A detailed discussion of the assignment of Γ_1 to the EPI and the choice of the proportionality constant *B* is given in the Supplemental Material [16].

The EPI strength is often described by a dimensionless parameter λ (the zero-order moment of the Eliashberg spectral function) rather than $\lambda \langle \omega^2 \rangle$. To calculate λ from $\lambda \langle \omega^2 \rangle$, one would need to know the complete *q*-and ω dependent Eliashberg spectral function. As a crude approximation, $\lambda \langle \omega^2 \rangle$ is often simply divided by the square of an effective phonon frequency ω^* . Commonly used values are 40 meV for cuprates [21,29] and 25 meV for pnictides [28]. Using these values, we estimate $\lambda \sim 0.3-0.5$ for cuprates and $\lambda \sim 0.2-0.3$ for pnictides. This estimate agrees well with λ obtained from angle-resolved photoemission [34,35], neutron scattering [36–38], and tunneling [39] spectroscopy.

Generally, the effective electron-phonon coupling λ is proportional to the square of the energy E_1 , defined via the deformation potential [1,40] $\delta U = E_1 \Delta$, which gives the energy shift of the conduction band edge as a function of the strain Δ . For a small variation of *a* (for the cuprates $\Delta a/a \sim 3\%$), we may expand around the equilibrium value a_0 to first order:

$$\lambda * (a) \approx \gamma [E_1(a_0) + \frac{\partial E_1}{\partial a} (a - a_0)]^2$$
$$\approx \lambda * (a_0) + \tilde{\gamma} \frac{\partial E_1}{\partial a} (a - a_0). \tag{2}$$

The linear relation between λ and a above justifies the fit of $\Gamma_1(a)$ in Fig. 2. Using a simple estimate for $E_1 \approx \hbar^2/3ma^2$, where *m* is the electron mass, $\partial E_1/\partial a$ is negative, in agreement with the negative slope of the experimentally obtained $\Gamma_1(a)$.

In addition to the increase of λ with decreasing *a*, the phonon frequencies observed by Raman spectroscopy also increase [41,42]. Both effects lead to an increase of the relaxation rate (see next paragraph). The observed blue-shifts of the phonon bands by a few percent per picometer of contraction of *a* are consistent in both sign and magnitude with the observed increase of Γ_1 .

In both cuprates and pnictides, it has been proposed that T_c is determined by two parameters: the doping level x and the length a of the crystallographic a axis [5–7], or,



FIG. 2. Primary electron energy relaxation rate Γ of pnictides and cuprates as a function of the *a*-axis length. Large symbols are at or close to optimal doping, open symbols at other doping levels. Dashed lines are linear fits. The inset is a zoom into the region of the five different Ba(Fe_{0.975}Co_{0.025})₂As₂ samples, which have very similar a and Γ values.

equivalently, some related structural parameter, such as the Cu-O in-plane bond length or the anion height in the pnictides. In the cuprates, superconductivity occurs when structure, doping-induced strain, or pressure-induced strain compresses *a* well below its equilibrium value [5,6] (in a cubic lattice) of a = 3.94 Å, with a maximum T_c at a = 3.84 Å [Fig. 3(a)]. The direct correspondence between *a* and Γ_1 shown in Fig. 2 suggests that, equivalently to a, Γ_1 can be used as a second parameter that determines T_c [see Fig. 3(b)]. $T_c(R)$ systematically follows an arc with a distinct maximum around $K \sim 16$ ps⁻¹. For the cuprates, *a* and consequently Γ_1 depend on the doping levels, while for



FIG. 3. (a) Critical temperature for cuprates as a function of the *a* axis [2 times the in-plane Cu-O distance as published in Ref. [5] (refer to the caption of Fig. 6 of Ref. [5] for the numbering of the compounds)]. Full symbols are our samples at or close to optimal doping (same symbol and color coding as Fig. 2), open circles are from Ref. [5], line is a fit to a Lorentzian as a guide to the eye. (b) The superconducting transition temperature T_c as a function of the primary relaxation rate Γ_1 . To plot the top axis, we used Eq. (1) with [30] $B = 3h/2\pi k_B$. Full symbols indicate (almost) optimally doped samples, open symbols other doping levels.

Ba(Fe_{1-x}Co_x)₂Se₂ the two parameters are practically independent. The femtosecond pump-probe experiment, thus, directly yields a parameter— Γ_1 —that is uniquely related to T_c .

Allen's proposition [8] that Γ_1 be proportional to the EPI and the Bardeen-Shockley deformation potential theorem [1] that relates the EPI to strain on the *a* axis together suggest a correspondence between a and the EPI, which we verified experimentally. Relating T_c to the EPI rather than to a can give us better insight into the applicability of different mechanisms of superconductivity. BCS theory, and by extension Eliashberg theory, predicts a monotonically increasing T_c with increasing λ , which is contrary to the systematics we observe. On the other hand, in bare strongly correlated electron models, such as the Hubbard model and the t-J model, the tunneling t decreases with increasing distance, but the dependence of T_c on t is not clear. Until now, the dependence of other interactions, such as spin fluctuations, on the *a* parameter has not been studied, but it is possible that these may have an-as yet undetermined—effect on T_c .

The observed nonmonotonic behavior strongly suggests a crossover phenomenon. Thus, competing interactions need to be considered, such as the crossover from weak coupling (BCS-like) to strong coupling [43] as a function of λ . An alternative approach includes strong correlations via the Coulomb interaction into an EPI model within the strong coupling approach [44]. In other words, the crossover behavior also highlights the necessity of the interplay of competing ground states [20] for achieving high T_c 's. In any case, the EPI is clearly involved in a very unconventional way [45]. Indeed, the systematic, large, yet strongly unconventional isotope effect departing strongly from BCS behavior observed across the compounds corroborates this notion [46,47]. Although the present data and analysis presented in Fig. 3 do not identify the mechanism, they emphasize a role for unconventional electron-lattice effects and give a stringent verification criterion for any hopeful high- T_c superconductivity theory [48,49].

We thank D. Brida, F. Cilento, I. R. Fisher, P. Kusar, D. Polli, and L. Vidmar for stimulating discussions. This work was supported by the Slovenian Research Agency (ARRS) (Grants No. 430-66/2007-17, No. BI-CN/07-09-003, and No. BI-IT/11-13-001), ROBOCON 2011-2012, the Royal Society (Grant No. JP090316), and the European Commission [Grant No. ERG-230975 and the European Community Access to Research Infrastructure Action, Contract No. RII3-CT-2003-506350 (Centre for Ultrafast Science and Biomedical Optics, LASERLAB-EUROPE)].

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