# Observation of Overlapping Spin-1 and Spin-3 $\bar{D}^{0} K^{-}$Resonances at Mass 2.86 GeV/ $\boldsymbol{c}^{\mathbf{2}}$ 

R. Aaij et al.*<br>(LHCb Collaboration)<br>(Received 30 July 2014; published 14 October 2014)


#### Abstract

The resonant substructure of $B_{s}^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$decays is studied using a data sample corresponding to an integrated luminosity of $3.0 \mathrm{fb}^{-1}$ of $p p$ collision data recorded by the LHCb detector. An excess at $m\left(\bar{D}^{0} K^{-}\right) \approx 2.86 \mathrm{GeV} / c^{2}$ is found to be an admixture of spin-1 and spin-3 resonances. Therefore, the $D_{s, J}^{*}(2860)^{-}$state previously observed in inclusive $e^{+} e^{-} \rightarrow \bar{D}^{0} K^{-} X$ and $p p \rightarrow \bar{D}^{0} K^{-} X$ processes consists of at least two particles. This is the first observation of a heavy flavored spin-3 resonance, and the first time that any spin- 3 particle has been seen to be produced in $B$ decays. The masses and widths of the new states and of the $D_{s 2}^{*}(2573)^{-}$meson are measured, giving the most precise determinations to date.


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Studies of heavy meson spectroscopy provide an important probe of quantum chromodynamics. The observations of the $D_{s 0}^{*}(2317)^{-}$[1] and $D_{s 1}(2460)^{-}$[2] mesons led to renewed activity in the field, as their masses were found to be below the $D K$ and $D^{*} K$ thresholds, respectively, in contrast to prior predictions. These states are usually interpreted as being two of the orbitally excited ( $1 P$ ) charm-strange states, the other two being the $D_{s 1}(2536)^{-}$and $D_{s 2}^{*}(2573)^{-}$resonances. Several other charm-strange states, the $D_{s 1}^{*}(2700)^{-}$, $D_{s J}^{*}(2860)^{-}$, and $D_{s J}(3040)^{-}$resonances, have been discovered [3-6]. However, their quantum numbers and spectroscopic assignments are not known, with the exception of the $D_{s 1}^{*}(2700)^{-}$meson, which has spin-parity $J^{P}=1^{-}$ and is generally believed to be a radially excited $(2 S)$ state. Reviews of the expectations in theoretical models can be found in Refs. [7-10].

A state with $J^{P}=3^{-}$would be a clear candidate for a member of the $1 D$ family, i.e., a state with two units of orbital excitation. Spin-3 states have been observed in the light unflavored [11,12] and strange [13,14] meson sectors, but not previously among heavy flavored mesons. Production of high-spin states is expected to be suppressed in $B$ meson decays, and has not previously been observed [15]. However, high-spin resonances are expected to be relatively narrow, potentially enhancing their observability.

Analysis of the Dalitz plot [16] that describes the phase space of a three-body decay is a powerful tool for spectroscopic studies. Compared to measurements based on inclusive production processes, the lower background level allows broader states to be distinguished, and the well-defined initial state allows the quantum numbers to be unambiguously determined. Specifically, in

[^0]$B_{s}^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$decays, $K^{-} \pi^{+}$and $\bar{D}^{0} K^{-}$resonances appear as horizontal and vertical bands in the Dalitz plot formed from the invariant masses squared $m^{2}\left(K^{-} \pi^{+}\right)$vs $m^{2}\left(\bar{D}^{0} K^{-}\right)$, and the spin of the resonance can be inferred from the distribution of decays along the band. Measurement of the spin also determines the parity, since only natural spin-parity resonances can decay strongly to two pseudoscalars.

In this Letter, results of the first Dalitz plot analysis of the $B_{s}^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$decay are summarized. The inclusion of charge conjugated processes is implied throughout the Letter. The $\bar{D}^{0}$ meson is reconstructed through the $K^{+} \pi^{-}$ decay mode, which is treated as flavor specific; i.e., the heavily suppressed $B_{s}^{0} \rightarrow D^{0} K^{-} \pi^{+}, D^{0} \rightarrow K^{+} \pi^{-}$contribution is neglected. The amplitude analysis technique is used to separate contributions from excited charm-strange mesons and from excited kaon states. A detailed description of the analysis can be found in Ref. [17].

The analysis is based on a data sample corresponding to $3.0 \mathrm{fb}^{-1}$ of integrated luminosity, approximately one third (two thirds) of which was collected by the LHCb detector from $p p$ collisions at a center-of-mass energy of 7 (8) TeV during 2011 (2012). The LHCb detector is a single-arm forward spectrometer covering the pseudorapidity range $2<\eta<5$, designed for the study of particles containing $b$ or $c$ quarks, and is described in detail in Ref. [18]. Signal candidates are accepted offline if one of the final state particles deposited sufficient energy transverse to the beam line in the hadronic calorimeter to fire the hardware trigger. Events that are triggered at the hardware level by another particle in the event are also retained. The software trigger [19] requires a two-, three-, or four-track secondary vertex with a large sum of the transverse momentum, $p_{\mathrm{T}}$, of the tracks and a significant displacement from all primary $p p$ interaction vertices.

The off-line selection requirements are similar to those used in Refs. [20,21] and are optimized using the $B^{0} \rightarrow$ $\bar{D}^{0} \pi^{+} \pi^{-}$decay as a control channel. Discrimination
between signal and background categories is achieved primarily with a neural network [22] trained on $B^{0} \rightarrow$ $\bar{D}^{0} \pi^{+} \pi^{-}$data, where signal and background are statistically separated with the sPlot technique [23] using the $B$ candidate mass as discriminating variable. A total of 16 variables are used in the network. They include the output of a " $D^{0}$ boosted decision tree" [24,25] that identifies $\bar{D}^{0}$ mesons produced in $b$ hadron decays, together with other variables that characterize the topology and the kinematic distributions of the $B$ decay. A requirement on the network output is imposed that reduces the combinatorial background remaining after the initial selection by a factor of 5 while retaining more than $90 \%$ of the signal. The four final state tracks also have to satisfy pion and kaon identification requirements.

To improve the mass resolution, track momenta are scaled $[26,27]$ with calibration parameters determined by matching the observed position of the dimuon mass peak to the known $J / \psi$ mass [28]. In addition, the momenta of the tracks from the $\bar{D}^{0}$ candidate are adjusted [29] so that their combined invariant mass matches the known $\bar{D}^{0}$ mass [28]. An additional $B_{s}^{0}$ mass constraint is applied in the calculation of the Dalitz plot variables.

Invariant-mass vetoes are applied to remove backgrounds containing $D^{* \pm}$ mesons, and from the $B_{s}^{0} \rightarrow D_{s}^{-} \pi^{+}$and $B_{s}^{0} \rightarrow D^{0} \bar{D}^{0}$ decays. Decays of $B_{s}^{0}$ mesons to the same final state but without an intermediate charm meson are suppressed by the $D^{0}$ boosted decision tree criteria and an additional requirement that the $\bar{D}^{0}$ candidate vertex is displaced by at least 1 mm from the $B_{s}^{0}$ decay vertex.

The signal and background yields are obtained from an extended unbinned maximum likelihood fit to the threebody invariant mass distribution of $B_{s}^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$candidates in the range $5200-5900 \mathrm{MeV} / \mathrm{c}^{2}$. In addition to signal decays and combinatorial background, the fit model includes components to describe partially reconstructed $B_{s}^{0} \rightarrow \bar{D}^{* 0} K^{-} \pi^{+}$decays, with $\bar{D}^{* 0} \rightarrow \bar{D}^{0} \pi^{0}$ or $\bar{D}^{0} \gamma$ and the $\pi^{0}$ or $\gamma$ not included in the reconstruction, $B^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$ decays, and $B^{0} \rightarrow \bar{D}^{(*) 0} \pi^{+} \pi^{-}$and $\bar{\Lambda}_{b}^{0} \rightarrow \bar{D}^{(*) 0} \bar{p} \pi^{+} \quad[30]$ decays with misidentification of a final state particle. Contributions from other $B_{s}^{0}$ and $B^{0}$ decays are negligible.

The signal and $B^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$shapes are each modeled with the sum of two Crystal Ball [31] functions which share a common mean and have tails on opposite sides. The combinatorial background is modeled using a linear function. Smoothed histograms are used to describe the shapes of $B_{s}^{0} \rightarrow \bar{D}^{* 0} K^{-} \pi^{+}, B^{0} \rightarrow \bar{D}^{(*) 0} \pi^{+} \pi^{-}$, and $\bar{\Lambda}_{b}^{0} \rightarrow \bar{D}^{(*) 0} \bar{p} \pi^{+}$ decays. These shapes are determined from simulated events reweighted to account for the known Dalitz plot distributions of the background decays $[21,30]$ and particle identification and misidentification probabilities.

The results of the fit are shown in Fig. 1. Within a signal region of $\mu_{B_{s}^{0}} \pm 2.5 \sigma_{1}$, where the peak position $\mu_{B_{s}^{0}}$ and core width $\sigma_{1}=12.7 \pm 0.2 \mathrm{MeV} / c^{2}$ are taken from the results of the fit, there are 12954 candidates. Of these,


FIG. 1 (color online). Fit to the $B_{s}^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$candidate invariant mass distribution. Data points are shown in black, the result of the fit as a solid blue line, and the components as detailed in the legend.
$11300 \pm 160$ are signal decays, while $950 \pm 60$ are combinatorial background, $360 \pm 130$ are $B^{0} \rightarrow \bar{D}^{(*) 0} \pi^{+} \pi^{-}$ decays, and $300 \pm 80$ are $\bar{\Lambda}_{b}^{0} \rightarrow \bar{D}^{(*) 0} \bar{p} \pi^{+}$decays.

The Dalitz plot distribution of the candidates in the signal region, shown in Fig. 2, is fitted with a model that includes both signal and background components. The Dalitz plot distribution of combinatorial background is obtained from a sideband region above the signal peak in the $B_{s}^{0}$ candidate mass, while those for $B^{0} \rightarrow \bar{D}^{(*) 0} \pi^{+} \pi^{-}$ and $\bar{\Lambda}_{b}^{0} \rightarrow \bar{D}^{(*) 0} \bar{p} \pi^{+}$backgrounds are obtained from simulation reweighted in the same way as their $B_{s}^{0}$ candidate mass shapes.

The signal model is defined by considering many possible contributions and removing those that do not significantly affect the fit. It contains 15 resonant or nonresonant amplitudes added coherently in the isobar [32-34] model formalism. These include the $\bar{K}^{*}(892)^{0}$, $\bar{K}^{*}(1410)^{0}, \bar{K}_{2}^{*}(1430)^{0}$, and $\bar{K}^{*}(1680)^{0}$ resonances. The $K^{-} \pi^{+} \mathrm{S}$ wave is modeled using the LASS shape [35], which combines the $\bar{K}_{0}^{*}(1430)^{0}$ resonance with a slowly varying (nonresonant) component, in addition to the


FIG. 2. Dalitz plot distribution of $B_{s}^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$candidates in the signal region. The effect of the $D^{0}$ veto can be seen as an unpopulated horizontal band.
$\bar{K}_{0}^{*}(1950)^{0}$ state. The $D_{s 2}^{*}(2573)^{-}$and $D_{s 1}^{*}(2700)^{-}$states are included, in addition to both spin-1 and spin-3 resonances near $m\left(\bar{D}^{0} K^{-}\right) \approx 2860 \mathrm{MeV} / c^{2}$ labeled $D_{s 1}^{*}(2860)^{-}$ and $D_{s 3}^{*}(2860)^{-}$, respectively. A nonresonant $S$-wave $\bar{D}^{0} K^{-}$component is included, modeled with an exponential form factor, as are additional amplitudes mediated by "virtual" resonances (i.e., with peak position outside the phase space of the Dalitz plot so that only the tail of the line shape contributes): $D_{s v}^{*-}$ and $D_{s 0 v}^{*}(2317)^{-}$in $m\left(\bar{D}^{0} K^{-}\right)$, and $B_{v}^{*+}$ in $m\left(\bar{D}^{0} \pi^{+}\right)$. All components, except those explicitly noted above, are modeled with relativistic Breit-Wigner functions. The parameters of the line shapes are fixed to their known values [28], except for the masses and widths of the $D_{s 2}^{*}(2573)^{-}, D_{s 1}^{*}(2860)^{-}$, and $D_{s 3}^{*}(2860)^{-}$resonances, the parameters describing the LASS function and the exponential form factor of the nonresonant model, which
are free to vary in the fit. The angular distributions are given in the Zemach tensor formalism $[36,37]$ and each amplitude includes Blatt-Weisskopf barrier form factors [15].

The signal model is multiplied by an efficiency function and normalized to unity when integrated across the Dalitz plot. The efficiency is determined as a function of Dalitz plot position from samples of simulated events with corrections applied for known discrepancies between data and simulation in the efficiencies of the trigger, track reconstruction, and particle identification. The trigger efficiency correction is applied separately for candidates in events triggered at hardware level by the signal decay products and for those triggered independently. The largest source of efficiency variation across the Dalitz plot arises due to a rapid decrease of the probability to reconstruct low momentum particles. The particle identification


FIG. 3 (color online). Projections of the data and the Dalitz plot fit result onto (a) $m\left(K^{-} \pi^{+}\right)$, (b) $m\left(\bar{D}^{0} K^{-}\right.$), and (c) $m\left(\bar{D}^{0} \pi^{+}\right)$, with zooms into $m\left(\bar{D}^{0} K^{-}\right)$around (d) the $D_{s 2}^{*}(2573)^{-}$resonance and (e) the $D_{s J}^{*}(2860)^{-}$region. The data are shown as black points, the total fit result as a solid black curve, and the contributions from different resonances as detailed in the legend (small components, including the background contributions, are not shown).
requirements lead to a maximum efficiency variation of about $\pm 20 \%$, while other effects are smaller.

Projections of the data and the unbinned maximum likelihood fit result are shown in Fig. 3. The largest components in terms of their fit fractions, defined as the ratio of the integrals over the Dalitz plot of a single decay amplitude squared and the total amplitude squared, are the $\bar{K}^{*}(892)^{0}(28.6 \%), D_{s 2}^{*}(2573)^{-}(25.7 \%)$, LASS (21.4\%), and $\bar{D}^{0} K^{-}$nonresonant ( $12.4 \%$ ) terms. The fit fractions for the $D_{s 1}^{*}(2860)^{-}$and $D_{s 3}^{*}(2860)^{-}$components are $(5.0 \pm$ $1.2 \pm 0.7 \pm 3.3) \%$ and $(2.2 \pm 0.1 \pm 0.3 \pm 0.4) \%$, respectively, where the uncertainties are statistical, systematic, and from Dalitz plot model variations, as described below. The phase difference between the $D_{s 1}^{*}(2860)^{-}$ and $D_{s 3}^{*}(2860)^{-}$amplitudes is consistent with $\pi$ within a large model uncertainty.

To assess the significance of the two states near $m\left(\bar{D}^{0} K^{-}\right) \approx 2860 \mathrm{MeV} / c^{2}$, the fit is repeated with all combinations of either one or two resonant amplitudes with different spins up to and including 3. All other combinations give values of negative log-likelihood more than one hundred units larger than the default fit. A comparison of the angular distributions in the region near $m\left(\bar{D}^{0} K^{-}\right) \approx 2860 \mathrm{MeV} / c^{2}$ of the data and the best fits with the spin- 1 only, spin- 3 only, and both resonances is presented in Fig. 4. Including both spin components visibly improves the fit. Large samples of pseudoexperiments are generated with signal models corresponding to the best fits with the spin- 1 or spin- 3 amplitude removed, and each pseudoexperiment is fitted under both the one- and tworesonance hypotheses. By extrapolating the tails of the


FIG. 4 (color online). Projections of the data and Dalitz plot fit results with alternative models onto the cosine of the helicity angle of the $\bar{D}^{0} K^{-}$system, $\cos \theta\left(\bar{D}^{0} K^{-}\right)$, for $2.77<m\left(\bar{D}^{0} K^{-}\right)<$ $2.91 \mathrm{GeV} / c^{2}$, where $\theta\left(\bar{D}^{0} K^{-}\right)$is the angle between the $\pi^{+}$and the $\bar{D}^{0}$ meson momenta in the $\bar{D}^{0} K^{-}$rest frame. The data are shown as black points, with the fit results with different models as detailed in the legend. The dip at $\cos \theta\left(\bar{D}^{0} K^{-}\right) \approx-0.6$ is due to the $\bar{D}^{0}$ veto. Comparisons of the data and the different fit results in the 50 bins of this projection give $\chi^{2}$ values of 47.3, 214.0, and 150.0 for the default, spin- 1 only, and spin- 3 only models, respectively.
distributions of the difference in negative log-likelihood values to the values observed in data, the statistical significances of the spin-3 and spin-1 components are found to be 16 and 15 standard deviations, respectively. These significances remain in excess of 10 standard deviations in all alternative models considered below.

The considered sources of systematic uncertainty are divided into two main categories: experimental uncertainties and model uncertainties. The experimental systematic uncertainties arise from imperfect knowledge of: the relative amount of signal and background in the selected events; the distributions of each of the backgrounds across the phase space; the variation of the efficiency across the phase space; the possible bias induced by the fit procedure; the momentum calibration; the fixed masses of the $B_{s}^{0}$ and $\bar{D}^{0}$ mesons used to define the boundaries of the Dalitz plot. Model uncertainties occur due to: fixed parameters in the Dalitz plot model; the treatment of marginal components in the default fit model; the choice of models for the $K^{-} \pi^{+} \mathrm{S}$ wave, the $\bar{D}^{0} K^{-} \mathrm{S}$ and P waves, and the line shapes of the virtual resonances. The systematic uncertainties from each source are combined in quadrature.

The masses and widths of the $D_{s 2}^{*}(2573)^{-}, D_{s 1}^{*}(2860)^{-}$, and $D_{s 3}^{*}(2860)^{-}$states are determined to be

$$
\begin{aligned}
m\left(D_{s 2}^{*}(2573)^{-}\right) & =2568.39 \pm 0.29 \pm 0.19 \pm 0.18 \mathrm{MeV} / c^{2} \\
\Gamma\left(D_{s 2}^{*}(2573)^{-}\right) & =16.9 \pm 0.5 \pm 0.4 \pm 0.4 \mathrm{MeV} / c^{2} \\
m\left(D_{s 1}^{*}(2860)^{-}\right) & =2859 \pm 12 \pm 6 \pm 23 \mathrm{MeV} / c^{2} \\
\Gamma\left(D_{s 1}^{*}(2860)^{-}\right) & =159 \pm 23 \pm 27 \pm 72 \mathrm{MeV} / c^{2} \\
m\left(D_{s 3}^{*}(2860)^{-}\right) & =2860.5 \pm 2.6 \pm 2.5 \pm 6.0 \mathrm{MeV} / c^{2} \\
\Gamma\left(D_{s 3}^{*}(2860)^{-}\right) & =53 \pm 7 \pm 4 \pm 6 \mathrm{MeV} / c^{2}
\end{aligned}
$$

where the first uncertainty is statistical, the second is due to experimental systematic effects, and the third is due to model variations. The largest sources of uncertainty on the parameters of the $D_{s 1}^{*}(2860)^{-}$and $D_{s 3}^{*}(2860)^{-}$resonances arise from varying the $K^{-} \pi^{+}$S-wave description and, for the $D_{s 1}^{*}(2860)^{-}$width, from removing the $\bar{K}^{*}(1680)^{0}$ and $B_{v}^{*+}$ components from the model. The results for the $D_{s 2}^{*}(2573)^{-}$mass and width are determined with significantly better precision than previous measurements. Those for the parameters of the $D_{s 1}^{*}(2860)^{-}$and $D_{s 3}^{*}(2860)^{-}$ resonances must be considered first measurements, since previous measurements of the properties of the $D_{s J}^{*}(2860)^{-}$ state $[3,5,6]$ involved an unknown admixture of at least these two particles. The results for all the complex amplitudes determined by the Dalitz plot fit, as well as derived quantities such as branching fractions of the resonant contributions and detailed descriptions of the systematic uncertainties, are given in Ref. [17].

In summary, results of the first amplitude analysis of the $B_{s}^{0} \rightarrow \bar{D}^{0} K^{-} \pi^{+}$decay show, with significance of more than 10 standard deviations, that a structure at
$m\left(\bar{D}^{0} K^{-}\right) \approx 2.86 \mathrm{GeV} / c^{2}$ contains both spin-1 and spin-3 components. The masses of the $D_{s 1}^{*}(2860)^{-}$and $D_{s 3}^{*}(2860)^{-}$states are found to be similar, while a larger width of the spin-1 state than that of the spin-3 state is preferred. The results support an interpretation of these states being the $J^{P}=1^{-}$and $3^{-}$members of the $1 D$ family, though the $1^{-}$state may be partially mixed with the vector member of the $2 S$ family to give the physical $D_{s 1}^{*}(2700)^{-}$ and $D_{s 1}^{*}(2860)^{-}$states. The discovery of the $D_{s 3}^{*}(2860)^{-}$ resonance represents the first observation of a heavy flavored spin-3 particle, and the first time that a spin-3 state is seen to be produced in $B$ decays. This demonstrates that the spectroscopy of the $1 D$ families of heavy flavored mesons can be studied experimentally.

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R. Aaij, ${ }^{41}$ B. Adeva, ${ }^{37}$ M. Adinolfi, ${ }^{46}$ A. Affolder, ${ }^{52}$ Z. Ajaltouni, ${ }^{5}$ S. Akar, ${ }^{6}$ J. Albrecht, ${ }^{9}$ F. Alessio, ${ }^{38}$ M. Alexander ${ }^{51}$ S. Ali, ${ }^{41}$ G. Alkhazov, ${ }^{30}$ P. Alvarez Cartelle, ${ }^{37}$ A. A. Alves Jr., ${ }^{25,38}$ S. Amato, ${ }^{2}$ S. Amerio, ${ }^{22}$ Y. Amhis, ${ }^{7}$ L. An, ${ }^{3}$ L. Anderlini, ${ }^{17, a}$ J. Anderson, ${ }^{40}$ R. Andreassen, ${ }^{57}$ M. Andreotti, ${ }^{16, b}$ J. E. Andrews, ${ }^{58}$ R. B. Appleby, ${ }^{54}$
O. Aquines Gutierrez, ${ }^{10}$ F. Archilli, ${ }^{38}$ A. Artamonov, ${ }^{35}$ M. Artuso, ${ }^{59}$ E. Aslanides, ${ }^{6}$ G. Auriemma, ${ }^{25, c}$ M. Baalouch, ${ }^{5}$ S. Bachmann, ${ }^{11}$ J. J. Back, ${ }^{48}$ A. Badalov, ${ }^{36}$ C. Baesso, ${ }^{60}$ W. Baldini, ${ }^{16}$ R. J. Barlow, ${ }^{54}$ C. Barschel, ${ }^{38}$ S. Barsuk, ${ }^{7}$ W. Barter, ${ }^{47}$ V. Batozskaya, ${ }^{28}$ V. Battista, ${ }^{39}$ A. Bay, ${ }^{39}$ L. Beaucourt, ${ }^{4}$ J. Beddow, ${ }^{51}$ F. Bedeschi, ${ }^{23}$ I. Bediaga, ${ }^{1}$ S. Belogurov, ${ }^{31}$ K. Belous, ${ }^{35}$ I. Belyaev, ${ }^{31}$ E. Ben-Haim, ${ }^{8}$ G. Bencivenni, ${ }^{18}$ S. Benson, ${ }^{38}$ J. Benton, ${ }^{46}$ A. Berezhnoy, ${ }^{32}$ R. Bernet, ${ }^{40}$ M.-O. Bettler, ${ }^{47}$ M. van Beuzekom, ${ }^{41}$ A. Bien, ${ }^{11}$ S. Bifani, ${ }^{45}$ T. Bird, ${ }^{54}$ A. Bizzeti,,${ }^{17, d}$ P. M. Bjørnstad, ${ }^{54}$ T. Blake, ${ }^{48}$ F. Blanc, ${ }^{39}$ J. Blouw, ${ }^{10}$ S. 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Charles, ${ }^{8}$ Ph. Charpentier, ${ }^{38}$ M. Chefdeville, ${ }^{4}$ S. Chen, ${ }^{54}$ S.-F. Cheung, ${ }^{55}$ N. Chiapolini, ${ }^{40}$ M. Chrzaszcz, ${ }^{40,26}$ K. Ciba, ${ }^{38}$ X. Cid Vidal, ${ }^{38}$ G. Ciezarek, ${ }^{53}$ P. E. L. Clarke, ${ }^{50}$ M. Clemencic, ${ }^{38}$ H. V. Cliff, ${ }^{47}$ J. Closier,,${ }^{38}$ V. Coco, ${ }^{38}$ J. Cogan, ${ }^{6}$ E. Cogneras, ${ }^{5}$ P. Collins, ${ }^{38}$ A. Comerma-Montells, ${ }^{11}$ A. Contu, ${ }^{15}$ A. Cook, ${ }^{46}$ M. Coombes, ${ }^{46}$ S. Coquereau, ${ }^{8}$ G. Corti, ${ }^{38}$ M. Corvo, ${ }^{16, b}$ I. Counts,,${ }^{56}$ B. Couturier,,${ }^{38}$ G. A. Cowan, ${ }^{50}$ D. C. Craik, ${ }^{48}$ M. Cruz Torres, ${ }^{60}$ S. Cunliffe, ${ }^{53}$ R. Currie, ${ }^{50}$ C. D'Ambrosio, ${ }^{38}$ J. Dalseno, ${ }^{46}$ P. David, ${ }^{8}$ P. N. Y. David, ${ }^{41}$ A. Davis, ${ }^{57}$ K. De Bruyn, ${ }^{41}$ S. De Capua, ${ }^{54}$ M. De Cian, ${ }^{11}$ J. M. De Miranda, ${ }^{1}$ L. De Paula, ${ }^{2}$ W. De Silva, ${ }^{57}$ P. De Simone, ${ }^{18}$ D. Decamp, ${ }^{4}$ M. Deckenhoff, ${ }^{9}$ L. Del Buono, ${ }^{8}$ N. Déléage, ${ }^{4}$ D. Derkach,,${ }^{55}$ O. Deschamps, ${ }^{5}$ F. Dettori, ${ }^{38}$ A. Di Canto, ${ }^{38}$ H. Dijkstra, ${ }^{38}$ S. Donleavy, ${ }^{52}$ F. Dordei, ${ }^{11}$ M. Dorigo, ${ }^{39}$ A. Dosil Suárez, ${ }^{37}$ D. Dossett, ${ }^{48}$ A. Dovbnya, ${ }^{43}$ K. Dreimanis, ${ }^{52}$ G. Dujany, ${ }^{54}$ F. Dupertuis, ${ }^{39}$ P. Durante, ${ }^{38}$ R. Dzhelyadin, ${ }^{35}$ A. Dziurda, ${ }^{26}$ A. Dzyuba, ${ }^{30}$ S. Easo, ${ }^{49,38}$ U. Egede, ${ }^{53}$ V. Egorychev, ${ }^{31}$ S. Eidelman, ${ }^{34}$ S. Eisenhardt, ${ }^{50}$ U. Eitschberger, ${ }^{9}$ R. Ekelhof, ${ }^{9}$ L. Eklund, ${ }^{51}$ I. El Rifai, ${ }^{5}$ Ch. Elsasser, ${ }^{40}$ S. Ely, ${ }^{59}$ S. Esen, ${ }^{11}$ H.-M. Evans, ${ }^{47}$ T. Evans, ${ }^{55}$ A. Falabella, ${ }^{14}$ C. Färber, ${ }^{11}$ C. Farinelli, ${ }^{41}$ N. 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Nguyen-Mau, ${ }^{39, p}$ M. Nicol, ${ }^{7}$ V. Niess, ${ }^{5}$ R. Niet, ${ }^{9}$ N. Nikitin, ${ }^{32}$ T. Nikodem, ${ }^{11}$ A. Novoselov, ${ }^{35}$ D. P. O'Hanlon, ${ }^{48}$ A. Oblakowska-Mucha, ${ }^{27}$ V. Obraztsov, ${ }^{35}$ S. Oggero, ${ }^{41}$ S. Ogilvy, ${ }^{51}$ O. Okhrimenko, ${ }^{44}$ R. Oldeman, ${ }^{15, \mathrm{n}}$ G. Onderwater, ${ }^{65}$ M. Orlandea,,${ }^{29}$ J. M. Otalora Goicochea, ${ }^{2}$ P. Owen, ${ }^{53}$ A. Oyanguren, ${ }^{64}$ B. K. Pal ${ }^{59}$ A. Palano, ${ }^{13, q}$ F. Palombo, ${ }^{21, \mathrm{r}}$ M. Palutan,${ }^{18}$ J. Panman, ${ }^{38}$ A. Papanestis, ${ }^{49,38}$ M. Pappagallo, ${ }^{51}$ L. L. Pappalardo, ${ }^{16, b}$ C. Parkes, ${ }^{54}$ C. J. Parkinson, ${ }^{9,45}$ G. Passaleva, ${ }^{17}$ G. D. Patel, ${ }^{52}$ M. Patel, ${ }^{53}$ C. Patrignani, ${ }^{19, \mathrm{j}}$ A. Pazos Alvarez, ${ }^{37}$ A. Pearce, ${ }^{54}$ A. Pellegrino, ${ }^{41}$ M. Pepe Altarelli, ${ }^{38}$ S. Perazzini, ${ }^{14, h}$ E. Perez Trigo, ${ }^{37}$ P. Perret, ${ }^{5}$ M. Perrin-Terrin, ${ }^{6}$ L. Pescatore, ${ }^{45}$ E. Pesen, ${ }^{66}$ K. Petridis, ${ }^{53}$ A. Petrolini, ${ }^{19, j}$ E. Picatoste Olloqui, ${ }^{36}$ B. Pietrzyk, ${ }^{4}$ T. Pilař, ${ }^{48}$ D. Pinci, ${ }^{25}$ A. Pistone, ${ }^{19}$ S. Playfer, ${ }^{50}$ M. Plo Casasus, ${ }^{37}$ F. Polci, ${ }^{8}$ A. Poluektov, ${ }^{48,34}$ E. Polycarpo, ${ }^{2}$ A. Popov, ${ }^{35}$ D. Popov, ${ }^{10}$ B. Popovici, ${ }^{29}$ C. Potterat, ${ }^{2}$ E. Price, ${ }^{46}$ J. Prisciandaro, ${ }^{39}$ A. Pritchard, ${ }^{52}$ C. Prouve, ${ }^{46}$ V. Pugatch, ${ }^{44}$ A. Puig Navarro, ${ }^{39}$ G. Punzi, ${ }^{23,5}$ W. Qian, ${ }^{4}$ B. Rachwal, ${ }^{26}$ J. H. Rademacker, ${ }^{46}$ B. Rakotomiaramanana, ${ }^{39}$ M. Rama, ${ }^{18}$ M. S. Rangel, ${ }^{2}$ I. Raniuk, ${ }^{43}$ N. Rauschmayr, ${ }^{38}$ G. Raven, ${ }^{42}$ S. Reichert, ${ }^{54}$ M. M. Reid,,${ }^{48}$ A. C. dos Reis,,${ }^{1}$ S. Ricciardi, ${ }^{49}$ S. 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Tuning, ${ }^{41}$ M. Ubeda Garcia, ${ }^{38}$ A. Ukleja, ${ }^{28}$ A. Ustyuzhanin, ${ }^{63}$ U. Uwer, ${ }^{11}$ V. Vagnoni, ${ }^{14}$ G. Valenti, ${ }^{14}$ A. Vallier, ${ }^{7}$ R. Vazquez Gomez, ${ }^{18}$ P. Vazquez Regueiro, ${ }^{37}$ C. Vázquez Sierra, ${ }^{37}$ S. Vecchi, ${ }^{16}$ J. J. Velthuis, ${ }^{46}$ M. Veltri, ${ }^{17, u}$ G. Veneziano, ${ }^{39}$ M. Vesterinen, ${ }^{11}$ B. Viaud, ${ }^{7}$ D. Vieira, ${ }^{2}$ M. Vieites Diaz, ${ }^{37}$ X. Vilasis-Cardona, ${ }^{36,8}$ A. Vollhardt, ${ }^{40}$ D. Volyanskyy, ${ }^{10}$ D. Voong, ${ }^{46}$ A. Vorobyev, ${ }^{30}$ V. Vorobyev, ${ }^{34}$ C. Voß,,${ }^{62}$ H. Voss, ${ }^{10}$ J. A. de Vries, ${ }^{41}$ R. Waldi, ${ }^{62}$ C. Wallace,,${ }^{48}$ R. Wallace, ${ }^{12}$ J. Walsh, ${ }^{23}$ S. Wandernoth, ${ }^{11}$ J. Wang, ${ }^{59}$ D. R. Ward, ${ }^{47}$ N. K. Watson, ${ }^{45}$ D. Websdale, ${ }^{53}$ M. Whitehead, ${ }^{48}$ J. Wicht, ${ }^{38}$ D. Wiedner, ${ }^{11}$ G. Wilkinson, ${ }^{55}$ M. P. Williams, ${ }^{45}$ M. Williams, ${ }^{56}$ F. F. Wilson, ${ }^{49}$ J. Wimberley, ${ }^{58}$ J. Wishahi, ${ }^{9}$ W. Wislicki, ${ }^{28}$ M. Witek, ${ }^{26}$ G. Wormser, ${ }^{7}$ S. A. Wotton, ${ }^{47}$ S. Wright, ${ }^{47}$ S. Wu, ${ }^{3}$ K. Wyllie, ${ }^{38}$ Y. Xie, ${ }^{61}$ Z. Xing, ${ }^{59}$ Z. Xu, ${ }^{39}$ Z. Yang, ${ }^{3}$ X. Yuan, ${ }^{3}$ O. Yushchenko, ${ }^{35}$ M. Zangoli, ${ }^{14}$ M. Zavertyaev, ${ }^{10, v}$ L. Zhang, ${ }^{59}$ W. C. Zhang, ${ }^{12}$ Y. Zhang, ${ }^{3}$ A. Zhelezov, ${ }^{11}$ A. Zhokhov, ${ }^{31}$ L. Zhong ${ }^{3}$ and A. Zvyagin ${ }^{38}$
(LHCb Collaboration)

[^1]${ }^{9}$ Fakultät Physik, Technische Universität Dortmund, Dortmund, Germany<br>${ }^{10}$ Max-Planck-Institut für Kernphysik (MPIK), Heidelberg, Germany<br>${ }^{11}$ Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany<br>${ }^{12}$ School of Physics, University College Dublin, Dublin, Ireland<br>${ }^{13}$ Sezione INFN di Bari, Bari, Italy<br>${ }^{14}$ Sezione INFN di Bologna, Bologna, Italy<br>${ }^{15}$ Sezione INFN di Cagliari, Cagliari, Italy<br>${ }^{16}$ Sezione INFN di Ferrara, Ferrara, Italy<br>${ }^{17}$ Sezione INFN di Firenze, Firenze, Italy<br>${ }^{18}$ Laboratori Nazionali dell'INFN di Frascati, Frascati, Italy<br>${ }^{19}$ Sezione INFN di Genova, Genova, Italy<br>${ }^{20}$ Sezione INFN di Milano Bicocca, Milano, Italy<br>${ }^{21}$ Sezione INFN di Milano, Milano, Italy<br>${ }^{22}$ Sezione INFN di Padova, Padova, Italy<br>${ }^{23}$ Sezione INFN di Pisa, Pisa, Italy<br>${ }^{24}$ Sezione INFN di Roma Tor Vergata, Roma, Italy<br>${ }^{25}$ Sezione INFN di Roma La Sapienza, Roma, Italy<br>${ }^{26}$ Henryk Niewodniczanski Institute of Nuclear Physics Polish Academy of Sciences, Kraków, Poland<br>${ }^{27}$ AGH-University of Science and Technology, Faculty of Physics and Applied Computer Science, Kraków, Poland<br>${ }^{28}$ National Center for Nuclear Research (NCBJ), Warsaw, Poland<br>${ }^{29}$ Horia Hulubei National Institute of Physics and Nuclear Engineering, Bucharest-Magurele, Romania<br>${ }^{30}$ Petersburg Nuclear Physics Institute (PNPI), Gatchina, Russia<br>${ }^{31}$ Institute of Theoretical and Experimental Physics (ITEP), Moscow, Russia<br>${ }^{32}$ Institute of Nuclear Physics, Moscow State University (SINP MSU), Moscow, Russia<br>${ }^{33}$ Institute for Nuclear Research of the Russian Academy of Sciences (INR RAN), Moscow, Russia<br>${ }^{34}$ Budker Institute of Nuclear Physics (SB RAS) and Novosibirsk State University, Novosibirsk, Russia<br>${ }^{35}$ Institute for High Energy Physics (IHEP), Protvino, Russia<br>${ }^{36}$ Universitat de Barcelona, Barcelona, Spain<br>${ }^{37}$ Universidad de Santiago de Compostela, Santiago de Compostela, Spain<br>${ }^{38}$ European Organization for Nuclear Research (CERN), Geneva, Switzerland<br>${ }^{39}$ Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland<br>${ }^{40}$ Physik-Institut, Universität Zürich, Zürich, Switzerland<br>${ }^{41}$ Nikhef National Institute for Subatomic Physics, Amsterdam, The Netherlands<br>${ }^{42}$ Nikhef National Institute for Subatomic Physics and VU University Amsterdam, Amsterdam, The Netherlands<br>${ }^{43}$ NSC Kharkiv Institute of Physics and Technology (NSC KIPT), Kharkiv, Ukraine<br>${ }^{44}$ Institute for Nuclear Research of the National Academy of Sciences (KINR), Kyiv, Ukraine<br>${ }^{45}$ University of Birmingham, Birmingham, United Kingdom<br>${ }^{46}$ H.H. Wills Physics Laboratory, University of Bristol, Bristol, United Kingdom<br>${ }^{47}$ Cavendish Laboratory, University of Cambridge, Cambridge, United Kingdom<br>${ }^{48}$ Department of Physics, University of Warwick, Coventry, United Kingdom<br>${ }^{49}$ STFC Rutherford Appleton Laboratory, Didcot, United Kingdom<br>${ }^{50}$ School of Physics and Astronomy, University of Edinburgh, Edinburgh, United Kingdom<br>${ }^{51}$ School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom<br>${ }^{52}$ Oliver Lodge Laboratory, University of Liverpool, Liverpool, United Kingdom<br>${ }^{53}$ Imperial College London, London, United Kingdom<br>${ }^{54}$ School of Physics and Astronomy, University of Manchester, Manchester, United Kingdom<br>${ }^{55}$ Department of Physics, University of Oxford, Oxford, United Kingdom<br>${ }^{56}$ Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA<br>${ }^{57}$ University of Cincinnati, Cincinnati, Ohio 45221, USA<br>${ }^{58}$ University of Maryland, College Park, Maryland 20742, USA<br>${ }^{59}$ Syracuse University, Syracuse, New York 13244, USA<br>${ }^{60}$ Pontifícia Universidade Católica do Rio de Janeiro (PUC-Rio), Rio de Janeiro, Brazil (associated with Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil)<br>${ }^{61}$ Institute of Particle Physics, Central China Normal University, Wuhan, Hubei, China<br>(associated with Center for High Energy Physics, Tsinghua University, Beijing, China)<br>${ }^{62}$ Institut für Physik, Universität Rostock, Rostock, Germany<br>(associated with Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany)<br>${ }^{63}$ National Research Centre Kurchatov Institute, Moscow, Russia<br>(associated with Institute of Theoretical and Experimental Physics (ITEP), Moscow, Russia)

${ }^{64}$ Instituto de Fisica Corpuscular (IFIC), Universitat de Valencia-CSIC, Valencia, Spain (associated with Universitat de Barcelona, Barcelona, Spain)<br>${ }^{65}$ KVI-University of Groningen, Groningen, The Netherlands (associated with Nikhef National Institute for Subatomic Physics, Amsterdam, The Netherlands)<br>${ }^{66}$ Celal Bayar University, Manisa, Turkey (associated with European Organization for Nuclear Research (CERN), Geneva, Switzerland)

${ }^{a}$ Also at Università di Firenze, Firenze, Italy.<br>${ }^{\mathrm{b}}$ Also at Università di Ferrara, Ferrara, Italy.<br>${ }^{\text {c }}$ Also at Università della Basilicata, Potenza, Italy.<br>${ }^{\mathrm{d}}$ Also at Università di Modena e Reggio Emilia, Modena, Italy.<br>${ }^{\mathrm{e}}$ Also at Università di Padova, Padova, Italy.<br>${ }^{\mathrm{f}}$ Also at Università di Milano Bicocca, Milano, Italy.<br>${ }^{\mathrm{g}}$ Also at LIFAELS, La Salle, Universitat Ramon Llull, Barcelona, Spain.<br>${ }^{h}$ Also at Università di Bologna, Bologna, Italy.<br>${ }^{i}$ Also at Università di Roma Tor Vergata, Roma, Italy.<br>${ }^{\mathrm{j}}$ Also at Università di Genova, Genova, Italy.<br>${ }^{\mathrm{k}}$ Also at Politecnico di Milano, Milano, Italy.<br>${ }^{1}$ Also at Universidade Federal do Triângulo Mineiro (UFTM), Uberaba-MG, Brazil.<br>${ }^{\mathrm{m}}$ Also at AGH-University of Science and Technology, Faculty of Computer Science, Electronics and Telecommunications, Kraków, Poland.<br>${ }^{\text {n }}$ Also at Università di Cagliari, Cagliari, Italy.<br>${ }^{\circ}$ Also at Scuola Normale Superiore, Pisa, Italy.<br>${ }^{\mathrm{p}}$ Also at Hanoi University of Science, Hanoi, Viet Nam.<br>${ }^{\mathrm{q}}$ Also at Università di Bari, Bari, Italy.<br>${ }^{\mathrm{r}}$ Also at Università degli Studi di Milano, Milano, Italy.<br>${ }^{\text {s }}$ Also at Università di Pisa, Pisa, Italy.<br>${ }^{t}$ Also at Università di Roma La Sapienza, Roma, Italy.<br>${ }^{\text {u }}$ Also at Università di Urbino, Urbino, Italy.<br>${ }^{v}$ Also at P.N. Lebedev Physical Institute, Russian Academy of Science (LPI RAS), Moscow, Russia.


[^0]:    * Full author list given at the end of the article.

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[^1]:    ${ }^{1}$ Centro Brasileiro de Pesquisas Físicas (CBPF), Rio de Janeiro, Brazil
    ${ }^{2}$ Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil
    ${ }^{3}$ Center for High Energy Physics, Tsinghua University, Beijing, China
    ${ }^{4}$ LAPP, Université de Savoie, CNRS/IN2P3, Annecy-Le-Vieux, France
    ${ }^{5}$ Clermont Université, Université Blaise Pascal, CNRS/IN2P3, LPC, Clermont-Ferrand, France ${ }^{6}$ CPPM, Aix-Marseille Université, CNRS/IN2P3, Marseille, France
    ${ }^{7}$ LAL, Université Paris-Sud, CNRS/IN2P3, Orsay, France
    ${ }^{8}$ LPNHE, Université Pierre et Marie Curie, Université Paris Diderot, CNRS/IN2P3, Paris, France

