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Journal of Geophysical Research: Space Physics

RESEARCH ARTICLE

10.1002/2014JA020836

Key Points:

- We derive a generic shape for interplanetary magnetic clouds and shocks
- We compare observed distributions from several lists of MCs/shocks
- The ellipsoidal model is the best for both MC axis and shock shell

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Citation:

Janvier, M., S. Dasso, P. Démoulin, J. J. Masías-Meza, and N. Lugaz (2015), Comparing generic models for interplanetary shocks and magnetic clouds axis configurations at 1 AU, *J. Geophys. Res. Space Physics, 120,* 3328–3349, doi:10.1002/2014JA020836.

Received 18 NOV 2014 Accepted 20 MAR 2015 Accepted article online 26 MAR 2015 Published online 19 May 2015

Comparing generic models for interplanetary shocks and magnetic clouds axis configurations at 1 AU

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JGR

Abstract Interplanetary coronal mass ejections (ICMEs) are the manifestation of solar transient eruptions, which can significantly modify the plasma and magnetic conditions in the heliosphere. They are often preceded by a shock, and a magnetic flux rope is detected in situ in a third to half of them. The main aim of this study is to obtain the best quantitative shape for the flux rope axis and for the shock surface from in situ data obtained during spacecraft crossings of these structures. We first compare the orientation of the flux rope axes and shock normals obtained from independent data analyses of the same events, observed in situ at 1 AU from the Sun. Then we carry out an original statistical analysis of axes/shock normals by deriving the statistical distributions of their orientations. We fit the observed distributions using the distributions derived from several synthetic models describing these shapes. We show that the distributions of axis/shock orientations are very sensitive to their respective shape. One classical model, used to analyze interplanetary imager data, is incompatible with the in situ data. Two other models are introduced, for which the results for axis and shock normals lead to very similar shapes; the fact that the data for MCs and shocks are independent strengthens this result. The model which best fits all the data sets has an ellipsoidal shape with similar aspect ratio values for all the data sets. These derived shapes for the flux rope axis and shock surface have several potential applications. First, these shapes can be used to construct a consistent ICME model. Second, these generic shapes can be used to develop a quantitative model to analyze imager data, as well as constraining the output of numerical simulations of ICMEs. Finally, they will have implications for space weather forecasting, in particular, for forecasting the time arrival of ICMEs at the Earth.

1. Introduction

Interplanetary coronal mass ejections (ICMEs) are the interplanetary manifestations of coronal mass ejections (CMEs) and are identified by a number of typical properties that differ from those of the ambient solar wind [e.g., *Gosling*, 1990, 2000; *Neugebauer and Goldstein*, 1997; *Wimmer-Schweingruber et al.*, 2006; *Zurbuchen and Richardson*, 2006; *Rouillard*, 2011]. A region of compressed plasma and magnetic field, called the sheath, is typically present at the front of ICMEs. When the leading front is faster than the ambient solar wind (above the local fast MHD mode speed), an ICME is preceded by a shock.

An ICME can be distinguished from the ambient solar wind by analyzing both remote and in situ observations, with remote observations being the privileged method to give hints on their 3-D shape. Nonetheless, coronagraphs and heliospheric imagers still only provide 2-D images of the denser parts of CMEs through the Thomson scattering of white light by free electrons [*Howard*, 2011; *Thernisien et al.*, 2011]. Furthermore, since the location of the scattered light cannot unambiguously be determined along the line of sight, a shape model is typically needed to analyze the observations.

Classical shape models are pointlike or are represented by a sphere surrounding or attached to the Sun [*Lugaz et al.*, 2010, and references therein]. These models allow the estimation of the propagation direction and the speed of ICMEs, especially when triangulation with different spacecraft is possible [*Liu et al.*, 2013]. More elaborated analytical models have been proposed such as a dense shell located around a flux-rope-like shape [*Thernisien et al.*, 2006], parametric models of sheath shapes [*Tappin and Howard*, 2009; *Howard and Tappin*, 2010], and another parametric shape applied to both sheaths and flux ropes was proposed by *Wood and Howard* [2009]. All these models were fitted visually to CMEs observed with coronagraphs and/or heliospheric

©2015. American Geophysical Union. All Rights Reserved. imagers. However, it remains difficult to quantify the quality of the fit for each of these models and to confirm whether the derived shape is indeed representative of the CME 3-D shape (e.g., multiple solutions are possible for a given set of CME observations). Finally, while other techniques have been tested, as reviewed by *Mierla et al.* [2010], present multispacecraft remote observations cannot uniquely determine the 3-D shape of the bright front, even when they can be tracked and be unambiguously connected to the CME source [*Harrison et al.*, 2008; *Möstl et al.*, 2009; *Lugaz and Roussev*, 2011].

Magnetic Clouds (MCs) can be distinguished inside a fraction of ICMEs, when they are observed in situ. An MC is identified as a structure presenting an enhanced magnetic field intensity, a large scale and coherent magnetic field rotation (associated with the passage of a large-scale flux rope, FR), and low proton temperatures [e.g., *Burlaga et al.*, 1981; *Dasso et al.*, 2005]. Theoretical models describing the global shape of MCs in the heliosphere have been developed and compared with single spacecraft in situ observations [e.g., *Marubashi and Lepping*, 2007; *Hidalgo and Nieves-Chinchilla*, 2012]. However, reconstructing the 3-D global FR shape from in situ measurements is an ill-posed problem, as there is no unique solution. Moreover, the models frequently contain many free parameters, so that minimizing the difference between observations and models can sometimes provide several compatible solutions.

Simultaneous multispacecraft observations of a given event can provide a better understanding of the global shape of MCs. Some studies have shown that the directions of the local axis of a given MC, at well-separated locations from different spacecraft, are consistent with a smooth global axis of the cloud in the heliosphere (see, e.g., *Burlaga et al.* [1981] and Figure 2 in *Ruffenach et al.* [2012]) but this is not always the case (e.g., *Farrugia et al.* [2011]). However, this kind of simultaneous observations of the same event is not frequent.

Numerical simulations have also been used to better understand the propagation and evolution of MCs in the solar wind [e.g., *Riley et al.*, 2003; *Manchester et al.*, 2004; *Lugaz and Roussev*, 2011]. There are, however, limitations for emulating some physical processes, such as magnetic reconnection, the effects of the turbulence on macroscopic structures such as the drag [e.g., *Matthaeus and Velli*, 2011], or the dynamical evolution of structures strongly dominated by the magnetic field (such as magnetic clouds). Some ICME propagation properties can be found by combining observations with simulations [e.g., *Lugaz et al.*, 2009; *Lugaz and Roussev*, 2011].

Recently, *Janvier et al.* [2013] analyzed the distribution of MC local orientation from a sample of more than 100 events observed at 1 AU by Wind and derived the mean shape of the MC axis with an original statistical method. A comparable technique was also used for deriving the shock surface driven by ICMEs from observations of the shock normal in a sample of more than 250 events observed at 1 AU by the ACE spacecraft [*Janvier et al.*, 2014a].

In this paper, we apply, extend, and combine the techniques previously used [Janvier et al., 2013, 2014a], with the aim of determining the generic shape of the MC axis and the shock surface, combining different samples/databases for MCs and shocks. In section 2, we present the samples of MCs and shocks we use in this statistical study and provide a comparison of the results given for the same events analyzed by different authors. We also define the angles used to determine the orientation of the MC axis and normal to the shock surface. In section 3, we first set the techniques to derive the axis and shock shapes with the same formalism. Then, we apply them to various data sets and we compare these results to three analytical models. We find that one of the models is the closest to all the observations analyzed, and we test the robustness of our results. Then we summarize our main results in section 4 and outline the implications of our results in section 5.

2. Samples of Observed MCs and Shocks and Definition of the Shape Parameters 2.1. Sets of Observed MCs, Similarities, and Differences

In the present study, we use three lists of MCs where the FR parameters are already determined by a common method, namely, the data were fitted with the static, linear force-free cylindrical model, also known as the Lundquist's model [see, e.g., *Lundquist*, 1950; *Goldstein*, 1983; *Lepping et al.*, 1990]. A detailed description of the model and its limitations can be found in *Lepping et al.* [1990, 2003] and more information on the fitting methods used can be found in *Lynch et al.* [2003] and *Feng et al.* [2007].

Lynch et al. [2005] analyzed 132 MCs observed nearby Earth by Wind and ACE spacecraft during the period 1995–2003. *Feng et al.* [2010] analyzed 62 MCs preceded by a shock and observed by Wind during the period 1995–2007. Finally, we use an extended list of events (Table 2 at http://wind.nasa.gov/mfi/mag_ cloud_S1.html) which is based on the results of *Lepping and Wu* [2010] and includes more recent MCs. This list

contains the parameters obtained for 121 MCs observed by Wind spacecraft during the period 1995–2009. We remove from *Lepping and Wu* [2010]'s list the MCs that were crossed too close from their boundaries, limiting the list to 107 MCs (for coherence with previous study, see *Janvier et al.* [2013]).

The above fitting method has several limitations. For example, due to its simplicity, the model does not take into account the expansion of MCs, although this could affect the fitted model parameters and the derived quantities [e.g., see *Nakwacki et al.*, 2008, Tables 3 and 4]. Another important limitation is the assumed circular cross section, and as such several noncircular models have been proposed [e.g., *Hu and Sonnerup*, 2002; *Vandas et al.*, 2005; *Hidalgo*, 2003]. From a statistical study of the closest approach of the spacecraft from the MC axis, using the *Lepping and Wu* [2010]'s list, *Démoulin et al.* [2013] showed that the MC cross section is flatter in the radial direction (from the Sun) by a third to a half on average. Indeed, some MCs have a relatively flattened cross section, especially at their cores [*Hu and Dasgupta*, 2005; *Liu et al.*, 2008; *Möstl et al.*, 2009; *Isavnin et al.*, 2011]. The effects of a noncircular cross section on the derived properties of MCs (e.g., their axis direction) remain to be characterized for large sets of MCs. So far such lists are only available for the fit with the Lundquist model, so with a circular cross section.

While the three MC lists used in the present study [*Lynch et al.*, 2005; *Feng et al.*, 2010; *Lepping and Wu*, 2010] are based on the same fitting method to determine the FR parameters, the fit has been applied in different ways to the various MC samples. For example, *Lynch et al.* [2005] imposed that the spacecraft closest approach to the FR axis is the temporal midpoint of the FR, so that the FR radius is not a parameter of the fit (in contrast with other authors) but is instead determined from the FR properties: orientation, mean velocity, and impact parameter (defined as the closest distance approach of the spacecraft to the FR axis divided by the FR radius). Among the differences in the method implementation, the difference in the FR boundary selection is, in our opinion, the most important, as it could have large implications on the derived FR orientation [e.g., *Dasso et al.*, 2006; *Ruffenach et al.*, 2012]. The boundaries are typically set where abrupt changes of the magnetic field and plasma parameters are detected [e.g., *Dasso et al.*, 2007]. However, if such changes are not colocated, then different criteria can provide different boundary locations. As such, it often occurs that one MC can be defined with different boundary locations on the authors [e.g., *Riley et al.*, 2004; *Al-Haddad et al.*, 2013].

An important physical process during the evolution of MCs in the solar wind to be considered and which strongly affects the determination of their boundaries is their erosion as they travel away from the Sun. As the magnetic field of MCs can reconnect with that of the ambient solar wind, a part of the original FR disappears, so that a case-dependent fraction of an MC can have a mixture of both MC and solar wind properties. This leads to large uncertainties when an FR is actually identified. Thus, a detailed analysis of each MC is needed to determine which remaining region of the FR is crossed by the spacecraft, and the fit should only be applied to this specific part of the MC. As an example, minimum variance and Lundquist's fit can result in significantly different orientations, without coherence along the axis of an MC observed by four spacecraft (ACE, STEREO A and B, and Wind) [*Farrugia et al.*, 2011], while both methods give consistent results when refined time intervals (e.g., considering an eroded FR) are used [*Ruffenach et al.*, 2012].

2.2. Sets of Observed Shocks

In the present paper, we study the probability distributions of shock orientation parameters from different samples. We use lists of shocks studied in *Feng et al.* [2010] and *Wang et al.* [2010]. The shocks of *Feng et al.* [2010] were observed by Wind spacecraft during the period 1995–2007 and were all located at the front of an MC sheath. The list contains 62 shocks. Shock and shock-like events from *Wang et al.* [2010] were observed by ACE spacecraft during the period 1998–2008. They were investigated with the purpose of analyzing their effects on the Earth magnetosphere and ionosphere. In the following, we only retain the well-defined shock events, which represent a total of 216 cases (117 shocks in front of ICMEs and 99 shocks with no detected ICMEs behind).

Both of these shock studies are based on a shock fitting procedure using the MHD Rankine-Hugoniot relations as developed by *Lin et al.* [2006]. The model used to determine the geometry of the shock is based on the one-fluid anisotropic Rankine-Hugoniot relations. A Monte Carlo calculation and a minimization technique between the generated models and observations were also similarly used. However, while the basic technique is the same in both studies, there are variations affecting the computed shock parameters. First, the data are from two different spacecraft, involving different measurements with their own specificities. Second, the results depend on the selected time intervals, both for the upstream and downstream regions



Figure 1. Diagram of an MC and associated parameters: (a) perspective view, (b) side view. The MC axis is drawn in blue, its borders in black and one representative magnetic field line is added. The inclination angle, *i*, is defined by the angle made by the axis direction projected on the *y*-*z* plane with the *y* direction (in GSE coordinates). The maximum angular extension of the MC axis, as viewed from the Sun, is $\varphi_{max, axis}$ while the shock extends up to $\varphi_{max, shock}$. The location angle λ is defined by the angle between the radial direction from the Sun and the normal to the MC axis or the shock.

of the shocks, which are used to select the magnetic field and plasma parameters used in the minimisation technique. Finally, the results also depend on the terms included in the Rankine-Hugoniot relations (see the two methods studied in *Lin et al.* [2006]). As a consequence, differences between the results of both studies have to be expected when the same shock is analyzed. We analyze these differences in section 2.4.

2.3. Angles Defining the MC Axis and Shock Normal

The directions of the FR local axis and the shock normal are obtained from the fitting and minimization procedures for both MCs and shocks, respectively. For in situ observations at 1 AU, i.e., nearby Earth, unit vectors used to express directions are classically defined in the GSE system of reference. Setting a spherical coordinate system with a south-north polar axis, the orientation vector is classically defined by its latitude and longitude. However, the polar axis direction is singular, as it corresponds to any values of longitude. Therefore, as the absolute value of the latitude becomes larger, any small change in the vector orientation leads to a large uncertainty in the longitude determination. This is a problem when characterizing the orientation of the axis of an MC, which may be highly inclined to the ecliptic. However, MC axes are found to rarely lie in the radial direction. Thus, Janvier et al. [2013] introduced a new spherical coordinate system, with a polar axis along the Sun-Earth direction (along $-\hat{\mathbf{x}}_{GSE}$). Projecting the unit vector on a plane perpendicular to $\hat{\mathbf{x}}_{GSE}$. they introduced the inclination angle i on the ecliptic. It is measured from the west-east direction (\hat{y}_{GSF}) in a clockwise direction (when looking toward the Sun, see Figure 1a). A second angle was defined as the location angle λ , which measures the angle between the FR axis direction and the orthoradial. Equivalently, λ is also the angle between the radial direction and the normal to the FR axis ($\hat{\mathbf{n}}_{axis}$ located within the plane i = constant, Figure 1b). Then, for both cases (shock normal and MC axis), λ is defined in the same way, as the angle between $-\hat{\mathbf{x}}_{GSE}$ and $\hat{\mathbf{n}}$ ($\hat{\mathbf{n}}_{shock}$ or $\hat{\mathbf{n}}_{axis}$) and both λ_{axis} and λ_{shock} measure the location of the spacecraft crossing if the MC/shock axis shape is known. For λ_{axis} and λ_{shock} values close to zero, the spacecraft crossing is close to the apex of each structure, while both λ_{axis} and λ_{shock} increase as the crossing is more on the flank of the encountered structure, therefore defining λ as a "location" angle (see section 3).

In summary, (λ, i) defines a new spherical coordinate system where $-\hat{\mathbf{x}}_{GSE}$ is the polar axis. Both angles λ and i are related with the latitude θ and the longitude ϕ of $\hat{\mathbf{n}}_{axis}$ or $\hat{\mathbf{n}}_{shock}$ by

$$\sin \lambda = -\cos\phi\cos\theta \tag{1}$$

$$\tan i = \tan \theta / |\sin \phi| \,. \tag{2}$$

Then, λ and *i* are both functions of ϕ and θ . However, with MC data [*Janvier et al.*, 2014b] as well as for shocks (not shown), λ is mostly correlated with ϕ , and *i* with θ .

2.4. Precision of the Axis and Shock Normal Directions

The typical level of precision that can be determined for $\hat{\mathbf{n}}_{axis}$ and $\hat{\mathbf{n}}_{shock}$ is investigated in more detail below, by comparing the orientation parameters for events that are common to different data sets. To do so, we associated events by comparing the times defining the boundaries of MCs or shocks.

The time window for the association of MCs from different lists was set to 10 h, for both front and rear boundaries. We chose a rather large window, as the definition of the MC boundaries is dependent on the plasma and magnetic data used, as well as on the authors' selection criteria. However, we also computed an association with a smaller time window (e.g., 5 h), which provided comparable results but with less cases. Extending the time window to more than 10 h, however, leads to a few MCs of one list associated to two MCs of another list and, therefore, wrong results.

For shocks, the time window was set to 1 h, as shocks are better temporally localized than MC boundaries. We also included in this time window the delay between ACE and Wind observations. Note that further extending this time window (e.g., 2 h) only provides a few more associations.

The Lepping and Wu's list has 45% and 49% of MCs in common with the Lynch's and Feng's list, respectively, and the Wang's list has only 14% of shocks in common with the Feng's list (which is limited to shocks associated to MCs). This indicates that we can compare the results obtained for the same events, while also having a significant number of independent events.

The relations between λ and *i* for the same events in different pairs of event lists are analyzed in Figure 2. We show there the values of $|\lambda|$, i.e., we have grouped together the values of λ obtained in the west and east legs of the MCs, increasing the statistics (this is also justified by a weak asymmetry between the two MC legs, as found in *Janvier et al.* [2013]). Moreover, this allows the direct comparison of the results obtained for the MCs with those obtained for the shocks, as the sign of λ cannot be determined for the latter. For convenience, we mark in the following and in all graphs λ instead of $|\lambda|$. The data are fitted by a linear function (in blue), which provides an easy visual interpretation of how close two results are for one same event. We also report two rank-order correlation coefficients, the Pearson (c_p) and Spearman (c_s) ones, as well as the standard deviation (SD) between the two data sets. As a whole, the location angle λ (Figure 2, left) between two samples is not as well correlated as the inclination angle *i* (Figure 2, right). The parameter λ also has a larger global bias since the linear fit (blue line) is located farther away from the identity line (in brown) than for the *i* angle, for which both lines almost coincide. Finally, λ has a lower standard deviation than *i* by a factor 2 to 5, but this is not a striking result considering that the range of variation for $i (\approx [-150^\circ, 150^\circ])$ is 5 times larger than the range of variation for λ ($\approx [0^\circ, 60^\circ]$) so that the standard deviation relative to the range of variation is broadly comparable for λ and *i*.

For MCs, the quality of the fit is measured by χ , the square root of the chi square function between the measurement of the magnetic field inside the FR and the fitted profile. The values of both χ and the impact parameter, p, could a priori affect the precision of $\hat{\mathbf{n}}_{axis}$. In fact, we found no significant improvement in the rank-order correlation coefficients, nor in the standard deviation values, when we analyzed sets of data containing only lower χ values. Next, by taking the common cases in Lepping and Wu's and Feng's lists of MCs, we found that both the correlation coefficients and the standard deviation value are not significantly affected by |p|. However, if Lynch's MCs are associated with either Lepping and Wu's or Feng's MCs, the correlation coefficients significantly increase as the maximum value of |p| decreases from 1 to 0.5. Thus, the results of *Lynch et al.* [2005] depend more on the magnitude of the estimated |p| values than for the other two lists.

The large dispersion in the values of λ found by different authors, especially for its lower values, is not straightforward to interpret. Indeed, for low values of λ (i.e., near the apex), one would expect that shocks, and similarly MCs, have a better determined normal as the spacecraft crosses its structure orthogonally. These expectations appear to be not true considering the results found in Figure 2. A possible candidate to account for such an effect may be the determination of the flux rope boundaries. Thus, the location of the MC/shock crossing (as quantified by λ) is not an important parameter in determining the precision of the normal/axis direction.

In conclusion, the large dispersion of λ and *i* angles between different MC lists is consistent with the results of *Al-Haddad et al.* [2013] who tested the results of a larger variety of methods but on a more limited sample of MCs. This large dispersion, both for the MC axis and shock normal directions, does not allow the comparison of these directions for individual MCs (as attempted by *Feng et al.* [2010]). However, we will show in section 3 that the distributions of λ provide robust information on the MC axis and the shock shapes.



Figure 2. (left) Correlations between the absolute value of the location angle λ (defined in Figure 1b) values, and (right) correlations between the inclination angle values, *i* obtained for the same cases in different samples of MCs and shocks. We show the values of $|\lambda|$ (noted λ for convenience) for the MCs for a better comparison with the shocks (for which the sign of λ cannot be determined). The two first rows are the correlations for MCs, with the orientation parameters found by *Lepping and Wu* [2010] reported on the horizontal axis. The values found by (top) *Lynch et al.* [2005] and (middle) *Feng et al.* [2010] are reported on the vertical axis. The bottom row represents the correlation between the parameters obtained by associating the shocks studied by *Feng et al.* [2010] with those by *Wang et al.* [2010]. The parameters c_p and c_s are the Pearson and Spearman ranking correlation coefficients, and "SD" is the standard deviation, in degree, between the two data sets (red points). The blue line is the least squares fit for the data, while the brown line represents the identity function (i.e., equal values of λ , or *i*, for each set of events). These results show a correlation both for λ and *i* between different data sets but with a large dispersion as indicated by "SD."

2.5. Probability Distributions of the Orientation Parameters

Analyses of the inclination angle *i* for the 107 MCs detected by Wind [*Lepping and Wu*, 2010] and for the 216 shocks detected by ACE [*Wang et al.*, 2010] were performed by *Janvier et al.* [2013, 2014a], respectively. Taking into account the statistical fluctuations of limited samples, no global tendency was found for *i* (its probability distribution appeared to be uniform for both MC and shocks). We confirm this isotropy of inclination in the present paper by analyzing the histograms of *i* for the MCs analyzed by *Lynch et al.* [2005] and *Feng et al.* [2010] and for the shocks analyzed by *Feng et al.* [2010], as shown in Figure 3 where no global tendency is present over the statistical fluctuations both for the full sets (blue histograms) as well as with restricted sets defined with a restricted range of the impact parameter (pink and light brown histograms) as described at the end of



Figure 3. Histograms of the inclination angle *i* (defined in Figure 1a) for different data sets as written in the top labels. *N* is the total number of cases in the histogram. N_{axis} (N_{shock}) is the number of MCs (shocks) in each bin, plotted versus *i* for the (top row) MC axis and the (bottom row) shock normal. The 20 bins are regularly spaced between *i* = -180 and 180°. Figures 3 (top left) and 3 (middle) show the total number of cases in blue, while the overplotted histograms show cases constrained to an impact parameter |p| lower than a given threshold (|p| < 0.7 in magenta and |p| < 0.5 in orange). This way, the bars in blue are always the longest ones in the histogram, as they correspond to the number of cases without constraints on |p| and are covered with the magenta and light orange bars. Figures 3 (bottom left) and 3 (middle) show the distribution of *i* for the shocks reported in *Wang et al.* [2010], either taken all together (Figure 3, left) or with the constraint that an MC was observed following the shock (Figure 3, middle). These histograms all show no global tendency with *i* (within the statistical fluctuation limit).

this section. We selected 20 bins in the histograms as a compromise between statistical fluctuations in each bin and a visualization of the variations with *i*.

We interpret this isotropy of inclination as follows. The MCs and the majority of the shocks observed at 1 AU are generated by CMEs launched from the Sun. During a time period of several years, as covered by the data sets, the Sun launched CMEs from a large number of unrelated source regions with diverse orientations. If there is no preferential orientation in the sources, a spacecraft is expected to cross the MCs and shocks associated with the CMEs with an approximative uniform probability of *i*. As such, the above results indicate that there is no privileged direction of $\hat{\mathbf{n}}_{axis}$ and $\hat{\mathbf{n}}_{shock}$ around the Sun apex line (within the limits of the statistical fluctuations).

In contrast, the probability distributions of λ (Figure 4), for both MCs and shocks, are largely nonuniform, even when considering statistical fluctuations (which are typically of the order of $\sqrt{n_c}$ where n_c is the number of cases in a histogram bin). All the MC axis distributions are globally decreasing functions of λ (except for the narrow peak at $\lambda \approx 30^\circ$ for Lynch et al., however, this peak may not be statistically significant). Then the axis distributions are different than the shock distributions, which all peak around $\lambda \approx 30^\circ$ (Figure 4). Even though subgroups of events lead to larger statistical fluctuations, the shape of the distributions remains almost the same. For example, similar histograms are found when considering subgroups of MCs with different fitting qualities [see, e.g., *Janvier et al.*, 2013, Figure 5] or when considering subgroups of shocks corresponding to different categories of ICMEs ([see, e.g., *Janvier et al.*, 2014a, Figure 5] and Figure 4 for shocks associated to MCs).

The quality of the estimation of the FR axis direction decreases with the absolute value of the impact parameter |p| [e.g., *Riley et al.*, 2004], which is related to the distance of the spacecraft trajectory to the FR axis. We investigated the effect of |p| on the above distributions and found no significant effect for both parameters *i* and λ : the histograms with |p| < 0.7 (pink) and |p| < 0.5 (light brown) have a similar dependence with *i* and λ than when all cases are considered (blue) as shown in Figures 3 and 4. This is because large |p| values are present in all the values taken by *i* and λ , so that the general tendencies remain the same. The sample that has the largest relative number of cases with |p| > 0.5 is that of *Lynch et al.* [2005], with 45% of the cases (Figure 4, top middle). We anticipate that the conclusion derived from the general properties of the orientation parameter distributions will be weakly affected by the (non)inclusion of the cases with large |p| values.



Figure 4. Histograms of the location angle λ (defined in Figure 1b) for different data sets as written in the top labels. *N* is the total number of cases in the histogram. *N*_{axis} (*N*_{shock}) is the number of MCs (shocks) in each bin, plotted versus λ for the (top row) MC axis and the (bottom row) shock normal. The 20 bins are regularly spaced between $\lambda = 0$ and 90°. The color convention is the same as in Figure 3. These histograms are examples of distributions of λ used to constrain the MC axis and shock shapes.

3. Best Synthetic Models to Fit In Situ Data

In this section, we explore the properties of the shapes given by different synthetic models, for both the axis of MCs and the shock fronts. These properties are directly compared with those given by in situ data, allowing us to select the best models to reproduce the mean shape of both MC axis and shocks. To do so, the probability distributions of the parameters describing these synthetic models are least squares fitted to the distribution of the observed MC axis and shock normal.

3.1. Generic Equations for Axisymmetric Models

We first start with the description of the basic and general equations that we use to describe the models. These equations were previously introduced for the MC axis and shock front [*Janvier et al.*, 2013, 2014a] using spherical coordinates (ρ , Φ , φ) centered on the Sun (S). For a given point on the shock surface, Φ is the angle defining the position around the Sun apex line, while for the MC axis, Φ is constant since the axis is supposed to be contained in a plane for a given event.

For the shock front, we suppose in the present work a symmetry of rotation, so that the shock surfaces are all independent of Φ . This simplifies the expression for ρ , the distance between the Sun (S) and the spacecraft crossing point (M). Then, the vector from the Sun to the point M can be written as a function of φ as (Figure 1b):

$$\vec{SM} = \rho(\varphi)\hat{\mathbf{u}}_{\rho}.$$
(3)

The location angle λ is defined as the angle between the radial direction from the Sun (along $\hat{\mathbf{u}}_{\rho}$) and the local normal ($\hat{\mathbf{n}}$) to the axis/shock shape. λ is related to $\rho(\varphi)$ as follows:

$$\tan \lambda = \frac{\hat{\mathbf{n}} \cdot \hat{\mathbf{u}}_{\varphi}}{\hat{\mathbf{n}} \cdot \hat{\mathbf{u}}_{\rho}} = -\frac{\mathrm{d}\ln\rho}{\mathrm{d}\varphi} \,. \tag{4}$$

The above two expressions remain the same for both the shock and the MC axis.

The shock surface extends from $\varphi = 0$ at the apex to $\pm \varphi_{\max, \text{shock}}$ on the flank, with a symmetry of rotation around the Sun apex line (Figure 1b). For consistency, the axis shape is also symmetric around the apex and it extends up to $\varphi = \pm \varphi_{\max, \text{axis}}$. In both cases, λ is included in the interval [0, 90°], with $\lambda = 0$ at the apex and λ approaching 90° in the legs of the MC axis/flank of the shock front.

Supposing that $\rho(\varphi)$ is a decreasing function of φ (so that the shape $\rho(\varphi)$ is concave toward the Sun, in agreement with observations and simulations [e.g., *Cane*, 1985; *Lugaz et al.*, 2014], equation (4) implies that λ is a

monotonously increasing function of φ . It implies that spacecraft crossings in the range $\varphi \pm d\varphi$ correspond to the unique range $\lambda \pm d\lambda$. The conservation of the number of cases implies

$$\mathcal{P}_{\varphi}(\varphi) \mathrm{d}\varphi = \mathcal{P}(\lambda) \mathrm{d}\lambda \,, \tag{5}$$

where $\mathcal{P}_{\varphi}(\varphi) d\varphi$ is the probability of spacecraft crossings in the interval $\varphi \pm d\varphi/2$ and $\mathcal{P}(\lambda) d\lambda$ is the probability in the interval $\lambda \pm d\lambda/2$.

A spacecraft located at 1 AU, over several years, will cross a large number of ICMEs launched from the Sun from a broad range of latitudes and longitudes with no privileged direction of propagation. It implies that one can suppose a nearly uniform distribution of crossings. Then, the MC axis is expected to be detected with a uniform distribution of φ . The normalization of the total probability to unity implies that $\mathcal{P}_{\varphi}(\varphi) = 1/\varphi_{max}$. This probability is different for shocks, however, since they extend as a surface: the probability of detection in the range $\varphi \pm d\varphi$ is proportional to the corresponding fraction of the cross section of the sphere of radius D = 1 AU centered on the Sun, so $\mathcal{P}_{\varphi} d\varphi \propto 2\pi D^2 \sin \varphi \, d\varphi$. The coefficient of proportionality is again found by normalizing the total probability to unity. Summarizing, the probability of crossing axis/shock is as follows:

$$\mathcal{P}_{\varphi}(\varphi) = 1/\varphi_{\text{max}}$$
 for MC axis, (6)

$$= \frac{\sin \varphi}{1 - \cos \varphi_{\max}} \quad \text{for shocks.}$$
(7)

With the above result for $\mathcal{P}_{\varphi}(\varphi)$, equation (5) defines $\mathcal{P}(\lambda)$ when $d\varphi/d\lambda$ is known, i.e., when the shape is known since the derivation of equation (4) with respect to λ defines $d\varphi/d\lambda$. All in all, $\mathcal{P}(\lambda)$ writes

$$\mathcal{P}(\lambda) = \mathcal{P}_{\varphi}(\varphi) \frac{1}{\cos^2 \lambda (-d^2 \ln \rho / d\varphi^2)}.$$
(8)

This expression is common for both the MC axis and the shock, as $\mathcal{P}_{\varphi}(\varphi)$ can then be replaced by its proper expression from equation (6) or equation (7). Since φ can be expressed as a function of λ with equation (4) when $\rho(\varphi)$ is specified, $\mathcal{P}(\lambda)$ in equation (8) can be written as a function of λ .

A quantitative comparison between two probability distribution functions, with one corresponding to the real shape \mathcal{P}_{real} (i.e., estimated from observations) and the other corresponding to a given synthetic model \mathcal{P}_{model} , can be done by computing the distance between the two probability curves, as follows:

dist(real, mod.) =
$$\sqrt{\frac{1}{90} \int_{0}^{90} \left(\mathcal{P}_{\text{real}}(\lambda) - \mathcal{P}_{\text{model}}(\lambda) \right)^2 d\lambda}$$
. (9)

With a given analytical model of $\rho(\varphi)$ for the MC/shock shape, equation (8) provides a continuous function of λ . However, since the observed probabilities are binned, the comparison requires to also bin the probability obtained from the synthetic model (the probability function of this binned model is then noted $\mathcal{P}_{bmod}(\lambda)$). Then, equation (9) is transformed into

diff(obs., mod.) =
$$\sqrt{\frac{1}{n_b} \sum_{i=1}^{n_b} \left(\mathcal{P}_{obs}(\lambda_i) - \mathcal{P}_{bmod}(\lambda_i) \right)^2},$$
 (10)

where $n_{\rm b}$ is the number of bins of the observed probability $\mathcal{P}_{\rm obs}$.

3.2. Wood's Model

We first start our investigation of the most appropriate synthetic model with the Wood's model. In a series of papers, Wood and coauthors used images from both STEREO spacecraft to visually fit the ICME front and/or the leading and trailing edges of flux ropes with the following model:

$$\rho_{\rm w}(\varphi) = \rho_{\rm max} \exp(-|\varphi/\sigma|^{\alpha}/2). \tag{11}$$

The parameter σ defines the azimuthal extension and α characterizes how flat the apex is [see *Wood et al.*, 2009a; *Wood and Howard*, 2009; *Wood et al.*, 2010, 2011, 2012].

With a cylindrical rotation, equation (11) defines a surface, and *Wood et al.* [2009a] set a thin shell of density around it to model the bright front of ICMEs. Then, Wood et al. computed synthetic images by simulating the Thomson scattering. The comparison with the observed COR and HI images of ICMEs observed by both STEREO spacecraft leads to the determination by visual inspection of the best values for σ and α . The results are ICME case dependent with σ in the interval [25°, 43°] and α in [2, 3.3].

Wood et al. [2009a] also used equation (11) to define a density shell model around a flux rope, as follows. They first defined the flux rope leading and trailing edges with equation (11) and with two sets of σ and α values. Then, they defined a flux-rope-like boundary with an elliptical (or circular) cross section passing through these two edges. Finally, they included a density layer around the cross-section boundary. The visual fit of the simulated brightness images with both STEREO data determines the best parameter values. The resulting σ values are in the interval [21°, 40°] and the α values in [2, 8]. Wood et al. [2009a] did not explicitly model the axis of the flux rope, but since its shape is between the leading and trailing edge shapes, we show below the same range of σ and α parameters for the axis as quoted above.

In order to derive the statistical properties for the in situ data implied with the Wood's model, defined by equation (11), we apply below the equations derived in section 3.1. Then, tan λ is obtained from equation (4):

$$\tan \lambda = \alpha \, \sigma^{-\alpha} \varphi^{\alpha-1} / 2 \,. \tag{12}$$

For the shape to not be sharp at the apex, i.e., $\lambda = 0$ for $\varphi = 0$, the condition $\alpha > 1$ should be satisfied. Next, since tan λ is a monotonously growing function of φ , the inversion of equation (12) provides

$$\varphi_{w}(\lambda) = \left(\frac{2\sigma^{\alpha} \tan \lambda}{\alpha}\right)^{1/(\alpha-1)}.$$
(13)

The profile of equation (11) has no physical meaning for large $|\varphi|$ values, i.e., for very small ρ values (as the shape would spiral around its origin). We then set a minimum value $\rho > \rho_{\min}$, which implies $|\varphi| < \varphi_{\max}$ and $\lambda < \lambda_{\max}$ with

$$\varphi_{\max} = \sigma \left(2 \ln \frac{\rho_{\max}}{\rho_{\min}} \right)^{1/\alpha}, \tag{14}$$

$$\lambda_{\max} = \tan^{-1} \left(\alpha \, \sigma^{-\alpha} \varphi_{\max}^{\alpha - 1} / 2 \right). \tag{15}$$

In Figure 5 we selected $\rho_{min} = 0.2$ AU and $\rho_{max} = 1$ AU, which implied λ_{max} ranging from 74° to 87° for α ranging from 2 to 8. The shape defined by this model, equation (11), is shown in Figure 5 (left) with different colors for four values of α (= 2, 4, 6, 8). With the same colors, the corresponding probabilities of λ for the axis and the shocks, equation (16) below, are shown in Figures 5 (middle) and 5 (right), respectively. These theoretical results are compared with the observed probability drawn with histograms for MCs analyzed by Lepping and Wu and for shocks analyzed by Wang et al., respectively.

The probability $\mathcal{P}(\lambda)$ is computed from equation (8), where φ is replaced with equation (13), so that the final expression is expressed as a function of λ :

$$\mathcal{P}_{w}(\lambda) = \frac{\mathcal{P}_{\varphi}(\varphi_{w})}{\alpha - 1} \left(\frac{2\sigma^{\alpha}}{\alpha}\sin^{2-\alpha}\lambda\,\cos^{-\alpha}\lambda\right)^{1/(\alpha - 1)},\tag{16}$$

with $\mathcal{P}_{\varphi}(\varphi_w)$ defined by equation (6) or equation (7). Since $\alpha > 1$, $\alpha/(\alpha - 1) > 0$ and $\mathcal{P}_w(\lambda)$ are always growing to infinity as λ approaches 90° (infinite branch). If one restricts φ to the interval $[0, \varphi_{max}]$, $\lambda < \lambda_{max} < 90^{\circ}$ so that the singularity disappears in $\mathcal{P}_w(\lambda)$. However, $\mathcal{P}_w(\lambda)$ remains a sharply growing function of λ for large λ values, and this behavior starts at lower values of λ for low values of α (see the curves in Figures 5 (middle) and 5 (right)). $\mathcal{P}_w(\lambda)$ is also singular at $\lambda = 0$, again with an infinite branch, for $\alpha > 2$ for the MC axis case (Figure 5, middle) and for $\alpha > 3$ for the shock case (Figure 5, right). This behavior is due to the relationship between λ and



Figure 5. Shapes and probabilities per unit λ , in degree, for the Wood's model (section 3.2). (left) The MC axis or the cross section of the shock in a plane including the Sun (located at the origin) and the axis/shock apex, as defined by equation (11) and limited to $\rho > \rho_{min} = 0.2$. The colored lines are for four different values of the α parameter. The corresponding probabilities of λ are shown together with, in the background, the observed probability drawn with histograms (middle) for MCs analyzed by Lepping and Wu and (right) for shocks analyzed by Wang et al. The large differences between the colored lines representing Wood's model and the histograms from the observed distribution show that the model is not consistent with the observations.

 φ as shown in Figure 6 for two σ values (panels) and four α values (color curves). For low and large values of λ , the curves are flat. With a uniform distribution of φ , this implies a larger accumulation of cases with similar λ where the curve is more horizontal, so a larger probability $\mathcal{P}(\lambda)$ for MC axis and shocks.

The above properties of $\mathcal{P}_{w}(\lambda)$ imply strong differences with the observed probabilities of the location angle for both the MC axis and the shock normal (Figure 4). This is shown in Figures 5 (middle) and 5 (right), where the observed λ probabilities for both MC axis and shocks, deduced from lists of MC/shock events, are put in the background for comparison (light blue histograms). The probability curves for the synthetic model of *Wood et al.* [2009a] are computed with the parameter α in the range deduced from STEREO observations. A similar behavior is found for all σ values, as illustrated with the evolution of $\lambda(\varphi)$ with two values of σ in Figure 6. As σ increases, φ extends on a broader interval, while $\lambda(\varphi)$ keeps a similar shape implying similar $\mathcal{P}_{w}(\lambda)$.

As such, Wood's model, as described by equation (11), is too blunt around the apex, then too tightly curved on the flanks and again too flat in the legs/flanks to provide a satisfying evolution of $\mathcal{P}_w(\lambda)$ comparable with in situ observations. Even scanning the most appropriate range of α (within [2, 4]), for which $\mathcal{P}_w(\lambda)$ is less singular, does not provide a probability distribution comparable to any of the observed distributions (Figure 4). Indeed, the differences between the model and the observations always remain of the order of the mean probability value (diff ≈ 13 to 33×10^{-3} with diff defined by equation (10)).

We conclude that the description of the axis and the shock shapes by equation (11) does not provide any probability distribution compatible with the statistical in situ results. At first sight, the shapes shown in Figure 5 (left) are not too far from the typically expected shape (e.g., as shown in Figure 1b and as observed







Figure 7. Shapes and probabilities per unit λ , in degree, for the cosine model (section 3.3). (left) The MC axis or the cross section of the shock, as defined by equation (17), for different values of the *n f* parameter. The corresponding probabilities of λ are shown together with, in the background, the observed probability drawn with histograms (middle) for MCs analyzed by Lepping and Wu and (right) for shocks analyzed by Wang et al. The colored lines show that the cosine model is the most consistent with the observed probability distributions for the case with *n f* \approx 0.3.

by STEREO). However, $\mathcal{P}(\lambda)$ is a very sensitive function as it contains a second derivative of the shape (equation (8)). It implies that, even with limited statistics, the observed probabilities $\mathcal{P}(\lambda)$ provide strong constraints on the axis and shock shapes.

3.3. Cosine Model

Other analytical models can be used to study the properties of the statistical distributions of parameters for both shocks and MC axis. For example, a simple analytical model was introduced by *Janvier et al.* [2014a] to describe the mean shape of shocks:

$$\rho_c(\varphi) = \rho_{\max} \cos^n(f\varphi), \qquad (17)$$

with $f = 90^{\circ}/\varphi_{max}$ so that $\rho(\varphi_{max}) = 0$. This model can similarly describe the shape of the MC axis. In the following, we refer to this model as the cosine model, and all relevant parameters are denoted with a subscript "c." The shape defined by the cosine model is shown in Figure 7 (left) for five values of the product nf, with nf the product between n and f, the most sensitive degree of freedom in this model.

For an apex fixed at a given distance, e.g., 1 AU (where the Wind and ACE spacecraft are located), this model has only two parameters (as the Wood's model): $\{n, f\}$ or equivalently $\{nf, \varphi_{max}\}$. Computing d ln $\rho_c/d\varphi$ and inverting equation (4) allows to express φ_c explicitly as a function of λ :

$$\varphi_c(\lambda) = \frac{1}{f} \tan^{-1} \left(\frac{\tan \lambda}{nf} \right) \,. \tag{18}$$

The probability $\mathcal{P}_{c}(\lambda)$ of equation (8) is explicitly computed by including a second derivation of d ln $\rho_{c}/d\varphi$. Eliminating φ with equation (18), the expression for $\mathcal{P}_{c}(\lambda)$ is rewritten as

$$\mathcal{P}_{c}(\lambda) = \mathcal{P}_{\varphi}(\varphi_{c}) \frac{n(1 + \tan^{2} \lambda)}{(nf)^{2} + \tan^{2} \lambda}.$$
(19)

With φ_c expressed with equation (18), $\mathcal{P}_c(\lambda)$ becomes an explicit function of λ .

The probability $\mathcal{P}_{c}(\lambda)$ is strongly dependent on the product nf as shown in Figure 7 for the axis and the shocks in Figures 7 (middle) and 7 (right), respectively, with the same color convention than for the shapes (Figure 7, left). Values of $nf \geq 0.5$ give $\mathcal{P}_{c}(\lambda)$ functions that are too flat compared with the observed probabilities (as reported in the background for both MC axis and shock normal). This is especially true for the shocks, since the observed decrease of $\mathcal{P}(\lambda)$ for large λ is not reproduced for $nf \geq 0.5$ (e.g., the blue curve for nf = 0.7 is monotonously increasing). On the contrary, values $nf \leq 0.25$ imply that the $\mathcal{P}_{c}(\lambda)$ functions are too peaked near the origin compared with the observations (e.g., the black curve for nf = 0.2). Furthermore, we found the same constraints on nf by comparing the cosine model to the other observed probabilities (e.g., those shown in Figure 4). It implies that the nf values compatible with observations are located in a narrow interval [0.25, 0.5]. This corresponds to a well-constrained shape as shown in Figure 7 (left), in between red and pink shapes, because a large modification of $\mathcal{P}_{c}(\lambda)$ implies only a small deformation of the shape.

We quantify the above results by minimizing the least squares difference between the observation and model distributions, so minimizing the function "diff" defined in equation (10) for each observed probability. This

Observations		Cos.	Cos. Mod.		Ellip. Mod.	
Data Set	N _{case}	nf	diff ^a	b/a	diff ^a	
Results With MC Axis						
Lepping and Wu, all	107	0.36	4.5	1.28	4.1	
Lepping and Wu, quality 1,2 ^b	74	0.36	6.9	1.25	6.4	
Lynch et al.	132	0.50	5.0	1.10	4.4	
Feng et al., axis	62	0.34	4.8	1.29	4.5	
Results With Shock Normal						
Feng et al., shock	62	0.40	7.8	1.21	6.9	
Wang, all	216	0.29	4.5	1.39	3.7	
Wang, ICME not detected ^c	99	0.32	6.0	1.32	5.1	
Wang, all ICME	117	0.26	4.4	1.45	3.6	
Wang, nonflux rope ICME	36	0.23	6.1	1.53	5.8	
Wang, MC-like	36	0.23	6.5	1.57	5.8	
Wang, MC	45	0.32	7.8	1.36	7.3	

Table 1. Best Fitted Cosine and Ellipsoidal Models to Various Data Sets

^aThe difference computed with equation (10) and multiplied by 1000.

^bThe quality is defined in *Lepping et al.* [1990] according to the χ^2 value of the fit of a flux rope model to data. Here the two best groups are used.

^cShocks not followed by an ICME. Most of them are thought to be shock flanks which extend beyond the ICME [see *Janvier et al.*, 2014a].

provides the best parameters n f and φ_{max} . In fact, φ_{max} has a very weak effect on $\mathcal{P}_{c}(\lambda)$ [Janvier et al., 2014a] so that only the best n f value is determined. The results are summarized in Table 1. For MC axis, n f is almost the same, ≈ 0.35 , for the data of Lepping and Wu [2010] and Feng et al. [2010], while n f is slightly larger, ≈ 0.5 , for Lynch et al. [2005] because its $\mathcal{P}(\lambda)$ has a larger tail for large λ values (Figure 4). For shocks, all the results are clustered around n f = 0.3.

The above results imply that the deduced mean shape of MC axis is nearly independent of the data set selected. This includes partly different MCs (see section 2.4), and more importantly different input in the analyzed procedure from different authors (e.g., the MC axis depends critically on the author's choice of the MC boundaries, [*Dasso et al.*, 2006]). The deduced mean shape of shocks is also very close from the one deduced from the data sets of *Feng et al.* [2010] and *Wang et al.* [2010], while the determined shock normals have significant differences for the same analyzed shock (section 2.4).

3.4. Ellipsoidal Model

The ellipsoidal model was introduced by *Janvier et al.* [2013] to describe the mean shape of the MC axis. Its derivation is less simple than for the above cosine model, although $\mathcal{P}(\lambda)$ can still be derived analytically. The MC axis is described by an ellipse of half size *a* and *b* in the radial and orthoradial directions, respectively (Figure 8). The ellipse center is at a distance *d* from the Sun, and we define a point M on the axis where the spacecraft crosses the structure, situated at a distance ρ_e from the Sun:

$$\rho_e = \sqrt{(d + a\cos\delta)^2 + (b\sin\delta)^2},\tag{20}$$

where δ is the angle defining the position of M from the ellipse center. The azimuthal coordinate, φ_{e} , writes

$$\tan \varphi_e = b \sin \delta / (d + a \cos \delta). \tag{21}$$

These equations, although first defining the MC axis, can similarly describe the shock shape (considering a surface symmetric around the Sun apex line) as a parametric curve $(\rho_e(\delta), \varphi_e(\delta))$. The maximum angular extension of the model, φ_{max} , is defined by

$$\tan\varphi_{\rm max} = b/\sqrt{d^2 - a^2}.$$
(22)



Figure 8. Diagram defining the elliptical model for the flux rope axis or shock shape. M is the point of interest (where the spacecraft crosses the structure). φ_e is the angle of the cylindrical coordinates (φ_e, φ_e). The location angle λ is defined between the normal and the local radial from the Sun. The maximum angular extension φ_{max} is outlined by radial segments tangent to the ellipse. The parameter δ is the angle used to parameterize the ellipse.

For an apex fixed at a given distance, this model has only two parameters similar to the two previous models: a/d and b/d, or equivalently b/a and φ_{max} .

The location angle λ is expressed with equation (4) as follows:

$$\tan \lambda = \frac{a \sin \delta \cos \varphi_e - b \cos \delta \sin \varphi_e}{a \sin \delta \sin \varphi_e + b \cos \delta \cos \varphi_e}.$$
(23)

Both $\varphi_{\rho}(\delta)$ and $\lambda(\delta)$ are monotonously growing functions of δ , then φ_{ρ} is an implicit function of λ .

The derivation of the probability $P_{e}(\lambda)$ requires several computation steps as outlined in *Janvier et al.* [2013]. The result is as follows:

$$\mathcal{P}_{e}(\lambda) = \mathcal{P}_{\varphi}(\varphi_{e}) / |d\lambda/d\varphi|, \qquad (24)$$

with

$$\frac{d\lambda}{d\varphi} = -1 + \frac{1 + \tan^2 \delta}{1 + (a/b)^2 \tan^2 \delta} \frac{a}{b \cos \varphi_e} \frac{d + a \cos \delta}{a \sin \delta \sin \varphi_e + b \cos \delta \cos \varphi_e}$$
(25)

With equations (21) and (23) providing the monotonous functions $\varphi_e(\lambda)$ and $\delta(\lambda)$, $\mathcal{P}_e(\lambda)$ is an implicit single-value function of λ .

We show in Figure 9 (left) the different shapes obtained with such a model for different aspect ratios. We also show the associated probability functions (colored curves) on top of histograms of the observed distributions of λ for both MC axis (Figure 9, middle) and shock normal (Figure 9, right), with the same drawing convention as in Figure 7. For both MC axis and shock normals, the probability function $\mathcal{P}_{e}(\lambda)$ matches the observed $\mathcal{P}(\lambda)$ the best for a value $b/a \approx 1.3$ (green curve). This corresponds to an ellipsoidal shape slightly elongated in the orthoradial direction. Although the parameterized curve does not change much for nearby values, the probability $\mathcal{P}_{e}(\lambda)$ is very sensitive to the parameter b/a as there are large differences from the observed $\mathcal{P}(\lambda)$ for these nearby values, e.g., b/a = 1.1 and 1.5 (red and pink curves, respectively, in Figure 9). Compared to the cosine model, the ellipsoidal model provides an even closer match with the observations, especially for large λ values of the $\mathcal{P}(\lambda)$ function for shock normals (e.g., one can compare the green curves in Figures 7 and 9).

We find the best ellipsoidal description of the MC axis and shock front by using the least squares difference technique (as in section 3.3). In Figure 10, we show how to obtain the best fits for two different samples of MCs and shocks with a pair of plots for each sample. We also show three values of φ_{max} (color curves). For each sample, we show in the left panel of each pair the evolution of the diff value, equation (10), as a function of the



Figure 9. Shapes and probabilities per unit λ , in degree, for the ellipsoidal model (section 3.4). We added a straight sunward edge to the ellipsoidal shape (dashed line) to visualize the maximum extension $\pm \varphi_{max}$ (defined in Figure 1b). (left) The MC axis or the cross section of the shock, as defined by equation (20), for different values of the aspect ratio b/a parameter. The corresponding probabilities of λ are shown together with, in the background, the observed probability drawn with histograms (middle) for MCs analyzed by Lepping and Wu and (right) for shocks analyzed by Wang et al. The comparison between the colored lines and the histograms shows that the ellipsoidal model with $b/a \approx 1.3$ best fits with the observed data.

ellipse aspect ratio b/a. The lowest values of diff correspond to the best fits, and the associated probability functions are then reported on top of the observed probability distribution in the right panel of each pair.

The minimum diff values are all similar for low φ_{max} values (e.g., 15° and 30°) for both MCs and shocks (Figure 10), while they increase for larger φ_{max} values (e.g., 60°). Indeed, the probability of λ is weakly dependent of φ_{max} for low φ_{max} values [*Janvier et al.*, 2013, 2014a], then ICMEs with variable φ_{max} can be analyzed together. However, the probability function evolution, for large φ_{max} values, $\mathcal{P}_{e}(\lambda)$ has a tail too large for $\lambda \geq 60^{\circ}$ values compared with observations (as shown with the green arrows in Figure 10), especially for shocks (Figure 10, bottom, right plot of each pair). As such, within the limits of small statistics for large λ values, large values of φ_{max} are not consistent with the observed probability functions, which indicates that ICME shocks are not typically so spatially broad. This is in agreement with the predominance of solar sources of near-Earth ICMEs close to central meridian (64% are within 20° of central meridian [*Richardson and Cane*, 2010]) as well as with a mean half angular extension of CMEs of 30° estimated from coronagraphic observations from CMEs launched close to the solar limb to minimize the projection effects [*Wang et al.*, 2011].



Figure 10. Minimization of the difference between the observations and the ellipsoidal model (section 3.4). (top) Results for the MC axis using two different samples of MCs and (bottom) shock normal results using two samples of shocks. The difference function is defined by equation (10) and it is plotted as a function of the aspect ratio b/a in the left-hand plot of each pair. The results are shown for three values of φ_{max} (equal to $\varphi_{max, axis}$ for MCs and to $\varphi_{max, shock}$ for shocks as defined in Figure 1b). In the right-hand plot of each pair, the probabilities of the best models (i.e., minimizing diff of equation (10)) are shown together with, in the background, the observed probability drawn with histograms. The green arrows show how the tail increases with $\varphi_{max} = 60^{\circ}$. The main result is that the deduced shape, characterized by b/a minimizing the difference function, is almost independent of φ_{max} for low values (< 60°), while for larger φ_{max} value the ellipsoidal model is farther away from observations.



Figure 11. (Half) Shapes and probability distributions of (top) MC axis and (bottom) shock front deduced from observations with various dispersions of the MC axis and shock normal. The observed probability (histogram, *Feng et al.* [2010]) is deconvoluted with a Gaussian kernel, equation (A1), with a standard dispersion $\sigma_d = 10^\circ$ for MC and $\sigma_d = 14^\circ$ for shocks (derived from Figure A1, see section 1). The resulting curve is plotted as a blue curve, rather than a histogram, for superposition. The other curves are the results of a further convolution by a Gaussian kernel with a standard dispersion σ_c . The red curves have $\sigma_c = \sigma_d$ resulting only in a smoothing of the original histogram. The green and pink curves have $\sigma_c > \sigma_d$ resulting in a broadening of the original histogram. The main result is that the deduced MC axis and shock shapes are weakly affected by the errors on λ even when these errors are enhanced by a factor 3 compared with the estimations from observations (Figure A1).

The best b/a values are summarized in Table 1 for $\varphi_{max} = 30^{\circ}$. In all cases a lower minimum diff value is found for the ellipsoidal model, confirming the conclusion drawn above from Figures 7 and 9 that the ellipsoidal model is a better fit than the cosine model. For MC axis, b/a is close to 1.3 except for the data of *Lynch et al.* [2005] with $b/a \approx 1.1$, indicating a slightly more bent shape. For the shock normal, the value of b/a that fits the best with observations is around 1.4, except for the data of *Feng et al.* [2010] for which $b/a \approx 1.2$, indicating also a slightly more bent shape. These variations of b/a are comparable to the uncertainty of $b/a \approx \pm 0.1$ for both MC axis and shock normals as indicated by the minimum region extension of the diff function (Figure 10).

More globally, a comparable shape is expected for the MC axis and the shock surface as the flux rope is only separated from the shock by the sheath (Figure 1b). This is indeed what is found here with both cosine and ellipsoidal models, when their $\mathcal{P}(\lambda)$ is fitted to observations (Figures 7 and 9). This is quite a remarkable result, considering that (1) the in situ data sets and (2) the techniques to find the MC axis and shock normal are all different. These comparable results from different types of data provide a strong case for the shape determined by cross-validating the results.

3.5. Robustness of the Derived Axis and Shock Shapes

The λ values deduced for the different samples of MCs and shocks, and analyzed by different authors, show a large dispersion (section 2.4, Figure 2). This seems a priori incompatible with the results above, where similar axis and shock shapes are derived from these various data sets (sections 3.3 and 3.4, Table 1). To understand these results, we investigate the effect of the λ error level in Appendix A for both the axis and the shock normal on the determined shapes.

We investigate the implications of errors on $\mathcal{P}_{obs}(\lambda)$, then on the deduced MC axis and shock shapes. We conclude that, while there are large fluctuations in the λ estimations by different authors for the same events (Figure 2), the observed probability distributions $\mathcal{P}_{obs}(\lambda)$ are less affected by these errors because of the averaging implied when building a histogram. Furthermore, the deduced axis and shock shapes are even much less affected by these errors because they depend only on the global properties of the histograms. Indeed,

increasing the estimated dispersion, σ_c , by up to a factor 3 only has a weak effect on the deduced shapes (Figure 11, left, the same color being used for the same case on corresponding left and right plots of a panel pair). Moreover, the deconvolution of $\mathcal{P}_{obs}(\lambda)$ by a Gaussian kernel sets an upper limit to the standard deviation of the λ errors, up to $\approx 18^{\circ}$ for MC axis and $\approx 8^{\circ}$ for shock normals. Within such limits, the deduced MC axis and shock shapes are not significantly influenced by the error level on λ .

The above results contrast with the results of *Feng et al.* [2010] who compared the MC axis and shock normal directions directly with each MC-shock pair. The large errors shown in Figure 2 do not allow to derive meaningful results from this direct approach. However, with the same data set, we can perform a statistical analysis and derive the generic MC axis and shock shape as shown above.

4. Summary of the Main Results

In the present paper, we propose an original statistical study based on different catalogs of flux ropes and shocks observed in situ. We compare different analytical models to derive and quantify the most probable generic flux rope axis and shock shape. While in situ data provide only local information along the space-craft trajectory crossing an MC/shock, our method combines the information from large sets of events to statistically derive global information on their generic shape.

Our study is based on a series of papers reporting fitted parameters associated with flux ropes inside magnetic clouds [*Lynch et al.*, 2005; *Feng et al.*, 2010; *Lepping and Wu*, 2010] as well as parameters associated with properties of shocks driven by ICMEs [*Feng et al.*, 2010; *Wang et al.*, 2010]. While the FR fits are all made with the Lundquist model, and the shocks with the MHD Rankine-Hugoniot relations, differences in their application lead to a dispersion of the deduced parameters for the same events (section 2.4, Figure 2). This dispersion is more important for the location angle λ , which defines the location of the spacecraft crossing the interplanetary structure (see Figure 1b for the definition of λ). However, the probability distributions of observed λ have comparable behavior for all data sets (decreasing function for the MC axis and a Gaussian-like distribution peaking around $\lambda \sim 30^{\circ}$ for shock normals, see Figure 4).

We then compared the observed distributions with those obtained from three synthetic models for the MC axis and shock fronts: the Wood's [from *Wood et al.*, 2009b]), cosine [*Janvier et al.*, 2014a], and ellipsoidal [*Janvier et al.*, 2013] models. We investigated the different analytical distribution functions $\mathcal{P}(\lambda)$ for each model, by varying the shape of the MC axis/shock. We scanned the range of possible parameter values for each model and we determine the best model parameters by computing the difference between the distribution function $\mathcal{P}(\lambda)$ with each observed distribution $\mathcal{P}_{obs}(\lambda)$.

The Wood's model was developed to analyze imager data of CMEs obtained from three view points (the two STEREO and SOHO spacecraft). While this model provides axis/shock shapes which at first look plausible, its derived probability function of λ , $\mathcal{P}_w(\lambda)$, is incompatible with all the observed distributions, $\mathcal{P}_{obs}(\lambda)$, of MC axis and shock for all the range of parameters derived by fitting this model to imager data (Figure 5). Also, this model has a too flat shape at the apex, which would indicate that most magnetic clouds and shocks would have been crossed at a low λ , which is not the case. Then, these differences are intrinsic to the model rather than to the specific CME cases studied with the imaging instruments and cannot also be accounted as the result of an evolution of the shape from the inner heliosphere to 1 AU.

By contrast to the Wood's model, both the cosine and ellipsoidal models are able to reproduce the observations, $\mathcal{P}_{obs}(\lambda)$, within a narrow range of parameter values (Figures 7 and 9). Still, the ellipsoidal model provides the best fit for both the λ distribution for MC axis and shock normals for all data sets (section 3.4). The best ellipsoidal shape is obtained for an aspect ratio $b/a \sim 1.2$ for the MC axis and $b/a \sim 1.3$ for the shock normal. This is quite a remarkable result, first, because it allows us to define the quantitative generic shape of the MC axis and the shock front, and second, because it shows that both structures have a similar shape, while MC and shock data are independent.

Moreover, although the observed probability distributions $\mathcal{P}_{obs}(\lambda)$ have some differences from one sample of MC/shock to another (Figure 4), the results of the ellipsoidal and cosine models are close for different data sets (Figure 10 and Table 1), confirming that the derived shapes of axis/shock is weakly dependent on the details of $\mathcal{P}_{obs}(\lambda)$. Indeed, for any model, $\mathcal{P}(\lambda)$ is a very sensitive function of the axis/shock shape as it contains a second derivative of the shape (equation (8)). This implies that the global behavior of $\mathcal{P}(\lambda)$ defines precisely the generic shape of MC axis/shock.

We investigated the reason for such weak dependence on the MC axis/shock shapes, by analyzing the effect of statistical errors introduced in $\mathcal{P}_{obs}(\lambda)$. We found, in particular, that different levels of errors introduced moderate modifications of the probability distributions while the modifications of the axis/shock shape are minor (Figure 11). Indeed, a significant change of the shapes would require a large modification of $\mathcal{P}_{obs}(\lambda)$, as shown in Figures 5, 7, and 9. We conclude that the observed distributions $\mathcal{P}_{obs}(\lambda)$ set a strong constraint on the generic axis/shock shapes.

5. Conclusions and Implications

We have derived the generic shape of MC axis and ICME shocks from different published catalogs of events computing the MC axis or shock normal from in situ data. The MC fits are all made with the Lundquist model, and the shocks are analyzed with the MHD Rankine-Hugoniot relations. Both methods have their own limitations. However, these catalogs have presently the largest number of studied cases compared with other techniques. Moreover, our statistical methods developed to deduce the shapes of these structures can be applied to any other data samples that provide the MC axis and/or the shock normals. This is a further motivation to extend other catalogs.

Deriving generic shapes for the MC axis and shocks has several implications. First, they could be used in analysis of imager data with single viewpoint or stereoscopic observations, as follows. Presently the imager data of ICME require a model in order to derive physical properties such as the velocity and the direction of propagation. Past studies were derived with simple models (the CME front is either supposed to have a negligible extension, or to be spherical around the Sun or attached to it, or to be described by Wood's model). However, the results are sensitive to the model selected [e.g., Möstl et al., 2014]. We propose the ellipsoidal model, derived from our statistical results, as an alternative model to analyze imager data. Nonetheless, with this elliptical model, it is possible to generalize the equations derived by Davies et al. [2013] for a detached spherical model to an ellipsoidal model of the ICME front. Introducing a more elaborated model implies more free parameters which are not necessarily constrained by imager data. However, the in situ data constrain well the aspect ratio b/a of the model to a narrow range of values, then they provide a reference case for application to imager data.

A second implication of our results is for forecasting ICME arrival times at Earth. The arrival time depends on the solar launch time, the velocity history of the ICME front during the transit and also on the shape of the front for ICMEs impacting Earth away from their apex. This last effect can provide delays up to 2 days as shown by Möstl and Davies [2013] with a circular front. Introducing an ellipsoidal shape could be important away from the apex to better define the front position, but also to better determine the ICME trajectory from imager data (previous paragraph), so finally where the front is crossed. Then, the ellipsoidal model is expected to improve our forecast abilities as it provides a step forward in modeling the ICME front shape with constraints derived from in situ data. A first application of this was performed on a very fast ICME observed by seven spacecraft [*Möstl et al.*, 2015]. The deduced aspect ratio, 1.4 ± 0.4 , is comparable to the one deduced above from in situ measurements.

Finally, the present analysis of in situ data can be extended to other solar distances. This requires a consistent set of in situ measurements at different distances away from the Sun. How would the shapes of the MC axis and associated interplanetary shock change with heliodistance? Would the expansion be self-similar for both structures? In that sense, the future missions Solar Probe Plus and Solar Orbiter will be of great interest to advance our knowledge of the evolution of ICMEs in the inner heliosphere.

Appendix A: Effects of Errors on the Derivation of Axis and Shock Shapes

A1. Estimation of the λ Error Distribution

The differences between the λ values obtained by different authors for the same event were analyzed in section 2.4. We quantified the large dispersion of the λ values obtained by different authors (Figure 2) and reported the distribution of the values of the λ differences in Figure A1 with histograms. The mean of this distribution is negligible for MCs ($\approx 1^{\circ}$) and small for shocks ($\approx 7^{\circ}$). The standard deviation is smaller for MCs $(\sigma_{obs} \approx 11^{\circ})$ than for shocks $(\sigma_{obs} \approx 19^{\circ})$. It is remarkable that even with a limited number of common cases (45 MCs and 36 shocks), implying large statistical fluctuations within each histogram bin, both distributions are comparable to a normal (Gaussian) distribution (red curve) with the same mean and standard deviation.



Figure A1. Probability distributions of the difference of λ , in degree, obtained by two author groups studying the same events (left: MCs and right: shocks). The correlation of the λ values are presented in Figures 2 (middle) and 2 (bottom left). A Gaussian function with the same mean and standard deviation is superposed in red. These results are used to estimate the error distribution of λ for MCs and shocks.

We analyze below the implications of λ errors on $\mathcal{P}_{obs}(\lambda)$, then on the deduced MC axis and shock shapes. To do so, we propose to first estimate the error distributions for MCs and shocks and to provide a simple model of the error distribution. Then, we attempt to remove these errors on $\mathcal{P}_{obs}(\lambda)$, and finally, we reintroduce variable level of errors in the newly obtained cleaned distribution to study their implications on the deduced MC and shock shapes.

The errors in the determination of λ are spread in the observed probability distributions of λ (Figure 4). In order to estimate the λ error distribution, we decompose λ as $\lambda = \lambda_{true} + \lambda_{error}$ where λ_{true} is the true λ value and λ_{error} the error due to the limitations of both observations (data only along the spacecraft trajectory) and modeling (boundary selection and fit of the data to a model, see sections 2.1 and 2.2). Considering two samples A and B of common events, we can only access the distribution of $\lambda_{error,A} - \lambda_{error,B}$ (Figure A1) and not the individual distributions of $\lambda_{error,A}$ and $\lambda_{error,B}$ (as we do not know λ_{true}). Since the mean values of the $\lambda_{error,A} - \lambda_{error,B}$ distributions are small (Figure A1), in both for MCs and shocks, there are only weak systematic biases. This small bias can also be observed in Figure 2 (left), with a similar number of cases above or below the identity straight line (brown line) and also by comparing blue (fitted) and brown lines. Next, we assume that $\lambda_{error,A}$ and $\lambda_{error,B}$ are independent statistical variables with the same standard deviation $\sigma_A = \sigma_B$. Since the variance of the difference of two independent variables is the sum of their two variances ($\sigma^2 = \sigma_A^2 + \sigma_B^2$), then $\sigma_A = \sigma_B \approx 8^\circ$, and for shocks $\sigma_A = \sigma_B \approx 14^\circ$. Next, since the distributions of $\lambda_{error,A} - \lambda_{error,B}$ for MCs and shocks are comparable with a normal distribution (Figure A1), we suppose below that the error distribution of each set of observations is a normal distribution of $\sigma_{error,A} - \lambda_{error,B}$ for MCs and shocks are comparable with a normal distribution (Figure A1), we suppose below that the error distribution of each set of observations is a normal distribution with $\sigma = \sigma_{obs}/\sqrt{2}$:

$$P_{\rm err}(\lambda) = \frac{1}{\sigma\sqrt{2\pi}} e^{-(\lambda/\sigma)^2/2}.$$
 (A1)

In this framework, the observed distribution, $\mathcal{P}_{obs}(\lambda)$, is the result of the true distribution, $\mathcal{P}_{true}(\lambda)$, convoluted with $\mathcal{P}_{err}(\lambda)$ (called the kernel of the convolution).

A2. Deconvolution of the Observed Probabilities

The deconvolution of a signal is a delicate problem, in particular, since we only have a crude approximation of the kernel with equation (A1) [*Press et al.*, 1992, chapter 13]. Moreover, there are boundary effects at $\lambda = 0^{\circ}$ and 90°. In order to limit them we take into account the properties of $\mathcal{P}_{obs}(\lambda)$. At $\lambda = 0^{\circ}$, $\mathcal{P}_{obs}(\lambda)$ is maximum for MCs and close to zero for shocks. We keep these properties by imposing a symmetric (antisymmetric) distribution for MCs (shocks), respectively. In the vicinity of $\lambda = 90^{\circ}$, the distributions are small so we fix $\lambda > 90^{\circ}$ with zero values on an interval larger than the kernel used. We compare different techniques of deconvolution present in the Mathematica software (damped least squares, Wiener filter, and total variation). The first one provides the best results since the estimated $\mathcal{P}_{true}(\lambda)$ distribution has less oscillations and the back convolution of the results by the same kernel is closer to the original distribution.

The results of the deconvolution with $\mathcal{P}_{err}(\lambda)$ with a standard deviation σ_d , for both MCs and shocks studied by *Feng et al.* [2010], are shown in Figure 11 with the blue curves on the right panels. For MCs, we round $\sigma_d \approx 8^\circ$

to 10°, closer to the shock value of $\sigma_d = 14^\circ$. The convolution of these results by the same kernel ($\sigma_c = \sigma_d$) are shown with the red curves. They are a smoothed version of the original distributions. Next, the green and pink curves are the result by a convolution larger by 10° and 20°, respectively ($\sigma_c - \sigma_d = 10^\circ$ and 20°). The distributions $\mathcal{P}(\lambda)$ broaden as σ_c is increased, as expected.

A3. Implications for the Derived MC and Shock Shapes

We find the best ellipsoidal model for each distribution, similar to the procedure of section 3.4. While the value of σ_c changes significantly the λ distributions, its effect is small on the derived shapes (Figure 11, left). Indeed, there is almost no difference between the shapes derived from $\mathcal{P}_{obs}(\lambda)$ (histograms) and its deconvoluted version (blue curves). This result could be anticipated from Figure 9 which shows that a large change of $\mathcal{P}(\lambda)$ is needed to have a meaningful change of the derived shape. Indeed, even further convoluting $\mathcal{P}_{obs}(\lambda)$ with a kernel broader by 10° or 20°, so increasing the error on λ , only results in a slightly more bent axis. Quantitatively, for $\sigma_c - \sigma_d = 0^\circ$, 10° and 20° (red, green, and pink curves), we obtain b/a = 1.3, 1.2, and 1.1 for MCs, and b/a = 1.2, 1.1, and 1.0 for shocks, respectively. Comparable results are also found with the cosine model with a weak effect of the λ error magnitude on the parameter nf, then on the deduced shape.

We also explore the effect of a broader kernel for the deconvolution. Increasing σ_d implies a deconvoluted $\mathcal{P}(\lambda)$ with more oscillations. This is a classical result of the deconvolution, with even negative values appearing in a deconvoluted function when the deconvolution kernel is broader than the original function. This is already present for $\sigma_d = 14^\circ$ for shocks in Figure 11 and the probability $\mathcal{P}(\lambda)$ has been represented with the constraint $\mathcal{P}(\lambda) \geq 0$ and a renormalization of the probability to get an integral equal unity. This unphysical negative probability indicates that $\sigma_d = 14^\circ$ is an overestimation of the errors (said differently, with such dispersion on the estimations of λ , $\mathcal{P}_{obs}(\lambda)$ should be broader). With the above results from Figure 11, this further implies that the computed shock shape is weakly affected by errors on λ .

Acknowledgments

We thank the referees for their careful reading and whose comments helped to improve the manuscript. The data used in the present paper are available in Lynch et al. [2005]. Feng et al. [2010], and Lepping and Wu [2010] (also available at http://wind.nasa.gov/mfi/mag_cloud_ S1.html) for the magnetic cloud data sets, and in Fena et al. [2010] and Wang et al. [2010] for the shocks data set. We thank all these authors for making such data publicly available. M.J. acknowledges fundings from the Northern Research Partnership with travel support to the Observatoire de Paris. S.D. acknowledges partial support from the Argentinian grants UBACyT 20020120100220 (UBA), PICT-2013-1462 (FONCyT-ANPCyT), and PIP-11220130100439CO (CONICET). N. L. was funded by grant NNX13AH94G. This work was also partially supported by a 1 month invitation of P.D. to the Instituto de Astronomía y Física del Espacio, and by a 1 month invitation of S.D. to the Observatoire de Paris, S.D. is member of the Carrera del Investigador Científico, CONICET.

Yuming Wang thanks Ian G. Richardson and another reviewer for their assistance in evaluating this paper.

References

- Al-Haddad, N., T. Nieves-Chinchilla, N. Savani, C. Möstl, K. Marubashi, M. Hidalgo, I. I. Roussev, S. Poedts, and C. J. Farrugia (2013), Magnetic field configuration models and reconstruction methods for interplanetary coronal mass ejections, *Sol. Phys., 284*, 129–150, doi:10.1007/s11207-013-0244-5.
- Antoniadou, I., A. Geranios, M. Vandas, M. Panagopoulou, O. Zacharopoulou, and O. Malandraki (2008), Elliptical magnetic clouds and geomagnetic storms, *Planet. Space Sci.*, 56, 492–500, doi:10.1016/j.pss.2007.10.002.
- Burlaga, L., E. Sittler, F. Mariani, and R. Schwenn (1981), Magnetic loop behind an interplanetary shock—Voyager, Helios, and IMP 8 observations, J. Geophys. Res., 86, 6673–6684, doi:10.1029/JA086iA08p06673.
- Cane, H. V. (1985), The evolution of interplanetary shocks, J. Geophys. Res., 90, 191-197, doi:10.1029/JA090iA01p00191.
- Dasso, S., C. H. Mandrini, P. Démoulin, M. L. Luoni, and A. M. Gulisano (2005), Large scale MHD properties of interplanetary magnetic clouds, Adv. Space Res., 35, 711–724, doi:10.1016/j.asr.2005.02.096.
 - Dasso, S., C. H. Mandrini, P. Démoulin, and M. L. Luoni (2006), A new model-independent method to compute magnetic helicity in magnetic clouds, *Adv. Space Res.*, 455, 349–359, doi:10.1051/0004-6361:20064806.

Dasso, S., M. S. Nakwacki, P. Démoulin, and C. H. Mandrini (2007), Progressive transformation of a flux rope to an ICME, Sol. Phys., 244, 115–137, doi:10.1007/s11207-007-9034-2.

Davies, J. A., C. H. Perry, R. M. G. M. Trines, R. A. Harrison, N. Lugaz, C. Möstl, Y. D. Liu, and K. Steed (2013), Establishing a stereoscopic technique for determining the kinematic properties of solar wind transients based on a generalized self-similarly expanding circular geometry, Astrophys. J., 777, 167, doi:10.1088/0004-637X/777/2/167.

Démoulin, P., S. Dasso, and M. Janvier (2013), Does spacecraft trajectory strongly affect detection of magnetic clouds?, Adv. Space Res., 550, A3, doi:10.1051/0004-6361/201220535.

Farrugia, C. J., et al. (2011), Multiple, distant (40°) in situ observations of a magnetic cloud and a corotating interaction region complex, J. Atmos. Sol. Terr. Phys., 73, 1254–1269, doi:10.1016/j.jastp.2010.09.011.

Feng, H. Q., D. J. Wu, and J. K. Chao (2007), Size and energy distributions of interplanetary magnetic flux ropes, J. Geophys. Res., 112, A02102, doi:10.1029/2006JA011962.

Feng, H. Q., D. J. Wu, J. K. Chao, L. C. Lee, and L. H. Lyu (2010), Are all leading shocks driven by magnetic clouds?, J. Geophys. Res., 115, A04107, doi:10.1029/2009JA014875.

Goldstein, H. (1983), On the field configuration in magnetic clouds, in *Solar Wind Five*, edited by M. Neugebauer, pp. 731–733, NASA Conf. Publ., NASA CP-2280, Washington D. C.

Gosling, J. T. (1990), Coronal mass ejections and magnetic flux ropes in interplanetary space, in *Physics of Magnetic Flux Ropes (A92-31201 12-75)*, vol. 58, pp. 343–364, AGU, Washington, D. C.

Gosling, J. T. (2000), Coronal mass ejections, in 26th International Cosmic Ray Conference ICRC XXVI, edited by B. L. Dingus, D. B. Kieda, and M. H. Salamon, pp. 59–79, AIP Conference Proceedings 516, Am. Inst. of Phys., College Park, Md., doi:10.1063/1.1291469

Harrison, R. A., et al. (2008), First imaging of coronal mass ejections in the heliosphere viewed from outside the Sun-Earth line, *Sol. Phys.*, 247, 171–193, doi:10.1007/s11207-007-9083-6.

Hidalgo, M. A. (2003), A study of the expansion and distortion of the cross section of magnetic clouds in the interplanetary medium, J. Geophys. Res., 108(A8), 1320, doi:10.1029/2002JA009818.

Hidalgo, M. A., and T. Nieves-Chinchilla (2012), A global magnetic topology model for magnetic clouds. I, Astrophys. J., 748, 109, doi:10.1088/0004-637X/748/2/109.

Howard, T. A. (2011), Three-dimensional reconstruction of coronal mass ejections using heliospheric imager data, J. Atmos. Sol. Terr. Phys., 73, 1242–1253.

AGU Journal of Geophysical Research: Space Physics

Howard, T. A., and S. J. Tappin (2010), Application of a new phenomenological coronal mass ejection model to space weather forecasting, Space Weather, 8, S07004, doi:10.1029/2009SW000531.

Hu, Q., and B. Dasgupta (2005), Calculation of magnetic helicity of cylindrical flux rope, *Geophys. Res. Lett.*, 32, L12109, doi:10.1029/2005GL023004.

Hu, Q., and B. U. Ö. Sonnerup (2002), Reconstruction of magnetic clouds in the solar wind: Orientations and configurations, J. Geophys. Res., 107(A7), 1142, doi:10.1029/2001JA000293.

Isavnin, A., E. K. J. Kilpua, and H. E. J. Koskinen (2011), Grad-shafranov reconstruction of magnetic clouds: Overview and improvements, Sol. Phys., 273, 205–219, doi:10.1007/s11207-011-9845-z.

Janvier, M., P. Démoulin, and S. Dasso (2013), Global axis shape of magnetic clouds deduced from the distribution of their local axis orientation, *Adv. Space Res.*, 556, A50, doi:10.1051/0004-6361/201321442.

Janvier, M., P. Démoulin, and S. Dasso (2014a), Mean shape of interplanetary shocks deduced from in situ observations and its relation with interplanetary CMEs, Adv. Space Res., 565, A99, doi:10.1051/0004-6361/201423450.

Janvier, M., P. Démoulin, and S. Dasso (2014b), In situ properties of small and large flux ropes in the solar wind, J. Geophys. Res. Space Physics, 119, 7088–7107, doi:10.1002/2014JA020218.

Lepping, R. P., and C. C. Wu (2010), Selection effects in identifying magnetic clouds and the importance of the closest approach parameter, Ann. Geophys., 28, 1539–1552, doi:10.5194/angeo-28-1539-2010.

Lepping, R. P., L. F. Burlaga, and J. A. Jones (1990), Magnetic field structure of interplanetary magnetic clouds at 1 AU, J. Geophys. Res., 95, 11,957–11,965, doi:10.1029/JA095iA08p11957.

Lepping, R. P., D. B. Berdichevsky, A. Szabo, C. Arqueros, and A. J. Lazarus (2003), Profile of an average magnetic cloud at 1 AU for the quiet solar phase: Wind observations, Sol. Phys., 212, 425–444.

Lin, C. C., J. K. Chao, L. C. Lee, L. H. Lyu, and D. J. Wu (2006), A new shock fitting procedure for the MHD Rankine-Hugoniot relations for the case of small He² + slippage, *J. Geophys. Res.*, 111, A09104, doi:10.1029/2005JA011449.

Liu, Y., J. G. Luhmann, K. E. J. Huttunen, R. P. Lin, S. D. Bale, C. T. Russell, and A. B. Galvin (2008), Reconstruction of the 2007 May 22 magnetic cloud: How much can we trust the flux-rope geometry of CMEs?, Astrophys. J., 677, L133–L136, doi:10.1086/587839.

Liu, Y. D., J. G. Luhmann, N. Lugaz, C. Möstl, J. A. Davies, S. D. Bale, and R. P. Lin (2013), On Sun-to-Earth propagation of coronal mass ejections, *Astrophys. J., 769*, 45, doi:10.1088/0004-637X/769/1/45.

Lugaz, N., and I. Roussev (2011), Numerical modeling of interplanetary coronal mass ejections and comparison with heliospheric images, J. Atmos. Sol. Terr. Phys., 73, 1187–1200.

Lugaz, N., A. Vourlidas, I. I. Roussev, and H. Morgan (2009), Solar-terrestrial simulation in the STEREO Era: The 24–25 January 2007 eruptions, Sol. Phys., 256, 269–284, doi:10.1007/s11207-009-9339-4.

Lugaz, N., J. N. Hernandez-Charpak, I. I. Roussev, C. J. Davis, A. Vourlidas, and J. A. Davies (2010), Determining the azimuthal properties of coronal mass ejections from multi-spacecraft remote-sensing observations with STEREO SECCHI, Astrophys. J., 715, 493–499, doi:10.1088/0004-637X/715/1/493.

Lugaz, N., C. J. Farrugia, and N. Al-Haddad (2014), Complex evolution of coronal mass ejections in the inner heliosphere as revealed by numerical simulations and STEREO observations: A review, in *IAU Symposium, IAU Symposium*, vol. 300, edited by B. Schmieder, J.-M. Malherbe, and S. T. Wu, pp. 255–264, Cambridge Univ. Press, Cambridge, U. K.

Lundquist, S. (1950), Magnetohydrostatic fields, Ark. Fys., 2, 361-365.

Lynch, B. J., T. H. Zurbuchen, L. A. Fisk, and S. K. Antiochos (2003), Internal structure of magnetic clouds: Plasma and composition, J. Geophys. Res., 108(A6), 1239, doi:10.1029/2002JA009591.

Lynch, B. J., J. R. Gruesbeck, T. H. Zurbuchen, and S. K. Antiochos (2005), Solar cycle-dependent helicity transport by magnetic clouds, J. Geophys. Res., 110, A08107, doi:10.1029/2005JA011137.

Manchester, W. B. I., T. I. Gombosi, I. Roussev, A. Ridley, D. L. De Zeeuw, I. V. Sokolov, K. G. Powell, and G. Tóth (2004), Modeling a space weather event from the Sun to the Earth: CME generation and interplanetary propagation, *J. Geophys. Res.*, 109, A02107, doi:10.1029/2003JA010150.

Marubashi, K., and R. P. Lepping (2007), Long-duration magnetic clouds: A comparison of analyses using torus- and cylinder-shaped flux rope models, Ann. Geophys., 25, 2453–2477, doi:10.5194/angeo-25-2453-2007.

Matthaeus, W. H., and M. Velli (2011), Who needs turbulence? A review of turbulence effects in the heliosphere and on the fundamental process of reconnection, *Space Sci. Rev.*, 160, 145–168, doi:10.1007/s11214-011-9793-9.

Mierla, M., et al. (2010), On the 3-D reconstruction of coronal mass ejections using coronagraph data, Ann. Geophys., 28, 203–215, doi:10.5194/angeo-28-203-2010.

Möstl, C., and J. A. Davies (2013), Speeds and arrival times of solar transients approximated by self-similar expanding circular fronts, Sol. Phys., 285, 411–423, doi:10.1007/s11207-012-9978-8.

Möstl, C., C. J. Farrugia, H. K. Biernat, M. Leitner, E. K. J. Kilpua, A. B. Galvin, and J. G. Luhmann (2009), Optimized grad-shafranov reconstruction of a magnetic cloud using STEREO-Wind observations, Sol. Phys., 256, 427–441, doi:10.1007/s11207-009-9360-7.

Möstl, C., et al. (2014), Connecting speeds, directions and arrival times of 22 coronal mass ejections from the Sun to 1 AU, Astrophys. J., 787, 119, doi:10.1088/0004-637X/787/2/119.

Möstl, C., et al. (2015), Strong coronal deflection of a solar storm and its interplanetary evolution to Earth and Mars, *Nat. Commun.*, in press. Nakwacki, M., S. Dasso, C. H. Mandrini, and P. Démoulin (2008), Analysis of large scale MHD quantities in expanding magnetic clouds, *J. Atmos. Sol. Terr. Phys.*, *70*, 1318–1326, doi:10.1016/j.jastp.2008.03.006.

Neugebauer, M., and R. Goldstein (1997), Particle and field signatures of coronal mass ejections in the solar wind, in *Coronal Mass Ejections, Geophysical Monograph 99*, edited by N. Crooker, J. A. Joselyn, and J. Feynman, pp. 245–251, AGU, Washington, D. C.

Press, W. H., S. A. Teukolsky, W. T. Vetterling, and B. P. Flannery (1992), Numerical Recipes, Cambridge Univ. Press, Cambridge, U. K. Richardson, I. G., and H. V. Cane (2010), Near-Earth interplanetary coronal mass ejections during solar cycle 23 (1996–2009): Catalog and summary of properties, Sol. Phys., 264, 189–237, doi:10.1007/s11207-010-9568-6.

Riley, P., J. A. Linker, Z. Mikić, D. Odstrcil, T. H. Zurbuchen, D. Lario, and R. P. Lepping (2003), Using an MHD simulation to interpret the global context of a coronal mass ejection observed by two spacecraft, J. Geophys. Res., 108(A7), 1272, doi:10.1029/2002JA009760.

Riley, P., et al. (2004), Fitting flux ropes to a global MHD solution: A comparison of techniques, J. Atmos. Sol. Terr. Phys., 66, 1321–1331, doi:10.1016/j.jastp.2004.03.019.

Rouillard, A. P. (2011), Relating white light and in situ observations of coronal mass ejections: A review, J. Atmos. Sol. Terr. Phys., 73, 1201–1213, doi:10.1016/j.jastp.2010.08.015.

Ruffenach, A., et al. (2012), Multispacecraft observation of magnetic cloud erosion by magnetic reconnection during propagation, J. Geophys. Res., 117, A09101, doi:10.1029/2012JA017624. **AGU** Journal of Geophysical Research: Space Physics

Tappin, S. J., and T. A. Howard (2009), Interplanetary coronal mass ejections observed in the heliosphere: 2. Model and data comparison, Space Sci. Rev., 147, 55–87, doi:10.1007/s11214-009-9550-5.

Thernisien, A., A. Vourlidas, and R. A. Howard (2011), CME reconstruction: Pre-STEREO and STEREO era, J. Atmos. Sol. Terr. Phys., 73, 1156–1165, doi:10.1016/j.jastp.2010.10.019.

Thernisien, A. F. R., R. A. Howard, and A. Vourlidas (2006), Modeling of flux rope coronal mass ejections, *Astrophys. J., 652*, 763–773, doi:10.1086/508254.

Vandas, M., E. Romashets, and S. Watari (2005), Magnetic clouds of oblate shapes, *Planet. Space Sci.*, 53, 19–24, doi:10.1016/j.pss.2004.09.024.

Wang, C., H. Li, J. D. Richardson, and J. R. Kan (2010), Interplanetary shock characteristics and associated geosynchronous magnetic field variations estimated from sudden impulses observed on the ground, J. Geophys. Res., 115, A09215, doi:10.1029/2009JA014833.

Wang, Y., C. Chen, B. Gui, C. Shen, P. Ye, and S. Wang (2011), Statistical study of coronal mass ejection source locations: Understanding CMEs viewed in coronagraphs, J. Geophys. Res., 116, A04104, doi:10.1029/2010JA016101.

Wimmer-Schweingruber, R. F., et al. (2006), Understanding interplanetary coronal mass ejection signatures, Space Sci. Rev., 123, 177–216, doi:10.1007/s11214-006-9017-x.

Wood, B. E., and R. A. Howard (2009), An empirical reconstruction of the 2008 April 26 coronal mass ejection, Astrophys. J., 702, 901–910, doi:10.1088/0004-637X/702/2/901.

Wood, B. E., R. A. Howard, A. Thernisien, S. P. Plunkett, and D. G. Socker (2009a), Reconstructing the 3D morphology of the 17 May 2008 CME, Sol. Phys., 259, 163–178, doi:10.1007/s11207-009-9391-0.

Wood, B. E., R. A. Howard, S. P. Plunkett, and D. G. Socker (2009b), Comprehensive observations of a solar minimum coronal mass ejection with the solar terrestrial relations observatory, Astrophys. J., 694, 707–717, doi:10.1088/0004-637X/694/2/707.

Wood, B. E., R. A. Howard, and D. G. Socker (2010), Reconstructing the morphology of an evolving coronal mass ejection, *Astrophys. J.*, 715, 1524–1532, doi:10.1088/0004-637X/715/2/1524.

Wood, B. E., C. -C. Wu, R. A. Howard, D. G. Socker, and A. P. Rouillard (2011), Empirical reconstruction and numerical modeling of the first geoeffective coronal mass ejection of solar cycle 24, Astrophys. J., 729, 70, doi:10.1088/0004-637X/729/1/70.

Wood, B. E., A. P. Rouillard, C. Möstl, K. Battams, N. P. Savani, K. Marubashi, R. A. Howard, and D. G. Socker (2012), Connecting coronal mass ejections and magnetic clouds: A case study using an event from 22 June 2009, *Sol. Phys.*, 281, 369–389, doi:10.1007/s11207-012-0036-3.

Zurbuchen, T. H., and I. G. Richardson (2006), In-situ solar wind and magnetic field signatures of interplanetary coronal mass ejections, Space Sci. Rev., 123, 31–43, doi:10.1007/s11214-006-9010-4.