- 1 The effect of wind and plume height
- ² reconstruction methods on the accuracy
- of simple plume models- a second look at
- the 2010 Eyjafjallajökull eruption

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Abstract

- 16 Real-time monitoring of volcanic ash plumes with the aim to estimate the mass eruption rate
- is crucial for predicting atmospheric ash concentration. Mass eruption rates are usually
- assessed by 0D and 1D plume models, which are fast and require only a few observational
- input parameters, often only the plume height. A model's output, however, depends also on
- the plume height data handling strategy (sampling rate, gap reconstruction methods and
- 21 statistical treatment), especially in long-term eruptions with incomplete plume height records.
- 22 To represent such an eruption, we used Eyjafjallajökull 2010 to test the sensitivity of six
- 23 simple and two explicitly wind-affected plume models against 22 data handling strategies.
- 24 Based on photogrammetric measurements, the wind deflection of the plume was determined
- and used to re-calibrate radar-derived height data. The resulting data was then subjected to
- 26 different data handling strategies, before being used as input for the plume models. The
- 27 model results were compared to the erupted mass measured on the ground, allowing us to
- assess the prediction accuracy of each combination of data handling strategy and model.
- 29 Combinations that provide highest prediction accuracies vary, depending on data coverage,
- 30 eruption intensity, and fragmentation mechanism. However, for this type of moderate-to-
- weak eruption (VEI 3 in terms of maximum intensity), the most important factor was found to
- be the prevailing wind speed. When wind speeds exceed 20 m/s, most combinations of

strategies and models provide predictions that underestimate the erupted mass by more than 40%. Under such conditions, the optimal choice of data handling strategy and plume model is of particular importance.

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Introduction

Volcanic ash injected into the atmosphere during explosive eruptions can pose a serious threat for aviation and air-travel infrastructure (Kienle et al. 1980; Grindle and Burcham 2002). Next to direct observations of the ash cloud (e.g. satellite imagery and lidar retrievals) predictions of movement of volcanic ash clouds are based on atmospheric ash dispersion models (Dacre et al. 2011; Kristiansen et al. 2012; Dioguardi et al. 2016, 2020). Inaccurate predictions can on one hand lead to severe damage to and even loss of aircraft (Guffanti et al. 2010), or the other hand to airport closures framed or perceived as over-cautious (Harris et al. 2012; Harris 2015) and flight diversions or cancellations, which involve large preventable costs (e.g., Brannigan 2011; Macrae 2011; Ragona et al. 2011). This underlines the need for accurate, reliable and confident model forecasts, the lack of which is the current bottle neck in our forecasting capability. Key to achieving such forecasts is thus to be able to provide an ash dispersion model with accurate near-term eruption source parameters, i.e. physical quantities, which characterize the eruptive source. In this regard the most important eruption source parameter is the mass eruption rate (MER) (e.g., Degruyter and Bonadonna 2012; Mastin 2014; Bonadonna et al. 2016), that is the mass flux of the eruptive gas-ash mixture, expressed in kg/s (Wilson and Walker 1987). MER cannot be directly measured. However, methods have been developed that infer MER using observable properties of the plume. These include using video analyses of ash plumes and ejecta (e.g., Wilson and Self 1980; Valade et al. 2014; Dürig et al. 2015b, a; Pioli and Harris 2019; Tournigand et al. 2019), emitted infra-sound waves (Johnson and Ripepe 2011; Ripepe et al. 2013), thermal infrared signatures (e.g., Harris 2013; Ripepe et al. 2013; Harris et al. 2013; Cerminara et al. 2015), electrostatic field (Büttner et al. 2000; Calvari et al. 2012), interpretation of microwave radar signals (Montopoli 2016; Marzano et al. 2020) or satellite-based estimates (e.g., Pouget et al. 2013; Pavolonis et al. 2018; Gouhier et al. 2019; Bear-Crozier et al. 2020). For real-time MER assessment, however many of these approaches are still in an experimental state or struggle with high uncertainties as they often depend on data that are hard to obtain in situ, e.g. the vent geometry (Dürig et al. 2015a). These methods will thus not be considered here. The most straightforward and reliable observable in an explosive eruption is usually the height of the eruptive column H. A number of plume models linking H with the mass eruption rate at the vent have been developed (for in-depth overview see Costa et al. 2016). These range from "simple" theoretical (Wilson and Walker 1987; Woods 1988) and empirical OD models (Sparks et al. 1997; Mastin et al. 2009), through explicitly wind-affected steady 1D models (Bursik 2001; Degruyter and Bonadonna 2012; Devenish 2013; Woodhouse et al. 2013; Mastin 2014; de'Michieli Vitturi et al. 2015; Folch et al. 2016; Aubry et al. 2017) to elaborate time-dependent multi-phase models in 2D (Neri et al. 1998) or 3D space (Esposti Ongaro et al. 2007; Suzuki and Koyaguchi 2012; Cerminara et al. 2016). At present, real-time MER assessments must rely on simple 0D and explicitly wind-affected 1D models, which have the advantage of providing fast results (e.g., Sparks et al. 1997; Bursik 2001; Woodhouse et al. 2013). A monitoring system that uses a suite of such models to assess the mass eruption rate in near-real time is the software REFIR (Real-time Eruption source parameters FutureVolc Information and Reconnaissance system) (Dürig et al. 2018; Dioguardi et al. 2020). Simple OD models are limited by initial assumptions, accuracy of measured parameters (plume height and mass) and simplifications on which they are based. To assess the effect of these shortcomings, this

study explores three aspects that might limit the models' accuracies:

- 1. the effect of plume height uncertainties resulting from a stepwise horizontal ground-based radar scanning technique on MER estimates.
- 2. the sensitivity of data handling strategies on model predictions when dealing with incomplete sets of plume height recordings.
- the impact of wind on MER prediction by non-explicitly wind-affected plume models in comparison to the impact of using different data handling strategies.

The term "data handling strategies" refers to the statistical treatment of plume height data before it is used as a model input. Note that with "plume height" we refer to the maximum elevation of the plume above vent, unless stated otherwise. Since plume height H and mass eruption rate Q are related in a highly non-linear way, the time-averaged mass eruption rate $\overline{Q(t)}$ is in most cases not identical to Q resulting from using the time-averaged plume height $\overline{H(t)}$ as input. Thus:

$$\overline{Q(t)} \neq Q(\overline{H(t)}) \tag{1}$$

Although rarely acknowledged, this fact implies that not only the plume height *H* itself, but also the time interval over which it is measured, as well as the statistical strategy for its assessment, are expected to affect a model's outcome.

In our model sensitivity study, we focus on the 2010 Eyjafjallajökull (Iceland) eruption. This event featured a wind-affected plume (Gudmundsson et al. 2012), which was monitored by a stepwise horizontally scanning radar. The resulting plume height records were incomplete (Arason et al. 2011).

The 2010 Eyjafjallajökull eruption therefore represents an ideal test case for the exploration of the

99 three aspects mentioned above.

The Eyjafjallajökull 2010 eruption

101 The 2010 eruption of Eyjafjallajökull had four phases of activity.

- Phase I: lasting from 14 April 2010 until noon of 18 April, was an initial explosive phase with phreatomagmatic activity (Gudmundsson et al. 2012; Dellino et al. 2012).
 - Phase II: (second half of 18 April 4 May) was a phase of low discharge that was effusive with relatively weak but sustained explosive activity (Gudmundsson et al. 2012).
 - Phase III: (5 17 May) saw a significant increase of explosive activity, coinciding with a change in melt composition from benmoreite to trachyte (Gudmundsson et al. 2012). This phase was characterized by the emission of distinct explosive ash pulses (Dürig et al. 2015b, a) and is often referred to as "second explosive phase" (Gudmundsson et al. 2012; Dellino et al. 2012).
 - Phase IV: (18 22 May) was characterized by a decline in eruption activity and plume height.
 Although the end of eruption is set on 22 May, minor isolated explosive events occurred on
 4-8 June 2010 (Gudmundsson et al. 2012). No ash plumes were detected on radar after
 10:20 UTC on 21 May, when the plume fell below the detection limit of 2.5 km (Arason et al.
 2011).

The eruption's fallout was measured in considerable detail at about 400 locations in Iceland (Gudmundsson et al. 2012), allowing us to compare model predictions on the erupted mass with the actual amount of mass deposited as tephra. For the part of the tephra that fell into the ocean south and southeast of Iceland a considerable uncertainty exists, but the magnitude of this component can nevertheless be estimated using well-established thinning behaviour of tephra layers with distance (e.g., Thorarinsson 1954; Pyle 1989; Fierstein and Nathenson 1992). On 14-16 April, during phase I, westerly upper-tropospheric winds prevailed, changing to northerly winds by 17 April, directing the plume to the south (Gudmundsson et al. 2012). As a result, the erupted mass could be assessed separately as phases *Ia* and *Ib* (see Table 1).

The monitoring conditions of this eruption are classified as relatively challenging since it is a moderate-to-weak eruption that took place under adverse weather conditions (frequent clouds at low and medium altitudes and strong wind) (Arason et al. 2011; Gudmundsson et al. 2012; Björnsson et al. 2013), which meant direct observations of the volcanic plume were often not possible.

129 Data

130 The data used in this study are:

- 131 i) Plume height obtained by the Icelandic Meteorological Office (IMO) from the C-band 132 radar in Keflavík (Arason et al. 2011).
 - ii) Plume height as measured from photographs taken from inspection aircraft (Figure 1).
 - iii) Plume height as measured on photographs taken from the ground from areas to the west of the volcano.
 - iv) Wind speed and direction at plume-relevant altitudes retrieved either from ERA5 or ICRA. ERA5 is a global reanalysis product by the European Centre for Medium-Range Weather Forecasts with a horizontal resolution of 30 km (Hersbach et al. 2020). ICRA is a local reanalysis product by the Icelandic Met Office over Iceland, using the non-hydrostatic numeric weather prediction model HARMONIE-AROME with a horizontal resolution of 2.5 km (Nawri et al. 2017; Schmidt et al. 2018). Both models have a temporal resolution of 1h. Since ICRA data were only available up to an altitude of 6 km a.s.l., we used composite data sets for the ICRA labelled wind speed profiles: ICRA reanalysis data below 6 km, and ERA5 reanalysis data above.

Radar data

Located at 155 km distance from the vent, the C-band radar at Keflavík airport, was the only weather radar operating in Iceland at the time of the eruption. The radar's sampling strategy was to scan at vertical angles of 0.5°, 0.9°, 1.3°, 2.4°, 3.5°, 4.5° and 6° (Arason et al. 2011). The width of the beam was 0.9° providing some overlap between scans. For Eyjafjallajökull, the vertical distance between the beams of the lowest scanning angles was about 1.1 km and about 3 km between 1.3° and 2.4°. For a target above the volcano, this leads to a stepping in the plume height records, with preferential sampling at about 2.5, 3.9, 5.0 and ~8 km height above sea level (for details see Arason et al., 2011).

Photos

The monitoring of vent activity and visual observations of plume behaviour took place on inspection flights (see Fig. 1; for complete list of surveillance flights, see Appendix. 6.3 in Thorkelsson et al. (2012)). For flights where the aircraft location was recorded with GPS, it was possible to determine the position of the camera at the time of a photo with an accuracy higher than 1 km (Gudmundsson et al. 2015). This is the maximum error in the distance between aircraft and the volcanic vents, or any other reasonably well-defined target.

In most cases the plume was bent over by the wind, and its bearing was usually obtained from the position of the aircraft when it was upwind and in line with the plume. Occasionally this was also done by flying along the plume and determining the location relative to known landmarks. Errors in distance to the top of the plume were in this way contained within 1 km in most cases, and less than 2 km in all cases. In the vast majority of cases this amounted to 5-10% of the distance.

The height of plume was either assessed directly by using the altimeter of the plane (Fig. 1d) or calculated using the Python software Pixelcalc (Magnússon 2012). The plume top was referenced by triangulation, using photos of the plume taken in short time intervals from different angles. Given a known camera-target distance Pixelcalc converts distances between two points on the photo to actual 3D distances at the location of the target by using the lens and camera specifications, which are derived from the photo's metadata. The software corrects for Earth's curvature at distances where it becomes significant. In most cases the plume height is obtained by measuring the distance on the photo between the plume top and the surface, taking into account plume deflection by wind and surface elevation under the plume top, to obtain height above sea level. In some cases, where data on cloud top height are available, height over clouds (i.e., the distance between cloud top and plume top) is determined. Such cloud heights are in some cases obtained by direct observation using aircraft altimeter or through independent cloud height measurement using Pixelcalc. The uncertainties of the heights and horizontal deflection distances vary from one photo to another, depending on the uncertainties in distances, pixel size and image geometry. Assuming maximum errors for these parameters, we found the uncertainties of plume height and deflection to be less than 0.5 km.

In addition to the airborne imagery, photographs taken on the ground were used. For these the location of the camera is accurately known which allowed us to calculate the distance to the plume top. Independent information of plume azimuth was used to correct for plume top deflection relative to vents.

The total number of photos taken on inspection flights are counted in thousands. Not all flights provided photos that allow reliable determination of plume height, e.g., due to cloud cover. Only the photos best suited for analysis were used, yielding in total 165 observations of plume heights, covering 17 of the 38 eruption days examined. From these photos, 148 were taken in the air, and 17 on the ground. In 85 cases these photos could also be used to assess the plume deflection (i.e., the horizontal shift of the plume top towards the vent location).

Methods

192 Models

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For estimating the MER, we used six *simple* (non-explicitly wind-affected) plume models and two wind-affected models, which are for simplicity referred to by the name of their first authors:

• Wilson (Wilson and Walker, 1987) - a theoretical model based on the theory of buoyant plumes by Morton et al. (1956) which estimates the mass eruption rate Q by:

$$Q_{Wilson} = (H/c)^4 (2)$$

- where H denotes the plume height (in m) and c is a constant which is 236 m (s/kg) $^{1/4}$.
- 199 To the group of non-explicitly wind-affected numerical models tested in this study we include three
- derivatives of the Wilson model, which use Eq. (2), but with different constants c based on empirical
- data from plumes with basaltic or andesitic tephra. They are referred to as:
- Wehrmann (Wehrmann et al. 2006), which uses for c a value of 295 m(s/kg) $^{1/4}$.
- Scollo (Scollo et al. 2007), using 247 m(s/kg)^{1/4} for c.
- Andronico (Andronico et al. 2008), for which 244 m(s/kg)^{1/4} is selected for c.
- Two empirical models were used, which are based on correlations between plume height during
- 206 eruption and the quantity of tephra found in deposits:
- Sparks (Sparks et al., 1997) an empirical model which approximates Q by:

$$Q_{Sparks} = \rho \cdot (H/c)^{3.86} \tag{3}$$

- 209 where ρ is the dense-rock equivalent (DRE) density of the tephra within the plume. Following
- 210 Gudmundsson et al. (2012), a DRE density of 2600 kg/m³ was used for all computations and the
- 211 constant *c* is given by Sparks et al. (1997) as 1670 m(s/kg) $^{1/3.86}$.
- Mastin (Mastin et al., 2009) an empirical model with ρ defined as in (3) which estimates the
- 213 mass eruption rate by:

$$Q_{Mastin} = \rho \cdot (H/c)^{4.15} \tag{4}$$

- where c is given by Mastin et al. (2009) as 2000 m(s/kg) $^{1/4.15}$.
- 216 Since these models are empirically constrained they reflect the influence of the wind on plume-
- 217 height to some degree (Mastin 2014) and can therefore be seen as implicitly wind-affected.
- 218 To juxtapose these simple plume models with explicitly wind-affected models we included two
- 219 examples of the latter category:
 - Woodhouse (Woodhouse et al. 2013) an empirical relationship of a numerical 1D model, which estimates the MER by:

$$Q_{Woodhouse} = \left(\frac{h}{0.318} \cdot \frac{1 + 4.266\widetilde{W}_s + 0.3527\widetilde{W}_s^2}{1 + 1.373\widetilde{W}_s}\right)^{3.953}$$
(5)

where h denotes the centreline plume height (in km) and \widetilde{W}_s quantifies the strength of the wind shear from the ground to a reference height H_1 , according to:

$$\widetilde{\mathcal{W}}_{S} = 1.44 \frac{V_{1}}{\overline{N}H_{1}} \tag{6}$$

with V_1 being the wind speed at H_1 and \overline{N} being the average buoyancy frequency. The latter parameter is determined by:

$$\bar{N}^2 = \frac{1}{h} \int_0^h N^2(z) dz = \frac{1}{h} \frac{g}{C_{a0} T_{a0}} \int_0^h \left(1 + \frac{C_{a0}}{g} \frac{dT_a}{dz} \right) dz \tag{7}$$

- with g, C, and T being the gravitational acceleration, heat capacity and temperature. Parameter z denotes the vertical coordinate above the source, subscript a refers to the atmosphere, and 0 to the volcanic source vent height. Note that a plume's top height H coincides with the elevation of its centreline h only for strong eruptions with vertical ash columns (Mastin 2014), which introduces an error when using H as an input for a weak or moderate eruption. Since for Eyjafjallajökull 2010 the exact conversion from H to h is unknown, for simplicity, in this study we assumed that the centreline height h was always 10% lower than H.
 - Aubry (Aubry et al. 2017): A scaling relationship which uses multiple linear regression to relate the logarithm of the MER to the logarithm of the plume height H (in km), the logarithm of the average buoyancy frequency \overline{N} (eq. (7)), and a windscaling parameter \mathcal{W}_0^* :

$$\log(Q_{Aubry}) = C + C_H \log(H) + C_N \log(\overline{N}) + C_W \mathcal{W}_0^*$$
(8)

where the constants C = 7.4, $C_H = 3.4$, $C_N = 2.3$ and $C_W = 1.1$ are empirically determined. The wind scaling parameter \mathcal{W}_0^* is described by:

$$W_0^* = \frac{W}{U_0} = \frac{W}{1.85\sqrt{Rn_0T_0}} \tag{9}$$

- where W is the horizontal wind speed averaged over the plume height, U_0 is the eruption exit velocity, R=461.5 J/K/kg is the gas constant of volcanic gas at vent, n_0 is the magma volatile content, and T_0 is the exit temperature. Here we assume that n_0 = 3 wt% (Woodhouse et al. 2013) and T_0 = 1323 K for Eyjafjallajökull(Keiding and Sigmarsson 2012).
- For the goals of this study, we put our focus on the simple plume models. These have the advantage that they use plume height as the only independent variable. In their entirety, the six simple models represent the empirical variation of the predictions by the theoretical *Wilson* model. In contrast to simple models, the more sophisticated explicitly wind-affected models depend on additional variables and parameters, (e.g., atmospheric parameters, wind entrainment coefficient, volatile content, magmatic temperature, top vs centreline height) which are further sources of uncertainties that have to be taken into account when analysing the model results.

Plume height data handling strategies 247 248 The radar data set is based on sampling intervals of 5 minutes, but the data set is incomplete (Arason 249 et al. 2011). Reasons for missing data were (Arason et al. 2011): i) 250 The plume was below the visible horizon from Keflavík, which limited the lowest 251 observable plume to 2.5 km. 252 ii) The plume was obscured by precipitating clouds. 253 iii) The radar was malfunctioning. 254 The plume was absent, and the data gap was "real". iv) 255 Here we explore 22 strategies to construct a data set with an improved coverage of the complete 256 eruption (see Table 2). In the example of Figure 2a, a data set was segmented into 3h and 6h static 257 blocks, composed of 36 and 72 bundled five-minute slots, respectively, illustrating how much of the 258 eruption was covered according to the blocks. For example, a data coverage of 50% means for a 6h 259 block that 36 of its 72 entries are missing. In this study, we distinguish between data voids and gaps. 260 Voids are defined as empty or missing 5-minute slots in a block that otherwise contains data. In 261 contrast, a completely empty block of data is called a qap. Figure 2b and c summarize the 3h- and 6h 262 gaps in the radar records of the Eyjafjallajökull 2010 eruption. 263 The tested strategies can be divided into five main categories (see Table 2). Aspects included in the 264 tested strategies are: sampling method, void reconstruction, gap reconstruction, timebase, time 265 steps and a factor introduced to correct for data reduction bias (Y-correction): 266 Static plume height reconstruction (SH) 267 Static plume height reconstruction (SH) strategies bundle data by splitting the data set into static 268 time intervals (blocks) and using plume height averages. The vast majority of studies using plume 269 heights for MER modelling apply SH-strategies. Studies on Eyjafjallajökull used the data by Arason et 270 al. (2011) with blocks typically ranging from 1 h (Woodhouse et al. 2013) to 6 h (Kaminski et al. 2011; 271 Bursik et al. 2012; Mastin 2014). Others report plume heights averaged over eruptive episodes that 272 can include multiple eruptive phases (Aubry et al. 2021). 273 Sampling method: SH strategies applied static sampling whereby the whole data set was simply split 274 into fixed time intervals (static blocks) of a given uniform duration (see Fig. 2f). 275 Void reconstruction: Voids, i.e., missing plume height values within a block, were filled with the 276 mean value of the interval (see Fig. 2e). 277 Gap reconstruction: When applied, the heights of the missing blocks were reconstructed. The 278 missing blocks were replaced by linearly interpolating between the previous and following block (see

- with *gap*. In contrast, static sampling strategies which applied both void and gap reconstruction are termed *interpolated (int)*.
- 282 *Timebase:* describes the width (i.e., duration) of a block. *SH*-strategies were tested for four
- 283 timebases, covering the range from highest to lowest resolution (see time steps).
- 284 *Time steps:* describes which time interval is used for data sampling. For static sampling strategies,
- the time step is identical to the timebase.
- No data bundling is required when using five-minute time steps. In this case the integrated mass
- 287 M_{5min} over the tested eruption period of duration D (in seconds) was calculated by:

$$M_{5min} = \sum_{j=1}^{f} Q_{j,model}(H_{5min,j}) \cdot \Delta t$$
 (10)

- with the time step Δt =300s, f = $D/\Delta t$, and $Q_{j,model}(H_{5min,j})$ being the mass eruption rate Q_j provided by a
- specific plume model with $H_{5min,j}$ as input parameter.
- 291 By increasing the time steps, the data coverage is increased (see Fig. 2) at the cost of temporal
- resolution. For example, when using static blocks with a time step of 3h, the integrated mass M_{3h} is
- 293 given by:

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$$M_{3h} = \sum_{i=1}^{f} Q_{i,model}(H_{3h,i}) \cdot \Delta t$$
 (11)

- where $H_{3h,j}$ is the 3 h averaged plume height and the time step Δt =300s × 36 = 10,800s.
- Correspondingly, Δt is doubled when using a 6h time step, and a 6h plume height average is used as
- 297 model input. As time step of lowest temporal resolution, we used the complete eruptive phase for a
- 298 static block (see Table 1):

$$M_{phase} = Q_{model}(H_{phase}) \cdot \Delta t \tag{12}$$

- with Δt being the phase's duration and H_{phase} being the phase-averaged plume height. Equation (12)
- was also applied for testing the complete eruption with $\Delta t = E$, where E is the whole recorded
- eruption period. The corresponding diagrams are labelled as *all* (for all phases). In total, we used four
- different time steps for SH strategies (5min, 3h, 6h, phase). For example, an SH-strategy with a
- timebase of 6 h and applied gap reconstruction is denoted *SH_6h_int*.
- 305 **Y-correction**: To adjust for the bias induced by data reduction, four of the tested SH strategies
- 306 multiplied the resulting masses with a correction factor 1/Y (see below). Strategies with Y-correction
- 307 use the additional letter "Y" as identifier. For example, if Y-correction was applied to the strategy
- 308 SH_6h_int, it is denoted SH_Y6h_int.

- Static Sampling of five-minute intervals (S. 5min. gap)
- Being a special case of the SH strategy, the S_5min_gap strategy uses equation (10) for the
- 311 computation of the total erupted mass and does not apply gap reconstruction. Since it uses the
- 312 highest possible temporal resolution, voids cease to exist, and every missing data is a gap, which is
- 313 treated as a "real measurement" by the *S_5min_gap* strategy.
- 314 Static MER reconstruction (*SM*)
- When using average plume heights for reconstructing voids and gaps, we would expect to produce a
- 316 systematic arithmetic error in the computation of erupted mass by the equations (10)-(12), since,
- according to equation (1), the average plume heights do not yield representative MERs. The static
- 318 MER reconstruction (SM) strategy follows therefore a different path. Instead of using average
- 319 heights, void and gap reconstruction is applied by reconstructing the "missing" MERs for each time
- 320 step.

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- 321 **Sampling method**: SM strategies apply static sampling.
- 322 *Void reconstruction*: Voids were filled with the average MER value of the interval. The erupted mass
- 323 *M* of a block *B* was therefore computed by:

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$$M_{3h,B} = \left(\sum_{j=1}^{36} Q_{j,model}(H_{5min,j}) \cdot \Delta t\right) \cdot \frac{36}{(36-\lambda)}$$
 (13)

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$$M_{6h,B} = \left(\sum_{j=1}^{72} Q_{j,model}(H_{5min,j}) \cdot \Delta t\right) \cdot \frac{72}{(72-\lambda)}$$
 (14)

- where λ is the number of voids in block B and $\Delta t = 300$ s.
- 327 *Gap reconstruction:* When applied, the MERs of the missing blocks were reconstructed. The missing
- intervals were replaced by linearly interpolating between the masses of the previous and following
- 329 block.
- 330 *Timebase:* Two different timebases were tested (3 h and 6 h) with the *SM* strategies. In addition, we
- tested a strategy with a five minute timebase and MER-reconstructed gap (SM_5min_int).
- 332 *Time steps:* see timebase.
- 334 Dynamic plume height and MER reconstruction (*DHM*)
- 335 The DHM strategies combine plume height and MER reconstruction, and apply dynamic sampling,
- which is particularly useful for real-time monitoring purposes (Dürig et al. 2018; Dioguardi et al.
- 337 2020).

- 338 Sampling method: Dynamic sampling, using blocks of a uniform duration with moving start and end
- times. The width of the block is defined by the timebase, while the temporal increment with which

- 340 the block is moved is described by the time step. For example, a dynamic sampling strategy using a
- 341 3h timebase means that at any given time the data of the last 3 hours are considered.
- 342 Void reconstruction: Voids were filled with the interval-averaged plume heights, as described for SH
- 343 strategies.
- 344 Gap reconstruction: The missing blocks were replaced by linearly interpolating between the masses
- 345 of the previous and following block, as described for SM strategies. For the presented DHM
- 346 strategies, gap reconstruction was always applied.
- 347 *Timebase:* Two different timebases were tested (3 h and 6 h) with the *DHM* strategies.
- 348 *Time steps:* All *DHM* strategies strategies used five-minute time steps.
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- 350 The REFIR strategies (REFIR)
- 351 The strategies discussed so far produce best MER estimates independently from plume height
- 352 uncertainties. To consider these, the DHM strategies were modified by computing the MER for a
- 353 dynamic block B with:
- $Q_{model,B} = (Q_{model}(H_B s_B) + Q_{model}(H_B) + Q_{model}(H_B + s_B))/3$ 354 (15)
- where H_B is the average height and s_B the plume height uncertainty of the block at time t. 355
- 356 These strategies were computed with the software REFIR (Dürig et al. 2018; Dioguardi et al. 2020),
- 357 which uses equation (15) to obtain a best MER estimate. We note that while the software is designed
- 358 to apply a combination of models linked by weight factors, here we applied it exclusively to individual
- 359 models.
- 360 Sampling method: Dynamic sampling, see DHM.
- 361 Void reconstruction: see DHM.
- 362 Gap reconstruction: see DHM.
- 363 Timebase: Four different timebases were tested (15 min, 30 min, 1 h and 3 h) with REFIR strategies.
- 364 *Time steps:* All *REFIR* strategies used five-minute time steps.
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- Erupted tephra mass 366
- 367 The erupted mass M was used as validation parameter to test the capability of the assessed models
- 368 and data handling strategies in reproducing mass eruption rates. The individual model-derived
- 369 results for the four main stages of the eruption were compared to the total masses obtained for each

of the analyzed phases (Ia, Ib, II, III, IV and all, see Table 1), based on the mapped fallout and exponential dispersal models for the offshore part (Gudmundsson et al. 2012). We denote the measured range of uncertainty *ME*.

373 Computation of *Y*-ratios

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- To study the impact of data reduction on prediction quality, a subset of 49 selected six-hour blocks was used, for which the radar data provides high data coverage (containing at least 60 of 72 data points measured at five-minute intervals). The voids were filled with 6h averages, as described for the SH strategies. For each of the 6h blocks with the best data coverage the predicted mass erupted M_i was computed, based on:
- 379 I. Five minute radar height data H_{5min} . The integrated mass M_{i_5min} was calculated by using eq. 380 (8) with f = 72.
- 381 II. Mean, median and maximum heights $(H_{3h_avg}, H_{3h_med}, H_{3h_max})$ within two 3h intervals. The integrated mass M_{i_3h} over a 6h interval was quantified by:

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$$M_{i_3h} = \sum_{j=1}^{2} Q_{j,model}(H_{3h,j}) \cdot \Delta t$$
 (16)

- 384 with Δt =10,800s (= 3h) and $H_{3h,j}$ being H_{3h_avg} , H_{3h_med} , H_{3h_max} ...
- 385 III. Mean, median and maximum heights (H_{6h_avg} , H_{6h_med} , H_{6h_med}) within the 6h interval, using

$$M_{i 6h} = Q_{model}(H_{6h}) \cdot \Delta t \tag{17}$$

- with Δt =21600s (= 6h) and H_{6h} being H_{6h_avg} , H_{6h_med} or H_{6h_max} , depending on the tested procedure.
- 388 Varying plume model, time interval (3h, 6h) and statistical treatment (mean, median, maximum)
- results in 24 estimates for M_i for each of the 49 analyzed 6h blocks. These mass estimates were
- compared to the respective value M_{i_5min} based on the 5 minutes data sets, by generating the ratios
- 391 *Y*:

$$Y_i = M_i / M_{i \ 5min} \tag{18}$$

- Strategies which apply Y-correction (see Table 2) multiply the estimated mass *M* with the according time interval-specific correction factor 1/*Y*.
- 395 Plume height uncertainties
- We take two types of plume height uncertainties into account for the MER calculations: i) the
- 397 observation uncertainty of the corrected radar plume heights, and ii) the uncertainties introduced by
- using the average plume height of a block to calculate the MER.
- The uncertainty of the radar, ΔH , is assumed to be 0.5 km based on the maximum uncertainty of the
- 400 photo heights and the uncertainty estimates given in Aubry et al. (2021). The uncertainty arising from
- 401 the block averaging of plume heights is assumed to be equal to two standard deviations σ within

each block, corresponding to a 95% significance level. The total plume height uncertainty of a block s_B is then calculated as:

$$s_B = \sqrt{\Delta H^2 + \left(2 \cdot \sigma(H_{block})\right)^2} \tag{19}$$

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For strategies where no height averaging is used, σ is equal to zero, and therefore only radar uncertainties are considered.

Erupted mass uncertainty

The results obtained depend critically on the error in erupted mass. The isopach map reported in Gudmundsson et al. (2012) is based on about 400 data points obtained during and immediately after the eruption. Post-depositional erosion and compaction that often limit the accuracy of tephra layer thickness and size (Biass et al. 2013; Engwell et al. 2013) are therefore considered to be minor for the Eyjafjallajökull data. Good spatial coverage in the near field where thicknesses are several meters on a relatively regular glacier surface result in relative errors in thickness of only a few percent. In the far field the relative errors rise, reaching up to 40% for thicknesses <0.2 cm. The resulting error reported for volume on land is 15% (Gudmundsson et al., 2012). For the offshore part the error was estimated as 40%, based on minimum and maximum extrapolations that are consistent with observations in the Faroe Islands and mainland Europe (for more detail see methods in Gudmundsson et al. 2012). The resulting best estimate of maximum total error was 25%. The contemporary measurements of density of the tephra yielded 1400+/-40 kg m⁻³ (Gudmundsson et al., 2012) a relative error of 3%. Treating these two errors as independent, the effect of the error in density is negligible, resulting in a relative error in mass of 25%.

423 Results

- 424 Plume heights and ERA5 wind speeds
- In Figure 3, the radar-derived plume heights are compared with plume heights obtained by photos.
- The comparison of the 165 data pairs suggests that on average, photo-based plume heights show an
- offset from the radar data of 0.5 km (see Figures 3b and 3c). As a first step for data quality
- 428 improvement, this systematic shift was therefore corrected by adding 0.5 km to all radar-derived
- 429 plume heights (see Figure 3d).
- 430 Figure 4a shows the wind speed profiles over the vent during the Eyjafjallajökull 2010 eruption,
- 431 based on the ERA5 reanalysis data. The highest wind speeds, with up to 64 m/s, occurred during
- 432 phase I in regions above 6000 m at a time when the recorded plume heights reached similar altitudes

(for more detailed, phase-specific plots, see Online Resource 1). In Figure 4b, we show the differences in wind speeds between ICRA and ERA5.

Evaluation of plume height data handling strategies and models

Mean values and standard deviations of the resulting *Y*-ratios based on the 49 selected 6h blocks are presented in Table 3. Three statistical treatments were tested for model input, using average, median and maximum plume height, respectively. The larger the deviation of *Y* from 1, the less reliable the tested method of approximation (assuming M_{i_5min} to be the true value). The *Y*-ratios closest to 1 are found using median plume heights. However, using the median also results in significantly larger standard deviations compared to average plume heights. When using 3h- or 6h-blocks, all models must be corrected with 1/*Y* to be comparable to the summation of masses with 5min time step. For *Y*-corrections we focused on averaged heights, for which *Y* is almost constant for all models. *Y* ranges between 0.89 and 0.91 for 6h-blocks and 0.91-0.92 for 3h-blocks. Therefore, *Y*-correction strategies for 6h-blocks (denoted *Y6h*, see Table 2) were tested by using average heights and a model-independent correction factor of 1/0.9 = 1.1. Accordingly, a correction factor of 1/0.915 = 1.09 was used for *Y3h* strategies.

Figure 5 demonstrates how the temporal evolution of the erupted mass varies, depending on the applied plume height strategy and plume model. In both cases, the whole eruption was used as the reference period, with the measured range of the erupted mass (reported in Gudmundsson et al. 2012) indicated by the red error bar. The curves of Figure 5a show the modelled erupted mass using strategy SH 3h gap. This strategy uses 3h-averaged plume heights in combination with applied voidreconstruction but without gap reconstruction (see Table 2). While for this strategy both windaffected models provide estimates that lie within the measured range, this applies only for one out of the six simple plume models tested (Wilson). Figures 5b-d show the outcome of Wilson when applying different strategies. Comparison of model-estimates to the measured mass for individual eruptive phases is illustrated in Figure 6. When using strategy SH 3h gap for phase I, most of the models underestimate the erupted mass, while for phases II to IV Wilson, Andronico, Scollo and Sparks provide estimates that coincide with the measured range. The same applies to Woodhouse for the phases I, II and III, while this wind-affected model provides too large estimates for phase IV. The other wind-affected model tested with SH_3h_gap, Aubry, provides estimated masses that are above the measured range suggested by Gudmundsson et al. (2012), but provides estimates that are on the lower margin for phase I. This combination results in a coinciding estimate, when considering the whole eruptive period (see Fig. 5a). Systematically on the lower end of the estimated range of modelled masses are Wehrmann and Mastin, suggesting, that SH_3h_gap is not the optimal choice for these models. This overview is an example for just one of the 22 tested strategies with reference

467 to the whole eruption. The phase-specific results for Wilson model outcomes according to the 468 strategies in Fig. 5b can be found in Online Resource 2. 469 Figure 7 compares the measured masses of all reference periods with the estimates of four models 470 using six different strategies with a timebase of 3 hours. The ranges of measured mass for each 471 eruption phase are marked in green. For example, for phase III the Mastin model (see Fig. 7b) 472 achieves best fitting estimates when applying the REFIR_3h strategy. Figure 7 demonstrates the 473 impact that the choice of a strategy has on the modelled MER prediction. Phase II is the phase with 474 the most abundant gaps in the radar records (see Fig. 2). Thus, it is not surprising that this is also the 475 phase where the selected strategy has the biggest influence on the predicted MER. For example, for 476 Mastin the prediction with sampling strategy REFIR_3h is 246 % larger than with SH_3h_gap. 477 As a general finding, applying sampling strategies with gap reconstruction (int) always results in 478 larger masses than applying no gap reconstruction methods (qap). The SM 3h int strategies provide 479 systematically larger results than DHM_3h or SH_3h_int strategies, due to the non-linear relation 480 between H and Q. For the same reason, the mass eruption rates $Q_{model}(H_B + s_B)$ and $Q_{model}(H_B - s_B)$ in 481 equation (15) are not symmetrically distributed towards $Q_{model}(H_B)$. Consequently, the REFIR_3h 482 strategy provides larger values as best MER estimate compared to other strategies. 483 When using the whole eruption as the reference period, the effect of the selected timebase for the 484 REFIR strategy on the model outcome (i.e., the erupted mass estimates) is at maximum 6.8% and 485 therefore small in comparison to the modelled mass uncertainties (see Online Resource 3). The 486 largest effect of the selected timebase on the outcome is found for phase IV, where the model 487 results vary with 12.0% at maximum (see Online Resource 4). Presented results for REFIR methods in 488 the following are limited to the two endmembers (REFIR 3h and REFIR 15min). 489 For the static sampling strategies SH and SM, the timebase can have some considerable impact on 490 the model outcome, especially for phases with abundant gaps. For example, for phase II, the mass predictions increase by 39 to 42% (depending on the model), if strategy SH_6h_gap is applied instead 491 492 of SH_3h_gap . 493 Discongruence indices and congruency maps 494 A result table containing the modelled masses for all phases, data handling strategies and models can 495 be found in Online Resource 5. In order to systematically assess how well the model-estimates 496 coincide with the measured data, we defined discongruence indices (DIs) in Table 4, based on the 497 error ME of measured mass data (Table 1). A model prediction that lies within the range of the 498 measured mass is characterized by a discongruence index of 0. The more the model output deviates 499 from the ground truth, the larger the DI. To better visualize the results, we produced congruency

maps, where each index is assigned a colour. Examples for such congruency maps are shown in Figure 8. There, the dark blue fields mark methods and strategies that lead to estimates that coincide with the range of mass from ground-based measurements. Combinations of strategies and plume models, which provide estimates that are just outside of the range of the measured values are marked in light blue. Predictions that considerably over- or underestimate the erupted mass (DI of 5) are displayed in orange. The resulting congruency map for the complete phase is presented as Online Resource 6, and all phase-specific results are provided in Online Resource 7. Based on the resulting DIs, it was possible to construct tables with their averaged values that allow us to analyse the prediction qualities of models and data handling strategies for individual eruptive phases, as well as for the complete eruption (Tables 5 and 6). Phase-specific comparison of plume height data handling strategies Table 5 lists for each phase the strategies' success, represented by discongruence indices averaged over all tested plume models (separated between simple and explicitly wind-affected models). When using the entire eruption (all) as the reference period, the overall average DI for all strategies is 0.7. According to the results, the most successful strategy for the simple models is REFIR_3h with a DI of 0.3. For wind-affected models a number of strategies resulted in predicted mass values congruent to the measured mass, including SH 6h gap, SH 6h int, SM 3h gap, DHM 6h and DHM 3h. According to the model-specific DIs averaged over all strategies (Table 6), the models by Wilson and Sparks were found to have the highest prediction success rate, with DIs of 0.05 and 0.015, respectively, when considering the entire eruption. When studying individual phases, Andronico and Sparks turn out to be most successful, with an average DI of 0.05 for phase III. Below we summarize the results for each of the phases: Phase Ia: the overall average DI is 2.16, significantly larger than for any other phase. According to Table 6, the most successful strategy for both simple and explicitly wind-affected models is REFIR 15min with DIs of 1.7 and 0.5, respectively. Phase Ib: here strategies provide higher success rates. Optimal strategies for simple models are the REFIR strategies, as well as SM 6h gap and SM 6h int, featuring DIs of 0.5. For wind-affected models, however, other strategies (e.g., SH_6h_int or DHM_6h) provide better results, while REFIR strategies result in overestimates of predicted masses. Phase II: due to relatively weak activity, phase II has the lowest data coverage per block (see Fig. 2d). Many strategies and models tend to overestimate the erupted mass of this phase. This applies especially to strategies where gaps were filled by interpolated data (DHM, REFIR and static sampling

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532 methods with gap reconstruction). For simple models, the best results with a DI of 0.3 are found for 533 SM 6h gap, SH 6h gap and SH phase, which are strategies with large timebases and no gap 534 reconstruction. For wind-affected models, the best results were achieved with SM 3h gap, 535 SH_3h_gap and SH_Y3h_gap. 536 Phase III: featured increased explosive eruption at relatively low wind speeds. There, strategies 537 showed the highest success rates of all phases with an average DI of 0.45 (0.5 for simple models, 0.2 538 for explicitly wind-affected models). The most successful strategies for simple models were the REFIR strategies with a DI of 0.3. For Woodhouse and Aubry most of the tested strategies result in 539 540 predictions that coincide with the measured mass. Exceptions are the REFIR strategies (DI = 1.0), and 541 strategies that apply Y-correction (DI = 0.5). 542 Phase IV: For the weaker final eruptive phase, the optimal strategies for simple and explicitly windaffected models were found to be REFIR 15min (DI = 0.2) and S 5min qap (DI = 0), respectively. 543 544 Effect of using ERA5 vs ICRA weather data So far, the results presented for the explicitly wind-affected models (Woodhouse, Aubry) are based 545 546 on ERA5 wind speed data. How much do the results of these models (i.e., estimated erupted mass) 547 change, when the ICRA data of (considerably) higher spatial resolution are used? In most cases 548 (except for phase IV), the ICRA data leads to slightly larger mass estimates, but these changes are 549 almost insignificant, considering the uncertainties (see Online Resource 8 for Woodhouse). For 550 example, when applying the REFIR 3h strategy to Woodhouse, the differences between model-results 551 based on ERA5 versus ICRA wind speeds is only approximately 2% for the whole eruption (and 1.3% 552 of the uncertainty). The absence of sizeable changes can be explained by the fact that both sets of 553 weather data feature similar wind speeds over most of the eruption period (see Fig. 4b). The only 554 major difference (of more than 10 m/s) occurred during phase II, on 29 April below 2000 m a.s.l. For 555 this phase, the modelled mass differed by 4.7%, which is small considering the model uncertainties. 556 We thus conclude that for reanalysis of the Eyjafjallajökull 2010 eruption, using weather data of 557 higher spatial resolution only effects the overall outcome in a minor way. However, this result 558 should not be generalized. A reanalysis of other eruptions, especially short-termed ones, will 559 probably benefit from a higher spatial resolution of weather data. Wind effect on plume deflection and plume model predictions 560 561 The horizontal deflection of the plume top plotted over the contemporary wind speed at plume top 562 level, based on ICRA reanalysis weather data (Figure 9a) shows an approximately linear correlation between these parameters. This is also indicated by a Pearson correlation coefficient (R) of ~0.68. For 563 564 Figure 9a, wind speeds at variable elevation were used. To find out for which fixed altitude the wind

speeds of both ERA5 and ICRA data (Fig. 9b). Next to the raw data ($ERA5\ 1h$ and $ICRA\ 1h$), wind speeds averaged over 2h and 3h were also used. The best correlation at fixed elevation is observed for 2h-averaged ERA5 wind speeds at 2900 m a.s.l. (R = 0.65). At that altitude ICRA wind speeds correlate slightly less with deflection (R = 0.63), but below 2500 m a.s.l. it is the ICRA data that shows a better correlation with wind speeds compared to ERA5.

From the models tested, not only *Woodhouse* and *Aubry* incorporate a wind-effect. There is an implicit dependency on wind for the other (simple) models as well, as revealed by Figure 10. There, the ratio of modelled vs measured mass was plotted over phase-averaged wind speeds. For the modelled mass, three non-explicitly wind-affected models were investigated in combination with four strategies: *Wilson* (*Wil*, as representative for the simple numerical 0D models), *Sparks* (*Spa*) and *Mastin* (*Mas*). Here we selected strategies that do not apply gap reconstruction, to avoid the bias caused by the fact that there is a large variance in data gaps between the different phases. Two general trends (indicated by trendlines) can be observed:

- At low wind speeds the different strategies and models lead to predictions with a large span.
 This range decreases for larger wind speeds.
- 2) With higher wind speeds all shown strategies and non-explicitly wind-affected models tend to increasingly underestimate the actual erupted mass. While for a wind speed of 14.5 m/s $M_{modelled}$ / $M_{measured}$ averages at around 103%, this ratio drops for 16.2, 19.2 and 36.4 m/s to 79%, 67% and 46%, respectively. Thus, for wind speeds over 20 m/s the model predictions underestimate the erupted mass on average by more than 40%.

Both trends are also confirmed in Figure 8, which compares the congruency maps of high-wind eruptive phase Ia (Fig. 8a) with the phase of lowest wind speeds (phase II, Fig. 8b), thus contrasting the two end members of Fig. 10. Compared to phase Ia, phase II was of much longer duration, and it was characterized by abundant data gaps, which should result in large differences between gap-reconstructing strategies and those which ignore them. Yet, for phase II, 54 combinations of strategies and models provide predictions that lie within the uncertainties of the measurements *ME* (tiles marked with dark blue color), as opposed to only 14 combinations found for phase Ia. While for most combinations, the explicitly wind-affected models *Woodhouse* and *Aubry* appear to be robust against this wind effect, for the simple models only very few combinations give predictions close to the measurements.

Discussion

The comparison between radar and photographic data suggests that the former systematically underestimated the plume height by 0.5 km. This finding is in contrast to the assessment of webcam

images analyzed by Arason et al. (2011), which suggested that the radar over-estimated the plume heights. These webcams were, however, located to the north and west-northwest of the volcano, while the plume was deflected away from the cameras, towards the south to southeast. Using the distance to the vents instead of the plume top would therefore lead to an underestimation in webcam-derived plume heights which might explain the differences with our results (see Fig. 3d). For example, a plume top of 5 km height that is shifted towards the south with a deflection d of 6 km would be perceived as being only 3 km high on images produced by the webcam at Þórólfsfell, located 9 km to the north from the vents. The difference between photos and radar measurements is mainly a consequence of the radar's horizontally stepping scanning procedure and the eruptive and atmospheric circumstances during the 2010 eruption. This implies that such an offset could change in a future eruption at Eyjafjallajökull, even if the same radar sensor is applied. The data sets on which the empirical models are based include observations for various situations regarding wind speed, but it is known that scenarios of weak eruptions under strong wind-conditions are underrepresented (Mastin 2014). Furthermore, under high wind speeds plume height is reduced, due to the facts that the plume is bent-over and that there is more efficient turbulent entrainment of air into the column (Bursik 2001). For the phases of weak activity and relatively low wind speeds, however, the empirical models by Mastin (phase II with 0.35) and Sparks (phase IV with 0.10) still have shown to be among the ones with highest prediction success. As a general finding, the explicitly wind-affected models tend to have larger ranges of uncertainty and over rather than underestimate the measured mass (see, e.g., Fig. 11). Results from the simple models fall at the other end of the modelled range, with Wehrmann being the most extreme example, which tend to systematically underestimate the mass eruption rates, especially under windy conditions. This discrepancy between estimates from simple and explicitly wind-affected models under windy conditions is consistent with previous findings (Bursik 2001; Mastin 2014). When analyzing the entire eruptive period by comparing the strategy-averaged DIs for simple plume models (see Table 5), the REFIR_15min approach turned out to be the optimal strategy. In contrast, using REFIR strategies with explicitly wind-affected models lead often to overestimated mass predictions. These models are affected by larger uncertainties than the simple plume models (see, e.g., Fig 11), which leads to larger MER predictions, due to the definition of the best estimate by equation (15). Of particular interest is also the comparison between phase Ib and III, which were similarly well covered (9.3 vs 9.2 plume height measurements per hour), had only slightly dissimilar prevailing wind speeds (19.2 vs 16.2 m/s), but differed in eruptive styles: phase Ib was phreatomagmatic, whereas

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phase III was magmatic. Despite different outcomes for most of the other strategies, the REFIR strategies appear to be the most robust for both types of eruptive styles. This robustness is noteworthy, considering that phreatomagmatism is based on thermohydraulic fuel-coolant interaction processes (Wohletz 1986; Büttner and Zimanowski 1998; Dürig et al. 2020), which produce more fine-grained ash particles, release larger kinetic energy and generate steam - all of which are factors that are expected to affect the plume rise behaviour (Koyaguchi and Woods 1996; Sparks et al. 1997). An important choice when selecting the plume height data handling strategy is the decision of whether gap reconstruction is applied or not. In a real-time monitoring scenario (as well as in reanalyses), where radar is the only source for plume heights, it is difficult to distinguish "real" gaps from data missing for other reasons. For example, it was suggested that the data gap between 15 and 16 April 2010 (within phase Ia) was real, and a consequence of low plume heights (Mastin 2014). According to our results, however, the optimal strategies for that phase are those that apply gap reconstruction (e.g., REFIR 15min), indicating that the gap was not reflecting the status of the actual plume. This is corroborated by photographs taken on that day, that prove the existence of a plume in that period. In contrast, our findings for phase II indicate that the gaps during that phase were real. In such scenarios of very weak eruptive activities, strategies with large timebases (such as SH_phase) or applied gap reconstruction (such as SM_6h_int) result in overestimated mass predictions, especially for explicitly wind-affected models. For modelling long-lasting eruptions with diverse episodes, comparable to Eyjafjallajökull 2010, we would therefore recommend a mixture of strategies, tailored to phase and model-type. Similar to applying gap reconstruction, using a too large timebase result in real data gaps being missed. Using a too short timebase, on the other hand, might lead to errors when monitoring an evolving plume that has not reached stable buoyancy yet. Since this would violate the steady state assumption of the models, the model predictions would not be reliable. We consider the latter effect, however, as insignificant, when modelling a long-lasting eruption like Eyjafjallajökull 2010. A key finding of this study is the dominating influence of the wind speed on the prediction quality of plume height data for mass eruption rates, at least for moderate eruptions with bent-over plumes. This is highlighted by the results of the phase-specific comparison of plume height data handling strategies (Table 5) and illustrated in Figures 8 and 10. Phase Ia is characterized by the highest wind speeds, and despite having a good data coverage (8.1 measurements per hour, see Table 1) the strategies are on average considerably less successful than for phases Ib and III. All our results indicate that for a moderate-to-weak eruption like Eyjafjallajökull 2010, it is increasingly challenging for wind speeds exceeding ~20 m/s to find combinations of plume models and data handling

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666 strategies with which the mass eruption rate can be accurately predicted in real-time. This inference 667 highlights how important it is to monitor such eruptions in real-time and use the 'optimal' 668 combination of plume height data handling strategy and plume models. 669 The strategies presented were tested by focusing only on the best MER estimates, without 670 considering the ranges of uncertainty (with the REFIR strategies being notable exceptions). These can 671 become substantial and exceed the span of the measured mass by several orders of magnitude 672 (Figure 11, for uncertainty ranges in modelled MERs, see also online resource 5). The uncertainties 673 for $M_{modelled}$, as defined by equation (19), depend on model, timebase, strategy and the relative data 674 coverage of the studied period. For example, when considering the entire eruption period, the 675 uncertainties for SH_3h_int increase by 9 - 12% (depending on the model) compared to SH_3h_gap 676 (15 - 17% for SM_3h_int vs SH_3h_gap). For phase II alone, the uncertainty ranges between the two 677 strategies increase by up to 41% (up to 43% for for SM_3h_int vs SH_3h_gap). 678 Selecting a short timebase has a significant effect on the modelled mass uncertainties. For example, 679 compared to the 3h-timebase, the REFIR uncertainties for a timebase of 15 minutes is reduced by up 680 to 24% when considering the whole eruption period. For phase IV, this decrease reaches 32.5%. The 681 largest uncertainties are found for the largest possible timebase, with strategy SH_phase (see Fig. 682 11b). 683 It is important to note that our error estimates did not consider model-inherent uncertainties (an 684 example for the uncertainties of the Mastin model is shown in Fig. 11a). For some strategies, the 685 model uncertainties could be larger than the ranges defined by equation (19). A model-strategy combination with a large DI does not necessarily provide a "wrong" prediction, since its uncertainty 686 687 interval could (at least partly) overlap with the measured range. On the other hand, combinations 688 that result in predictions affected by a large uncertainty range are unfavorable for real-time 689 monitoring purposes. Our approach is optimized for finding the model-strategy pairs which provide 690 the best estimates that are closest to the measurement, but we note that this is not the only method 691 to assess the quality of strategies and models, and more advanced comparison methods might also 692 consider the range and overlap of modelled mass uncertainties. 693 The radar data by Arason et al. (2011) has been used by a plethora of studies on the 2010 ash plume 694 of Eyjafjallajökull (Kaminski et al. 2011; Bursik et al. 2012; Gudmundsson et al. 2012; Degruyter and 695 Bonadonna 2012; Devenish 2013; Ripepe et al. 2013; Woodhouse et al. 2013; Mastin 2014; Dürig et 696 al. 2015b; Dioguardi et al. 2020). Our suggested height correction still lies within the reported error 697 margins, but when used as input for plume models it will increase the MER predictions. Due to our 698 definition of uncertainties by equation (19), for strategies that do not apply height reconstruction,

11b, the effect of the height correction on the modelled mass is represented by the distance between the lower error bar and the best estimate for these strategies (e.g., all *SM*-strategies).

In their study on Eyjafjallajökull, Woodhouse et al. (2013) applied an *SH* strategy with a timebase of 1h, but using the maximum plume height within each block instead of plume height averages. We note that the 10% plume height reduction applied to convert *H* into *h* for *Woodhouse* is in the same range as the height correction applied to the radar data. We therefore used comparable plume heights as input as Woodhouse et al. (2013). Using the maximum plume heights per block instead of averages resulted in MER predictions for phase la that exceeded our estimates by an order of magnitude. We suggest that, when using *Woodhouse* to re-model the Eyjafjallajökull 2010 eruption, using data handling strategies like *SH_3h_gap* with block-averaged plume heights might be the more suitable strategy.

The *SH* strategies are the most commonly used for plume modelling (Kaminski et al. 2011; Bursik et al. 2012; Degruyter and Bonadonna 2012; Woodhouse et al. 2013; Mastin 2014; Dürig et al. 2015b), and our findings indicate that these strategies (especially *SH_3h_gap*) are often a good choice when using explicitly wind-affected models, but they are far less successful with simple models. From the

dynamic sampling strategies, which are typically used for real-time monitoring, DHM strategies prove

to provide best results for explicitly wind-affected models. When used with simple models, however,

the plume height uncertainties are only dependent on the radar height uncertainty itself. In Figure

Conclusions

the optimal choice is the *REFIR* strategy.

ground-based photographs of the plume together with ground-based measurements of the erupted mass to study and compare the predictive qualities of eight plume models in combination with 22 data handling strategies. Although the latter has a significant influence on the model outcome, their influence has, to our knowledge, not yet been studied to this extent before.

The best re-analysis results for simple (non-explicitly wind-affected) plume models are in most cases obtained by using strategies implemented in the software REFIR (Real-time Eruption source parameters FutureVolc Information and Reconnaissance system), which apply dynamic sampling in the form of a moving average and consider the plume height uncertainties. The only exception is found for phase II, where the eruptive activity was weak, and the plume height was under the detection limit of the radar for a considerable amount of time, causing data gaps in the records.

Focusing on the different eruptive phases of the Eyjafjallajökull 2010 eruption, we used aerial and

There, interpolating strategies generate ghost-data points, which lead to an overestimation of the erupted mass. Under such conditions, strategies without gap reconstruction and with long timebases (such as SH_phase or SM_6h_gap) are more reliable. For explicitly wind-affected models, the best strategies were found to be static sampling strategies with short timebases and without gap reconstruction (such as SH_3h_gap). Our findings suggest that no single model has always the best answers, and different models and data handling strategies work best under different plume and data conditions. Which model and strategy to choose for optimal prediction results depends on data coverage, eruption intensity and, according to our findings from Eyjafjallajökull, to a lesser extent on fragmentation mechanism (e.g., magmatic vs phreatomagmatic). The dominant factor on the prediction quality, however, was found to be the wind speed. The higher the wind speed, the more the non-explicitly wind-affected models tend to underestimate the MER. Conversely, the explicitly wind-affected Woodhouse model overestimates it, when applying the REFIR strategies. Namely for wind speeds over 20 m/s, only a few combinations of data handling strategies and plume models provide accurate predictions when monitoring an Eyjafjallajökull 2010 – type of eruption. A possible solution for obtaining accurate estimates in real time for such long-term eruptions of variable and moderate intensity under varying wind speeds would therefore be to not rely on a single combination of data handling strategy and plume model, but to be able to use a range of such combinations, thus providing the possibility to adapt to the scenario monitored.

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752 Tables

Table 1:

Modelled eruptive phases and ground truth. Modelled phases of the 2010 Eyjafjallajökull eruption are listed, together with the estimated ranges of erupted airborne tephra mass, as reported in Gudmundsson et al. (2012). The errors of erupted mass are denoted *ME*. In our study these values were used as ground truth for testing the model predictions with different plume height data handling strategies. Additional columns indicate duration, number of recorded radar measurements, data points (i.e., plume height measurements) per hour and time-averaged wind speed for each phase. Computation of wind speeds were based on ERA5 reanalysis data for the (radar-detected) plume heights.

phase	from (dd/mm)	until (dd/mm/yy)	duration (min)	erupted mass ± ME (×10 ¹⁰ kg)	number of radar measurements	data points per hour	wind speed m/s
la	14/04	16/04/10	3785	9.80 ± 2.10	511	8.1	36.4
Ib	17/04	18/04/10	2165	3.50 ± 0.98	335	9.3	19.2
l (total)	14/04	18/04/10	5945	13.30 ± 3.08	846	8.5	30.1
II	18/04	4/05/10	23765	4.20 ± 1.40	1005	2.5	11.8
III	5/05	17/05/10	18725	18.90 ± 4.90	2858	9.2	16.2
IV	18/05	21/05/10	4950	1.40 ± 0.42	430	5.2	14.5
all	14/04	21/05/10	53385	37.8 ± 9.8	5139	5.8	15.6

Tested data handling strategies. The columns list the aspects that were varied: sampling method, void reconstruction, gap reconstruction, timebase (i.e., duration of a block), time stepping and Y-correction.

Table 2:

Strategy	sampling	void	gap	timebase	time	Υ-
		reconstructed	reconstructed		step	correction
		variable	variable			
S_5min_gap	static	- n. a	- none -	5 min	5 min	- none -
SH_phase	static	height	- n. a	phase	phase	- none -
SH_6h_gap	static	height	- none -	6 h	6 h	- none -
SH_Y6h_gap	static	height	- none -	6 h	6 h	Yes
SH_3h_gap	static	height	- none -	3 h	3 h	- none -
SH_Y3h_gap	static	height	- none -	3 h	3 h	Yes
SH_6h_int	static	height	height	6 h	6 h	- none -
SH_Y6h_int	static	height	height	6 h	6 h	yes
SH_3h_int	static	height	height	3 h	3 h	- none -
SH_Y3h_int	static	height	height	3 h	3 h	yes
SH_5min_int	static	- n. a	height	5 min	5 min	- none -
SM_6h_gap	static	MER	- none -	6 h	6 h	- none -
SM_3h_gap	static	MER	- none -	3 h	3 h	- none -
SM_6h_int	static	MER	MER	6 h	6 h	- none -
SM_3h_int	static	MER	MER	3 h	3 h	- none -
SM_5min_int	static	- n. a	MER	5 min	5 min	- none -
DHM_3h	dynamic	height	MER	3 h	5 min	- none -
DHM_1h	dynamic	height	MER	1 h	5 min	- none -
REFIR_3h	dynamic	height	MER	3 h	5 min	- none -
REFIR_1h	dynamic	height	MER	1 h	5 min	- none -
REFIR_30min	dynamic	height	MER	30 min	5 min	- none -
REFIR_15min	dynamic	height	MER	15 min	5 min	- none -

768 Table 3:

Results for Y-values, based on 49 static 6h-blocks with a data coverage of 60/72 or higher. Numerical OD models stand for *Wilson, Wehrmann, Scollo* and *Andronico* models. For *Woodhouse*, ERA5 weather data was used. Y-correction strategies multiplied the predicted mass with 1/Y.

		6h		3	Sh	
		mean	stdev	mean	stdev	
	average	0.90	0.10	0.91	0.09	
numerical 0D models	median	0.95	0.25	0.95	0.19	
	maximum	2.36	2.15	2.06	1.45	
	average	0.91	0.09	0.92	0.08	
Sparks	median	0.96	0.24	0.95	0.19	
	maximum	2.29	2.00	2.01	1.36	
	average	0.89	0.11	0.91	0.10	
Mastin	median	0.95	0.26	0.95	0.20	
	maximum	2.44	2.31	2.12	1.55	
	average	0.91	0.09	0.92	0.09	
Woodhouse	median	0.97	0.26	0.95	0.19	
	maximum	2.37	2.13	2.08	1.46	

Table 4:

List of discongruence indices (*DIs*). A *DI* of 0 refers to a model-estimate, which lies within the range of measured mass according to Gudmundsson et al. (2012). This range is illustrated by red error bars in Fig. 5 and Fig. 6 and specified by the uncertainty *ME*. A *DI* of 0 is therefore congruent with the "ground truth". The larger the discongruence index, the more the model-output deviates from the ground truth.

Discongruence	minimum deviation from measured	maximum deviation from measured			
Index (DI)	mass	mass			
0	0	ME			
1	ME	1.5 <i>ME</i>			
2	1. 5 <i>ME</i>	2 ME			
3	2 <i>ME</i>	2.5 <i>ME</i>			
4	2.5 <i>ME</i>	3 <i>ME</i>			
5	3 <i>ME</i>	> 3 ME			

782 Table 5:

Average discongruence indices listed by data handling strategy and reference period. The first value is the resulting *DI* for the six simple models tested (*Wilson, Andronico, Scollo, Wehrmann, Sparks, Mastin*), the second column presents the averages for the two wind-affected models (*Woodhouse, Aubry*). The smaller the value, the more often fits the modelled result with the measured mass. Values representing the most successful strategies for a phase are printed in bold.

Row	la	a	I	b	I	I	I	I	I,	/	а	II	avera	ge
S_5min_gap	3.0	0.5	1.5	0	2.8	1.0	0.8	0	2.3	0	1.7	0	2.0	0.3
SH_phase	3.0	0.5	2.0	0	0.3	2.0	1.3	0	0.5	1.0	1.0	1.0	1.4	0.8
SH_6h_gap	2.8	0.5	1.5	0	0.3	1.5	0.5	0	0.5	1.0	1.3	0	1.2	0.5
SH_Y6h_gap	2.5	0.5	1.3	0.5	0.5	1.5	0.5	0.5	0.5	1.0	0.7	1.0	1.0	0.8
SH_3h_gap	3.5	0.5	1.7	0	0.5	0.5	0.5	0	0.5	1.0	1.3	0	1.3	0.3
SH_Y3h_gap	2.8	1.0	1.3	0	0.5	0.5	0.5	0	0.5	1.0	1.2	0	1.1	0.4
SH_6h_int	2.8	0.5	1.5	0	0.7	2.0	0.5	0	0.5	1.0	1.0	0	1.2	0.6
SH_Y6h_int	2.5	0.5	1.3	0.5	0.7	2.5	0.5	0.5	0.3	1.5	0.5	1.0	1.0	1.1
SH_3h_int	3.0	1.0	1.7	0	0.8	2.0	0.5	0	0.5	1.0	0.8	0	1.2	0.7
SH_Y3h_int	2.8	0.5	1.3	0	0.7	2.0	0.5	0.5	0.3	1.5	0.5	1.0	1.0	0.9
SH_5min_int	2.7	1.0	1.3	0	0.7	2.0	0.5	0	0.5	1.0	0.5	1.0	1.0	0.8
SM_6h_gap	2.2	0.5	0.5	0.5	0.3	1.5	0.5	0	0.5	1.0	0.5	0.5	0.8	0.7
SM_3h_gap	2.8	1.0	0.7	0.5	0.5	0.5	0.5	0	0.5	1.0	0.8	0	1.0	0.5
SM_6h_int	2.2	0.5	0.5	0.5	0.7	2.5	0.5	0	0.3	1.5	0.5	1.0	0.8	1.0
SM_3h_int	2.5	0.5	0.7	0.5	0.8	2.0	0.5	0	0.3	2.0	0.5	1.0	0.9	1.0
SM_5min_int	2.5	0.5	1.3	0	0.7	2.0	0.5	0	0.5	1.0	0.5	1.0	1.0	0.8
DHM_6h	3.0	1.0	1.7	0	0.7	2.0	0.5	0	0.5	1.0	0.8	0	1.2	0.7
DHM_3h	3.0	1.0	1.7	0	0.7	2.0	0.5	0	0.5	1.0	0.7	0	1.2	0.7
REFIR_3h	1.7	1.0	0.5	1.0	1.0	3.0	0.3	1.0	0.5	2.0	0.3	1.0	0.7	1.5
REFIR_15min	1.7	0.5	0.5	1.0	0.8	2.5	0.3	1.0	0.2	2.0	0.5	1.0	0.7	1.3
average	2.7	0.7	1.2	0.3	0.7	1.8	0.5	0.2	0.5	1.2	0.8	0.5	1.1	0.8

791 Table 6:

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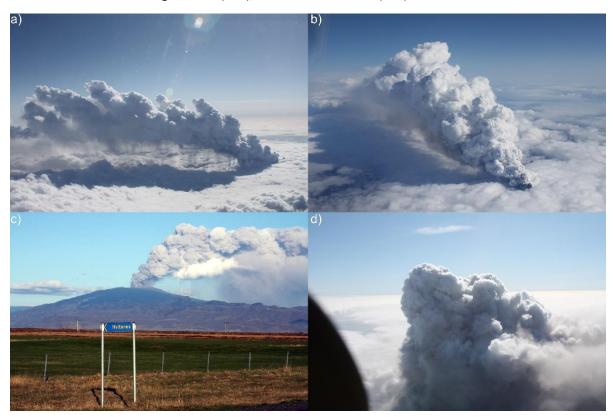
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Average discongruence indices over all strategies, listed by reference period and plume model.

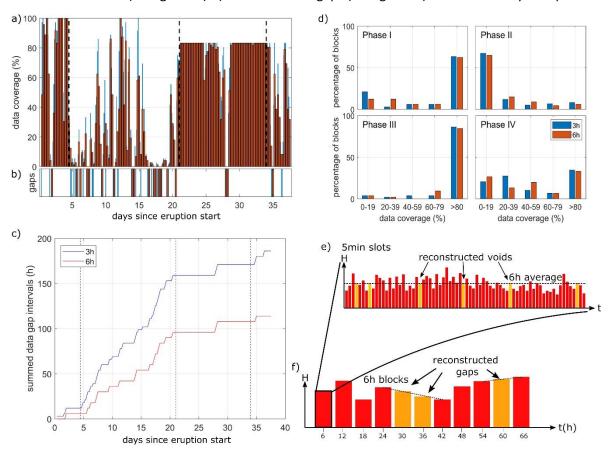
Row	Wilson	Wehrmann	Scollo	Andronico	Sparks	Mastin	Woodhouse	Aubry	average
la	1.55	4.90	2.20	1.85	1.85	3.55	0.95	0.40	2.16
Ib	0.40	3.10	0.70	0.70	0.70	1.75	0.10	0.40	0.98
П	1.05	0.80	0.70	0.70	0.80	0.35	1.10	2.45	0.99
Ш	0.10	2.00	0.10	0.05	0.05	0.95	0.10	0.25	0.45
IV	0.10	1.85	0.10	0.10	0.10	1.00	1.10	1.25	0.70
all	0.05	2.55	0.45	0.20	0.15	1.30	0.55	0.50	0.72
average	0.54	2.53	0.71	0.60	0.61	1.48	0.65	0.88	

Figure 1

Examples of photos that were used to validate the plume height records from radar. a) Aerial picture of the Eyjafjallajökull plume, taken on 14 April 2010 at 10:20 UTC. b) This photo was taken 5 minutes later from a different angle. Since the GPS coordinates of the plane were logged, the horizontal location of the plume top could be constrained by triangulation. At that time, the plume top reached an altitude of (6.0 ± 0.3) km above vent. c) Example of a photo taken on the ground, from a distance of 29 km from the vent. This picture dates from 10 May (19:50 UTC), when the plume was deflected by 1.7 km towards 193° (SSW), with its top reaching an elevation of (2.2 ± 0.2) km above vent. d) This photo was taken on the last day of the eruption (21 May) at 18:00 UTC. In this case the elevation of the plume was directly assessed by flying at the same elevation as the plume top and using the onboard altimeter. The aircraft flew at 12,000ft a.s.l., which translates into a plume height of (2.3 ± 0.1) km. Photo credits: Th. Högnadóttir (a, b); M.T. Gudmundsson (c, d).



The radar record of the 2010 Eyjafjallajökull eruption. Data from Arason et al. (2011). a) Data coverage of 3h- (blue) and 6h -(red) blocks. For example, a 6h-block with 50% data coverage represents a set of 72 5-minute slots, of which 36 contain data. b) Timing of data gaps (i.e. blocks that are completely empty). c) Increasing the time step (i.e., block width), leads to a reduction of total overall gap time. d) Histograms show that data coverage of the blocks differed between the eruptive phases. e) Voids in the plume height records are reconstructed by filling them with the block's mean value (orange bars). f) Reconstructed gaps (orange bars) are obtained by interpolation.



 Plume height validation by means of photographic plume analysis. a) Radar-based plume height records of the Eyjafjallajökull 2010 eruption were compared with elevation data retrieved from photos. b) Photo plume heights are systematically shifted upward by 0.5 km relative to radar plume heights. c) This means that, statistically, the radar signal underestimated the actual plume height by 0.5 km. d) Due to windy conditions, the ash plume showed at times a considerable deflection *d*, which would lead to an underestimation of the plume if the distance to the plume top is assumed to equal the distance to the vent *s*.

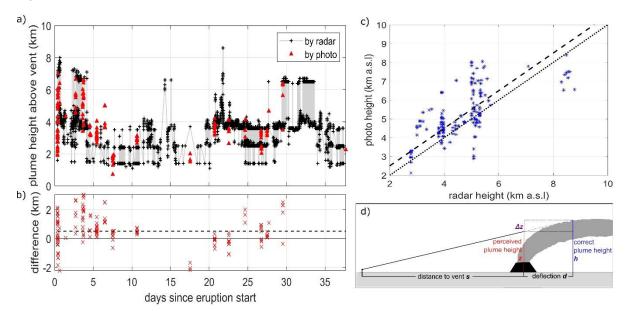
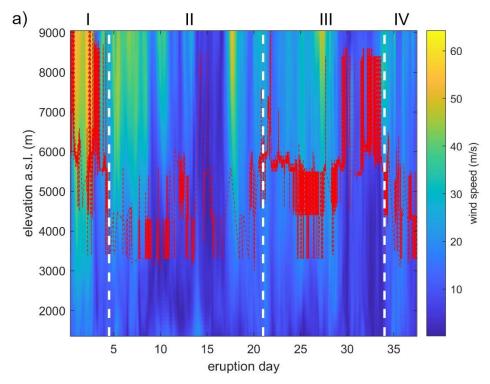
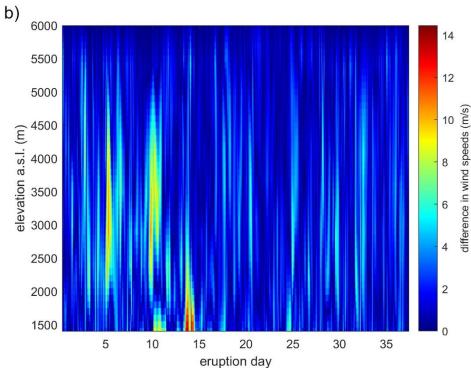


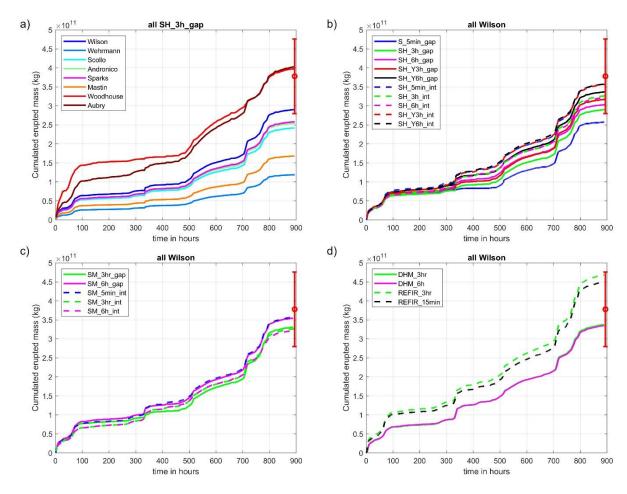
Figure 4

Wind speeds above Eyjafjallajökull during the 2010 eruption. a) Plume height (red curve) is plotted together with altitude-specific wind speeds above the vent, based on ERA5 reanalysis data. Altitude refers to sea level. Vertical dashed white lines mark margins of eruptive phases. b) Overall, the absolute differences in wind speeds between ICRA and ERA5 were relatively small, with only sporadic disparities, mainly at ground level on day 14.

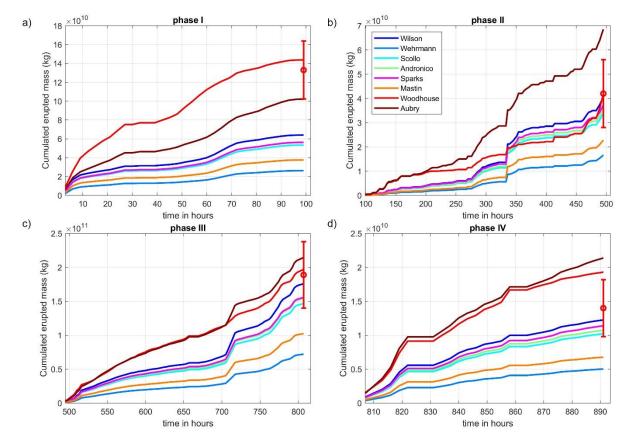




Modelled erupted mass. Erupted mass is computed by multiplying the modelled mass eruption rates by the block duration and summing the results over the reference period (here: the entire eruption). The range of measured erupted mass as reported by Gudmundsson et al. (2012) (see also Table 1) is displayed as red error bar with width ME. a) For each of the 8 tested models, 6h-averaged plume heights were used as input with void but no gap reconstruction, thus applying strategy SH_3h_gap (see Table 2). Wind speeds from ERA5 were used for Woodhouse and Aubry. b) Results for S_5min_gap and SH plume height strategies applied to the Wilson model. c) Results for SM strategies. c) Predicted mass by Wilson with SM strategies.



 Modelled curves of erupted mass for each eruptive phase, applying strategy SH_3h_gap for eight models. The range of measured erupted mass (ground truth) is indicated with a red error bar. Reference periods are: a) phase I, b) phase II, c) phase III, d) phase IV.



Phase-specific comparisons of modelled versus measured mass. Results for six strategies (marked by different symbols) are presented for the whole eruption (all) and individual phases. The plots show the model-specific outcomes for: a) Wilson, b) Mastin, c) Woodhouse d) Aubry (with using wind speeds from ERA5 for both wind-affected models). The green lines indicate the range of erupted mass, interpolated according to ground measurements. A symbol lying within this corridor indicates that the respective strategy and plume model provides a 'successful' prediction under the tested eruptive conditions.

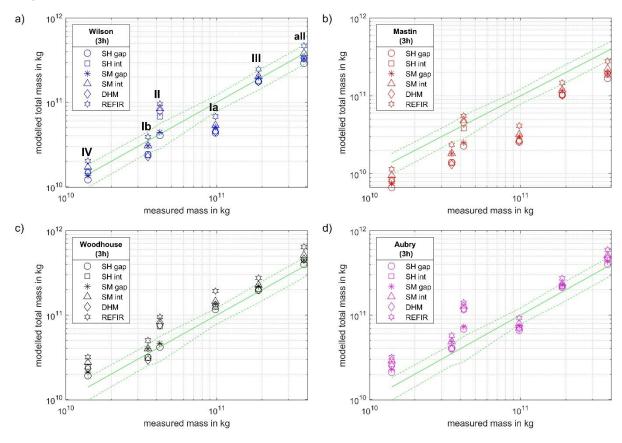


Figure 8

 Congruency maps for combinations of strategies and models. ERA5 wind speeds were used for *Woodhouse* and *Aubry*. Each cell's colour indicates how well the estimate of a strategy and model pair fits with the measured data. Dark blue tiles indicate predictions that coincide with measurements. a) Congruency map of all strategies and models for phase Ia, which was characterized by the highest wind speeds. b) Congruency map for phase II, the phase with the most gaps in the radar records.

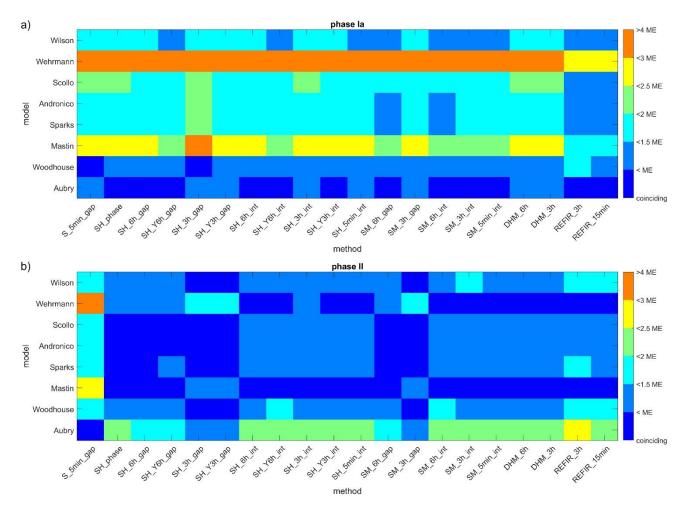


Figure 9

Wind-induced deflection of plume top. a) Photo-derived deflection of plume top is plotted versus wind speeds at maximum plume height, according to ICRA reanalysis data. The data plots with a Pearson correlation coefficient of 0.68. b) Correlation between deflection of the plume top and wind speeds at different altitude levels (elevation above sea level).

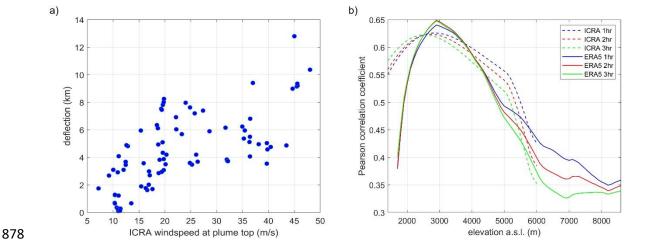


Figure 10

Wind-effect on simple (i.e., non-explicitly wind-affected) model predictions. Using four data handling strategies for three models (*Wil: Wilson, Spa: Sparks, Mas: Mastin*), the ratio of modelled vs measured mass is plotted over phase-averaged ERA5 wind speeds. The black curves serve for visualization of what appears to be a general trend: the stronger the wind, the more the simple plume models tend to underestimate the mass eruption rate, regardless of the applied strategy.

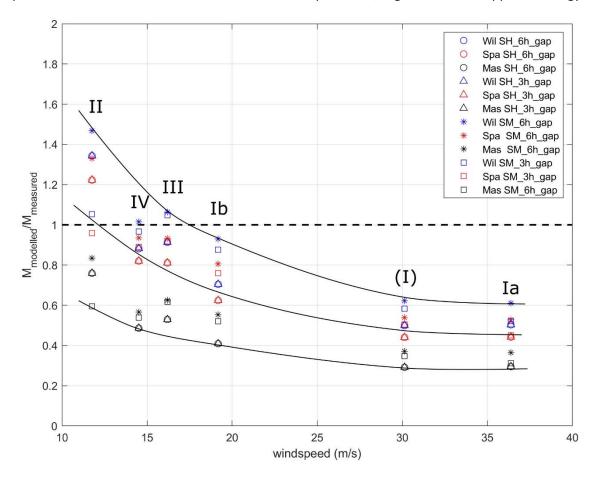
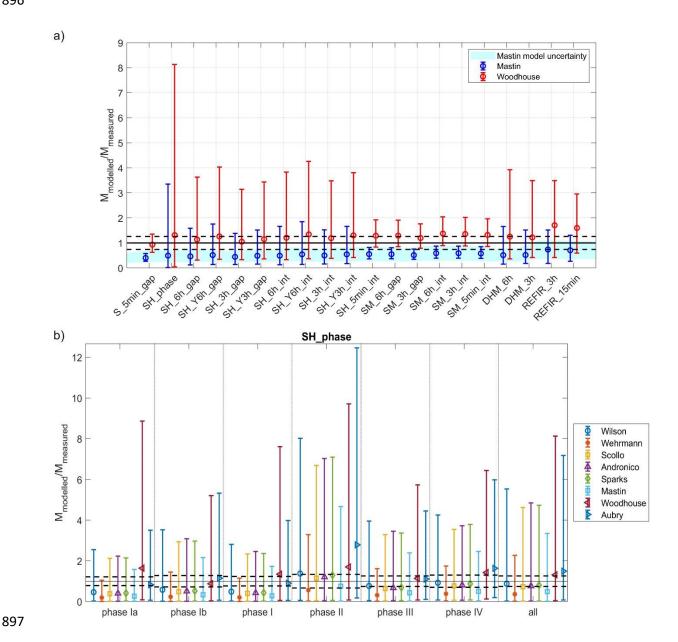


Figure 11

Ranges of uncertainty for modelled masses. a) Strategy-specific uncertainties for *Mastin* and *Woodhouse*, when modelling the complete eruption period (*all*). For most strategies, the effect of plume height errors according to equation (19) is larger than the model uncertainties (blue-shaded background for *Mastin*). b) Ranges of predicted mass uncertainties for strategy *SH_phase* for all studied eruptive phases and the complete eruption (*all*). Although depending on model and phase, for this strategy the error bars are always considerably larger than the range of measured mass, due to the large timebase.





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908 Online Resources

- 909 Online Resource 1 (.tif):
- 910 Corrected radar heights and ERA-5 wind speeds for different eruptive phases. a) phase I, b) phase II,
- 911 c) phase III, d) phase IV.
- 912 Online Resource 2 (.tif):
- Phase-specific results for five plume height strategies applied to the Wilson model. The range of
- measured erupted mass ("ground truth") is indicated with a red error bar. a) phase I, b) phase II, c)
- 915 phase III, d) phase IV.
- 916 Online Resource 3 (.tif):
- 917 Results for all models, using the REFIR strategies (REFIR_15min, REFIR_30min, REFIR_1h and
- 918 REFIR_3h), and the whole eruption (i.e, all phases) as reference period. Woodhouse and Aubry were
- 919 used with wind speeds from ERA5. Dashed horizontal lines indicate the range of measured erupted
- 920 mass.
- 921 Online Resource 4 (.tif):
- 922 Phase-specific results for all models, using the REFIR strategies (REFIR 15min, REFIR 30min,
- 923 REFIR_1h and REFIR_3h). Dashed horizontal lines indicate the range of measured erupted mass. a)
- 924 phase I, b) phase II, c) phase III, d) phase IV.
- 925 Online Resource 5 (.xlsx):
- 926 Modelled masses (in kg). Sheets are named after the plume height strategy applied. Columns show
- 927 eruptive phases. Rows show model results. Next to the best estimates, the range of uncertainty is
- 928 specified by providing the minimum (min) and maximum values (max).
- 929 Online Resource 6 (.jpg):
- 930 Congruency map for complete eruption (all).
- 931 Online Resource 7 (.jpg):
- 932 Phase-specific congruency maps for all strategies tested.
- 933 Online Resource 8 (.tif):
- 934 Phase-specific MER predictions for *Woodhouse* with *REFIR 3h*, using wind speeds of ERA 5 and ICRA.
- In addition to 1h-timed wind speeds, 3h-averaged wind speeds were tested.

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938	Declarations
939	Funding
940	TD was supported by the IRF (Rannís) PostDoctoral project grant 206527-051
941	Conflicts of interest/Competing interests
942	There are no competing interests
943	Availability of data and material
944	All data will be provided upon request to the lead author
945	Code availability
946	Not applicable
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