

**OPTIMIZATION OF TWO SIDED ASSEMBLY  
LINE BALANCING WITH RESOURCE  
CONSTRAINT**

**MUHAMMAD RAZIF BIN ABDULLAH MAKE**

**MASTER OF SCIENCE**

**UNIVERSITI MALAYSIA PAHANG**



### **SUPERVISOR'S DECLARATION**

I hereby declare that I have checked this thesis, and, in my opinion, this thesis is adequate in terms of scope and quality for the award of the degree of Master of Science.

A handwritten signature in black ink, appearing to read "DR. MOHD FADZIL FAISAE AB. RASHID".

(Supervisor's Signature)

Full Name : DR. MOHD FADZIL FAISAE AB. RASHID

Position : ASSOCIATE PROFESSOR

Date : 21/2/2022



### STUDENT'S DECLARATION

I hereby declare that the work in this thesis is based on my original work except for quotations and citations which have been duly acknowledged. I also declare that it has not been previously or concurrently submitted for any other degree at Universiti Malaysia Pahang or any other institutions.

---

(Student's Signature)

Full Name : MUHAMMAD RAZIF BIN ABDULLAH MAKE

ID Number : MMM15012

Date : 20/2/2022

**OPTIMIZATION OF TWO SIDED ASSEMBLY LINE BALANCING WITH  
RESOURCE CONSTRAINT**

**MUHAMMAD RAZIF BIN ABDULLAH MAKE**

Thesis submitted in fulfillment of the requirements  
for the award of the degree of  
Master of Science

College of Engineering  
**UNIVERSITI MALAYSIA PAHANG**

**FEBRUARY 2022**

## **ACKNOWLEDGEMENTS**

Firstly, I am grateful to the God for the blessing and gratefulness to have good health and wellbeing that were necessary to complete this project. I wish to express my sincere gratitude to my supervisor Dr. Mohd Fadzil Faisae Bin Ab. Rashid for the continuous support of my research project. His guidance helps me a lot on this research project and this thesis writing. I appreciate his support with the outstanding professional conduct.

I would like to acknowledge the Ministry of Higher Education and Universiti Malaysia Pahang for funding this research through Fundamental Research Grant Scheme number FRGS/1/2014/TK01/UMP/02/9 (RDU140103).

I also thank to my parents and my family for their support and encouragement through completing this project. Their tolerance and understanding of this project inspired me to be more confident in my capacity to achieve my objectives.

Last but not least, I would like to thank to all of my friends, who directly or indirectly supported me in completing this research project.

## ABSTRAK

Masalah pengimbangan garis pemasangan dua sisi (2S-ALB) secara praktikalnya amat berguna dalam meningkatkan pengeluaran produk dengan jumlah besar. Banyak penyelidikan telah mencadangkan pelbagai pendekatan untuk mengkaji dan mengimbangi masalah ALB yang dikenali ini. Walaupun banyak perhatian telah diberikan untuk menyelesaikan dan mengoptimumkan 2S-ALB, kebanyakan kajian menganggap stesen kerja memiliki kemampuan yang serupa. Penyelidikan ini dilaksanakan pada barisan pemasangan automotif, di mana sebahagian besar peralatan yang digunakan dalam pemasangan adalah berbeza dari satu stesen kerja ke stesen kerja yang lain. Anggapan bahawa semua stesen kerja mempunyai keupayaan yang serupa menyebabkan penggunaan sumber yang tidak cekap dalam reka bentuk barisan pemasangan. Penyelidikan ini bertujuan untuk memodelkan dan mengoptimumkan 2S-ALB dengan kekangan sumber. Selain mengoptimumkan pengimbangan barisan, model yang diusulkan juga akan meminimumkan jumlah sumber daya dalam barisan pemasangan dua sisi. Penyelidikan dimulakan dengan formulasi masalah melalui menetapkan empat objektif optimum. Pengoptimuman objektif yang dipertimbangkan adalah untuk meminimumkan bilangan stesen kerja, bilangan stesen kerja pasangan, jumlah masa terbiar dan jumlah sumber. Bagi tujuan pengoptimuman, Particle Swarm Optimization diubahsuai untuk mencari penyelesaian terbaik selain mengurangkan kebergantungan pada satu penyelesaian terbaik. Ini dilakukan dengan menggantikan penyelesaian terbaik dengan tiga penyelesaian teratas dalam proses pembiakan. Satu set masalah penanda aras untuk 2S-ALB digunakan untuk menguji cadangan Pengoptimuman melalui Modified Particle Swarm Optimization (MPSO) yang dicadangkan dalam komputasi eksperimen. Kemudian, 2S-ALB yang dicadangkan dengan model dan algoritma kekangan sumber disahkan menggunakan masalah kajian kes. Hasil eksperimen komputasi menggunakan masalah ujian penanda aras menunjukkan bahawa MPSO yang dicadangkan dapat mencari penyelesaian yang lebih baik pada 91.6%. Prestasi MPSO yang baik ini disebabkan oleh kebolehan algoritma ini mengekalkan kepelbagaiannya partikel disepanjang iterasi. Sementara itu, hasil kajian kes menunjukkan bahawa 2S-ALB yang dicadangkan dengan model kekangan sumber dan algoritma MPSO dapat digunakan untuk masalah yang sebenarnya. Di masa depan, masalah pengoptimuman pelbagai objektif akan dikaji untuk dioptimumkan bagi jenis barisan pemasangan umum yang lain.

## ABSTRACT

Two-sided assembly line balancing (2S-ALB) problems are practically useful in improving the production of large-sized high-volume products. Many research has proposed various approaches to study and balance this well-known ALB problem. Although much attention has been given to solve and optimize 2S-ALB, the majority of the research assumed the workstation has similar capabilities. This research has been conducted in an automotive assembly line, where most of the equipment used in assembly is different from one workstation to another. The assumption that all workstation has similar capabilities lead to inefficient resource utilization in assembly line design. This research aims to model and optimize 2S-ALB with resource constraints. Besides optimizing the line balancing, the proposed model also will minimize the number of resources in the two-sided assembly line. The research begins with problem formulation by establishing four optimization objectives. The considered optimization objectives were to minimize the number of workstations, number of mated-workstation, total idle time, and number of resources. For optimization purpose, Particle Swarm Optimization is modified to find the best solution besides reducing the dependencies on a single best solution. This is conducted by replacing the best solution with the top three solutions in the reproduction process. A set of benchmark problems for 2S-ALB were used to test the proposed Modified Particle Swarm Optimization (MPSO) in the computational experiment. Later, the proposed 2S-ALB with resource constraint model and algorithm was validated using a case study problem. The computational experiment result using benchmark test problems indicated that the proposed MPSO was able to search for better solution in 91.6% of the benchmark problems. The good performance of MPSO is attributed to its ability to maintain particle diversity over the iteration. Meanwhile, the case study result indicated that the proposed 2S-ALB with resource constraint model and MPSO algorithm are able to be utilized for the real problem. In the future, the multi-objective optimization problem will be considered to be optimized for other types of general assembly lines.

## TABLE OF CONTENT

### **DECLARATION**

### **TITLE PAGE**

<b>ACKNOWLEDGEMENTS</b>	<b>ii</b>
-------------------------	-----------

<b>ABSTRAK</b>	<b>iii</b>
----------------	------------

<b>ABSTRACT</b>	<b>iv</b>
-----------------	-----------

<b>TABLE OF CONTENT</b>	<b>v</b>
-------------------------	----------

<b>LIST OF TABLES</b>	<b>viii</b>
-----------------------	-------------

<b>LIST OF FIGURES</b>	<b>ix</b>
------------------------	-----------

<b>LIST OF SYMBOLS</b>	<b>x</b>
------------------------	----------

<b>LIST OF ABBREVIATIONS</b>	<b>xi</b>
------------------------------	-----------

<b>CHAPTER 1 INTRODUCTION</b>	<b>1</b>
-------------------------------	----------

1.1    Project Background	1
---------------------------	---

1.2    Problem Statement	2
--------------------------	---

1.3    Objectives	3
-------------------	---

1.4    Scope of Study	4
-----------------------	---

1.5    Thesis Overview	4
------------------------	---

<b>CHAPTER 2 LITERATURE REVIEW</b>	<b>5</b>
------------------------------------	----------

2.1    Introduction	5
---------------------	---

2.2    Two-sided Assembly Line Balancing (2S-ALB)	7
---	---

2.3    Optimization Method	9
----------------------------	---

2.3.1    Genetic Algorithm	11
----------------------------	----

2.3.2    Ant Colony Optimization	13
----------------------------------	----

2.3.3    Simulated Annealing	14
------------------------------	----

2.3.4	Other Optimization Methods	15
2.3.5	Comparison of Different Optimization Methods	16
2.4	Objective Function	18
2.4.1	Minimizing Workstation Number	20
2.4.2	Minimizing Mated Station Number	21
2.4.3	Minimizing Line Length	23
2.4.4	Minimizing Cycle Time	24
2.4.5	Workload / Task Smoothness	26
2.4.6	Other Objective Functions	28
2.5	Constraint	28
2.5.1	Zoning Constraint	30
2.5.2	Cycle Time Constraint	32
2.5.3	Operation Direction Constraint	33
2.5.4	Other Constraint	35
2.6	Discrete Event Simulation	38
2.7	Research Potential	40
<b>CHAPTER 3 METHODOLOGY</b>		<b>42</b>
3.1	Introduction	42
3.2	Methodology	42
3.3	2S-ALB with Resource Constraint Problem Modelling	44
3.3.1	Precedence Relation	45
3.3.2	Computational Data Presentation	46
3.3.3	Multi-objective Modelling & Execution	47
3.3.4	Numerical Example	49
3.4	Modified PSO	52

3.5	Computational Experiment	56
3.6	Case Study	57
3.6.1	Discrete Event Simulation	59
<b>CHAPTER 4 RESULTS AND DISCUSSION</b>		<b>62</b>
4.1	Introduction	62
4.2	Optimization Result for Benchmark Problem	62
4.3	Result for Case Study	69
4.3.1	Result of Case Study Simulation	71
4.4	Analysis & Discussion	74
<b>CHAPTER 5 CONCLUSION</b>		<b>77</b>
5.1	Research Summary	77
5.2	Research Contribution	77
5.3	Research Conclusion	78
5.4	Recommendation	78
<b>REFERENCES</b>		<b>80</b>

## REFERENCES

- Abdullah Make, M. R., Ab. Rashid, M. F. F., & Razali, M. M. (2017). A review of two-sided assembly line balancing problem. *The International Journal of Advanced Manufacturing Technology*, 89(5), 1743-1763. doi:10.1007/s00170-016-9158-3
- Adnan, M. A., & Razzaque, M. A. (2013, 20-22 March 2013). *A comparative study of Particle Swarm Optimization and Cuckoo Search techniques through problem-specific distance function*. Paper presented at the 2013 International Conference of Information and Communication Technology (ICoICT).
- Ağpak, K., Yegül, M. F., & Gökçen, H. (2012). Two-sided U-type assembly line balancing problem. *International Journal of Production Research*, 50(18), 5035-5047. doi:10.1080/00207543.2011.631599
- Ağpak, K., & Zolfaghari, S. (2015). Mathematical models for parallel two-sided assembly line balancing problems and extensions. *International Journal of Production Research*, 53(4), 1242-1254. doi:10.1080/00207543.2014.955218
- Alakaş, H. (2021). General resource-constrained assembly line balancing problem: conjunction normal form based constraint programming models. *Soft Computing*, 25. doi:10.1007/s00500-021-05602-x
- Alavidoost, M. H., Babazadeh, H., & Sayyari, S. T. (2016). An interactive fuzzy programming approach for bi-objective straight and U-shaped assembly line balancing problem. *Applied Soft Computing*, 40, 221-235. doi:<http://dx.doi.org/10.1016/j.asoc.2015.11.025>
- Amorim-Lopes, M., Guimarães, L., Alves, J., & Almada-Lobo, B. (2021). Improving picking performance at a large retailer warehouse by combining probabilistic simulation, optimization, and discrete-event simulation. *International Transactions in Operational Research*, 28(2), 687–715. <https://doi.org/https://doi.org/10.1111/itor.12852>
- Armin, S. (1993). Data of Assembly Line Balancing Problems. *Operations Research*.
- Aydin, M. E., & Fogarty, T. C. (2004). A Distributed Evolutionary Simulated Annealing Algorithm for Combinatorial Optimisation Problems. *Journal of Heuristics*, 10(3), 269-292. doi:10.1023/B:HEUR.0000026896.44360.f9
- Baril, C., Gascon, V., Miller, J., & Côté, N. (2016). Use of a discrete-event simulation in a Kaizen event: A case study in healthcare. *European Journal of Operational Research*, 249(1), 327-339. doi:<https://doi.org/10.1016/j.ejor.2015.08.036>
- Bartholdi, J. J. (1993). Balancing two-sided assembly lines: a case study. *International Journal of Production Research*, 31(10), 2447-2461. doi:10.1080/00207549308956868

- Baykasoglu, A. (2006). Multi-rule Multi-objective Simulated Annealing Algorithm for Straight and U Type Assembly Line Balancing Problems. *Journal of Intelligent Manufacturing*, 17(2), 217-232. doi:10.1007/s10845-005-6638-y
- Baykasoglu, A., & Dereli, T. (2008). Two-sided assembly line balancing using an ant-colony-based heuristic. *The International Journal of Advanced Manufacturing Technology*, 36(5-6), 582-588. doi:10.1007/s00170-006-0861-3
- Baykasoglu, A., Ozbakur, L., Gorkemli, L., & Gorkemli, B. (2009, 6-9 July 2009). *Balancing parallel assembly lines via Ant Colony Optimization*. Paper presented at the Computers & Industrial Engineering, 2009. CIE 2009. International Conference on.
- Becker, C., & Scholl, A. (2006). A survey on problems and methods in generalized assembly line balancing. *European Journal of Operational Research*, 168(3), 694-715. doi:<http://dx.doi.org/10.1016/j.ejor.2004.07.023>
- Boysen, N., Fliedner, M., & Scholl, A. (2007). A classification of assembly line balancing problems. *European Journal of Operational Research*, 183(2), 674-693. doi:<http://dx.doi.org/10.1016/j.ejor.2006.10.010>
- Boysen, N., Fliedner, M., & Scholl, A. (2009). Sequencing mixed-model assembly lines: Survey, classification and model critique. *European Journal of Operational Research*, 192(2), 349-373. doi:<http://dx.doi.org/10.1016/j.ejor.2007.09.013>
- Buyukozkan, K., Kucukkoc, I., Satoglu, S. I., & Zhang, D. Z. (2016). Lexicographic bottleneck mixed-model assembly line balancing problem: Artificial bee colony and tabu search approaches with optimised parameters. *Expert Systems with Applications*, 50, 151-166. doi:<http://dx.doi.org/10.1016/j.eswa.2015.12.018>
- Caggiano, A., Marzano, A., & Teti, R. (2016). Resource Efficient Configuration of an Aircraft Assembly Line. *Procedia CIRP*, 41, 236-241. doi:<http://dx.doi.org/10.1016/j.procir.2015.12.130>
- Çerçioğlu, H., Özcan, U., Gökcen, H., & Toklu, B. (2009). A simulated annealing approach for Parallel Assembly Line Balancing Problem. *Journal of the Faculty of Engineering and Architecture of Gazi University*, 24(2), 331-341.
- Chen, S.-F., & Liu, Y.-J. (2001). An adaptive genetic assembly-sequence planner. *International Journal of Computer Integrated Manufacturing*, 14(5), 489-500. doi:10.1080/09511920110034987
- Chiang, W.-C., Urban, T. L., & Luo, C. (2015). Balancing stochastic two-sided assembly lines. *International Journal of Production Research*, 1-19. doi:10.1080/00207543.2015.1029084
- Chutima, P., & Chimklai, P. (2012). Multi-objective two-sided mixed-model assembly line balancing using particle swarm optimisation with negative knowledge. *Computers & Industrial Engineering*, 62(1), 39-55. doi:<http://dx.doi.org/10.1016/j.cie.2011.08.015>

- Chutima, P., & Naruemitwong, W. (2014). A Pareto biogeography-based optimisation for multi-objective two-sided assembly line sequencing problems with a learning effect. *Computers & Industrial Engineering*, 69, 89-104. doi:<http://dx.doi.org/10.1016/j.cie.2014.01.001>
- Dagkakis, G., Rotondo, A., & Heavey, C. (2019). Embedding optimization with deterministic discrete event simulation for assignment of cross-trained operators: An assembly line case study. *Computers & Operations Research*, 111, 99–115. <https://doi.org/https://doi.org/10.1016/j.cor.2019.06.008>
- Ding, F.-Y., Zhu, J., & Sun, H. (2006). Comparing two weighted approaches for sequencing mixed-model assembly lines with multiple objectives. *International Journal of Production Economics*, 102(1), 108-131. doi:<http://dx.doi.org/10.1016/j.ijpe.2005.02.007>
- Dorigo, M., & Blum, C. (2005). Ant colony optimization theory: A survey. *Theoretical Computer Science*, 344(2–3), 243-278. doi:<http://dx.doi.org/10.1016/j.tcs.2005.05.020>
- Erel, E., & Sarin, S. C. (1998). A survey of the assembly line balancing procedures. *Production Planning & Control*, 9(5), 414-434. doi:[10.1080/095372898233902](https://doi.org/10.1080/095372898233902)
- Esmaeilbeigi, R., Naderi, B., & Charkhgard, P. (2015). The type E simple assembly line balancing problem: A mixed integer linear programming formulation. *Computers & Operations Research*, 64, 168-177. doi:<http://dx.doi.org/10.1016/j.cor.2015.05.017>
- García-Villoria, A., & Pastor, R. (2013). Erratum to “A solution procedure for type E simple assembly line balancing problem”. *Computers & Industrial Engineering*, 66(1), 201-202. doi:<http://dx.doi.org/10.1016/j.cie.2013.05.015>
- Gökçen, H., Ağpak, K., & Benzer, R. (2006). Balancing of parallel assembly lines. *International Journal of Production Economics*, 103(2), 600-609. doi:<http://dx.doi.org/10.1016/j.ijpe.2005.12.001>
- Gonçalves, J. F., & de Almeida, J. R. (2002). A Hybrid Genetic Algorithm for Assembly Line Balancing. *Journal of Heuristics*, 8(6), 629-642. doi:[10.1023/a:1020377910258](https://doi.org/10.1023/a:1020377910258)
- Hazır, Ö., & Dolgui, A. (2015). A decomposition based solution algorithm for U-type assembly line balancing with interval data. *Computers & Operations Research*, 59, 126-131. doi:<http://dx.doi.org/10.1016/j.cor.2015.01.010>
- Hu, X., Wu, E., & Jin, Y. (2008). A station-oriented enumerative algorithm for two-sided assembly line balancing. *European Journal of Operational Research*, 186(1), 435-440. doi:<http://dx.doi.org/10.1016/j.ejor.2007.01.022>
- Jung, W.-K., Kim, H., Park, Y.-C., Lee, J.-W., & Suh, E. S. (2020). Real-time data-driven discrete-event simulation for garment production lines. *Production Planning & Control*, 1–12. <https://doi.org/10.1080/09537287.2020.1830194>

- Kennedy, J., & Eberhart, R. (1995, Nov/Dec 1995). *Particle swarm optimization*. Paper presented at the Neural Networks, 1995. Proceedings., IEEE International Conference on.
- Khorasanian, D., Hejazi, S. R., & Moslehi, G. (2013). Two-sided assembly line balancing considering the relationships between tasks. *Computers & Industrial Engineering*, 66(4), 1096-1105. doi:<http://dx.doi.org/10.1016/j.cie.2013.08.006>
- Kim, Y. K., Kim, Y., & Kim, Y. J. (2000). Two-sided assembly line balancing: A genetic algorithm approach. *Production Planning & Control*, 11(1), 44-53. doi:[10.1080/095372800232478](https://doi.org/10.1080/095372800232478)
- Kim, Y. K., Song, W. S., & Kim, J. H. (2009). A mathematical model and a genetic algorithm for two-sided assembly line balancing. *Computers & Operations Research*, 36(3), 853-865. doi:<http://dx.doi.org/10.1016/j.cor.2007.11.003>
- Kriengkorakot, N., & Pianthong, N. (2007). The assembly line balancing problem. *KKU Engineering Journal*, 34(2), 133-140.
- Kucukkoc, I., Karaoglan, A. D., & Yaman, R. (2013). Using response surface design to determine the optimal parameters of genetic algorithm and a case study. *International Journal of Production Research*, 51(17), 5039-5054. doi:[10.1080/00207543.2013.784411](https://doi.org/10.1080/00207543.2013.784411)
- Kucukkoc, I., & Zhang, D. Z. (2014a). Mathematical model and agent based solution approach for the simultaneous balancing and sequencing of mixed-model parallel two-sided assembly lines. *International Journal of Production Economics*, 158, 314-333. doi:<http://dx.doi.org/10.1016/j.ijpe.2014.08.010>
- Kucukkoc, I., & Zhang, D. Z. (2014b). Simultaneous balancing and sequencing of mixed-model parallel two-sided assembly lines. *International Journal of Production Research*, 52(12), 3665-3687. doi:[10.1080/00207543.2013.879618](https://doi.org/10.1080/00207543.2013.879618)
- Kucukkoc, I., & Zhang, D. Z. (2015a). Balancing of parallel U-shaped assembly lines. *Computers & Operations Research*, 64, 233-244. doi:<http://dx.doi.org/10.1016/j.cor.2015.05.014>
- Kucukkoc, I., & Zhang, D. Z. (2015b). A mathematical model and genetic algorithm-based approach for parallel two-sided assembly line balancing problem. *Production Planning & Control*, 26(11), 874-894. doi:[10.1080/09537287.2014.994685](https://doi.org/10.1080/09537287.2014.994685)
- Kucukkoc, I., & Zhang, D. Z. (2015c). Type-E parallel two-sided assembly line balancing problem: Mathematical model and ant colony optimisation based approach with optimised parameters. *Computers & Industrial Engineering*, 84, 56-69. doi:<http://dx.doi.org/10.1016/j.cie.2014.12.037>
- Lam, N. T., Toi, L. M., Tuyen, V. T. T., & Hien, D. N. (2016). Lean Line Balancing for an Electronics Assembly Line. *Procedia CIRP*, 40, 437-442. doi:<http://dx.doi.org/10.1016/j.procir.2016.01.089>

- Lang, S., Behrendt, F., Lanzerath, N., Reggelin, T., & Müller, M. (2020). Integration of Deep Reinforcement Learning and Discrete-Event Simulation for Real-Time Scheduling of a Flexible Job Shop Production. *2020 Winter Simulation Conference (WSC)*, 3057–3068. <https://doi.org/10.1109/WSC48552.2020.9383997>
- Lapierre, S. D., & Ruiz, A. B. (2004). Balancing Assembly Lines: An Industrial Case Study. *The Journal of the Operational Research Society*, 55(6), 589-597.
- Lee, T. O., Kim, Y., & Kim, Y. K. (2001). Two-sided assembly line balancing to maximize work relatedness and slackness. *Computers & Industrial Engineering*, 40(3), 273-292. doi:[http://dx.doi.org/10.1016/S0360-8352\(01\)00029-8](http://dx.doi.org/10.1016/S0360-8352(01)00029-8)
- Li, S.-x., & Shan, H.-b. (2008, 1-3 Sept. 2008). *GSSA and ACO for assembly sequence planning: A comparative study*. Paper presented at the Automation and Logistics, 2008. ICAL 2008. IEEE International Conference on.
- Li, Y., Yang, X., Wu, J., Sun, H., Guo, X., & Zhou, L. (2021). Discrete-event simulations for metro train operation under emergencies: A multi-agent based model with parallel computing. *Physica A: Statistical Mechanics and Its Applications*, 573, 125964. [https://doi.org/https://doi.org/10.1016/j.physa.2021.125964](https://doi.org/10.1016/j.physa.2021.125964)
- Mahfoud, S. W., & Goldberg, D. E. (1995). Parallel recombinative simulated annealing: A genetic algorithm. *Parallel Computing*, 21(1), 1-28. doi:[http://dx.doi.org/10.1016/0167-8191\(94\)00071-H](http://dx.doi.org/10.1016/0167-8191(94)00071-H)
- Manavizadeh, N., Hosseini, N.-s., Rabbani, M., & Jolai, F. (2013). A Simulated Annealing algorithm for a mixed model assembly U-line balancing type-I problem considering human efficiency and Just-In-Time approach. *Computers & Industrial Engineering*, 64(2), 669-685. doi:<http://dx.doi.org/10.1016/j.cie.2012.11.010>
- Melman, G. J., Parlikad, A. K., & Cameron, E. A. B. (2021). Balancing scarce hospital resources during the COVID-19 pandemic using discrete-event simulation. *Health Care Management Science*, 24(2), 356–374. <https://doi.org/10.1007/s10729-021-09548-2>
- Merengo, C., Nava, F., & Pozzetti, A. (1999). Balancing and sequencing manual mixed-model assembly lines. *International Journal of Production Research*, 37(12), 2835-2860. doi:[10.1080/002075499190545](https://doi.org/10.1080/002075499190545)
- Micieta, B., & Stollmann, V. (2011). Assembly Line Balancing (pp. 257-264): DAAAM International
- Moon, I., Logendran, R., & Lee, J. (2009). Integrated assembly line balancing with resource restrictions. *International Journal of Production Research*, 47(19), 5525-5541. doi:[10.1080/00207540802089876](https://doi.org/10.1080/00207540802089876)
- Mosadegh, H., Zandieh, M., & Ghomi, S. M. T. F. (2012). Simultaneous solving of balancing and sequencing problems with station-dependent assembly times for

- mixed-model assembly lines. *Applied Soft Computing*, 12(4), 1359-1370. doi:<http://dx.doi.org/10.1016/j.asoc.2011.11.027>
- Naderi, B., Azab, A., & Borooshan, K. (2019). A realistic multi-manned five-sided mixed-model assembly line balancing and scheduling problem with moving workers and limited workspace. *International Journal of Production Research*, 57(3), 643-661. doi:10.1080/00207543.2018.1476786
- Ogan, D., & Azizoglu, M. (2015). A branch and bound method for the line balancing problem in U-shaped assembly lines with equipment requirements. *Journal of Manufacturing Systems*, 36, 46-54. doi:<http://dx.doi.org/10.1016/j.jmsy.2015.02.007>
- Özbakır, L., & Tapkan, P. (2011). Bee colony intelligence in zone constrained two-sided assembly line balancing problem. *Expert Systems with Applications*, 38(9), 11947-11957. doi:<http://dx.doi.org/10.1016/j.eswa.2011.03.089>
- Özcan, U. (2010). Balancing stochastic two-sided assembly lines: A chance-constrained, piecewise-linear, mixed integer program and a simulated annealing algorithm. *European Journal of Operational Research*, 205(1), 81-97. doi:<http://dx.doi.org/10.1016/j.ejor.2009.11.033>
- Özcan, U., Gökçen, H., & Toklu, B. (2010). Balancing parallel two-sided assembly lines. *International Journal of Production Research*, 48(16), 4767-4784. doi:10.1080/00207540903074991
- Özcan, U., & Toklu, B. (2009a). Balancing of mixed-model two-sided assembly lines. *Computers & Industrial Engineering*, 57(1), 217-227. doi:<http://dx.doi.org/10.1016/j.cie.2008.11.012>
- Özcan, U., & Toklu, B. (2009b). Multiple-criteria decision-making in two-sided assembly line balancing: A goal programming and a fuzzy goal programming models. *Computers & Operations Research*, 36(6), 1955-1965. doi:<http://dx.doi.org/10.1016/j.cor.2008.06.009>
- Özcan, U., & Toklu, B. (2010). Balancing two-sided assembly lines with sequence-dependent setup times. *International Journal of Production Research*, 48(18), 5363-5383. doi:10.1080/00207540903140750
- Pearce, B. W. (2015). *A Study on General Line Balancing Modeling Method and Techniques*. (Doctor of Philosophy Industrial Engineering), Clemson University.
- Purnomo, H. D., & Wee, H.-M. (2014). Maximizing production rate and workload balancing in a two-sided assembly line using Harmony Search. *Computers & Industrial Engineering*, 76, 222-230. doi:<http://dx.doi.org/10.1016/j.cie.2014.07.010>
- Purnomo, H. D., Wee, H.-M., & Rau, H. (2013). Two-sided assembly lines balancing with assignment restrictions. *Mathematical and Computer Modelling*, 57(1-2), 189-199. doi:<http://dx.doi.org/10.1016/j.mcm.2011.06.010>

- Rashid, M. F. F., Hutabarat, W., & Tiwari, A. (2011). A review on assembly sequence planning and assembly line balancing optimisation using soft computing approaches. *The International Journal of Advanced Manufacturing Technology*, 59(1), 335-349. doi:10.1007/s00170-011-3499-8
- Roshani, A., Fattahi, P., Roshani, A., Salehi, M., & Roshani, A. (2012). Cost-oriented two-sided assembly line balancing problem: A simulated annealing approach. *International Journal of Computer Integrated Manufacturing*, 25(8), 689-715. doi:10.1080/0951192X.2012.664786
- Rubiano-Ovalle, Ó., & Arroyo-Almanza, A. (2009). Solving a Two-Sided Assembly Line Balancing Problem using Memetic Algorithms. *Ingeniería y Universidad*, 13, 267-280.
- Sabuncuoglu, I., Erel, E., & Tanyer, M. (2000). Assembly line balancing using genetic algorithms. *Journal of Intelligent Manufacturing*, 11(3), 295-310. doi:10.1023/a:1008923410076
- Saidani, M., Kim, H., & Kim, J. (2021). Designing optimal COVID-19 testing stations locally: A discrete event simulation model applied on a university campus. *PLOS ONE*, 16(6), e0253869. <https://doi.org/10.1371/journal.pone.0253869>
- Salveson, M. E. (1955). The assembly line balancing problem. *Journal of Industrial Engineering*, 6(3), 18-25.
- Scholl, A., & Becker, C. (2006). State-of-the-art exact and heuristic solution procedures for simple assembly line balancing. *European Journal of Operational Research*, 168(3), 666-693. doi:<http://dx.doi.org/10.1016/j.ejor.2004.07.022>
- Sepahi, A., & Naini, S. G. J. (2016). Two sided assembly line balancing problem with parallel performing properties. *Applied Mathematical Modelling*. doi:<http://dx.doi.org/10.1016/j.apm.2016.02.022>
- Shan, H., Li, S., Gong, D., & Lou, P. (2006, 6-7 Nov. 2006). *Genetic simulated annealing algorithm-based assembly sequence planning*. Paper presented at the Technology and Innovation Conference, 2006. ITIC 2006. International.
- Shuang, B., Chen, J., & Li, Z. (2008). Microrobot based micro-assembly sequence planning with hybrid ant colony algorithm. *The International Journal of Advanced Manufacturing Technology*, 38(11), 1227-1235. doi:10.1007/s00170-007-1165-y
- Simaria, A. S., & Vilarinho, P. M. (2004). A genetic algorithm based approach to the mixed-model assembly line balancing problem of type II. *Computers & Industrial Engineering*, 47(4), 391-407. doi:<http://dx.doi.org/10.1016/j.cie.2004.09.001>
- Simaria, A. S., & Vilarinho, P. M. (2009). 2-ANTBAL: An ant colony optimisation algorithm for balancing two-sided assembly lines. *Computers & Industrial Engineering*, 56(2), 489-506. doi:<http://dx.doi.org/10.1016/j.cie.2007.10.007>

- Sivasankaran, P., & Shahabudeen, P. (2014). Literature review of assembly line balancing problems. *The International Journal of Advanced Manufacturing Technology*, 73(9), 1665-1694. doi:10.1007/s00170-014-5944-y
- Sotskov, Y. N., Dolgui, A., Lai, T.-C., & Zatsiupa, A. (2015). Enumerations and stability analysis of feasible and optimal line balances for simple assembly lines. *Computers & Industrial Engineering*, 90, 241-258. doi:<http://dx.doi.org/10.1016/j.cie.2015.08.018>
- Spinellis, D. D., & Papadopoulos, C. T. (2000). A simulated annealing approach for buffer allocation in reliable production lines. *Annals of Operations Research*, 93(1), 373-384. doi:10.1023/a:1018984125703
- Storn, R., & Price, K. (1997). Differential Evolution – A Simple and Efficient Heuristic for global Optimization over Continuous Spaces. *Journal of Global Optimization*, 11(4), 341-359. doi:10.1023/a:1008202821328
- Sungur, B., & Yavuz, Y. (2015). Assembly line balancing with hierarchical worker assignment. *Journal of Manufacturing Systems*, 37, Part 1, 290-298. doi:<http://dx.doi.org/10.1016/j.jmsy.2014.08.004>
- Taha, R. B., El-Kharbotly, A. K., Sadek, Y. M., & Afia, N. H. (2011). A Genetic Algorithm for solving two-sided assembly line balancing problems. *Ain Shams Engineering Journal*, 2(3–4), 227-240. doi:<http://dx.doi.org/10.1016/j.asej.2011.10.003>
- Tapkan, P., Ozbakir, L., & Baykasoglu, A. (2012). Modeling and solving constrained two-sided assembly line balancing problem via bee algorithms. *Applied Soft Computing*, 12(11), 3343-3355. doi:<http://dx.doi.org/10.1016/j.asoc.2012.06.003>
- Tapkan, P., Özbakır, L., & Baykasoglu, A. (2016). Bee algorithms for parallel two-sided assembly line balancing problem with walking times. *Applied Soft Computing*, 39, 275-291. doi:<http://dx.doi.org/10.1016/j.asoc.2015.11.017>
- Tasan, S. O., & Tunali, S. (2007). A review of the current applications of genetic algorithms in assembly line balancing. *Journal of Intelligent Manufacturing*, 19(1), 49-69. doi:10.1007/s10845-007-0045-5
- Tuncel, G., & Aydin, D. (2014). Two-sided assembly line balancing using teaching–learning based optimization algorithm. *Computers & Industrial Engineering*, 74, 291-299. doi:<http://dx.doi.org/10.1016/j.cie.2014.06.006>
- Vilarinho, P. M., & Simaria, A. S. (2002). A two-stage heuristic method for balancing mixed-model assembly lines with parallel workstations. *International Journal of Production Research*, 40(6), 1405-1420. doi:10.1080/00207540110116273
- Wang, J. F., Liu, J. H., & Zhong, Y. F. (2005). A novel ant colony algorithm for assembly sequence planning. *The International Journal of Advanced Manufacturing Technology*, 25(11), 1137-1143. doi:10.1007/s00170-003-1952-z

- Wei, N.-C., & Chao, I. M. (2011). A solution procedure for type E simple assembly line balancing problem. *Computers & Industrial Engineering*, 61(3), 824-830. doi:<http://dx.doi.org/10.1016/j.cie.2011.05.015>
- Xiaofeng, H., Erfei, W., Jinsong, B., & Ye, J. (2010). A branch-and-bound algorithm to minimize the line length of a two-sided assembly line. *European Journal of Operational Research*, 206(3), 703-707. doi:<http://dx.doi.org/10.1016/j.ejor.2010.02.034>
- Yang, X.-S. (2010). *Engineering Optimization An Introduction with Metaheuristic Applications*: John Wiley & Sons, Inc., Hoboken, New Jersey.
- Yuan, B., Zhang, C., Shao, X., & Jiang, Z. (2015). An effective hybrid honey bee mating optimization algorithm for balancing mixed-model two-sided assembly lines. *Computers & Operations Research*, 53, 32-41. doi:<http://dx.doi.org/10.1016/j.cor.2014.07.011>
- Zacharia, P. T., & Nearchou, A. C. (2013). A meta-heuristic algorithm for the fuzzy assembly line balancing type-E problem. *Computers & Operations Research*, 40(12), 3033-3044. doi:<http://dx.doi.org/10.1016/j.cor.2013.07.012>
- Zhang, Y., Cassandras, C. G., Li, W., & Mosterman, P. J. (2018). A Discrete-Event and Hybrid Simulation Framework Based on SimEvents for Intelligent Transportation System Analysis. *IFAC-PapersOnLine*, 51(7), 323–328. <https://doi.org/https://doi.org/10.1016/j.ifacol.2018.06.320>
- Zhang, Z.-q., Cheng, W.-m., Tang, L.-s., & Zhong, B. (2007, 20-22 Aug. 2007). *Ant Algorithm with Summation Rules for Assembly Line Balancing Problem*. Paper presented at the Management Science and Engineering, 2007. ICMSE 2007. International Conference on.
- Zhao, Y. Z., & de Souza, R. (2000). Genetic Production Line-Balancing for the Hard Disk Drive Industry. *The International Journal of Advanced Manufacturing Technology*, 16(4), 297-302. doi:<10.1007/s00170005016>