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# A study of error diversity in robotic swarms for task partitioning in foraging tasks

Edgar Buchanan  $^{1,\ast}$ , Kieran Alden  $^1$ , Andrew Pomfret  $^1$ , Jon Timmis  $^2$ , and Andy M. Tyrrell  $^{1\star}$ 

<sup>1</sup>School of Physics, Engineering and Technology, University of York, UK <sup>2</sup>School of Computer Science, University of Sunderland, UK

Correspondence\*: Corresponding Author edgar.buchanan@york.ac.uk

# 2 ABSTRACT

1

3 Often in swarm robotics, an assumption is made that all robots in the swarm behave the same and will have a similar (if not the same) error model. However, in reality this is not the case and 4 5 this lack of uniformity in the error model, and other operations, can lead to various emergent 6 behaviours. This paper considers the impact of the error model and compares robots in a swarm that operate using the same error model (uniform error) against each robot in the swarm having a 7 different error model (thus introducing error diversity). Experiments are presented in the context 8 of a foraging task. Simulation and physical experimental results show the importance of the error 9 model and diversity in achieving expected swarm behaviour. 10

11 Keywords: swarm robotics, fault-tolerance, error diversity, task partitioning, foraging

# **1 INTRODUCTION**

Robot swarms are capable of performing different tasks in an efficient and decentralized way, in part, due to their high level of parallelization. In the past, swarm robotic systems were assumed to be inherently robust to failures due to their high degree of robot redundancy. However, Winfield and Nembrini (2006) demonstrated that this is not always the case, and that specific processes must be introduced to increase the robustness of the swarm. Bjerknes and Winfield (2012) demonstrated that in various scenarios, specific partial failures in robots can lead to task degradation or, in the worst case, the task not being achieved.

18 Fundamental mechanisms to achieve robust fault-tolerant swarm robotic systems, have been considered by different authors including detecting faults (Tarapore et al., 2015; Christensen et al., 2009), diagnosing 19 the fault type (Keeffe et al., 2017; Li and Parker, 2007) or recovering from the fault (Humza et al., 2009; 20 21 Timmis et al., 2010), or a combination of all of these fault-tolerant methods (Parker, 1998; Parker and 22 Kannan, 2006). However, in all of these works, authors classify the robots according to their behaviour i.e. a robot being either faulty or non-faulty, where faulty robots exhibit abnormal behaviour compared with 23 non-faulty robots. However, in reality, it is often hard to distinguish between a faulty and non-faulty robot 24 25 due to the diversity of errors across the swarm.

The importance of considering error diversity in swarm robotics can be summarized in three points. 1) It is possible to reduce the reality gap between swarm behaviours in simulation and the swarm behaviours in hardware. 2) The error non-diversity could lead to false positive results, as well as missing critical faults that ultimately led to failures. 3) It is important for each robot to learn and adapt to its own inherent error inthis way, the robot swarm will exhibit better performance.

To the best of the authors' knowledge, there is no literature where diversity in terms of levels of error 31 is considered in fault tolerance experiments. Most related research examines diversity across the swarm 32 from an evolutionary perspective, where controllers can be evolved independently for each robot in the 33 swarm. For example, reinforcement learning has been used to train task-specialized robots where each 34 robot in the swarm learns to perform a specific task (Balch, 1998; Li et al., 2003; Balch, 2005) or tasks have 35 been previously allocated to robot members (Zhang et al., 2008). Robot controllers are generally evolved 36 with two methods: genetically homogeneous or genetically heterogeneous (Bongard, 2000; Mitchell A. 37 Potter, Lisa A. Meeden, 2001; Trianni and Nolfi, 2011; Tuci, 2014; Hart et al., 2018). In the homogeneous 38 method, the controller is expressed as a single genotype which is then cloned to each robot in the swarm. 39 With respect to the heterogeneous method, each robot has its own genotype and after evolution, each 40 robot has a specific role in the task. Despite this work on controller-heterogeneous swarm systems, there 41 is no research that considers the appropriate level of error for each robot during the simulation and its 42 impact on the performance of the swarm in simulation and in hardware. In this paper, we identify and 43 study the discrepancy of results when degrees of diversity of error are considered, referred in this paper as 44 heterogeneous error or if all the robots share the same degree of error they are referred to homogeneous 45 error. 46

The task considered in this paper is task partitioning in foraging. Task partitioning, first observed in biological systems (Ratnieks and Anderson, 1999), has been used in the swarm robotics context to prevent bottlenecks close to the home area where the items are deposited Goldberg and Matarie (2001); Brutschy et al. (2014); Pini et al. (2011). Other approaches such as Pini et al. (2013, 2014); Buchanan et al. (2016) have focused on fault-tolerance in order to increase performance when the dead-reckoning error is present in a robot. Task partitioning has been also used to study the effect of task decomposition on emergent swarm intelligence (Harwell et al., 2020).

Task partitioning is a technique that consists of dividing a single task into multiple smaller subtasks, with 54 the objective to reduce the amount of distance travelled by each robot and hence decreasing the error in 55 56 dead reckoning. A robot finds an item in the environment and transports the item towards the home area for a short distance referred to as Partition Length (P). Then, the item is exchanged by either leaving the 57 item on the floor for a different robot to collect (indirect transfer) or waiting for the second robot to receive 58 the item directly from the first robot (direct transfer). Since the robots are travelling a shorter distance P59 compared to the total distance between the home area and the items source, the dead-reckoning is smaller. 60 The amount of distance P depends on the approach taken. 61

62 The experimental framework in this paper follows a top-down approach from the macro to the micro 63 perspective, combined with three layers of abstraction: emulation, simulation and hardware.

In the first stage, emulation, an ensemble of different machine learning techniques is trained with a dataset generated from latin-hypercube sampling in simulations. The main advantage of using emulation is to save time and computation resources, compromising the resolution of the simulation. In other words, the emulation is used to explore the experiments from a macro or global perspective which is only concerned with the behaviour of the swarm as a whole. An emulation is generated for each strategy with each error type. The second and third stages, simulation and hardware, are studies from the micro or local perspective which is concerned with the contribution of each robot to the task. This aids in obtaining a comprehensive

72 understanding of the behaviour of the swarm.

- 73 The contributions are summarized as follows:
- demonstration that the assumption made that all the robots in a simulated robotic swarm shared the
   same error model can lead to unexpected swarm behaviours when testing the behaviour with physical
   robots where each robot experiences a different error.
- difference in behaviours introduced by the error diversity can be mitigated by having each robot learn
   the task according to the success of its performance, thus reducing errors for all robots.
- 79 The hypotheses explored in this paper are as follows:
- 80 1. the consideration of error diversity leads to different correlation values than non-diversity.
- 81 2. each robot adapts differently to its inherent error.

The rest of the paper is organized as follows. In section 2, a case study is presented and each task partitioning
strategy is described. The methodology followed in the experiments for this paper is described in section 3.
Experiments and comments on results are presented in section 4, and section 5 provides the summary and
conclusions.

# 2 CASE STUDY: FORAGING TASK PARTITIONING STRATEGIES

Foraging with dead-reckoning as navigation is used as a task to study the impact of the error diversity anduniformity across the robots in the swarm to the behaviour and performance of the swarm.

88 Within a simple foraging task, a group of robots explore the environment searching for items to collect. 89 Then, after an item is found, the position is recorded by the robot and finally, the robot transports the item 90 towards the home area. For this paper single home area, however, this work could be used for multiple 91 places home (Lu et al., 2018).

Due to systematic and unsystematic errors in dead-reckoning navigation, the real-time position is often inaccurate leading to an error in the positioning estimation. Error accumulates as a robot travels, which in turn affects the estimated item position. As a consequence, when the robot attempts to go back to where it found the last item, in order to collect further items, the robot reaches a different location. One simple way to mitigate this error is to partition the distance travelled by each individual robot.

In this paper, two task partitioning foraging strategies are used to examine the effect of error diversity 97 and uniformity. The objective of this approach is to compare traditional foraging with a strategy where 98 robots learn to divide the task into multiple smaller tasks, depending on the success, or otherwise, of item 99 collection. Different emergent behaviours are expected to appear when error diversity and uniformity are 100 considered for each strategy. In the first part of this section the foraging task is described and the first 101 strategy, Non-partitioning Strategy (NPS) (Pini et al., 2011), is introduced. A second strategy is then 102 described Dynamic Partitioning Strategy (DPS) (Buchanan et al., 2016), where the number of partitions is 103 defined by a penalty and reward mechanism. 104



**Figure 1.** Foraging arena (left) and finite state machine used by the robots (right). Left: the arena has a rectangular shape defined by the width (w) and length (l). The distance between home area and items source is represented by d.  $P_i$  represents the individual partition length for robot i. Right: Non-partitioning strategy finite state machine composed of three states: *explore*, go to nest and go to source.

### 105 2.1 Foraging task and non-partitioning strategy

106 In both strategies, contained in the environment is a virtual beacon which guides the robots towards the 107 home area (nest). The arena, shown in Figure 1, is rectangular and is defined by the width (w) and length 108 (l) and the distance between the home area and the items to be collected (source (d)).

109 In the Non-partitioning Strategy (NPS) the robots take the items directly from the item source to the 110 home area. The controller is a Finite State Machine (FSM) composed of three states as shown in Figure 1 111 and each state is now described.

First, the robot starts in the *explore* state in which all the robots are searching for items in the arena. The exploration consists of a motor schema-based navigation (Arkin, 1987) with two behaviours: (i) stay on the path and (ii) avoid obstacles. Once an item is within the range of vision of the robot, the robot records the position, picks up the item and then enters the *go to nest* state.

In the *go to nest* state, the robot travels towards the home area by following the virtual beacon. The robot aligns itself towards the source of the light and moves straight to that location. The robot knows it has reached the home area when ground sensors on the robot detect a change in colour. The item is deposited, and the robot transitions to the *go to source* state.

120 The *go to source* state consists of the robot travelling back to where the estimated position of the items 121 source is recorded. The robot uses dead-reckoning as navigation, to guide itself to reach the items source. 122 If an item is found the robot picks up another item and switches to *go to nest* state, if the robot does not 123 find an item then it changes to *explore* state.

In an ideal scenario, the robot would be continuously retrieving items from the source without transitioning to the *explore* state. However, in reality, robots are susceptible to systematic and non-systematic errors introduced by the dead-reckoning noise, which in turn, affects target position estimation. The error accumulates the longer the distance a robot travels, therefore, the probability of finding the items source decreases as *d* increases due to the drift from the actual items source and the estimated item's source position.

In order to decrease the error introduced by dead-reckoning noise, the task can be decomposed intosmaller sub-tasks performed by each robot and this is described in the following section.

#### 132 2.2 Dynamic partitioning strategy

In Dynamic Task Partitioning (DPS), each robot i changes its individual distance travelled ( $P_i$ ) using a penalty and reward mechanism. Every time a robot finds an item in the *go to source* state  $P_i$  is increased. If the robot i does not find an item then  $P_i$  is decreased.

136  $P_i$  is calculated with Equation 1 where k defines the amount of distance changed to  $P_i$  and  $\alpha$  defines the 137 ratio between reward and penalty. As  $\alpha$  decreases, the robot is rewarded.  $P_i(t)$  is the partition length after 138 the application of the penalty and rewards, and  $P_i(t-1)$  is the value beforehand.

$$P_i(t) = \begin{cases} P_i(t-1) + k(1-\alpha) & \text{if item found} \\ P_i(t-1) - k\alpha & \text{if item not found} \end{cases}$$
(1)

# 3 METHODOLOGY

139 This section presents the methodology followed for all experimental work in the paper. First, parameters 140 and outputs are defined, then, the experimental framework followed and tools used are introduced and 141 finally, the statistical techniques used to analyse the experiments results are described.

#### 142 3.1 Terms, parameters and outputs

143 In order to understand the impact of having different error models for each robot in a swarm, compared 144 to all robots having the same error model, it is important to perform a study from the macro (the swarm as 145 a whole) and the micro (each robot by itself) perspectives.

From a macro perspective, the *total items collected* output provides a good performance metric for the swarm as a whole and this can be compared with different *swarm sizes* and distances between home arena and items source. The *social entropy* provides a metric for how homogeneous the swarm is, according to the different individual errors.

From a micro perspective, it is important the outputs reflect the performance of each robot by itself. The *collection ratio* output represents how successful a robot is at finding the item, providing an indication of how bad the error is for each robot. In a similar way, the *explore ratio* provides an indication of the amount of time the robot spends exploring.

#### 154 3.1.1 Terms and parameters

To allow appropriate results to be collected and meaningful analysis to be undertaken, a number of environmental and system parameters must be defined for the experiments. The terms that are used for the experiments are *simulation length*, *swarm size* and the parameters are *d*, *P* and  $\alpha$ .

158 *Terms:* 

159 The *experiment length* term represents the duration of the experiment until it stops.

160 The *swarm size* term represents the total number of robots performing the task. The minimum *swarm size* 161 is 2 because at least a pair of robots are required to have task partitioning. The maximum *swarm size* is 15 162 as with greater values the robots spend more time avoiding each other than collecting items for the given 163 environments.

164 *Parameters:* 

165 The distance between the home area and the items source is shown as *d*.

166 *Swarm density* is an implicit parameter explored in this paper which is correlated to the swarm size and *d*.

167 The *partition length* (P) parameter represents the distance that a robot travels from where it found an 168 item for the first time, towards the home area, measured in meters. All robots start with the same P.

169 The  $\alpha$  parameter regulates the amount of penalty and reward assigned to each robot in the swarm for 170 DPS.

171 3.1.2 Outputs

The outputs collected and subsequently used to compare and contrast the various methods from the experiments are *final*  $\tilde{P}$ , *total items collected*, *explore ratio*, *collection ratio* and *social entropy*. These outputs are described next.

175 The *total items collected* output represents the number of items collected at the end of the experiment.

176  $P_i$  The *final*  $\tilde{P}$  represents the last median of  $\tilde{P}$  of all from all the robots when the experiment stops from a 177 uni-modal distribution.

The *explore ratio* represents the amount of time spent by the swarm in the *explore* state. The *explore ratio* is measured as  $\frac{T_E}{T_T}$  where  $T_E$  represents the sum of total time spent by all the robots undertaking iterations in the *explore* state and  $T_T$  is the *simulation length* multiplied by the *swarm size*.

181 The *collection ratio* isolates the frequency a robot successfully collects an item allowing for the 182 identification of a correlation between the level of error and how often a robot retrieves an item.  $\frac{I_F}{(I_F+I_L)}$ . 183  $I_F$  is a counter that records the number of times a robot transitions to the *go to nest* state from the 184 *neighbourhood exploration* state.  $I_L$  is a counter that records the number of times a robot enters the *explore* 185 state from the beginning of the simulation.

186 Social entropy is a metric that measures diversity in robot swarms and was initially introduced by Balch 187 (1998). This metric is used to measure robot homogeneity across the swarm according to the classification 188 of robots by their individual performance, where a robot can classify as faulty (high error) or non-faulty 189 (low error). Social entropy H(R) is calculated with Equation 2 where M is the number of subsets (faulty 190 and non-faulty robots),  $p_i$  is the proportion of agents in each subset i and R represent the group of robots. 191 The lower value of H(R) the more homogeneous the swarm is. This parameter output is explored in more 192 detail in Section 4.2.2.

$$H(R) = -\sum_{i=1}^{M} p_i log_2(p_i)$$
<sup>(2)</sup>

#### 193 3.2 Experimental framework and tools

The experimental framework is a top-down approach divided into three stages, as illustrated in Figure 2. The first stage consists of studying the effect of implementing heterogeneous and homogeneous errors from a macro perspective (considering the swarm as a whole) by performing a sensitivity analysis on each strategy, via emulation. The second stage consists on studying the effects of heterogeneous and homogeneous error from a local perspective (considering each robot as an individual) in simulation. Finally, experiments with physical robots validate the results from emulation and simulation.



**Figure 2.** Framework for the experiments in this paper. 1) An emulation is generated from different machine learning techniques in order to perform an enriched model analysis from a macro perspective which could not be possible to do in simulations due to constraints in time, battery span and computational power. 2) Simulations are used to study the model from a micro perspective. 3) Experiments in hardware are used to validate results shown in emulation and simulation.

200 3.2.1 Simulation and hardware

201 The simulator used throughout the work described in this paper was ARGoS (Pinciroli et al., 2011), selected due to the support provided to run experiments for large numbers of robots. For the experiments in 202 this paper, a simulated and real version of the psi-swarm robot platform (Hilder et al., 2014) (Figure 2). 203 This robot has an infra-red and ground colour detector sensors. Since this robot does not have a camera, 204 a virtual camera is used in hardware experiments instead to aid the robot to detect the items. The virtual 205 camera consists of a tracking system that retrieves the position of an ArUco tag (Garrido-Jurado et al., 206 2014) attached on top of each robot. A blue-tooth signal is sent to the robot to let it know that it has found 207 an item. 208

209 The source code for the psi-swarm controller used in the experiments detailed in this paper can be found 210 online at https://github.com/edgarbuchanan/psiswarm\_task\_partitioning.

# 211 3.2.2 Training data

A total of 4 datasets are generated from the outputs of the latin-hypercube sampling (Mckay et al., 1998) in simulations for each strategy (NPS and DPS) and for each error type (heterogeneous and homogeneous). On average, 5 hours of simulated time represents roughly 1 minute in real-time. The number of replicates needed for the experiments shown in this paper is 180 (see Section 3.3 for more information). Therefore, for a set of experiments for a single strategy, it would take 3 hours in real-time. The amount of time required for experiments escalates if a population of samples and/or number of generations is required. Therefore, for parameter analysis that requires a large number of sample, the data set can take a long time to produce.

# 219 3.2.3 Emulator

Incorporating a combination of machine learning algorithms, an emulation is created that can be used as a surrogate for original simulations. This emulator is capable of making efficient predictions of simulation output for a given parameter set, reducing the time and resource requirements inherent in simulation due to the large number of replicates and size of the parameter space.

Parameters and outputs considered for the training of each emulator can be found in Tables 1.

The procedure to generate the emulator and use this to perform a predicted sensitivity analyses is as follows. For each parameter in each strategy, a value range is assigned and sampled using Latin-Hypercube

	Strate	egy Name	e	Interval	
	NP	s Swarm	size	[2-14]	
		a Swarm	size	[0.3-2.0 III] [2-14]	
	DP	S d	~~~~~	[0.5-2.0 m]	
		α		[0-1]	
		Outp	outs	Interval	
		total items c	ollected	$\frac{11100 \text{ Val}}{[0 \text{ max}]}$	
		explore 1	ratio	[0 1]	
		collection	ratio	[0 1]	
i. Simulation models	]	ii. Supervised Learning		iii. Enriched N	Model Analysis
	Train and Validate		Extended Analysis	1	
For beterogeneous and		Noural Naturati		Sensitivity analysis of parameter space	Behaviour analysis of parameter space

 Table 1. Parameters and outputs used for the latin-hypercube sampling

 Parameters

**Figure 3.** From simulation to emulation block diagram. A data set is generated from latin-hypercube analysis in simulations (i). This data set is used to train and validate the ensemble composed with different machine learning techniques (ii). Different statistical tools are used to analyse the ensemble model (iii).

Sampling, which ensures adequate coverage of the parameter space (Figure 3i). Then, each of the four
datasets is used to train and validate the performance of five machine learning techniques (Neural Network,
Random Forest, General Linear Models, Support Vector Machine and Gaussian Process).

These five individual emulators are combined to form one predictive emulation, or ensemble, where predictions are generated by weighting the performance of each algorithm on a test set (Figure 3ii). Combining the five algorithms has been shown to increase the accuracy of prediction over using each emulator in isolation (Alden et al., 2018).

Finally, the emulation is used to perform an enriched sensitivity analysis of the parameter space (Figure 3iii). Using sensitivity analyses, important parameters are revealed for each strategy, the understanding of the relationships between parameters and outputs with each is increased and regions for the parameters where maximum and minimum performance can be found.

The statistical tools used to provide a better understanding for each strategy are the following. To assess the degrees of dependency between parameters and outputs, Partial Rank Correlation Coefficients are calculated for each parameter-output response pair (Mckay et al., 1998). To determine whether the parameters can be optimised to produce the desired behaviour, the evolutionary algorithm Non-dominated Sorting Genetic Algorithm II (NSGA-II) (Deb et al., 2002) has been used. More information for each tool can be found in Section 3.3. In this paper, we have included figures that show key results from these analyses, which are then discussed in more detail. However, for completeness, we include the results of the emulation training and test procedures and all statistical analyses in the supporting website https://www.york.ac.uk/ robot-lab/taskpartitioning/.

#### 248 3.3 Statistical tests and techniques

This section shows the statistical tests used to analyse the results from the experiments. The statistical analysis is performed using Spartan (Alden et al., 2013) for more information about each technique, please refer to (Alden et al., 2014) and (Alden et al., 2018).

252 1) Consistency analysis: The consistency analysis technique allows the identification of the number of 253 executions that minimizes the effect of aleatory uncertainty caused by inherent stochastic variation within non-deterministic simulations. In this technique, 20 distributions are compared with the Vargha-Delaney 254 255 test for a different number of runs. The Vargha-Delaney A test is a non-parametric effect magnitude test 256 that can be used to indicate the difference between two distributions (Delaney and Vargha, 2000). The more different the distributions are, the closer the score is to 0 and 1. We believe that our data does not need 257 258 to transformed as suggested in Neumann et al. (2015) because the amount of time that it takes for these variables to change is greater than the length of the tick used for simulations (0.1s). The value of 180 as 259 sample size has an A-Test score below 0.56 which suggests that the aleatory uncertainty in the outputs has 260 261 been mitigated and also avoids over-fitting the experiments with a larger sample size. In summary, this technique is used to minimize variation from non-determinism in the results to get the correct interpretation 262 of the results. 263



Figure 4. Consistency analysis that shows that the sample size value of 180 is large enough to avoid aleatory uncertainty effect (A-test lower than 0.56) in the outputs (item collected, P, explore ratio and collection ratio).

264 2) Partial Rank Correlation Coefficients: The Partial Rank Correlation Coefficients (PRCC) are used 265 here in order to identify the degrees of dependency between each parameter. This is done by performing a 266 Latin-hypercube sampling across parameters space and the number of samples is 1000. The main difference 267 between random sampling and Latin-hypercube sampling is that with the latter, it is possible to increase 268 reliability that the entire space is covered adequately. PRCC provides a measure of the influence of a single 269 parameter with a single output. Strong correlations (close to 1 or -1) correspond to influential parameters 270 over their respective output in spite of non-linearity introduced by other parameters. In summary, this technique allows us to identify the key parameters for specific outputs and in this way, it is possible toidentify if the error diversity of lack of it has any influence on these key parameters.

3) Non-dominated Sorting Genetic Algorithm II: Non-dominated Sorting Genetic Algorithm II (NSGA-II)
is an evolutionary technique that explores the entire parameter space in order to maximize and/or minimizes
multiple outputs. Once, all the solutions population converge (or meet the specific convergence criteria)
this set of solutions is referred to as pareto front. In later sections of this paper, it will be revealed that the
consideration of error diversity distorts this pareto front and this is correlated to the number of high-error
robots.

# 279 3.4 Error model

The error model consists of adding noise to each motor as shown in Equations 3 and 4. The simulated noise  $\mu$  is generated from taking a sample from a Gaussian distribution each time tick with median k[t]and  $\sigma$  where  $\sigma$  changes for each robot. Curvature functions k for each robot can be found in the Appendix. Every time a robot changes the speed of its motors, timer t is set to 0. This noise model recreates the bias in the robot of moving towards a single direction. Examples of trajectories with physical robots are shown in Figure 5.



**Figure 5.** Trajectories of two different physical robots, A (left) and F (right), moving forwards for 30 seconds with a speed of 0.02 m/s.

Experiments recorded with physical robots and trajectories produced in the simulator for the first 6 robots are shown in Figure 6. The error model in simulation closely resemble the error model in hardware. A model of the psi-swarm used in the simulator in this work can be found in https://github.com/ edgarbuchanan/psiswarm\_model.

$$rightWheelSpeed = actuatedRightWheelSpeed \pm \mu * actuatedRightWheelSpeed$$
 (3)

 $leftWheelSpeed = actuatedLeftWheelSpeed \pm \mu * actuatedLeftWheelSpeed$  (4)

It is important to mention that for the heterogeneous error, the error model for each robot is fixed and it does not change for the experiment shown in this paper.

# 4 EXPERIMENTS AND RESULTS IN A MULTI-SCALE MODEL APPROACH

This section presents experiments to demonstrate the performance difference between heterogeneous and homogeneous errors. First, by using emulation, a sensitivity analysis is performed for each strategy



**Figure 6.** Trajectories of the physical (left column) robots and their respective simulated versions (right column). The letter on top of each figure represents the ID of the robot and each robot moves forwards along the x-axis for 30 seconds with a speed of 0.02 m/s and 10 iterations are shown for each robot. X(m) and Y(m) represent the coordinates of the robot.

(NPS and DPS) from a macro perspective. Second, through experiments in simulations and hardware, theperformance of the swarm from a micro perspective is considered.

Parameter - output	Heterogeneous	Homogeneous
Swarm size - total items collected	0.95	0.97
Swarm size - explore ratio	-0.03	0.8
Swarm size - collection ratio	0.31	-0.94
d - total items collected	-0.87	-0.94
d - explore ratio	0.17	-0.99
d - collection ratio	-0.91	0.97

**Table 2.** LHA correlation values for NPS. Values in bold represent a big difference between heterogeneous

 and homogeneous

### 296 4.1 A study from a macro perspective using emulation

297 This section presents the results from the emulation for each strategy NPS and DPS.

#### 298 4.1.1 Non-partitioning strategy

The first strategy to be described is the Non-partitioning Strategy (NPS) where the robots take the items directly from the items source and transport them to the home area.  $P_i$  is the same as d and it does not change across the simulation.

For the NPS emulation two parameters are considered: *swarm size* and *d*. The *swarm size* is the number of robots that comprise the swarm where the range is between 2 to 14 robots. Heterogeneous and homogeneous errors are considered for the emulation, in a range for *d* from 0.5 to 2.0 m. The width of the arena does not change, and the home area and items source are against the arena walls.

306 Latin-hypercube analysis.

Results from the latin-hypercube analysis are illustrated in Figure 7, summarized in Table 2 and key scatter plots are shown in Figure 8.

Results for heterogeneous error show that the *swarm size* term is only positively highly correlated (absolute correlation coefficient greater than 0.7) with the *total items collected* output (Figure 7). This means that as the *swarm size* increases, the *total items collected* output increases, and this is because there are more robots collecting items in the arena.

The parameter *d* is negatively highly correlated with the *total items collected* and *collection ratio*. As *d* decreases, it takes less time to transport the items from the items source to the home area. In addition, since the distance, the robots are travelling is smaller the probability of finding items increases.

Results for homogeneous error show that the *swarm size* term is not only highly correlated with the *total items collected* output but also with both the *explore ratio* and *collection ratio* (Figure 7, right). As the *swarm size* increases, time spent in the *explore* state increases because robots spend more time avoiding each other. As a consequence robots travel more when transporting items. Therefore, the error increases and the probability of finding items decreases and is reflected in the *collection ratio* output which it has a highly negative correlation with the *swarm size* term.

In a similar way, *d* is not only highly correlated with *total items collected* and *collection ratio* but also with the *explore ratio* for both error types. As *d* increases, the probability of finding items decreases, therefore, robots spend more time exploring than transporting items because they are getting lost more often.



**Figure 7.** LHA for NPS (left) and DPS (right) with homogeneous and heterogeneous error. Left: Correlations change for each error type except for the *total items collected* for both parameters (*swarm size* and *d*) and collection ratio for *d* parameter. Right: results are similar between heterogeneous and homogeneous error except for correlation between the *swarm size* term and the *explore ratio* and *collection ratio* 

Even though robots with homogeneous and heterogeneous errors are performing the same strategy, NPS, with the same settings, results from LHA differ. The main reason for this difference is that the individual errors in each robot, for the heterogeneous error, affect the performance of the swarm performance as a whole in different ways and this is explained below.

330 Total items collected is very similar for homogeneous and heterogeneous error as shown in Figure 8. However, as for the *explore ratio* the correlation coefficient is very different from each other, -0.03 331 for heterogeneous error and 0.8 for homogeneous error. With the heterogeneous error model, there are 332 fluctuations across the *swarm size* term space due to the individual errors considered. For example, between 333 swarm size 2 and 3 robots (robots A, B and C), the explore ratio ranges from 0.4 to 0.8. This is because 334 this group of robots are characterized by their small error compared to other robots in the swarm, as shown 335 in the error models in the previous section (Figure 6). Therefore, these robots spend more time transporting 336 items than exploring. However, this does not occur with the homogeneous error, as shown in Figure 8, 337 where the *explore ratio* increases steadily without any oscillations present. 338

The *collection ratio* output for heterogeneous error also has fluctuations, as shown in Figure 8. In the regions where high error robots are introduced the *collection ratio* drops and increases again when low error robots are introduced (i.e. the range between 5 and 7 robots). However, with homogeneous error the *collection ratio* decreases steadily with no fluctuations as the swarm density increases and the robots spend more time avoiding each other. This is due to there being no high-error robots that are introduced at any point because all the robots have the same error.

As shown, results are different from LHA between heterogeneous and homogeneous errors for the explore ratio and the collection ratios. This is because fluctuations introduced between high and low error robots, affect the correlation coefficients. Complementary LHA scatter plots can be found on-line https://www.york.ac.uk/robot-lab/taskpartitioning/.

349 Non-dominated Sorting Genetic Algorithm II.

NSGA-II was used to find the Pareto front for the best values for *swarm size* and *d* parameters in order to maximize *total items collected* and *collection ratio*, and minimize *explore ratio* as shown in Figure 9.



**Figure 8.** LHA for the *swarm size* term for NPS with heterogeneous (left column) and homogeneous (right column) errors and for the *total items collected* (top row), *explore ratio* (middle row) and *collection ratio* (bottom row) outputs. The blue rectangles represent the proportion of low-error robots and the green box represents the proportion of high-error robots. Robot individual error models introduce fluctuations with heterogeneous error as shown with the *explore ratio* and *collection ratio*. However, this doesn't happen with homogeneous error because all the robots share the same error parameters.

The pareto front is discontinuous for the heterogeneous error (left column), as the emulation captures the 352 heterogeneity in the errors. For instance, for small swarm sizes, from 2 to 3 robots (robots A, B and C), the 353 error is small, which means that the robots can travel longer distances. This minimizes the explore ratio 354 and they spend the least amount of time avoiding each other since the swarm density is minor. Robots 355 between swarm size 2 and 4 with d of 0.5 maximize the collection ratio. This is because the robots are 356 travelling a shorter distance between home and source, therefore error accumulation is small. Between 5 357 and 7 (robots E, F and G), robots are characterized by their high degree of error. Therefore, these robots 358 behave more like obstacles and they impede item collection. As a consequence, the swarm is affected 359 negatively. Lastly, between 8 and 14 (robots H, I, J, K, L, M and N), robots with low-error are again 360 introduced which contribute to a high total items collected output. Further work could potentially use this 361 discontinuous pareto front in order to identify the threshold of the number of high error robots that when 362

Parameter - output	Heterogeneous	Homogeneous
Swarm size - total items collected	0.9	0.97
Swarm size - explore ratio	0.42	-0.41
Swarm size - collection ratio	-0.29	0.37
d - total items collected	-0.76	-0.93
d - explore ratio	-0.73	-0.36
d - collection ratio	-0.42	-0.56
lpha - total items collected	0.07	-0.22
lpha - explore ratio	-0.97	-0.97
lpha - collection ratio	0.99	0.99

**Table 3.** LHA correlation values for DPS. Values in bold represent a big difference between heterogeneous

 and homogeneous

overcome the swarm throughput is affected negatively. This would help to measure the degrees of therobustness of the task.

The pareto front is continuous for the homogeneous error (right column). As all the robots contribute in the same way. If the *total items collected* was to be maximized the *swarm size* needs to be increased. However, if the *collection ratio* is maximized and the *explore ratio* minimized the size of the *swarm size* needs to be decreased. In order to optimize the three outputs it is necessary to have the smallest *d*.

369 Summary.

From this analysis, it can be concluded that it is important to consider heterogeneous and homogeneous errors, as the results can be misleading if they are considered separately because of the different correlation values and this validates the first hypothesis. In addition, the use of different statistical techniques helps to provide a better, more in-depth, understanding of the system. NSGA-II exploits the heterogeneity and finds new solutions that maximize and minimize outputs and strategies described in the following section to decrease this effect by dividing the task into multiple components.

376 4.1.2 Dynamic partitioning strategy

The Dynamic Partitioning Strategy (DPS) is a strategy where robots change their individual partition length ( $P_i$ ) according to a penalty and reward mechanism.  $P_i$  changes with the parameter  $\alpha$ .

379  $\alpha$  regulates the amount of penalty and reward to  $P_i$ . As  $\alpha$  increases the robot *i* gets penalized and not 380 rewarded, and as  $\alpha$  decreases the robot is rewarded more than being penalized. The interval used for the 381 experiments shown in this section is [0,1]. Initial  $P_i$  is randomly selected from a uniform distribution from 382 the same interval as *d*.

383 *Latin-hypercube analysis.* 

Results from the latin-hypercube analysis are summarized in Table 3 and key scatter plots are shown in Figure 10.

Results between heterogeneous and homogeneous error are very similar for all the correlations, except for the correlation between the *swarm size* term and the *explore ratio* and the *collection ratio*, as shown in Figure 7. This discrepancy is produced by the heterogeneity within the individual errors. However, the correlation is kept low with the absolute correlation coefficient being lower than 0.7.

The *total items collected* output is, once again, mainly correlated to the *swarm size* and *d* parameters for the reasons explained in the previous section. However,  $\alpha$  has a negative correlation with *explore ratio* and



**Figure 9.** NSGA-II results for NPS with heterogeneous (left column) and homogeneous (right column) error. The two-dimensional inputs are *swarm size-d* (top row). Two-dimensional outputs are shown as *total items collected-collection ratio* (middle row) and *total items collected-explore ratio* (bottom row). With both the heterogeneous error and the homogeneous error, the *total items collected* are maximized with high *swarm sizes* (yellow box). With both the heterogeneous error and the homogeneous error. The *collection ratio* is maximized with low swarm sizes (blue rectangles). The *explore ratio* is maximized with low *swarm sizes* and high *d* for heterogeneous error and low *swarm sizes* and low *d* with homogeneous error. The latter result demonstrates that since this proportion of robots experiences a low error, it is better for these robots to travel a longer *d* as the robot density is lower the robots spend less time avoiding each other. The pareto front is discontinuous for the heterogeneous error which means that these robots with high error harm more the item collection than contribute to it.

a positive correlation with *collection ratio*, This means that as  $\alpha$  increases the robots are exploring less and finding items more often because all the robots are adjusting their  $P_i$ . In other words, as  $\alpha$  increases robot are travelling shorter distances which allows for less dead-reckoning error accumulation.



**Figure 10.** LHA for the *d* parameter for DPS with heterogeneous (left column) and homogeneous (right column) errors and the explore ratio (top row) and collection ratio (bottom row) outputs. The blue rectangle represents the proportion of low-error robots.

Fluctuations introduce by low-error robots affect the estimation of the correlation coefficient.

The discrepancy mentioned before for the *swarm size* term is shown in Figure 10. For the heterogeneous error, the *collection ratio* decreases and the *explore ratio* increases, whereas as for the rest of the swarm this correlation pattern can not be seen. This could be due to high error robots compensating for the heterogeneous error. Whereas for the homogeneous error, the *explore ratio* and the *collection* ratio decreases and increases steadily respectively for the homogeneous error. As the swarm size increases, there is a higher supply of robots which allows for the creation of a chain successfully between the home area and the source.

#### 402 Non-dominated Sorting Genetic Algorithm II.

403 Large swarm sizes provide the best item collection and  $\alpha$  regulates the *explore ratio* and ratio *collection* 404 where as  $\alpha$  increases, the *collection ratio* increases and the *explore ratio* decreases, see (Figure 11) for this 405 effect with the heterogeneous error. In a similar way, NSGA-II for the heterogeneous error exploits the 406 small swarm size in order to achieve the best *explore ratio* and *collection ratio*.

The Pareto front for DPS is smooth and discontinuities, or gaps, are smaller than NPS. This is because DPS has better regulation over individual errors homogenising the swarm. Each robot *i* is learning its own *P<sub>i</sub>* for the given *alpha* (see next section for more details). This can be also seen for the  $\alpha$  and *swarm size* inputs where there are only two batches of solutions, the ones closer to swarm size of 2 robots and the ones

eter values for micro	perspective experime	nts
	Parameter	Value
	Experiments length	5 hours
	Swarm size	6
	d	1 m
	Р	0.5 m
	lpha	0.5

Table 4. Param

closer to the swarm size 14. This means that fluctuations by high and low error robots between the intervals 411 4 and 10 are ignored and have no significant contributions to the results. 412

413 Results for the homogeneous error show that a larger swarm provides the best item collection and as  $\alpha$  increases the *collection ratio* increases and the *explore ratio* decreases. The Pareto front for the set of 414 415 solutions is continuous and smooth.

Summary 416

 $\alpha$  helps to regulate the *collection ratio* in order to optimize the *explore ratio*. The *total items collected* 417 output is provided mainly by the *swarm size* and d. In this way, it is possible to find a set of parameters that 418 419 provides a good trade-off between the explore ratio and the throughput of items according to the needs 420 of the user. Finally, fluctuations caused by individual error models are reduced and a continuous Pareto front for the output is generated for the heterogeneous error, due to individual convergence of  $P_i$  for each 421 robot and, since the robots are travelling shorter distances, the error is lower and more uniform. More 422 423 information about  $P_i$  convergence can be found in the experiments from simulation and hardware in the 424 next section.

#### 4.2 A study from a micro perspective using simulator and hardware 425

426 In the previous section, the effect of considering individual robot errors in emulation with each strategy 427 was explored. An emulator was used to aid with this study and it was found that results differ for heterogeneous and homogeneous error. In this section, this discrepancy is explored in detail by using 428 experiments from a micro perspective with simulations and hardware (stages 2 and 3 from the experimental 429 430 framework shown in Figure 2).

The parameter values chosen, unless stated, for the experiments in this section are shown in Table 4. 431

Heterogeneous and homogeneous errors 432 4.2.1

433 As discussed in Section 3.4 when modelling the error for each robot, it was found that the error varies between robots. This section describes error diversity and non-diversity in simulations (Figure 12). 434

In the first set of experiments, the robots are performing DPS where  $P_i$  is the same as d. Convergence of 435  $P_i$  is shown in Figure 13. All the robots converge to a single similar P with homogeneous error. However, 436 robots with heterogeneous error converge to different  $P_i$  for each robot *i*. 437

438 The impact of different errors is reflected in the individual performance. In experiments shown in Figure 14, all robots start with a  $P_i$  of 0.4 m and  $\alpha$  of 0.5 with homogeneous and heterogeneous error 439 models for DPS. The robots with homogeneous error have a similar individual performance as each other. 440 However, robots with heterogeneous error have different individual performance according to each robot. 441

Robot specialization emerges from DPS in the sense that every robot learns its own  $P_i$  according to 442 their inherent degree of error as shown in Figure 13. This is consistent with the results presented in 443



**Figure 11.** NSGA-II results for DPS with heterogeneous (left column) and homogeneous (right column) error. Two-dimensional inputs are shown as *swarm size-d* (first row) and *swarm size-alpha* (second row). Two-dimensional outputs are shown as *total items collected-explore ratio* (third row) and *total items collected-collection* ratio (fourth row).



Figure 12. Screenshot of one of the experiments in simulation (left) and hardware (right).



Figure 13. Convergence to a solution with homogeneous (left) and heterogeneous (right) errors with DPS. Robots with homogeneous error converge to a single  $P_i$  and robots with heterogeneous error converge to different  $P_i$ .



**Figure 14.** Individual performance with homogeneous (left) and heterogeneous (right) error models. Robots with homogeneous have similar individual performance and robots with heterogeneous error have different individual performance.

Figure 14 where the  $P_i$  for each robot is correlated with the amount of time that a robot spends exploring the environment. For example, robot A spends the least amount of time in the explore state and, hereby, has the greater  $P_i$  with a value close to 0.5 m. Robots D and E spend the greatest amount of time in the explore state and these robots travel the small  $P_i$  with a value close to 0.3 m. In addition, this consistent with the trajectories shown in Figure 6.

For instance, Figure 13 shows that robots D, E and F learn the smallest  $P_i$  and this is related to their individual performance where these robots spend more time in the *explore* state than the rest of the robots as shown in Figure 14. In addition, Figure 6 shows that these same robots have bigger error drifts.



Figure 15. Item collection with homogeneous and heterogeneous errors with different values for  $\alpha$ . The peak for item collection is 0.4 for homogeneous and 0.5 for heterogeneous error model.



**Figure 16.** Individual performance for different swarm sizes for the homogeneous error (left) and heterogeneous error (right) for NPS in red and DPS in blue. The individual performance decreases after the first robot for NPS and after 7 robots for DPS with the homogeneous error. The individual performance peaks at 4 robots for NPS and at 8 robots with DPS for the heterogeneous error.

It is important to bear in mind the difference in performance between heterogeneous and homogeneous errors, in order to select the appropriate value of  $\alpha$  for the swarm to maximize the item collection as shown in Figure 15. In the case of a homogeneous error model,  $\alpha$  should be 0.4 in order to have the best item collection. As with the heterogeneous error model, that value would be 0.5.

456 Figure 16 shows the individual performance for different swarm sizes, strategies (NPS and DPS) and error types (homogeneous and heterogeneous). The individual performance is estimated by dividing the 457 total items collected by the swarm size. For the homogeneous error the individual performance starts to 458 drop after swarm size 2 for NPS and after swarm size of 7 for DPS. The results differ with the *homogeneous* 459 *error* and this is due to the mix of low and high error robots in the swarm as mentioned in the previous 460 section. For example, NPS peaks at 4 robots because the first 4 robots experience low error and after this, 461 the robots introduced experience high error as shown in Figure 8. This is not the case for DPS where the 462 distribution resembles more like a bimodal distribution with two peaks at 4 and 9, each peak at the location 463 where robots with low error are introduced. More results regarding the robot swarm flexibility against a 464 changing d, change of error models and change of *swarm size* can be found in the supplementary material 465 https://www.york.ac.uk/robot-lab/taskpartitioning/. 466

Indirect item transference is the method chosen for most of the experiments shown in this section because
it has the highest item collection with the lowest convergence speed. This is an important aspect to consider
due to the battery life of the physical robot only lasting 30 minutes.

To conclude, the above results demonstrate that each robot exhibits different performance and this validates the second hypothesis. It is important to consider individual models for each robot when working with swarm robotics. By doing so, it is possible to reduce the reality gap and be able to select the best  $\alpha$ that maximizes the item collection and, in addition, potentially select the best  $P_i$  and  $\alpha$  for each robot to improve the item collection. In Section 4.2.3 experiments with physical robots are shown and how they compare with simulations.

# 476 4.2.2 Social entropy

Results from NSGA-II in emulation for NPS showed a discontinuous Pareto front for the heterogeneous
error and a continuous Pareto front for the homogeneous error (Figure 9). In this section, these results are
explored in more detail to understand the reason of this discrepancy, using an approach based on a social
entropy metric. This metric measures the error diversity across the swarm and is described in Section 3.1.

Decision trees and nearest neighbour classifiers are used to categorize robots into two groups according to their individual performance. Principal Component Analysis (Wold et al., 1987) is used to convert the variables from the individual performance data to their principal components. This is done in order to transform possibly correlated variables into a set of values of linearly uncorrelated variables. The requirement for classification is that the accuracy should be higher than 90%. Figure 17 illustrates the social entropy for each swarm size in the interval [2,14] for each strategy. The social entropy is overlapped with the results from the NSGA-II reported in Section 4.1.

The social entropy for NPS illustrates that the Pareto front breaks when the social entropy highest peak 488 is reached. For a swarm interval between 2 and 4 robots, the social entropy is low. This means that the 489 swarm is homogeneous and composed of robots with low degree of error. This is the reason for the cluster 490 of points in d of 1.75 m. However, after the first robot with high degree of error is introduced (robot D or 491 fourth robot), the social entropy increases. At this stage, the swarm is homogeneous enough to have the 492 Pareto front continuous. However, the discontinuity in the Pareto front appears when the second robot with 493 494 high degree of error is introduced (robot E or fifth robot). The social entropy reaches its highest peak point at this point. The social entropy starts to decrease after the sixth robot (robot F) is introduced. The social 495 entropy decreases steadily because more robots with low degree of error are added to the swarm and this 496 decreases the diversity. The Pareto front reappears after the ninth robot is introduced. After this point the 497 Pareto front is similar to the homogeneous error Pareto front (Figure 9). 498

Overall, the social entropy across the swarm for DPS is similar to with NPS. The social entropy peak again is located after the fifth robot and the Pareto front becomes discontinuous after this point. However, in contrast to NPS the social entropy remains high (greater than 0.8). This prevents the Pareto front from being continuous until the social entropy drops below 0.8. DPS creates a clear distinction between high and low degree of error and because of this, the social entropy increases. This might be because task partitioning is sensible for high noisy degree of error robots.

As noted the social entropy changes with each strategy and the reason is that each strategy provides a different performance for each robot. For NPS, the highest degree of error robots classified are 2, robots D and G. DPS, for this scenario, the robots experience the least amount of time in the explore state. The number of high-degree error robots increases to 4 (D, E, G and J).

In the case of DPS, robots D, E, G and J experience the highest degree of error. Therefore, these robots can not be further optimized. This is consistent with the results shown in Figure 17 where the  $P_i$  for robots D and E with a *d* of 0.4 m does not increase indefinitely as with robots A, B, C and F. This means that



**Figure 17.** Social entropy and individual performance (left and right column) for each strategy: NPS and DPS (first and second rows respectively). Social entropy changes for each strategy due to the number of robots classified as high error.

robots have not reached the optimal distance that decreases the error. In other words, robots D, E, G, and J experience such a high degree of error, that the partitioning strategies are unable to provide a suitable  $P_i$ for the robots to increase their performance.

515 4.2.3 Experiments with physical robots

In this section, the experiments studied in the previous section are explored with physical robots. Three different arena sizes are used for the experiments using 6 robots where individual performance and convergence are explored. A single replicate for each arena is shown in this section. It is important to mention definite conclusions cannot be made from the results shown in this section due to this low sample size, however the results are promising. A screenshot from an experiment is shown in Figure 12.

Results for robots performing NPS are shown in Figure 18. Regardless of the arena size, the robots experience different individual performance which means that they are not identical to each other. In addition, robots spend most of their time exploring instead of retrieving items in the home area. Finally, robots spend less time in the *go to source* than *go to nest* state. This is because since robots are travelling a longer  $P_i$  they experience a greater drift from the original position, causing the target to be beyond the walls of the small arena as previously seen. This effect decreases as the arena increases because the target is within the arena boundaries.

528 Individual performance for robots with DPS can be found in Figure 19. In a similar way to experiments 529 with NPS, robots performing DPS experience an increment in the amount of time spent in the *explore* state 530 as the arena size increases. In contrast with NPS, robots spend more time in the *going to source* state. The



**Figure 18.** Individual performance for physical robots performing NPS for three different arenas with dimensions of  $1.0 \times 1.3 \text{ m}$  (top row),  $2.1 \times 1.2 \text{ m}$  (middle row) and  $2.4 \times 1.6 \text{ m}$  (bottom two). The go to source rate is smaller than the go to nest as the arena becomes smaller.

reason for this, is that the robots are travelling shorter  $P_i$  which decreases the probability of the target being beyond the arena size, for the small arena, in a similar way to that in the simulations.

Since the battery of these robots last 30 minutes, the convergence experiments were divided into three different sets shown in Figure 21. In each set, the robots started with a different P of 1, 0.7 and 0.4 m for an arena of size 2.1 x 1.2 m. All the robots converge to a distance close to 0.4 m that changes from robot to robot. The velocity of convergence is not only related to the degree of error in the robot but also, to the speed of the robot which changes slightly for each robot. Furthermore, from the figures can be seen that there is no change in the  $P_i$  at least for the first 5 minutes of the experiments. This is the time that it takes to find the first item.

As for the item collection, DPS performs better than NPS as the arena size increases as shown in Figure 21 because of the following issues. First, as the area of the arena decreases, the probability of finding the items source increases even though the collection rate is low. This means that partitioning is not required. Second, robots are spending more time dropping and picking up items with DPS which causes a delay in the item getting to the nest. Finally, robots spend more time avoiding each other when they are in the *go to nest*.



**Figure 19.** Individual performance for physical robots performing DPS for three different arenas with dimensions of  $1.0 \times 1.3 \text{ m}$  (a),  $2.1 \times 1.2 \text{ m}$  (c) and  $2.4 \times 1.6 \text{ m}$  (e). Time spent in the *go to source* state is roughly similar to the *go to nest* state and time spent in the *explore* state is lower than with DPS.

In summary, results from experiments with physical robots are similar to results from simulation. The shape of the arena affects the performance of the *go to source* state mainly for NPS. DPS performs better than NPS as the size of the arena increases. Finally, final  $P_i$  changes according to the amount of error in the robot *i*. However, there are some differences due to the reality gap because the models used in the simulator do not provide enough information about the real world.

# 5 DISCUSSION

550 It is a common assumption that all the robots are similar and a single robot model in simulations represents 551 the entire group of robots in a robotic swarm. Furthermore, it was assumed that all robots would have the 552 same behaviour when performing a task. However, work in this paper has shown that this is not necessarily 553 the case.



**Figure 20.** Convergence of  $P_i$  for different *initial partition length*  $(P_i^0)$  of 1.0 (top left), 0.7 (top right) and 0.4 m (middle left) for an arena of 2.1 x 1.1 m. Convergence for arenas 1.0 x 1.3 m (middle right) and 2.4 x 1.6 m (bottom left) for  $P_i^0$  of 0.4 are also shown. The convergence changes from robot to robot and is due to the error and velocity of the robot.

At the moment of retrieving the trajectories for each robot as shown in Section 3.4 each robot experiences a different degree of error. Each robot has a different bias, small or large, of moving towards the left or right direction. The trajectories of 14 robots was modelled and recorded.

In the enriched analysis in Section 4.1 it was shown that two different patterns emerged from heterogeneous and homogeneous errors for each strategy. Each pattern represents different properties of the task partitioning approach. On one hand, the pattern shown with homogeneous error provides information of the interactions of each parameter with each output. On the other hand, the pattern with heterogeneous error provides information how the swarm copes with robots with high and low degree of error for each strategy.

The individual contribution of each robot changes according to its inherent error as shown in Section 4.2. If the homogeneous error is considered, all the robots converge to the same  $P_i$  value. However, if the heterogeneous error is considered, then each robot converges to a different  $P_i$ .  $P_i$  is able to adapt to changes in the error itself, d and swarm size.



Figure 21. Item collection with physical robots and different arena sizes. DPS starts to overcome NPS as the arena size increases.

The social entropy measurement for each strategy bridges the results between the macro and micro perspective (Section 4.2.2). The number of high-degree error robots plays an important role at the moment of defining optimality. As the number of high degree of error robots increases, this affects the range of optimal solutions. In addition, even though the task partitioning strategies increase the performance of each robot, there are a specific number of robots that gain no benefit from task partitioning, due to their high degree of error.

573 Finally, the experiments with physical robots shown in Section 4.2.3 validate the previous results in 574 terms that each robot performs differently and each robot converges to a different solution according to the 575 inherent error.

576 The work presented in this paper is limited to a single task, a single robot platform and a single type of 577 error but there is no reason this work could be applied to other domains. Here are some examples of future 578 work:

- The work presented in this paper could be extended to other tasks such as collective object transportation and collective decision-making. In collective object transportation, there is a high reliance on the input from the sensors and the error in the sensors could be studied. In collective decision-making, error diversity could lead to false positives in decisions.
- The error diversity could be analysed for other robot platforms and this could lead to interesting results.
   On one hand, the error diversity is so uniform that the approach in this paper becomes insignificant, on
   the other hand, the error diversity could be greater and its importance becomes greater.
- In this paper it was shown that the number of high error robots changes the dynamics of the swarm behaviour. Swarm diagnosis and recovery can be implemented to address these robots with errors.

In conclusion, it is important to consider both, homogeneous and heterogeneous errors, in order to have acomprehensive understanding of the performance of a swarm.

# 6 CONCLUSION

Task partitioning strategies have been shown to increase performance in foraging tasks in robotic swarms with dead-reckoning noise (Pini et al., 2013, 2014; Buchanan et al., 2016). However, a common assumption is that all the robots in a swarm share the same error model. In this paper how different degrees of error affect the swarm were studied.

In this paper, work has shown how each robot in the swarm experiences different degrees of error 594 (heterogeneous error) and there is a single degree of error that describes all the robots (homogeneous error) 595 and results undertaking a foraging task differ when considering heterogeneous and homogeneous error. 596 Work has shown that it is important to consider both error types to have a full understanding of the system. 597 Finally, the number of high degree of error in the swarm defines optimality in the system. The degrees of 598 robustness can be measured by identifying the ranges of optimality and the reality gap is able to be reduced. 599 Work in this paper has also shown that it is possible to distinguish robots that harm the performance of the 600 swarm. 601

Further work will consider measuring the degrees of robustness in tasks other than foraging. It will be important to examine how a range of different degrees of errors would affect fault detection and diagnosis. Our hypothesis is that the number of false positives would increase and a threshold that differentiates robots between faulty and non-faulty would be required.

# **AUTHOR CONTRIBUTIONS**

The individual contribution for this article were as follows: conceptualization: E.B., K.A., A.P., J.T.,
A.M.T.; methodology: E.B., K.A.; software: E.B.; validation: E.B., K.A.; formal analysis: E.B., K.A.;
investigation: E.B., K.A., A.P., J.T., A.M.T.; visualization: E.B.; supervision: E.B., A.P., J.T., A.M.T.;
project administration: E.B., K.A., A.P., J.T., A.M.T.; funding acquisition: E.B.; writing—original draft:
E.B., K.A., A.P., J.T., A.M.T.. All authors have read and agreed to the published version of the manuscript.

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# DATA AVAILABILITY STATEMENT

612 The code to replicate the experiments shown in this paper can be found in https:// 613 github.com/edgarbuchanan/psiswarm\_task\_partitioning and https://github. 614 com/edgarbuchanan/psiswarm\_model.

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