



Article An Efficient and Robust Current Control for Polymer Electrolyte Membrane Fuel Cell Power System

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Abstract: Taking into account the restricted ability of polymer electrolyte membrane fuel cell (PEMFC) to generate energy, it is compulsory to present techniques, in which an efficient operating power can be achieved. In many applications, the PEMFC is usually coupled with a high step-up DC-DC power converter which not only provides efficient power conversion, but also offers highly regulated output voltage. Due to the no-linearity of the PEMFC power systems, the application of conventional linear controllers such as proportional-integral (PI) did not succeed to drive the system to operate precisely in an adequate power point. Therefore, this paper proposes a robust non-linear integral fast terminal sliding mode control (IFTSMC) aiming to improve the power quality generated by the PEMFC; besides, a digital filter is designed and implemented to smooth the signals from the chattering effect of the IFTSMC. The stability proof of the IFTSMC is demonstrated via Lyapunov analysis. The proposed control scheme is designed for an experimental closed-loop system which consisted of a Heliocentric hy-Expert™ FC-50W, MicroLabBox dSPACE DS1202, step-up DC-DC power converter and programmable DC power supplies. Comparative results with the PI controller indicate that a reduction of 96% in the response time could be achieved using the suggested algorithm; where, up to more than 91% of the chattering phenomenon could be eliminated via the application of the digital filter.

Keywords: polymer electrolyte membrane fuel cell; proton exchange membrane fuel cell; PEM fuel cell; PEMFC; PI; integral fast terminal sliding mode; sliding mode control; SMC; digital filter; MicroLabBox dSPACE DS1202

1. Introduction

In the recent few decades, global warming has been characterized by an abrupt increase due to the carbon dioxide emissions caused by human activities [1]. As a solution for this matter and in order to reduce its development, coal plants over the world are being replaced by clean and renewable energies such as wind turbines, solar panels, bio-oils and fuel cells [2].

Polymer electrolyte membrane fuel cells (PEMFCs) are among the most efficient electrical generators due to several properties like high energy density, performance and high robustness [3], which leads to multiple applications such as portable power generation, cars, aircrafts and space shuttles [4–10]. In such application, DC-DC high step-up power converters are usually desired not only for boosting the PEMFC low voltage, but also to provide regulated output voltage for end use. The DC-DC power converter, which could be an inductive switching converter or a switched capacitor converter [11], is an adaptation stage circuit that is inserted between the load and the PEMFC stack. One of the most common adaptation stage circuits is the DC-DC boost converter, which is classified as one



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Copyright: © 2021 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). of the most and simplest used converters. This latter has the ability to step-up a lower input voltage into a higher output voltage via controlled pulse-width-modulation (PWM) switching technique.

In order to have an efficient power conversion from the PEMFCs to the DC link (or load), many control techniques and algorithms have been adopted during the recent years. The advantages and disadvantages of the most recent reported ones are enlisted in Table 1. Hence, in [12], an appropriate power point was obtained using a proportional-integral-derivative (PID) for a PEMFC power system. Results showed that by selecting the accurate parameters, the proposed approach could provide satisfactory results in terms of high tracking efficiency. The application of fuzzy logic control (FLC) on PEMFC power systems was introduced by [13]. In comparison with perturb and observe (P&O), satisfactory results such as a reduction of 90% in the signal ripples were obtained using the proposed control scheme. In [14], a back-stepping technique was proposed for a high step-up converter to keep the PEMFC power system operating at the maximum power point. Results have indicated the out-performance of the proposed technique over the proportional integral control in terms of robustness and settling time. Authors of [15,16] used conventional sliding mode control (SMC) aiming to overcome the drawbacks of the classical linear PI controller; their proposed method showed acceptable results in terms of robustness against sharp load variation, but since the SMC was used, the chattering phenomenon was present during the tests. However, as a solution for the chattering phenomenon, authors of [17–19] have, respectively, proposed quasi-continuous, twisting and super twisting algorithms. Results have demonstrated that chattering reduction of 91%, 82% and 84% can be achieved via the proposed algorithms.

Recently, terminal sliding mode controls (TSMCs) have attracted the attention of many researchers due to their capabilities to overcome the drawbacks of the conventional SMC while offering several superior properties such as speeding up the convergence rate and providing high precision control [20–22] Shotorbani et al. [20] compared the performance of the distributed terminal sliding mode controller (DTSMC) with divers control schemes such as PI, SMC, proportional finite-time control (PFTC), proportional asymptotic convergent control (PACC) and proportional-integral finite-time control (PIFTC). Results have confirmed the effectiveness of the proposed DTSMC over the other controllers; in terms of accuracy, smooth tracking and robustness when facing external disturbances. A fast terminal sliding mode control (FTSMC) was designed by Gudey and Gupta [21], for a low-voltage PEMFC based micro-grid system. Experimental results have demonstrated the effectiveness of the proposed FTSMC (faster convergence and slighter steady-state error) to overcome the inability of the classical SMC to regulate the micro-grid bus voltage. An integral terminal sliding mode control (ITSMC) was designed by [22] for a hybrid AC/DC micro-grids based on a wind turbine and PEMFC generator source. Improved performance in terms of robustness was obtained using the proposed ITSMC scheme with respect to control Lyapunov function (CLF) and SMC.

With respect to state of the art, the main contribution of this work is the real-time implementation of a robust no-linear integral fast terminal sliding mode control (IFTSMC), which is a combination of FTSMC [21] and ITSMC [22], aiming to keep the PEMFC system operating at an appropriate and efficient power point; besides, a digital filter is designed and implemented to smooth the signals from the chattering effect of the IFTSMC. The stability proof of the IFTSMC is demonstrated via Lyapunov analysis. The control objective is not only to remain the fuel cell running at an adequate efficient power point, but also to pursuit the trajectory with high tracking performance.

This paper is arranged as follows: Section 2 presents the materials and methods including the models, the control design, as well as the system set-up; whereas the results and discussions are presented in Section 3; finally, conclusions are presented in Section 4.

Reference	Year	Controller	Converter	Features	Drawbacks
Ref. [12]	2020	PID	DC/DC buck and boost converters	 Easy to implement Low computational requirements. The most common used in the industry. 	 Sensitive when facing large load variation. Inappropriate gains leads to the instability of the system. Tuning the controller parameters is difficult.
Ref. [13]	2017	FLC	DC/DC boost converter	- Easy to understand. - It simplifies implementation. - Similar to human reasoning. - Simple to extend by adding new rules.	 Human expertise is required to achieve a suitable accuracy The system states have to be known. It is not always accurate since the results are perceived as a guess. Stability is not guaranteed.
Ref. [14]	2018	BSTP	DC/DC boost converter	 Popular technique for high order systems. Guaranteed stability design through Lyapunov function. Uncertainties could be handled to a certain level. 	 Complex Lyapunov function. High design complexity The exact mathematical model of the system is required Sensitive to parameter variation. Necessity of measuring all the state variables.
Ref. [15]	2019	SMC	DC/DC boost converter	 Simple structure. Easy parameter tuning. Applicable for a wide range of nonlinear systems. Robust to uncertainties and disturbances. Stability is guaranteed. 	 Excessive chattering effect. Unguaranteed finite time convergence. The trajectories are not robust against perturbations during the reaching phase.
Ref. [17] Ref. [18] Ref. [19]	2020 2020 2019	QC TA STA	DC/DC boost converter	 Chattering reduction in comparison with SMC. Finite time convergence. Robust to parameter uncertainties and disturbances. 	 Complex design. Unable to use for first-order systems. Precise and accurate response is not guaranteed. Complex stability demonstration.
Ref. [20]	2017	DTSMC	Voltage source converter	 Finite time convergence. Capable of reducing the chattering. Robust to parameter uncertainties and disturbances. 	 Slow convergence speed. Requires the knowledge of the system boundary uncertainties. Convergence problem may occur in case if the system states move away from the equilibrium. Problem of intrinsic singularity.
Ref. [21]	2016	FTSMC	DC/AC inverter	 Finite time convergence. Fast convergence rate. Capable of reducing the chattering. Robust to uncertainties and disturbances. 	 Problem of intrinsic singularity. Can not be applied to higher order systems. The boundary information of system uncertainties is usually required to be known in advance. Problem of intrinsic singularity.
Ref. [22]	2020	ITSMC	AC/DC inverter	 Finite time convergence. High tracking accuracy. Robust to parameter uncertainties and disturbances. Applicable to high order systems. 	- Slow convergence rate. - Requires the knowledge of the system boundary uncertainties. - Problem of intrinsic singularity.

Table 1. Summary of the recent reported approaches used for PEMFC power system.

2. Materials and Methods

The closed-loop system consists of the PEMFC which is the source of the electricity, a DC-DC boost converter that manipulates the produced DC voltage to feed the load demand, and finally, a digital controller that drives the converter commutations to keep the PEMFC working at an efficient and adequate power point. The diagram of the closed-loop system is presented in Figure 1.

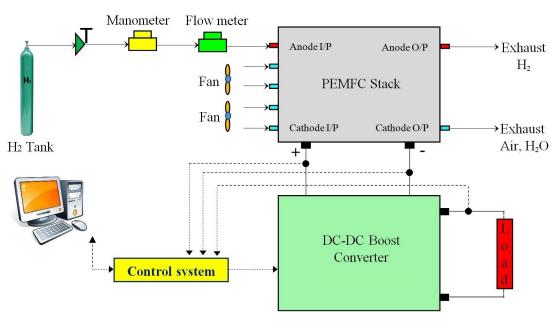


Figure 1. Closed loop system.

2.1. Polymer Electrolyte Membrane Fuel Cell

According to [23], the electrical energy generated by the PEMFC can be expressed as Equation (1). This is derived from a thermo-dynamical analysis of the device which takes into account the temperature and fuels partial pressures. Therefore, the looses are not considered in this theoretical expression.

$$E = 1.229 - 0.85 \cdot 10^{-3} (T - 298) + 4.3 \cdot 10^{-5} \cdot T \cdot [ln(P_{H2}) + \frac{1}{2} ln(P_{O2})]$$
(1)

where *T* (K) is the stack temperature; P_{H_2} (atm) and P_{O_2} (atm) are, respectively, the partial pressure of H₂ and O₂. In order to make a realistic expression derived from Equation (1), three main electric losses which could be classified as activation (e_{act}), ohmic (e_{ohm}) and concentration (e_{con}) losses, are added to the Equation (1). Hence, a realistic PEMFC output voltage is expressed as Equation (2) [24,25].

$$V_{cell} = E - e_{act} - e_{ohm} - e_{con} \tag{2}$$

where e_{act} , e_{ohm} and e_{con} , are respectively, given in Equation (3) [24–27].

$$\begin{cases}
e_{act} = \sigma_1 + \sigma_2 \cdot T + \sigma_3 \cdot T \cdot ln(C_{O2}) + \sigma_4 \cdot T \cdot ln(I) \\
e_{ohm} = I \cdot (R_{mem} + R_{con}) \\
e_{con} = \psi \cdot ln \left(1 - \frac{J}{J_{max}}\right)
\end{cases}$$
(3)

The parameters σ_1 , σ_2 , σ_3 and σ_4 are parametric coefficients determined by the constructor, *I* is the current of the PEMFC, C_{O2} is the oxygen concentration in the catalysts (mol·cm⁻³), ψ is a constant parameter, *J* is the current density, J_{max} is the maximum current density, R_{mem} is the internal resistance of the electrolyte membrane, and R_{con} is the resistance occurred due to the contact between the bipolar plates and the carbon electrodes.

The power generated by the PEMFC stack can be calculated using Equation (4); where N_{cell} represents the number of cells used in the stack [25].

$$P_{stack} = V_{cell} \cdot I \cdot N_{cell} \tag{4}$$

The efficiency of the PEMFC is determined as the ratio of the electric power provided by the stack P_{stack} (W) to the one provided by the stack input P_{in} . This latter can be written as Equation (5); where, *LHV* is the hydrogen lower heating value (J/kg), and \dot{m}_{H_2} is the hydrogen mass flow rate (kg/s).

$$P_{in} = LHV \cdot \dot{m}_{H_2} \tag{5}$$

Therefore, using Equation (4) and (5), the efficiency of the PEMFC can expressed as Equation (6) [28,29]. This equation was used with experimental data in order to plot the efficiency which process is explained in further sections.

$$\eta_{stack} = \frac{P_{stack}}{P_{in}} = \frac{V_{cell} \cdot I \cdot N_{cell}}{LHV \cdot \dot{m}_{H_2}}$$
(6)

2.2. DC-DC Boost Converter

A DC-DC boost converter is a switch-mode power supply which converts a direct voltage coming from a DC source into another higher direct voltage value by adjusting the switch duty cycle d. The output voltage of the DC-DC boost converter can be calculated as Equation (7) [30,31].

$$V_{out} = \left(\frac{1}{1-d}\right) \cdot V_{in} \tag{7}$$

As shown in Figure 2, a boost converter is consisted of an inductance, a metal oxide semiconductor field-effect transistor (MOSFET) switch, a Schottky diode, a capacitor, and a load resistance. The DC-DC converter operates in two modes, continuous conduction mode (CCM) and discontinuous conduction mode (DCM), depending on its storage capacity and the switching period T [32,33].

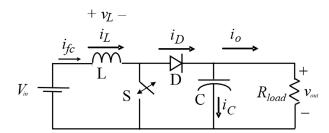


Figure 2. DC-DC boost converter.

By assuming that the boost converter operates in the CCM, and by applying the Kirchhoff's laws to the circuit, the averaged state-space representation can be determined as Equation (8) [34,35]

$$\begin{cases} \begin{bmatrix} \frac{di_L}{dt} \\ \frac{dV_{out}}{dt} \end{bmatrix} = \begin{bmatrix} 0 & \frac{-(1-d)}{L} \\ \frac{(1-d)}{C} & -\frac{1}{RC} \end{bmatrix} \cdot \begin{bmatrix} i_L \\ V_{out} \end{bmatrix} + \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} V_{in} \\ y = \begin{bmatrix} 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} i_L \\ V_{out} \end{bmatrix}$$
(8)

2.3. Control Design

In this section, a proportional-integral (PI) and an integral fast terminal sliding mode control (IFTSMC) are designed to stabilize and remain the PEMFC operating at an efficient and adequate power point.

2.3.1. PI Control

PI controller is widely used in most power electronic closed-loop systems. It is the most straightforward classical control which uses a feedback loop to generate an error e_r . More

specifically, the controller must track a set-point or a reference by adjusting the appropriate signal that supplied to the system. Hence, the controller uses the reference and the feedback, which is a measurement acquired by a sensor, to generate the control signal. The overall control function u of the PI controller is given in Equation (10) [36–38]; where e_r is the error between the PEMFC current i_L and the reference current i_{ref} (expressed in Equation (9)). K_p and K_i represents, respectively, the proportional and the integral coefficients.

$$e_r = i_L - i_{ref} \tag{9}$$

$$u = K_p e_r + K_i \int_0^t e_r dt \tag{10}$$

The major drawback of the PI controller appears in determining its proportional and integral gain coefficients that correspond, respectively, with K_P and K_i . Besides, its vulnerability, due to the load variations, could be a major problem. However, in order to decrease the complexity of selecting the gain coefficients, the Ziegler-Nichols tuning method was used since it is an efficient trial and error method.

2.3.2. Integral Fast Terminal Sliding Mode Control (IFTSMC)

IFTSMC is a new type of terminal sliding mode control which was invented by the scientist Venkataraman and Gulati [39] in the Jet Propulsion Laboratory. It is a nonlinear and a robust control based on the concept of the conventional TSMC and through a development of SMC. The command law u of the IFTSMC consists of two terms, a discontinuous term u_{sw} that remains the system on the sliding surface, and an equivalent term u_{eq} that brings the system to the sliding surface [40]. The total command law can be expressed as Equation (11).

$$u = u_{eq} + u_{sw} \tag{11}$$

The discontinuous term u_{sw} is defined in Equation (12); where, where *k* is a positive constant and sign(s) is the signum function [41].

$$u_{sw} = -\frac{L}{V_{out}} \cdot k \cdot sign(s) \tag{12}$$

The equivalent term u_{eq} is obtained by setting a sliding surface *s* and is finally achieved by establishing $\dot{s} = 0$ [40]. The sliding surface given in Equation (13) is proposed; where the parameters α , λ , *p* and *q* are constants that satisfy the following condition: $\alpha > 0$, $\lambda > 0$, p > 0, q > 0, 1 < p/q < 2 [42–44].

$$s = e_r + \alpha \int_0^t e_r.dt + \lambda \left(\int_0^t e_r.dt\right)^{p/q}$$
(13)

The time derivative of the surface can be expressed as in Equation (14).

$$\dot{s} = \dot{e_r} + \alpha \cdot e_r \lambda \left(\frac{p}{q}\right) \cdot e_r \cdot \left(\int_0^t e_r . dt\right)^{\frac{p-q}{q}}$$
(14)

Also, the error expression was already defined in the Equation (9). As the reference current is constant, therefore, a derivative expression can be obtained from (8) which results in the following Equation (15).

$$\dot{e}_r = -\frac{(1-d)}{L}i_L + \frac{1}{L}\cdot V_{in}$$
 (15)

Thus, through a combination of Equation (14), with the latter Equation (15), a complete expression of the surface derivative is gathered in the following Equation (16).

$$\dot{s} = -\frac{(1-d)}{L} \cdot V_{out} + \frac{1}{L} \cdot V_{in} + \alpha \cdot e_r + \lambda \left(\frac{p}{q}\right) \cdot e_r \cdot \left(\int_0^t e_r \cdot dt\right)^{\frac{p-q}{q}}$$
$$\dot{s} = \frac{u}{L} \cdot V_{out} - \frac{1}{L} \cdot V_{out} + \alpha \cdot e_r + \frac{1}{L} \cdot V_{in} + \lambda \left(\frac{p}{q}\right) \cdot e_r \cdot \left(\int_0^t e_r \cdot dt\right)^{\frac{p-q}{q}}$$
(16)

Finally, stating that that $\dot{s} = 0$, the equivalent term of the control law is achieved as in Equation (17).

$$u_{eq} = 1 - \frac{V_{in}}{V_{out}} - \frac{\alpha \cdot e_r \cdot L}{V_{out}} - \frac{\lambda \cdot e_r \cdot L}{V_{out}} \left(\frac{p}{q}\right) \cdot \left(\int_0^t e_r \cdot dt\right)^{\frac{p-q}{q}}$$
(17)

Previous remarks in terms of the chosen surface, provided certain limitations to take into account at the moment of the constants tuning. However, these have also been adjusted through the minimization of the integral of the absolute error (IAE) that belongs to the Equation (18). This aims to achieve a suitable performance by taking into account the error reduction in real time.

$$IAE = \int_0^t |e(t)|dt \tag{18}$$

2.3.3. IFTSMC Stability Proof

The previous obtained control law can be analyzed in terms of the Lyapunov theory of stability. This states that if there exist a positive definite function: $R^n \to R$ so that V(x) > 0, V(0) = 0, $V(\infty) = \infty$ and $\dot{V}(x) < 0$, $\forall x \neq 0$; therefore the dynamical system is asymptotically stable. Consequently, to prove the stability of the PEMFC system, a positive definite Lyapunov candidate function is chosen as the Equation (19).

$$V(s) = \frac{1}{2}s^2\tag{19}$$

Thus, the derivative of the latter expression is established in the next expression such that \dot{s} from (16) is replaced as follows.

$$\dot{V}(s) = s\dot{s}$$

$$= s\left(\frac{u}{L}V_{out} - \frac{1}{L}V_{out} + \frac{1}{L}V_{in} + \alpha \cdot e_r + \lambda\left(\frac{p}{q}\right) \cdot e_r \cdot \left(\int_0^t e_r dt\right)^{\frac{p-q}{q}}\right) \quad (20)$$

The replacement of the control term u with the Equations (11), (12) and (17), yields to the following expression. Further mathematical development as follows, accomplishes with the Lyapunov stability proof since $\dot{V}(s)$ is concluded to be less or equal to zero.

$$\dot{V}(s) = s \left(\frac{(u_{eq} + u_{sw})}{L} \cdot V_{out} - \frac{1}{L} \cdot V_{out} + \frac{1}{L} \cdot V_{in} + \alpha \cdot e_r + \lambda \left(\frac{p}{q}\right) \cdot e_r \cdot \left(\int_0^t e_r \cdot dt\right)^{\frac{p-q}{q}} \right)$$

$$= s \left(\frac{V_{out}}{L} \left[1 - \frac{V_{in}}{V_{out}} - \frac{\alpha \cdot e_r \cdot L}{V_{out}} - \frac{\lambda \cdot e_r \cdot L}{V_{out}} \left(\frac{p}{q}\right) \cdot \left(\int_0^t e_r \cdot dt\right)^{\frac{p-q}{q}} - \frac{L}{V_{out}} \cdot k \cdot sign(s) \right] \right)$$

$$+ s \left(-\frac{1}{L} \cdot V_{out} + \frac{1}{L} \cdot V_{in} + \alpha \cdot e_r + \lambda \left(\frac{p}{q}\right) \cdot e_r \cdot \left(\int_0^t e_r \cdot dt\right)^{\frac{p-q}{q}} \right)$$

$$= -k \cdot s \cdot sign(s)$$

$$= -k \cdot |s|$$

$$\leq 0$$
(21)

2.4. Digital Filter Design

In order to reduce ripples and chattering phenomenon, a digital filter was designed in Matlab. The command *filter*(b,a,x) requires the numerator b and denominator a coefficients which represent a rational transfer function, whereas the data input is defined as x. Provided that a = 1 and b = 1/N, the result is a moving-average expression that filters the high frequency signals along the the number of elements N to be filtered (this is also known as the filter order) expressed in Equation (22) [45].

$$y[k] = \sum_{i=1}^{N} \frac{1}{N} x[k-i]$$
(22)

The implementation of previous expression has been done through a Finite Impulse Filter (FIR) block in Simulink. The filter order was defined along the research as it is explained in the following sections. The sampling frequency was chosen is 10 kHz since it fits with the hardware limitations and data acquired.

2.5. Description of the Test Bench

The experimental test bench, which is shown in Figure 3, was built at the laboratory of advanced control in the university of Vitoria-Gasteiz, Spain. It is consisted of a Heliocentric hy-ExpertTM FC-50W and its auxiliaries, MicroLabBox dSPACE DS1202, step-up DC-DC power converter and programmable DC power.

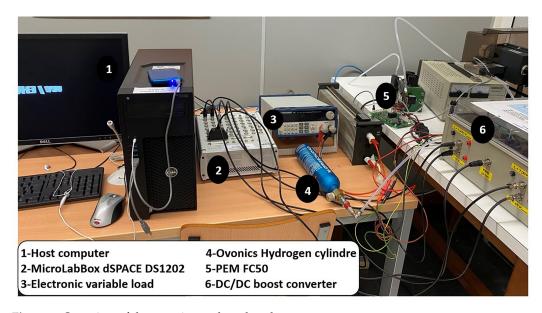


Figure 3. Overview of the experimental test bench.

Table 2 lists the technical specifications of the Heliocentric FC-50; where this latter consists of 10 cells stacked together to generate a rated power around 40 W.

The host computer has an INTEL processor type I7 7700k 4.5 GHz based on Kaby Lake architecture, and a powerful RAM of 32GB. It is used to design the controller and manage the system via the Matlab/Simulink[™] environment software. The input and output signals are measured and observed via the ControlDesk software tools. The control algorithm has been implemented on a dSPACE DS1202 card to generate the pulse width modulation (PWM) signal, which activates the IGBT trigger of the boost converter. This latter was constructed by the research-group-TEP192 with the characteristics listed in Table 3.

FC50 Characteristics	Electrical Characteristics			
Type of cell	Proton exchange membrane	Operating voltage	2.5–9 V	
Cooling system	Ventilators	Operating current	0–10 A	
Fuel type	Pure hydrogen	Rated. Output power	40 Watt	
Dimensions $W \times H \times D$	$120 \text{ mm} \times 103 \text{ mm} \times 135 \text{ mm}$	Max. Output power	50 Watt	
Weight	1150 g	Open-circuit voltage	9.0 V	
H_2 Flow meter		H_2 Kit of 15 bar		
Precision	0.8% of the quantified value	Inlet H ₂ pressure	1–15 bar	
Range of measuring	10–1000 sml/min	Outlet H_2 pressure	0.4–0.8 bar	
Thermal		H_2 Kit of 200 bar		
Operating temperature	+15–50 °C	Inlet H ₂ pressure	200 bar	
Max. Start temperature	+45 °C	Outlet H_2 pressure	1–15 bar	
Fuel detector		H_2 Detector		
Recommended H ₂ purity	5 with 99.99%	Type of sensors	H ₂ 4%	
H_2 input pressure	0.4–8 bar (5.8–11.6 psig)	Measuring principle	3 electrode sensor	
H_2 consumption	Max. 700 sml/min (at 0 °C, 1013 bar)	Operating range	0–4%	

Table 2. PEM FC50 technical data.

The MicroLabBox dSPACE DS1202 is a powerful tool that used to linkage between the software (Simulink) and the hardware (the converter), via its real-time interface (RTI). It has the ability to receive and send the information among the converter, the Mat-lab/Simulink[™] and ControlDesk software, as well as monitoring the signals of the real processes throughout the operation. It contains two digital input/output PWM ports, two RS232, two CAN, as well as 48 input/output channels which make it adapted to many different functions and activities. Furthermore, it has a powerful CPU of 2GHz and a field-programmable gate array (FPGA) that allows the user to make tests even for speedy control loops. A block diagram of the integrated MicroLabBox with the PEMFC, the boost converter, the host computer as well as the programmable DC power is shown in Figure 4. The programmable DC power is manufactured by BK-PRECISION, type 8500B, and it is used as a variable load resistance in order to test the performance of the proposed control algorithm.

The design of the digital controller on the Simulink[™] graphical interface as well as its connections with the RTI blocks are shown in Figure 5.

Table 3. Technical data of the boost converter.

Parameter	Value
Inductance	6 µH
Input capacitor	1500 μF
Output capacitor	3000 μF
Max. Switching frequency	25,000 HZ
Max. Input voltage	$V_{in}max = 60 \text{ V}$
Max. Iput current	$I_{in}max = 30 \text{ A}$
Max. Output voltage	$V_{out}max = 250 \text{ V}$
Max. Output current	$I_{out}max = 30 \text{ A}$

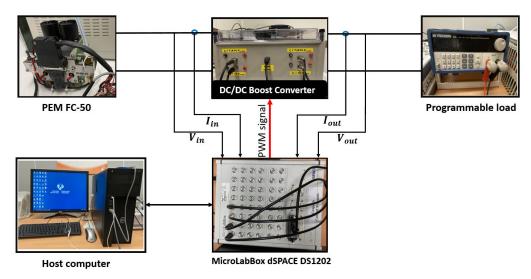


Figure 4. System implementation.

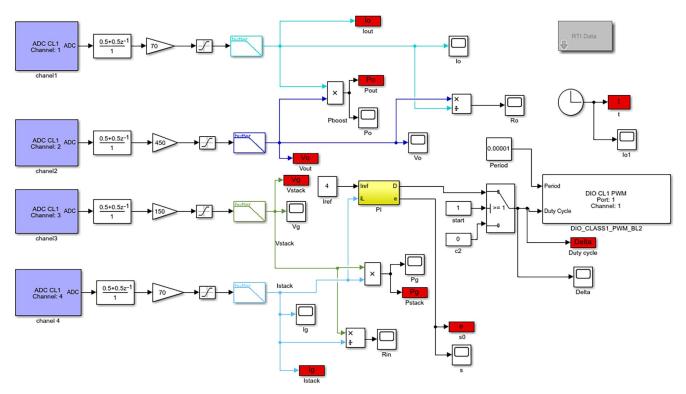


Figure 5. Real-time control structure.

3. Results and Discussion

The current/voltage and current/power characteristics of the practical FC-50W for diverse temperatures, are presented in Figure 6. It is noticed that the performance of the FC-50W is enhanced by the increase of temperature from 20 °C to 46 °C which could be interpreted by the rise of the membrane conductivity, and by the improvement in the exchange of the current density which will results in diminishing the activation losses. Notwithstanding these improvements, at higher temperatures such as T > 46 °C, the conductivity of the membrane starts to drop due to the lack of the relative humidity; which will result in a reduction in the performance of the PEMFC. It should be noted that the performance study of the FC-50W was limited due to the constraints in the oxygen and hydrogen partial pressures; these were narrowed since the rates are automatically controlled by an integrated control.

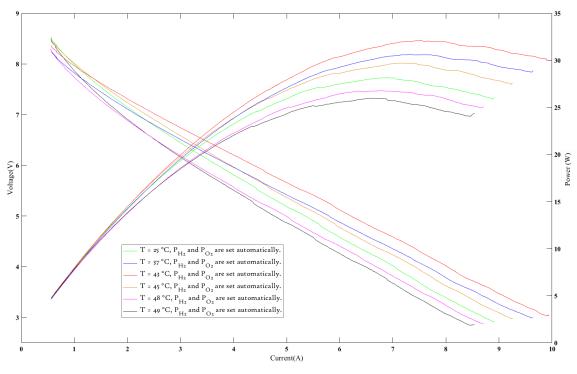


Figure 6. I/V and I/P characteristics of the FC-50W for diverse operating temperatures.

When studying the performance and the behaviour of the PEMFC, a contrast between the maximum operating power point and maximum efficiency operating point must be made. In Figure 7, the current/efficiency characteristics of the Heliocentric hy-ExpertTM FC-50W are presented. This was obtained based on Equation (6) through a variation of the stack current and gathering the mass flow rate variation of the hydrogen which was given by the Heliocentris software. Therefore, the curve was possible to be achieved. According to this figure, it can be seen that the best efficiency is obtained at low load currents [1-2 A]. However, according to Figure 6, the optimum operating power point is obtained at a high current range [6–8 A]. Therefore, it is mandatory to choose between the optimum power or efficiency, and this could be selected depending on the required power for the specific application. In this work, the authors preferred to establish an efficient operating power point while providing an important amount of power. Thus, by designing a suitable controller that able to remain the FC-50W operating at I = 4 A, an efficiency of almost 50% while producing a power of 25 W can be achieved.

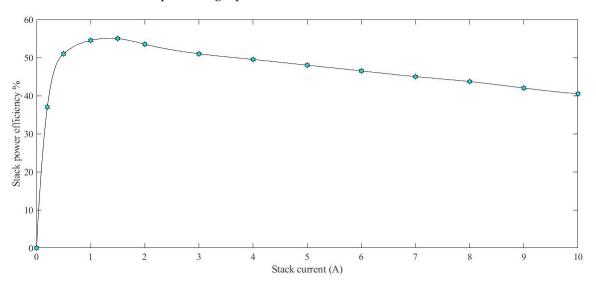


Figure 7. FC-50W current/efficiency characteristics.

To hold and keep the FC-50W operating at the selected reference current $I_{ref} = 4$ A, PID and IFTSMC controllers were proposed. Their coefficient parameters obtained through Ziegler-Nichols and *min*{*IAE*} are enlisted in Table 4.

Table 4. Controllers parameters gains.

IFTSMC	PI
p=1	$K_{cr} = 0.04$
q = 3	$P_{cr} = 12.08$
lpha=0.1	$K_p = 0.02$
$\lambda = 0.1$	$K_i = 10$
k = 0.5	-

In order to test and view the performance of the proposed controllers, variations in the load resistance are adjusted, respectively, from 20 Ω to 50 Ω at t = 20 s, and from 50 Ω to 20 Ω at t = 40 s. These load variations, the duty cycle signal for both PI and IFTSMC, as well as their generated errors, are presented in Figure 8. Despite the sharp variations of the load resistance, it is clearly shown that both of controllers succeeded to converge the error to zero value; which will guarantee as a result the stability of the system. Figure 8 also demonstrates the drawbacks of the PI controller in terms of the converging time; hence, it takes up to more than 12 s to reach the equilibrium point while the proposed IFTSMC algorithm takes only 0.45 s.

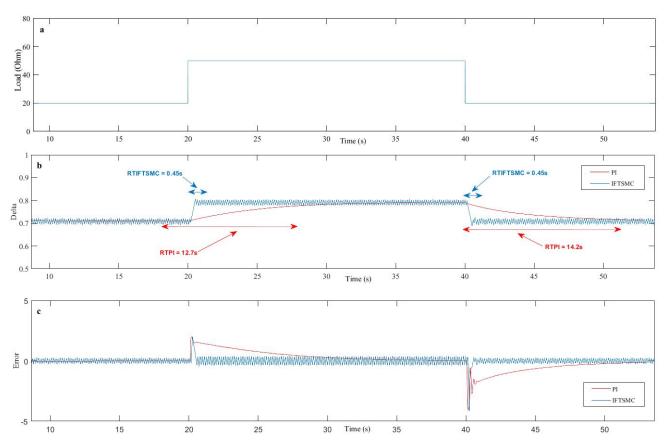


Figure 8. (a): Load variations; (b): Duty cycle signal; (c): Error.

The electric outputs of the FC-50W stack, under the application of PI and IFTSMC, are presented in Figure 9; where the three graphs shows, respectively, the stack current, stack voltage and stack power. At t = 20 s, by applying load variation from 20 Ω to 50 Ω , the PI shows an undershoot of 2.006 A in current, an overshoot of 1.147 V in voltage, and

an undershoot of 10.05 W in power; while the proposed IFTSMC shows an undershoot of 1.997 A in current, an overshoot of 1.107 V in voltage, and an undershoot of 9.99 W in power. On the other hand, at t = 40 s, by applying load variation from 50 Ω to 20 Ω , the PI shows an overshoot of 4.086 A in current, an undershoot of 2.014 V in voltage, and an overshoot of 9.17 W in power; while the proposed IFTSMC shows an overshoot of 4.141 A in current, an undershoot of 9.26 W in power. According to these results, it is clear that both of PI and IFTSMC have almost the same performance in term of overshoots and undershoots; where the IFTSMC has an improvement of 0.06 W over the PI when increasing the load resistance, while the PI has an improvement of 0.09 W over the IFTSMC when decreasing the load resistance. However, it is clearly shown that the feature of the proposed IFTSMC appears in its capability to converge the system to the reference value with high speed (response time = 0.45 s).

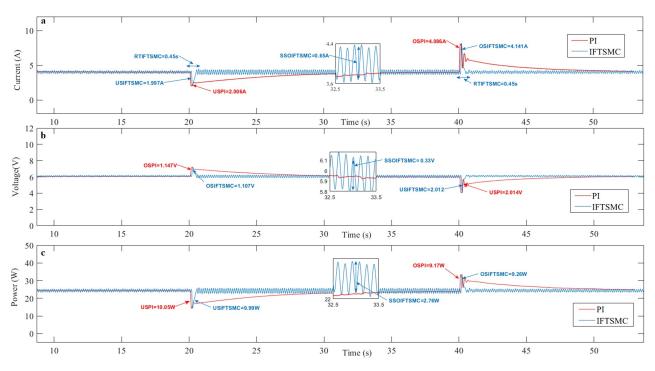


Figure 9. (a): Stack current; (b): Stack voltage; (c): Stack power.

Figure 10 shows the output signals behaviour of the step-up DC-DC converter. According to this figure, gradual and smooth movements to the desired value are obtained. However, in spite of the chattering phenomenon which is caused by the proposed IFTSMC control during the steady state, its robustness to converge the system in a short times which will results in a high tracking accuracy, is an important advantage over the conventional PI.

According to Figures 9 and 10, it is noticed that the chattering phenomenon, which is a normal behavior of sliding mode control, occurred in the steady state could represent an obstacle for the proposed IFTSMC control; therefore, to eliminate these ripples, a a digital filter that diminished the high frequency components along 400 points was applied to the duty cycle (command law). The filtered signals of the FC-50W stack are presented in Figure 11. This latter demonstrates that by applying a digital filter, a chattering reduction from 0.65 A, 0.33 V, 2.76 W (Figure 9) to 0.08 A, 0.03 V, 0.36 W (Figure 11), are respectively obtained. By means of power percentage, a chattering reduction up to 91% is obtained which results in a soft and smooth signals.

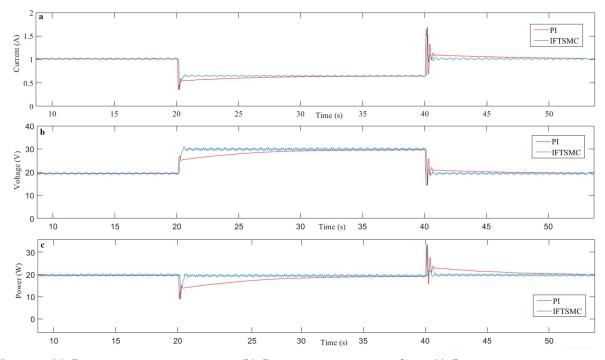


Figure 10. (a): Boost converter output current; (b): Boost converter output voltage; (c): Boost converter output power.

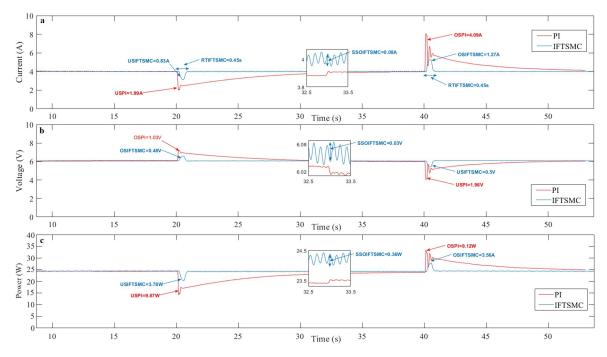


Figure 11. (a): Filtered stack current; (b): Filtered stack voltage; (c): Filtered stack power.

According to these results, it is clearly seen that the IFTSMC with the application of the digital filter has succeeded to keep the FC-50W stack operating at the desired power point while providing high tracking performance. Hence, high convergence speed with chattering reduction up to more than 91% are obtained using the proposed IFTSMC algorithm. Besides, soft and fast dynamic behavior while guaranteeing the system stability are also obtained.

4. Conclusions

A Heliocentric hy-Expert[™] FC-50W feeding programmable DC power supplies via a controlled boost converter is studied in this work. The closed-loop system which includes the FC-50W and its auxiliaries, the converter, the host computer and the programmable DC power supplies are implemented and linked to the MicroLabBox dSPACE DS1202. The suggested IFTSMC control scheme is designed to keep the PEMFC power system operating at an appropriate and efficient power point as well as to pursuit the trajectory with high tracking performance. The stability proof of the proposed IFTSMC is demonstrated via Lyapunov analysis; where its chattering phenomenon is cancelled via the application of a digital filter.

The experimental characteristics of the FC-50W for diverse temperatures are investigated and it is concluded that the performance of the PEMFC is enhanced by the increase of temperature from 20 °C to 46 °C, while it is reduced for higher temperatures. On the other hand and based on the efficiency characteristics of the PEMFC, it is concluded that for the performance improvement, it is mandatory to to choose between the optimum power point or the optimum efficiency.

An experimental comparative study is investigated between the IFTSMC and the well-known PI controller so as to reveal the merits of the proposed technique. Results have indicated that despite the sharp variations of the load resistance, both of controllers succeeded to converge the error to zero value; where, gradual and smooth movements to the desired value with global system stability are obtained. Results also have indicated that both of PI and IFTSMC have almost the same performance in term of overshoots and undershoots; however, it is clearly proven that the feature of the proposed IFTSMC appears in its capability to converge the system to the reference value with high speed (response time = 0.45 s).

The experimental comparative study also has proven the effectiveness of the LFP application, hence, up to more than 91% of the chattering phenomenon of the IFTSMC could be eliminated. Therefore, it is clearly proven that the IFTSMC with the application of the digital filter has succeeded to keep the FC-50W stack operating at the desired power point while providing high tracking performance such as high convergence speed with significant chattering reduction. Finally, the obtained results of this work are quite encouraging and they give prospects for further advanced research to enhance and improve the performance of the PEMFC.

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Abbreviations

The following abbreviations are used in this manuscript:

PEMFC	nalumar alactralizita membrana fuel call
PEMFC	polymer electrolyte membrane fuel cell
IFTSMC	proportional-integral
	integral fast terminal sliding mode control
PEMFCs	proton exchange membrane fuel cells
PWM	pulse width modulation
PID	proportional-integral derivative
FOPID	fractional-order proportional-integral-derivative
TZTP	two-zero/three-pole
PID-SSA	PID using slap swarm algorithm
IRA	incremental resistance algorithm
GAO	grey antlion optimizer
GWM	grey wolf optimizer
MBA	mine-blast algorithm
FLC	fuzzy logic control
P&O	perturb and observe
FLC-PSO	fuzzy logic control based on particle swarm optimization
ANFIS	adaptive neuro-fuzzy inference system
SMC	sliding mode control
HOSM-QC	high order sliding mode based on quasi-continuous algorithm
HOSM-TA	high order sliding mode based on twisting algorithm
HOSM-STA	high order sliding mode based on super-twisting algorithm
TSMCs	terminal sliding mode controls
DTSMC	distributed terminal sliding mode controller
PFTC	proportional finite-time control
PACC	proportional asymptotic convergent contro
PIFTC	proportional-integral finite-time contro
FTSMC	fast terminal sliding mode control
ITSMC	integral terminal sliding mode control
CLF	control Lyapunov function
TDE	time delay estimation
LHV	hydrogen lower heating value
MOSFET	metal oxide semiconductor field effect transistor
CCM	continuous-conduction-mode
DCM	discontinuous-conduction-mode
TSMC	terminal sliding mode
DAC	•
	digital to analog converter
ADC	analog to digital converter

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