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# Secure Outage Probability in the Presence of Two Eavesdroppers and Composite Fading

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**Abstract**—We investigate the secure outage probability (SOP) in the presence of two eavesdroppers over  $\mathcal{F}$  composite fading channels. The derived analytic results are relatively simple and their validity is justified through comparisons with respective simulation results. Subsequently, they are used to quantify the impact of the involved parameters on the achievable secure communication in the considered set up.

## I. INTRODUCTION

Device-to-device (D2D) communications provide direct connection between wireless devices and are attractive for several reasons, e.g., improvement of cell edge throughput and lower power consumption [1]. Thus, there is an increasing interest towards D2D communications as they are anticipated to be a core part of several emerging use cases. Some examples are the Internet of wearable things (IoWT) for digital health-care applications [2] and unmanned aerial vehicle (UAV)-assisted Industrial Internet of Things (IIoT) Networks [3].

In D2D communications, user equipments (UEs) are operated in close proximity to the human body, e.g., held in a user's hand, carried in a pocket or worn on the body in the case of a smart watch. Based on this and due to the transitory behavior of humans, UEs are often mobile and operated in populated environments. Consequently, D2D communication links are fundamentally heavily susceptible to multipath fading and shadowing caused by the user's body and/or nearby objects [4]. This can degrade significantly the quality of radio links and reduce the performance of D2D systems. Therefore, it is important to accurately characterize the combined effects of multipath fading and shadowing [5], [6] as this affects the achievable level of both quality of service and secure communications [7–9] and the references therein.

In fact, since UEs are personal devices, often operated in dense and crowded environments, the privacy and security of D2D communications are also important considerations. In D2D communications, a legitimate user communicates with the intended user (in this case forming a legitimate D2D pair) in the presence of an Eavesdropper (Eve) [10]. In this scenario, secure communication is achievable when the channel quality of a legitimate D2D pair is better than that of the wiretap D2D pair (i.e., between a legitimate user and the non-intended user,

Eve). The maximum transmission rate achieved in secure communication is defined as the secrecy capacity, at which the Eve is not able to obtain any information. The notion of secrecy capacity has become an important metric in the performance analysis of wireless systems. It has been extensively studied for non-degraded channels [11], multipath fading channels [12–15], large-scale fading channels [16], [17], composite fading channels [18–22] and multi-antenna channels [23]. For example, in [12], the secrecy capacity was analyzed over  $\kappa$ - $\mu$  fading channels based on empirical measurements, whereas [19] addressed the secrecy outage analysis over correlated Nakagami- $m$  / gamma composite fading conditions.

Motivated by the importance of encapsulating realistic fading behavior in the analysis of physical layer security in emerging communication scenarios, the present contribution quantifies the achievable secure outage probability over composite fading channels. More specifically, this study is addressed in the presence of two eavesdroppers and  $\mathcal{F}$  composite fading channels, which has been shown extensively that they are typically encountered in realistic D2D communications scenarios, including personal and vehicular communications. To that end, we derive an analytic expression for the secure outage probability (SOP), which is expressed in closed-form and is tractable both analytically and numerically. Capitalizing on this, we analyze the behavior of the considered set up over different  $\mathcal{F}$  composite fading conditions and quantify the effect of increasing numbers of Eves on the respective SOP performance. To the best of the authors' knowledge, the derived analytic results are novel and are expected to provide useful insights that will be useful in the design and deployment of D2D communication systems.

## II. SYSTEM AND CHANNEL MODEL

The physical signal model proposed for the  $\mathcal{F}$  composite fading channel is similar to that for the Nakagami- $m$  fading channel [24]. However, in contrast to the Nakagami- $m$  signal, in an  $\mathcal{F}$  composite fading channel, the root-mean-square (rms) power of the received signal is subject to random variations induced by shadowing. The  $\mathcal{F}$  composite fading model has widely been used for both conventional and emerging wireless

applications, e.g., optical [25], cellular [26], cognitive radio and vehicular [25] communications. Of note, the probability density function (PDF) and cumulative distribution function (CDF) of the received signal envelope ( $R$ ) in  $\mathcal{F}$  fading channels were first presented in [26]. Yet, in our analysis we use the modified version presented in [27].

Regarding the considered system model, we assume that a legitimate transmitter (Alice) sends a confidential message  $W$  to the corresponding legitimate receiver (Bob) in the presence of two Eves. Alice encodes a message block,  $W = [W(1), W(2), \dots, W(i)]$ , into a codeword,  $X = [X(1), X(2), \dots, X(i)]$ , for transmission over the channel. Bob can obtain information about the transmitted message by decoding the received signal,  $Y_M$ , while Eves are also capable of eavesdropping the transmitted message by decoding the received signal,  $Y_E$ . In this case, the received signal at Bob and at the  $k^{\text{th}}$  Eve are respectively given by [28]

$$Y_M(i) = h_M(i)X(i) + n_M(i), \quad (1)$$

$$Y_{E_k}(i) = h_{E_k}(i)X(i) + n_{E_k}(i) \quad (2)$$

where  $h_M(i)$  and  $h_{E_k}(i)$  denote the complex channel fading coefficients from Alice to Bob (main channel) and from Alice to the  $k^{\text{th}}$  Eve (wiretap channel), respectively. Moreover,  $n_M(i)$  and  $n_{E_k}(i)$  are the zero-mean circularly symmetric complex Gaussian noise random variables with unit variance of the main channel and wiretap channel, respectively. In order to simplify the analysis, we assume that both the main channel and each wiretap channel undergo  $\mathcal{F}$  composite fading, where the channel gains remain constant during the transmission of entire codewords, i.e.,  $\forall i \in \mathbb{Z}^+$ :  $h_M(i) = h_M$  and  $h_{E_k}(i) = h_{E_k}$ . Moreover, codewords are independent from each other and have an average transmit signal power ( $P$ ), i.e.,  $\frac{1}{N} \sum_{i=1}^N \mathbb{E}\{|X(i)|^2\} \leq P$ , whereas the average noise power in the main channel and wiretap channel are denoted by  $N_M$  and  $N_{E_k}$ . Consequently, the corresponding instantaneous signal-to-noise ratio (SNR) and average SNR at Bob are given by  $\gamma_M = P|h_M|^2/N_M$  and  $\bar{\gamma}_M = P\mathbb{E}\{|h_M|^2\}/N_M$ , respectively. Likewise, the instantaneous SNR and average SNR at the  $k^{\text{th}}$  Eve are given by  $\gamma_{E_k} = P|h_{E_k}|^2/N_{E_k}$  and  $\bar{\gamma}_{E_k} = P\mathbb{E}\{|h_{E_k}|^2\}/N_{E_k}$ , respectively. Also, the PDFs of  $\gamma_M$  and  $\gamma_{E_k}$  can be expressed with the corresponding parameters  $\{m_M, m_{s_M}, \bar{\gamma}_M\}$  and  $\{m_{E_k}, m_{s_{E_k}}, \bar{\gamma}_{E_k}\}$ , respectively, as

$$f_{\gamma_M}(\gamma_M) = \frac{m_M^{m_M} (m_{s_M} - 1)^{m_{s_M}} \bar{\gamma}_M^{m_{s_M}} \gamma_M^{m_M - 1}}{B(m_M, m_{s_M}) [m_M \gamma_M + (m_{s_M} - 1) \bar{\gamma}_M]^{m_M + m_{s_M}}}, \quad (3)$$

$$f_{\gamma_{E_k}}(\gamma_{E_k}) = \frac{m_{E_k}^{m_{E_k}} (m_{s_{E_k}} - 1)^{m_{s_{E_k}}} \bar{\gamma}_{E_k}^{m_{s_{E_k}}} \gamma_{E_k}^{m_{E_k} - 1}}{B(m_{E_k}, m_{s_{E_k}}) [m_{E_k} \gamma_{E_k} + (m_{s_{E_k}} - 1) \bar{\gamma}_{E_k}]^{m_{E_k} + m_{s_{E_k}}}}. \quad (4)$$

### III. SECURE OUTAGE PROBABILITY

The capacity of the main channel is given by  $C_M = \log_2(1 + \gamma_M)$  and the PDF of  $\gamma_M$  is given by (3). The

transmitted message is secure only when  $C_M$  is greater than that of any wiretap channel. Thus,  $C_E = \log_2(1 + \gamma_{E_m})$  where  $\gamma_{E_m} = \max(\gamma_{E_1}, \gamma_{E_2})$ , whose PDF is given by

$$f_{\gamma_{E_m}}(\gamma_{E_m}) = \sum_{i=1}^2 \left[ \prod_{j=1, j \neq i}^2 F_{\gamma_{E_j}}(\gamma_{E_m}) \right] f_{\gamma_{E_i}}(\gamma_{E_m}) \quad (5)$$

where

$$F_{\gamma_{E_j}}(\gamma_{E_m}) = \sum_{k_j=0}^{m_{E_j}-1} \binom{m_{E_j}-1}{k_j} \frac{(-1)^{k_j}}{B(m_{E_j}, m_{s_{E_j}}) (m_{s_{E_j}} + k_j)} \times \left( 1 - \frac{[(m_{s_{E_j}} - 1) \bar{\gamma}_{E_j}]^{m_{s_{E_j}} + k_j}}{[m_{E_j} \gamma_{E_m} + (m_{s_{E_j}} - 1) \bar{\gamma}_{E_j}]^{m_{s_{E_j}} + k_j}} \right) \quad (6)$$

which holds for  $m_{E_j} \in \mathbb{N}$ , whilst  $\binom{a}{b}$  is the binomial coefficient [29]. Thus, the secrecy capacity is expressed as

$$C_S(\gamma_M, \gamma_{E_m}) = \begin{cases} \log_2(1 + \gamma_M) - \log_2(1 + \gamma_{E_m}), & \gamma_M > \gamma_{E_m} \\ 0, & \gamma_M \leq \gamma_{E_m}. \end{cases} \quad (7)$$

When Alice sends data at a secrecy rate,  $\mathcal{R}_s > 0$ , higher than the secrecy capacity,  $C_s$ , the target error probability can not be satisfied. This leads to an outage in the communication between Alice and Bob, namely SOP, which is defined

$$P_{out}(\mathcal{R}_s) = \mathbb{P}[C_s \leq \mathcal{R}_s] = 1 - \mathbb{P}[C_s > \mathcal{R}_s] \quad (8)$$

where  $\mathbb{P}[C_s > \mathcal{R}_s]$  denotes the probability of successful secure transmission, which is given by

$$\mathbb{P}[C_s > \mathcal{R}_s] = \mathbb{P}\left[\log_2\left(\frac{1 + \gamma_M}{1 + \gamma_E}\right) > \mathcal{R}_s\right] \quad (9a)$$

$$= \mathbb{P}[\gamma_M > 2^{\mathcal{R}_s} (1 + \gamma_E) - 1] \quad (9b)$$

$$= \int_0^\infty f_{\gamma_E}(\gamma_E) \left[ \int_{2^{\mathcal{R}_s} (1 + \gamma_E) - 1}^\infty f_{\gamma_M}(\gamma_M) d\gamma_M \right] d\gamma_E \quad (9c)$$

$$= \int_0^\infty f_{\gamma_E}(\gamma_E) \left[ 1 - F_{\gamma_M}(2^{\mathcal{R}_s} (1 + \gamma_E) - 1) \right] d\gamma_E \quad (9d)$$

$$= 1 - \int_0^\infty f_{\gamma_E}(\gamma_E) F_{\gamma_M}(2^{\mathcal{R}_s} (1 + \gamma_E) - 1) d\gamma_E \quad (9e)$$

where  $F_{\gamma_M}(\cdot)$  is the CDF of  $\gamma_M$ , which for  $\mathcal{F}$  fading is

$$F_{\gamma_M}(\gamma_M) = \sum_{l=0}^{m_M-1} \binom{m_M-1}{l} \frac{(-1)^l}{B(m_M, m_{s_M})} \left\{ \frac{1}{m_{s_M} + l} - \frac{(m_{s_M} - 1)^{m_{s_M} + l} \bar{\gamma}_M^{m_{s_M} + l}}{(m_{s_M} + l) [m_M \gamma_M + (m_{s_M} - 1) \bar{\gamma}_M]^{m_{s_M} + l}} \right\}, m_M \in \mathbb{N}. \quad (10)$$

Hence, the corresponding SOP in the presence of multiple Eves can be expressed from (8) and (9e), such that

$$P_{out}(\mathcal{R}_s) = \int_0^\infty f_{\gamma_{E_m}}(\gamma_{E_m}) F_{\gamma_M}(2^{\mathcal{R}_s} (1 + \gamma_{E_m}) - 1) d\gamma_{E_m}. \quad (11)$$

Let us begin by studying the case of two Eves which experience independent and identically distributed (*i.i.d.*) composite fading. By substituting (5) and (10) into (11), we obtain

$$\mathcal{P}_{out}(\mathcal{R}_s) = 2 \sum_{l=0}^{m_M-1} \sum_{k_1=0}^{m_E-1} \binom{m_M-1}{l} \binom{m_E-1}{k_1} \times \frac{(-1)^{l+k_1} m_E^{m_E} [(m_{s_E}-1)\bar{\gamma}_E]^{m_{s_E}} \{ \mathcal{I}_1 - \mathcal{I}_2 - \mathcal{I}_3 + \mathcal{I}_4 \}}{B^2(m_E, m_{s_E}) B(m_M, m_{s_M}) (m_{s_M}+l)(m_{s_E}+k_1)} \quad (12)$$

where

$$\mathcal{I}_1 = \int_0^\infty \frac{\gamma_{E_m}^{m_E-1}}{[m_E \gamma_{E_m} + (m_{s_E}-1)\bar{\gamma}_E]^{m_E+m_{s_E}}} d\gamma_{E_m} \quad (13)$$

$$\mathcal{I}_2 = \int_0^\infty \frac{\gamma_{E_m}^{m_E-1}}{[m_E \gamma_{E_m} + (m_{s_E}-1)\bar{\gamma}_E]^{m_E+m_{s_E}}} \times \left[ \frac{m_M(2^{\mathcal{R}_s}(1+\gamma_{E_m})-1)}{(m_{s_M}-1)\bar{\gamma}_M} + 1 \right]^{-(m_{s_M}+l)} d\gamma_{E_m} \quad (14)$$

$$\mathcal{I}_3 = \int_0^\infty \frac{\gamma_{E_m}^{m_E-1} [(m_{s_E}-1)\bar{\gamma}_E]^{m_{s_E}+k_1}}{[m_E \gamma_{E_m} + (m_{s_E}-1)\bar{\gamma}_E]^{m_E+2m_{s_E}+k_1}} d\gamma_{E_m} \quad (15)$$

and

$$\mathcal{I}_4 = \int_0^\infty \frac{\gamma_{E_m}^{m_E-1} [(m_{s_E}-1)\bar{\gamma}_E]^{m_{s_E}+k_1}}{[m_E \gamma_{E_m} + (m_{s_E}-1)\bar{\gamma}_E]^{m_E+2m_{s_E}+k_1}} \times \left[ \frac{m_M(2^{\mathcal{R}_s}(1+\gamma_{E_m})-1)}{(m_{s_M}-1)\bar{\gamma}_M} + 1 \right]^{-(m_{s_M}+l)} d\gamma_{E_m}. \quad (16)$$

With the aid of [29, Eq. (3.194.3)], [29, Eq. (3.197.1)] and after some manipulations, the following expressions are obtained

$$\mathcal{I}_1 = \frac{B(m_E, m_{s_E})}{m_E^{m_E} [(m_{s_E}-1)\bar{\gamma}_E]^{m_{s_E}}} \quad (17)$$

$$\mathcal{I}_2 = \frac{\mathcal{D}_1^{m_E} \mathcal{D}_2^{m_{s_M}+l} B(m_E, \mathcal{D}_3)}{m_E^{m_E} [(m_{s_E}-1)\bar{\gamma}_E]^{m_{s_E}}} \times {}_2F_1\left(m_E + m_{s_E}, m_E; m_E + \mathcal{D}_3; 1 - \mathcal{D}_1\right) \quad (18)$$

$$\mathcal{I}_3 = \frac{B(m_E, 2m_{s_E} + k_1)}{m_E^{m_E} [(m_{s_E}-1)\bar{\gamma}_E]^{m_{s_E}}} \quad (19)$$

and

$$\mathcal{I}_4 = \frac{B(m_E, \mathcal{D}_4) \mathcal{D}_1^{m_E} \mathcal{D}_2^{m_{s_M}+l}}{m_E^{m_E} [(m_{s_E}-1)\bar{\gamma}_E]^{m_{s_E}}} \times {}_2F_1(m_E + 2m_{s_E} + k_1, m_E; m_E + \mathcal{D}_4; 1 - \mathcal{D}_1) \quad (20)$$

where  $\mathcal{D}_1 = \frac{m_E[m_M(2^{\mathcal{R}_s}-1) + (m_{s_M}-1)\bar{\gamma}_M]}{m_M 2^{\mathcal{R}_s} (m_{s_E}-1)\bar{\gamma}_E}$ ,  $\mathcal{D}_2 = \frac{(m_{s_M}-1)\bar{\gamma}_M}{m_M(2^{\mathcal{R}_s}-1) + (m_{s_M}-1)\bar{\gamma}_M}$ ,  $\mathcal{D}_3 = m_{s_E} + m_{s_M} + l$ ,  $\mathcal{D}_4 = 2m_{s_E} + k_1 + m_{s_M} + l$  and  ${}_2F_1(\cdot, \cdot; \cdot; \cdot)$  denotes the Gauss hypergeometric function [29, Eq. (9.111)]. Substituting (17), (18), (19) and (20) into (12) and after some algebraic manipulations, the SOP in the presence of two Eves which experience

*i.i.d.*  $\mathcal{F}$  composite fading can be obtained in closed-form as

$$\mathcal{P}_{out}(\mathcal{R}_s) = \sum_{l=0}^{m_M-1} \sum_{k_1=0}^{m_E-1} \binom{m_M-1}{l} \binom{m_E-1}{k_1} \times \frac{2(-1)^{l+k_1}}{B^2(m_E, m_{s_E}) B(m_M, m_{s_M}) (m_{s_M}+l)(m_{s_E}+k_1)} \times \left\{ B(m_E, m_{s_E}) - B(m_E, 2m_{s_E}+k_1) - \mathcal{D}_1^{m_E} \mathcal{D}_2^{m_{s_M}+l} [\mathcal{Q}_1 - \mathcal{Q}_2] \right\} \quad (21)$$

where

$$\mathcal{Q}_1 = B(m_E, \mathcal{D}_3) {}_2F_1(m_E + m_{s_E}, m_E; m_E + \mathcal{D}_3; 1 - \mathcal{D}_1) \quad (22)$$

and

$$\mathcal{Q}_2 = B(m_E, \mathcal{D}_4) {}_2F_1(m_E + 2m_{s_E} + k_1, m_E; m_E + \mathcal{D}_4; 1 - \mathcal{D}_1). \quad (23)$$

#### IV. NUMERICAL RESULTS

Fig. 1 shows the behavior of the SOP over  $\mathcal{F}$  composite fading channels in the presence of a single Eve ( $L = 1$ ) for different values of  $m_M$ ,  $m_{s_M}$ ,  $\bar{\gamma}_M$  and  $\mathcal{R}_s$  when  $m_E = 2$ ,  $m_{s_E} = 2$  and  $\bar{\gamma}_E = 10$  dB. It is clear that, irrespective of the values of  $m_M$ ,  $m_{s_M}$  and  $\mathcal{R}_s$ , the SOP decreases as  $\bar{\gamma}_M$  increases. For comparison, in Fig. 1, we consider the red continuous curve as a reference, where both main channel and Eve channel experience the same fading conditions ( $m_M = m_E = 2$ ,  $m_{s_M} = m_{s_E} = 2$ ). When looking at the cases of ( $m_E = 10$ ,  $m_{s_E} = 2$ ) and ( $m_E = 2$ ,  $m_{s_E} = 10$ ), i.e., when the main channel conditions ( $m_M = 2$ ,  $m_{s_M} = 2$ ) are worse than those for the Eve channel ( $m_E = 3$ ,  $m_{s_E} = 3$ ), the SOP decreases compared to the reference plot. Moreover, it is obvious that as the secrecy rate ( $\mathcal{R}_s$ ) increases, the SOP increases. Interestingly, the effect of  $m_E$  (i.e., the multipath fading parameter) on the SOP becomes less significant compared to that of  $m_{s_E}$  (i.e., the shadowing parameter). Figs. 1 also include the SOP (line with circles) over  $\mathcal{F}$  composite fading channels in the presence of two Eves ( $L = 2$ ) which experience *i.i.d.*  $\mathcal{F}$  composite fading. For all of the composite fading conditions, it is clear that the SOP increases as the number of Eves increases to two ( $L = 2$ ), demonstrating the impact of an increasing number of Eves upon the SOP.

Fig. 2 illustrates the corresponding SOP in the presence of two Eves which experience independent and not identically distributed (*i.n.i.d.*)  $\mathcal{F}$  composite fading when  $m_M = 2$ ,  $m_{s_M} = 2$  and  $\mathcal{R}_s = 0.2$ . For comparison, in Fig. 2, we consider the red continuous curve as a reference, where the both Eve channels experience the same fading conditions ( $m_{E_1} = m_{E_2} = 2$ ,  $m_{s_{E_1}} = m_{s_{E_2}} = 2$ ,  $\bar{\gamma}_{E_1} = \bar{\gamma}_{E_2} = 10$  dB). When the  $m_{E_2}$ ,  $m_{s_{E_2}}$ ,  $\bar{\gamma}_{E_2}$  parameters increase, i.e., the second Eve channel conditions become better than those for the first Eve channel conditions ( $m_{E_1} = 2$ ,  $m_{s_{E_1}} = 2$ ,  $\bar{\gamma}_{E_1} = 10$ ), the SOP increases compared to the reference plot.

#### V. CONCLUSION

This paper addressed the physical layer security and fading characteristics of device to device communications in terms

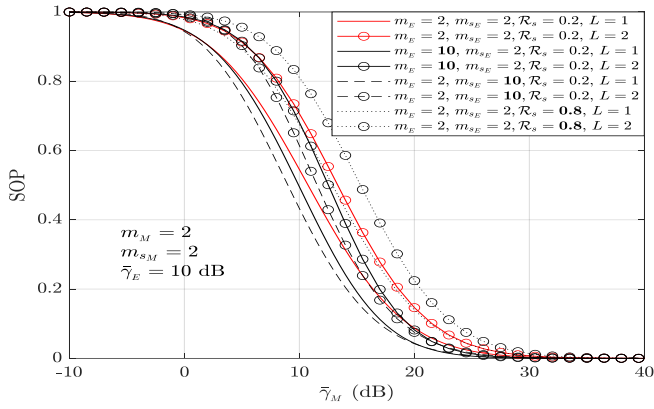


Fig. 1. SOP versus  $\tilde{\gamma}_M$  considering different  $m_E$ ,  $m_{s_E}$ ,  $\mathcal{R}_s$  and  $L$  (a number of Eves) when  $m_M = 2$ ,  $m_{s_M} = 2$  and  $\tilde{\gamma}_E = 10$  dB.

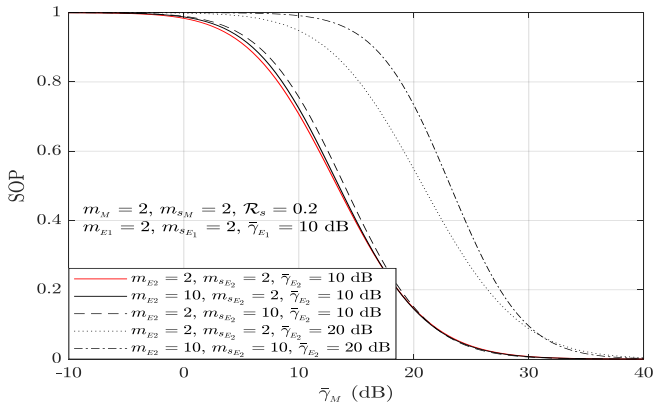


Fig. 2. SOP versus  $\tilde{\gamma}_M$  in the presence of *i.i.d.* two Eves when  $m_M = 2$ ,  $m_{s_M} = 2$  and  $\mathcal{R}_s = 0.2$  dB.

of the achievable secure outage probability in the presence of two eavesdroppers and  $\mathcal{F}$  composite fading channels. In this context, a novel closed-form expression was derived for the corresponding SOP which then assisted in developing useful insights into the behavior of the SOP as a function of the key parameters of  $\mathcal{F}$  composite fading channels as well as the number of Eves. The derived analytic results are novel and were corroborated by results from computer simulations.

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