






Number-resolved detection of dark ions in Coulomb crystals

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While it is straightforward to count laser-cooled trapped ions by fluorescence imaging, detecting the number of dark ions embedded and sympathetically cooled in a mixed ion crystal is more challenging. We demonstrate a method to track the number of dark ions in real time with single-particle sensitivity. This is achieved by observing discrete steps in the amount of fluorescence emitted from the coolant ions while exciting secular motional resonances of dark ions. By counting the number of fluorescence steps, we can identify the number of dark ions without calibration and without relying on any physical model of the motional excitation. We demonstrate the scheme by detecting H_2^+ and H_3^+ ions embedded in a Be^+ ion Coulomb crystal in a linear radio-frequency trap. Our method allows observing the generation and destruction of individual ions simultaneously for different types of ions. Besides high-resolution spectroscopy of dark ions, another application is the detection of chemical reactions in real time with single-particle sensitivity. This is demonstrated in this Letter.

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Trapped and laser-cooled ions have been used to investigate fundamental light-atom interactions [1–5], for the observation of ion-neutral chemical reactions [6–10], as well as for optical frequency standards [11,12] and quantum computing [13–15].

Sympathetic cooling is a way for extending this technology to atomic or molecular ions that do not possess suitable transitions for laser cooling. In this scheme, the ions are trapped together with another ion species that can be laser cooled. Due to the mutual Coulomb interaction, the ions rapidly thermalize, indirectly cooling all species. At sufficiently low temperatures, the ions form regular Coulomb crystals in the trap [16]. The technique has found application in precision spectroscopy of HD^+ and H_2^+ molecular ions [17–21], optical atomic clocks based on quantum logic spectroscopy of Al^+ [22,23], spectroscopy of highly charged ions [24,25], and the study of chemical reactions with molecular ions [7,26–29].

While the number of laser-cooled ions can be easily measured by fluorescence imaging, identification and counting of the nonfluorescing dark ions is more difficult. One method is to eject the ions from the trap and to accelerate them onto a detector in an electric field. The different ion species can be distinguished by their arrival times [30–33]. While this method allows a quantitative measurement of the number of ions of each species, it has the disadvantage that it is de-

structive and a new ion crystal has to be prepared after each measurement.

In linear Paul traps, lighter ions are more tightly confined than heavier ions. Lighter sympathetically cooled ions therefore form a dark region in the center of the fluorescence image of an ion crystal consisting of a heavier coolant species. The number of dark ions can then be obtained by comparing experimental images with simulated ones [17,34,35]. This method is nondestructive, and the ion images can be acquired quickly and postprocessed later. However, different dark-ion species cannot be distinguished.

Instead, secular excitation has been used for the nondestructive detection of trapped ions. In this method the secular motion of the ions, i.e., the harmonic motion in the time-averaged trap potential, is excited resonantly by applying an additional oscillating electric field. This transfers energy into the motion of the surrounding coolant ions and thereby increases their temperature. Due to the temperature dependence of the Doppler broadening this leads to a change in the amount of fluorescence that can be observed from the coolant ions. The secular motion of the ions in three-dimensional Coulomb crystals has rich dynamics that can complicate the analysis of the secular excitation spectra. For example, the frequencies of the secular resonances are influenced by space-charge effects and the mechanical coupling between the ions [36–38]. The energy transfer to the coolant ions is expected to increase with an increasing number of dark ions. Therefore, the fluorescence change induced by motional excitation serves as a measure of the number of dark ions. However, the relationship between the fluorescence change and the number of excited dark ions is in general nonlinear and is influenced by various experimental parameters, such as the strength of the motional excitation and the geometry of the mixed ion crystal. Therefore, evaluating the number of dark ions quantitatively is challenging and often requires intricate modeling and calibration of the signal using

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molecular dynamics simulations [26,39]. This problem has been limiting the usage of the secular excitation method for highly precise spectroscopy so far.

In this Letter, we show that by properly choosing experimental parameters, discrete steps in the secular excitation signal can be observed that are identified with individual dark ions leaving the trap or being generated within the trap. Hence such a signal is autocalibrating and counting the number of ions gives the ultimate accuracy. The signal does not have to be calibrated using a physical model of the secular excitation. Spurious signals at other frequencies that may arise from motional coupling have no influence on the counting process and can be safely ignored.

We experimentally demonstrate this method by resonantly exciting the radial motion of H_2^+ and H_3^+ ions embedded in a laser-cooled Be^+ ion crystal. We observe concomitant changes in the amount of fluorescence from the Be^+ ions when the number of trapped H_2^+ or H_3^+ ions changes due to chemical reactions with neutral rest gas molecules.

Spectroscopy of dark ions requires a scheme for detecting that the target transition is being excited. This can for example be achieved by monitoring that new ion species are created by state-dependent photoionization [40] or resonance-enhanced multiphoton dissociation [18–20,39]. The reliable detection of single dark ions demonstrates that this detection scheme can be single-event sensitive and that the spectroscopy will be ultimately limited only by quantum projection noise. Nonlinearities in the signal intensity may introduce a systematic frequency shift, especially when the spectrum consists of multiple overlapping lines [39]. Accurate counting of the dark ions gives rise to a spectroscopy signal with negligible nonlinearity.

Chemical reactions at ultracold temperatures can be investigated precisely for a small number of atoms or ions after careful quantum-state preparation [41]. Our detection scheme can be employed to efficiently capture such events with single-particle sensitivity.

We use a linear Paul trap to confine the ions. As shown in Fig. 1, it consists of four blade electrodes that are spaced 0.45 mm from the trap axis and have an axial length of 3.00 mm. Axial confinement is provided by two end-cap electrodes that are located 3.50 mm from the trap center.

The trap is driven with a radio frequency (rf) of 66.05 MHz with an amplitude of around 120 V, and a static voltage of 400 V is applied to the end caps. For Be^+ this results in a radial secular frequency of around 1.6 MHz, corresponding to a Mathieu stability parameter $q \approx 0.07$ [5], and an axial secular frequency of 645 kHz. The single-particle radial secular frequency scales proportional to the ion's charge-to-mass ratio. The theoretical values are 4.8 and 7.2 MHz for H_3^+ and H_2^+ , respectively.

The Be^+ ions are laser cooled by driving the $2s\ ^2S_{1/2}(F=2) \rightarrow 2p\ ^2P_{3/2}(F=3)$ cycling transition with circularly polarized 313-nm light that is generated by sum-frequency generation of two continuous-wave fiber lasers at 1051 and 1550 nm and subsequent frequency doubling [42]. The cooling transition has a natural linewidth of $\Gamma = 2\pi \times 18$ MHz [43], and the cooling beam contains two frequency components that are red detuned from the transition by 130 and 460 MHz. We found that adding the far-detuned component

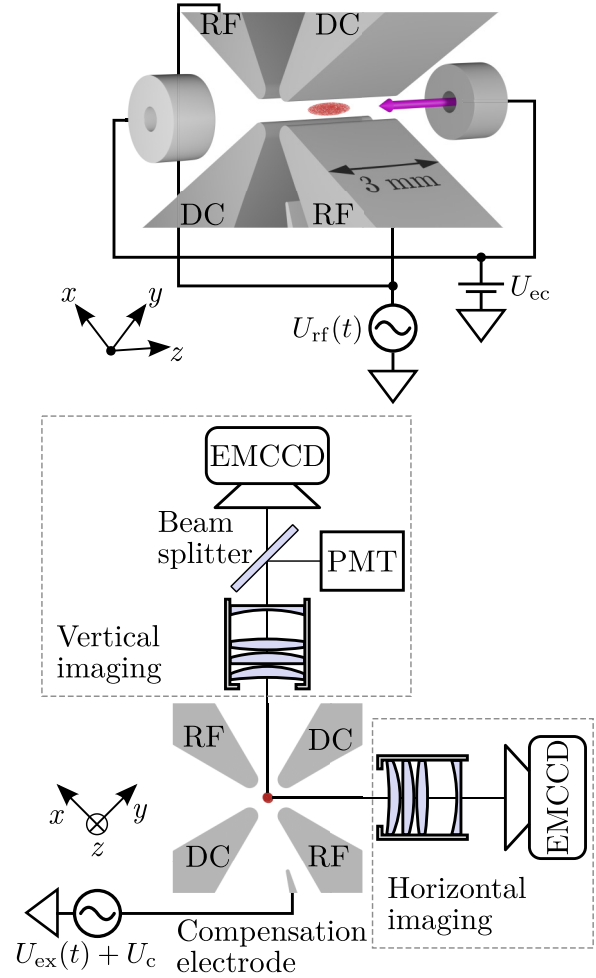


FIG. 1. Geometry of the ion trap setup. Radial (top) and axial (bottom) view. The Coulomb crystal is not drawn to scale. Radial confinement is generated by the rf voltage $U_{rf}(t)$ that is applied to one diagonal pair of blade electrodes. A static voltage U_{cc} is applied to the end-cap electrodes for axial confinement. The cooling beam (purple) is directed along the trap axis (z). The fluorescence from the laser-cooled Be^+ ions is imaged onto two EMCCD cameras. The static compensation voltage U_c and voltages applied to the two dc blade electrodes are used to compensate stray fields in the trap caused by patch potentials and electrode misalignment. A sinusoidal voltage $U_{ex}(t)$ is added to the compensation electrode in order to excite the secular motion of the trapped ions.

makes the system more robust against losing the trapped ions when strongly driving secular excitations. Both frequency components can be switched on or off separately and have similar intensities of around I_{sat} , where $I_{sat} = 765 \text{ W/m}^2$ is the saturation intensity of the cooling transition [43]. The cooling beam is aligned parallel to the trap axis and propagates through holes in the end-cap electrodes. A weak magnetic field is applied parallel to the beam in order to define the quantization axis. We use an electro-optic modulator to create 1.25 GHz sidebands on the cooling laser in order to repump the ions out of the $2s\ ^2S_{1/2}(F=1)$ dark state.

The trap is housed in an ultrahigh vacuum chamber. The background pressure measured with a cold-cathode ion gauge is around 4×10^{-11} mbar.

We load Be^+ ions into the trap with the help of a beam of beryllium atoms from an oven. The beam is sent through the trapping region where it is overlapped with a 235-nm laser beam that resonantly ionizes the atoms [44]. During Be^+ loading, initially only the far-detuned frequency component is applied to efficiently cool the hot ions. Once fluorescence from trapped ions is detected, the near-detuned frequency component is turned on. This strongly increases the fluorescence signal, such that the ion crystal shape can be monitored. The ionization laser is turned off when the desired ion crystal size is reached.

We then turn on a home-built electron gun for 1 s with a current of about $95 \mu\text{A}$. The electrons ionize some of the hydrogen molecules from the residual gas in our vacuum chamber, and the resulting molecular ions become embedded in the ion crystal.

As shown in Fig. 1, we use two imaging systems to observe the fluorescence from the laser-cooled ions from the horizontal and vertical direction perpendicular to the trap axis. In each system, the light is imaged onto an electron-multiplying CCD (EMCCD) camera using a home-built objective with magnification $M \approx 9$ and a numerical aperture of 0.23. The vertical imaging system additionally contains a beam splitter that sends roughly half of the light onto a photomultiplier tube (PMT).

Figures 2(a) and 2(b) show typical fluorescence images of an ion crystal in our setup. We believe that the asymmetric shape visible in Fig. 2(b) is due to imperfect alignment of the trap electrodes.

In order to measure the radial secular frequencies of the trapped ions, we excite their motion by applying a sinusoidal voltage to the compensation electrode that is located close to the trap electrodes (see Fig. 1). We sweep the frequency range between 2 and 10 MHz in 500 steps and for each frequency collect photon counts with the PMT for 10 ms. This is slow enough that the ion motion reaches steady state for each frequency point. Figure 3 shows a typical resulting secular spectrum. Two peaks at 4.6 and 7.1 MHz can be observed which we attribute to H_3^+ and H_2^+ ions, respectively. The electrode that we use for the secular excitation is low-pass filtered with a 1-nF capacitor and is not impedance matched to the 50Ω output impedance of the function generator that produces the excitation signal. This makes the electric field amplitude at the position of the ions frequency dependent. In addition, the efficiency of the motional excitation might be different for H_3^+ and H_2^+ ions. We therefore use two different excitation amplitudes for the frequency range from 2 to 5.5 MHz and from 5.5 to 10 MHz. The amplitudes are chosen to give roughly the same signal strength per ion for the H_2^+ and H_3^+ resonances.

We then repeatedly perform secular scans over a period of a few minutes. Figure 4 shows how the height of the secular resonances changes over time in a typical experiment. We normalize the peak heights of each scan to the off-resonant scattering rate. This compensates for small drifts in the cooling laser power and Be^+ ion loss during the measurement. The height of the H_2^+ signal drops in steps until after around 360 s the peak is no longer visible. The height of the H_3^+ signal increases in steps that coincide with drops of the H_2^+ signal. We attribute this to individual H_2^+ ions reacting with

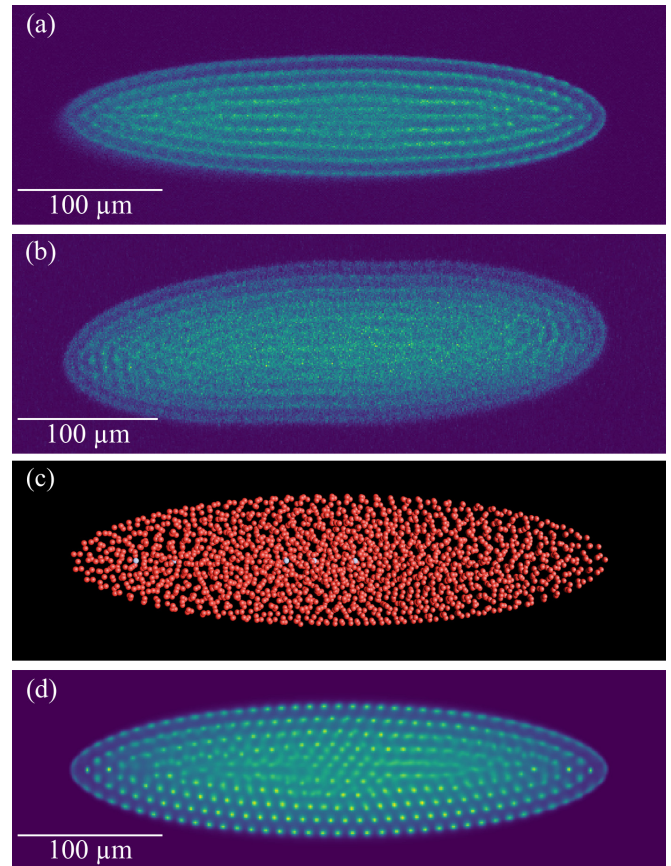


FIG. 2. Fluorescence images of an ion crystal consisting of around 2000 Be^+ ions with a few embedded H_2^+ and H_3^+ ions: (a) Horizontal and (b) vertical view. (c) Coulomb crystal containing 2000 Be^+ ions (red spheres) and 5 H_2^+ ions (light blue spheres) obtained by the molecular dynamics simulation. (d) Simulated ion image for the crystal shown in (c) at 10 mK.

molecular hydrogen from the residual gas to form neutral hydrogen and H_3^+ according to the exothermic chemical reaction $\text{H}_2^+ + \text{H}_2 \rightarrow \text{H}_3^+ + \text{H}$ [45]. The clearly visible steps in the signals show that we are observing individual ions being

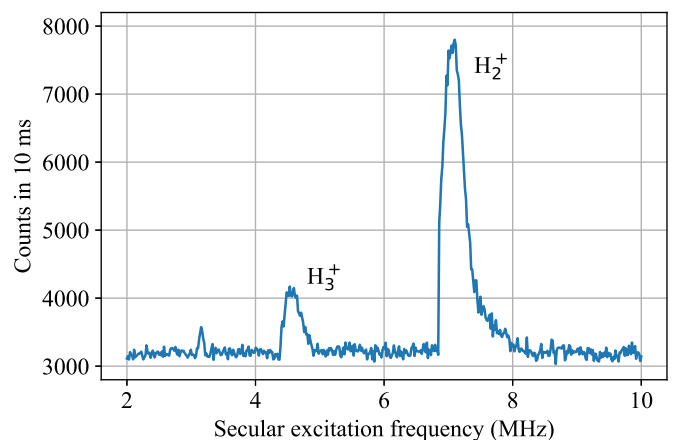


FIG. 3. Secular spectrum showing the presence of H_2^+ and H_3^+ ions embedded in the Be^+ coolant ions.

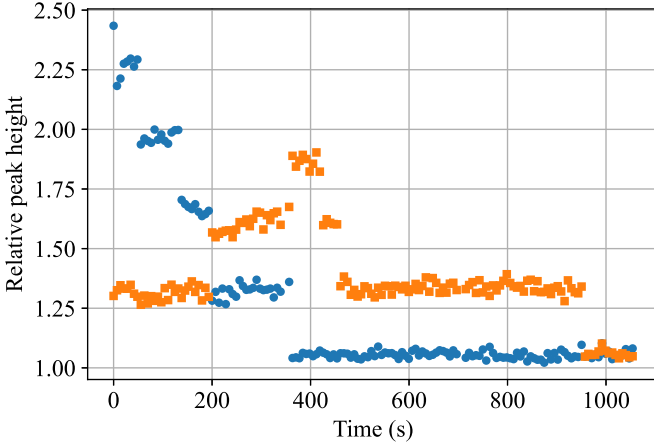


FIG. 4. Change of the fluorescence peak heights at the H_2^+ (blue circles) and H_3^+ (orange squares) resonances over time. For each measurement, the peak heights are normalized to the off-resonant scattering rate. The stepwise changes of the peak heights are caused by individual ions undergoing chemical reactions with residual gas molecules. Within each step, the peak heights scatter by much less than the step-to-step difference. Each secular scan therefore allows a reliable determination of the ion numbers.

destroyed or created within the Coulomb crystal. Sometimes the H_2^+ signal drops without a corresponding increase in the H_3^+ signal. One possible explanation is that the H_2^+ ion reacted with a different residual gas molecule such as N_2 , O_2 , or H_2O [46]. Another possibility is that the kinetic energy transferred to the H_3^+ molecule in the chemical reaction is large enough to sometimes allow the product to escape from the trap. Rate constants for the chemical reactions between H_2^+ and typical residual gas molecules are in the range of $2\text{--}7 \times 10^{-9} \text{ cm}^3 \text{ s}^{-1}$ [45,46]. An exponential fit to the H_2^+ ion number yields a total decay rate of 0.006 s^{-1} which corresponds to a residual gas pressure in the range of $4 \times 10^{-11}\text{--}1 \times 10^{-10} \text{ mbar}$, in rough agreement with the pressure indicated by the vacuum gauge. The number of H_3^+ ions subsequently drops in similar steps over the timescale of a few minutes. We attribute this to proton transfer reactions of the type $\text{H}_3^+ + X \rightarrow \text{HX}^+ + \text{H}_2$ which are possible with a number of residual gas molecules such as N_2 , CO , CO_2 , and H_2O [47].

One striking feature of Figs. 4 and 5 is that the fluorescence peak heights are nearly linear in the number of dark ions. We use the LAMMPS molecular dynamics code [48,49] to further investigate this behavior. We first simulate the stationary configuration of the mixed ion crystals without applying the excitation as shown in Fig. 2(c). We generate simulated fluorescence images, taking into account the motion of the ions and the spot size and depth of field of the imaging objective. We then estimate the number of trapped ions in the experiment and their temperature by comparing the simulated images with the experimental ones [34,35,37]. A good agreement is obtained between experimental and simulated images for around 2000 Be^+ ions at 10 mK mixed with a few dark ions as shown in Fig. 2(d). In order to simulate the secular excitation spectra, we add an oscillating electric field perpendicular to the trap axis. The amount of fluorescence from the coolant ions is calculated during the motional excitation. The simulation is

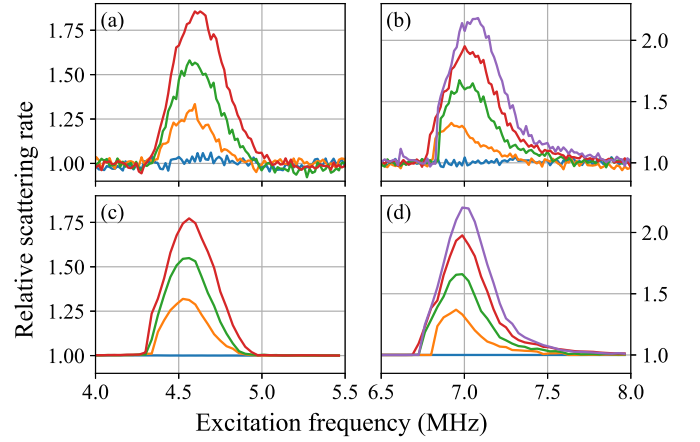


FIG. 5. Experimental secular excitation spectra for (a) 0–3 H_3^+ ions and (b) 0–4 H_2^+ ions. (c) and (d) are spectra obtained from molecular dynamics simulations with 2000 Be^+ ions and the same numbers of H_2^+ and H_3^+ ions as in the experiment. The simulated excitation amplitudes are 2.9 V/m for the H_3^+ resonance and 2.5 V/m for the H_2^+ resonance.

repeated for different excitation frequencies and numbers of dark ions. Figures 5(a) and 5(b) show experimental secular excitation spectra for different numbers of H_3^+ and H_2^+ ions, and Figs. 5(c) and 5(d) show the corresponding simulated spectra. The stepwise change of the fluorescence peak height for different numbers of ions is reproduced in the simulations. Both the simulation and the measurement suggest that the change in the amount of fluorescence is roughly proportional to the number of dark ions that are being excited at their secular frequency.

We now derive a model for the dependence of the peak scattering rate on the number of ions that are being excited. For a cycling cooling transition in an atom at rest the photon scattering rate is given by

$$w(\Delta) = \frac{s\Gamma/2}{1 + s + (\frac{\Delta}{\Gamma/2})^2}, \quad (1)$$

where Δ is the laser detuning and $s = I/I_{\text{sat}}$ is the saturation parameter. During the secular excitation, the temperature of the coolant ions increases to T_s , and the scattering rate per Be^+ ion is given by [39]

$$R(T_s) = \int_{-\infty}^{\infty} w(\Delta - kv)p(v, T_s)dv, \quad (2)$$

where $p(v, T) = \sqrt{m_{\text{Be}}/(2\pi k_B T)} \exp[-m_{\text{Be}}v^2/(2k_B T)]$ is the Maxwell-Boltzmann distribution. v is the velocity of the ion along the cooling laser beam, k is the cooling laser wave number, and m_{Be} is the Be^+ mass. We assume that the coolant ion temperature T_s during the secular excitation is determined by the balance between the heating due to the motional excitation and the average laser cooling power. This condition is expressed as

$$N_{\text{Be}}p_c(T_s) = N_{\text{ex}}p_h, \quad (3)$$

where N_{Be} is the number of Be^+ ions and N_{ex} is the number of dark ions that are being excited. p_h is the heating power per excited dark ion. Note that the average cooling power per

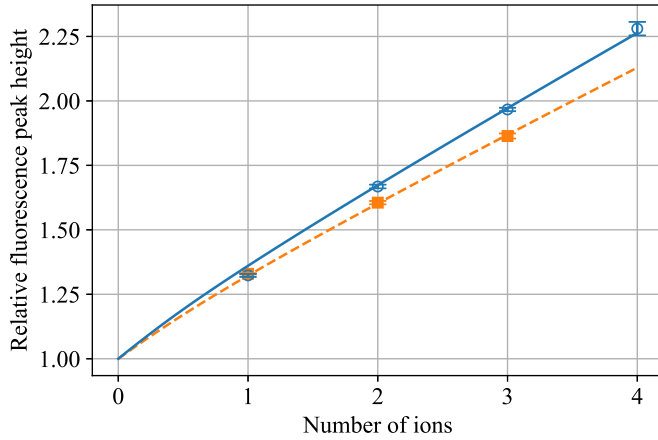


FIG. 6. Average peak heights of the H_2^+ (blue circles) and H_3^+ (orange squares) secular resonances. The error bars show the standard error of the mean. The solid and dashed lines are fits of our model curve $R(T_s)/R(T_0)$ to the H_2^+ and H_3^+ data, respectively. Separate fits are performed for the H_2^+ and H_3^+ resonances since the secular excitation strength is different for the two species and two different fit parameters $\alpha_{\text{H}_2^+}$ and $\alpha_{\text{H}_3^+}$ were necessary.

coolant ion $p_c(T_s)$ is temperature dependent because of the Doppler broadening of the cooling transition

$$p_c(T_s) = -\hbar k \int_{-\infty}^{\infty} v w (\Delta - kv) p(v, T_s) dv. \quad (4)$$

We confirmed the validity of our assumption of Eq. (3) using the molecular dynamics simulations (see Supplemental Material [50]). The relative fluorescence peak heights of the secular resonances shown in Fig. 4 correspond to $R(T_s)/R(T_0)$ where T_0 is the equilibrium temperature of the Be^+ ions in the absence of heating due to secular excitation. Under our exper-

imental conditions, T_0 is around 10 mK. For simplicity we use $T_0 = 0$ K which introduces a marginal ($\sim 2\%$) difference in the scattering rate. It is difficult to precisely estimate the heating rate p_h from the experimental parameters. We therefore treat $\alpha = p_h/N_{\text{Be}}$ as a free parameter in our model. We evaluated $R(T_s)/R(T_0)$ numerically and determined α to best reproduce the experimental data. No other fit parameters were used. The results are shown in Fig. 6 for different numbers of H_2^+ and H_3^+ ions. For our parameters the model predicts a nearly linear dependence of the scattering rate on the number of dark ions, which agrees with the experimental observations.

With a larger number of dark ions, the model predicts that the fluorescence peak height starts to saturate, and the fluorescence steps become smaller accordingly. We have conducted experiments for a larger number of dark ions and confirmed that up to eight dark ions can be reliably counted under our experimental conditions. Additional molecular dynamics simulations with different numbers of dark/coolant ions and different dark-ion species suggest that our method is robust for a wide range of experimental parameters.

In conclusion, we have demonstrated that the secular excitation technique can be used to detect dark ions embedded in laser-cooled ion Coulomb crystals with single-particle resolution. Secular excitation only relies on the Coulomb interaction between the different ion species. We therefore believe that this method could be used for single-particle sensitive detection of a wide range of atomic or molecular ions that do not possess suitable cycling transitions for fluorescence detection.

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