Effects of gravity modulation on the dynamics of a radial $A + B \rightarrow C$ reaction front

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Abstract

The dynamics of radial $A+B \rightarrow C$ reaction fronts can be affected by buoyancy-driven convection. Motivated by recent advances in the theory of reaction–diffusion–advection (RDA) systems, we investigated experimentally a radial $A+B \rightarrow C$ RDA system under modulated gravity environment, using a Hele-Shaw cell setup on board a parabolic flight. We evaluated characteristic properties of the RDA models, such as the temporal evolution of the total amount of product C, the width and position of the reaction front and compared them with theoretical predictions. During increased gravity, we observed an increase in both the total amount of product C formed and the front width, compared to the corresponding normal-gravity experiments. This is caused by the stronger buoyancy-driven convection in the former case. Finally, we report on experiments performed entirely in the absence of gravity, thus eliminating any buoyancy-driven convection. Despite the short observation time, the comparison with the ground experiments showed the significant effect that

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buoyant convection has on radial RDA fronts, enhancing mixing and increasing product generation.

1. Introduction

Reaction–Diffusion (RD) $A+B \rightarrow C$ fronts are generated when two (initially separated) chemical species, A and B, come into contact, mix diffusively and react to form a product, C, via the scheme $A + B \rightarrow C$. This leads to the formation of a sustained *chemical front*, i.e., a spatially localized region with a non-zero production rate. These RD fronts have been the focus of interest in an increasing number of studies since the work by Gálfi and Rácz in 1988 [1]. In a radial geometry (Fig. 1), a chemical front develops as a one-dimensional system (along the radial direction, r), when only A is present for $r < r_0$ and only B for $r > r_0$, where r_0 is the point of initial contact. At $t = 0$, A and B come in contact triggering a reaction front where A and B are consumed and C is generated. Typical properties such as the concentration profiles of A, B and C, as well as the front width, W_C, are introduced in the schematic of Fig. 1a for $t > 0$.
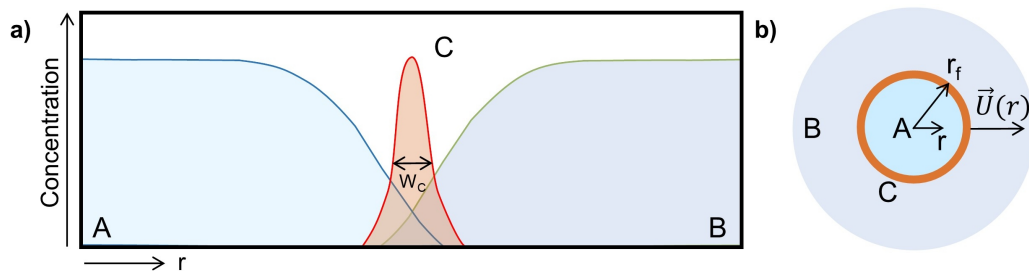
Fig. 1. (a) Schematic of a RD front in a qualitative concentration-distance view. The concentrations of the reactants (A, B) and product (C) are not to scale. (b) Schematic of a radial RDA front in top view. The injection flow results in a flow velocity $\vec{U}(r)$ that depends on the radial distance r. Characteristic measures such as the front's width, W_C and outer radius, r_f are also shown.

Since the dynamics underlying these systems affect the spatiotemporal distribution of the product and the initial conditions may affect the reaction yield, understanding the underlying physics

and chemistry has long been of great scientific interest [2–4]. Detailed analytical [1], experimental [5] and computational studies [6, 7] have provided scaling laws for relevant reaction front variables.

RD dynamics have been used to describe a large variety of physical systems, e.g., epidemiology, as recently applied to the spread of COVID-19 [8], pattern formation in biology [9], demographics and paleoanthropology (where human presence and expansion has been modelled through RD equations, accounting for environmental factors [10]), linguistics (as in the case of language death processes [11]), population dynamics [12], ecology [13], finance [14], digital image restoration [15] and particle physics [16].

In numerous natural and technological applications, the reactant A is injected at a steady flow rate into a region initially occupied by reactant B. These reaction–diffusion–advection (RDA) systems are of significantly increased complexity, especially when the advection flow field is not uniform. Consequently, reaction front systems under flow conditions have come into the focus of current research.

Applications of these $A + B \to C$ RDA systems are found in combustion [17], atmospheric chemistry [18], environmental systems [19, 20], engineering geology [21], and carbon capture and storage (CCS) [22]. In chemical engineering and technology, RDA dynamics can play a role in microchip-oriented studies investigating certain types of microreactor technologies, e.g., under creeping laminar flow conditions [23, 24]. They further provide access to small-scale pattern formation in autocatalytic processes [25]. In the past, radial RDA setups were used to generate self-assembled precipitation structures [26–28], selective composition of the reaction product and thermodynamically locked crystals [29].

Fig. 1b depicts a schematic overview of the RDA front in a planar geometry with central injection. A solution of reactant A is continuously fed into a solution of reactant B, which is initially present in the radial reactor, to form the product C. The flow velocity $\vec{U}(r)$ depends on the radial position r. Important variables to describe the reaction front are its radial distance from the inlet, r_f, and the front width, W_C. The full set of variables will be defined in detail later. For this radial geometry, scalings of the dynamics have been obtained by a one-dimensional approach that takes into account the gap-averaged radial flow velocity component, exploiting the radial symmetry of

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the system [30, 31]. A typical experimental setup used is a Hele-Shaw cell, where the liquids are contained in a thin gap between two parallel plates. These plates are separated by a small, but finite gap height h. Hence, in practice, the assumption of a 1D problem is only valid if diffusive equilibration is fast enough so that the parameters can be considered as constant in the other geometrical directions.

When advection becomes significant, the effect of Taylor dispersion [32, 33] further enhances the mixing. In the fluid gap between the parallel plates of a Hele-Shaw cell, for the flow rates used, a parabolic velocity profile (Poiseuille flow) is formed. The higher flow velocity in the center of the gap deforms the reaction front, while diffusive transport takes place along the resulting small-scale concentration gradients. To account for Taylor dispersion, an approximate model for the non-uniform velocity field in the gap was included in [34]. Later, an actual 2D numerical study of a reaction front in a radial Poiseuille flow was conducted [35]. Nevertheless, the full interaction of hydrodynamics and diffusive mixing can lead to more complex spatio-temporal concentration distributions in propagating concentration fronts [36, 37], which can also depend on the initial conditions even in the long-time regime [24].

In addition, buoyancy-driven phenomena are known to affect the progression of reaction fronts [38], even for a horizontally oriented Hele-Shaw cell with a small gap height [39–41]. Buoyant convection contributes to chemo-hydrodynamic pattern formation both in miscible [42–44] and immiscible [45, 46] reactive systems under gravity. Thus, additional convective mixing [39–41] can still be expected in a radial RDA system because of a slight density difference between the reactant and product solution, making a direct comparison to theory complicated or even impossible [20, 30, 34]. Microgravity experiments enable us to distinguish between the contributions of buoyancy and deformation by the Poiseuille flow, making it possible to validate theoretical predictions on reactive chemical fronts. This strategy has also been employed for more fundamental diffusion-controlled experiments in microgravity conditions such as the hard-to-wet-surfaces experiment [47], investigating the dissolution and diffusion of solid tablets in liquids, and the experimental investigation of g-jitter effects on diffusion in binary mixtures, both on board the International Space Station (ISS); or the GRADFLEX experiment, on board the FOTON M3 spacecraft [48]. Furthermore, the reaction–

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diffusion dynamics of a low Lewis number flame ball were studied under microgravity aboard the ISS [49]. Several other experiments also used microgravity to eliminate buoyancy-driven flows in order to investigate mass transfer phenomena such as Marangoni flows [50] or reaction–diffusion in immiscible systems [41].

In addition to the decoupling of buoyancy-driven effects from other phenomena, experimenting on reduced or increased gravity gives us a first glimpse of how fundamental chemical processes might behave in the absence of gravity, revealing their potential use for *in situ* in-space manufacturing [51]. Microscale processes as in our study might provide solutions to problems that arise when transferring chemical technology to space [52, 53]. They further appear promising for process intensification in environments with reduced or increased gravity levels [52].

In this work, we provide novel experimental insights into radial RDA dynamics for different levels of acceleration, in order to obtain quantitative data against which theoretical models can be tested. Due to the radially decaying front velocity, the influence of buoyancy strongly differs from the reaction-diffusion systems studied before. Hence, we conducted experiments using a well-known chemical reaction [34, 54] in radial Hele-Shaw cells on board a parabolic flight (PF), i.e. under a sequence of alternating gravity levels (Section 2). We assessed the temporal evolution of the chemical fronts by examining characteristic front properties, such as the total amount of product formed (Section 3.1), and the position and overall width of the chemical fronts (Section 3.2). Comparison with the respective experiments on the ground allows us to evaluate the role of buoyant convection in the front dynamics, to relate the observed trends to the theoretical predictions, and to identify important requirements for future microgravity experiments on radial RDA fronts.

2. Chemical reaction, experimental setup and image analysis

As a model system for an $A + B \rightarrow C$ reaction, we employed the formation of the complex $FeSCN^{2+}$ (product C) from potassium thiocyanate KSCN (reactant A) and iron(III) nitrate $Fe(NO_3)_3$ (reactant B). This system was chosen for our radial injection study as the reaction front can be directly captured by absorption measurements: the product is intense in color in contrast to the colorless ractants [34]. Moreover, the fast reaction kinetics allows us to draw comparisons

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Table 1

Physical properties of reactant and product solutions (at 20 ^oC)

Solution	Density, kg m^{-3}	Viscosity, mPa s
A: KSCN, 0.03 mol L^{-1}	999.6 ± 0.1	0.97 ± 0.01
B: (FeNO$_3$)$_3$, 0.03 mol L^{-1}, HNO$_3$, 0.1 mol L^{-1}	1007.4 ± 0.1	1.08 ± 0.01
C: reacted mixture A and B, volume ratio 1:1	1003.0 ± 0.1	0.97 ± 0.01

with existing theoretical RDA predictions, which assume instantaneous reaction [30, 35, 55]. The experiments were performed in a quasi-two-dimensional planar geometry using the Hele-Shaw (HS) cell design described below.

The solutions were prepared from reagent-grade chemicals (Sigma-Aldrich) and deionized water. The HS cell was filled with a 0.03 mol L^{-1} Fe(NO$_3$)$_3$ aqueous solution, adjusted to acidic conditions (pH = 1) with HNO$_3$. Subsequently, a 0.03 mol L^{-1} KSCN solution was injected into the HS cell through the central inlet at a constant flow rate Q as in the work by Tóth et al. [34]. When the two solutions come in contact, the monocomplex FeSCN^{2+} is predominantly produced at the solution concentrations used, following Eq. 1

$$\text{SCN}^- + \text{Fe}^{3+} \underset{k'}{\overset{k}{\rightleftharpoons}} \text{FeSCN}^{2+} \tag{1}$$
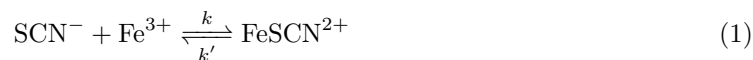
where $k \simeq 200$ L mol^{-1} s^{-1} and $k' \simeq 1.5$ s^{-1} [56]. Using the above, a fully mixed solution with equal volumes of reactant solutions results in a concentration of product C (FeSCN^{2+}) of $C_{fm} = 0.0075$ mol L^{-1}, as:

$$\frac{[\text{FeSCN}^{2+}]}{[\text{SCN}^-][\text{Fe}^{3+}]} = \frac{C_{fm}}{(0.015 \text{ mol L}^{-1} - C_{fm})^2} = \frac{k}{k'} \tag{2}$$

Table 1 lists the physical properties of the two reactant solutions and the resulting fully mixed product solution, as measured with an Anton Paar SVM 3001 pycnometer-viscosimeter (Anton Paar GmbH, Graz, Austria) at a temperature of 20 ^oC. The small viscosity differences combined with the low flow rates used prevent the emergence of viscous fingering during the experiment [20].

The central component of our setup is the radial Hele-Shaw cell that is schematically depicted

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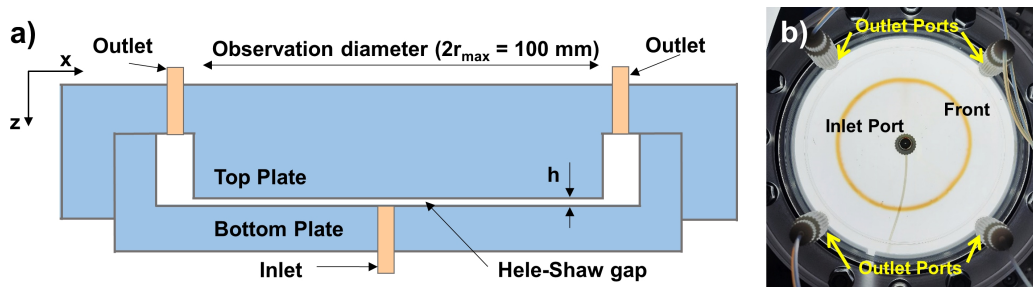
Fig. 2. Schematic vertical cross-section of the Hele-Shaw cell used in the experiments (a) and photograph of an experiment in progress showing the brown annular reaction front (top view) (b).

in Fig. 2a. The cell consisted of two parallel plates made of poly(methyl) methacrylate (PMMA). The overall observable radius (r_{max}) was 50 mm. The distance between the parallel plates could be set to three different gap height (h) values, namely: 0.2, 0.4, and 0.6 mm.

As shown in Fig. 2, the inlet port of the cell was attached through a threaded bore at the center of the bottom plate. To integrate the inlet tube, we used a custom-made connector system, consisting of a modified polytetrafluoroethylene (PTFE) connector plug (Bohlender GmbH, Grünsfeld, Germany) with an inner diameter of 1.0 mm. Four outlet ports with tubings were placed at the top of the reactor, through which the outflow was discharged into a waste container. To ensure that the flow was uniform, a large ring-shaped reservoir is machined into the upper PMMA plate outside the observable diameter. It serves as a buffer volume that prevents the generation of pressure gradients in the azimuthal direction. In this way, a preferential flow direction was avoided and the reaction front was kept radially symmetric within the HS cell. The gap-averaged (z-averaged) velocity U_r of the radial Poiseuille flow depends on the distance r from the injection point:

$$U_r(r) = \frac{Q}{2\pi h r} \tag{3}$$

In our HS cell design, the gap height h was set by a defined step in the rim of the top plate, which rests on the bottom plate (Fig. 2a). A rubber O-ring was placed in a groove between the two PMMA plates to prevent leakage (not shown in the sketch for simplicity). The two HS plates were clamped together with 8 bolts and nuts that passed through holes near the edge of the two

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plates. Between these bores, 4 additional bores were installed, so that the HS cell could be fixed to the rest of the experimental setup.

The HS cells were mounted on a rotating circular aluminum disk supported by a central aluminum shaft (Fig. 3).
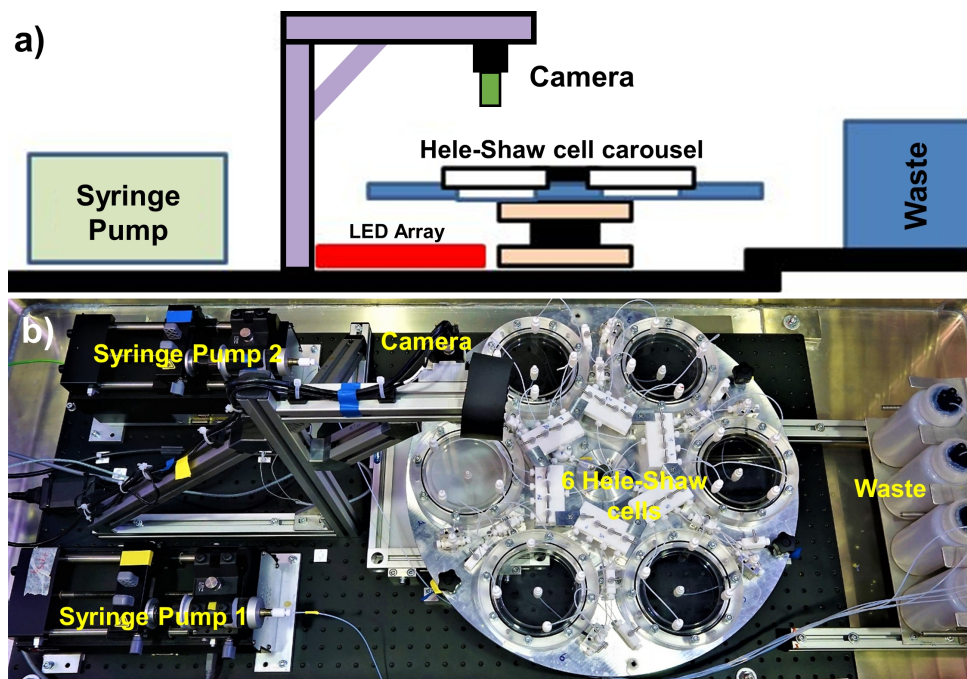
Fig. 3. Schematic diagram (a) and photograph (b) of the integrated experimental setup used for the parabolic flight experiments. The setup details are described in the text.

This experimental arrangement made it convenient to replace the HS cell occupying the optical path during the interval between the sequences of parabolas. A total of six HS cells could be integrated into the flight setup, but only one of them could be operated at a time. The plate of the rotating disk had six orifices where the cells were mounted so that the desired Hele-Shaw cell was optically accessible. The shaft of the carousel was fixed to an optical breadboard. The shaft was hollow and equipped with a lateral opening, such that the tubing for the reactant supply and the outflow of the product solutions could be accommodated inside.

The liquid injection system comprised two syringe pumps (PHD ULTRA™, Harvard Apparatus,

Holliston, MA, USA) with two 50 mL gastight Hamilton 1050 syringes (Hamilton Company, Reno, NV, USA) and the liquid circuit. The syringe pumps offered a wide range of flow rates and operated in a stable way, i.e. no pulsation effect was observed in any of the gravity conditions visited during the parabolic flights. The selected injection flow rates were low enough to reduce hydrodynamic entrance phenomena that can cause intense reactant premixing [57]. PTFE tubing with a nominal diameter of 0.8 mm and various valves (Bohlender GmbH, Grünsfeld, Germany) were used for the liquid circuit. The tube length between the inlet valve and the inlet port of each HS cell amounted to ≈ 175 mm. To activate the injection of the KSCN solution into one of the HS cells, the respective inlet valve was opened and the syringe pump set to run.

The reaction front was visualized by homogeneous illumination from below via a white light LED array with an integrated frosted glass plate (Smart Vision Lights, Norton Shores, MI, U.S.A.). The light emitted from the LED panel passes through the HS cell, where it is partially absorbed by the reaction product. It then reaches a JAI GO-5100M, 2464 x 2056 px CMOS camera (JAI A/S, Copenhagen, Denmark) mounted above the HS cell. The camera objective (KOWA LM12SC Objective, Kowa Optimed Deutschland GmbH, Düsseldorf, Germany) was equipped with a Schneider BP 465-70 HT blue bandpass filter (Jos. Schneider Optische Werke GmbH, Bad Kreuznach, Germany). The blue filter significantly enhances the contrast between the product and reactant solutions in the cases of small gap heights (the filter was used only for experiments with $h = 0.2$ or 0.4 mm). For all experiments, the objective was set to an f-stop value of 2.8 and a magnification value of 0.2. The camera was operated at a framerate of 10 Hz.

In addition, two temperature probes were integrated close to the HS cell of the running experiment in order to detect any spatial or temporal temperature gradients that might affect the front dynamics. The temperature difference between the two thermocouples did not exceed 1.0 K during the course of the experiment.

The whole setup was also equipped with an accelerometer (JoyWarrior56FR1, Code Mercenaries GmbH, Schönefeld, Germany) that was mounted near the carousel shaft. The accelerometer provided real-time acceleration values along all 3 axes (see Fig. 4).

The parabolic flight experiments were carried out on board a modified Airbus A310 aircraft
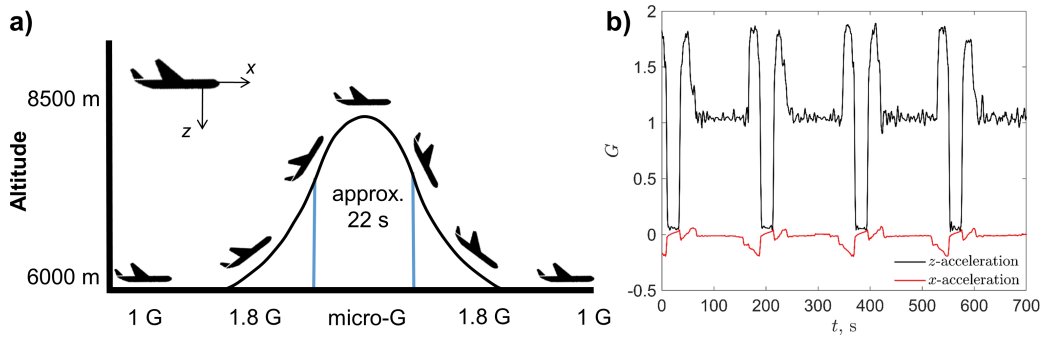
Fig. 4. A typical parabolic maneuver (a) and the two-axis acceleration values (for z-and x-axis, shown in black and red, respectively) acquired during a period of 4 parabolas (b). The frame of reference is also depicted with regards to the aircraft.

(Air Zero G, Novespace, Bordeaux, France), during the 73rd ESA Parabolic Flight Campaign. To comply with the safety regulations of the A310 Zero-G aircraft, the experimental hardware was placed inside an aluminum container (750 mm x 1650 mm x 670 mm, Zarges GmbH, Weilheim, Germany).

During a typical parabola, shown in Fig. 4a), the aircraft initially starts ascending at a $\approx 50°$ pitch angle with respect to the horizon using engine thrust and elevator control, while experiencing hypergravity. That means that the acceleration pointing down to the floor of the aircraft feels like approximately twice that of gravity. After a short transition phase, the microgravity phase starts, lasting around 22 s. This weightlessness feeling is achieved by reducing the motors' thrust and lowering the aircraft's pitch to maintain a net-zero lift configuration. During this phase, all the forces exerted on the aircraft roughly sum up to zero. Consequently, the aircraft is technically in freefall following a ballistic trajectory, with the low engine thrust compensating for the drag losses. The micro-G phase begins while the aircraft is still ascending and lasts for the entire top section of the parabola, until the aircraft reaches a downward pitch angle of about 40°. This is followed by an exit pull-out maneuver, necessary to remove the aircraft from a high-speed downwards motion and lead into a steady flight configuration in order to repeat the maneuver. The forces felt are again about twice as that of gravity, i.e. a hypergravity phase is experienced again.

Between the parabolic maneuvers a one-minute period of steady flight with normal gravity intervenes. The parabolic flight comprised a combination of 6 groups of 5 parabolic maneuvers. Each experiment was performed during a sequence of 5 parabolas, where one HS cell (with a constant gap height) was fed with reactant A solution at a constant Q in each case. During the sequence of parabolas, the HS cell was subjected to the different gravity regimes, that is, hyper-G ($\approx 1.8\ G$), zero-G ($\approx 10^{-2}\ G$) and 1-G. Here, $G = g/g_0$ denotes the normalized acceleration, where g is the instantaneously measured (i.e., apparent) acceleration and g_0 is the gravity acceleration on Earth, for which a value of 9.8 m s^{-2} is used. The frame of reference was set using the aircraft's principal axes; the z-axis is the yaw axis and the x-axis is the roll axis of the aircraft (Fig. 4a). This reference system coincides with the reference system applied in the experimental setup in Fig. 5. The typical acceleration values along the z- and x-axes of the aircraft are presented in Fig. 4b, in the course of 4 parabolas. The acceleration along the y-axis (the pitch axis of the aircraft) is of even lower magnitude than along the $x-$axis acceleration and was therefore excluded from the graph for clarity.

In parallel to the parabolic flight experiments, ground reference runs were performed with the flight hardware setup in an identical manner. Each experiment conducted in parabolic flights was repeated several times in laboratory conditions on ground with identical parameters (i.e. same h, Q combination) to ensure reproducibility.

Image processing. From the acquired images, the spatial and temporal concentration distribution of the product, $c(x, y, t)$ was obtained as in the work by Tóth et al. [34]. Here, x and y are the Cartesian coordinates in the HS cell. The time $t = 0$ was set when the front first appeared in the center of the HS cell (distinct color change in inner diameter of inlet plug), i.e., t is the time elapsed since the KSCN solution starts to be delivered to the HS cell. To determine the concentration distribution, the first step was to calculate the local relative gray value, $I(x, y, t)$, cf. Fig. 5c, from the local gray scale intensity, $I_c(x, y, t)$, and the reference intensity, $I_0(x, y)$, of the background image of the HS cell, containing only the Fe(NO$_3$)$_3$ solution:
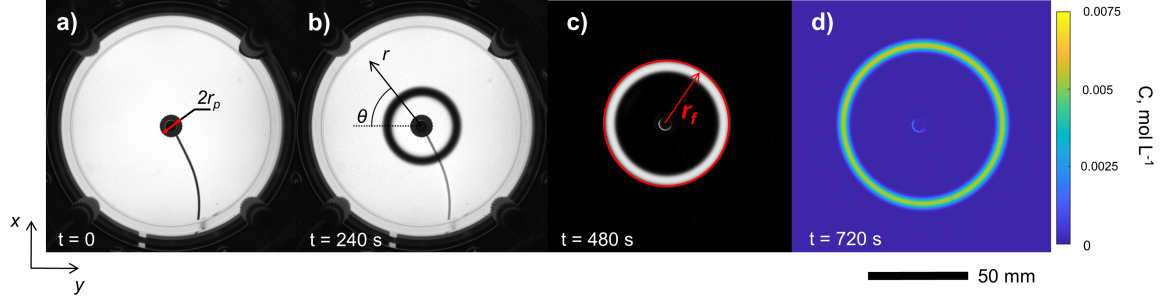
Fig. 5. Steps in the image processing procedure: raw image at $t = 0$ (a), raw image with a chemical front at t=240 s (b), processed image with front tracking at $t = 480$ s, the front's outer limit, r_f, is highlighted (c), concentration distribution at $t = 720$ s (d).

$$I(x, y, t) = \frac{I_0(x, y) - I_c(x, y, t)}{I_0(x, y)} \tag{4}$$

The $I(x, y, t)$ value can then be directly assigned to a local concentration value $C(x, y, t)$ using previously obtained calibration curves. For calibration, the HS cell is filled with solutions with various, but constant product concentrations as described by Tóth et al. [34]. It should thus be noted that the determined concentration values are, per se, averaged over the total gap height

$$C(x, y, t) \equiv \frac{1}{h} \int_0^h C(x, y, z, t) \, dz \tag{5}$$

A distinct calibration curve was determined for each cell (gap height) and used in the subsequent analysis. In cells with narrow gap sizes (0.2 mm and 0.4 mm), a blue filter is used to enhance the optical contrast; this was also used during calibration. The calibration curves and their parameter values corresponding to each gap height are available as Supplementary Material. From the local concentration distribution, the total amount of product, n_C, present in the reactor can be calculated for each time, t, as:

$$n_C(t) = h \int C(x, y, t) \, dxdy \tag{6}$$

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A normalized total amount of product can be introduced:

$$\bar{n}_C(t) = \frac{n_C(t) - n_{C,1}}{n_{C,fm}} \tag{7}$$

where $n_{C,1}$ is the total amount of product present after the reaction front detaches from the inlet plug radius, r_p. This value roughly corresponds to the amount of product that already enters the HS cell by the reaction in the inlet valve and tubing. Subtracting this baseline takes into account the fact that in the parabolic flight (PF) experiment, depending on the experimental conditions (i.e., acceleration conditions, manual valve handling between the parabola sequences), different quantities of product C might be present in the reactor at $t = 0$ due to premixing effects. The fully mixed amount of product $n_{C,fm}$ represents the product contained in the HS cell reactor if equal volumes of the reactant solutions were homogeneously mixed. It can be calculated as:

$$n_{C,fm} = \pi r_{max}^2 h C_{fm} \tag{8}$$

where C_{fm} corresponds to the molar concentration of the product in a fully mixed solution of equal reactant volumes, thus $C_{fm} = 0.0075 \text{ mol L}^{-1}$.

Furthermore, the total production rate, $\dot{n}_C(t)$:

$$\dot{n}_C(t) = \frac{dn_C(t)}{dt} \tag{9}$$

refers to the production rate of C averaged over the entire HS cell volume. Hence, this time-dependent reaction rate is an indicator of the total reaction progress over time.

To describe the local front properties, a radial concentration profile, $C(r,t)$, was computed by averaging over the polar angle, θ (at equidistant angle intervals of $\Delta\theta = 2.4°$), on a cylindrical coordinate system. Here, the origin is located in the center of the circular front, as shown in Fig. 5b. Then, the time-dependent width of the product front, $W_C(t)$, can be calculated as the full-width at half-maximum ($FWHM$) of the $C(r,t)$ profile (cf. SI). The region occupied by the PTFE inlet plug is excluded from the image analysis, hence $r > r_p$ (Fig. 5a), as are all the pixels

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that are covered by the inlet tube. Additionally, to characterize the front progression, the leading edge radius of the reaction front, r_f, is tracked by a thresholding operation (Fig. 5c). All the image analysis described was carried out using MATLAB routines.

3. Results and discussion

3.1. Amount of reaction product

In Fig. 6 and Fig. 7, the product generation is presented for experiments in HS reactor cells with a height of 0.2 mm and 0.4 mm, respectively, for a duration of 500-700 s, meaning that several consecutive parabolas have an effect on the dynamics. The flow rate Q was constant throughout the experiment at 0.072 mL min^{-1} (0.2 mm gap, Fig. 6) and 0.144 mL min^{-1} (0.4 mm gap, Fig. 7). These values were selected to adapt the duration of the experiment to the time required to perform a sequence of 5 parabolas.

As a result, the two experiments share a common residence time, $\tau = \pi r_{max}^2 h Q^{-1}$ and a common average velocity distribution, $U_r(r)$. The same parameters were used in the respective ground reference runs in the laboratory. The results shown here from the ground reference experiments are an average over 3 repetition runs (cf. SM).

The normalized amount of product, $\overline{n}_C(t)$, and the product generation rate, $\dot{n}_C(t)$, are plotted against the injected volume, $\mathcal{V}$:

$$\mathcal{V} = Qt \tag{10}$$

where t is the time elapsed since the formation of the front in the HS cell. Note that $\mathcal{V}$ is directly proportional to time, since Q is constant in each experiment. This representation allows us to compare the required input of the KSCN reactant solution to generate the respective amount of product.

Fig. 6 and Fig. 7 show the evolution of the normalized total amount of product $\overline{n}_C$ (upper panel), the product generation rate $\dot{n}_C$ (lower panel), and the corresponding relative acceleration values G during the parabolic flight experiment (right-hand axis). At first sight, it is confirmed

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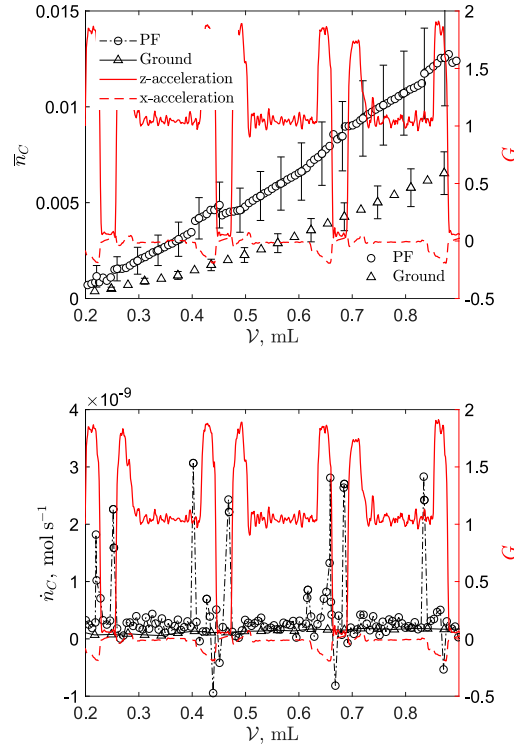
Fig. 6. Comparison of the normalized amount of product, $\overline{n}_C$ (top) and the total production rate, $\dot{n}_C$ (bottom) in experiments with h=0.2 mm, Q=0.072 mL min^{-1} on ground and during the PF. The corresponding acceleration values for the x- and z-axes are provided by the right axis.

that the dynamics are clearly affected by the modulation of the gravitational acceleration. For both gap heights h of the HS cell, $\overline{n}_C$ is larger in the PF experiment. This can be attributed to the periodic change in acceleration (1-G, hyper-G and micro-G) along the z-axis and the additional slight modulations of the acceleration along the x-axis experienced by the fronts during the PF, and during the phase when the front enters the reactor (i.e., in Fig. 7, the front has already experienced a parabola at $\mathcal{V} = 0.2$ mL).

For the 0.4 mm gap height reactor (Fig. 7), the normalized amount of product formed $\overline{n}_C$ is considerably larger than for the 0.2 mm gap height reactor (Fig. 6). For example, at the same
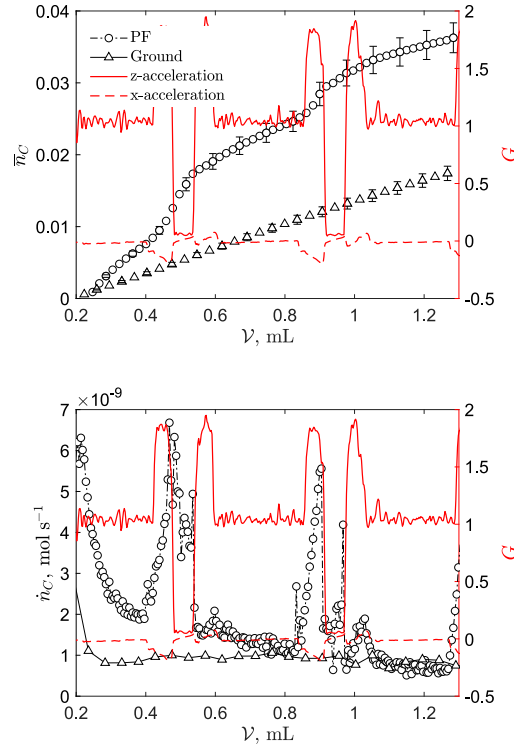
Fig. 7. Comparison of the normalized amount of product, $\overline{n}_C$ (top) and the total production rate, $\dot{n}_C$ (bottom) in experiments with h=0.4 mm, Q=0.144 mL min^{-1} on ground and during the PF. The corresponding acceleration values for the x- and z-axes are provided by the right axis.

injected volume $\mathcal{V} = 0.8$ mL, in the 0.2 mm gap reactor $\overline{n}_C = 0.006$ on ground and $\overline{n}_C = 0.011$ during the PF, while in the 0.4 mm gap reactor, $\overline{n}_C = 0.010$ on ground and $\overline{n}_C = 0.024$ during the PF. The difference is even more significant considering that the corresponding time to inject the same $\mathcal{V}$ (which is the determining factor for diffusive mixing) is smaller in the 0.4 mm gap reactor. For this normalized product value (where the increase in the surface area between the reactant solutions is already taken into account), this can be attributed to the increased buoyant effects at a higher gap height, both on ground and during the PF. However, the contribution of the deformation by the Poiseuille flow also depends on the gap height. To compare the amount of

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product formed during the PF and on the ground, it should further be noted that, at $\mathcal{V} = 0.8$ mL, the PF experiment in the 0.4 mm reactor was only subject to two acceleration modulation cycles (parabolas), while 3 parabolas were flown in the 0.2 mm gap reactor. Hence, the relative difference between the PF and ground experiments for the 0.4 mm gap is still comparable to the difference in the 0.2 mm case, despite the greater intensity of the buoyant phenomena present in the 0.4 mm gap experiment.

In the HS reactors with both gap heights, there is a jump to larger $\bar{n}_C$ values that coincides with the hyper-G phase of the parabolic maneuver. The underlying mixing effect induced by the gravity modulations is described in detail in the following. In the absence of density gradients, the front acquires and then conserves a parabolic shape (schematically sketched in Fig. 8a) attributed to the Poiseuille profile of the velocity field.
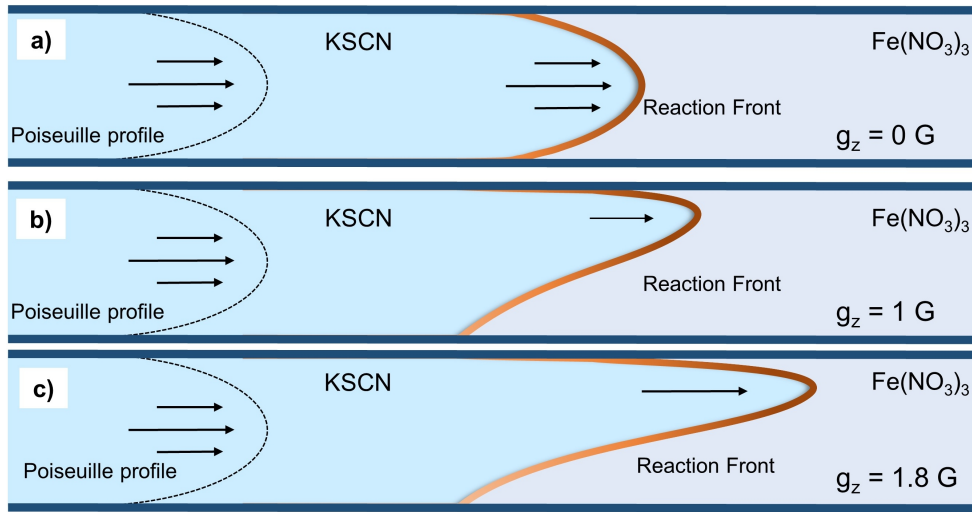
Fig. 8. Schematic representation of buoyant front deformation under three different gravitational levels: micro-G (a), 1 G (b) and 1.8 G (c) for the chemical front studied.

Under normal gravity conditions, the less dense KSCN solution (the densities of the solutions are presented in Table 1) flows preferentially towards the top of the HS gap, as depicted in Fig. 8b. This buoyant phenomenon is intensified either by increasing the gap height or by increasing the gravitational acceleration (Fig. 8c). In addition to the modulations of the z-axis acceleration, the

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nonzero x-axis acceleration during the hyper-G phase at the beginning of a parabola (Fig. 4b and Fig. 6, Fig. 7) interferes with the front dynamics. Although smaller in magnitude than the z-axis acceleration, the x-axis acceleration can likewise cause a local stretching of the front and hence enhance product generation. This effect can notably distort the annular shape of the front in the 0.4 mm reactor at the later stage of the experiment. At large t, the front has reached a larger radius, which leads to significantly lower velocities in the radial spreading of the front (cf. Eq. 3), and thus to a stronger impact of the slight horizontal acceleration. Therefore, only the first two parabolas are evaluated in the 0.4 mm gap experiment, where the circularity of the front is still preserved.

The error range for the amount of generated product in both Fig. 6 and Fig. 7 (upper panels) was estimated from the uncertainty in determining the calibration coefficients, and the manufacturing tolerance of the HS gap height (additional information on the uncertainty propagation estimation is provided as Supplementary Material). A further contribution to the experimental uncertainty during the PF is seen for the experiment with a 0.2 mm gap. During the acceleration modulations, specifically when changing from hyper-G to micro-G, a reduction in the amount of generated product was observed. This unphysical progression is probably due to the mechanical stresses to which the experimental setup is subjected during the gravity modulations. Especially during the hyper-G phase, the setup experiences twice the acceleration as on Earth, resulting in a possible bending and slight alteration of the optical path distances. Flight maneuver instabilities, motor vibrations and local inhomogeneities in the atmosphere might be transferred to the setup to some extent despite the stabilizing profile construction. The calculation of the concentration distribution from the optical recordings of the reaction front is most sensitive to such disturbances in the case of the smallest gap size as the absolute concentration of the formed product is lowest with small gaps of this kind. Hence, the magnitude of this uncertainty was assessed based on the extent of the drop in the amount of generated product, and added to the given error range in both Fig. 6 and Fig. 7 (upper part).

In the lower panels of Fig. 6 and Fig. 7, the production rate $\dot{n}_C(t)$ is presented. For the 0.2 mm PF experiment, the production rate is scattered around the relatively constant ground values, but

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the average is at a higher level, compared to the respective ground experiment. This is mainly ascribed to the enhanced mixing by the acceleration modulations, as the front deformations during the comparatively shorter hyper-G phases carry on and continue to have an effect during the 1-G phases. In addition, the slight vibrations in the acceleration curves, that are generally seen in-flight, might also add to the enhanced mixing. The production rate highlights the dynamic situation during the parabolas. Instant spikes in the production rate are observed during the hyper-G phase at the beginning of a parabola, connected to the higher absolute x-axis acceleration values that act normal to the front.

The $\dot{n}_C(t)$ values for the 0.4 mm PF experiment appear much more robust than for the 0.2 mm case, as a result of the larger absolute amount of product present in the reactor compared to the experimental fluctuations. Negative production rates are absent throughout the whole experimental run, while spikes in production are observed during the hyper-G phases, as in the 0.2 mm gap experiment. This further suggests that the high production rates in the 0.2 mm gap are indeed a consequence of the enhanced mixing and are not primarily caused by the above-mentioned mechanical stresses acting on the setup.

The pronounced increase in $\dot{n}_C(t)$ during the hyper-G phases and, in particular, during the phases of nonzero x-axis acceleration is evident in the 0.4 mm experiment (values more than triple those of the corresponding ground cases are reached). In the normal gravity phases, the ground reference values are approached. Furthermore, it should be mentioned that the steep decline in high production rates, $\dot{n}_C(t)$ at the very early stage (i.e. for $0.2 < \mathcal{V} < 0.4$, Fig. 7) is caused by initial disturbances at the front, such as the effect of a residual premixed volume entering the cell and slowly spreading while the front progresses. This is most notable in the 0.4 mm case (both for on-ground and PF experiments) due to the wider reaction front. Additionally, the gravity modulations when the front enters the reactor (i.e., at $\mathcal{V} < 0.2$ mL, not shown in Fig. 7 since the front is partially covered by the inlet plug), might still affect the front dynamics; this is particularly noticeable at the very beginning of the $\dot{n}_C(t)$ curve.

For a qualitative comparison with the theoretical model [30, 34], the dimensional total amount of product $n_C(t)$ is plotted in Fig. 9 for the two different gap heights against the time elapsed, t.

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Fig. 9 focuses on the evolution in the later stage of the experiment, but before the front distortion caused by the x-axis acceleration becomes significant. The progression of the ground reference experiments at such a late stage suggests a linear dependence between the amount of product formed and time, i.e., $n_C \propto t$. Since this is in accordance with the analytical models [30, 34], the curves are approximated by a linear fit:

$$n_C(t) = St + p \tag{11}$$

where p is an offset factor. This approach yields an average production rate S (having units of mol s^{-1}), neglecting the discrete modulations in the PF experiment. The finding that $S_{PF} > S_{Ground}$ emphasizes how strongly the relatively short micro-G and hyper-G phases influence the production rate with respect to the long normal gravity intervals.
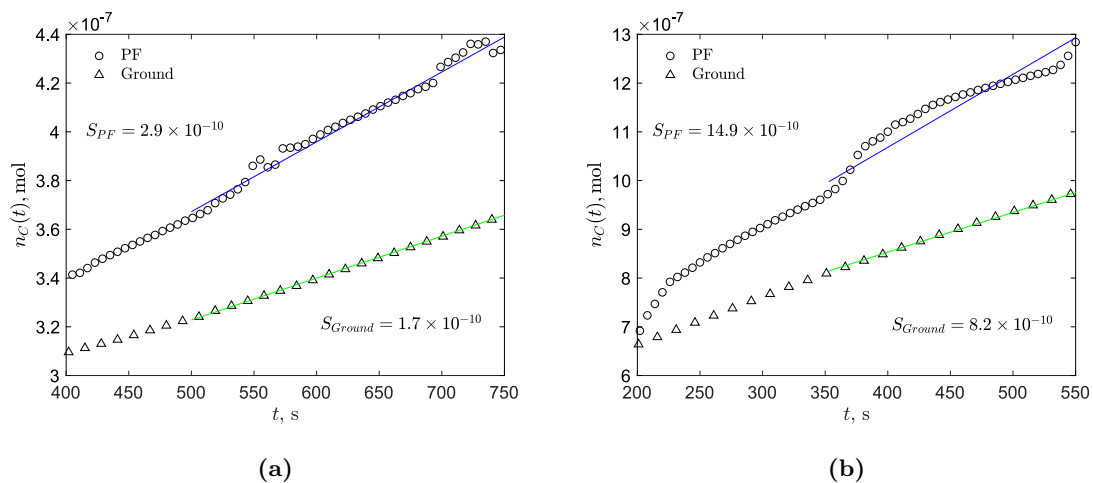

Fig. 9. Comparison between the dimensional total amount of product, $n_C(t)$ on ground and during the PF for two different experiments: h=0.2 mm, Q=0.072 mL min^{-1} (a) and h=0.4 mm, Q=0.144 mL min^{-1} (b). The S values have units of mol s^{-1}.

A similar fit (as in Eq. 11) is also suggested in studies that are based on a quasi-1D theory [30, 34]. This approximation requires both diffusion to eliminate the concentration gradients across the gap, and buoyancy effects to be absent. Indeed, the initially high density gradients will weaken

in the later stages, and the product formation by diffusive mass transfer along the flow direction becomes more significant due to the decreasing velocities. However, the gravity-induced convective mixing that intensifies during the hyper-G phase is still notable. The higher S values during the PF compared to the ground case clearly indicate that this ideal situation has not yet been approached for either gap heights.

Comparison with a pure microgravity case. In some PF experiments with a large gap height (i.e., 0.6 mm and Q=0.216 mL min^{-1}), the front was completely distorted towards the end of the experiment and the radial symmetry was lost, such that no consistent image analysis was possible (cf. SM). Therefore, a high flow rate Q= 8.22 mL min^{-1} was used instead for the 0.6 mm cell, resulting in $\tau \approx 22$ s, which leads to injection occuring almost exclusively during a single micro-G period. Hence, this experiment serves as a comparison case which can provide initial insights into a radial RDA front without interfering buoyancy-driven effects. Here, the flow follows a parabolic profile and the reaction takes place at the stretched contact area between solutions A and B, as depicted in Fig. 8a. This "pure" microgravity experiment is presented in Fig. 10 together with the corresponding ground reference experiment.

Under these conditions, again, a significant deviation from the ground experiment is noticeable. In both cases, we observe a linear increase in the total amount of product formed. However, when the micro-G and the ground experiments are compared, the $n_C(t)$ in the constant 1-G ground experiments was always higher than in the PF experiments. It should be emphasized again that the acceleration conditions in this PF experiment are essentially different from the previous cases (zero-G in contrast to repeated gravity modulations) and hence had an opposite effect, i.e., a reduction in product formation. The remaining slight gravity modulations in the 0.6 mm cell at the very beginning and at the end of the experiment are negligibly small as they are not sufficient to exceed the product formation on Earth. Although the velocity of the radial flow is much higher than in the cases examined previously, buoyancy-driven phenomena play a major role in the ground reference case. The recorded reaction front images even show the emergence of a radially striped pattern towards the end of the experiment (cf. SM) which is a known buoyancy-driven instability

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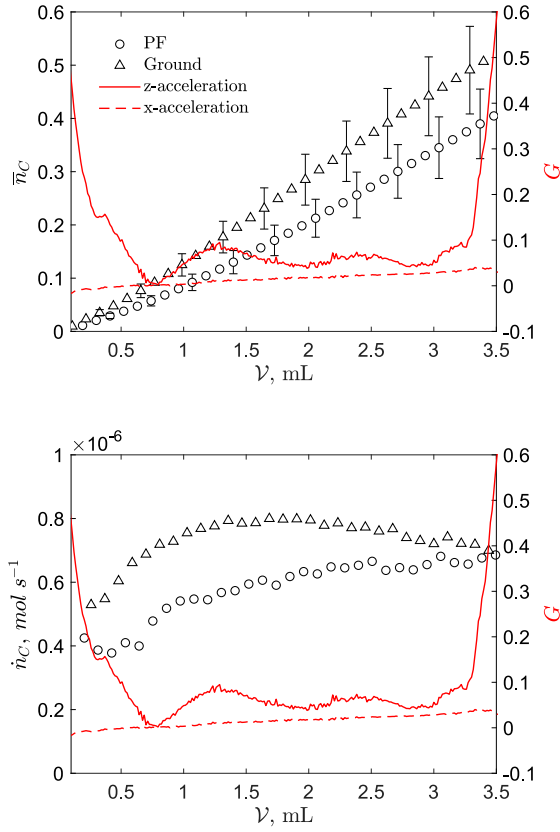
Fig. 10. Comparison of the normalized amount of product, $\overline{n}_C$ (top) and the total production rate, $\dot{n}_C$ (bottom) in experiments with h=0.6 mm, Q=8.22 mL min^{-1} on ground and during the PF. The corresponding acceleration values for the x- and z-axes are provided by the right axis.

in radial HS cells [58, 59]. The decreasing production rate $\dot{n}_C(t)$ in the later stages of the ground experiment is explained by the fact that the product starts leaving the observation window of the reactor. For example, at $\mathcal{V} = 3$ mL, the concentration C of the product at the rim of the reactor is approximately 5% of the maximum value in the radial concentration profile, i.e. a significant amount of product already flowed out. The faster progression of the reaction front towards the rim of the reactor in the ground experiment is also visible in the snapshots in the SM.

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3.2. Geometrical front properties

Since the PF experiment in the 0.2 mm gap height HS cell was subject to high experimental uncertainties as discussed before, the investigation of the geometrical front properties concentrates on the 0.4 mm gap height experiment. Two different measures for the front radius are analyzed and depicted in Fig. 11a for the ground and PF experiments. The r_C value is defined as the averaged radius for the position of maximum concentration of the product C, and r_f is defined as the position of the outer rim of the reaction front (as shown in Fig. 5c).
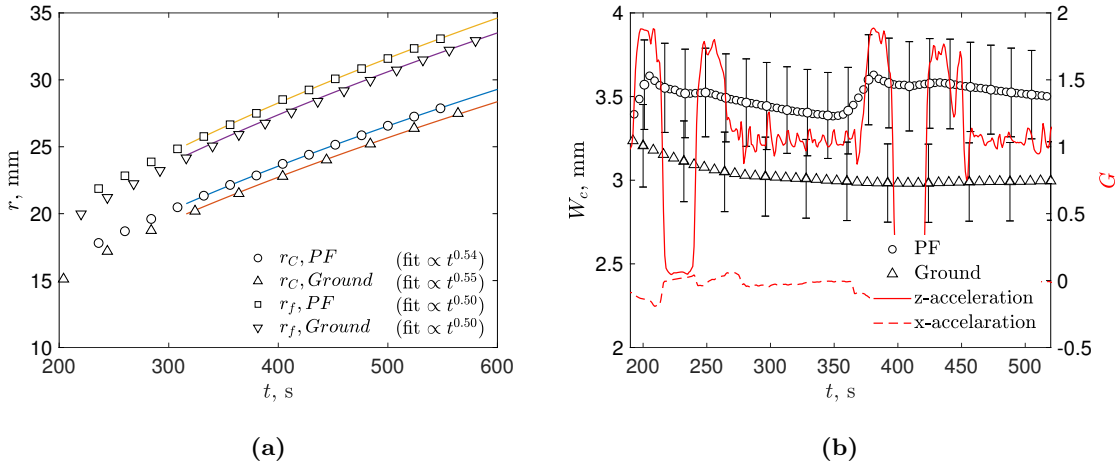
Fig. 11. Temporal progression of the front radii r_f and r_C (a) and of the front width W_C (acceleration values provided by the right axis) (b), on ground and during the PF for h=0.4 mm, Q=0.144 mL min^{-1}.

Based on these definitions, the r_f value always exceeds the r_C value. Ideally, r_f is strictly dictated by the injection flow, and should scale with the square root of the injected volume, $\mathcal{V}$

$$r_f \propto \mathcal{V}^{0.5} \tag{12}$$

If the injection flow rate is constant, Eq. 12 implies that $r_f \propto t^{0.5}$. This is observed in Fig. 11a, in good agreement with the theoretical prediction. Likewise, the evolution of r_C is close to the $\propto t^{0.5}$ relationship proposed by Comolli et al. [35]. Indeed, we expect the gravity effects present in

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both the PF and the ground experiments to have a stronger impact on the position of the maximum C concentration (r_C), as this should coincide with the position of the highest density gradients. The amount of premixed volume entering the HS cell from the inlet tubing also might affect r_C more than r_f. In general, both front positions r_C and r_f are larger in the PF experiments, which can again be attributed to the enhanced mixing caused by the acceleration modulations along 2 different axes. However, no marked modulations in the front position curves are obtained due to the continuous spreading of the front caused by the injection flow.

Fig. 11b presents the temporal evolution of the front width. For the ground experiment, the front initially thins, then asymptotically approaches a constant value of $W_C \approx 3$ mm. The decrease at the beginning is ascribed to the non-ideal initial conditions, i.e., the spreading of the premixed volume as described above. The constant final width W_C qualitatively agrees with the progression predicted from theory [35]. In more detail, by utilizing an estimation for the governing time scale of the RDA dynamics [35], we get a critical time, t_c:

$$t_c = \frac{hQ}{230\pi D^2} \tag{13}$$

where D is the mass diffusivity. In our work we assumed that the diffusivities of all species are equal to a value of $D = 8.2 \times 10^{-10}$ m^2 s^{-1}, which was estimated using experimental results [34] for the same reaction system [35].

For times shorter than t_c, the front dynamics are mainly governed by advective phenomena (e.g., deformation by the Poiseuille profile), while the front is dominated by diffusive mass transfer for experiment durations beyond t_c. For the reactor with a 0.4 mm gap height, using Eq. 13, it is estimated that $t_c \approx 2000$ s, which is significantly longer than the duration of the experiment. Thus, the front dynamics are still mainly controlled by advection by the injection flow, along with the effect of the premixed volume and buoyant convection. Only at much later stages would a continuous diffusive widening of the front (i.e., $W_C \propto t^{0.5}$) be expected from previous models [34, 35, 55].

In the PF experiment, the effect of the gravity modulation on the z- and x-axes leads to the

generation of more product and, as a consequence, to larger front widths. The W_C evolution correlates directly with the acceleration modulations, as the front width increases sharply during the hyper-G phase at the beginning of a parabola, while it decreases slowly during the subsequent micro-G and normal gravity phases (Fig. 11).

Comparison with a pure microgravity case. Lastly, Fig. 12 depicts the temporal progression of the reaction front width W_C and its radius r_f for the 0.6 mm HS cell and a flow rate of $Q = 8.22$ mL min^{-1} (i.e., the same experiment as in Fig. 10, with the whole injection taking place within one micro-G period). Due to the extremely large W_C, and the emergence of the radially striped pattern in the ground experiment, r_C is not considered and only the radius of the outer rim of the front r_f is evaluated in Fig. 12a for these experimental parameters. The wide reaction front also takes a considerable time to detach from the region covered by the inlet plug. Hence, a meaningful evaluation of W_C only is possible after some seconds in Fig. 12b.

(a)   (b)
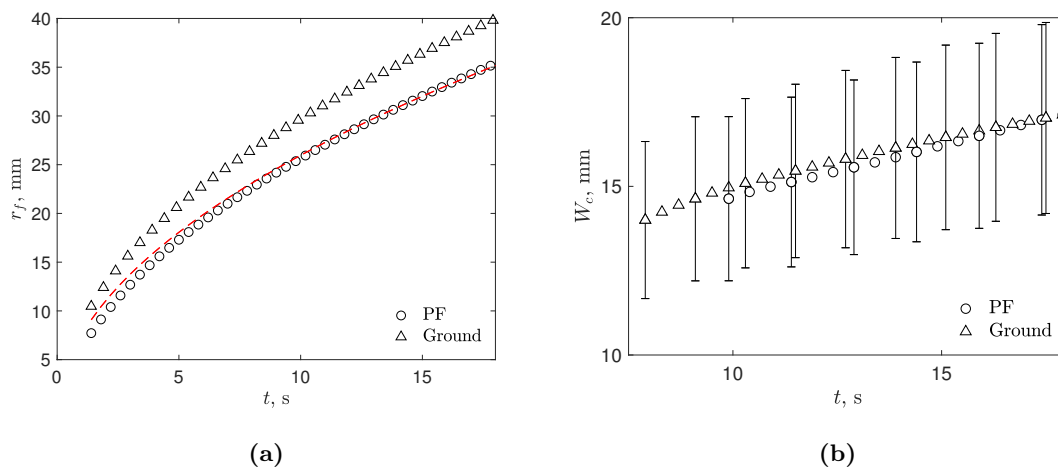
Fig. 12. Comparison of the temporal evolution of the front outer radius, r_f (a) and the front width, W_C (b) between a 1-G and micro-G experiment for h=0.6 mm, Q=8.22 mL min^{-1}. The dashed red line acts as a guide to the eye for a $\propto t^{0.5}$ scaling in (a).

While buoyancy effects strongly influence the evolution of W_C at low flow rates, the experiment under pure microgravity provides an initial quantitative approach for a comparison with the Taylor

dispersion width, W_C^0, derived using the correlations proposed by [35]:

$$W_C(t) = 1.23 \sqrt{2Dt\left(1 + \frac{3t_c}{4t}\right)} \tag{14}$$

For the early regime, $t \ll t_c$, this can be simplified as

$$W_C^0 \approx 1.23 \sqrt{\frac{3}{2}Dt_c} \tag{15}$$

The underlying theory [35] predicts that the value of W_C^0 will remain approximately constant until the front slowly transitions to the diffusive regime and can be better described by Eq. 14, for $t \gtrsim t_c$. Using Eq. 13 for the case of $Q = 8.22$ mL min^{-1}, $h = 0.6$ mm, with the same diffusion coefficient as before, $D = 8.2 \times 10^{-10}$ m^2 s^{-1}, yields $t_c = 7 \times 10^5$ s. It is thus evident that in these high flow rate experiments, the front evolves long before the diffusion-controlled stage, when the front width is expected to follow a power-law (scaling with $t^{1/2}$) [35, 55]. The predicted value of the dispersive width, $W_C^0 \approx 18$ mm, approximately agrees with the experimentally observed W_C (see Fig. 12b).

In both experiments (ground and PF) the front width grows slightly towards the predicted W_C^0. However, the duration of the experiment is short, and the reactor has a limited horizontal extension in comparison to the wide front. Thus, the evolution is still in a transient initial phase, in contrast to the steady W_C^0 value that is expected in the case of a more extended reactor geometry. Certain variations in the initial conditions (volume of premixed solution, local product concentration distribution) add to the observed discrepancy from the estimate in Eq. 14 and can lead to unsteady product distributions before the quasi-steady Taylor dispersion regime is reached [24].

Despite the differences in the product formation, the evolution of the front width W_C obtained for the ground and PF experiment lie close together. However, comparing the evolution and magnitude of r_f in Fig. 12a reveals that the front progresses significantly faster on ground than in micro-G, including in the later stages. This can be attributed to a noticeable density current that causes the front tip to advance in the ground experiment. The density current is practically absent in the PF experiment. Moreover, the generation of the radially striped pattern might also affect the r_f dynamics towards the end of the ground experiment.

4. Conclusions

In this paper, we presented initial experiments on Reaction–Diffusion–Advection (RDA) fronts using radial Hele-Shaw cells under modulated gravity on board a parabolic flight. We *quantitatively* evaluated several RDA front parameters for a comprehensive characterization of the system dynamics and comparison with theoretical predictions. Although the density difference between the reactant solutions and the gap heights of the Hele-Shaw cells were small, the evolution of the front was still severely affected by the changing acceleration levels along the z- and x-axes. These modulations were directly reflected in the temporal evolution of product formation and of the front width. The resulting enhanced mixing under hyper-G conditions increased the total amount of product generated. Although the acceleration modulations in a horizontal direction were much lower in magnitude than the modulations in a vertical direction, they significantly contributed to the observed dynamics. In the short micro-G and longer 1-G phases, the observed peaks in production rate were further reduced. Moreover, an experiment performed entirely under micro-G conditions using a high flow rate confirmed the expected overall decrease in product formation in the absence of gravity. The comparison with the ground reference experiment proved that the micro-G conditions affect the front progression, even though the strong injection flow might be expected to dominate the dynamics at first sight. This experiment appears promising for a direct and quantitative comparison of our RDA model system with future theoretical studies.

Our parabolic flight experiments made it possible to test several *qualitative* and *quantitative* aspects of previous theoretical predictions. An approximately linear scaling of the total amount of generated product was found in the range of experimental parameters considered, with a larger slope accounting for the enhanced mixing under the influence of gravity. This simple scaling might be a convenient description even though it stems from the purely diffusive 1D theory, while our experiments are dominated by Taylor dispersion. Our experimental data reproduced the predicted front progression and a quantitative agreement for the front width was obtained for the high flow rate experiment.

However, our observations are also limited by certain experimental constraints. The selection of the ferric thiocyanate system allowed us to obtain data for fast reaction kinetics (i.e., high

Damköhler numbers, which characterize the chemical reaction time scale in relation to the time scale of diffusive and convective mass transfer), approaching the theoretical predictions derived for instant reactions. Altering the mass transfer-to-reaction dynamics using a different kind of chemical system might reveal additional RDA dynamics regimes that are of great interest in technological applications, such as biological processes that involve macromolecules, polymerization and, even, particle precipitation processes for selective product generation. In the same vein, employing more complex systems with higher acting density or viscosity gradients might be considered for future studies, as it would provide a wider view of the respective interactions and instabilities in radial RDA systems.

In addition, a longer and more stable micro-G environment throughout the whole injection time, such as in a sounding rocket flight (or in an ISS experiment), is required to avoid buoyancy effects and to cover different regimes. A longer experimental duration and continuous microgravity will lead to a complete absence of buoyancy-induced convective mixing and thus to lower total amounts of product. This would allow us to fully unravel the complex interactions in RDA systems. As a step towards this, our experiments have shown that a homogeneous and radially symmetric reaction front can be obtained, if horizontal acceleration is absent. Hence, our liquid-tight, robust Hele-Shaw cell design provides a good basis for future microgravity experiments in platforms offering extended microgravity periods.

Furthermore, the current study under modulated gravity provides a basis for transferring reaction–diffusion dynamics to space conditions. Our preliminary hands-on experience allows us to better estimate the performance of future extra-terrestrial chemical plants where processes involving reaction–diffusion–advection fronts will be significantly slowed down in environments with gravity levels lower than on Earth, in the absence of intense buoyant mixing, or, accelerated under hypergravity conditions. Thus, we hope that the results of this work will encourage future research involving chemical processes in space.

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Declaration of Interests. The authors report no conflict of interest.

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