

Observer Based Tuning Techniques and Integrated SAW Torque Transducers for Two-Inertia Servo-Drive Systems

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Abstract

A controller design and tuning methodology is proposed that facilitates the rejection of periodic load-side disturbances applied to a torsional mechanical system, whilst simultaneously compensating for the disturbance observer's inherent phase delay, thereby facilitating the used of lower bandwidth, practically realisable, disturbance observers. The merits of implementing both a full- and reduced order observer, is investigated, with the latter being implemented with a new low-cost, high-bandwidth torque sensing device based on surface acoustic wave technology.

Introduction

Rejection of periodic load disturbances by feed-forward is a classical control problem when the torsional system interconnecting the motor and load can be considered infinitely stiff, and/or the dynamic load perturbations can be measured or estimated to a sufficiently high bandwidth [1]. In the majority of cases, load torque cannot be directly measured, and therefore, controllers usually require an observer (termed disturbance observer) to provide a dynamic estimate of the unknown input. Unfortunately, since feed-forward compensation is applied directly into the servo-amplifier, its effectiveness is heavily reliant on the ability of the observer to provide a high bandwidth, delay free, load torque signal, since any phase delay will significantly impede the ability of the controller to compensate effectively. However, observer algorithms are fundamentally derivative in nature (i.e. they amplify high frequency sensor noise), and those generally intended for industrial motion control applications (where usually the sole feedback sensor is the quantised position signal from an encoder) are therefore required to exhibit relatively low bandwidths, usually <100Hz [2], in order to attenuate high frequency noise and compensate for additional measurement delays [3]. Moreover, in such applications, the dynamics imparted by relatively low bandwidth observers unduly influences the system dynamics, ultimately affecting the desired rejection performance [2,3]. Nevertheless, for the sake of simplifying the theoretical analysis, state observer dynamics are assumed to be of a sufficiently high bandwidth that they can be ignored [1,4]. Few algorithms exist that compensate for the limitations imparted by a relatively low bandwidth observer, particularly in high performance motion control applications.

Furthermore, until recently, difficulties in acquiring reliable, low-noise, low-cost, shaft torque transducers that are non-invasive to the mechanical drive system, have precluded the use of direct shaft torque feedback for disturbance rejection in all but a minority of specialised closed-loop servo-drive systems. Often, commonly employed torque transducers viz. strain gauge, optical and inductive

devices, are too mechanically compliant when incorporated in a drive system, thereby degrading stability margins and reducing closed-loop bandwidth. Moreover, the additional cost associated with their integration is prohibitive. Here then, an investigation into improved tuning methodologies for classical disturbance observers, is investigated, with appraisal of a new, low-cost, non-contact torque measurement device, based on surface acoustic wave (SAW) technology [5]. SAW devices are mechanically robust, exhibit high sensitivity and bandwidth, and are largely unaffected by electromagnetic noise. They can be directly integrated into an electrical machine assembly without significantly affecting the mechanical stiffness of the motor shaft. For the study, SAW devices and RF module are mounted inside a commercial off-the-shelf permanent magnet synchronous machine (PMSM), directly onto the motor shaft between the front bearing and the rotor magnets, as illustrated in Fig 1.

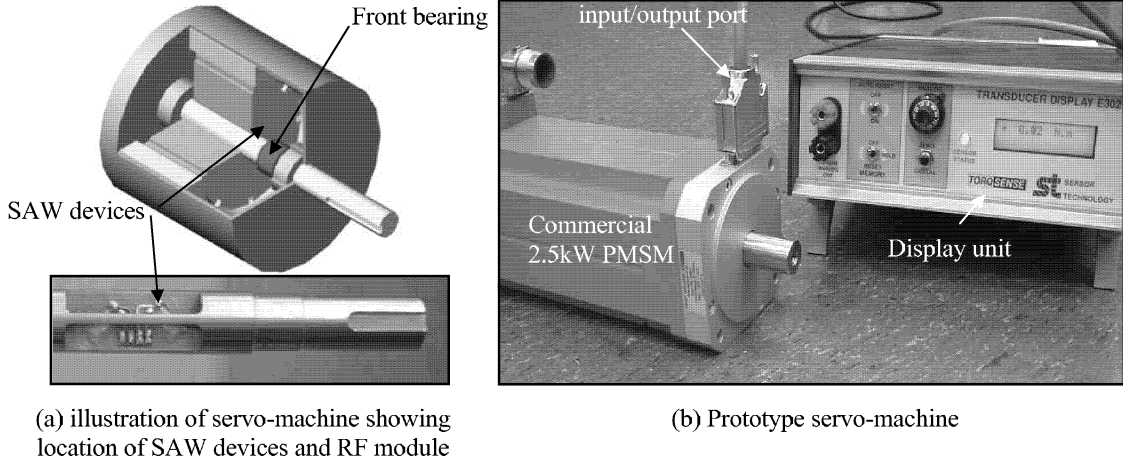
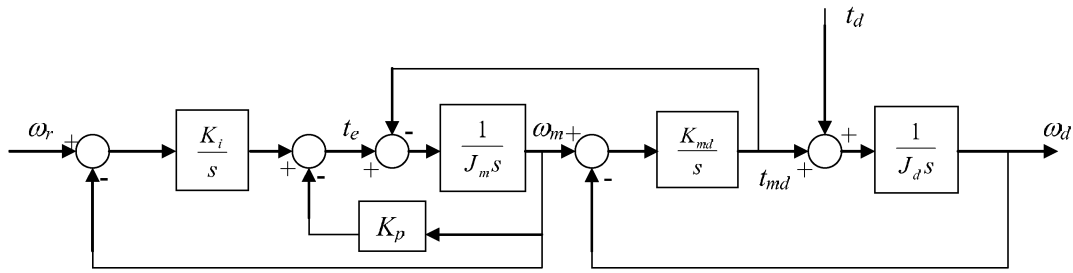


Figure 1. PMSM with integrated 20Nm SAW torque transducer.

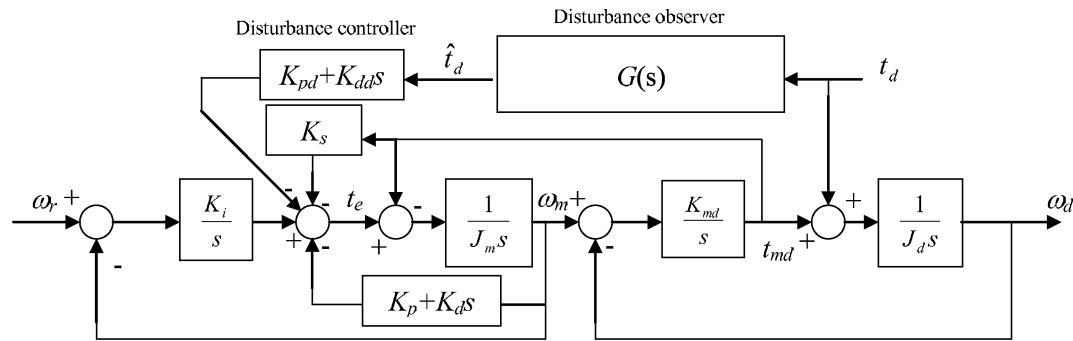
For simulation studies, a lumped two-inertia system model is used to represent the mechanical test facility that consists of J_m and J_d coupled via a shaft of finite stiffness K_{md} , which is subject to torsional torque t_{md} and excited via the motor electromagnetic torque t_e , and load torque perturbations t_d . Similarly, the motor and load velocities are denoted by ω_m and ω_d , respectively. Neglecting damping, ω_a is the anti-resonant frequency, ω_n the resonant frequency and R the load-motor inertia ratio of the mechanical system, viz:

$$\frac{\omega_d(s)}{t_e(s)} = \frac{\omega_a^2}{J_m s^3 + J_m \omega_n^2 s} \quad \omega_a = \sqrt{K_{md} \left(\frac{1}{J_d} \right)} \quad \omega_n = \omega_a \sqrt{R+1} \quad R = \frac{J_d}{J_m} \quad (1)$$

A classical proportional and integral (PI) type control structure and two-inertia mechanical model is shown in Fig. 2(a). By augmenting this basic controller with feedback of additional state variables, enhanced disturbance rejection performance can be achieved. The general structure for such an extended controller is shown in Fig. 2(b), where $G(s)$ represents the transfer function of the disturbance observer, \hat{t}_d the observed disturbance torque and K_{pd} , K_{dd} , the associated transfer feedback gains. Furthermore, K_s and K_d represent the transfer feedback gains associated with shaft-torque and motor acceleration feedback, respectively. For example, setting K_{pd} , K_{dd} and K_d to zero will form a PI controller plus shaft torque feedback. This is commonly referred to as resonance ratio control (RRC) [6]. Similarly, setting K_{pd} , K_{dd} and K_s to zero will form a classical PI plus derivative (PID) controller [7] (i.e. implemented when a torque transducer is available). Moreover, both the RRC and PID controller structures can be additionally implemented with disturbance feedback, by setting the disturbance gains K_{pd} , K_{dd} to a non-zero value.



(a) Classical PI controller.



(b) Extended PI Controller augmented with feedback of additional state variables.

Figure 2. Controllers for two-inertia mechanical model.

Disturbance Observer Structure

Periodic load-side disturbances are a common feature of industrial automated production systems, for instance, where objects are dropped at equal time intervals onto a conveyer belt. For such systems, disturbance torque (as opposed to shaft or electromagnetic torque) cannot be sensed directly, and this requires an observer to provide a dynamic estimate. Assuming the disturbance torque is a state-variable, and is slow varying, implying that $\frac{dt_d}{dt} \rightarrow 0$, a state-variable representation of the two-inertia system can be obtained that includes the disturbance torque as a state, as follows:

$$\frac{d}{dt} \begin{bmatrix} \omega_m \\ t_{md} \\ \omega_d \\ t_d \end{bmatrix} = \begin{bmatrix} 0 & -\frac{1}{J_m} & 0 & 0 \\ K_{md} & 0 & K_{md} & 0 \\ 0 & \frac{1}{J_d} & 0 & -\frac{1}{J_d} \\ 0 & 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} \omega_m \\ t_{md} \\ \omega_d \\ t_d \end{bmatrix} + \begin{bmatrix} \frac{1}{J_m} \\ 0 \\ 0 \\ 0 \end{bmatrix} t_e \quad (2)$$

Design of the state observer is based on Gopinath's method because of its ease of implementation [8]. To derive a suitable dynamic observer, the state vector is partitioned into two parts:

$$\begin{bmatrix} \dot{x}_m \\ \dot{x}_e \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \cdot \begin{bmatrix} x_m \\ x_e \end{bmatrix} + \begin{bmatrix} B_1 \\ B_2 \end{bmatrix} u \quad (3)$$

where, x_m represents directly measured states, i.e. $x_m = y$, where y is the measured outputs of the plant, and x_e represents the remaining states that need to be observed. In the case of the PID controller, only the motor speed ω_m is sensed, and the required partitions are represented by dotted lines in (2). For the RRC controller, both ω_m and t_{md} are sensed, and the partitions are represented as dashed lines in (2). Notably, the order of the observer is reduced by the number of measured states. Hence, the PID controller requires a 3rd order observer, and the RRC controller only requires a 2nd order observer. For completeness, the dynamic structure of the observer is shown in Fig. 3, showing all the observed output states (only \hat{t}_d is employed by the extended PID/RRC controllers).

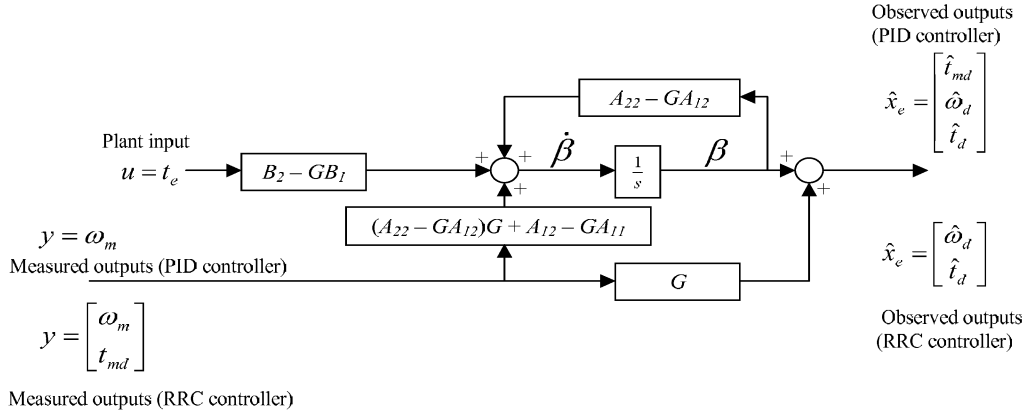


Figure 3. Block diagram representation of the observer structure.

The transfer function describing the relationship between the observed \hat{t}_d and actual load-torque t_d can be obtained from (3) [8], for the PID controller:

$$G(s)^{PID} = \frac{\hat{t}_d(s)}{t_d(s)} = \frac{-G_3\omega_a^2}{J_ms^3 - s^2G_1 + s(\omega_a^2J_m + G_2K_{md}) - G_3\omega_a^2} \quad (4)$$

and the controller:

$$G(s)^{RRC} = \frac{\hat{t}_d(s)}{t_d(s)} = \frac{G_2\omega_a^2}{s^2 - sG_1K_{md} + G_2\omega_a^2} \quad (5)$$

respectively, where the denominator equations describe the observer pole locations. The observer poles are therefore assigned according to the coefficients of the 2nd and 3rd optimal ITAE polynomials [8,9] resulting in the optimal observer gains given in Table I, where ω_{ob} is the equivalent -3dB observer bandwidth. If the observer bandwidth (and therefore the observer poles) is (are) assigned to be much greater than the highest frequency component of disturbance torque, it can be assumed that the observer does not unduly influence the assigned closed-loop regulation dynamics. Unfortunately, in practice, the observer structure is inherently derivative in nature and therefore sensitive to noisy input signals such as the motor speed signal that is obtained from the first derivative of quantised encoder position. As a result, therefore, the observer bandwidth must be minimised, since there exists a trade-off between the bandwidth of the observer and filtering of high frequency noise. Unfortunately, if consideration is not given to the additional dynamics imparted by a relatively low bandwidth disturbance observer, the closed-loop performance deteriorates as the observer bandwidth is reduced [9]. A tuning methodology is therefore proposed in the forgoing sections that facilitates the use of low bandwidth observers without sacrificing the control objectives.

TABLE I. OPTIMAL OBSERVER AND CONTROLLER GAINS

DISTURBANCE OBSERVER		CONTROLLER	
FULL-ORDER (PID CONTROLLER)	REDUCED-ORDER (RRC CONTROLLER)	PID	RRC
$G_1 = -1.75\omega_{ob}J_m$	$G_1 = \frac{-1.4\omega_{ob}}{K_{md}}$	$K_p \approx 1.85\omega_a J_d$	$K_p \approx 1.85\omega_a J_m$
$G_2 = \frac{(2.15\omega_{ob}^2 - \omega_a^2)J_m}{K_{md}}$	$G_2 = \frac{\omega_{ob}^2}{\omega_a^2}$	$K_i \approx 0.6\omega_a^2 J_d$	$K_i \approx 0.6\omega_a^2 J_m$
$G_3 = \frac{-\omega_{ob}^3 J_m}{\omega_a^2}$		$K_d = J_d - J_m$	$K_s = \frac{J_m}{J_d} - 1$

PID/RRC with Disturbance Feedback

Equations (6) and (7) provide the closed-loop transfer functions describing the regulation dynamics ($\omega_d(s)/t_d(s)$) for the PID and RRC controllers with disturbance feedback, respectively. For the PID controller (6), it can be seen that the numerator is 5th order (excluding the s/J_d multiplier term) which is comprised of a real zero and two pairs of complex zeros that can be assigned by the selection of the observer bandwidth, ω_{ob} and the disturbance feedback gains K_{pd} and K_{dd} . Similarly, for the RRC controller (7), the numerator is 4th order which is comprised of two pairs of complex zeros that can be assigned. Thus, in both cases, by proper adjustment of these gains, a pair of complex conjugate zeros are assigned to the imaginary axis (no damping) for a user-defined frequency, ω_{hj} , thereby rejecting periodic load-side disturbances of that frequency, whilst eliminating the effects of the observer dynamics on the rejection performance, i.e. a relatively low bandwidth disturbance observer can be implemented, attenuating high frequency noise, without sacrificing the control objective. However, to impart adequate closed-loop damping whilst additionally rejecting periodic load disturbances (a common industrial requirement), it is desirable to have the ability to independently assign both the closed-loop poles and zeros simultaneously. The closed-loop poles, when disturbance feedback is not implemented (denoted the first bracket 4th order polynomial expression in the denominator of (6) and (7)) are independently assigned according to the coefficients of the optimal 4th order ITAE polynomial [8], by the controller gains in Table I [9,10]. Moreover, it has been shown that the basic PI controller and two-inertia model imparts optimum closed-loop damping performance when $R \approx 1$ (according to the optimal ITAE polynomial) and increasingly under damped responses for $R < 1$ [7,9,10]. Moreover, the extra degree of freedom afforded by the PID and RRC controller enables R to be virtually adjusted to $\tilde{R} \approx 1$ by adjusting K_d or K_s , respectively— see Table I.

$$\frac{\omega_d}{t_d} = \frac{s \left\{ \begin{aligned} &\tilde{J}_m s^5 + (K_p + 1.75\omega_{ob}\tilde{J}_m)s^4 \\ &+ (2.15\omega_{ob}^2\tilde{J}_m + 1.75\omega_{ob}K_p + K_i + K_{md})s^3 \\ &+ (2.15\omega_{ob}^2K_p + \omega_{ob}^3\tilde{J}_m + 1.75\omega_{ob}[K_i + K_{md}])s^2 \\ &+ (\omega_{ob}^3K_p + 2.15\omega_{ob}^2[K_i + K_{md}] - J_d K_{dd}\omega_{ob}^3\omega_a^2)s \\ &+ \omega_{ob}^3[K_i + K_{md}] - J_d K_{pd}\omega_{ob}^3\omega_a^2 \end{aligned} \right\}}{J_d \left\{ \begin{aligned} &(\tilde{J}_m s^4 + K_p s^3 + (\tilde{J}_m \omega_a^2(1 + \tilde{R}) + K_i)s^2 + K_p \omega_a^2 s + K_i \omega_a^2) \\ &\cdot (s^3 + 1.75\omega_{ob}s^2 + 2.15\omega_{ob}^2 s + \omega_{ob}^3) \end{aligned} \right\}} \quad (6)$$

$$\text{where } \tilde{J}_m = J_m + K_d \text{ and } \tilde{R} = J_d/\tilde{J}_m$$

$$\frac{\omega_d}{t_d} = \frac{s \left\{ \begin{aligned} &J_m s^4 + (K_p + 1.4\omega_{ob} J_m) s^3 \\ &+ (\omega_{ob}^2 J_m + 1.4\omega_{ob} K_p + [K_i + K_{md}(1 + K_s)]) s^2 \\ &+ (\omega_{ob}^2 K_p + 1.4\omega_{ob} [K_i + K_{md}(1 + K_s)]) - J_d K_{dd} \omega_{ob}^2 \omega_a^2 s \\ &+ \omega_{ob}^2 [K_i + K_{md}(1 + K_s)] - J_d K_{pd} \omega_{ob}^2 \omega_a^2 \end{aligned} \right\}}{J_d \left\{ \begin{aligned} &(J_m s^4 + K_p s^3 + (J_m \omega_a^2 (1 + \tilde{R}) + K_i) s^2 + K_p \omega_a^2 s + K_i \omega_a^2) \\ &\cdot (s^2 + 1.4\omega_{ob} s + \omega_{ob}^2) \end{aligned} \right\}} \quad (7)$$

$$\text{where } \tilde{R} = R(1 + K_s)$$

Equation (8) shows a 5th order polynomial expression factored into two parts. The first, a complex root, represents the user defined rejection frequency, ω_{rj} , where the damping ratio equals zero. The second factor, a 3rd order polynomial expression, defines the arbitrary location of the other roots.

$$\begin{aligned} &(s^2 + \omega_{rj}^2)(s^3 + as^2 + bs + c) \\ &= s^5 + s^4 a + s^3(b + \omega_{rj}^2) + s^2(c + \omega_{rj}^2 a) + sb\omega_{rj}^2 + c\omega_{rj}^2 \end{aligned} \quad (8)$$

By equating the numerator of (6) with the expanded polynomial in (8), expressions for the disturbance feedback gains K_{pd} and K_{dd} can be derived for the PID controller that enables ω_{rj} and the observer bandwidth to be independently assigned, as follows:

$$K_{pd} = \frac{\omega_{ob}^3 (K_i + K_{md}) - \omega_{rj}^2 (\tilde{J}_m \omega_{ob}^3 + 2.15\omega_{ob}^2 K_p + 1.75\omega_{ob} (K_i + K_{md}) - \omega_{rj}^2 (\tilde{J}_m \omega_{ob} 1.75 + K_p))}{J_d \omega_{ob}^3 \omega_a^2} \quad (9)$$

$$K_{dd} = \frac{\omega_{ob}^3 K_p + 2.15\omega_{ob}^2 (K_i + K_{md}) - \omega_{rj}^2 (\tilde{J}_m 2.15\omega_{ob}^2 + 1.75\omega_{ob} K_p + K_i + K_{md} - \omega_{rj}^2 \tilde{J}_m)}{J_d \omega_{ob}^3 \omega_a^2} \quad (10)$$

Similarly, for the controller, the numerator of (7) is equated to a factorised 4th order polynomial expression:

$$\begin{aligned} &(s^2 + \omega_{rj}^2)(s^2 + bs + c) \\ &= s^4 + s^3 b + s^2(c + \omega_{rj}^2) + s\omega_{rj}^2 b + c\omega_{rj}^2 \end{aligned} \quad (11)$$

giving the following disturbance feedback gains:

$$K_{pd} = \frac{\omega_{ob}^2 (K_i + K_{md}(1 + K_s)) - \omega_{rj}^2 (\omega_{ob}^2 J_m + 1.4\omega_{ob} K_p + K_i + K_{md}(1 + K_s) - \omega_{rj}^2 J_m)}{J_d \omega_{ob}^2 \omega_a^2} \quad (12)$$

$$K_{dd} = \frac{\omega_{ob}^2 K_p + 1.4\omega_{ob}(K_i + K_{md}(1 + K_s)) - \omega_{rj}^2(K_p + 1.4\omega_{ob}J_m)}{J_d\omega_{ob}^2\omega_a^2} \quad (13)$$

By way of example, the user defined rejection frequency is set at $\omega_{rj} = 62.8$ rad (10Hz) with the mechanical parameters defined in Table II. Figure 4 shows the regulation bode magnitude plots for the PID and RRC controller, respectively, as ω_{ob} is adjusted. It can be seen that, for both controllers, reducing the observer bandwidth does not significantly influence the control objective, i.e. the attenuation at ω_{rj} remains constant.

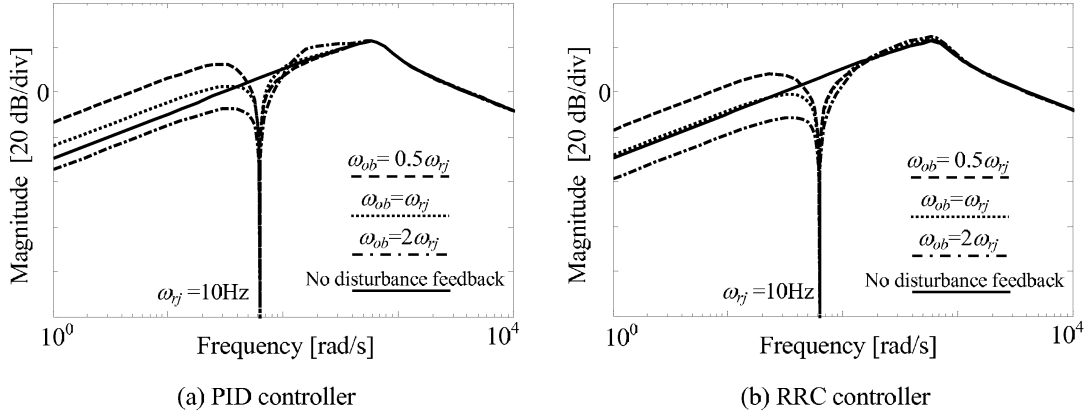


Figure 4. Regulation performance of proposed controller structures and tuning methodology

However, it can be seen that, in general, the RRC controller improves low frequency attenuation for a given observer bandwidth, when compared to that of the PID controller. It should be noted that for both controllers, the observer bandwidth cannot be made infinitely small, since, for low bandwidth observers, low frequency disturbances are amplified when compared to case with no disturbance feedback (i.e. when $K_{pd}, K_{dd} = 0$), as evidenced in Fig 4. It is therefore desirable to employ an observer of sufficient relative bandwidth to ensure adequate rejection of the low frequency band, particularly in the event of a variation in the disturbance frequency.

Experimental Validation

The proposed control techniques, simulation results and observations are now validated on the experimental test-facility, comprising of the 2.2kW prototype PMSM with integrated 20Nm SAW-based torque transducer, Fig. 1(b), and a similarly rated loading machine (representing the motor and load inertias, J_m and J_d , respectively). The machines are coupled back-to-back via a shaft and couplings. Once again, Table II gives the resulting mechanical parameters.

The experimental results now presented are in response to a 3Nm sinusoidal disturbance torque with a frequency of 62.8 rad/s (10Hz), where the speed controller reference is chosen to be constant at 10rad/s. For all results, shaft torque measurements are obtained from the integrated torque transducer. Figure 5 shows the time domain regulation performance imparted by the PID controller with no disturbance feedback. It can be seen that the oscillatory load torque induces a corresponding unwanted oscillatory component of load-side speed.

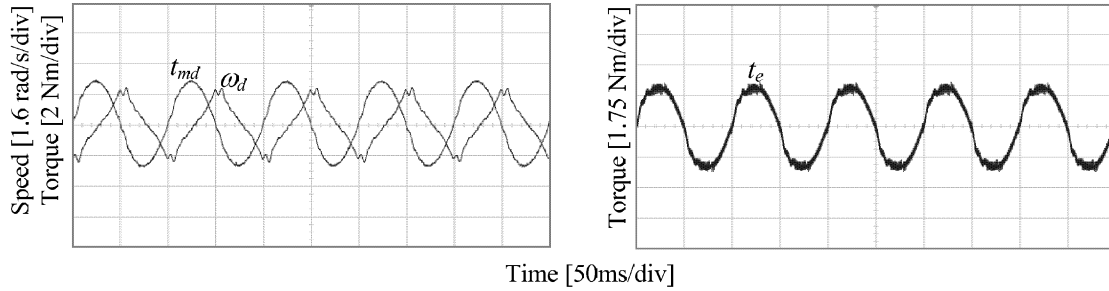


Figure 5. PID controller with without disturbance torque feedback.

Figure 6 now shows the PID controller responses with disturbance feedback, as the observer bandwidth is increased, where $\omega_{ob} = 0.5\omega_{rj}$, ω_{rj} and $1.25\omega_{rj}$, respectively. It can be seen that the load perturbations are rejected from the load-speed, and rejection performance is not unduly influenced by the bandwidth of the observer. Furthermore, when the observer bandwidth is less than the rejection frequency, Fig 5.10(a), i.e. when $\omega_{ob} = 0.5\omega_{rj}$, the controller noise is attenuated to levels comparable to that obtained with no disturbance feedback, Fig. 6.

TABLE II
MECHANICAL PARAMETERS

R	0.5
J_d	0.00025 kgm ²
K_{md}	80 Nm/rad
ω_a	565.7rad/s (90Hz)

Notably, when $\omega_{ob} > 1.5\omega_{rj}$ (>15Hz) instability occurred when using the PID controller due to the elevated noise levels. This is a result of the requirement of a higher order disturbance observer (compared with the RRC controller), thereby exacerbating the effects of high frequency noise originating from the motor speed signal. Furthermore, the PID controller requires a motor acceleration signal estimated via the double-derivative of the encoder position. By comparison, the RRC controller can accommodate a significantly higher bandwidth observer before instability occurs (thereby ensuring adequate rejection of all low frequencies in the event of the rejection frequency varying—see Fig. 4), when $\omega_{ob} > 3.5\omega_{rj}$ (>35Hz), by virtue of the reduced noise levels. By way of example, Fig. 7 shows the responses of the RRC controller for $\omega_{ob} = 3\omega_{rj}$, and $2\omega_{rj}$, respectively

Furthermore, Figs. 6 and 7 demonstrate the equivalence of the PID and RRC controllers with observer disturbance feedback. However, by virtue of increased observer bandwidth, and improved rejection performance, (compare Figs 4(a) and (b)) the RRC controller, in general, imparts improved disturbance rejection over the low frequency band resulting in ‘flatter’ unperturbed load speed traces, as evidenced in Fig 7.

Conclusion

To address the effects of periodic load-side disturbance torques on the load speed profile, extended controllers, based on classical feed-forward compensation, have been proposed. For the investigation, a SAW torque transducer is mounted inside a commercial off-the-shelf permanent magnet synchronous machine. Specifically, both PID and RRC controllers are augmented with an additional feedback of observed disturbance torque (since it cannot be measured), via a proportional and derivative based controller. The extended controllers afford the flexibility to simultaneously impart optimal closed-loop damping, by allowing the independent selection of virtual inertia ratio, whilst

additionally, facilitating the independent assignment of regulation transmission zero's, such that, when properly assigned, enable the rejection of a periodic disturbance torque from the load speed.

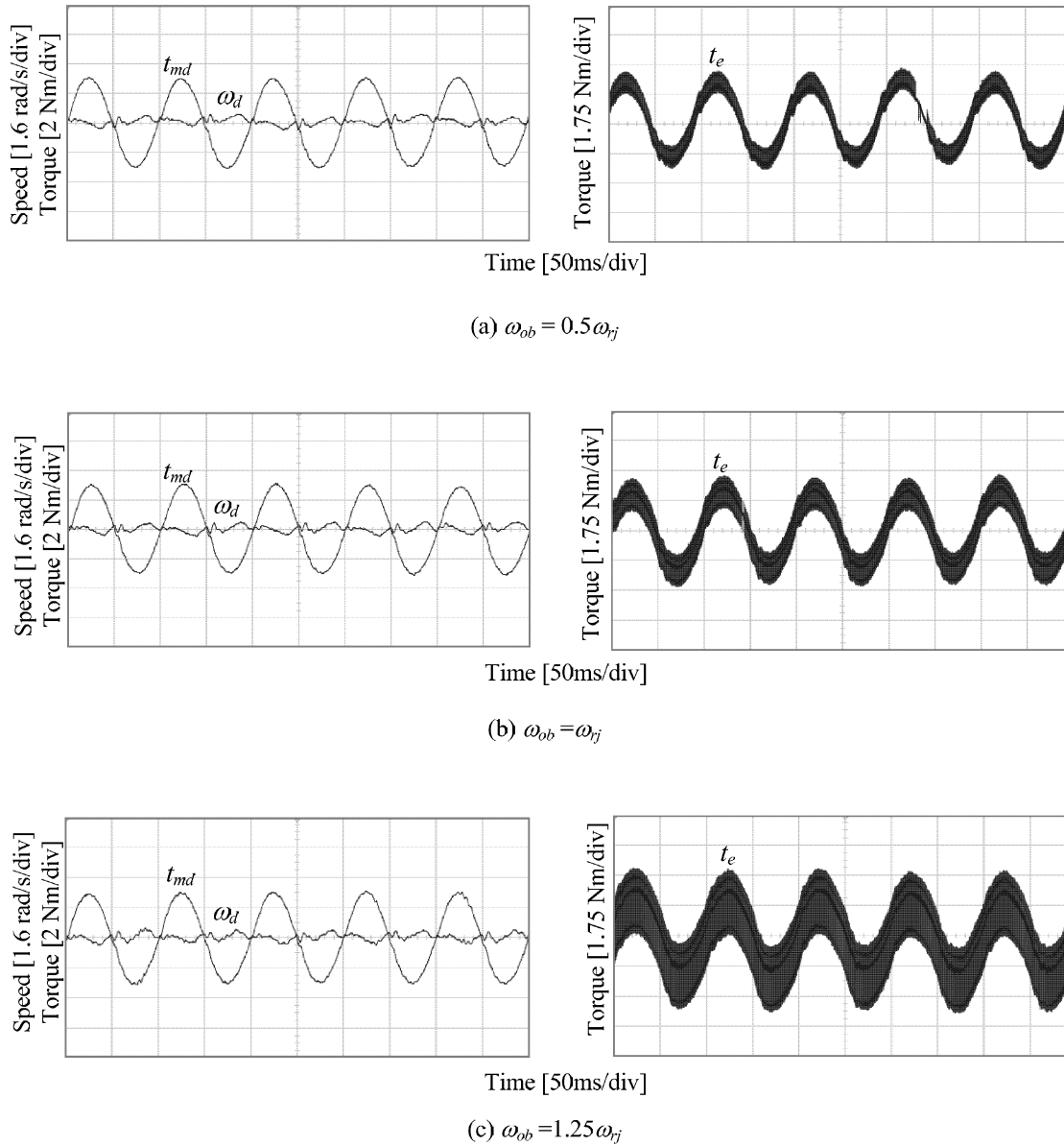


Figure 6. PID controller with observed disturbance torque feedback.

Moreover, to realise disturbance feedback, the PID controller requires a full, third-order disturbance observer, since only motor position feedback is employed, whereas the RRC controller, which employs both shaft torque and motor position sensors, can be implemented with a second-order observer. Appraisal has been given to the combined observer and controller dynamics, with the zeros reassigned, demonstrating, for the first time, that the bandwidth of the observer need not effect the rejection of a periodic disturbance, thereby enabling significantly lower bandwidth observers to be employed, i.e. the observer bandwidth can be lower than the rejection frequency. It is shown that higher bandwidth disturbance observers are required to maximise the disturbance attenuation over all of the low frequency band (as well as the desired rejection frequency), thereby attenuating a wide range of possible frequencies. In such cases, therefore, it is shown that the RRC controller is the

preferred solution by virtue of reduced noise sensitivity. Furthermore, it is demonstrated that a integrated 20Nm SAW torque transducer, as employed by the RRC controller, is not unduly affected by machine generated electromagnetic noise. Additionally, since the SAW devices are inherently low cost in mass production, and the mechanical modifications to the commercial PMSM, are minimal, the cost of high volume integration is estimated to increase the total machine cost by only a few percent.

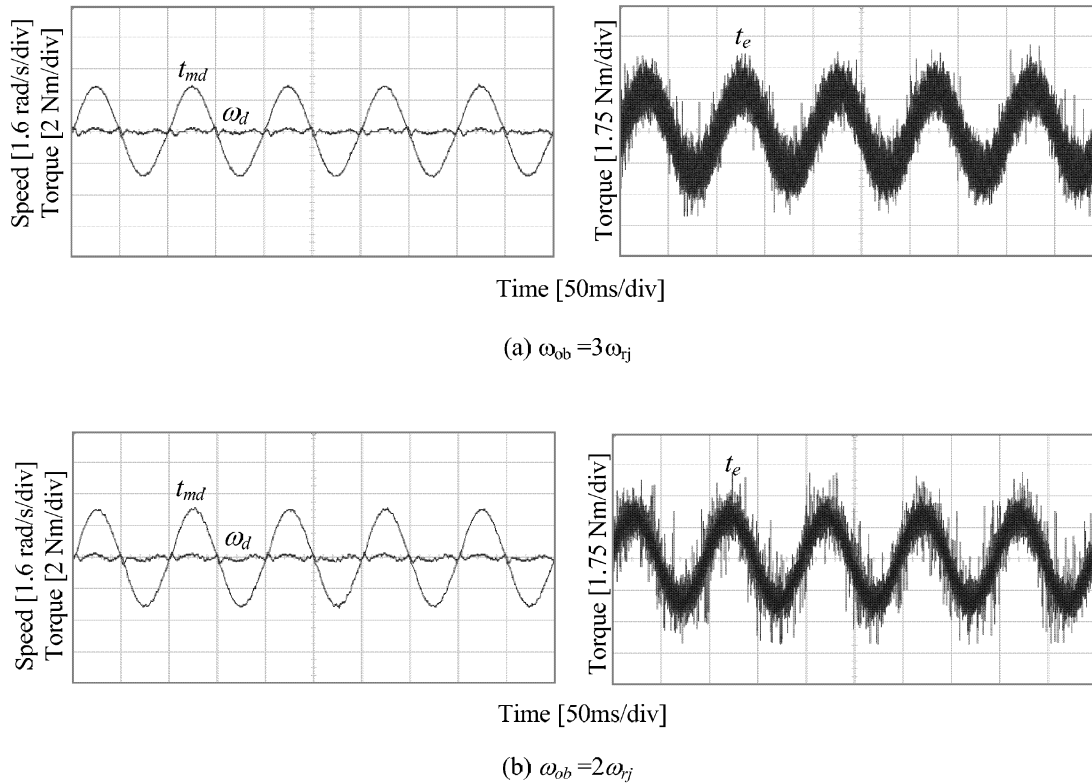


Figure 7. RRC controller with observed disturbance torque feedback.

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