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Rozek, Agata; Lowry, Stephen C.; Rozitis, Benjamin; Dover, Lord R.; Taylor, Patrick A.; Virkki, Anne
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# Physical properties of near－Earth asteroid（2102）Tantalus from multiwavelength observations 

Agata Rożek ${ }^{\oplus}$ ，${ }^{1,2 \star}$ Stephen C．Lowry，${ }^{2}$ Benjamin Rozitis，${ }^{3}$ Lord R．Dover ${ }^{\oplus},{ }^{2}$ Patrick A．Taylor ${ }^{\oplus}, 4,5,6$ Anne Virkki，${ }^{4,7}$ Simon F．Green，${ }^{3}$ Colin Snodgrass ${ }^{\bullet}$ ， 1,3 Alan Fitzsimmons，${ }^{8}$ Justyn Campbell－White ${ }^{\bullet}$ ，${ }^{9}$ Sedighe Sajadian，${ }^{10}$ Valerio Bozza，${ }^{11,12}$ Martin J．Burgdorf ${ }^{\oplus}$ ，${ }^{13}$ Martin Dominik ${ }^{\oplus},{ }^{14}$ R．Figuera Jaimes，${ }^{15}$ Tobias C．Hinse ${ }^{\oplus},{ }^{16,17}$ Markus Hundertmark，${ }^{18}$ Uffe G．Jørgensen，${ }^{19}$ Penélope Longa－Peña，${ }^{20}$ Markus Rabus ${ }^{\oplus}$ ，${ }^{21}$ Sohrab Rahvar ${ }^{\odot}$ ，${ }^{22}$ Jesper Skottfelt ${ }^{23}$ and John Southworth ${ }^{\circledR 24}$ Affiliations are listed at the end of the paper

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#### Abstract

Between 2010 and 2017，we have collected new optical and radar observations of the potentially hazardous asteroid （2102）Tantalus from the ESO NTT and Danish telescopes at the La Silla Observatory，and from the Arecibo planetary radar． The object appears to be nearly spherical，showing a low－amplitude light－curve variation and limited large－scale features in the radar images．The spin－state is difficult to constrain with the available data；including a certain light－curve subset significantly changes the spin－state estimates，and the uncertainties on period determination are significant．Constraining any change in rotation rate was not possible，despite decades of observations．The convex light curve－inversion model，with rotational pole at $\lambda=210^{\circ} \pm 41^{\circ}$ and $\beta=-30^{\circ} \pm 35^{\circ}$ ，is more flattened than the two models reconstructed by including radar observations： with prograde $\left(\lambda=36^{\circ} \pm 23^{\circ}, \beta=30^{\circ} \pm 15^{\circ}\right)$ ，and with retrograde rotation mode（ $\left.\lambda=180^{\circ} \pm 24^{\circ}, \beta=-30 \pm 16^{\circ}\right)$ ．Using data from WISE，we were able to determine that the prograde model produces the best agreement in size determination between radar and thermophysical modelling．Radar measurements indicate possible variation in surface properties，suggesting one side might have lower radar albedo and be rougher at the centimetre－to－decimetre scale than the other．However，further observations are needed to confirm this．Thermophysical analysis indicates a surface covered in fine－grained regolith，consistent with radar albedo，and polarisation ratio measurements．Finally，geophysical investigation of the spin－stability of Tantalus shows that it could be exceeding its critical spin－rate via cohesive forces．


Key words：techniques：photometric－techniques：radar astronomy－minor planets，asteroids：individual：（2102）Tantalus－ methods：observational．

## 1 INTRODUCTION

The asteroidal Yarkovsky－O＇Keefe－Radzievskii－Paddack（YORP） effect is a tiny recoil torque resulting from reflection，absorption and re－radiation of thermal photons illuminating surfaces of small bodies （Rubincam 2000）．It is considered to be one of the main drivers in the physical and dynamical evolution of small asteroids close to the Sun． The YORP effect changes the rotational momentum of small bodies affecting both the spin－axis orientation and the rate of rotation．The latter can be directly detected through ground－based observations （e．g．Lowry et al．2007；Taylor et al．2007）．The effect is strongest on near－Earth asteroids（NEAs）as it scales inversely with the squares of size and solar distance．Notably，all direct detections to date are in the spin－up sense and the detections are not always in line with theoretical predictions due to the high sensitivity of YORP to surface properties and shape details（e．g．Statler 2009；Rozitis \＆Green 2013； Golubov et al．2016），and internal properties（e．g．Lowry et al．2014）．
＊E－mail：a．rozek＠ed．ac．uk

In order to increase the number of detections to aid theoretical ad－ vances of the YORP effect，we are conducting a long－term observing campaign of a relatively large sample of NEA to measure their YORP strengths．Observations of 42 NEAs were carried out，primarily from a European Southern Observatory（ESO）Large Programme aimed at optical and infrared photometric monitoring．While this initial phase is now completed，additional data are still being collected with associated programmes at other ground－based facilities．A detection of a change in the sidereal rotation rate can be achieved in a few ways． One method involves direct measurement of the rotation period at different times．This was possible for the very first asteroidal YORP detection（Lowry et al．2007）．Asteroid（54509）YORP＇s rotation period is only around 730 s．Due to the fast rotation and a small variation in viewing geometry，a very precise determination of the sidereal rotation period was possible．For this analysis，observations from each apparition were grouped in year－long batches（mid－2001 to mid－2002，mid－2002 to mid－2003，and so on），and a different period value was obtained for each of the five years of the observing campaign．A linear change in the rotation period was measured and attributed to YORP as the most likely explanation（Taylor et al．
2007). However, this object was very small (about $57-\mathrm{m}$ radius) making the YORP effect relatively strong. For objects with a weaker YORP acceleration and a slower rotation this technique becomes less practical as it becomes more difficult to make sufficiently accurate period measurements for periods on the order of hours to detect a subtle YORP-induced change.

A second approach combines a shape model determined using other types of observations with long-term light-curve observations. This can be a radar-derived model, which was the case for asteroids (54509) YORP, (101955) Bennu, and (68346) 2001 KZ66 (Taylor et al. 2007; Nolan et al. 2019; Zegmott et al. 2021), or a spacecraft model, which helped detect a spin-state change for (25143) Itokawa (Lowry et al. 2014). A subset of the light curves may be used for breaking pole degeneracy inherent in radar data interpretation, like was done for example when determining YORP detection limit for asteroid (85990) 1999 JV6 (Rożek et al. 2019b). All available lightcurve observations are then compared with synthetic light curves, generated using a shape model developed assuming a constant rotation period, and any offset in the rotational phase required to align them is measured. A quadratic trend in the measured phase offsets indicates a linear change in the rotation rate.

Finally, another approach incorporates a linear change in the rotation rate directly in the shape modelling of the object, normally in the light-curve inversion (Kaasalainen et al. 2007; Ďurech et al. 2008, 2012, 2018, 2022). The method requires a range of shape models to be developed assuming either a constant or varying sidereal rotation period. The quality of the fit of model light curves to the data is compared between the constant-period and varying-period solutions to assess the spin-state. We adopted this technique here, although we did not obtain a conclusive YORP measurement.

The subject of this study, (2102) Tantalus, is a potentially hazardous asteroid classified as an Sr spectral type (Thomas et al. 2014). It was observed photometrically in 1994 and 1995 from Bochum and Odřejov Observatories by Pravec et al. (1997) (these light curves are publicly available, and we include them in our analysis, labelled 1-3 in Table 1) with the reported mean synodic period $2.391 \pm 0.01 \mathrm{~h}$, close to the rubble pile rotationally induced fission limit.

Observations in 2014 and 2017 from Palmer Divide Station (these light curves are labelled 12-30 in Table 1 Warner 2015, 2017) suggest a spin period of around $2.383 \pm 0.001 \mathrm{~h}$. Additionally, a secondary period of $16.38 \pm 0.02 \mathrm{~h}$ was detected in the data that suggested the presence of an elongated satellite. Further optical observations from a small telescope in Spain (Isaac Aznar Observatory, 0.36 m) confirmed the approximately $2.39-\mathrm{h}$ rotation period and revealed a possible 8.22 h secondary period Vaduvescu et al. (2017). The asteroid diameter was most recently estimated to be $1.762 \pm 0.603 \mathrm{~km}$ with the NEOWISE survey (Masiero et al. 2017).

We observed Tantalus both photometrically with optical telescopes, and using the Arecibo planetary radar. In this paper, we discuss the observing campaign (Section 2), how we attempted to constrain YORP using photometric light curves alone (Section 3), and how we combined optical light-curve and radar observations to develop a spin-state and shape model (Section 4), radar surface properties developed from calibrated radar spectra (Section 5), thermophysical properties developed by combining our shape models with the WISE infrared data (Section 6), and finally geophysical analysis using one of the shape models (Section 7). Issues concerning modelling a nearly spherical object are highlighted here.

## 2 OBSERVATIONS

We observed Tantalus primarily with the EFOSC2 camera on the 3.6-m NTT telescope at ESO's La Silla Observatory in Chile on eight
nights between 2010 August and 2013 November (labelled with lightcurve IDs 4-11 and 'NTT' as observing facility in Table 1). These light curves were obtained under ESO programme 185.C-1033. We collected further optical light curves in June and July 2017 with the Danish 1.54 m telescope, also located at La Silla (label 'Danish' in Table 1, IDs 31 and 32) using the DFOSC instrument. These observations were obtained as part of the MiNDSTEp consortium that operates the Danish telescope for six months each year.

The relative optical light curves record the asteroid's brightness variation compared with background stars within the frame and relative to other observations in a series. A series of images in the Bessel R filter (for light-curve IDs 4-9 from the NTT and 31-32 from the Danish telescope) or Bessel V (light-curve IDs 10 and 11) were acquired on each night. Individual frames were reduced using basic CCD reduction techniques, bias subtraction and flatfield correction. Additionally, we removed fringe patterns from the R-frames acquired at the NTT by subtracting an EFOSC2 fringe map (provided by ESO) scaled by the computed fringe amplitude in individual images (Snodgrass \& Carry 2013). Due to the low signal from the asteroid, images on some nights (light-curve IDs 3 and 9) were summed in batches of 3 to improve the signal-to-noise ratio (S/N). The light-curve data can be accessed in Table A1, available at the CDS.

The asteroid was observed with the Arecibo planetary radar over five nights in January 2017 under NEA monitoring programme R3037 (data summary in Table 2). Two types of radar data were collected: continuous-wave (cw) observations, which display the Doppler shift of the signal reflected off the asteroid's surface due to its rotation, and delay-Doppler imaging, which is a two-dimensional diagram of radar echo power as a function of both Doppler shift and delay of the returning signal (e.g. Benner et al. 2015). The imaging frames were collected mainly with a $150-\mathrm{m}$ resolution in delay, except on 2017 January 1 when an imaging resolution of 75 m was achieved. Additionally, ranging observations were taken on 2017 January 1 and 4 with a delay resolution of 600 m , but those have a resolution that is too low for shape reconstruction and were used to improve orbital parameters only.

## 3 LIGHT-CURVE ANALYSIS

Light-curve data for Tantalus span 23 yr and a wide range of observing geometries (see Table 1), which is in many cases a good starting point for shape and spin-state modelling. However, the lightcurve peak-to-peak amplitude is not very high, ranging between 0.07 and 0.25 mag with a few of the light curves having low $\mathrm{S} / \mathrm{N}$ (for example light curves with IDs 2, 19, and 31). Close inspection shows that in some cases the peak-to-peak amplitude is exaggerated due to the scatter of light-curve points and hence might be actually lower than listed in Table 1. Moreover, some light curves represent only short fragments of rotation (like light curves with IDs 5, 17, and 27). This presents certain difficulties in obtaining spin-state and shape solutions.

Initially, all of the available light curves were used to determine a convex shape model, using established convex inversion procedures described by Kaasalainen \& Torppa (2001) and Kaasalainen, Torppa \& Muinonen (2001) and implemented by Ďurech, Sidorin \& Kaasalainen (2010). For each period tested, a shape and pole were optimised using six different starting pole positions (Kaasalainen et al. 2001). At the end of the optimisation, the quality of the fit, $\chi^{2}$ (defined with equation 13 by Kaasalainen \& Torppa 2001), for the best of the six models is recorded, but the shape and pole information is discarded. We have run a period search using this method in a wide

Table 1. A chronological list of optical light curves of asteroid (2102) Tantalus that were used in this study. For each light curve a numerical 'ID', Universal Time (UT), 'UT Date' at the beginning of the night, the heliocentric ( $R_{\mathrm{h}}$ '), and geocentric (' $\Delta$ ') distances measured in au, the solar phase angle (' $\alpha$ '), the observer-centred ecliptic longitude (' $\lambda_{o}$ '), and latitude (' $\beta_{o}$ '), 'Total' length of the light curve, the apparent peak-to-peak 'Amplitude', 'Filter', and the 'Observing facility' used to obtain the light curve are listed. Where applicable a 'Reference' to the already published work is given. Each row represents a single light curve (sometimes a few segments were observed on a single night). The shape modelling using light-curve inversion was done twice, once using the full light-curve data set and one restricted to a subset of light curves marked with black circles in the 'LC-subset model' column (Section 3). For the model combining radar data with optical light curves, we used a subset of the light curves from our observing campaign selected for S/N and observing geometry coverage (black circles in the 'LC + radar model' column; Section 4). Observing facility key (with MPC site code): (Bochum, 809), European Southern Observatory 0.61-m Bochum telescope in La Silla, Chile; (Ondřejov, 557), Academy of Sciences of the Czech Republic Ondřejov Observatory telescope, Czechia; (NTT, 809), European Southern Observatory 3.58-m New Technology Telescope in La Silla, Chile; (CS3-PDS, U82), Palmer Divide Station (various telescopes with $0.3-0.5 \mathrm{~m}$ mirrors), California, USA; (Danish, 809), European Southern Observatory 1.54-m Danish telescope in La Silla, Chile.

| ID | UT Date (yyyy-mm-dd) | $\begin{gathered} R_{\mathrm{h}} \\ (\mathrm{au}) \end{gathered}$ | $\begin{gathered} \Delta \\ (\mathrm{au}) \end{gathered}$ | $\alpha$ $\left({ }^{\circ}\right)$ | $\begin{aligned} & \lambda_{o} \\ & \left({ }^{\circ}\right) \end{aligned}$ | $\beta_{o}$ <br> $\left({ }^{\circ}\right)$ | Total <br> (h) | Ampl. <br> (mag) | Filter | Observing facility | LC-subset model | $\begin{gathered} \mathrm{LC}+\text { radar } \\ \text { model } \end{gathered}$ | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1994-Dec-09 | 1.182 | 0.534 | 55.64 | 119.6 | -79.3 | 7.4 | 0.13 | $R$ | Bochum | $\bullet$ |  | Pravec et al. (1997) |
| 2 | 1995-Jun-28 | 1.327 | 0.343 | 21.93 | 255.9 | 20.9 | 3.9 | 0.20 | $R$ | Ondřejov | $\bullet$ |  | Pravec et al. (1997) |
| 3 | 1995-Jun-29 | 1.331 | 0.348 | 22.01 | 254.3 | 18.3 | 2.5 | 0.23 | $R$ | Ondřejov | $\bullet$ |  | Pravec et al. (1997) |
| 4 | 2010-Aug-31 | 1.651 | 1.460 | 37.24 | 162.5 | -81.6 | 2.4 | 0.11 | $R$ | NTT | - | $\bullet$ |  |
| 5 | 2010-Oct-13 | 1.568 | 1.439 | 38.46 | 211.3 | -77.5 | 1.0 | 0.07 | $R$ | NTT | $\bullet$ |  |  |
| 6 | 2010-Oct-14 | 1.566 | 1.436 | 38.53 | 212.3 | -77.5 | 3.0 | 0.21 | $R$ | NTT | - | $\bullet$ |  |
| 7 | 2010-Oct-15 | 1.563 | 1.432 | 38.59 | 213.4 | -77.6 | 1.7 | 0.12 | $R$ | NTT | - |  |  |
| 8 | 2011-Jan-30 | 1.138 | 0.887 | 56.59 | 22.7 | -26.0 | 1.8 | 0.10 | $R$ | NTT | - | $\bullet$ |  |
| 9 | 2011-Sep-01 | 1.416 | 1.282 | 43.59 | 233.5 | -6.3 | 1.4 | 0.11 | $R$ | NTT | - | - |  |
| 10 | 2013-Nov-05 | 1.408 | 1.143 | 44.26 | 174.2 | -78.1 | 2.1 | 0.14 | V | NTT | - | - |  |
| 11 | 2013-Nov-07 | 1.400 | 1.124 | 44.59 | 175.2 | -78.6 | 2.4 | 0.15 | $V$ | NTT | $\bullet$ | $\bullet$ |  |
| 12 | 2014-Jun-19 | 1.204 | 0.455 | 55.15 | 229.9 | 73.1 | 3.9 | 0.15 | None | CS3-PDS |  |  | Warner (2015) |
| 13 | 2014-Jun-19 | 1.205 | 0.454 | 55.05 | 229.7 | 72.8 | 2.4 | 0.20 | None | CS3-PDS |  |  | Warner (2015) |
| 14 | 2014-Jun-19 | 1.206 | 0.453 | 54.99 | 229.6 | 72.6 | 1.2 | 0.11 | None | CS3-PDS |  |  | Warner (2015) |
| 15 | 2014-Jun-20 | 1.209 | 0.449 | 54.39 | 229.0 | 71.0 | 3.3 | 0.20 | None | CS3-PDS |  |  | Warner (2015) |
| 16 | 2014-Jun-20 | 1.210 | 0.448 | 54.29 | 228.9 | 70.7 | 3.2 | 0.14 | None | CS3-PDS |  |  | Warner (2015) |
| 17 | 2014-Jun-20 | 1.210 | 0.447 | 54.23 | 228.8 | 70.4 | 0.5 | 0.06 | None | CS3-PDS |  |  | Warner (2015) |
| 18 | 2014-Jun-21 | 1.214 | 0.443 | 53.63 | 228.4 | 68.8 | 3.4 | 0.16 | None | CS3-PDS |  |  | Warner (2015) |
| 19 | 2014-Jun-21 | 1.215 | 0.442 | 53.51 | 228.3 | 68.5 | 3.2 | 0.23 | None | CS3-PDS |  |  | Warner (2015) |
| 20 | 2014-Jun-22 | 1.219 | 0.438 | 52.81 | 227.9 | 66.5 | 4.0 | 0.21 | None | CS3-PDS |  |  | Warner (2015) |
| 21 | 2014-Jun-22 | 1.219 | 0.437 | 52.71 | 227.8 | 66.1 | 2.5 | 0.10 | None | CS3-PDS |  |  | Warner (2015) |
| 22 | 2014-Jun-23 | 1.223 | 0.434 | 52.06 | 227.4 | 64.2 | 3.4 | 0.13 | None | CS3-PDS |  |  | Warner (2015) |
| 23 | 2014-Jun-23 | 1.224 | 0.433 | 51.97 | 227.4 | 63.9 | 2.6 | 0.13 | None | CS3-PDS |  |  | Warner (2015) |
| 24 | 2014-Jun-23 | 1.225 | 0.433 | 51.91 | 227.3 | 63.6 | 0.9 | 0.06 | None | CS3-PDS |  |  | Warner (2015) |
| 25 | 2017-Jan-06 | 1.016 | 0.183 | 74.7 | 21.1 | 15.2 | 2.3 | 0.16 | None | CS3-PDS |  |  | Warner (2017) |
| 26 | 2017-Jan-06 | 1.016 | 0.185 | 74.81 | 21.0 | 15.6 | 1.4 | 0.13 | None | CS3-PDS |  |  | Warner (2017) |
| 27 | 2017-Jan-06 | 1.015 | 0.185 | 74.87 | 20.9 | 15.9 | 0.6 | 0.13 | None | CS3-PDS |  |  | Warner (2017) |
| 28 | 2017-Jan-16 | 0.978 | 0.336 | 81.15 | 12.2 | 38.8 | 1.4 | 0.11 | None | CS3-PDS |  |  | Warner (2017) |
| 29 | 2017-Jan-17 | 0.974 | 0.351 | 81.16 | 11.6 | 40.0 | 2.2 | 0.14 | None | CS3-PDS |  |  | Warner (2017) |
| 30 | 2017-Jan-18 | 0.971 | 0.368 | 81.12 | 11.1 | 41.0 | 2.1 | 0.11 | None | CS3-PDS |  |  | Warner (2017) |
| 31 | 2017-Jun-11 | 1.287 | 0.384 | 38.52 | 300.6 | 36.9 | 2.6 | 0.25 | $R$ | Danish | $\bullet$ | $\bullet$ |  |
| 32 | 2017-Jul-02 | 1.381 | 0.386 | 16.39 | 259.3 | -4.9 | 1.6 | 0.11 | $R$ | Danish | - |  |  |

$2-18-\mathrm{h}$ interval (the periodogram obtained this way, recording the quality of the fit for each tested period, is included in Fig. A1). There appears to be two significant $\chi^{2}$ minima, one around the 2.39 h literature synodic rotation period Pravec et al. (1997), Warner (2015, 2017), Vaduvescu et al. (2017), and another at twice that period. The 16 -h periodicity reported is not apparent in the full data set. The longer period, around 4.8 h , is not considered likely as the ligh curve-inversion produces nonviable models, considerably elongated along the $z$-axis, and initial radar modelling with this period failed to reproduce echo bandwidth at all observed geometries. A close-up of the periodogram around the literature synodic period (upper panel in Fig. 1), shows a family of possible solutions around the best-fitting solution within this interval corresponding to $\chi^{2}$ minimum with a few periods having a quality of fit within 1 per cent difference. This means there is a certain level of ambiguity to the period solution.

Following the same method as Ďurech et al. (2012) to assess uncertainty, $1 \sigma$ would correspond to 3.5 per cent increase of $\chi^{2}$
for the search including all available light curves (for around 1600 light-curve points and 1500 degrees of freedom), and 5 per cent for restricted data set (about 750 light curve points and 650 degrees of freedom). In practice, the fits to data of synthetic light curves generated from models that differ by less than 10 per cent are virtually indistinguishable. Therefore, to assess the uncertainties of parameters such as pole and period we consider standard deviation of models with the $\chi^{2}$ within 10 per cent of minimal value.

We used the best-fitting period, $\mathrm{P}=2.385 \mathrm{~h}$, as a starting point for further convex inversion modelling and searched for the pole solution using a $5^{\circ} \times 5^{\circ}$ grid of possible pole positions. At each point of the grid, the period and shape were optimized and the quality of the fit recorded. We show the results of such a search, assuming a constantperiod solution, in Fig. 2. The colours in this figure correspond to the quality of the fit, with darker colours marking better solutions with lower $\chi^{2}$ values and the best-fitting pole indicated with a cross. The pole appears not to be very well constrained despite a wide range of

Table 2. Observations of asteroid (2102) Tantalus with the Arecibo planetary radar. 'UT Date' is the universal-time date on which the observations began, and the time-span of the received data is listed by the UT 'Start' and 'Stop' times. 'RTT' is the round-trip light time to the target. 'Baud' is the time resolution of the pseudo-random code used for imaging; baud does not apply to cw data. The baud length is translated to delay resolution ('Res.') expressed in metres. 'Runs' is the number of completed transmit-receive cycles. All but the most crude ranging observations, with resolution of 600 m , collected on the January 1 and 4 , were used in the shape modelling. The ranging observations are listed here for completeness.

| UT Date <br> (yyyy-mm-dd) | Start-Stop <br> (hh:mm:ss-hh:mm:ss) | RTT <br> $(\mathrm{s})$ | Baud <br> $(\mu \mathrm{s})$ | Res. <br> $(\mathrm{m})$ | Runs |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 2017-01-01 | $22: 48: 15-23: 05: 02$ | 144 | cw | - | 4 |
|  | $23: 13: 19-23: 25: 16$ |  | 4 | 600 | 3 |
|  | $23: 33: 14-00: 28: 41$ |  | 0.5 | 75 | 12 |
| $2017-01-04$ | $21: 19: 51-21: 46: 35$ | 169 | cw | - | 5 |
|  | $21: 57: 00-22: 11: 02$ | 170 | 4 | 600 | 3 |
|  | $22: 20: 44-23: 57: 05$ |  | 1 | 150 | 16 |
| $2017-01-05$ | $21: 01: 26-21: 22: 25$ | 181 | cw | - | 4 |
|  | $21: 34: 24-23: 38: 35$ |  | 1 | 150 | 21 |
| $2017-01-06$ | $20: 48: 13-21: 23: 39$ | 193 | cw | - | 6 |
|  | $21: 33: 07-22: 47: 29$ | 194 | 1 | 150 | 12 |
| $2017-01-07$ | $20: 49: 31-21: 32: 27$ | 207 | cw | - | 6 |
|  | $21: 42: 05-22: 20: 05$ |  | 1 | 150 | 6 |



Figure 1. Periodograms obtained using convex light-curve inversion methods searching around the literature value. The top panel shows the results of a period search using all available light curves and the bottom panel shows the results of the period search excluding some of the light curves, with the vertical dashed line marking $P=2.385 \mathrm{~h}$, corresponding to the minimum $\chi^{2}$ value in the shown interval. The uncertainties for both period determinations would be 0.003 h for the full period scan and 0.07 h for restricted. Horizontal continuous lines in both plots mark 1 per cent increase above the minimum $\chi^{2}$ value for each search, and dashed lines -10 per cent increase.


Figure 2. The upper panel shows a $\chi^{2}$-plane for a constant period pole search using light-curve inversion and the full available light-curve data set, and the lower panel is the same, but for search performed using a selection of the available light curves. Darker colours indicate lower $\chi^{2}$ values, and the lines mark gradual increases over the minimum $\chi^{2}$ value, with a solid line for 1 per cent increase, a dotted line for 5 per cent, and a dashed line for 10 per cent. The positions of a rotation pole corresponding to the minimum $\chi^{2}$ is marked with a cross in each panel, placed at $\lambda=210^{\circ}$ and $\beta=-30^{\circ}$ in the upper panel, and $\lambda=170^{\circ}$ and $\beta=-25^{\circ}$ in the lower panel.
observational geometries covered. This is likely due to the symmetry of the body meaning there is not much variation in observed light curves with changing aspects.

Following the procedure outlined by Rożek et al. (2019a), the pole search was repeated for different values of possible spin-rate change, which we hereafter call 'YORP factor', as the YORP effect is currently the best explanation for gradual changes in rotation rates which can be detected for small NEAs. The YORP factor corresponds to a linear change in a rotation rate (where the rotation rate $\omega \equiv 2 \pi / \mathrm{P}$ ) measured in $\mathrm{rad} / \mathrm{d}^{2}$. The strongest is measured YORP factor to date was $3.5 \times 10^{-6} \mathrm{rad} / \mathrm{d}^{2}$ measured for asteroid (54509) YORP (Lowry et al. 2007; Taylor et al. 2007). Notably, 54509 is the smallest object with YORP detection, relatively close to the Sun, but this value is an outlier and the other detections are for YORP factors of the order of $10^{-8} \mathrm{rad} / \mathrm{d}^{2}$, including for objects of similar diameter and orbital semimajor axis to Tantalus (as listed for example in Zegmott et al. 2021). We searched a range of possible YORP factors between -1.5 and $1.5 \times 10^{-7} \mathrm{rad} / \mathrm{d}^{2}$, and the results are illustrated in Fig. 3. There appears to be a minimum in the $\chi^{2}$ distribution corresponding to a YORP factor $2 \times 10^{-8} \mathrm{rad} / \mathrm{d}^{2}$. However, the quality of the fit for


Figure 3. The results of a combined pole and spin-state change (YORP factor) search using all available light curves are shown in the upper panel, and using a selection of light curves in the lower panel. The horizontal axis indicates the rate of change of angular rotation rate expressed in $\mathrm{rad} / \mathrm{d}^{2}$ (the YORP factor) and on the vertical axis, the quality of the fit for the best shape model developed assuming the given YORP factor. The $\chi^{2}$ differences are very small, with the green horizontal lines marking 1 per cent increase above the minimal values, and the red lines marking 5 per cent increase. The grey circle in each panel indicates the minimum $\chi^{2}$ value.
a constant-period solution is within 1 per cent increase above the lowest $\chi^{2}$ value and the light curve fits are very similar.

Fits of the synthetic light curves to the data for the best-fitting constant-period shape model are shown in Figs 4 and A2 (the spinstate solution is summarised in Table 3). The light-curve fits are not perfect. While the amplitude of the synthetic light curves generally agrees with observations, the minima and maxima are misaligned. This effect can be sometimes seen in convex shape modelling if there are issues leading to the shape of the light curve being dominated by non-shape effects related for example to observing conditions, crowding of the star field, and quality of the detector, or timing errors. We tested this hypothesis by removing the 2014 and 2017 unfiltered light curves (Warner 2015, 2017), and using the light curves marked with black circles in the 'LC-only' column of Table 1.

Dropping the subset of light curves and repeating the modelling procedure brings curious results. The rotation period is even less constrained with multiple periods having the quality of fit $\chi^{2}$
within 1 per cent of the best solution (Fig. 1). Despite having less constraint with considerable fraction of light-curves missing, the best solution is only $0.0002 h$ away from the best-fitting period obtained from the full light-curve data set, well within uncertainties in both measurements $(0.003 \mathrm{~h}$ for the full period scan and 0.07 h for restricted). Removing light curves has understandably made the pole determination even more ambiguous, but with the global minimum most likely in mid-negative ecliptic latitudes (as shown in Fig. 2), and shifts the minimum for YORP-factor search towards negative values (Fig. 3). The two YORP-factor searches give seemingly different results. However, formal uncertainties would in both cases produce overlapping error bars, encompassing constant-period, spin-up, and slow-down solutions. The best-fitting variable period solutions for either full or restricted light-curve data sets give synthetic lightcurve fits of very similar quality to the constant-period solution. We conclude a detection of any period change is not possible with the current data set using the light-curve inversion method.

The light-curve inversion produces a very symmetrical shape. Both the shape developed using the full light-curve set and a subset of light curves have a nearly circular polar projection. This is consistent with the low amplitude of light curves observed at a wide range of observing geometries. The constant-period and varying-period best-fitting solutions for the inversion of the full light-curve set are nearly identical with the same best-fitting pole (shape model is shown in Fig. 5).

## 4 RADAR MODELLING

Observations of Tantalus are not restricted to optical photometry. Another source of shape information is the set of radar observations obtained in 2017 (listed in Table 2). Those observations reveal a quite symmetrical shape with a rounded limb and almost featureless surface. In only a few of the images, for example in the middle of the highest resolution imaging sequence obtained on 2017 January 1 (illustrated in Fig. 6; subsequent nights of observations are illustrated in Figs A3-A10), some slight deformation of the asteroid can be noted. The limb of the radar echo appears asymmetrical meaning there might be an indentation, like a crater, that causes the signal to travel a longer distance to this part of the surface.

We assumed the sidereal rotation period derived from light-curve inversion as a starting point for the shape determination. This value was later refined as the model progressed. A subset of the highest quality light curves collected by us was selected (marked with a black circle in the 'LC + radar model' column of Table 1) and combined with the cw observations, and $75-$ and $150-\mathrm{m}$ resolution Dopplerdelay imaging. We performed a pole search using a $5^{\circ} \times 5^{\circ}$ grid of possible pole positions. The grid was constructed in such a way that the pole locations were evenly spaced in ecliptic latitude $\beta$, but in the longitudal dimension, $\lambda$, the search always started at $\lambda=0^{\circ}$ and subsequent points were $5^{\circ}$ as measured along a circle of latitude. At each point of the grid of possible pole positions, we used the SHAPE modelling software (Magri et al. 2007a) to optimize the ellipsoidal shape and rotation rate, keeping the pole position fixed.

The results of this pole search are illustrated in Fig. 7, similarly to Fig. 2. The outcome is a slightly better constraint on the pole position, roughly in agreement with the convex light-curve inversion. The best solution corresponds to a retrograde solution with mid-negative latitude and longitude roughly between $150^{\circ}$ and $250^{\circ}$ (the mean $\beta=-39^{\circ} \pm 16^{\circ}$ and $\lambda=190^{\circ} \pm 24^{\circ}$ ). Due to inherent ambiguity between north and south in radar imaging (the radar image is 'folded' along the line of sight, e.g. Ostro et al. 2002) there is a second, almost equally good pole solution being a mirror with respect to the ecliptic plane and shifted by $180^{\circ}$ in longitude (the mean $\beta=38^{\circ} \pm 15^{\circ}$ and


Figure 4. Example light curves collected for (2102) Tantalus. The left-hand column of images corresponding to light curve with ID 1, middle column - ID 11, and right column to ID 29 as listed in Table 1. The top row presents the data plotted over synthetic light curves generated using the 'full' constant-period light-curve inversion model (full set of synthetic light curves for this model is shown in Fig. A2). The second row includes example fits for the retrograde radar shape model (full set of light curves shown in Fig. A11). Finally, the bottom row show example fits for the prograde radar shape model (full set of light curves shown in Fig. A12).
$\lambda=11^{\circ} \pm 23^{\circ}$ ). The sidereal rotation period is consistent between the mean value for retrograde, $P=2.391 \pm 0.001 \mathrm{~h}$, and prograde, $P=2.3902 \pm 0.0006 \mathrm{~h}$, families of solutions. Similarly, the average sizes of the triaxial ellipsoid axes are consistent, with $1.2 \pm 0.3$, $1.2 \pm 0.3$, and $1.1 \pm 0.2 \mathrm{~km}$, a very slightly oblate spheroid, for both retrograde and prograde models.

For further improvement and investigation of shape details, a family of 28 pole solutions, with the $\chi^{2}$ quality of fit as illustrated in Fig. 7 within 5 per cent of the $\chi^{2}$ for best solution, were selected. For each of the selected pole positions, the ellipsoid shape model was converted from triaxial-ellipsoid description to a triangular mesh by dividing the surface of the ellipsoid into 1000 vertices collected into 1996 triangular facets. At this stage, the locations of individual vertices were optimised by shifting each individual vertex along the normal of the initial ellipsoid surface. We show the final product of this stage in Fig. 8. The spin-state parameters of the best-fitting retrograde and prograde solutions obtained after optimizing those shape models are summarized in Table 3, and shape parameters in Table 4. The average edge length for all 28 optimized models
was $76 \pm 12 \mathrm{~m}$. The average equivalent volume sphere diameter is $1.2 \pm 0.2 \mathrm{~km}$, with the diameters of an ellipsoid with the same moments of inertia being $1.2 \pm 0.2,1.2 \pm 0.2$, and $1.1 \pm 0.2 \mathrm{~km}$, so the object is essentially spherical. The only notable feature is a craterlike indentation (close to the north pole of the retrograde model, and south pole of the prograde model). This is identifiable in the plane-ofsky projections of both shape models illustrated in Fig. 6 (the feature is marked with red arrows in the radar images and blue arrows in the plane-of-sky projections). Optical light curves, as illustrated in Figs 4, A11, and A12, are not sufficiently well reproduced from either radar model to enable reliable rotational phase offset measurement, as was done for example for (68346) 2001 KZ66 (Zegmott et al. 2021). We therefore conclude that no spin-state change can be dependably detected for Tantalus.

## 5 RADAR PROPERTIES

Analysis of the cw spectra, summarized in Table 5 and shown in Fig. 9, shows some discrepancy between prograde and retrograde


Figure 5. Projections of the convex inversion shape model developed using the full light-curve data set. The XYZ-axes are aligned with the body principal moments of inertia. The units are arbitrarily selected so that the radius along the $x$-axis is 1 . The flat face visible from the positive end of the $y$-axis is an artefact of the modelling method. The presented shape model corresponds to the best-fitting constant-period solution with $\lambda=210^{\circ}$ and $\beta=-30^{\circ}$. The best-fitting variable-period solution with $v=2 \times 10^{-8} \mathrm{rad} / \mathrm{d}^{2}$ has the same pole position and the shape is indistinguishable from the constant-period solution.
models due to the difference in subradar latitude between the assumed poles and the radar line of sight, and the uncertainty in size determination. The best-fitting prograde model is 230,150 , and $180-$ $m$ larger than the retrograde along each dimension. As a result of that, the radar albedo ( $\hat{\sigma}_{\mathrm{OC}}$ ) measurements are systematically lower for the prograde model. The values, $\hat{\sigma}_{\mathrm{OC}}=0.20 \pm 0.05$ for the retrograde model and $0.15 \pm 0.04$ for prograde, are still consistent and agree with typical values determined for radar-observed S-type main-belt asteroids, which is $\hat{\sigma}_{O C}=0.14 \pm 0.04$ (Magri et al. 2007b). If we use equations in Shepard et al. (2008, 2010, 2015), $\hat{\sigma}_{\text {OC }}$ would correspond to near-surface bulk densities between 2000 and $3100 \mathrm{~kg} \mathrm{~m}^{-3}$ for the retrograde model and 1800 to $2600 \mathrm{~kg} \mathrm{~m}^{-3}$ for prograde, which lie within the values expected for S-type asteroids (Carry 2012).

The ratio of the same circular polarisation as the emitted signal (SC) to the opposite circular polarization (OC) detected for the object is $\mu_{\mathrm{C}}=0.19 \pm 0.06$. This measurement is based on the calibrated radar echo and is independent of shape information. This value is consistent with the typical $\mu_{\mathrm{C}}=0.270 \pm 0.079$ for S-type nearEarth objects (Benner et al. 2008), albeit at the lower limit. The polarisation ratio is a zeroth-order gauge to the surface roughness to the extent that zero means a smooth surface in the wavelength scale ( 13 cm for Arecibo), but beyond that it's not a linear scale of surface roughness because it's affected by different factors, such as the permittivity and particle-size frequency distribution in the nearsurface (Virkki \& Muinonen 2016). The $\mu_{\mathrm{C}}$ for Tantalus is highest on January 5, and lowest on January 1, when the asteroid is viewed from almost opposite directions. Incidentally, the radar albedo is lowest on January 5 and highest on the 1 . This might mean that there is some variation of surface material on Tantalus. One side would have a smoother, radar-reflective, so less porous, surface which could be exposed rock. On the other side, there could be a rough, radar-dark patch, perhaps a crater filled with fine-grained regolith (mapping of measured $\hat{\sigma}_{O C}$ and $\mu_{C}$ on the asteroid surface is presented in Fig. 10).


Figure 6. Comparison between best-fitting retrograde (first three columns) and prograde (last three columns) radar shape models of (2102) Tantalus and radar images (each row corresponds to the same radar image). The radar images were taken with Arecibo between 23:34 UTC on 2017 January 1 and 00:27 UTC on 2017 January 2. Subsequent nights of observations are illustrated in Figs A3-A10. Each three-image sub-panel is made of the observational data ('data'), echo simulated from the radar model ('fit'), and plane-of-sky projection of the radar model ('sky'). On the data and synthetic-echo images, the delay increases downwards and the frequency (Doppler) to the right. The plane-of-sky images are orientated with celestial north (in an equatorial coordinate system) to the top and east to the left. The principal axes of inertia are marked with coloured rods (red for axis of minimum inertia, green for intermediate axis), and the rotation vector ( $z$-axis of body-fixed coordinate system, roughly aligned with the axis of maximum inertia) is marked with a purple arrow. Note the rotation axis and $z$-axis of the body overlap with the axis of maximum inertia. Red arrows in selected images indicate asymmetry in the radar limb of the object, possibly corresponding to a surface indentation. The corresponding crater-like feature is marked with blue arrows in the plane-of-sky projections.


Figure 7. Similar to Fig. 2, but for a constant period pole search using an ellipsoid model and a combination of radar and light-curve data. Darker colours indicate lower $\chi^{2}$ values, and the lines mark gradual increases over the minimum $\chi^{2}$ value, with solid line for 1 per cent increase, dotted line for 5 per cent, and a dashed line for 10 per cent. Models with $\chi^{2}$ values smaller than 5 per cent above the minimum were selected for further improvement. The shape models were translated to the vertex representation and optimized using a combination of radar and light-curve data.

Table 3. Summary of spin-state parameters for (2102) Tantalus from lightcurve inversion and radar modelling. The presented sets of parameters correspond to the best-fitting solutions from two approaches to shape modelling; in the 'Light-curve' column for the output of full convex-light-curve inversion, and in the 'Radar retrograde' and 'prograde' columns for a result of a global shape modelling that included both the radar and light-curve data. The table lists the ecliptic coordinates of the rotation pole, longitude $(\lambda)$, and latitude $(\beta)$, with associated uncertainties $\left(\Delta_{\lambda}\right.$ and $\left.\Delta_{\beta}\right)$, the model epoch $\left(T_{0}\right)$, the sidereal rotation period $(P)$ with uncertainty $\left(\Delta_{P}\right)$. The uncertainties in pole and period are given as the standard deviation of the models within a 10 per cent increase of the minimum $\chi^{2}$ value (calculated from the ellipsoid models for the radar models).

| Parameter | Light-curve | Radar retrograde | Radar prograde |
| :--- | :---: | :---: | :---: |
| $\lambda$ | $210^{\circ}$ | $180^{\circ}$ | $36^{\circ}$ |
| $\Delta_{\lambda}$ | $41^{\circ}$ | $24^{\circ}$ | $23^{\circ}$ |
| $\beta$ | $-30^{\circ}$ | $-30^{\circ}$ | $30^{\circ}$ |
| $\Delta_{\beta}$ | $35^{\circ}$ | $16^{\circ}$ | $15^{\circ}$ |
| $T_{0}(\mathrm{JD})$ | 2449695.50000 | 2457754.49022 | 2457754.38451 |
| $P(\mathrm{~h})$ | 2.385 | 2.391 | 2.3901 |
| $\Delta_{P}(\mathrm{~h})$ | 0.003 | 0.001 | 0.0006 |

Interestingly, the cw spectrum collected on the January 5 also shows bifurcation, which is a characteristic shape of the cw spectrum for contact binary objects. However, it is very clear from the images that the object is symmetrical and the dip in echo power is only at about 25 per cent level, rather than 50-100 per cent level typical for a contact binary. Similar bifurcation of radar echo was recently noted for (16) Psyche and attributed to a possible radardark spot surrounded by regions of higher albedo (Shepard et al. 2021). This explanation seems sensible as the same cw spectrum produced overall lowest value of $\hat{\sigma}_{\text {OC }}$ for Tantalus, suggesting less radar-reflective material. However, this particular cw spectrum also appears to be the noisiest, and we noted significant pointing errors in acquiring this observation. A cw spectrum taken on January 6 comes from a similar location on the surface but has a higher albedo and does not appear bifurcated, so we conclude there is insufficient evidence
to claim that there is in fact a radar-dark spot on the surface in the specific location corresponding to the cw spectrum taken on January 5. Still, the whole region probed between January 4 and 7 appears less reflective in radar wavelengths than the other side of the asteroid, corresponding to the spectrum from January 1 . On the other hand, the spectrum from January 1 is isolated, with no nearby measurement to confirm the high albedo, so further observations are needed to confirm the surface variation.

It might be worth considering here how a less radar-reflective spot would affect the optical light curves as the light-curve inversion method assumed uniform optical albedo. Radio signal penetrates the surface, so the radar albedo carries information about the physical properties of the top layer of material on a small body at the scale of the radar wavelength (e.g. Virkki \& Muinonen 2016), while optical light operates at much shorter wavelengths. In fact, analysis of a sample of radar-observed main-belt asteroids shows no correlation between radar and optical albedos for S-types (Magri et al. 2007b). While there is some mismatch between the synthetic light curves generated from the radar shape model and the data collected, it is mostly in the rotation phase and not in the light-curve amplitude. A considerably darker spot on an otherwise symmetrical body would produce a dip in the asteroid brightness, but this is not evident in the data. Therefore, we conclude there is no convincing evidence of an optically dark spot.

## 6 THERMOPHYSICAL ANALYSIS

To ascertain the preferred shape model solution of Tantalus, and its thermophysical properties, we modelled and fitted the infrared observations of Tantalus that were serendipitously acquired by Wide-field Infrared Survey Explorer ( WISE) during its cryogenic operations in 2010 ( Table 6; Mainzer et al. 2011). Additional observations were also acquired in 2014, 2016, 2017, and 2020 (Masiero et al. 2017, 2020), but we did not include these data sets in our analyses because they were obtained during the non-cryogenic phase of the mission where reflected sunlight contributed significantly to the available near-infrared data. To retrieve the WISE data, the detections of Tantalus reported in the Minor Planet Center (MPC) database were used to query the WISE All-Sky Singe Exposure (L1b) source database via the NASA/IPAC Infrared Service Archive. Following Rozitis et al. (2018), the queries were performed in the moving object search mode with a match radius of 5 arcsec for the range of dates provided by the MPC. The resulting detections were only kept in the instances where the measured flux levels of Tantalus were at the $3 \sigma$ level or greater in both the W3 $(11.1 \mu \mathrm{~m})$ and $\mathrm{W} 4(22.6 \mu \mathrm{~m})$ channels, and when the measured positions were within 1 arcsec of the predicted positions. The retrieved WISE magnitudes were converted to fluxes by accounting for the red-blue calibrator discrepancy reported by Wright et al. (2010), and additional uncertainties of 4.5 and 5.7 per cent were added in quadrature to the retrieved uncertainties in the W3 and W4 channels, respectively, to account for other calibration issues (Jarrett et al. 2011). Finally, colour corrections were performed on the model fluxes, rather than the observed fluxes, using the WISE corrections provided by Wright et al. (2010). This resulted in 33 W3 and 33 W4 usable flux measurements on 2010 June 16-20, and 74 W 3 and 74 W 4 flux measurements on 2010 July 4-19 (Table 6).

Thermophysical modelling was performed using the Advanced Thermophysical Model (ATPM; Rozitis \& Green 2011, 2012, 2013) in combination with the light-curve- and radar-derived shape models of Tantalus. For a given shape model, the ATPM computes its surface temperature distribution by solving the 1D heat conduction


Figure 8. Same as Fig. 5 but for the non-convex shape models developed with a subset of optical light curves and the radar data. The six panels, on the left-hand side, illustrate the best-fitting retrograde model with $\lambda=180^{\circ}$ and $\beta=-30^{\circ}$. The panels, on the right-hand side, illustrate the best prograde solution with $\lambda=$ $36^{\circ}$ and $\beta=30^{\circ}$. The difference in quality of fit of artificial light curves and radar echos to data between the two models is negligible.

Table 5. Radar-derived disc-integrated properties for the cw spectra of (2102) Tantalus. 'UT Date' (in 'year-month-day' format) and 'UT Time' (in 'hours:minutes:seconds' format) is the universal-time date and time mid-receive. The body-fixed longitude, ' $\lambda_{B}$ ', and latitude, ' $\beta_{B}$ ', of the radar line-ofsight, and rotation phase, ' $\varphi$ ', were determined using the spin-state for two radar shape models (see Table 4). The rotation phase is measured in degrees as an offset of $x$-axis relative to its position at $T_{0}$. The radar cross-sections ( ' $\sigma_{\mathrm{OC}}$ ' column) were calculated from the OC power spectra. The 'Projected areas' and radar OC albedos (' $\hat{\sigma}_{\mathrm{OC}}$ ') were derived using the 3 D shape of either of the two models. The $\mathrm{SC} / \mathrm{OC}$ ratio (' $\mu_{C}$ ') for each spectrum is also given. In the last row, we list the means and standard deviations of OC albedos and SC/OC ratio. We note the difference in the mean radar albedo determination is primarily due to the size difference between the retrograde and prograde models.

| UT Date | UT Time | $\begin{aligned} & \lambda_{\mathrm{B}} \\ & \left({ }^{\circ}\right) \end{aligned}$ | Retrograde model |  |  |  | $\hat{\sigma}_{\text {OC }}$ | Prograde model |  |  |  |  | $\hat{\sigma}_{\text {OC }}$ | $\mu_{C}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & \beta_{\mathrm{B}} \\ & \left({ }^{\circ}\right) \end{aligned}$ | $\begin{gathered} \varphi \\ \left({ }^{\circ}\right) \end{gathered}$ | $\begin{gathered} \sigma_{\mathrm{OC}} \\ \left(\mathrm{~km}^{2}\right) \end{gathered}$ | $\begin{gathered} \text { Area } \\ \left(\mathrm{km}^{2}\right) \end{gathered}$ |  | $\begin{aligned} & \lambda_{B} \\ & \left({ }^{\circ}\right) \end{aligned}$ | $\begin{aligned} & \beta_{B} \\ & \left({ }^{\circ}\right) \end{aligned}$ | $\varphi$ $\left({ }^{\circ}\right)$ | $\begin{gathered} \sigma_{\mathrm{OC}} \\ \left(\mathrm{~km}^{2}\right) \end{gathered}$ | $\begin{gathered} \text { Area } \\ \left(\mathrm{km}^{2}\right) \end{gathered}$ |  |  |
| 2017-01-01 | 22:56:30 | 182 | 44 | 178 | 0.370 | 1.300 | 0.284 | 254 | -52 | 106 | 0.371 | 1.733 | 0.214 | $0.103 \pm 0.011$ |
| 2017-01-04 | 21:33:13 | 339 | 61 | 21 | 0.234 | 1.326 | 0.177 | 36 | -66 | 324 | 0.229 | 1.751 | 0.131 | $0.202 \pm 0.022$ |
| 2017-01-05 | 21:08:24 | 22 | 65 | 338 | 0.181 | 1.320 | 0.137 | 74 | -69 | 286 | 0.181 | 1.755 | 0.103 | $0.287 \pm 0.043$ |
| 2017-01-06 | 21:06:11 | 8 | 69 | 352 | 0.233 | 1.322 | 0.176 | 54 | -71 | 306 | 0.234 | 1.756 | 0.133 | $0.148 \pm 0.028$ |
| 2017-01-07 | 21:10:50 | 336 | 71 | 24 | 0.279 | 1.325 | 0.211 | 16 | -73 | 344 | 0.287 | 1.757 | 0.163 | $0.202 \pm 0.003$ |
| Mean values: $0.20 \pm 0.05$ |  |  |  |  |  |  |  |  |  |  |  |  | $0.15 \pm 0.04$ | $0.19 \pm 0.06$ |

equation for each triangular facet with a surface boundary condition that accounts for direct solar illumination, shadowing, multiple scattered sunlight, and self-heating from thermal re-emission. The effects of rough surface thermal-infrared beaming (i.e. thermal redirection of absorbed sunlight back towards the Sun) are incorporated by the fractional addition of hemispherical craters that represent the unresolved surface roughness. Surface temperatures were computed for thermal inertia ranging from 0 to $1000 \mathrm{~J} \mathrm{~m}^{-2} \mathrm{~K}^{-1} \mathrm{~s}^{-1 / 2}$ in steps of $10 \mathrm{~J} \mathrm{~m}^{-2} \mathrm{~K}^{-1} \mathrm{~s}^{-1 / 2}$ for the observational geometries given in Table 6 assuming an emissivity of 0.9 and a Bond albedo of 0.15 (i.e. calculated using an H of 16.0 and a G of 0.15 with the radarderived diameter; Rozitis et al. 2013). The predicted model fluxes were then calculated as a function of wavelength, thermal inertia, roughness fraction, and rotation phase by applying and summing the Planck function across all facets that were visible to the observer at the instances of the observations. Finally, $\chi^{2}$-minimization was performed between the data and thermophysical models using the rotational averaging technique described in Rozitis et al. (2018) to obtain the best-fitting diameter, thermal inertia, and roughness fraction for each possible shape model of Tantalus.

Fig. 11 and Table 7 summarize the resulting thermophysical fits and properties, respectively, for the three different shape models of Tantalus tested. As indicated, the thermophysical fits did not
prefer one shape model over the others based purely on their derived $\chi^{2}$ values, but only the radar prograde shape model produced a radiometric diameter that was consistent with its radarderived diameter within the uncertainties (Table 7). Therefore, we concluded that the prograde sense of rotation was the most likely orientation for Tantalus. The preferred solution had a thermal inertia of $270 \pm 80 \mathrm{~J} \mathrm{~m}^{-2} \mathrm{~K}^{-1} \mathrm{~s}^{-1 / 2}$, which was rather typical for a kilometre-sized NEA (i.e. $\sim 200 \mathrm{~J} \mathrm{~m}^{-2} \mathrm{~K}^{-1} \mathrm{~s}^{-1 / 2}$; Delbo' et al. 2007; Delbo et al. 2015). It also had a low roughness fraction of $0.13 \pm 0.09$, equivalent to $16^{\circ} \pm 7^{\circ}$ RMS slope, which was consistent with its slightly lower than average radar circular polarization ratio (i.e. another qualitative measure of surface roughness). Additionally, the uniform thermal light curves are shown in Figs 11(a) and (b) indicated that no large hemispherical differences in thermal inertia or roughness were present on Tantalus's surface.

Our derived thermal inertia value was about half that of $670 \pm$ $240 \mathrm{~J} \mathrm{~m}^{-2} \mathrm{~K}^{-1} \mathrm{~s}^{-1 / 2}$ obtained by Koren, Wright \& Mainzer (2015), who used a similar subset of WISE data. However, the rotation period of Tantalus was not well constrained at the time of their work, and thus Koren et al. (2015) allowed it to vary between 2 and 24 h in their thermophysical model. Therefore, their obtained thermal inertia value was centred on a median rotation period of 13 h . If we scale


Figure 9. The cw observations of (2102) Tantalus were collected in January 2017 at Arecibo. The disc-integrated properties of Tantalus based on the cw spectra are gathered in Table 5. The signal is recorded in two channels, with the same circular (SC) polarization as the transmitted radiation marked with a dashed line in each panel, and the opposite circular (OC) polarization, marked with a solid line. The spectra show SC/OC ratios typical for an S-type NEA.


Figure 10. A map of radar albedo ( $\sigma_{\mathrm{OC}}$, upper plot) and circular polarization ratio $\left(\mu_{\mathrm{C}}\right)$ for (2102) Tantalus based on cw measurements. The figure is a visualization of measurements listed in Table 5 with the darker colour in each plot corresponding to lower values of $\sigma_{\mathrm{OC}}$ or $\mu_{\mathrm{C}}$, and lighter to higher. The size of the spots of colour is arbitrary. Each plot is divided in two as measurements for the retrograde model were made in the Northern hemisphere in body-centric coordinates (upper half of both plots), and in the Southern hemisphere for the prograde model (lower half).

Table 4. Summary of shape parameters for asteroid (2102) Tantalus for the best-fitting 'retrograde' and 'prograde' shape models developed from combined radar and light-curve data. The extents are measured along the body-fixed coordinate system axis rather than the principal axis of inertia. The $D_{\text {eq }}$ is the diameter of a sphere with volume equivalent to the model volume. The DEEVE stands for the dynamically equivalent equal-volume ellipsoid and ' 2 a ', ' 2 b ', and ' 2 c ' are its diameters.

| Parameter | Retrograde | Prograde |
| :--- | :---: | :---: |
| Extent along $x$-axis $(\mathrm{km})$ | 1.3 | 1.5 |
| $y$-axis $(\mathrm{km})$ | 1.3 | 1.5 |
| $z$-axis $(\mathrm{km})$ | 1.2 | 1.4 |
| Surface area $\left(\mathrm{km}^{2}\right)$ | 5.13 | 6.78 |
| ${\text { Volume }\left(\mathrm{km}^{3}\right)}^{\mathrm{D}_{\text {eq }}(\mathrm{km})}$ | 1.05 | 1.58 |
| DEEVE diameter 2a $(\mathrm{km})$ | 1.3 | 1.5 |
| 2b $(\mathrm{km})$ | 1.3 | 1.5 |
| 2c $(\mathrm{km})$ | 1.3 | 1.5 |

Table 6. Observational geometry was used in the thermophysical modelling of (2102) Tantalus. For each set of dates in 2010 (column 'Dates') the following information is given: number of measurements in WISE W3 and W4 channels ('No. W3' and 'No. W4', respectively), heliocentric distance (' $R_{\mathrm{h}}$ '), heliocentric longitude (' $\lambda$ ') and latitude (' $\beta$ '), observer distance ( ${ }^{\prime} \Delta$ '), and observer longitude ( ${ }^{~} \lambda_{o}$ ') and latitude ( ${ }^{\prime} \beta_{o}$ ').

| Dates <br> $(\mathrm{dd} / \mathrm{mm})$ | No. <br> W 3 | No. <br> W 4 | $R_{h}$ <br> $(\mathrm{au})$ | $\lambda$ <br> $\left({ }^{\circ}\right)$ | $\beta$ <br> $\left({ }^{\circ}\right)$ | $\Delta$ <br> $(\mathrm{au})$ | $\lambda_{o}$ <br> $\left({ }^{\circ}\right)$ | $\beta_{o}$ <br> $\left({ }^{\circ}\right)$ |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $16-20 / 06$ | 33 | 33 | 1.657 | 300.8 | -42.4 | 1.308 | 356.9 | -58.6 |
| $4-19 / 07$ | 74 | 74 | 1.673 | 308.9 | -49.2 | 1.322 | 17.7 | -73.6 |

their thermal inertia value by $(2.39 / 13)^{0.5}$ to ensure that the nondimensional thermal parameter is conserved, then a corrected thermal


Figure 11. Thermophysical modelling of the WISE data of (2102) Tantalus. The thermal light curves of Tantalus obtained by WISE on 2010 June 16-20 and 2010 July 4-19 are given in Panels (a) and (b), respectively. Here, the W3 and W4 channel data points are given by the asterisks and circles, respectively, which have been rotationally phased relative to the first data point assuming a rotation period of 2.39 h . The solid (W3) and dashed (W4) lines give the best model fits for the three shape models tested after rotational averaging. Panel (c) gives contours in $\chi^{2}$ of $1 \sigma$ (thick lines) and $3 \sigma$ (thin lines) confidence level in derived thermal inertia and roughness fraction for the three shape models tested. Finally, Panel (d) shows the normalized frequency distributions of acceptable thermal inertia values contained within the $3 \sigma$ confidence level $\chi^{2}$ contours.

Table 7. Derived thermophysical properties for the three different shape models of (2102) Tantalus: the full light-curve-inversion model ('Lightcurve'), and the retrograde and prograde radar models.

| Shape model | Light-curve | Radar <br> retrograde | Radar <br> prograde |
| :--- | :---: | :---: | :---: |
| Reduced $\chi^{2}$ | 1.1 | 1.0 | 1.1 |
| Radar diameter $(\mathrm{km})$ | - | $1.26 \pm 0.20$ | $1.45 \pm 0.20$ |
| Radiometric diameter $(\mathrm{km})$ | $1.68 \pm 0.05$ | $1.66 \pm 0.05$ | $1.57 \pm 0.05$ |
| Geometric albedo | $0.25 \pm 0.01$ | $0.26 \pm 0.01$ | $0.29 \pm 0.02$ |
| Thermal inertia $\left(\mathrm{J} \mathrm{m}^{-2} \mathrm{~K}^{-1} \mathrm{~s}^{-1 / 2}\right)$ | $100 \pm 20$ | $110 \pm 30$ | $270 \pm 80$ |
| Roughness fraction | $0.12 \pm 0.09$ | $0.49 \pm 0.29$ | $0.13 \pm 0.09$ |

inertia of $\sim 290 \mathrm{~J} \mathrm{~m}^{-2} \mathrm{~K}^{-1} \mathrm{~s}^{-1 / 2}$ is obtained, which is consistent with our value.

Traditionally, asteroid thermal inertia values have been interpreted in terms of regolith grain size (e.g. Gundlach \& Blum 2013) but the recent Hayabusa2 and OSIRIS-REx missions have demonstrated that rock porosity can also dictate the thermal inertia for some asteroids (Okada et al. 2020; Rozitis et al. 2020). Therefore, Tantalus's moderately low thermal inertia value could either imply the presence of mm - to cm -sized regolith grains or highly porous rocks. However, Cambioni et al. (2021) suggest that the grain size interpretation is appropriate for S-type asteroids, such as Tantalus, because they are expected to produce more fine-grained regolith from impact cratering and thermal fracturing than other spectral types. Interestingly, this would imply that Tantalus's surface is dominated by small grains despite its relatively fast spin-rate.

## 7 GEOPHYSICAL ANALYSIS

To investigate the spin-stability of Tantalus, we applied several geophysical analyses to the prograde shape model that was preferred by the combined analysis of the radar and infrared data. In particular,


Figure 12. Geophysical analysis of Tantalus. Panel (a) - gravitational slopes computed with the radar prograde shape model assuming a bulk density of $2000 \mathrm{~kg} \mathrm{~m}^{-3}$. Panel (b) - same as Panel (a) but for gravitational potential. Panel (c) - areal distribution of gravitational slope computed for three different values of bulk density. Panel (d) - topographic variation in gravitational potential as a function of scaled spin, i.e. $\omega /(G \pi \rho)^{0.5}$. The current topographic variation of Tantalus is identified for three different values of bulk density. Panel (e) - fractional area experiencing negative effective gravity as a function of bulk density. The bulk density range for an S-type rubble-pile asteroid is shown for comparison. Panel (f) - minimum cohesive strength required to prevent the rotational breakup of Tantalus as a function of bulk density. The different lines show the cohesive strengths required for different assumed values of the angle of friction.
we applied a polyhedron gravity field model modified for rotational centrifugal forces (Werner \& Scheeres 1997; Rozitis, Maclennan \& Emery 2014) to determine the gravitational slopes, gravitational potential, and topographic variation (i.e. the relative standard deviation of gravitational potential variations across the surface of the asteroid; Richardson \& Bowling 2014; Richardson et al. 2019) of Tantalus as a function of bulk density (Fig. 12). Additionally, we also applied the Drucker-Prager failure criterion (Holsapple 2007) to determine if structural cohesive forces are required to prevent the rotational breakup of Tantalus (Fig. 12f). For these calculations, the appropriate bulk density range for Tantalus was 1500 to $2500 \mathrm{~kg} \mathrm{~m}^{-3}$ given that it is likely to be an S-type rubble-pile asteroid (Carry 2012) which happens to be consistent with that inferred previously from the radar albedo measurements.

As shown in Figs 12(a) and (b), there was a strong dependence of gravitational slope and potential with latitude because of Tantalus's fast spin-rate. Some slopes on the equator are greater than $90^{\circ}$ at the lower end of the bulk density range where centrifugal forces exceed its self-gravity (Fig. 12c), and there are also large topographic variations regardless of the precise bulk density value (Fig. 12d). The geophysical analysis is more sensitive to the large-scale shape features rather than the small-scale topography. The small-scale features produce the small 'spikes' seen in Fig. 12c, but they do not strongly influence the overall slope distributions. A minimum
bulk density of $\sim 2200 \mathrm{~kg} \mathrm{~m}^{-3}$ is required to prevent surface mass shedding (Fig. 12e), and a cohesive strength of up to $\sim 45 \mathrm{~Pa}$ is required to prevent structural failure depending on the assumed angle of friction (Fig. 12f). Therefore, Tantalus could be exceeding its critical spin-rate via cohesive forces like the rapidly spinning NEAs (29075) 1950 DA (Rozitis et al. 2014).

If Tantalus is exceeding its critical spin-rate, then it would be expected to undergo frequent landslide and mass shedding events (Scheeres 2015). Although not conclusive, the possible variations in radar surface properties noted previously could be evidence of a past landslide and/or shedding event. Additionally, Tantalus has historically been classified as a Q-type asteroid (Bus \& Binzel 2002), which has traditionally been interpreted as exposure of fresh unweathered material by a recent re-surfacing event (Binzel et al. 2010). Theoretical modelling of various space weathering processes has demonstrated that re-surfacing of asteroids by YORP spin-up could be a significant mechanism for producing Q-types in the near-Earth asteroid population (Graves et al. 2018). However, the most recent spectrum of Tantalus indicates an Sr-type classification (Thomas et al. 2014), and therefore it is possible that only parts of Tantalus's surface, if any, have undergone recent re-surfacing.

## 8 CONCLUSIONS

The asteroid (2102) Tantalus has a very symmetrical shape. Shape modelling using standard methods applied to radar data and optical light curves have shown no sign of an equatorial bulge typical for fast-spinning NEAs, but rather an almost spherical object, which is consistent with rotationally driven evolution of a body with low effective friction angle (Sugiura et al. 2021). The radar imaging indicates a crater-like feature close to one of the poles. The radar pole search shows two families of possible pole solutions, but with no clear preference for either based on the available optical and radar data. Including thermophysical analysis based on WISE data, we were able to constrain this to prograde rotation.

Surface properties of Tantalus are rather typical for an S-class object. Combined radar and thermophysical analysis suggest a surface covered in low-porosity fine-grained regolith. There is an indication of differentiation across the surface of Tantalus in radar spectra, but the spectrum showing the highest radar albedo and lowest $\mu_{C}$ (which indicates a more solid surface) is isolated. Additional data would be needed to confirm that this is not just an anomalous measurement. The cw radar spectrum showing the lowest albedo and highest $\mu_{\mathrm{C}}$, when combined with the peculiar shape of this spectrum might indicate a very localized rough radar-dark spot, like a rock-filled crater, surrounded by more reflective material. However, this conclusion is only tentative due to low SNR for this particular spectrum and inconsistency with albedo measurements made at similar locations on the surface.

Our analysis of optical light curves shows that caution should be advised when searching for signatures of period change using low-amplitude and low-S/N light curves. A detailed search shows a preference for slow-down of rotation for the whole available data set and excluding some of the data coming from the smaller telescopes produced a slightly better fit for a rotational spin-up. However, with the level of analysis applied here, we do not yet firmly conclude that we are seeing an actual spin-change for Tantalus. Close inspection of synthetic light curves generated with the radar shape model combined with the available light-curve data shows that the uncertainty in rotational phase determination might be driving the ambiguity in the spin-rate change estimates. Additionally, our mod-
elling indicated retrograde rotation from light-curve inversion alone. However, to reach an agreement between radar and thermophysical effective diameter determination, prograde rotation was preferred. Therefore, care should be taken when determining pole orientation for symmetrical objects from light curves alone.

Earlier photometric studies suggested a presence of a $16 \mathrm{~h}-$ rotation-period satellite (Warner 2015, 2017; Vaduvescu et al. 2017). That periodicity is not apparent in the full light-curve data set. Furthermore, the radar data show no sign of a companion larger than 75 m . With a primary diameter of 1.3 km , the difference in photometric signal from a secondary of diameter 75 m would be 0.0036 magnitudes. This cannot explain the light curve effects observed.

The radar-derived shape models of Tantalus are consistent with radar observations, however all three presented models demonstrate issues with fits to the optical data. When it comes to the lightcurve inversion model this might be due to the convex model's limitations; from radar observations, we know that there is a craterlike feature on the surface that would not be reproduced by convex inversion. Meanwhile, the radar modelling procedure can overfit for the noise in radar data, producing bump-like artefacts in the 3D model. These might cast shadows producing mismatch with optical light curves. Some of the light-curve effects might be also due to albedo variegation, which is possible given the variation suggested by analysis of radar-derived surface properties, but not very well constrained with presented data.

Tantalus makes a much closer approach to Earth in December 2038, coming at about 0.044 au , as compared to the December 2016 approach when its minimum distance from Earth was 0.137 au. It would be useful to obtain additional measurements of surface properties using planetary radar to confirm any surface variation during that approach. A smaller geocentric distance means a higher S/N for the radar echo and would provide an opportunity to investigate the surface topography in more detail, for example, to confirm the presence of any surface craters. Sadly, the Arecibo telescope used to obtain the results presented here collapsed on 2020 December 1 , considerably reducing observational capabilities in the planetary radar domain. Hopefully, the Goldstone Solar System Radar facility along with alternative instrumentation (to be commissioned) can be used for continued detailed characterization of NEAs.

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## DATA AVAILABILITY

The light-curve data published by Pravec et al. (1997) are publicly available from NASA Planetary Data System at https://sbnapps. psi.edu/ferret/datasetDetail.action?dataSetId = EAR-A-3-RDR-NE O-light-curveS-V1.1. The light-curve data published by Warner (2015) and Warner (2017) are publicly available at the Asteroid light-curve Photometry Database (Warner, Harris \& Pravec 2009), accessible through http://alcdef.org/. The light-curve data first published here can be accessed in an online Table A1 available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via http://cdsarc.u-strasbg.fr/viz-bin/cat/J/MNRAS. The shape models discussed here can be downloaded from the Database of Asteroid Models from Inversion Techniques (DAMIT) accessible through https://astro.troja.mff.cuni.cz/projects/damit/. The radar CW data are available online at https://www.lpi.usra.edu/resources/asteroids/aster oid/?asteroid_id $=1975 \mathrm{YA}$ and the radar imaging data are available from the authors upon request. The WISE infra-red data are available throug the NASA/IPAC Infrared Science Archive, which can be accessed at https://irsa.ipac.caltech.edu/Missions/wise.html.

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## SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.
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[^1]${ }^{13}$ Universität Hamburg, Faculty of Mathematics, Informatics and Natural Sciences, Department of Earth Sciences, Meteorological Institute, Bundesstraße 55, D-20146 Hamburg, Germany
${ }^{14}$ University of St Andrews, Centre for Exoplanet Science, SUPA School of Physics \& Astronomy, North Haugh, St Andrews, KY16 9SS, UK
${ }^{15}$ Facultad de Ingeniería y Tecnología, Universidad San Sebastian, General Lagos 1163, Valdivia 5110693, Chile
${ }^{16}$ Nicolaus Copernicus University, Institute of Astronomy, ul. Grudziadzka 5, PL-87-100 Torun, Poland
${ }^{17}$ Chungnam National University, Department of Astronomy, Space Science and Geology, 34134 Daejeon, South Korea
${ }^{18}$ Astronomisches Rechen-Institut, Zentrum für Astronomie der Universität Heidelberg (ZAH), D-69120 Heidelberg, Germany
${ }^{19}$ Centre for ExoLife Sciences, Niels Bohr Institute, University of Copenhagen, Øster Voldgade 5, DK-1350 Copenhagen, Denmark
${ }^{20}$ Centro de Astronomía, Universidad de Antofagasta, Av. Angamos 601 Antofagasta, Chile
${ }^{21}$ Departamento de Matemática y Física Aplicadas, Facultad de Ingeniería, Universidad Católica de la Santísima Concepción, Alonso de Rivera 2850 Concepción, Chile
${ }^{22}$ Department of Physics, Sharif University of Technology, PO Box 111559161 Tehran, Iran
${ }^{23}$ Centre for Electronic Imaging, School of Physical Sciences, The Open University, Milton Keynes MK7 6AA, UK
${ }^{24}$ Astrophysics Group, Keele University, Staffordshire ST5 5BG, UK
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[^1]:    ${ }^{1}$ Institute for Astronomy, University of Edinburgh, Royal Observatory, Edinburgh EH9 3HJ, UK
    ${ }^{2}$ School of Physical Sciences, University of Kent, Ingram Building, Canterbury CT2 7NH, UK
    ${ }^{3}$ School of Physical Sciences, The Open University, Milton Keynes MK7 6AA, UK
    ${ }^{4}$ Arecibo Observatory, Universities Space Research Association, HC 3 Box 53995, Arecibo, PR 00612, Puerto Rico, USA
    ${ }^{5}$ National Radio Astronomy Observatory, 1180 Boxwood Estate Rd., Charlottesville, VA 22903, USA
    ${ }^{6}$ Green Bank Observatory, P.O. Box 2, Green Bank, WV 24494, USA
    ${ }^{7}$ Department of Physics, University of Helsinki, Gustaf Hällströmin katu 2, FI-00560, Helsinki, Finland
    ${ }^{8}$ Astrophysics Research Centre, Queens University Belfast, Belfast BT7 1NN, UK
    ${ }^{9}$ SUPA, School of Science and Engineering, University of Dundee, Dundee DD1 4HN, UK
    ${ }^{10}$ Department of Physics, Isfahan University of Technology, Isfahan 8415683111, Iran
    ${ }^{11}$ Dipartimento di Fisica 'E.R. Caianiello', Università di Salerno, Via Giovanni Paolo II 132, I-84084 Fisciano, Italy
    ${ }^{12}$ Istituto Nazionale di Fisica Nucleare, Sezione di Napoli, Strada Comunale Cinthia, I-80126 Napoli, Italy

