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Measurement of the 1S_0 neutron-neutron effective range in neutron-deuteron breakup

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ABSTRACT

We report the most precise determination of the 1S_0 neutron-neutron effective range parameter (r_{nn}) from neutron-neutron quasifree scattering in neutron-deuteron breakup. The experiment setup utilized a collimated beam of 15.5 MeV neutrons and an array of eight neutron detectors positioned at angles sensitive to several quasifree scattering kinematic configurations. The two neutrons emitted from the breakup reaction were detected in coincidence and time-of-flight techniques were used to determine their energies. The beam-target luminosity was measured in-situ with the yields from neutron-deuteron elastic scattering. Rigorous Faddeev-type calculations using the CD Bonn nucleon-nucleon potential were fit to our cross-section data to determine the value of r_{nn} . The analysis was repeated using a semilocal momentum-space regularized N^4LO^+ chiral interaction potential. We obtained values of $r_{nn} = 2.86 \pm 0.01$ (stat) ± 0.10 (sys) fm and $r_{nn} = 2.87 \pm 0.01$ (stat) ± 0.10 (sys) fm using the CD Bonn and N^4LO^+ potentials, respectively. Our results are consistent with charge symmetry and previously reported values of r_{nn} .

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Since the discovery of the neutron [1,2], much effort has been devoted to characterizing the properties of nuclei based on the interactions of their constituent nucleons. Due to the technical challenges associated with quantum chromodynamics, interactions between individual nucleons are described by effective theories [3]. Modern nucleon-nucleon (NN) phenomenological potential models [4,5], one-boson exchange models [6,7], and chiral effective theory [3,8,9] are used to describe NN scattering data. Because no direct neutron-neutron (nn) scattering data exist, the isovector component of potential models are fit to proton-proton (pp) scattering data. Neutron-neutron potentials are assumed to be the same as those for nuclear pp interactions due to charge symmetry [10] with small adjustments for charge-symmetry breaking effects such as the different masses of the neutron and proton [4,6,11].

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The 1S_0 nn scattering length (a_{nn}) and effective range (r_{nn}) have long been used to quantify charge-symmetry breaking in the NN interaction [12–14]. While there have been several recent measurements of a_{nn} to resolve a long-standing discrepancy [15–20], measurements of r_{nn} have not been published for over 40 years. Early experiments that determined r_{nn} from the nn final state interaction (FSI) in various scattering systems resulted in a large spread of values (2.0 - 3.2 fm) with large uncertainties (20 - 60%) [21–27]. Gabioud *et al.* extracted both a_{nn} and r_{nn} based on measurements of the photon energy spectrum from the reaction $^2H(\pi^-, \gamma)2n$ and achieved the most precise result to date, $r_{nn} = 2.80 \pm 0.11$ (exp) ± 0.11 (theory), consistent with charge symmetry [28–30]. More recently, r_{nn} was calculated from the value of a_{nn} determined from measurements of the nn FSI in neutron-deuteron (nd) breakup [31–34]. These determinations are not ideal because the low relative momentum between the neutrons in the nn FSI makes this configuration much more sensitive to a_{nn} than to r_{nn} .

Neutron-neutron quasifree scattering (QFS) in the nd system is ideal for measuring r_{nn} . In this kinematic configuration, the momentum of the incident neutron is transferred exclusively to the

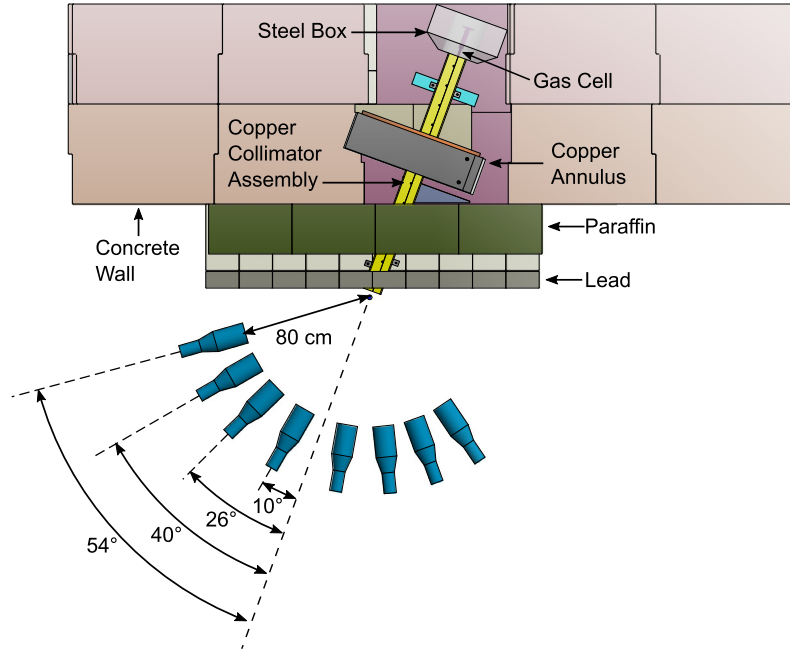


Fig. 1. A diagram of the experiment setup (distances are to scale). The CD_2 sample is 177.6 cm from the center of the neutron production cell, and the detectors are located 80 cm from the target (center-to-center distance) at nominal angles of 10° , 26° , 40° , and 54° on either side of the beam axis. More details are given in the text.

neutron in the deuteron, i.e., the proton remains at rest in the laboratory frame during the scattering process. The cross section for nn QFS in nd breakup is highly sensitive to r_{nn} and is insensitive to off-shell effects of the NN potential, three-nucleon forces, and a_{nn} [35,36]. For this reason, several early experiments determined r_{nn} from measurements of nn QFS in nd breakup. These experiments were performed at incident neutron energies between 14 and 25 MeV [37–41]. Although these measurements agreed well with theory, they were limited by large statistical uncertainties and were compared to theory which implemented several simplifying assumptions and used phenomenological NN interactions. A weighted average of the results gives a value of $r_{nn} = 2.68 \pm 0.16$ fm, consistent with the value from Gabioud [12]. The recommended value of $r_{nn} = 2.75 \pm 0.11$ fm is a weighted average of all previous measurements, but the value is dominated by the π^-d and nn QFS experiments [12]. The average value is consistent with the charge-symmetric proton-proton value of $r_{pp} = 2.85 \pm 0.04$ fm [12–14].

The situation was complicated by three recent measurements of nn QFS in nd breakup at incident neutron energies of 10.3, 26, and 25 MeV [42–44]. Rigorous Faddeev calculations [45] using the CD Bonn potential [6] underpredicted the measured cross section by about 16% [36,43,44]; the theory predicted the shape of the data but not its magnitude. Inclusion of three-nucleon ($3N$) forces did not significantly change the predicted cross section [35]. Experimentally, a large error ($\approx 16\%$) in the determination of the beam-target luminosity would explain the discrepancy. On the theory side, the discrepancy could be removed by scaling the 1S_0 nn interaction matrix element by a factor of 1.08. However, this remedy drastically alters the value of r_{nn} , resulting in a significant charge-symmetry breaking effect [36].

We have performed new measurements of the cross section for nn QFS in nd breakup to investigate the discrepancy reported in Refs. [42–44]. In contrast to previous experiments, the integrated beam-target luminosity was determined from the yields for nd elastic scattering. This removes several sources of systematic uncertainty because the nd elastic scattering yields are measured simultaneously with the breakup yields and the absolute neutron flux and number of deuterium nuclei in the target do not need

to be known independently. This technique has been successfully implemented in a previous measurement [46]. The present experiment was conducted at a different energy with more configurations sensitive to nn QFS than previous work [43,44]. In this letter, we discuss the setup of the experiment, the data-analysis procedures, and the results for the kinematic configurations sensitive to r_{nn} . More details about the experiment and results from other nd breakup configurations will be discussed in a forthcoming publication.

Measurements were performed at the tandem accelerator facility at the Triangle Universities Nuclear Laboratory. The experiment setup is shown in Fig. 1. A beam of deuterons was directed into a 7.26-cm long cell of deuterium gas pressurized to 7.1 atm to produce neutrons at 15.5 ± 0.25 MeV (full width) via the $^2\text{H}(d, n)^3\text{He}$ reaction. The incident deuteron beam was pulsed ($T = 400$ ns, $\Delta t = 2$ ns FWHM) and the arrival of each beam pulse was detected by a capacitive beam pickoff unit immediately upstream of the deuterium gas cell. This provided a time reference for neutron time-of-flight (TOF) measurements. The average deuteron beam current on target was kept at 800 nA.

The use of a copper collimator surrounded by a large shielding wall resulted in a rectangular neutron beam with a plateau of constant flux 36 mm wide \times 55 mm high at the location of the CD_2 target, which was suspended 177.6 cm downstream from the center of the neutron production cell.

Eight BC-501A liquid organic scintillators were used for neutron detection. The detectors were right cylinders (diameter = 12.7 cm, thickness = 5.08 cm) oriented with symmetry axes pointing at the scattering sample. Detectors were placed approximately 80 cm from the scattering sample (center-to-center distance) at nominal angles of 10° , 26° , 40° , and 54° on opposite sides of the neutron beam axis. The exact positions and scattering angles for each detector were determined from a survey of the detectors and scans of the neutron beam profile. Another cylindrical BC-501A scintillator (diameter = 3.81 cm, thickness = 3.81 cm) was placed in the neutron beam 507.4 cm downstream from the neutron production cell to monitor the neutron beam flux during data collection (not shown in Fig. 1).

Table 1
Properties of the scattering samples used.

Sample	Mass (g)	Diameter (mm)	Height (mm)
CD ₂	25.172	28.3	36.4
Graphite	42.055	28.6	38.0

To reduce background events, two cuts were applied to the data. A pulse-height threshold equal to one-half the energy of the ¹³⁷Cs Compton-scattering edge (239 keV-electron-equivalent) was used to reduce backgrounds from low-energy particles. Pulse-shape discrimination (PSD) techniques were used to reduce backgrounds from gamma-ray events.

Two right cylinders composed of deuterated polyethylene (CD₂, Cambridge Isotope Laboratories, Inc., DLM-220-0) and graphite were used as scattering samples. Physical properties of the samples are given in Table 1. Each sample was mounted in the beam with their symmetry axes vertical. The entire volume of each sample was within the area of constant neutron flux. The graphite sample was used to measure backgrounds from neutron scattering on carbon in the CD₂ sample. Other backgrounds such as neutron scattering from air were measured with an empty sample holder.

To avoid unacceptably high dead times of the data-acquisition system (DAQ), a trigger circuit with separate branches for single detector events and coincidence events was used. Coincidences between detectors on opposite sides of the neutron beam ($\Delta\phi = 180^\circ$) within a window of 850 ns triggered the DAQ. The single-event branch trigger rate was divided by a factor of 10, delayed 400 ns, and vetoed by the coincidence branch before triggering the DAQ. This allowed all coincidence events to be measured with a reasonable DAQ dead time ($\sim 10\%$) while accumulating sufficient counts from *nd* elastic scattering to achieve a statistical accuracy better than 0.1% in the beam-target luminosity determination.

Two types of coincidence spectra were measured: (1) the raw coincidence spectrum containing true and accidental coincidences, and (2) the accidental coincidence spectrum. Coincidences between events originating from two consecutive beam pulses ($\Delta t \sim 400$ ns) were used to measure the accidental coincidence spectra. The coincidence spectrum for the pair of detectors at 40° on opposite sides of the beam is shown in Fig. 2, where accidental coincidence spectrum has been subtracted from the raw coincidence spectrum for display.

A background due to detector cross talk, in which a single neutron scattered between two detectors and was detected in both, contributed to the raw coincidence spectrum. These events were separated by less than 100 ns in time and were indistinguishable from real *nn* coincidences. However, due to the experiment geometry, these events fell outside the region of the data reported here. Coincidences due to cross talk form the bands indicated by the red dashed lines in Fig. 2. The events around $E_1 = E_2 = 1.2$ MeV are due to cross-talk coincidences from gamma rays not removed by the PSD cut.

Coincidence events from *nd* breakup fall on a locus of kinematically allowed neutron energies. The red curve in Fig. 2 is the ideal locus, or *S* curve, defined by the central geometry of the detector pair. The variable *S* measures the arc length along the curve in a counterclockwise direction beginning at the point where the energy of the second neutron reaches a minimum [45], indicated by the red dot in Fig. 2. For each detector pair, the raw and accidental coincidence events in a band around the *S* curve were projected onto the ideal kinematic locus. The *S* curve was divided into 0.5 MeV-wide bins and each detected event was projected into the nearest bin on the *S* curve. The projected accidental coincidence spectrum was subtracted from the projected raw spectrum for each detector pair to obtain the true *nn* coincidence yields as a

function of *S*. The breakup cross section was computed using these yields.

The present data were compared to rigorous ab-initio three-body calculations using the CD-Bonn potential [6,7] and the semilocal momentum-space (SMS) regularized $N^4\text{LO}^+$ chiral interaction of the Bochum group [9] with the cutoff $\Lambda = 450$ MeV in the Faddeev formalism applying the technique described in Ref. [45]. A Monte-Carlo (MC) simulation of the experiment was used to average the point-geometry theory predictions over the energy spread and finite geometry of the experiment to allow accurate comparison between theory and data. The MC simulation was also used to determine the average values of the product of neutron detector efficiencies and neutron transmission probabilities as a function of *S*, which were necessary to compute the breakup cross section. Finally, the simulation was used to quantify contributions of background processes to neutron scattering yields. The details of the simulation can be found in Ref. [46].

Background processes that were simulated for both breakup and *nd* elastic scattering included: multiple scattering of neutrons in the sample, in-scattering of neutrons from shielding materials and adjacent detectors, and neutrons produced via $^2\text{H}(d, n)^3\text{He}$ on deuterons implanted in the gold beam stop at the end of the gas cell. Two additional backgrounds for *nd* elastic scattering were simulated: neutron scattering from the 1.6% hydrogen impurity in the CD₂ sample, and *nd* breakup events in which only one neutron was detected. The fraction of background events determined with the MC simulation was subtracted from the measured *nn* coincidence yields and the *nd* elastic scattering yields. The corrections for elastic scattering were between 7-12% and the average correction for breakup events varied from 6-8%, depending on the scattering configuration.

The yields from *nd* elastic scattering in each detector were used to determine the integrated beam-target luminosity. Backgrounds from neutron scattering on carbon and air were measured using the graphite sample and an empty target holder, respectively. The TOF spectrum for each detector accumulated with the empty target holder was normalized and subtracted from the spectra measured with the CD₂ and graphite samples. The empty-target TOF spectra were normalized using the integrated beam current (BCI), the gas pressure in the neutron production cell, and the DAQ live time fraction. The TOF spectra measured with the graphite sample were normalized to the spectra measured with the CD₂ sample in a similar way. The normalization factor also included the ratio of carbon nuclei in the two samples determined using data from a previous experiment [46]. The normalized graphite TOF spectra were subtracted from the CD₂ TOF spectra to obtain the raw yields from *nd* elastic scattering. Also, the raw yields were corrected for backgrounds quantified with the MC simulation.

The luminosity per BCI measured by all eight detectors agreed with a standard deviation of 2.1%. The geometric mean of the beam-target luminosity measured by all detectors except those at 10° was used to compute the breakup cross section. The *nd* yields measured by the detectors at 10° were excluded from the luminosity determination because of the large uncertainty in subtracting the background contributions ($\sim 70\%$) due to neutron scattering on carbon and air.

Several *nn* QFS configurations were measured using detectors positioned on opposite sides of the beam axis. The detector pair at $\theta_1 = \theta_2 = 40^\circ$ measured an exact quasifree-scattering configuration. The detector pair at $\theta_1 = \theta_2 = 26^\circ$ and the two pairs at $\theta_1 = 26^\circ, \theta_2 = 40^\circ$, measured configurations near *nn* QFS, where the proton energy reaches a minimum of 0.4 MeV and 0.1 MeV, respectively. Two other *nn* QFS configurations were measured; however, the cross sections for those configurations are dominated by *np* final-state interactions and therefore were not used to determine r_{nn} .

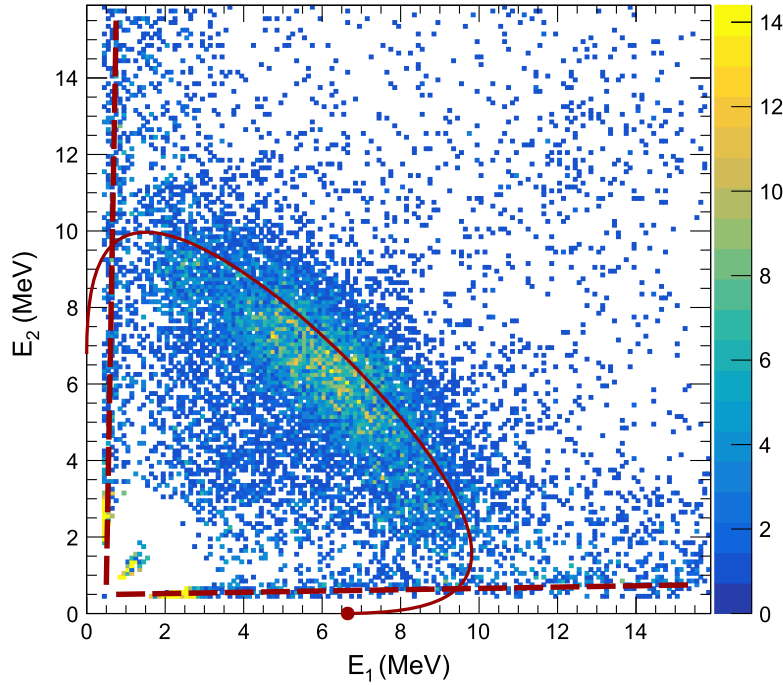


Fig. 2. Two-dimensional coincidence energy spectrum for the detectors at 40° on opposite sides of the beam axis. The accidental spectrum has been subtracted from the raw spectrum. The red curve is the ideal kinematic locus, and the red dot marks the point where $S=0$. The red dashed lines indicate regions affected by cross-talk events. The counts in the bins at low energy (E_1 and $E_2 < 3$ MeV) exceed the vertical scale and may contain 15 - 60 counts.

Table 2

Sources of systematic uncertainty in the determination of the cross section for nn QFS in nd breakup. All uncertainties are given as one standard deviation.

Source	Magnitude (%)
Coincidence yields	1.5
Elastic scattering yields	2.8
Efficiency normalization	2.9
Efficiency shape	3.0
Detector gain drift	1.0
Neutron transmission	2.7
nd elastic cross section	1.6
Detector solid angle	0.9
Single event live time	0.1
Coincidence event live time	0.6
Total	6.3

Our results for the nn QFS cross section are presented in Fig. 3. The measured data are given by the points and the error bars represent statistical uncertainty. Not shown on the plot is a systematic uncertainty of $\pm 6.3\%$. The data points for the configuration at $\theta_1 = 26^\circ$, $\theta_2 = 40^\circ$ are a statistically weighted average of the results from the two detector pairs. The curves in Fig. 3 represent the result of the MC simulation using nd breakup cross sections calculated with the CD Bonn potential with different values of r_{nn} . The curves provide a representative sample covering the full range of the values r_{nn} used in the analysis.

Sources of systematic uncertainty are listed in Table 2. The uncertainty in the measured nn coincidence yields is mainly due to the MC corrections for multiple scattering and in-scattering, but also includes contributions from the accidental background subtraction and neutrons produced at energies below 15.5 MeV via (d, n) reactions on contaminants in the gas cell. Subtraction of the graphite spectra and simulated backgrounds contribute the most to the uncertainty in the extracted elastic scattering yields. The MC simulation uses as input simulated detector efficiency curves fit to measurements of the neutron flux from the ${}^2\text{H}(d, n){}^3\text{He}$ reaction at zero degrees [47,48]. The uncertainty in the overall normal-

ization and shape of the efficiency curve were determined from those measurements as in Ref. [46]. The effect of small changes in the detector gain on the simulated detector efficiency was estimated using variations of the efficiency curve due to changes in the detector threshold setting. Neutron transmission factors were calculated with the MC simulation using cross sections and associated uncertainties from ENDF/B-VII.1 [49]. The nd elastic scattering cross section was computed using the CD Bonn potential, and the error is estimated as the difference between predictions of several modern NN potentials [50]. The uncertainty in the detector solid angle is due to the precision of measuring the positions of the detector faces (0.1 cm). The difference between multiple methods used to determine the DAQ live-time fraction is used as an estimate of its uncertainty.

To determine r_{nn} , the MC simulation was run using breakup cross sections calculated with the CD Bonn nn 1S_0 matrix element scaled by seven different factors, resulting in different values of r_{nn} . Scaling this matrix element also alters a_{nn} ; however, because the nn QFS cross section is sensitive only to variations in the effective range and not the scattering length, this is adequate to determine r_{nn} [36]. For every detector configuration, the value of χ^2 was computed as a function of r_{nn} using the integral of the cross section over the QFS peak where the sensitivity to changes of r_{nn} is greatest. A second-degree polynomial was fit to the χ^2 function and the minimum of this fit was taken as the best value of r_{nn} . The statistical uncertainty in the extracted value of r_{nn} is given by $\Delta r_{nn} = |r_{nn}(\chi_{min}^2 + 1) - r_{nn}(\chi_{min}^2)|$. The integral of the QFS theoretical cross section as a function of r_{nn} was used to convert the systematic uncertainty in the cross section to uncertainty in r_{nn} . The analysis was repeated using the SMS chiral $N^4\text{LO}^+$ potential of the Bochum group [9] with the cutoff $\Lambda = 450$ MeV. Our results are summarized in Table 3. The values of r_{nn} determined from the three nn QFS configurations agreed within statistical uncertainties. The final result is given as a weighted average of those values. The values extracted using the two different potentials agree well, and our values are consistent with the rec-

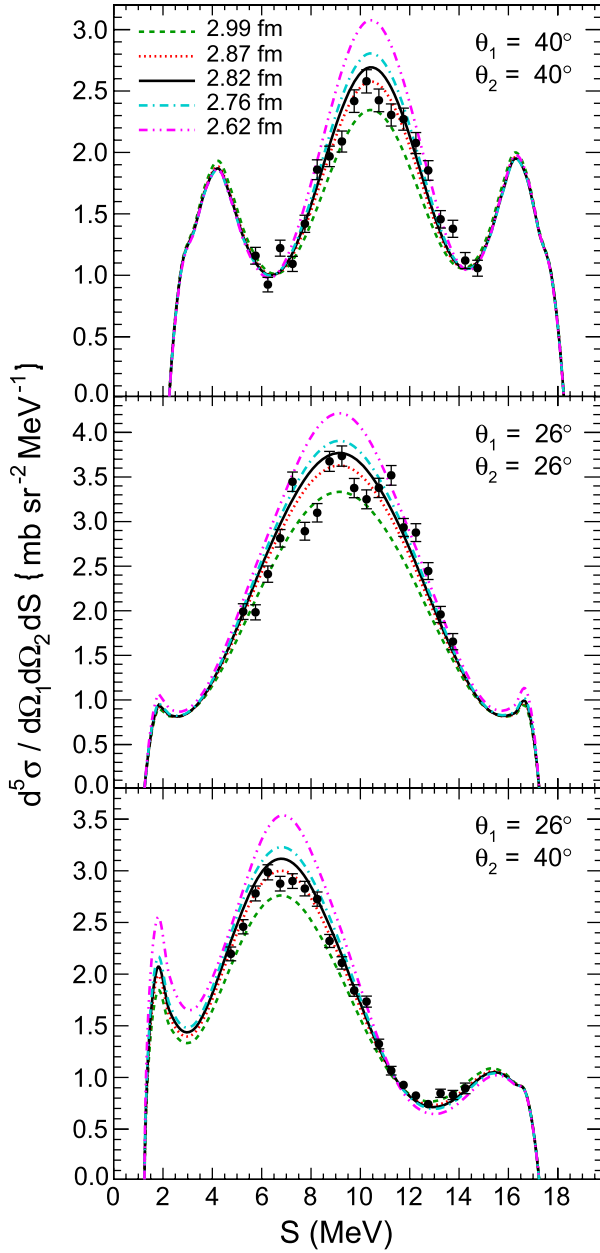


Fig. 3. Plot of the measured nd breakup cross section as a function of S for the mn QFS configurations most sensitive to r_{mn} . The error bars represent statistical uncertainties only; there is a systematic uncertainty of $\pm 6.3\%$. The solid curve is the result of the MC simulation using the standard CD Bonn potential. Other curves represent the MC simulation result using the CD Bonn potential with values of r_{mn} indicated by the legend in the top panel.

ommended value $r_{mn} = 2.75 \pm 0.11$ fm and the charge-symmetric value of $r_{pp} = 2.85 \pm 0.04$ fm [12–14].

We have performed measurements of the cross section for nn QFS in nd breakup using a new technique to determine the integrated beam-target luminosity based on the nd elastic scattering yields measured simultaneously with the mn coincidences from nd breakup. Our results, summarized in Table 3, provide the first measurement of the mn effective range parameter using modern NN potentials and the most precise determination from mn QFS in nd breakup. The data also suggest that the previously reported discrepancies between theory and data in the mn QFS cross section at 10.3, 26 and 25 MeV [42–44] may be due to systematic errors in the determination of the beam-target luminosity leading to incorrect normalization of the breakup cross section. Another possibility

Table 3

Values of r_{mn} determined from different angular configurations in this experiment using the CD-Bonn potential. The last two rows give the weighted average determined using the CD Bonn and N^4LO^+ potentials. All uncertainties are given as one standard deviation. See text for details.

Configuration	$r_{mn} \pm \sigma_{stat} \pm \sigma_{sys}$ (fm)
$\theta_1 = 40^\circ \theta_2 = 40^\circ$	$2.85 \pm 0.02 \pm 0.09$
$\theta_1 = 26^\circ \theta_2 = 26^\circ$	$2.85 \pm 0.02 \pm 0.11$
$\theta_1 = 26^\circ \theta_2 = 40^\circ$	$2.87 \pm 0.01 \pm 0.10$
CD Bonn Average	$2.86 \pm 0.01 \pm 0.10$
N^4LO^+ Average	$2.87 \pm 0.01 \pm 0.10$

is that the discrepancy is energy dependent and only becomes evident in measurements at incident neutron energies above 20 MeV. Further measurements at higher incident neutron energies should be carried out to investigate this possibility.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

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