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# A Fast Impedance Measurement Method for Lithium-ion Battery Using Power Spectrum Property

Jichang Peng, Jinhao Meng, *IEEE Member*, Xinghao Du, Lei Cai and Daniel-loan Stroe, *IEEE Member*

**Abstract**—Electrochemical Impedance Spectroscopy (EIS) can provide fruitful information for Lithium-ion (Li-ion) battery modelling and diagnosis, yet EIS measurement is time-consuming with low-frequency signal injection. By stacking a group of broadband signals, Pseudo Random Sequence (PRS) makes it possible to obtain the battery EIS in a few seconds at the expense of measurement accuracy and Signal-to-Noise Ratio (SNR). Thus, this paper focuses on developing a highly effective signal processing procedure to extract useful information from the PRS for accurate EIS measurement. To enhance the ability of the data cleaning procedure, a three-dimensional cloud is firstly reconstructed for each impedance by integrating its Power Spectrum (PS). The impedance with lower PS can be easily removed through a statistical based multiple selection mechanism, which enables the extraction of the EIS without altering the original measurement. Experimental results on a 3000mAh Li-ion battery prove the effectiveness of the proposed method.

**Index Terms**—Lithium-ion battery, Pseudo random sequence, Power spectrum, Statistical selection, Electrochemical impedance spectroscopy.

## I. INTRODUCTION

**T**HANKS to their superior properties in comparison to other technologies, Lithium-ion (Li-ion) batteries have been a dominant component for energy storage applications such as Electric Vehicles (EV) and consumer electronics. Considering that there have been nearly 6.74 million units for global EV sales in 2021 [1], advanced technologies to help

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manage the usage of Li-ion batteries are of great importance in every aspect.

The battery can transfer the chemical energy to electrical energy utilizing the electrochemical potential between the two electrodes. Unfortunately, due to various aging mechanisms, the performance of the batteries is incrementally decreasing being visible as capacity decreases and resistance increases (i.e., power fade). The lithium metal (-3.04V, 3850mAh/g) has a higher reduction potential and gravimetric capacities than the others materials like sodium (-2.71V, 1165mAh/g), magnesium (-2.37V, 2046mAh/g) and aluminum (-1.66V, 2978mAh/g) [2]. Thus, the Li-ion battery has the great merits of high energy/power density, but its voltage is still limited to less than 5V which indicates one single cell can not fulfil the requirement of a high power load as EVs. Normally, a group of cells will be connected in series or parallel to implement such a task. In this thread, Battery Management System (BMS) plays a key role in the electric, thermal and lifespan management of each cell, and the battery SOX (state of charge, state of health, state of power, state of function, etc.) is the critical indicators for a BMS functionality. Therefore, there is an urgent need to diagnose and prognose the status of the Li-ion battery, and to understand its electrochemical reactions mechanism for a specific battery-based application.

Electrochemical Impedance Spectroscopy (EIS) can provide fruitful information for the electrode kinetics, which has a great potential to be used for the Li-ion battery SOX estimation [3]–[5], the degradation pattern identification [6], [7], internal temperature estimation [8], [9], and safety monitoring [10], [11]. For example, over 20,000 EIS measurements from 45mAh Li-ion cells can accurately reflect the battery degradation pattern by Gaussian process regression in [6]. The distribution of relaxation times is analyzed in [7] to diagnose the degradation mechanisms in the electrodes of the cell. Few specially selected frequencies are chosen to diagnose the battery SOH in [5], which indicates EIS could be possibly used in batteries' second-life applications. The authors in [11] use AC impedance to predict the overcharge and thermal runaway of the Li-ion battery.

Battery EIS measurement is performed in the range of kHz to mHz [12]–[14]. It is a time-consuming procedure for EIS measurement, especially in low frequency areas. Another requirement is that the battery itself should be kept in thermo-electrical equilibrium during the test period. Accordingly, only a small signal can be injected into the Li-ion battery for not

triggering any significantly electrochemical reactions [15]. In [13], the authors measure the EIS of a 6.5Ah Li-ion battery with only 0.5A AC current amplitude for a frequency sweep from 10mHz to 5kHz. It can be concluded that EIS is a sensitive measurement, which is challenging to be implemented in BMS and applied online. Recently, some works [10], [12], [16]–[18] have managed to design a low cost prototype for a friendly EIS measurement in battery applications. An impedance-based BMS is designed to measure the impedance of a 50 Ah battery from 1 to 1000Hz [10]. Additionally, a low-complexity onboard impedance measurement system is proposed in [12] utilizing a high-power dual active bridge converter, which can measure the frequency in the range of 0.1-500 Hz. A MOSFET-based equalization circuit for the battery impedance measurement with a sinusoidal signal is proposed in [16]. A wireless charger is used to measure the battery impedance online in [18]. Besides hardware design, signal generation and processing also require more attention since more informative injection and accurate EIS calculation are always preferred in this case. More research is still needed to improve the efficiency as well as the accuracy of the EIS measurements.

To alleviate the above issues, great efforts have been made on developing the excitation signals with a series of frequency superposition and related data processing methods [19], [20]. Recently, multi-steps [21], multi-sines [22]–[25], and Pseudo Random Sequence (PRS) [8], [19], [26]–[28], *etc.* have been investigated for battery EIS measurement. Mutisinusoidal signal in the ranges of 1-1.8 kHz has been chosen to obtain the battery impedance in [23], which is further used to estimate the battery capacity. A step signal is proposed in [21] to improve the measurement speed of the multi-sines method, and a 200 Hz step waveform is selected to test a 2.6 Ah 18650 Li-ion battery for validation. A random integer number white noise approximation is proposed in [28] to measure the impedance of the battery online, while the cross-correlation technique is used for signal generation. Among all the broadband signal generation methods, PRS has a similar statistical property to white noise and is easy to implement as explained in [19], [29].

According to the above description, it's clear that much effort has been made to generate the multi-frequencies signal for battery EIS measurement. However, the responses of those broadband signals are more difficult to be processed compared with single frequency injection. A powerful signal processing procedure should be designed to accurately extract the useful EIS measurement from the especially low Signal-to-Noise Ratio (SNR) signals. Most existing works still use the Moving Average Filter (MAF) [19], [28] to smooth the measured impedance. Large deviations may exist because of the limited ability of those linear filters, which inspires us to propose a novel impedance measurement method utilizing the power spectral density characteristics of the exciting signal.

This paper proposes a fast Li-ion battery impedance measurement method to extract the impedance spectra from the PRS signals. Considering that the synthetic signals composed of multi-frequencies can not receive high SNR responses at all broadband frequencies, we design a novel data cleaning

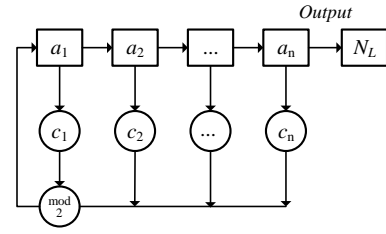


Fig. 1. The linear feedback shift registers for PRS generation

procedure to extract the worthwhile information from the original measurement by integrating the real and imaginary parts, and PS into a three Dimensional (3D) cloud. The Power Spectrum (PS) reflects the power of a signal at various frequencies and can be regarded as a critical indicator to evaluate the effectiveness of the measured impedance. To the best of our knowledge, this is the first time to use a 3D cloud data cleaning method for improving the accuracy of the battery EIS measurement.

The main contributions of this paper lie in the following aspects:

- 1) A Nyquist plot-based 3D cloud is first reconstructed for the data cleaning of impedance measured by PRS, which utilizes the PS property of the injected signal.
- 2) A statistical based multiple selection mechanism is designed to remove the outliers and obtain a smooth battery EIS curve without any deformations.
- 3) The accuracy of our method is proven through the experimental tests on a 3000mAh Li-ion battery under different SOCs and temperatures.

This paper is organized into five sections. Section II introduces the implementation of the fast battery impedance measurement. The proposed data processing procedure is detailed in Section III. Experimental validation is illustrated in Section IV. Section V summarises the main conclusion of this work.

## II. FAST BATTERY IMPEDANCE MEASUREMENT

PRS is used to measure the battery EIS in a short time. This section will briefly introduce the principle of PRS and its characteristics, and the battery impedance calculation method.

### A. Pseudo Random Sequence

PRS can simulate the white noise in discrete time, and is a superior way to excite the battery at all frequencies in theory compared with other signals. The Maximum Length Binary Signal (MLBS) is one of the commonly used PRSs, which could be finalized by multi-stage linear feedback shift registers as shown in Fig. 1. Let us define  $N_L$  as the length of PRS, and the PRS can be generated by an  $n$ -th order shift registers as follows.

$$N_L = 2^n - 1 \quad (1)$$

Afterwards,  $a_n$  can be obtained by modulo 2 operation,

$$a_n = \left( \sum_{i=1}^n c_i a_i \right) \text{mod } (2) \quad (2)$$

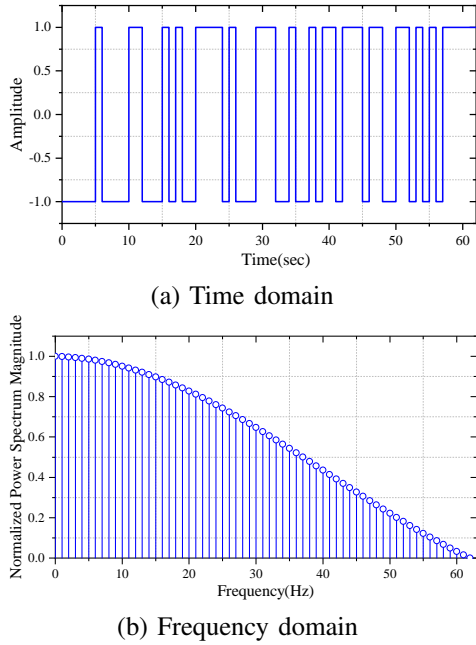


Fig. 2. An example of MLBS with  $N_L = 63$  and  $f_c = 1\text{Hz}$

where  $a_n$  has only two states 0 or 1 which indicate the binary sequence generates in GF(2).

The coefficients  $c_i$  can be calculated by a primitive polynomial according to the values of  $n$  and  $N_L$ . It is easy to understand the frequency resolution  $f_r$  of PRS should be,

$$f_r = f_c/N_L \quad (3)$$

where  $f_c$  is the clock frequency of the PRS.

A MLBS with  $N_L = 63$  and  $f_c = 1\text{Hz}$  is illustrated in Fig. 2 to explain the feature of a typical PRS. The amplitudes of the MLBS toggle between level 1 and -1 as Fig. 2(a). The Root Mean Square (RMS) of the MLBS is 1. In the frequency domain, the power spectrum magnitude follows the  $(\sin^2 x)/x^2$  envelope as illustrated in Fig. 2(b). It means that the PS of the MLBS gradually decays with increasing frequency. Additionally, the amplitude of the MLBS at  $f_n$  can be calculated as,

$$A_{MLBS}(f_n) = \frac{2a\sqrt{N_L+1}}{N_L} \frac{\sin(\pi n/N_L)}{(\pi n/N_L)} \quad (4)$$

where  $f_n = (n-1)f_r$ .

When the  $f_n = 1/3f_c$ , the magnitude of MLBS rapidly decreases. Thus,  $N_L$  and  $f_c$  must be carefully designed for a specific application.

### B. Battery Impedance Calculation

For the battery impedance measurement with PRS, the MLBS should be injected into the battery within the frequencies  $[f_{max}, f_{min}]$ . According to the property of MLBS,  $f_{min}$  has to be larger than  $f_r$  and  $f_{max}$  should be set to  $0.4f_c$ .

In the frequency range  $[f_{min}, f_{max}]$ , the impedance can be calculated from the injected signal and the corresponding battery responses. Let's define the current  $i(t)$  is injected into

a Li-ion battery, and the voltage  $v(t)$  is measured accordingly. Then, the Fourier transform of  $i(t)$  and  $v(t)$  can be obtained,

$$\begin{cases} V(k) = \sum_{k=0}^{N-1} v(t)e^{-j2\pi kt/N} \\ I(k) = \sum_{k=0}^{N-1} i(t)e^{-j2\pi kt/N} \end{cases} \quad (5)$$

From (5), the battery impedance at a specific frequency is calculated by,

$$\hat{Z}(k) = \frac{V(k)}{I(k)} \quad (6)$$

where  $\hat{Z}(k)$  is the impedance of the  $k$ -th frequency.

The  $k$ -th frequency is  $kf_k$ , while the  $f_k$  is defined as,

$$f_k = f_s/N_s \quad (7)$$

where  $f_s$  is the sampling frequency, and  $N_s$  is the number of the sampling data.

## III. THE PROPOSED DATA PROCESSING PROCEDURE

Although PRS can inject a broadband signal into the battery within a short period, impedance measurement through PRS suffers from noise and other interferences. Considering the fact that the signal with low PS is easily contaminated by noise and the PS of all the frequencies in Fig. 2 is not equally distributed, the PS property of PRS is utilized in this section for an accurate battery impedance measurement.

### A. Power Spectrum

PS describes the distribution of the signal's power with frequency variation. Since white noise is a stationary process, the PS of a PRS can be described by its autocorrelation function according to Wiener-Khinchin theorem as follows,

$$S_{xx}(f) = \sum_{k=-\infty}^{+\infty} r_{xx}[k]e^{-j2\pi kf} \quad (8)$$

$$r_{xx}(f) = E[x[n]x[n-k]] \quad (9)$$

where  $S_{xx}$  is the power spectrum of  $X[n]$ .

Once the periodogram is used for the PS calculation, the MLBS can be regarded as a finite energy sequence. According to (4), the PS  $P_{MLBS}(f_n)$  can be computed as,

$$P_{MLBS}(f_n) = \frac{(I_{MLBS}(f_n))^2}{f_n} \quad (10)$$

$$P_{MLBS-n}(f_n) = \frac{(I_{MLBS}(f_n))^2}{f_n * P_{MLBS}(f_1)} \quad (11)$$

where  $I_{MLBS}(f_n)$  is the amplitude of the MLBS at frequency  $f_n$  after Fourier transform.

It is easy to understand that there always exists a  $P_{MLBS-n}(f_n)$  for each  $f_n$ , which creates an opportunity to integrate the PS to the battery impedance. Once the PS is low, the signal is less informative with a lower possibility to be a valid value. Thus, PS can be regarded as a critical index to evaluate the signal at different frequencies.

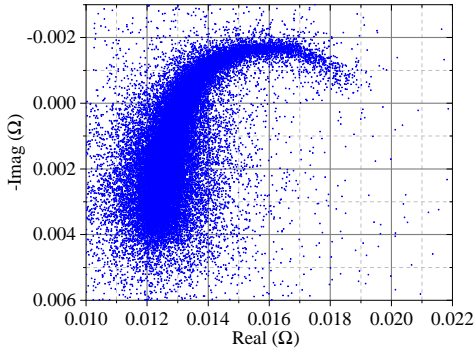


Fig. 3. The impedance of a Li-ion battery with MLBS

### B. Reconstruction of the 3D Cloud

Li-ion battery should be treated as a linear system for the impedance measurement, and we will use the galvanostatic mode in this work. The following impedance in Fig. 3 can be obtained from a Li-ion battery when using MLBS. It is found from Fig. 3 that the high frequency area is contaminated by noise, and the shape of the normal impedance could only be seen in low frequency range. The main reason for such a phenomenon is the attenuation of the PS with the increasing frequency. Therefore, it is difficult to directly obtain useful impedances from the Nyquist curve in Fig. 3.

The  $P_{MLBS-n}(f_n)$  of the MLBS signal for the above battery impedance is shown in Fig. 4. We find that the PS of the MLBS gradually attenuates with the increase of the frequency. Also, it is clearly recognized that the PS fluctuates even between similar frequencies. Generally, a large PS signal means more power is injected into the battery, which has a higher chance against noise interference and then measures an accurate impedance. Then, besides the impedance value for specific frequencies, can be regarded as another property for the impedance measurement. Based on the above rules, we reconstruct the Nyquist plot of the battery impedance with PS information to form a 3D cloud in Fig. 5. In this way, the PS property is merged into the battery impedance measurement, which could be further used for data cleaning.

In Fig. 5, the colormap of the 3D cloud shows the intensity of the PS for each measured impedance. For example, the green and yellow dots have a higher PS than the blue ones. It is obvious from Fig. 5 that the blue dots deviate from the main data group, which are more likely to be outliers of the EIS measurement. In addition, the green color dots with high-intensity PS are centered in the middle of the dataset which is also consistent with the basic shape of the impedance spectrum. Massive scattered and disordered blue dots in Fig. 5 also prove the correctness of the above analysis. Therefore, by the reconstruction of a 3D cloud, the PS property can be used to process the impedance measurement of a Li-ion battery. Once the impedance with low-intensity PS is removed, accurate battery impedance measurements can be expected.

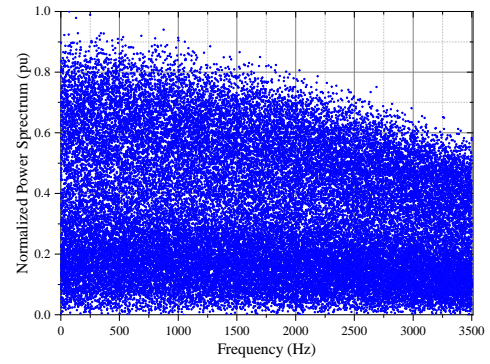


Fig. 4. The normalized power spectrum of a Li-ion battery with MLBS

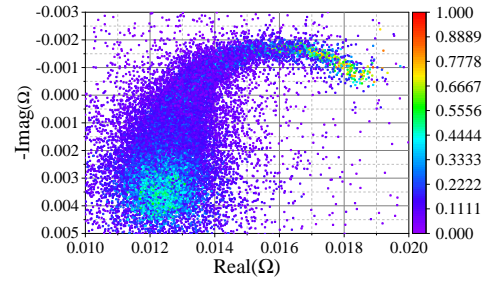


Fig. 5. The 3D cloud of Li-ion battery impedance

### C. 3D Cloud Cleaning Method for Impedance Measurement

From the above analysis, it is possible to clean the impedance on the foundation of the reconstructed 3D cloud. Here, we propose a statistical based multiple selection mechanism to obtain the battery EIS.

As shown in Fig. 5, the density of the dots in the 3D cloud can be utilized to process the calculation results of the impedance. In order to evaluate the statistical characteristics of the impedance dots in Fig. 5, a neighbourhood area  $A$  is defined at first. The average Euclidean distance  $\bar{d}_k$  of the  $k$ -th dot with coordinate  $(x_k, y_k, z_k)$  in  $A$  is then calculated as,

$$\bar{d}_k = (1/m) * \sum_{a=1}^m \sqrt{(x_k - x_a)^2 + (y_k - y_a)^2 + (z_k - z_a)^2} \quad (12)$$

where  $(x_a, y_a, z_a) \in A$  and  $m$  is number of dots in area  $A$ .

The mean  $\mathbb{E}[\bar{d}_k]$  and variance  $\mathbb{E}[\bar{d}_k^2]$  of  $\bar{d}_k$  can be obtained from (13) and (14),

$$\mathbb{E}[\bar{d}_k] = (1/N_k) * \sum_{k=1}^n \bar{d}_k \quad (13)$$

$$\Delta[d_k] = \sqrt{(1/N_k) * \sum_{k=1}^{N_k} (\bar{d}_k - \mathbb{E}[\bar{d}_k])^2} \quad (14)$$

where  $N_k$  is  $m + 1$ .

Afterwards, a reconstructed 3D cloud cleaning method is proposed in Algorithm 1 for automatically selecting the effective impedance values. Considering the natural diversity of the impedance in the high and low frequency region of the

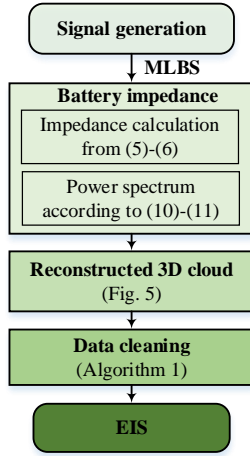


Fig. 6. The diagram of the proposed fast battery impedance measurement

3D cloud, all the measurements are divided into  $N_g$  groups for the convenience of data cleaning. In each group, a threshold  $\Gamma_{th}$  is calculated from the step 3 of Algorithm 1, where  $N_{th}$  is a coefficient tuning the threshold  $\Gamma_{th}$ . Then, the cleaning step can utilize  $\Gamma_{th}$  to decide which dot should be removed from the 3D cloud. After receiving the flag  $Imp_{flag,k}$  from Algorithm 1, the battery EIS  $\hat{Z}_{EIS}(k)$  can be obtained through the following operation,

$$\hat{Z}_{EIS}(k) = \hat{Z}(k) * Imp_{flag,k} \quad (15)$$

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#### Algorithm 1 Reconstructed 3D Cloud Cleaning

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**Input:**  $\mathbb{E}[\bar{d}_k]$ ,  $\Delta[d_k]$ ,  $A$

- 1: **Initialization:** Divide the impedance values into  $N_g$  groups
  - 2: **for**  $i \leftarrow 1$  to  $N_g$  **do**
  - 3:      $\Gamma_{th} \leftarrow \mathbb{E}[\bar{d}_k] + N_{th} * \Delta[d_k]$  //Calculate the threshold
  - 4:     **for**  $j \leftarrow 1$  to  $m$  **do**
  - 5:          $\bar{d}_k$  calculation //From (12)
  - 6:         **if**  $\bar{d}_k < \Gamma_{th}$  **then**
  - 7:              $Imp_{flag,k} \leftarrow 1$
  - 8:         **else**
  - 9:              $Imp_{flag,k} \leftarrow 0$
  - 10:         **end if**
  - 11:     **end for**
  - 12: **end for**
  - 13: **return**  $Imp_{flag}$
- 

Then, it is possible to fast and accurately obtain the Li-ion battery EIS through the above well-designed procedures in Fig. 6. The MLBS signal is generated for battery impedance measurement at first, and then the impedance and its PS are calculated in the frequency domain. Afterwards, a 3D cloud is reconstructed by integrating the impedance with its PS property. According to a statistical based multiple selection mechanism, the effective impedance could be kept as the final results.

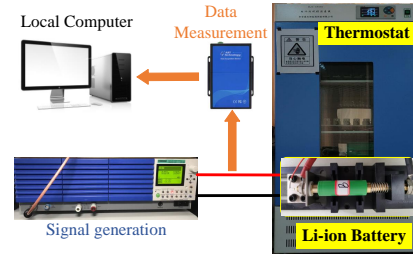


Fig. 7. The test bench for experimental validation

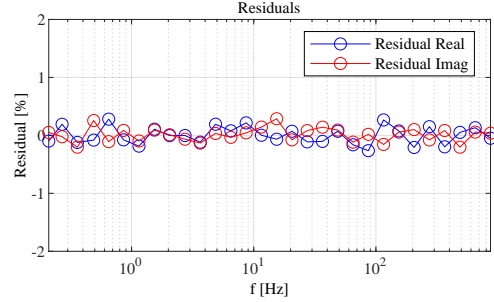


Fig. 8. The Kramers-Kronig test of the reference

## IV. EXPERIMENTAL VALIDATION

### A. Experimental Test Bench

In this section, we validate the proposed method using the test bench shown in Fig. 7. A bi-directional power source is chosen to provide the injected signals for the Li-ion battery, a data acquisition board is used to obtain all the voltage and current measurements. A 18650 NMC based Li-ion battery, with a capacity of 3000mAh and a voltage range between 2.0V and 4.25V, is chosen to verify the proposed method. The battery is placed in a temperature chamber to control the ambient temperature during the test. In this work, the impedance is measured within the frequency range between 0.21Hz and 3.5kHz, which is enough to show the impedance shape of the chosen 18650 Li-ion battery. All the Li-ion battery impedance in this work are measured using the setup presented by Fig. 7. The reference EIS in this work is obtained by injecting only one frequency each time to the battery. The Kramers-Kronig relations are tested at first to prove the reliability and accuracy of the reference. As shown in Fig. 8, the residuals of the reference values are quite small, which indicates the measured reference is effective to be used for the experimental validation.

### B. Validation of the 3D Cloud Cleaning

Following the steps in Algorithm 1, the number of dots in the nearest area  $m$  is defined as 100. Then, the 3D cloud in Fig. 5 is transferred to Fig. 9. By comparing the 3D cloud in those two figures, we find that those obvious outliers are removed from the dataset if only using the 3D cloud cleaning method one time. The contour of the EIS curve can be recognized from the dots in Fig. 9. When the impedance dots in the 3D cloud are converted to the Nyquist plot in Fig. 10, the result

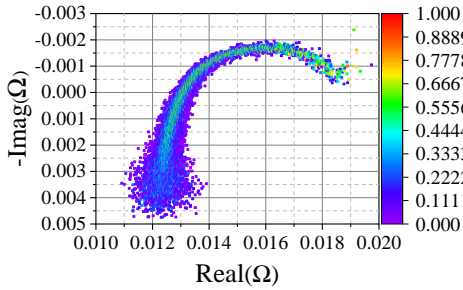
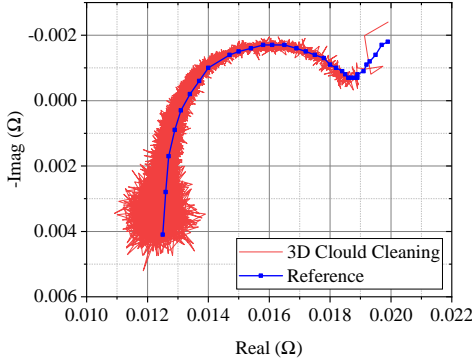


Fig. 9. 3D cloud cleaning with Algorithm 1


 Fig. 10. 3D cloud cleaning results in Nyquist plot with  $N_g=1$ 

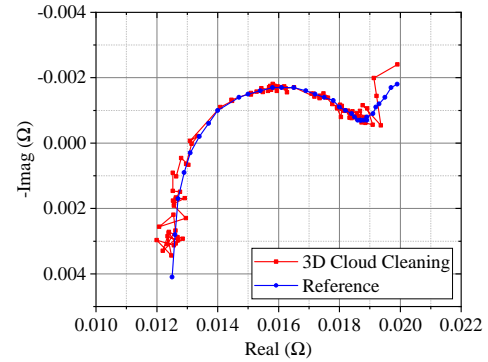
from one-time 3D cloud cleaning is not satisfactory. The red curve around the reference values reflects that there is still too much useless impedance information left.

In order to clean the data with higher efficiency, the 3D cloud is divided into groups in line with the frequency range characteristics. Considering that the PS has a good linear relationship with frequency variation in logarithmic coordinates, those dots in the 3D cloud can be briefly grouped into three frequency regions at [0.21Hz, 10Hz], [10Hz, 1kHz], and [1kHz, 3.5kHz]. Thus, it forms three groups based on the frequency regions above, and  $N_g$  in Algorithm 1 will be 3 in the following experiments. The division of the frequency ranges can follow the distribution of the impedance measurement in a 3D cloud, especially, the number of the measurements and their PS characteristics should be fully considered. In this way, the characteristics of PS in the low, moderate, and high frequency areas can be fully utilized.

The results for 3D cloud cleaning with  $N_g=3$  are shown in Fig. 11 that only 102 useful points are left, which indicates that the noise data is effectively removed after the 3D cloud cleaning procedure. The battery impedance values in Fig. 11 can be easily processed by data smooth filters such as Savitzky-Golay filter. Since the data smooth after 3D cloud cleaning is not difficult, other filters could also be used here.

### C. Validation on EIS measurement

This section validates the EIS measurement of the proposed method. MAF is chosen to deal with the battery impedance measurements in [19], [30] when PRS is used. Thus, MAF is selected as a comparison method in this work. The expression of MAF is as follows,


 Fig. 11. 3D cloud cleaning with  $N_g=3$ 

$$Z_{MAF}(i) = \frac{1}{M_w} \sum_{k=i}^{M_w} Z(i+k) \quad (16)$$

where  $M_w$  is the size of the moving window.

The EIS measurement results of the 18650 Li-ion battery under different SOC are shown in Fig. 12. For SOC=20%, the proposed method is clearly close to the reference compared with the MAF method as illustrated in Fig. 12(a). Although there exist some offsets in the low frequency area, no outliers are identified in the impedance spectra presented in Figs. 12(b)-(c) for the proposed method. Meanwhile, the MAF method shows a larger error, and several outliers exist in the middle or high frequency area.

In order to quantitative analysis of the accuracy of EIS measurement for different methods, the Mean Absolute Percentage Error (MAPE) and the Normalized Root Mean Square Error (NRMSE) are calculated as follows,

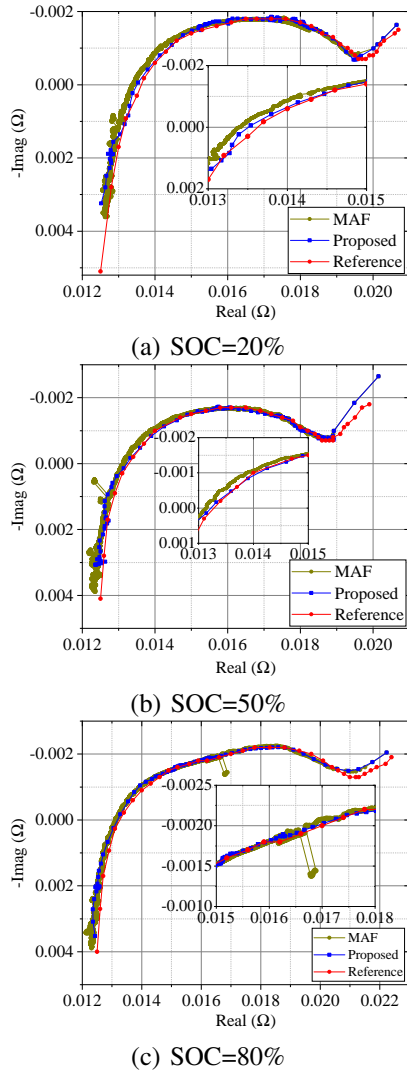
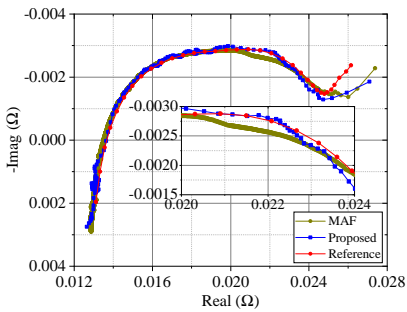
$$MAPE = \frac{1}{M} \sum_{i=1}^M \left| 1 - \frac{Z_m(i)}{Z_r(i)} \right| \quad (17)$$

$$NRMSE = \sqrt{\frac{1}{M} \sum_{i=1}^M \left( 1 - \frac{Z_m(i)}{Z_r(i)} \right)^2} \quad (18)$$

where  $M$  is the number of the measurement,  $Z_m$  and  $Z_r$  are the measured impedance and the corresponding reference respectively.

According to (16) and (17), the MAPE and NRMSE are listed in the TABLE. I. The average MAPE of the proposed method is 0.89%, while it is 1.62% for MAF. As for NRMSE, the proposed method is less than 33 % of the average NRMSE of MAF. Thus, both the MAPE and NRMSE of the proposed method are less than that of MAF, which proves the good accuracy of the proposed method.

For further verifying the performance of the proposed method under temperature variations, the test ambient temperature is controlled to 15°C and 35 °C, and the Li-ion battery SOC is kept to 50%. The EIS measurement results of 15°C are shown in Fig. 13. We find that large errors exist for MAF method in the middle frequency range. The proposed method still performs better than MAF in the whole frequency range. The MAPE and NRMSE of the results in 15°C and 35 °C


 Fig. 12. A comparison of the EIS measurement results at  $T=25^{\circ}C$ 

 Fig. 13. EIS measurement results for SOC=50%,  $T=15^{\circ}C$ 

are shown in the TABLE. II. It is noted that the accuracy of the proposed method has also been confirmed by a series of repeated tests. Based on the above validations, the superior performance of the proposed method can be confirmed.

## V. CONCLUSION

This paper utilizes the PS property of the injected MLBS signal to reconstruct a 3D cloud for fast Li-ion battery

TABLE I  
MAPE AND NRMSE OF EXPERIMENTAL RESULTS AT DIFFERENT SOCS

Methods	Error	SOC=80%	SOC=50%	SOC=20%
MAF	MAPE	2.23%	1.32 %	1.30%
	NRMSE	1.83%	1.03 %	0.82%
Proposed	MAPE	1.04%	0.90 %	0.74%
	NRMSE	0.12%	0.49 %	0.60%

TABLE II  
MAPE AND NRMSE OF EXPERIMENTAL RESULTS AT DIFFERENT TEMPERATURES

Methods	Error	$T=15^{\circ}C$	$T=25^{\circ}C$	$T=35^{\circ}C$
MAF	MAPE	2.92%	1.32 %	2.52%
	NRMSE	2.60%	1.03 %	2.05%
Proposed	MAPE	1.69%	0.90 %	2.39%
	NRMSE	0.64%	0.49 %	1.37%

impedance measurement. By creating a statistical based multiple selection mechanism for data cleaning, the massive impedance data can be effectively extracted from the original measurement. According to the PS characteristics in the different frequency ranges, the originally measured impedance is divided into 3 groups for 3D cloud data cleaning with higher efficiency. In this way, the proposed method can help measure the battery EIS accurately with MLBS in a short period.

The proposed method is validated on a 3000mAh Li-ion battery under various SOCs (20%, 50%, 80%) and temperatures ( $15^{\circ}C$ ,  $25^{\circ}C$ ,  $35^{\circ}C$ ). The MAPE and NRMSE of the proposed method are much lower than the commonly used MAF method. The average MAPE of the proposed method is around 55% of MAF, and the average NRMSE of the proposed method is less than 33% of MAF for different SOCs. The advantages of the proposed method are thus proved through experimental validation. It is noted the proposed method can help the onboard EIS measurement with low-cost hardware, which is critical for improving the capability of BMS.

Future work will be to develop advanced PRS signals for a more efficient and accurate battery EIS measurement.

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