

Logical Pluralism Hollandaise

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Johan van Benthem (2008) compares and contrasts two research programmes, which he calls *logical pluralism* and *logical dynamics*, stating his ‘preference’ (p. 25) for the second of these ‘alternatives’ (p. 8). In this note I want to put the matter into a slightly different perspective.

Logical dynamics is the study of the way that rational agents process information, obtained by various sources—observation, testimony, inference—and use it to act and interact. The formal underpinnings of such investigations are provided by versions of dynamic logic. Johan reports some resistance to this project by his Dutch colleagues—or at least to calling such a project logic. He would certainly have no such resistance from those of us in New Holland.¹ (I speak for myself here, but I am confident that the attitude is one shared by my own colleagues: I suspect that New Hollanders are much more laid back about these things than Hollanders.) Who cares whether one calls it logic, or by some fancy other name? The question is: is it an interesting project to which those trained in the techniques of contemporary logic can contribute? The answer is clearly yes. No problem.

What Johan calls logical pluralism is rather different from what many self-ascribed logical pluralists² call by that name. For him, logical pluralism is the study of sub-structural logics—logics obtained, generally speaking, by taking a sequent calculus for classical logic, and then modifying or eliminating some of its structural rules, such as Weakening and Contraction. That, of course is a perfectly fine enterprise too. But logical pluralism in the more usual sense is both broader and narrower than that. Broader: there are many interesting logics different from classical logic, and not all of these can be thought of as sub-structural—at least, not without a lot torturing. For example, there is a

¹The original name for what is now called Australia. I extend it to New Zealand by fiat.

²E.g., Batens (1985), (1990), Beall and Restall (2006), da Costa (1997).

vast variety of paraconsistent logics.³ One family of these, relevant logics—a favourite topic of many New Holland logicians—is a sort of substructural logic.⁴ But many of them (such as the non-adjunctive, non-truth-function, and many-valued ones) are not. Narrower: logical pluralism is not just a doctrine to the effect that there is a plurality of interesting logics, but also includes the claim that there is no one of them which is uniquely correct. There is no “one true logic”.⁵ Typically, different sorts logics are appropriate for different sorts of reasoning contexts.

Why do I emphasize this? After all, I have no objection to Johan using the words ‘logical pluralism’ as he does if he wants to. I emphasize it because I don’t think that Johan take the other sense of logical pluralism as seriously as he should—even by his own lights. The dynamical systems that Johan gives are all ones based on classical logic. (Substructural phenomena are to be “deconstruct[ed]” into classical logic plus an explicit account of the relevant informational events’ (p. 1).) Now it would seem clear that for a number of the applications that Johan has in mind, using a non-classical logic would be much more appropriate (whether or not one is a logical pluralist about the matter).

Let me illustrate with respect to Johan’s own examples. In any logic with a world-semantics, the consequence relation is defined in terms of truth-preservation over a set of worlds.⁶ The class of worlds therefore defines the logic. In Johan’s dynamic logics, the worlds are the “possible” worlds of classical modal logic, and so the underlying propositional logic is classical. But all of Johan’s constructions can performed with profit with a wider class of worlds—classically “impossible” worlds (be they intuitionist, many-valued, inconsistent, or whatever), making the underlying propositional logic non-classical.

Take, for example, the dynamic epistemic logic in his Section 3. Epistemic possibility is, as most agree, quite different from logical possibility.⁷ In particular, things may be epistemically possible for a rational agent, even though they are logically impossible. Thus, until the Wiles proof, mathematicians took it to be (epistemically) possible that Fermat’s Last Theorem was true, and (epistemically) possible that it was false. If we are to analyse knowledge using worlds, there must, then, be worlds where each alternative holds. And one of these is logically impossible. Moreover, what Wiles proof did was to cut down the space of epistemic possibilities to exclude those in which Fermat’s Last Theorem fails—just as Johan describes.

³For the variety of paraconsistent logics see Priest (2002).

⁴Some care needs to be taken here. Johan puts relevant logics in the family of non-monotonic logic. In one sense this is correct; in another it is not. In the sequent calculi for relevant logics, there are two ways of combining premises, an extensional one, and an intensional one. Weakening fails for intensional combination, but holds extensional combination. See Restall (2000). Thus, in relevant logics as normally conceived, if $\Sigma \vDash A$ then $\Sigma \cup \{B\} \vDash A$; the failure of this is normally taken to be the mark of a non-monotonic logic.

⁵This is not, incidentally, a view that I, myself, share. See Priest (2006), ch. 12.

⁶See Priest (2008), Part I.

⁷And metaphysical possibility too, but let us not go into these murky waters.

What is true for knowledge is true in spades for belief; so similar considerations apply to Johan's examples of dynamic doxastic and belief-revision logic in Section 4. Even rational agents can have logically false beliefs: very strong evidence can point the wrong way. I think that most logicians will have thought at some time that they had proved a logico-mathematical result, only to find out that there was a loophole in the "proof", and that there were counter-examples to the "theorem". So if belief is to be given a worlds-analysis, we need logically impossible worlds.

Not only can rational people believe things that are logically false, they can not believe or know things that are logically true. Hence, there must also be worlds where logical truths fail. Because there are no such worlds in standard doxastic and epistemic logics, including the dynamic versions constructed by Johan, these are beset with the thorny problem of "logical omniscience" (if $\models A$ then $\models \Box A$, where \Box is an epistemic or doxastic operator).

As for belief-revision, any account of the dynamics of this had better be based on some sort of paraconsistent logic. This is because people, even highly rational people, are wont to have inconsistent beliefs. We need an account of belief-change in which change takes us from one belief state to another, both of which are liable to be inconsistent (but non-trivial). So some sort of paraconsistent apparatus is required.⁸

Anyway, as far as Johan's particular constructions go, I emphasize that, with one exception, the non-classical versions can proceed in exactly the same way as in the classical versions: the truth conditions for the doxastic and epistemic operators, the preference ordering, and the operations on it, etc., can all be as he gives them. The exception is the class of worlds involved, and so the underlying propositional logic. Of course, how best to take such worlds to behave, and so which non-classical logic to employ, is a matter for substantial work. The world-semantics of relevant logic provides what is required in many cases: in these, every statement holds at some worlds, and every statement fails at some worlds. But whether this is the best machinery to use is another matter.⁹

It might be suggested that, in all the cases mentioned, the theory is of an ideally rational agent, who never countenances or believes contradictions or other logical impossibilities. Such idealizations have a point. But in the end, if you have a theory that applies only to God (who, being eternally omniscient, hardly has need of a mechanism for belief change or information processing), it is not of much use. We need theories to tell *us* how best to handle these matters—what is the rational thing to do, for example, if a person finds out that their beliefs are inconsistent?

⁸For an account of belief-change based on a paraconsistent logic, see Priest (2006), ch. 8.

⁹The machinery of relevant logic is deployed in the account of intentional operators in Priest (2005).

These particular examples makes the point about the usefulness of non-classical logics for Johan's project. But the point is reinforced by stepping back and looking at the bigger picture. The core of the project is the intelligent management and application of information. But the information with which we operate is always liable to be inconsistent—unless it comes from God. And there is no effective test for inconsistency to filter it out. Inconsistency, then, had better not imply triviality, or there could be no sensible use of such information. Some paraconsistent mechanism must get in on the act.

Indeed, many of the preceding examples invoke paraconsistent logic and its machinery in one way or another. (We in New Holland have had our own issues with conservative Northern colleagues about that topic!) Johan appears to cite paraconsistency as a rival to logical dynamics (p. 26). As should now be clear, this is not at all the case: the tools of paraconsistent logic are just what one needs to pursue a number of applications of logical dynamics effectively.

Paraconsistent logic is just one kind of non-classical logic, of course. Applications of logical dynamics of a kind different from those already noted may well benefit from the use of other non-classical logics—indeed, will do, if logical pluralists of the usual stripe are right. Johan says, referring to his own programme (p. 27), 'I myself see much of our current discussion as trying to break away from the magnetic spell of those mind grooves formed in the grand foundational period of the 1930s'. Indeed so. And arguably the biggest magnetic spell of all is the one cast by classical logic.

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