

Article



A Simulation-Based Performance Analysis Tool for Aircraft Design Workflows

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Abstract: A simulation-based approach for take-off and landing performance assessments is presented in this work. In the context of aircraft design loops, it provides a detailed and flexible formulation that can be integrated into a wider simulation methodology for a complete commercial aviation mission. As a matter of fact, conceptual and preliminary aircraft design activities require iterative calculations to quickly make performance predictions on a set of possible airplane configurations. The goal is to search for a design that best fits all top level aircraft requirements among the results of a great number of multi-disciplinary analyses, as fast as possible, and with a certain grade of accuracy. Usually, such a task is carried out using statistical or semi-empirical approaches which can give pretty accurate results in no time. However, those prediction methods may be inappropriate when dealing with innovative aircraft configurations or whenever a higher level of accuracy is necessary. Simulation-based design has become crucial to make the overall process affordable and effective in cases where higher fidelity analyses are required. A common example when flight simulations can be effectively used to support a design loop is given by aircraft mission analyses and performance predictions. These usually include take-off, climb, en route, loiter, approach, and landing simulations. This article introduces the mathematical models of aircraft take-off and landing and gives the details of how they are implemented in the software library JPAD. These features are not present in most of the currently available pieces of preliminary aircraft design software and allow one to perform high fidelity, simulation-based take-off and landing analyses within design iterations. Although much more detailed than classical semi-empirical approaches, the presented methodologies require very limited computational effort. An application of the proposed formulations is introduced in the second part of the article. The example considers the Airbus A220-300 as a reference aircraft model and includes complete take-off and landing performance studies, as well as the simulation of both take-off and landing certification noise trajectories.

Keywords: model-based design; multi-disciplinary modeling and simulation; aircraft performance modeling

1. Introduction

Nowadays the commercial transport aircraft market is strongly influenced by three main factors. The first conditioning factor, of which the aviation sector has been well aware for decades, is the need to reduce air transportation's environmental impact, as shown by the evermore ambitious targets defined by associations like ATAG and IATA or the Clean Sky 2 consortium. The second circumstance, bound to have a disrupting effect on all market assumptions made so far, is related to the COVID-19 outbreak in year 2020, which has caused severe damage to the air passenger transportation industry. In particular,

recent forecasts by IATA highlight a worldwide -48% RPK with respect to 2019 [1]. Possible future market scenarios following the worldwide management of the COVID-19 pandemic have been recently provided by ICAO [2]. According to ICAO, given the originally planned seat capacity, passenger demand could have increased 72 million for 2020, compared to 2019. However, the latest estimates expect the passenger demand to drop from the above baseline by 861 to 1524 million. This demand level would be 789 to 1452 million below the passenger demand of 2019, with the most substantial reductions expected to be in Europe and Asia/Pacific. The third main circumstance to be considered in the future evolution of the aircraft market is related to the need for most of the major airlines to replace several hundred heritage aircraft, especially in the regional aircraft segment from 20 up to 150 seats. These airplanes are currently in service around the world and are now coming to the end of their useful commercial lives.

According to the above-mentioned scenario, the period that lies ahead will be difficult and interesting at the same time for aircraft designers, who must face evermore demanding challenges. Preliminary aircraft design can address all these issues, defining a new frontier of innovation in terms of configurations and technologies suitable for the ever-increasing demand for more green and efficient aircraft. In particular, the regional aircraft market segment is playing an increasingly important role in the evolution of airline operations. For many years, this growth has been faced by a wide adoption of regional jets. Their success can be largely attributed to their popularity with passengers, who prefer them thanks to their comfort and velocity with respect to turboprops. However, despite the regional jets' success, turboprop engines are 10–30% more efficient than jet engines in cruise conditions, leading to potentially consistent reductions of the amount of fuel used per mission and the amount of pollutant emissions [3,4].

The preliminary design phase of new aircraft models has become very challenging due to evermore demanding requirements. The goal of the first stages of a design loop is to search for the configuration that best fits all requirements, among the results of a great number of multi-disciplinary analyses, as fast as possible, and with a certain grade of accuracy. Often, despite being preliminary design, a higher level of fidelity is required, and in such cases simulation-based design has become crucial to make the overall process affordable and effective. A common example where simulation-based design applies is given by aircraft mission analyses and performance predictions. These usually include take-off, climb, en route, loiter, approach, and landing simulations.

The continuous improvement of computer calculation capabilities over years has allowed for the growth of a large family of software tools dedicated to preliminary aircraft design activities, involving also multi-disciplinary analyses and optimizations [5]. The most popular among such computer programs are listed in the following:

- Pacelab Suite. A commercial software suite, written in C#, developed by the German company
 Pace, part of the Italian group TXT E-solutions, Milan Italy [6]. This software has rapidly become
 a leader on the aircraft preliminary design market due to its user-friendliness and its robust and
 efficient software architecture. The suite is made up of several interconnected modules, each of
 which adds very important features to the base version (e.g., on-board systems architecture or
 detailed cabin layout definition). However, some methodologies and databases lack the required
 scientific know-how that only research centers or universities can provide.
- SUAVE. A piece of open-source software, written in Python, developed at the University of Stanford, California, USA [7]. It comes with lots of interesting features, among which is the possibility to analyze unconventional configurations (e.g., blended-wing body) with different levels of fidelity, and there is the possibility to take into account different sources of energy (e.g., solar power). However, it has poor visualization features and no dedicated input files, lowering its user-friendliness.
- *FLIGHT*. In development since 2006 at the University of Manchester, UK, by Dr. Antonio Filippone, FLIGHT is state-of-the-art software for the prediction and modeling of fixed wing aircraft performance. Through analyzing the performance of airborne vehicles and any sub-systems,

FLIGHT can accurately map aircraft operation under all flight conditions, allowing for numerous logistical variations. A unique benefit of the software is the ability to calculate the impacts of noise and LTO emissions, both within and around an airport [8,9].

- ADAS. Software for the conceptual/preliminary design of transport aircraft (transport jet, regional turboprops, business jet) and light aircraft developed at the University of Naples Federico II, Naples, Italy, by Fabrizio Nicolosi and Giuseppe Paduano [10]. The software, in development since 2005, is completely written in Visual Basic and comes with a dedicated graphic user interface to enhance user-friendliness. Its architecture provides for independent design modules; however, it was not conceived for MDAO applications.
- *CEASIOM*. A conceptual aircraft design framework by CFS Engineering, Lausanne, Switzerland, written in Python, developed within the frame of the SimSAC (Simulating Aircraft Stability And Control Characteristics for Use in Conceptual Design) Specific Targeted Research Project (STREP) approved for funding by the European Commission 6th Framework Programme on Research, Technological Development and Demonstration. CEASIOM is meant to support engineers in the conceptual design process of the aircraft, with emphasis on the improved prediction of stability and control properties achieved by higher-fidelity methods than found in contemporary aircraft design tools. Moreover, CEASIOM integrates into one application the main design disciplines: aerodynamics, structures, and flight dynamics, impacting on the aircraft performance. However, the framework does not carry out the entire conceptual design process; thus, it requires as input an initial layout. as the baseline configuration that it then refines and outputs as the revised layout [11]. For this reason, the framework has been used in combination with the above-mentioned ADAS software [12].
- Piano. A professional tool by Lissys Limited, UK, for the analysis of commercial aircraft available since 1990. It is used in preliminary design, competitor evaluation, performance studies, environmental emissions assessments, and other developmental tasks by airframe and engine manufacturers, aviation research establishments, and governmental or decision-making institutions throughout the world [13].
- *ADS* (Aircraft Design Software). A piece of commercial software developed by OAD (Optimal Aircraft Design), Belgium, after six years of development which has become a standard for the conceptual design of the modern generation of light aircraft. The tool is suitable for several kind of customers, among which are aircraft designers, amateur builders, universities, and research institutes [14].
- AAA (Advanced Aircraft Analysis). Commercial software developed by DARCorporation, Lawrence, Kansas, USA, and widely used by industries and Universities. The tool is suitable for conceptual and preliminary design phases of both conventional and unconventional fixed wings aircraft configurations. The software allows for multi-fidelity analyses, combining classical and fast semi-empirical methodologies with physics-based methods. In addition, a graphic user interface provides for the required user-friendliness [15].
- *RDS^{win}*. Developed by the design and consulting company founded by Daniel P. Raymer, Conceptual Research Corporation, Playa del Rey, CA, USA, this commercial software was conceived to support industries, governments, and universities during preliminary aircraft design activities. It performs MDAO, as well as trade studies, and comes with a graphic user interface to enhance user-friendliness. The tool is suitable both for commercial transport aircraft and military fighters, giving to users the possibility to experiment also with unconventional configurations [16].

In addition, there are several architectures available nowadays dedicated to the multi-disciplinary design optimization (MDO), most of which were born from the specific needs of aircraft designers. A general survey of such methodologies and their implementations is found in [17], which introduces the well known unified descriptions of MDO architectures and discusses the features of both monolithic and distributed frameworks. A notable example of research effort involving some level of simulation-based performance analysis optimization is given by the work of Kroo from Stanford

University [18,19] with his Collaborative Application Framework for Engineering (CAFFE) [20,21]. Martins from the University of Michigan is the leader of a prolific research group (Multidisciplinary Design Optimization Laboratory, MDO Lab) that has released some well known optimization architectures, including the π MDO environment [22], the framework pyOpt [23,24], and the popular optimization software OpenMDAO [25]. Two other interesting works in the MDO field are the Decision Environment for Complex Designs (DECODE) project at the University of Southampton [26], based on the value-driven design concept, and the Chinese research on virtual simulation architectures inspired by the "design for operations" idea [27].

A key feature that most of these pieces of software provide is the possibility to parametrically define both aircraft components and complete aircraft configurations, leading to a very fast and intuitive definition process of a generic aircraft model. One feature missing in most of the above-mentioned tools is the ability to perform simulation-based performance analyses. The goal of this article is to present a mathematical model and its corresponding implementation that fills this gap, and to introduce a piece of software able to perform high fidelity take-off and landing analyses in the context of preliminary design.

The authors of the present article have been users of most of the above-mentioned computer programs, and they have reached a mature vision of the set of features one must expect from a modern MDAO software. This vision drove the development, started in 2015, of a modular framework named JPAD (Java API for Aircraft Designers) that gathers all the lessons learned in the last few decades of in-house tool development for aircraft design [28]. JPAD is an application programming interface (API) able to support civil transport aircraft designers in the need for building multi-disciplinary, simulation-based analysis and optimization workflows. The API is a Java software library containing classes and utility functions that can be used to build software systems running MDAO procedures [5,28–33]. JPAD comes in different interdependent software modules providing modeling, simulation, and analysis features. An introduction to the aircraft geometric modeling possibilities provided by JPAD is given by [34]. The API provides a simulation-based aircraft performance module whose implementation details are introduced by this article. An example of application of this feature can be found in [35], where several flight simulations have been used to find trade factors and response surfaces related to environmental noise, DOC, and pollutant emissions for the design of a transport aircraft configuration with rear-mounted engines. As described in [5], JPAD is also provided with an MDAO module which uses all the advantages provided by the Object-Oriented Programming philosophy to perform a full factorial DOE as well as multi-objective optimizations using computational intelligence like GA or PSO algorithms.

This article is organized as follows: Section 2 presents JPAD as a software library and gives an overview of the API as the technological foundation for the aircraft performance model. Section 3 introduces the performance simulation model and provides details of the implementation architecture. Finally, Section 4 presents an application example of the JPAD performance simulation module to the case of a reference regional transport aircraft.

2. Overview of the JPAD Software Library

The API of JPAD defines a unified model of a generic transport aircraft and comes as a software library in different interdependent modules. Rather than being monolithic computer code, this library provides a large collection of modeling, simulation, and analysis capabilities that can be used as building blocks of computational workflows. The modules at the core of the software architecture are shown in Figure 1. This level of modularity gives a unique flexibility to the software framework, which is easily extendable for future market and research challenges.



Figure 1. JPAD core architecture.

JPAD has been developed from scratch with the following driving ideas:

- 1. To provide a modern, user-friendly preliminary aircraft design toolbox;
- 2. To embed calculation methods with a validated level of accuracy and reliability;
- 3. To be able to perform multi-disciplinary analyses and optimizations;
- 4. To provide executables that require reasonably short computational times for a complete aircraft analysis process.

The multi-disciplinary approach in particular, which is very important in the modern software framework nowadays, is summarized in Figure 2. In addition, to ensure longevity and to enrich its applicative scenarios, the library provides multiple fidelity analysis methodologies and is designed to be extended very easily with newly implemented surrogate models. For instance, as discussed in [5,34], JPAD offers the possibility to easily generate and export an aircraft configuration CAD model in one or more standard formats and to execute high-fidelity analyses by means of third-party external tools (e.g., computational fluid dynamics or finite element method solvers). Without these features it would be extremely difficult to achieve an optimum design that reflects the requirements of aircraft performance, noise and emissions levels, and maintenance and operative costs.

In recent years, the development of JPAD has embedded the knowledge and experience gained by the developing team concerning the setup, testing, and validation of several approaches and methodologies related to aircraft design [36–38]. The experience includes several research efforts in innovative technologies, such as design campaigns on airfoil and high lift devices, and activities related to performance estimation of aircraft with morphing devices [39–41]. Moreover, JPAD incorporates an improved semi-empirical model for vertical tail plane design that was accomplished by means of a campaign of both numerical and experimental studies [33,42,43]. This methodology was also applied to size the vertical tail plane of a new twin-engine commuter aircraft [44]; then its validity was confirmed by wind tunnel tests [45]. Earlier research activities were focused on aerodynamic derivative estimation [46]. Another methodology for fuselage design and prediction of its aerodynamic characteristics based on a surrogate model was developed through CFD-RANS calculations performed on several fuselage geometries suited for regional transport aircraft [47]. Most of this knowledge have been included in the software library using lookup tables packed in dedicated databases [5].

A rather unique capability of JPAD, when compared to other similar software, is that it provides a performance analysis module based on a quite refined set of simulation models. The non-terminal, up-and-away flight phases of a mission are simulated by resolving a set of nonlinear aircraft performance equations (NAPE) adapted from [48]. The terminal flight phases of a mission, such as take-off and landing, have their dedicated models, which are tailored for the designer's specific needs to assess the compliance of results with regulation requirements. All available models are conveniently coupled to allow the simulation of a full mission with realistic navigation requirements and constraints. The details of take-off and landing simulations models are presented in the following section.



Figure 2. Complete JPAD analysis cycle.

3. A Simulation-Based Approach for Take-Off and Landing Performance Assessment

The performance analysis module in JPAD has been completely designed using a simulation-based approach to carry out both flight and ground performance studies with a high level of fidelity. This feature is usually not implemented inside most of the currently available preliminary aircraft design software, which relies on semi-empirical approaches, especially for the take-off and the landing phases.

The JPAD core library includes simulation procedures that predict aircraft performance figures related to each mission phase. The main mission analysis module features several sub-modules and provides the possibility to perform a single performance analysis (e.g., a detailed take-off, climb, or landing simulation), a complete mission profile analysis, or a combination of them. The user can easily configure which analyses must be carried out using a dedicated XML configuration file (see Figure 2). In terms of software engineering work, particular attention has been paid to the implementation of performance predictions within JPAD, to find the right balance between flexibility,

accuracy, computational time, and simulation details. Therefore, although the performance module is the most demanding one in terms of CPU time among all other low and middle fidelity analysis modules available in the library, the possibility for the user to manually enable or disable each sub-analysis enables quite acceptable computational demands for mission assessments.

In the overall JPAD core dependency map, the performance module requires some aircraft weight data as well as trimmed aerodynamic data concerning polar drag curves and lift curves in every standard flight condition (take-off, climb, cruise, and landing). The inputs can be assigned by the user manually—if the analysis is carried out in standalone mode, i.e., when a single focused performance study is required—or they can be fetched from a higher level aircraft analysis manager instance—e.g., when a full-blown design loop is executed. In the first case, two approaches are possible: working with parametrically defined parabolic drag polar curves, or using external drag polar curves if the user has higher fidelity data. In any case, lift curve data must be given using only the following parameters in clean, take-off, and landing configurations: lift curve slope, lift coefficient at zero angle of attack, and maximum lift coefficient. In addition, also the rudder effectiveness coefficient τ_r must be specified, in case of a standalone take-off study, to allow the estimation of the minimum control speed (V_{MC}). That is the minimum speed for which a sudden, single engine failure (with the remaining engines at take-off power) does not result in loss of primary flight control.

All performance assessment procedures use an engine database for each installed engine (multiple types of engine are possible in order to model hybrid propulsion aircraft). The user also has the possibility to define a wide set of calibration factors (all set to 1.0 by default) to trim all engine related quantities (thrusts, SFC, and emission indexes) for each engine rating (maximum take-off, APR, maximum climb, maximum continuous, maximum cruise, flight idle, and ground idle).

The performance module in JPAD currently features the following analyses:

- 1. Take-off;
- 2. Landing;
- 3. Take-off and landing noise trajectories;
- 4. Climb;
- 5. Cruise;
- 6. Descent;
- 7. Mission profile;
- 8. Payload-Range diagram;
- 9. *V-n* diagram.

Among them, this section focuses on take-off, landing, and certification noise trajectories analysis modules. A detailed description of the implemented simulation methodologies is provided, which highlights important features usually not considered by classical semi-empirical approaches used for typical preliminary design activities.

3.1. Take-Off Simulation Model

The take-off analysis module computes conventional aircraft take-off performance using a simulation model first proposed in [28]. However, due to major modifications that have been recently implemented, a review of the methodology is presented here.

The analysis procedure solves a set of ODEs that model the aircraft equations of motion during the whole take-off phase, including the ground roll, the transition to the airborne phase, and the initial climb, up to (and beyond) the conventional standard established by regulations. The aircraft is modeled as a point mass constrained to move in a vertical plane under the action of propulsive, aerodynamic ground contact forces and weight, and hence is treated as a dynamic system in its state-space representation. The unknowns are the following fundamental variables of motion that describe completely the aircraft's state during the whole maneuver:

1. Position *s*, i.e., center of gravity projected vertically on ground;

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- 2. Ground speed *V*;
- 3. Flight path angle γ ;
- 4. Center of gravity altitude above the ground *h*;
- 5. Mass *m*.

The take-off state equations are then written in the following compact form $\dot{x} = f(x, u)$ that can be expressed as [28]:

$$\begin{cases} \dot{s} \\ \dot{V} \\ \dot{\gamma} \\ \dot{h} \\ \dot{m} \end{cases} = \begin{cases} f_1(V) \\ f_2(V, \gamma, h, m; \alpha) \\ f_3(V, \gamma, h, m; \alpha) \\ f_4(V, \gamma) \\ f_5(V, \gamma, h) \end{cases}$$
 with
$$\begin{cases} x_1 = s \\ x_2 = V \\ x_3 = \gamma \\ x_4 = h \\ x_5 = m \end{cases}$$
 and $u = \alpha$ (1)

where the unknown $x = [x_1, x_2, x_3, x_4, x_5]^T$ are the vector of state variables, and the input u(t) is a given function of time that corresponds to an assumed angle of attack time history during take-off. The right-hand side of system (1) is defined by the following functions:

$$f_1(V) = x_2 \tag{2a}$$

$$f_{2}(V, \gamma, h, m; \alpha) = \frac{g}{W} \begin{cases} T(x_{2}) - D(x_{2}, x_{3}, x_{4}, x_{5}, u) \\ -\mu[W - L(x_{2}, x_{3}, x_{4}, x_{5}, u)] & \text{if } \mathcal{S}(x_{2}, u) < 1 \text{ (on ground)} \\ T(x_{2}) \cos u - W \sin x_{3} \\ -D(x_{2}, x_{3}, x_{4}, x_{5}, u) & \text{if } \mathcal{S}(x_{2}, u) \ge 1 \text{ (airborne)} \\ \text{if } \mathcal{S}(x_{2}, u) < 1 \text{ (on ground)} \end{cases}$$

$$f_{2}(V, \gamma, h, m; \alpha) = \frac{g}{2} \begin{cases} 0 & \text{if } \mathcal{S}(x_{2}, u) \ge 1 \text{ (airborne)} \\ I(x_{2}, x_{3}, x_{4}, x_{5}, u) & \text{if } \mathcal{S}(x_{2}, u) < 1 \text{ (on ground)} \end{cases}$$

$$(2c)$$

$$f_{3}(V, \gamma, h, m; \alpha) = \frac{g}{W x_{2}} \begin{cases} L(x_{2}, x_{3}, x_{4}, x_{5}, u) \\ +T(x_{2}) \sin u - W \cos x_{3} & \text{if } S(x_{2}, u) \ge 1 \text{ (airborne)} \end{cases}$$
(2c)

$$f_4(V,\gamma) = x_2 \sin x_3 \tag{2d}$$

$$f_5(V, \gamma, h) = \dot{m}_f(x_2, x_3, x_4)$$
(2e)

where *T* is the total thrust (for all engines set to maximum Take-off rating), *D* is the aerodynamic drag, *L* is the aerodynamic lift, *W* is the weight, and $\mu(W - L)$ is the tangential force proportional to the rolling friction coefficient μ .

Thrust calculations are performed for each engine separately and then summed together to have the total value *T*. Each thrust vector intensity is calculated by means of a known interpolating function $T_{tab}(V_a)$ based on a table lookup algorithm, where $V_a = V + V_w$ is the instantaneous airspeed and V_w is an assigned constant wind speed (horizontal component, negative in case of headwind). Consequently, the total thrust becomes a function $T(x_2)$ of the ground speed *V*. The total thrust vector is projected on the aircraft body-fixed reference frame and its components are used appropriately. The mass state function f_5 is given by the the fuel flow \dot{m}_f , which is calculated by a table lookup interpolating function included in the engine datapack. The drag *D* and lift *L*, as functions of airspeed, altitude, flight path angle, aircraft mass, and angle of attack, are given by the following conventional formulas:

$$D(x_2, x_3, x_4, x_5, u) = \frac{1}{2} \rho \left(x_2 + V_w \right)^2 S C_D(x_2, x_3, x_4, x_5, u)$$
(2f)

$$L(x_2, x_3, x_4, x_5, u) = \frac{1}{2} \rho \left(x_2 + V_w \right)^2 S C_L(x_2, x_3, x_4, x_5, u)$$
(2g)

The switching function S of aircraft velocity and angle of attack is defined as follows:

$$S(x_2, x_3, x_4, x_5, u) = \frac{L(x_2, x_3, x_4, x_5, u)}{W \cos x_3}$$
(2h)

The lift coefficient $C_L(x_2, x_3, x_4, x_5, u)$ is taken from the aircraft trimmed lift curve with high-lift devices (flaps, and slats if present) deflected in take-off positions. The same applies for the drag coefficient $C_D(x_2, x_3, x_4, x_5, u)$. This justifies the dependency of these two aerodynamic coefficients on aircraft mass. Both these coefficients are then scaled to take into account the ground effect on the induced drag, as proposed in [49].

The set of formulas (2) makes (1) a closed system of ODEs. When the function u(t) is assigned and the system is associated with a set of initial conditions, in this particular case equal to $x_0 = [0, 0, 0, 0, 0, 0]^T$, a well-posed IVP is formed, which can be solved numerically.

The function of time u(t) represents the input law of the angle of attack and is defined as follows:

$$u(t) = \begin{cases} \alpha_{\rm g} & \text{if } t < t_{\rm rot} \\ \alpha_1(t) & \text{if } t \ge t_{\rm rot} \end{cases}$$
(3)

where t_{rot} is the time during the ground roll at which the aircraft rotation starts, that is, when *V* reaches a given value V_{rot} called rotation speed. The function u(t) is represented in Figure 3. In Equation (3), the methodology assumes a constant angle of attack α_g during the ground roll phase up to the rotation speed, and a given non-zero law $\alpha_1(t)$ for the post-rotation angle of attack time history. After the rotation, the angle of attack changes according to an assigned initial value of its time derivative $\dot{\alpha}_0$, which decreases with time according to the following law:

$$\dot{\alpha} = \dot{\alpha}_0 \ (1 - k_\alpha \, \alpha) \tag{4}$$

that is, as a function of the instantaneous angle of attack, until the time t_{hold} is reached. In this particular instant the aircraft achieves the maximum admissible lift coefficient in take-off configuration, which is set by default at 90% of the maximum achievable take-off lift coefficient. In Equation (4), the slope k_{α} and the initial angle of attack time derivative $\dot{\alpha}_0$ are assigned as inputs. From time t_{hold} onward, the pilot keeps the angle of attack constant for an assigned time interval Δt_{hold} , during which the airplane decelerates due to a higher induced drag. After this short time interval, the pilot must reduce the angle of attack in order to contain the deceleration. Hence, a negative time derivative $\dot{\alpha}_{red}$ is considered after time $t_{hold} + \Delta t_{hold}$, assumed constant for simplicity. Finally, since the decrease in angle of attack provides also for a reduction in lift coefficient, the time t_{climb} will be reached when the load factor is reduced to a value of 1. This means that a balance of forces perpendicular to the flight path has been achieved and $\dot{\alpha}$ returns to a value of 0. The model assumes a steady climbing flight after time t_{climb} .

During the simulation, the fuselage attitude angle $\theta = \gamma + \alpha$ is constantly monitored to ensure the absence of tail strike. If the tail touches the ground a visual warning is launched by the calculation module.

The calculation of take-off distance in OEI condition is quite the same as the nominal AEO case, with the difference being that when one engine becomes inoperative during the maneuver there is a discontinuity in thrust, and a drag increment due to the failed engine [50]. In the event of an engine failure during the take-off ground run, the pilot must decide whether to continue the take-off, or instead, abort the maneuver and decelerate to a stop. Obviously, if the engine failure occurs when the aircraft is traveling very slowly, the aircraft should be kept on the ground and brought to a stop at some safe location off the runway. Conversely, if the engine failure occurs when the aircraft is faster than the decision speed, the take-off should be continued. The designer must provide a means for deciding whether it is safer to reject the take-off or continue the maneuver.



Figure 3. Qualitative representation of the angle of attack input law.

The critical velocity, denoted as V_{act} , is the velocity at which action is done. The time between the recognition of an engine failure, which occurs at V_{ef} , and the critical velocity V_{act} , when action is performed, is required to be more than one second. Generally, this time period, which is set by the reaction time of the average pilot, is taken to be about $1 \text{ s} \div 2 \text{ s}$. If the pilot's decision is to continue the take-off with one engine inoperative, the distance to the point where lift-off speed V_{LO} is achieved, and to the subsequent climb-out to 35 ft height above the runway, will obviously be longer than the case with all engines operating. The calculation of the take-off distance in this situation is quite the same as the one that determines the nominal take-off length, with the difference being that now there is an abrupt change in total thrust time history. In particular, individual contributions to $T(x_2)$ are still read from the database but considering a number of engines reduced by one from the time t_{ef} at which the engine failure occurred.

On the other hand, in case of rejected take-off, the pilot will apply the necessary braking procedures in order to get the maximum allowed deceleration while maintaining adequate control of the airplane's motion. From time t_{ef} when the engine failure occurs, i.e., when velocity assumes a value V_{ef} , until the pilot reacts by activating brakes, there is only a discontinuity in thrust. After an assigned time interval in which the pilot decides to abort the take-off, the thrust is set to minimum (ground idle engine rating), brakes are activated, and a higher friction coefficient is set. During this phase, the Equation (2b) changes in the following way:

$$f_2(x, u) = \frac{g}{W} \left\{ -D(x_2, u) - \mu_{\text{brakes}} [W - L(x_2, u)] \right\}$$
(5)

where μ_{brakes} is bigger than μ and it is usually about 0.3 or 0.4.

Instead of considering the limiting cases of an aborted take-off at low V_{act} and a OEI take-off at high V_{act} , it is useful to determine the critical velocity at which the distance required to continue the take-off with one engine inoperative equals the distance required to safely abort it. This velocity is the decision speed named V_1 by regulations, while the related distance is the balanced field length, BFL. To calculate this distance and the related velocity, both the OEI take-off distance and the aborted take-off distance are estimated at different V_{act} . These two distances are then plotted against the corresponding engine failure speeds, and the intersection of the two curves, at which the two distances are the same, defines the BFL and the V_1 (see Figure 4).

Although JPAD provides for default values for most of the inputs necessary to perform take-off simulations, the user has the possibility to manually assign each of them. The list of inputs to the take-off analysis module is reported in Table 1. The user can define the desired percentage of the

take-off stall speed required to calculate the rotation speed. However, according to FAR regulations [51] (part 25, subpart B, paragraph 25.107), the rotation speed may not be less than V_1 nor less than 1.05 times the minimum control speed. Furthermore, regulations define a minimum safety speed V_2 (both in AEO and OEI conditions) equal to at least 1.13 times the take-off stall speed, in cases of airplanes with two or three engines, and 1.08 times the take-off stall speed, in cases of aircraft with more than three engines. To ensure that those conditions are satisfied, the take-off calculation module of JPAD firstly calculates $V_{\rm MC}$ and BFL, along with the rotation speed necessary to fly over the obstacle at 1.13 times the take-off stall speed in OEI condition; successively, using those velocities, the software verifies whether or not the desired rotation speed may be feasible. In case of an unfeasible user-defined rotation speed, the most limiting one will be chosen.



Figure 4. A220-300 balanced field length and decision speed calculation—JPAD.

 Table 1. Summary of take-off simulation input parameters.

Input Variables	Description
$V_{ m w}$	Wind speed along runway (positive in case of tailwind)
μ	Wheel rolling friction coefficient (constant value or function of speed)
$\mu_{\rm b}$	Wheel braking friction coefficient (constant value or function of speed)
$\Delta t_{\rm hold}$	Time interval in which the pilot must hold the bar
$\alpha_{ m g}$	Aircraft angle of attack on the ground
h _{obstacle}	Obstacle height
k _{rot}	Percentage of the stall speed which defines the rotation speed
ά ₀	Initial value of the angle of attack time derivative
$k_{C_{I \max}}$	Safety margin with respect to the max lifting coefficient
k _{D,OEI}	Drag increment due to failed engine
k _α	Slope of the angle of attack time derivative in Equation (4)

Take-off simulations are hence reliable when the V_{MC} is correctly evaluated. This speed is the calibrated airspeed below which the airplane's directional or lateral control, on the ground or airborne, can no longer be maintained by the pilot after the failure of the most critical wing-mounted engine, as long as the thrust of the opposite engine on the other wing is at the maximum take-off setting (see Figure 5). Regulations define several different types of V_{MC} , but the most important one for multi-engine airplanes is the minimum control speed in air, V_{MCa} . This airspeed dictates a strong sizing criterion for vertical tails and for the aerodynamic flight control surfaces, especially for the rudder which is used to compensate the yawing moment caused by thrust asymmetry. The quantity V_{MCa} is the minimum speed at which a full rudder will be necessary to fly with a constant heading and with leveled wings (with gears retracted). In particular, engineers have to make sure that their design complies with requirements in terms of V_{MCa} in the following operating conditions:

- 1. One engine inoperative;
- 2. Thrust at take-off setting (maximum continuous thrust or APR setting);
- 3. Maximum rudder angle deflections;
- 4. Most unfavorable center of gravity position.

A visual representation of the forces *T* and Y_V determining the airplane equilibrium in yaw at speed V_{MCa} is provided by Figure 5. The critical engine, which is the most distant from the center of gravity, generates a thrust that decreases with airspeed, while the yawing moment $\mathcal{N}_V = Y_V \cdot l_V$ of the vertical tail may be expressed as:

$$\mathcal{N}_{\rm V} = \frac{1}{2} \rho \, V_{\rm MCa}^2 \, S \, b \, C_{\mathcal{N}_{\delta_{\rm r}}} \, \delta_{\rm r} \tag{6}$$

The most important parameters that characterize the aerodynamics of directional control are:

- 1. The vertical tail aspect ratio;
- 2. The ratio between the vertical tail span and the fuselage diameter at vertical tail aerodynamic center;
- 3. The horizontal tail position.



Figure 5. Qualitative representation of a two-engine aircraft with one engine inoperative and with a fully deflected rudder to ensure a constant heading.

The wing has a negligible effect, because of its distance from the asymmetric flow field induced by the rudder. The rudder control power $C_{N_{\delta_r}}$ is calculated as follows [52]:

$$C_{\mathcal{N}_{\delta_{\mathrm{r}}}} = C_{L_{\alpha},\mathrm{V}} \, K_{\delta_{\mathrm{r}}} \, K_{b} \, \tau_{\mathrm{r}} \, \frac{S_{\mathrm{V}}}{S} \frac{l_{\mathrm{v}}}{b} \, \eta_{\mathrm{v}} \tag{7}$$

Here $C_{L_{\alpha},V}$ is the isolated vertical tail lift curve slope, K_{δ_r} is the interference factor due to rudder deflection, K_b is a rudder span effectiveness factor, τ_r is the rudder effectiveness, η_v is the vertical tail dynamic pressure ratio, and $S_V l_V / (Sb)$ is the vertical tail volumetric coefficient (l_V is the distance from the aerodynamic center of the vertical tail to the center of gravity of the airplane, as shown in Figure 5). The K_b factor is a function of the rudder span-wise extension, as proposed in [53], while the rudder effectiveness τ_r can be assigned as a constant or as a function of the rudder deflection according

to well known classical semi-empirical approaches found in the literature [54,55]. Finally, the factor K_{δ_r} is expressed as

$$K_{\delta_r} = \begin{cases} 1.07 \left(1 + \frac{K_{\rm FV} - 1}{2.2} \right) & \text{for body mounted tail} \\ (1.33 - 0.09 \,\mathcal{R}_{\rm V}) \left(1 + \frac{K_{\rm FV} - 1}{2.2} \right) & \text{for T-tail configuration} \end{cases}$$
(8)

where \mathcal{R}_{V} is the vertical tail aspect ratio and K_{FV} is defined as the ratio between the yawing moment coefficient of the fuselage-vertical tail combination and the yawing moment coefficient of the isolated vertical tail. The value of K_{FV} is obtained from a surrogate model named VeDSC [52] that takes into account the interference effects due to mutual positions of the fin, fuselage, and horizontal empennage.

3.2. Landing Simulation Model

For the landing characteristics, JPAD also provides a simulation-based design approach involving the resolution of an ODE system. Landing simulations start at t = 0 s with the airplane at 1500 ft above the runway; the approach phase begins in steady flight conditions. The overall maneuver is the sequence of

- 1. A stabilized approach descending down to the conventional obstacle height of 50 ft;
- 2. A final approach down to 20 ft—that is, a smooth rotation in pitch with negligible initial variation of flight path angle;
- 3. A flare, with a smooth reduction of flight path angle evolving progressively into an almost horizontal trajectory;
- 4. A touch down and transition to ground roll;
- 5. A ground roll decelerating to a stop on the runway.

According to FAR regulations [56] (part 25, subpart B, paragraph 25.125), during the stabilized approach the aircraft must maintain a calibrated airspeed of not less than 1.23 times the 1-g stall speed in landing configuration; this speed must be kept all the way down to the altitude of 50 ft. Furthermore, the simulation model assumes a constant flight path angle γ for the approach, which can be assigned by the user (a typical value is -3 deg). This angle determines the amount of thrust necessary in the simulation to keep a stabilized glide path.

At the landing obstacle altitude of 50 ft the aircraft begins the final approach down to the initial flare rotation altitude assumed to be at 20 ft above the ground, a height suggested in [57] as an averaged value for transport aircraft. In this phase, the aircraft speed must be kept almost constant and the overall thrust is changed to the flight idle setting for each engine. As a consequence, the angle of attack begins to rise during the final approach to provide for the amount of lift necessary to keep the flight path angle constant.

During the flare rotation a smooth transition from a normal approach attitude to a landing attitude must be accomplished by gradually rounding out the flight path to one that is parallel with the ground, and within a few inches above the runway. During this rotation the angle of attack increases, providing for higher lift and a higher induced drag resulting in a deceleration of the aircraft. At the end of the flare the airplane must touch the ground with its main landing gears and a with a reasonably low value of the vertical speed. A typical value of the descent speed at touchdown is between 2 and 3 ft/s [58]. However, as found in [58], service experience on various families of Boeing aircraft indicates that most flight crews report a hard landing when the sink rate exceeds approximately 4 ft/s. In addition, FAR regulations [59] (part 25, subpart C, paragraph 25.473) specify a limit descent velocity of 10 ft/s at the design landing weight or a limit descent velocity of 6 ft/s at the design take-off weight. To allow the user to investigate different landing scenarios, the target rate of descent at touchdown can be selected as input parameter among the ones in Table 2.

Table 2. Landing simulation touchdown types.

Touchdown Type	Target Rate of Descent
Typical	3 ft/s
Perceived hard	4 ft/s
Certification hard with reduced descent speed	6 ft/s
Certification hard with maximum descent speed	10 ft/s

Finally, after the touchdown, and after few seconds of wheel free-roll, the pilot must apply breaking to all wheels, deflect all spoilers and adjust each engine setting to ground idle. The simulation ends when the aircraft speed reaches a value of zero.

The equations of motion in case of landing are the following, where t_{td} is the touchdown time:

$$f_1(V) = x_2 \tag{9a}$$

$$f_{2}(V, \gamma, h, m; \alpha) = \frac{g}{W} \begin{cases} T(x_{2}) \cos u - W \sin x_{3} \\ -D(x_{2}, x_{3}, x_{4}, x_{5}, u) & \text{if } \mathcal{S}(x_{2}, u) \geq 1 \text{ (airborne)} \\ T(x_{2}) - D(x_{2}, x_{3}, x_{4}, x_{5}, u) \\ -\mu [W - L(x_{2}, x_{3}, x_{4}, x_{5}, u)] & \text{if } \mathcal{S}(x_{2}, u) < 1 \text{ (on ground)} \\ \int L(x_{2}, x_{3}, x_{4}, x_{5}, u) \end{cases}$$
(9b)

$$f_{3}(V, \gamma, h, m; \alpha) = \frac{g}{W x_{2}} \begin{cases} +T(x_{2}) \sin u - W \cos x_{3} & \text{if } \mathcal{S}(x_{2}, u) \geq 1 \text{ (airborne)} \\ 0 & \text{if } \mathcal{S}(x_{2}, u) < 1 \text{ (on ground)} \end{cases}$$
(9c)

$$f_4(V,\gamma) = x_2 \sin x_3 \tag{9d}$$

$$f_5(V, \gamma, h) = \dot{m}_{\rm f}(x_2, x_3, x_4)$$
 (9e)

The aircraft drag coefficient, calculated from the input drag polar curve in landing configuration taking into account also the ground effect, is incremented during the ground roll phase to model the effect of spoiler deflection. This additive contribution is calculated as proposed in [60], using each spoiler's maximum deflection angle specified in the JPAD aircraft data model. Similarly, spoiler deflection also affects the lift coefficient, which is reduced by an amount dependent on each spoiler span ratio [60]. This effect provides for an increased wheel friction force, and so more effective deceleration. The increase in braking effectiveness due to spoilers may also be configured in JPAD by the user through the performance input file.

To take into account for thrust reverse during the landing simulation, the ground idle engine rating used for the ground roll phase can be modified by means of a dedicated calibration factor provided in the performance analysis input file. Otherwise, the ground idle rating of the JPAD engine database can be manually edited, including negative thrust ratios.

The function u(t) in system (9), still represents the input law of the angle of attack as a function of time and is constructed as follows:

- 1. At the beginning of the initial approach the angle of attack is calculated from the equilibrium lifting coefficient in landing configuration associated with the initial aircraft weight and with the prescribed approach speed of 1.23 times the stall speed at landing.
- 2. During both initial and final approach phases, the model implements a proportional control that senses the flight path angle $\gamma = x_3$ and regulates α to keep $\dot{\gamma}$ equal to zero.
- 3. From the height of 20 ft to touchdown a special algorithm calculates $\alpha(t)$ for the flare segment; this procedure is explained below in more detail.
- 4. Once the aircraft has touched the ground, a user-defined, constant value of the angle of attack is considered (this latter is set to zero degrees by default).

The flare rotation plays a very important role in the landing simulation since it must provide for a reasonable value of the vertical speed at touchdown and at the same time it has to ensure that the aircraft effectively touches the ground with a flight path angle very close to zero. The key parameter is the angle of attack time derivative, which is unknown. Thus, the following iterative process is applied to find a constant $\dot{\alpha}$ during flare that makes the overall landing maneuver compliant with all the required conditions (see also Figures 6 and 7):

- 1. Two initial attempts are made assuming the impossible case of a null angle of attack time derivative and the case of $\dot{\alpha} = 3 \text{ deg/s}$ during the flare rotation. These attempts are used to make a forecast of the required pitching angular velocity to match the target value of the rate of descent. The forecast is made by using linear interpolations or extrapolations.
- 2. In case the simulation step should overshoot the user-defined limitation on the allowed maximum achievable lifting coefficient during landing rotation (by default set to 90% of the landing maximum lift coefficient), a warning is launched and the last calculated lift coefficient is considered.
- 3. In case the aircraft should touch the ground with an angle of attack bigger than the fuselage upsweep angle, a tail strike warning is launched. At the same time, if the required angle of attack time derivative should provide for an angle of attack at touchdown lower than 0 deg, a nose strike warning is launched. This feature provides for an important aircraft design check, monitoring whether the aircraft has been designed with an adequate value of the aerodynamic efficiency in landing (higher lift capabilities lead to lower angles of attack at touchdown, while poor lift capabilities provide for higher angles of attack).
- 4. If the aircraft reaches the required altitude and at the same time provides for a touchdown vertical speed below or equal to the threshold, the flare simulation ends, and the ground roll phase can start.
- 5. If flare rotation simulation fails, the JPAD performance manager switches the air distance calculation to the simpler circular arc approach proposed in [58] before then moving on to the integration of the ODE set for the final ground segment.



Figure 6. A220-300 aircraft angles during the landing simulation—JPAD.

As for take-off simulations, JPAD provides default values of most of the simulation inputs for the landing simulation as well. However, the user has the ability to manually assign each of them. The list of inputs necessary to accomplish a landing analysis is reported in Table 3.



Figure 7. A220-300 aircraft angular velocities during the landing simulation—JPAD.

Table 3. Summary of landing simulation input parameters.

Input Variables	Description
Туре	Touchdown type, defining the target rate of descent (see Table 2)
$V_{\rm w}$	Wind speed along runway
μ	Wheel rolling friction coefficient (constant value or function of speed)
$\mu_{\rm b}$	Wheel braking friction coefficient (constant value or function of speed)
k _{LND,weight}	Percentage of the max take-off weight to be used for the initial approach phase
$h_{\rm LND, start}$	Initial landing altitude (by default set to 1500 ft)
hobstacle	Obstacle height
$\gamma_{approach}$	Flight path angle (by default set at $-3 \deg$)
$k_{C_{L,\max}}$	Safety margin with respect to the max lifting coefficient
k _{approach}	Percentage of the stall speed defining the approach speed
k _{flare}	Percentage of the stall speed defining the flare speed (circular arc approach)
k _{touchdown}	Percentage of the stall speed defining the touchdown speed (circular arc approach)

Starting from both take-off and landing simulations, a specific performance module has been completely dedicated to the calculation of certification take-off and landing noise trajectories. In both cases, part 36, appendix A, of the FAR [61] specifies all conditions under which aircraft noise certification tests must be conducted.

3.3. Take-Off and Landing Simulation Model for Noise Certification

The procedure for take-off noise trajectory analysis is almost the same as the AEO normal take-off, with the important difference that all simulations must be carried out considering an ISA temperature deviation of +10 °C. In addition to the normal take-off simulation, once the aircraft passes the obstacle at 35 ft, landing gear must be retracted. This is simulated by linearly reducing the current drag coefficient, from the trimmed drag polar in take-off configuration, of a quantity equal to the overall landing gear's drag coefficient. The time interval assumed to perform this reduction is set by default to 12 s; however, the user can change this value in the performance analysis configuration file.

The time history of the angle of attack defined in Figure 3 is used to model the input variable u(t) up to the obstacle altitude. From there, the instant at which the acceleration reaches a value near to zero is monitored to estimate the aircraft speed to be maintained during the rest of the simulation. This velocity must be in the interval $[1.13V_{s,TO} + 10 \text{ kts}, 1.13V_{s,TO} + 20 \text{ kts}]$. To ensure this condition in simulation, an iterative process is carried out by varying the rotation speed V_{rot} appropriately,

while making sure that in all cases the speed profile complies with all the limitations described for a normal take-off. Thus, if the calculated climb speed is less than the lower bound of the prescribed interval, the aircraft's rotation speed is increased to allow for a higher lift-off speed. The rotation speed is reduced in the opposite case.

To maintain a steady climb after the obstacle, a proper law $\alpha(t)$ has to be established in order to get a constant climb speed. To ensure such behavior, the model implements a proportional control that senses the flight speed *V* and the rate of climb *V* sin γ and regulates α to keep their variations close to zero. Two scenarios are considered at this point: a 100% take-off thrust simulation and another one with a thrust cutback occurring at a specific altitude prescribed by regulations. The cutback altitude is selected as follows: 689 ft (210 m) for airplanes with more than three engines; 853 ft (260 m) for airplanes with three engines; and 984 ft (300 m) for airplanes with fewer than three engines. The cutback thrust setting must be selected according to the FAR [62] (Appendix B, Part 36, Section B36.7). Upon reaching the cutback altitude, the aircraft thrust is reduced, but the total amount *T* must not be less than the thrust required to maintain either of the following (whichever is greater): a climb gradient of 4%, and in the case of multi-engine airplanes, level flight with one engine inoperative.

In both scenarios, 100% thrust and cutback, the simulation continues until the aircraft reaches a user-defined horizontal distance from the starting point, set by default at 8000 m. The 100% thrust case is related to the definition of a lateral noise certification point, which is that location on ground where the highest noise level is measured among all the possible measuring stations located on a line parallel to the runway center line (at a side distance of 450 m). The cutback thrust case is related to the flyover noise certification point which is set by the FAR at 6500 m from the brake-release point along the runway's center line. Ending the simulation further than 6500 m ensures that the aircraft passes above the flyover certification point. A representation of all noise certification measurement points is provided in Figure 8, while a complete overview of the input data needed to perform both take-off noise trajectories simulation is reported in Table 4.



Figure 8. Certification noise measurement points.

Table 4. Summary of parameters used in the simulation-take-off noise trajectories.

Input Variables	Description
X _{end}	Ground distance at which the simulation ends.
$n_{ m cutback}$ $\Delta t_{ m retraction}$	Landing gear's retraction time interval.
$\Delta t_{\rm cutback}$	Time interval to pass from 100% to the cutback thrust setting.

Landing noise trajectory simulations are practically the same as for normal landings. However, the need to only model the trajectory up to the end of the final approach allows one to completely ignore the flare and ground roll segments. According to FAR (appendix A, part 36) the approach noise certification point is defined as the location at 2300 m from the brake release (or 2000 m from the runway start) which corresponds to an aircraft altitude above the ground of 120.50 m (see Figure 8).

Both take-off and landing noise trajectories calculated using the proposed approach can be used as starting points for complete aircraft noise assessments. Thus, JPAD has been provided with an interface

to an external tool named ATTILA, developed at the University of Naples Federico II, dedicated to this specific type of analysis. The noise topic lies outside the scope of this paper; however, a description of the prediction methodology implemented in this software can be found in [63], both in terms of airframe and engine noise.

4. A Take-Off and Landing Performance Simulation Example

This section presents an application of the methodologies described above and demonstrates the capabilities of JPAD concerning typical preliminary design studies. Results from the simulations of both take-off and landing phases of a regional turbofan aircraft model similar to the Airbus A220-300 will be shown. For sake of completeness, simulation details concerning the certification noise trajectories for this aircraft model will be provided as well. Those data play a very important role in the noise assessment of an aircraft model, and in fact, they represent some of the major input data that JPAD can pass to the environmental noise analysis tool ATTILA mentioned in previous section. However, thanks to the simulation-based nature of the implemented calculation methodology, output data from the JPAD certification noise trajectory analysis can be used as a starting point for any tool dedicated to the aircraft noise estimation.

The selection of the Airbus A220-300 as the reference platform was driven by two main factors: within several studies, the authors have deeply analyzed this aircraft, which represents the state-of-the-art of the current regional jet market; on the other hand, a reliable geared turbofan engine database similar to the PW1524G has been generated by the authors as a result of their involvement in recent research efforts.

The first step of this case study concerned the generation of the aircraft parametric model. Besides the main geometrical data reported in Table 5 and engine data reported in Table 6, most of the inputs needed by JPAD to define a complete aircraft model have been derived directly from the A220-330 three-view drawings through a digitization process. The cabin layout has been modeled by taking as reference the seat map presented in [64], while data concerning airfoils of lifting surfaces have been taken from [65], considering the SC(2)-0714 airfoil as wing root and kink sections and the SC(2)-0710 airfoil as tip section. In addition, a NACA 0012 has been used as root and tip airfoil for both horizontal and vertical tails.

Overall length	38.71 m
Overall height	11.5 m
Wingspan	35.1 m
Wing area	112.3 m ²
Fuselage diameter	3.7 m
Cockpit crew	2 pilots
Cabin crew	3 (minimum)
Passengers	130 (2-class)–160 (full economy)
Seat configuration	2–3 (full economy)
Seat pitch	81.3 cm (full economy)
Seat width	47–48 cm (full economy)
Cargo volume	31.6 m ³
Cabin width	3.28 m
Cabin height	2.13 m

Table 5. A220-300 main geometrical data and interior arrangements [64,66,67].

The resulting aircraft model produced by JPAD is shown in Figure 9, where a three-view representation and a rendering of the automatically generated CAD model have been collected.

Once the aircraft model was created, the second step of this case study was related to the configuration of both take-off and landing simulations input files. It must be noted the take-off and landing presented in this paper were performed at the end of a complete JPAD multi-disciplinary analysis cycle, as shown in Figure 2. Thus, the performance module inherited all weights and trimmed

aerodynamic data coming from other JPAD analysis modules. For the sake of clarity, Table 7 shows a comparison between the calculated aircraft weights and the public domain data available for the Airbus A220-300 with respect to a design mission range of 3100 nm.

	PW1521G	PW1524G
Stages	1-GearBox-3-8-2-3	1-GearBox-3-8-2-3
BPR	12:1	12:1
Overall length	3.184 m	3.184 m
Diameter, fan tip	185.42 cm	185.42 cm
Dry mass	2177 kg	2177 kg
SL Static Thrust, Take-off	21,970 lbf	24,400 lbf
SL Static Thrust, Max Continuous	20,760 lbf	23,050 lbf
SL Static Thrust, Take-off Flat Rating	ISA+30 °C	ISA+30°C
SL Static Thrust, Max Continuous Flat Rating	ISA+25 °C	ISA+25 °C
Max Permissible ITT, Take-off	1054 °C	1054 °C
Max Permissible ITT, Max Continuous	1006 °C	1006 °C
Max Permissible Low Pressure Spool Speed	10,600 rpm	10,600 rpm
Max Permissible High Pressure Spool Speed	24,470 rpm	24,470 rpm
Min Low-Pressure Spool Speed, Flight Idle	1991 rpm	1991 rpm
Min Low-Pressure Spool Speed, Ground Idle	1574 rpm	1574 rpm
Min High-Pressure Spool Speed, Flight Idle	13,264 rpm	13,264 rpm
Min High-Pressure Spool Speed, Ground Idle	13,264 rpm	13,264 rpm

Table 6.	A220-300's	main	engine	data	[68,69]	ŀ
			()		L / 3	

Table 7. Main output data concerning the JPAD weight analysis of the A220-300 parametric model, compared with publicly available data.

Output Data	JPAD	A220-330	Difference (%)
MTOW	68,272 kg	67,585 kg	-1.01%
MLW	58,036 kg	58,740 kg	-1.19%
Max fuel mass	17,739 kg	17,726 kg	-1.00%
Design mission fuel mass	16,833 kg	_	—
MZFW	55,694 kg	55,792 kg	-0.17%
Max payload	18,711 kg	18,711 kg	0%
Design payload	14,462 kg	_	—
OEW	36,983 kg	37,081 kg	-0.39%
Trapped fuel and oil mass	341 kg		—
Crew mass	517 kg		—
Operating items mass	2096 kg		—
MEW	30,705 kg		—
Structural mass	19,841 kg	—	_

Typical simulation parameters have been used for take-off and landing analyses, as well as other parameters suggested by FAR. A summary of these data is provided in Table 8.

It must be noted that the flight path angle of -4 deg reported in Table 8 was selected as the one providing for the best agreement with public data concerning the landing field length of the Airbus A220-300.

For sake of clarity, emissions data reported for both take-off and landing simulations have been obtained from dedicated lookup tables included in the JPAD engine database. Those data, as well as thrust and SFC values, have been derived by the authors in the context of past research activities and have been validated by comparison to GasTurb software [70] output data for an engine model similar to the PW1524G used for the Airbus A220-300.



Figure 9. A220-300 3-view and CAD model representation made by JPAD. (**a**) Top view; (**b**) side view; (**c**) front view; (**d**) CAD model.

In terms of take-off, Table 9 reports a summary of the JPAD simulation output, while Figure 4 illustrates the calculations of the balanced field length and of the decision speed V_1 . Furthermore, Figure 10 shows the variation of normalized rotation speed $V_{rot}/V_{s,TO}$, as well as the normalized take-off safety speed $V_2/V_{s,TO}$, with increasing engine normalized failure speed $V_{ef}/V_{s,TO}$. As can be seen, the value of the $V_2/V_{s,TO}$ ratio is always above the minimum value of 1.13 prescribed by FAR.

The time histories of the main aircraft-related physical quantities during a take-off simulation are shown in Figures 11–15. The assumed input rotation speed ratio of 1.05 allows one to match all rotation speed checks performed by JPAD during the take-off simulation described in the previous section of this paper. The calculated BFL of 1936 m is in line with the expected value of 1890 m available for the Airbus A220-300, with a difference of about 2.4%.



Table 8. Input parameters used for take-off and landing simulations.

Figure 10. A220-300 take-off rotation speed and take-off safety speed variations with engine failure speed—JPAD.

 $\frac{V_{\rm MC}/V_{\rm s,TO}}{V_1/V_{\rm s,TO}}$ $\frac{V_{\rm rot}/V_{\rm s,TO}}{V_{\rm LO}/V_{\rm s,TO}}$ $\frac{V_2/V_{\rm s,TO}}{V_2/V_{\rm s,TO}}$

Take-off duration

Fuel used for take-off

Take-off NO_x emissions

Take-off CO₂ emissions

Take-off H₂O emissions

Main output data concerning the JPAD take-on simula	non of the A
Output	Value
Ground roll distance	1034 m
Rotation distance	358 m
Airborne distance	194 m
AEO take-off distance	1586 m
FAR-25 take-off distance (take-off distance times 1.15)	1824 m
BFL	1936 m
V _{MC}	54.69 m/s
V _{s.TO}	67.01 m/s
V_1	66.61 m/s
V _{rot}	70.36 m/s
V _{LO}	79.26 m/s
V_2	82.71 m/s
V _{MC} /V _{s,TO}	0.82
$V_1/V_{\rm s.TO}$	0.99
$V_{\rm rot}/V_{\rm s}$ TO	1.05

1.181.23

 $35 \mathrm{s}$

54.29 kg

1.27 kg

184.39 kg 67.87 kg

Table 9. Main output data concerning the JPAD take-off simulation of the A220-300.



Figure 11. A220-300 aircraft angles during the take-off simulation—JPAD.



Figure 12. A220-300 aircraft angular velocities during the take-off simulation—JPAD.



Figure 13. A220-300 calibrated air speed (CAS) and true air speed (TAS) during the take-off simulation—JPAD.



Figure 14. A220-300 horizontal forces during the take-off simulation—JPAD.



Figure 15. A220-300 vertical forces during the take-off simulation—JPAD.

Concerning the landing analysis, input data reported in Table 8 have been used to carry out a complete simulation considering the typical case of 3 ft/s of vertical speed at touchdown. The main output data of the simulation are provided in Table 10, while Figures 16–19 show the main physical quantities time histories. These have been reported to prove the compliance of the simulation with the specifications coming from FAR, especially the ones related to aircraft angles, speeds, and rate of descent. Moreover, the calculated landing field length of 1539 m differs from the public available A220-300 LFL value of 1509 m by less than 2%, proving the good level of accuracy reached by the proposed methodology.

Output	Value
Airborne distance	133 m
Flare rotation distance	84 m
Ground roll distance	706 m
Landing distance	923 m
FAR-25 LFL	1539 m
Total landing distance (from 1500 ft)	7313 m
V _{s,LND}	54.92 m/s
Vapproach	67.45 m/s
V _{flare}	66.72 m/s
V _{td}	65.79 m/s
$V_{\rm approach}/V_{\rm s,LND}$	1.23
$V_{\rm flare}/V_{\rm s,LND}$	1.21
$V_{\rm td}/V_{\rm s,LND}$	1.20
Vertical speed at touchdown	-0.91 m/s (-3 ft/s)
Total landing duration (from 1500 ft)	117 s
Landing duration	23 s
Total Fuel used (from 1500 ft)	40.61 kg
Total NO _x emissions	1.59 kg
Total CO ₂ emissions	128.39 kg
Total H ₂ O emissions	50.76 kg

Table 10. Main output data concerning the JPAD landing analysis of the A220-300.



Figure 16. A220-300 CAS and TAS during the landing simulation—JPAD.



Figure 17. A220-300 rate of descent during the landing simulation—JPAD.



Figure 18. A220-300 aircraft horizontal forces during the landing simulation—JPAD.



Figure 19. A220-300 aircraft vertical forces during the landing simulation—JPAD.

Finally, some of the main results of the take-off noise trajectories simulation are provided in Figures 20–23. Besides the two main trajectories (with and without a thrust cutback equal to 62% of the maximum take-off thrust), the provided charts show the evolutions of the aircraft's total thrust, aircraft angles, and the overall acceleration. In particular, as seen from Figure 23, after reaching a zero acceleration for the first time, the control law implemented for the angle of attack maintained a constant speed for the rest of the simulation. This occurred in both cases of a full thrust simulation and of thrust cutback, in agreement with the classical flight test operations.

For the sake of completeness, a comparison between publicly available noise certification data for the Airbus A220-330 with results obtained by means of JPAD using the calculated noise trajectories in combination with the ATTILA tool is provided in Table 11, for the three certification points previously discussed.



Table 11. Comparison between publicly available equivalent perceived noise level data certified for A220-330 and JPAD output using the ATTILA tool [63].

Figure 20. A220-300 calculated take-off noise trajectories with and without thrust cutback-JPAD.



Figure 21. A220-300 take-off thrust evolution during the certification of noise trajectories simulation—JPAD.



Figure 22. A220-300 aircraft angles evolution during the certification of noise trajectories simulation—JPAD.



Figure 23. A220-300 aircraft acceleration during the certification of noise trajectories simulation—JPAD.

5. Conclusions

Nowadays, preliminary aircraft design activities require reliable and fast calculation methods to quickly make performance assessments. Usually this task has been carried out using statistical or semi-empirical approaches which can give pretty accurate results in no time. However, those approaches may be inappropriate when dealing with innovative aircraft configurations or when a higher level of accuracy is required. Thanks to the continuous evolution of computer calculation capabilities, new and improved methodologies can now be implemented inside modern aircraft design software. An example of this can be found in the JPAD library presented in this paper.

In the framework of the development of JPAD, a detailed and flexible simulation-based analysis methodology for take-off and landing has been presented in this article. Some important simulation features not present in most of the currently available preliminary aircraft design software have received substantial attention.

An application of the proposed methodologies has been provided, considering as the reference aircraft model a state-of-the-art regional turbofan aircraft. Results, both in terms of take-off and landing simulations, are in line with public domain data related to this aircraft, proving the good level of accuracy reached by JPAD. Although far more detailed than classical semi-empirical approaches, the computational effort associated with the proposed methodologies is very limited. For the complete take-off analysis a simulation time of less than 1 s was observed; and 7.5 s was required by the landing simulation due to the touchdown vertical speed control. The benchmark was carried out on a personal computer with the following characteristics: i7-10875 octa-core CPU, 32 GB of RAM, and a 1TB Samsung EVO Plus SSD.

Thus, thanks to their increased level of accuracy and to their low computational load, the proposed methodologies can be easily used in complex multi-disciplinary analysis and optimization cycles usually required by typical preliminary aircraft design iterations.

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Abbreviations

The following abbreviations are used in this manuscript:

AEO All Engines Operative API Application Programming Interface APR Automatic Power Reserve ATAG Air Transport Action Group BFL. Balanced Field Length CAD Computer Aided Design CAS Calibrated Air Speed CFD **Computational Fluid Dynamics** DOC **Direct Operative Cost** DOE **Design Of Experiments** EU European Union EPNL Effective Perceived Noise Level GA Genetic Algorithm IATA International Air Transport Association ICAO International Civil Aviation Organization IVP Initial Value Problem **JPAD** Java API for Aircraft Designers

LFL	Landing Field Length
LND	Landing
LTO	Landing and Take-Off
MDAO	Multi-Disciplinary Design, Analysis and Optimization
MEW	Manufacturer's Empty Weight
MLW	Maximum Landing Weight
MTOW	Maximum Take-Off Weight
MZFW	Maximum Zero Fuel Weight
ODE	Ordinary Differential Equation
OEI	One Engine Inoperative
OOP	Object-Oriented Programming
OEW	Operating Empty Weight
PSO	Particle Swarm Optimization
RANS	Reynolds Averaged Navier-Stokes equations
RPK	Revenue Passenger Kilometers
SFC	Specific Fuel Consumption
TAS	True Air Speed
TO	Take-Off
TOFL	Take-Off Field Length

XML Extensible Markup Language

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