Observation of planar Hall effect in topological insulator—Bi$_2$Te$_3$

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ABSTRACT

Planar Hall effect (PHE) in topological insulators (TIs) is discussed as an effect that stems mostly from conduction due to topologically protected surface states. Although surface states play a critical role and are of utmost importance in TIs, our present study in Bi$_2$Te$_3$ thin films reflects the need for considering the bulk conduction in understanding the origin of PHE in TIs. This necessity emerges from our observation of an unconventional increase in the PHE signal with TI thickness and temperature where the bulk effect takes over. Here, we find an enhancement in the PHE amplitude by doubling the Bi$_2$Te$_3$ film-thickness on the Si (111) substrate—from 3 nΩ m in 14 quintuple layer (QL) to ≈ 3.1 nΩ m in 30 QL devices at B = 5 T. Also, the PHE amplitude in the 30 QL Bi$_2$Te$_3$ films grown on two different substrates, viz., Si (111) and Al$_2$O$_3$ (0001), shows an increase with temperature. Our experiments indicate that the contribution of bulk states to PHE in TIs could be significant.

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Topological insulators (TIs) have been the forerunners of research in condensed matter physics due to the plethora of possibilities that surface states offer for fundamental exploration. However, it is worthwhile to investigate the mesoscopic transport dominated by the bulk states. A phenomenon that has evoked widespread interest in recent times is the planar Hall effect (PHE), which is the development of transverse voltage in response to longitudinal current, under external in-plane magnetic field, in a configuration where transverse voltage due to Lorentz force is zero. The discovery of PHE dates back to 1954 and has been used extensively for its application to Hall sensors. PHE based magnetic random access memory devices are also known for memory storage applications. Hence, nonmagnetic materials exhibiting PHE are potential candidates for such applications since they eliminate spurious fringe field effects. PHE has been observed in a variety of systems such as ferromagnet/normal metal bilayers, ferromagnetic semiconductors, ferromagnetic metals, and topological superconductors. Recently, the effect is in the spotlight due to its role in probing topological characteristics such as chirality. In Weyl semimetals, the origin of PHE coupled with negative magnetoresistance is considered a signature of chiral anomaly. The origin of nonzero off diagonal terms in the resistivity tensor could be attributed to several mechanisms including classical orbital magnetoresistance. However, conventional PHE refers to transverse and longitudinal resistivities under in-plane magnetic field, given by the following equations, where periodicity of PHE is $\pi$:

$$\rho_{xy} = (\rho_1 - \rho_\perp) \sin \phi \cos \phi,$$

$$\rho_{xx} = \rho_\perp + (\rho_1 - \rho_\perp) \cos^2 \phi,$$

where $\phi$ is the angle between the current and magnetic field directions lying in the same plane, $\rho_{xy}$ and $\rho_{xx}$ are the transverse and longitudinal resistivities, respectively, and $\rho_1$ and $\rho_\perp$ are the longitudinal resistivities when $\phi$ is 0° and 90°, respectively.

PHE in topological insulators is believed to stem from surface state conduction. This was demonstrated by Taskin et al., where the PHE amplitude measured across the Fermi level exhibited local maxima on either side of the Dirac point in the surface state regime. Bulk crystals of Sn doped Bi$_x$Sb$_{y}$Te$_z$ also exhibit an oscillating PHE, which appears only in the topologically protected surface state regime. It is interesting to note that there is no experimental report of conventional PHE in Bi$_2$Se$_3$ despite being extensively studied. However, it does exhibit a nonlinear unconventional PHE, which refers to PHE with a periodicity of 2$\pi$. Such an unconventional PHE is also observed by Rakhmilevich et al., in Bi$_{0.22}$Sb$_{0.78}$Te$_2$/EuS, where induced ferromagnetism shows anisotropic magnetoresistance along with the PHE of periodicity 2$\pi$. Following these experiments, several
groups have worked on explaining the results theoretically: (i) Zheng et al.\textsuperscript{33} show that PHE can arise as a consequence of anisotropic back-scattering from the Dirac cone, tilted due to in-plane magnetic field. Including nonlinear terms in momentum to the surface state Hamiltonian explains the experimental result by Taskin et al., without the need to invoke scattering by impurities. (ii) Further, Nandy et al.\textsuperscript{34} model PHE in TIs in the bulk conduction limit using the Boltzmann transport equation and notice that PHE arises purely from the Berry curvature of bulk bands. (iii) A recent calculation\textsuperscript{35} using scattering theory shows that PHE in surface states of a TI stems from the transverse displacement of the dispersions under in-plane magnetic field and extends the calculations to spin–orbit coupled systems as well.\textsuperscript{46,47} We recognize that a comprehensive satisfactory understanding of PHE in topological insulators is yet to be developed. We attempt to address this and present our experimental results.

In this article, we performed PHE experiments in thin films of Bi\textsubscript{2}Te\textsubscript{3} by rotating the magnetic field in-plane by an angle \( \phi \) with respect to the direction of current. Bi\textsubscript{2}Te\textsubscript{3}\textsuperscript{36,37–44} is a three-dimensional (3D) TI with a small bulk bandgap <0.15 eV (Ref. 45) owing to which it is experimentally challenging to separate the bulk and surface contributions to the transport. An in-plane magnetic field has no orbital effect on the surface of the TI but does cause a transverse shift in the Dirac cone. Hence, the development of a response to in-plane magnetic field is intriguing.\textsuperscript{46,47} It is an interesting question to ask if PHE can be observed in a bulk conduction dominated 3D-TI. To answer this question, we examined the transport dynamics of Bi\textsubscript{2}Te\textsubscript{3}, whose relatively small bulk bandgap allows a significant mixing of the bulk and surface state signals. We investigate PHE in Bi\textsubscript{2}Te\textsubscript{3} films of two different thicknesses grown on different substrates. The following sections describe the growth of the films and the results of measurements and discuss the plausible mechanism.

High quality epitaxial films of Bi\textsubscript{2}Te\textsubscript{3} were deposited on Si (111) and Al\textsubscript{2}O\textsubscript{3} (0001) substrates using molecular beam epitaxy technique at a base pressure of \( \approx 10^{-9} \) mTorr. A constant rate ratio of 1:10 was maintained during growth of all the samples to ensure a Te rich growth atmosphere. A two-step growth process was employed. Substrate temperature was maintained at 230 °C for Al\textsubscript{2}O\textsubscript{3} (0001) and 200 °C for Si (111) optimized to attain the epitaxial film for the first 4 quintuple layers (QL). The samples were then annealed at 270 °C for 30 min, and the remaining thickness of the sample was grown at 270 °C. Thicknesses of 14 quintuple layers (QL) and 30 QL were grown on both substrates. All the samples were capped with 2 nm of Al\textsubscript{2}O\textsubscript{3}. Transport measurements were performed in a variable temperature insert cryostat coupled with the Attocube rotation stage for angle dependent scans; samples could reach a stable lowest temperature of 1.5 K. A Keithley current source (6221) and a nanovoltmeter (2182A) were used for DC resistance measurements. All the samples were manually patterned into Hall bars for measurements, thus avoiding any contamination due to lithographic processes. For the rest of the manuscript, we use the nomenclature of the samples: BS\textsubscript{1}4 and BS\textsubscript{3}0 for Bi\textsubscript{2}Te\textsubscript{3} on Si (111) of 14 and 30 QL, respectively, BA\textsubscript{1}4 and BA\textsubscript{3}0 for Bi\textsubscript{2}Te\textsubscript{3} on Al\textsubscript{2}O\textsubscript{3} (0001) of 14 and 30 QL, respectively.

Basic characteristics of the films were analyzed by XRD spectra [Fig. 1(a)], which show sharp characteristic Bi\textsubscript{2}Te\textsubscript{3} peaks. Raman spectra of the films show characteristic Bi\textsubscript{2}Te\textsubscript{3} phase as well (refer to the supplementary material). The resistivity vs temperature curves [Figs. 1(b) and 1(c)] of the two films show a metallic nature. The minor upturn in resistance at low temperatures for T <10 K may be attributed to the significant contribution from impurity bands\textsuperscript{48,49} or the e–e interaction. RHEED images shown in the inset exhibit highly epitaxial growth. We also remark that both films show hexagonal symmetry corresponding to the substrate indicative of epitaxial growth. Mobility calculated from the Hall measurements for BA\textsubscript{1}4 is higher than that of BS\textsubscript{1}4 [Fig. 1(d)]. This may be attributed to compressive strain on the films due to lattice mismatch, which is 9% for Bi\textsubscript{2}Te\textsubscript{3} grown on Al\textsubscript{2}O\textsubscript{3} and 18% on Si substrates.\textsuperscript{50,51}

The key result of our work is the demonstration of the planar Hall effect in Bi\textsubscript{2}Te\textsubscript{3} and its uncommon response to temperature and film-thickness. We measure the transverse resistivity as a function of \( \phi \) [inset of Fig. 2(a)], \( \rho_{xy} \) varies as \( \sin 2\phi \) with a period of \( \pi \) [Fig. 2(a)], as expected for the case of conventional PHE. We observe that the PHE amplitude (\( \rho_{xy} \) at \( \phi = 45° \)) varies monotonically with field and fits to the \( B^2 \) functional form [inset of Figs. 2(b) and 2(c)]. The longitudinal magnetoresistance (\( \rho_{xx} \)) varies as \( \cos^2 \phi \) consistent with Eq. (1) for conventional PHE (refer to the supplementary material). The PHE amplitude monotonically decreases with an increase in temperature [Fig. 2(d)], indicating that either (i) surface state contribution to the PHE signal is decreasing with temperature or (ii) bulk disorder-induced thermal excitations decrease the PHE signal from the bulk states of BA\textsubscript{1}4 and BS\textsubscript{1}4 devices (refer to the supplementary material). PHE amplitude vs T of Bi\textsubscript{2}Te\textsubscript{3}/Si (111)]. In the low mobility BS\textsubscript{1}4, either or both of the above effects may dominate causing a decrease in PHE amplitude with temperature. However, in the case of BA\textsubscript{1}4 devices having six times higher mobility than in BS\textsubscript{1}4, the contribution of the latter effect may be less, suggesting a more dominant surface contribution to the total PHE amplitude. This may also explain the larger magnitude of the PHE amplitude in BA\textsubscript{1}4 compared to that of BS\textsubscript{1}4. Experiments by Taskin et al.\textsuperscript{36} and Wu et al.\textsuperscript{47} have demonstrated that PHE dominated by surface states decays with temperature in
Bi$_2$SbTe$_3$ and Bi$_{1.5}$Sb$_{0.5}$Te$_2$S, respectively. Alternatively, the difference in PHE amplitude of the two devices can be explained from the chemical potential arguments. The chemical potential in BA14 is lower than that in BSI14, suggesting a larger surface contribution calculated using free-electron approximation ($m^* = 0.1 m_e$, where $m_e = 9.1 \times 10^{-31}$ kg and $m^*$ is the effective mass) to be lying 0.34 and 0.58 eV above the conduction band edge for BA14 and BSI14 devices, respectively. We remark that this is only a crude approximation since it does not consider the precise dispersion relation for each sample.

It is fruitful to study the magnetotransport in the out-of-plane magnetic field direction to understand the interplay of scattering from scalar impurities and spin–orbit coupling. As shown in Figs. 3(a) and 3(b), the resistivity of the sample shows a cusp at a low field when the sample is perpendicular to the plane of magnetic field, indicating weak antilocalization (WAL). By rotating the sample from out-of-plane to in-plane magnetic field configuration ($\theta$ is rotated from 90$^\circ$ to 0$^\circ$), we find that the cusp vanishes and resistivity decreases. The magnetoconductance cusp (insets of Fig. 3(a) and (b)) is fit to the Hikami–Larkin–Nagaosa (HLN) model [Eq. (2)]

$$\Delta \rho_{xx} = \rho(B) - \rho(0) = \frac{e^2}{\pi h} \left[ \psi \left( \frac{1}{2} + \frac{B_0}{H} \right) - \log \left( \frac{B_0}{H} \right) \right],$$

where $B_0 = \frac{\hbar}{e L_\rho}$ and $\Psi$ is the digamma function (refer to the supplementary material for details on fitting routine). The coherence length $l_\rho$ at 1.7 K is $\approx 160$ and 200 nm for BSI14 and BA14, respectively [Fig. 3(d)]. The power law $l_\rho \propto H^{-\alpha}$ fit to the temperature dependence of $l_\rho$ shows that the dephasing mechanism is likely to be e–e interaction. $\alpha$ [Fig. 3(c)] is $\approx 0.19$ and 0.23 for BA14 and BSI14, respectively. In the ideal case, the value of $\alpha$ is expected to be 1/2 for conduction due to single coherent channel. However, the observed lower values of $\alpha$ indicate that the bulk conduction dominates the transport in our Bi$_2$Te$_3$ samples irrespective of the substrate. WAL signal decays for $T > 10$ K; however, the PHE persists up to much higher temperatures, implying that the origin of the two effects is uncorrelated. For a comprehensive picture of the various parameters of the Bi$_2$Te$_3$ devices discussed in the manuscript, we illustrate the comparison in Table I.

Since it is important to understand if the origin of PHE stems from the surface or the bulk, we examine PHE in thicker samples (thickness = 30 QL) of Bi$_2$Te$_3$ maintaining exactly the same growth conditions as the respective thinner samples. Figure 4(a) shows the transverse resistivity as a function of magnetic field, which exhibits a conventional behavior: PHE amplitude varies as $B^2$ and is sinusoidal with respect to $\phi$. We compare the relative PHE amplitudes of the thicker and thinner film devices [Fig. 4(b)]. It is intriguing that the PHE amplitude of the BSI30 sample is higher than that of the BSI14 at $B = 5$ T. However, the magnitude of the PHE amplitude in BA30 drops relative to that of BA14 [Fig. 4(d)]. Relative to the respective thinner samples, the mobility in BSI30 enhances $\approx 6$ times as

### Table I. Summary of structural and transport properties of Bi$_2$Te$_3$ samples discussed in the manuscript.

<table>
<thead>
<tr>
<th>Thickness</th>
<th>Substrate</th>
<th>14 QL</th>
<th>30 QL</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Al$_2$O$_3$</td>
<td>Si</td>
<td>Al$_2$O$_3$</td>
</tr>
<tr>
<td>Mobility (cm$^2$ V$^{-1}$ s$^{-1}$)</td>
<td>401</td>
<td>70</td>
<td>670</td>
</tr>
<tr>
<td>Carrier conc. ($\times 10^{19}$ cm$^{-3}$)</td>
<td>2.38</td>
<td>7.5</td>
<td>1.6</td>
</tr>
<tr>
<td>Lattice constant (a = b) (Å)</td>
<td>4.37</td>
<td>4.35</td>
<td>4.34</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>−0.19</td>
<td>−0.23</td>
<td>−0.24</td>
</tr>
<tr>
<td>$l_\rho$ (nm)</td>
<td>213</td>
<td>149</td>
<td>108</td>
</tr>
</tbody>
</table>
compared to a marginal enhancement (≈ 1.7 times) in BA30; carrier concentrations of the samples do not vary significantly (refer Table I). This suggests that bulk-disorder is the primary reason for the above contrasting trends in the magnitude of PHE amplitude for the two sets of samples (BA14-BA30 and BSi14-BSi30). In BSi30, with a considerable drop in bulk-disorder, the PHE signal increases due to larger bulk contribution. While in BA30, an increase in thickness primarily reduces the surface contribution to the overall PHE amplitude explaining the drop in PHE amplitude relative to BA14. However, interestingly in both BSi30 and BA30, we observe an increase in PHE amplitude with an increase in temperature [Figs. 4(c) and 4(d)]. This contrasting trend of PHE amplitude with temperature for thicker films compared to that for the thinner films corroborates our inference that here in thicker films bulk states predominantly contribute to the PHE signal.

We now discuss all plausible mechanisms that lead to PHE in Bi$_2$Te$_3$. Taskin et al. propose anisotropic lifting of topological protection of the surface states causing PHE. However, in our case, it is evident that the carrier concentrations of the samples do not correspond to the energy of the topologically protected surface state regime, where this theory could be applied. The picture of chiral anomaly is ruled out. This suggests that bulk-disorder is the primary reason for the above contrasting trends in the magnitude of PHE amplitude for the two sets of samples (BA14-BA30 and BSi14-BSi30). In BSi30, with a considerable drop in bulk-disorder, the PHE signal increases due to larger bulk contribution. While in BA30, an increase in thickness primarily reduces the surface contribution to the overall PHE amplitude explaining the drop in PHE amplitude relative to BA14. However, interestingly in both BSi30 and BA30, we observe an increase in PHE amplitude with an increase in temperature [Figs. 4(c) and 4(d)]. This contrasting trend of PHE amplitude with temperature for thicker films compared to that for the thinner films corroborates our inference that here in thicker films bulk states predominantly contribute to the PHE signal.

In conclusion, our experiment demonstrates a comprehensive study of PHE in 3D-TI Bi$_2$Te$_3$. The PHE amplitude varies as a square of the magnetic field and agrees well with the conventional PHE equations. Interestingly, the PHE amplitude enhances in BSi30 as compared to that in the BSi14. Furthermore, in contrast to the 14 QL samples, the PHE amplitude in the 30 QL samples increases with temperature. While the origin of PHE in TIs is attributed to arise because of topologically protected surface states, our experiment provides a different perspective. We infer that the PHE has a significant contribution from bulk conduction as well, paving the way for further theoretical modeling of PHE in TIs that may assist in the future development of quantum technologies.

See the supplementary material that contains data of additional devices, fitting routine, and description of calculations used in the manuscript.

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DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding authors upon request.

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