



Genetic evaluation for persistency of lactation in Holstein cows using a random regression model

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Abstract

A model for analyzing test day records including both fixed and random coefficients was applied to the genetic evaluation of first lactation data for Holstein cows. Data comprising 87045 test-day milk yield records from calving between 1997 and 2001 from Holstein herds in 10 regions of the Brazilian state of Minas Gerais. Six persistency of lactation measures were evaluated using breeding values obtained by random regression analyses. The Wilmink function was used to model the additive genetic and permanent environmental effects. Residual variance was constant throughout lactation. Ranking for animals did not change among criteria for persistency measurements, but ranking changes were observed when the estimated breeding value (EBV) for persistency of lactation was contrasted with those estimated for 305-day milk yield (305MY). The rank correlation estimates for persistency of lactation and 305MY were practically the same for sire and cows, and ranged from -0.45 to 0.69. The EBVs for milk yield during lactation for sires producing daughters with superior 305MY indicate genetic differences between sires regarding their ability to transmit desirable persistency of lactation traits. This suggests that selection for total lactation milk yield does not identify sires or cows that are genetically superior in regard to persistency of lactation. Genetic evaluation for persistency of lactation is important for improving the efficiency of the milk production capacity of Holstein cows.

Key words: genetic evaluation, persistency of lactation, rank correlation, random regression models.

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Introduction

Milk production traits have traditionally held the leading position as regards selection goals but in dairy cattle breeding the emphasis is gradually shifting from increasing volume to improving the efficiency of production. Increasing attention has also been paid to other traits that are helpful for improving the management of dairy herds and for increasing the efficiency of breeding schemes. Functional traits must also be considered in selection, because these traits have a direct impact on total economic merit (Groen *et al.*, 1997).

The recent recognition of the importance of functional traits in cattle and the possible role of such traits in avoiding deterioration and possibly improving functional traits during breeding has stimulated research in many

countries (Interbull, 1999). For example, in the European Union increased milk production is not economically advantageous due to the existing quota system (Gengler, 1996; Tekerli *et al.*, 2000). Although most of the incomes of European breeders are generally derived from the sale of milk, they realize that single trait selection for milk yield will not necessarily yield for them the optimal genetic response in overall economic merit and profit potential. Therefore, there is a demand for the genetic evaluation of other traits to aid in selection decisions. Breeders try, among other measures, to reduce the costs of production by improving persistency of lactation (Teklerli *et al.*, 2000).

Persistency of lactation can be defined as the ability of a cow to maintain milk production after peak yield, with cows being persistent if they tend to maintain their peak yield within a lactation period. Improved persistency of lactation can contribute to reducing the cost of the production system because lactation persistency is associated with feeding and health costs, reproductive performance, resistance to disease and the return from milk considering a 305-day production cycle (Sölkner and Fuchs, 1987;

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Dekkers *et al.*, 1996, 1998). It may be desirable to select for increased persistency without increasing peak yield, the latter subjecting the cow to undesirable stress, health and fertility problems (Kruip *et al.*, 1996).

Although the notion of persistency of lactation yield seems clear, definitions are inconsistent (Grossman *et al.*, 1999) and no consensus has yet been reached. Definitions based on the ratio between milk yields at different stages of lactation or on differences between milk yields at test-days during lactation are arbitrary and do not uniquely characterize persistency because such parameters are not invariant with respect to the time period chosen (Rekaya *et al.*, 2001).

Several measurements of persistency have been proposed (Sölkner and Fuchs, 1987; Jaromzik *et al.*, 1997; Jakobsen *et al.*, 2002; Cobuci *et al.*, 2004) but the procedure most widely used today to measure lactation persistency is based on the byproduct of the random regression test day model. These models have been extensively applied to the evaluation of milk production traits since they allow a more precise assessment of the environmental effects acting on these traits. The use of the random regression test day model not only improves the accuracy of genetic evaluations but can also evaluate persistency because the estimated breeding value (EBV) for various parts of the lactation can be calculated (Jamrozik *et al.*, 1997).

In this study we evaluated six different measures for describing persistency of lactation in Holstein cows in order to assess the most suitable of these measures for use in random regression test-day models for the genetic evaluation of persistency of lactation.

Material and Methods

Data consisted of 160,038 test-day milk yield records from Holstein cows calving between 1997 and 2001 in herds supervised by the Milk Recording Service of the Holstein Association of Minas Gerais State (ACGH-MG), in southeastern Brazil.

Data were edited for test-day records between 6 and 305 days in milk (DIM) of first parity cows and calving between 18 and 48 months of age. After applying these criteria 87,045 records from 11,023 first lactation cows, daughters of 936 sires in 251 herds from Minas Gerais State were available for analyses.

We defined four age at calving classes (20 to 24, 25 to 29, 30 to 34 and 35 to 48 months) and four calving seasons (January through March, April through June, July through September and October through December) and combined them to produce 16 age-season classes. Cows in the same herd, year and month of milk recording defined the contemporary group fixed effect. The model used for test-day milk yield was:

$$y_{ijkl} = HYM_i + \sum_{m=1}^3 \beta_{km} Z_{jlm} + \sum_{m=1}^3 a_{jm} Z_{jlm} + \sum_{m=1}^3 p_{jm} Z_{jlm} + e_{ijkl},$$

where y_{ijkl} is record l of cow j made on the t^{th} days in milk of the first lactation for a cow belonging to subclass k for

age-season of calving, HYM_i is the fixed effect of herd-year-month of test i ; β_{km} is the fixed regression coefficient of test-day milk yield as a function of DIM, which describes the shape of the lactation curve within the age-season subclasses; a_{jm} and p_{jm} are random regression coefficients that describe the genetic and permanent environmental effects on each animal, respectively; e_{ijkl} is the random residual effect associated with y_{ijkl} ; Z_{jlm} is the covariable matrices represented by the Wilmink function in which $Z_{jlm} = (Z_{j11} Z_{j12} Z_{j13})' = (1 + t \text{DEX})^2$, and $\text{DEX} = e^{-0.05t}$, t and $m =$ days in milk after calving and the m^{th} parameter of the function, respectively.

The Wilmink function (1987) used to model genetic and permanent environmental effects is represented by

$$y = a_1 + a_2 t + a_3 e^{-0.05t}, \text{ for } t = \text{days in milk.}$$

It was assumed that

$$\begin{pmatrix} \mathbf{a} \\ \mathbf{p} \\ \mathbf{e} \end{pmatrix} \sim N(0, \mathbf{V}) \text{ with, } \mathbf{V} = \begin{pmatrix} \mathbf{G} \otimes \mathbf{A} & 0 & 0 \\ 0 & \mathbf{P} \otimes \mathbf{A} & 0 \\ 0 & 0 & \mathbf{R} \end{pmatrix}$$

where \mathbf{G} is the genetic covariance matrix of the random regression coefficients, assumed to be the same for all cows; \mathbf{A} is the additive genetic relationship matrix among animals; \otimes is the Kronecker product operator; \mathbf{P} is the permanent environment covariance matrix of the random regression coefficients, assumed to be the same for all cows; $\mathbf{R} = \mathbf{I}\sigma_e^2$, for \mathbf{I} an identity matrix, and σ_e^2 the residual variance assumed to be constant throughout the lactation.

The solutions for the additive genetic random regression coefficients of animal j are represented as $\hat{a}'_j = (\hat{a}_{1j} \hat{a}_{2j} \hat{a}_{3j})$. The estimated breeding value (EBV) of animal j in the t^{th} DIM is obtained by

$$EBV_{ij} = (\hat{a}_{1j} + \hat{a}_{2j} t + \hat{a}_{3j} e^{-0.05t}) = z' t \hat{a}_j,$$

and the estimated breeding value for 305-day milk yield (EBV_{305MY}) of animal j is obtained by the sum of the EBV of each t^{th} DIM.

$$EBV_{305MY} = \sum_{t=6}^{305} EBV_t.$$

Six different measures of persistency of lactation (PS_{*i*}) based on EBVs for test-days milk yield in different lactation periods were evaluated as follows:

$$\begin{aligned} PS_1 &= (EBV_{280} - EBV_{60}) \\ PS_2 &= \left(\sum_{t=106}^{205} EBV_t - \sum_{t=6}^{105} EBV_t \right) \\ PS_3 &= \left(\sum_{t=206}^{305} EBV_t - \sum_{t=6}^{105} EBV_t \right) \end{aligned}$$

$$PS_4 = \sum_{61}^{280} (EBV_t - EBV_{60})$$

$$PS_5 = \sum_{60}^{279} (EBV_t - EBV_{280})$$

$$PS_6 = (EBV_{290} - EBV_{90})$$

According to these expressions low values of PS₁ (Jamrozik *et al.*, 1997), PS₂ (Jakobsen *et al.*, 2002), PS₃ (Jakobsen *et al.*, 2002), PS₄ (Jamrozik *et al.* (1997) and PS₆ (Cobuci *et al.*, 2004) indicate high persistency of lactation, which is the case for a high value of PS₅ (Jakobsen *et al.*, 2002).

The solutions for random regression coefficients for each animal were obtained by the restricted maximum likelihood method using the expectation maximization algorithm (EM) of the REMLF90 program (Misztal, 2001). The convergence criterion was 10⁻⁹.

Results and Discussion

The average, standard deviation (SD) and range of the EBVs for each measure of persistency, 305-d milk yield (305MY) and random regression coefficients of the 936 sires included in the analyses are given in Table 1. The averages and SD of the EBVs for the measurements of persistency increased from PS₂ to PS₅. The average EBV was negative for PS₅, which showed a similar SD to PS₄ and reflects the way that the EBVs were measured. Overall, similar magnitudes in the range of the EBVs were observed for the PS₂, PS₃, PS₄ and PS₅ persistency measures. This similarity might be due to the fact that the measures were calculated based on EBVs for milk yield during different lactation periods. In contrast, the PS₁ and PS₆ measures were estimated based on the differences between the EBVs for milk yield on two test-days during the lactation, with PS₆ differing from PS₁ by assuming that the peak yield

of Holstein cows under tropical conditions is reached after 60 days of lactation.

Substantial variation in the magnitude of the genetic random regression coefficients of the Wilmink function for milk yield was observed among sires, indicating the possible presence of genetic variation in the shape of the lactation curves of sires and daughters. The *a*₁ coefficient corresponds to the initial milk production, the *a*₂ coefficient expresses the rate of decline in milk production after peak yield and the *a*₃ coefficient represents the rate of increase in milk production gain until peak yield. The estimates of the genetic random regression coefficients for the top ten sires with more than 25 daughters ranked for milk yield are given in Tables 2.

The EBVs for the 305MY of the top ten sires with more than 25 daughters and their corresponding EBVs for each measure of persistency of lactation are given in Table 3, from which it can be seen that there are differences in the ranking of sires regarding the persistency measures and milk yield. Rank correlation between sire and cows EBVs for persistency and 305MY are given in Table 4. Correlations between EBVs for persistency of lactation were larger than 0.89 for both sires and cows suggesting that, in general, the different measures of persistency evaluated in this study provided similar ranking. However, correlation as low as 0.89 might indicate serious re-ranking for the top animals. The PS₅ and PS₆ measures of persistency were recommended by Cobuci *et al.* (2004) for the genetic evaluation of cattle because these measures showed weaker genetic correlations (-0.31 and 0.31) with 305MY. The rank correlation between EBVs of sires for these two measures of persistency was -0.99. The dispersal of EBVs of sires with more than 25 daughters ranked for PS₅ and PS₆ follows a straight line, indicating that, with very few exceptions, the two measures of persistency rank sires equally (Figure 1).

Rank correlation estimates between persistency of lactation and 305MY differed among persistency measure-

Table 1 - Mean ± standard deviation (SD) and range of estimated breeding values for persistency of lactation (PS₁ to PS₆), 305-day milk yield (305MY) and random regression genetic coefficients (*a*₁, *a*₂ and *a*₃) of the Wilmink function for the sires of a population of Holstein cows.

Traits	Mean ± SD	Range
PS ₁	0.023 ± 0.966	5.442 to -3.769
PS ₂	1.668 ± 49.394	266.236 to -171.807
PS ₃	2.636 ± 90.885	510.386 to -316.105
PS ₄	2.812 ± 107.756	607.975 to -405.214
PS ₅	-2.390 ± 106.200	427.723 to -594.687
PS ₆	0.019 ± 0.874	4.896 to -3.512
305MY	11.117 ± 352.342	1378.87 to -1376.33
<i>a</i> ₁	0.024 ± 1.101	4.965 to -4.652
<i>a</i> ₂	9.0 × 10 ⁻⁵ ± 0.004	0.024 to -0.017
<i>a</i> ₃	-0.047 ± 1.395	7.388 to -7.841

Table 2 - Estimates of the genetic random regression coefficients (*a*₁, *a*₂ and *a*₃) of the Wilmink function for the top ten sires with more than 25 daughters ranked for milk yield.

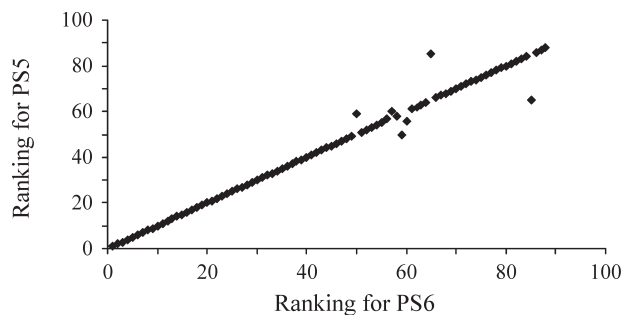
Sire	<i>a</i> ₁	<i>a</i> ₂	<i>a</i> ₃
SM1	3.2181	0.0102	-4.1076
SM2	2.9362	0.0108	-1.4718
SM3	3.4052	0.0075	-3.6204
SM4	3.4355	0.0059	-3.4652
SM5	1.6257	0.0136	-2.4346
SM6	3.2191	0.0083	-4.4048
SM7	3.4386	0.0043	-3.7200
SM8	1.8657	0.0138	-3.7007
SM9	2.3752	0.0078	-4.1336
SM10	-0.4027	0.0244	-1.4838

Table 3 - Estimated breeding values for different measures of persistency of lactation (PS₁ to PS₆) and 305-day milk yield (305MY) for the top ten sires with more than 25 daughters ranked for milk yield.

Sire	PS ₁	PS ₂	PS ₃	PS ₄	PS ₅	PS ₆	305MY
SM1	2.45	163.56	265.97	288.97	-252.15	2.08	1378.87
SM2	2.45	130.06	238.21	277.24	-264.05	2.17	1362.32
SM3	1.83	129.26	204.62	218.46	-186.02	1.54	1316.44
SM4	1.47	110.93	170.28	178.02	-146.97	1.22	1253.25
SM5	3.11	172.49	308.73	354.92	-333.10	2.75	1085.17
SM6	1.45	86.40	148.56	166.97	-152.38	1.26	905.09
SM7	1.79	94.96	174.07	202.68	-193.14	1.59	887.14
SM8	-2.21	-24.42	-137.82	-217.46	271.03	-2.21	866.83
SM9	1.26	68.59	123.68	142.76	-134.63	1.11	856.99
SM10	-1.17	-4.22	-65.83	-112.2	146.79	-1.20	854.48

Table 4 - Rank correlation between estimated breeding values for different measures of persistency of lactation (PS₁ to PS₆), 305-day milk yield (305MY) and random regression genetic coefficients (a_1 , a_2 and a_3) of sires (upper diagonal) and cows (lower diagonal).

Traits	PS ₁	PS ₂	PS ₃	PS ₄	PS ₅	PS ₆	305MY	a_1	a_2	a_3
PS ₁		0.92	0.98	0.99	-0.99	0.99	0.49	-0.00	0.99	-0.18
PS ₂	0.93		0.97	0.94	-0.89	0.89	0.69	0.25	0.88	-0.48
PS ₃	0.98	0.97		0.99	-0.96	0.96	0.59	0.11	0.96	-0.32
PS ₄	0.99	0.95	0.99		-0.98	0.98	0.53	0.04	0.98	-0.23
PS ₅	-0.99	-0.90	-0.97	-0.99		-0.99	-0.45	0.05	-0.99	0.13
PS ₆	0.99	0.90	0.97	0.99	-0.99		0.45	-0.05	0.99	-0.13
305MY	0.50	0.69	0.59	0.53	-0.46	0.46		0.81	0.44	-0.71
a_1	-0.03	0.23	0.08	0.01	0.07	-0.07	0.81		-0.06	-0.76
a_2	0.99	0.90	0.97	0.99	-0.99	0.99	0.45	-0.08		-0.11
a_3	-0.09	-0.42	-0.23	-0.14	0.04	-0.04	-0.65	-0.75	-0.02	

**Figure 1** - Dispersal in ranking of sires with more than 25 daughters for the PS₅ and PS₆ measurements of persistency of lactation.

ments and were dependent on the way persistency was defined (Table 4). The lowest rank correlation estimates between persistency of lactation and 305MY were obtained for PS₅ and PS₆, for both sires (-0.46 and 0.46) and cows (-0.45 and 0.45), and, as expected, agree with the results of Cobuci *et al.* (2004). These estimates demonstrate the weak association between production and persistency of lactation; thus, cows with the same milk production may present

different levels of persistency of lactation (Gengler, 1996; Jamrozik *et al.*, 1998; Van Der Linde *et al.*, 2000). These estimates also indicate that animals with larger EBVs for persistency of lactation are not exactly the same as those with larger EBVs for 305MY.

Except for PS₂, the rank correlation estimates between persistency and the genetic random regression coefficient a_2 for sires and cows were close to unity, confirming that a_2 is also a measure of persistency of lactation. Rank correlation between a_2 and MY305 was 0.45, the same value obtained for the estimates between MY305 and PS₅ and PS₆.

The dispersal in ranking of 88 sires with more than 25 daughters is shown in Figure 2 for 305MY and PS₅ and Figure 3 for 305MY and PS₆, the best sires for 305MY and persistency being shown in the lower left corner of these figures. The top five sires for 305MY ranked 82, 83, 72, 70 and 87 for PS₆ while, in contrast, the top five sires for PS₆ ranked 62, 40, 61, 88 and 8 for 305MY.

The percentage of sires or cows in common according to increasing levels of selection for persistency of lactation and 305MY are given in Figure 4 for sires and Figure 5 for

cows. At high selection intensities (<10%) there are few animals in common but, as expected, the percentage increases as the percentage of animals selected for 305MY increases. There were no significant differences between the PS1, PS3, PS4, PS5 and PS6 measurements, while the PS2 measurement showed the lowest percentages of animals in common.

The EBVs for milk yield across lactation for the top five sires for high 305MY with more than 25 daughters are shown in Figure 6. The EBV curves indicate genetic differences between the best top five sires selected for the milk yield. Similarly, the EBVs for milk yield across lactation of the top five sires ranked for PS₆ are given in Figure 7, which also shows the genetic differences between sires in terms of the persistency of lactation of their daughters. Thus, comparison between the EBVs of sires for persistency or milk yield across lactation (Figures 6 and 7) reveals that the curves differ for sires with higher EBV for 305MY or PS₆, confirming the weak association between 305MY and persistency of lactation. Additionally, the top five sires (SM1 to SM5) for 305MY ranked respectively 82, 83, 72, 70 and 87 for PS₆ while, in contrast, the top five sires (SP1 to SP5) for PS₆ ranked 62, 40, 61, 88 and 8 for 305MY.

The trends in estimated breeding values of sires and cows across lactation according to the year of birth of the cows is shown in Figure 8, from which it can be seen that there is a clear difference in average EBVs across the years. In the earlier years the curves are flat, and differences become clear (particularly after early lactation) in the last

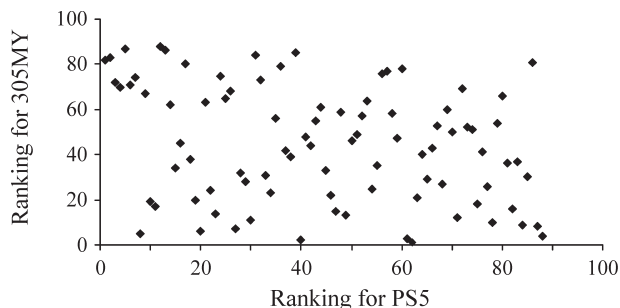


Figure 2 - Dispersion in ranking of sires with more than 25 daughters for 305-day milk yield (305MY) and persistency of lactation (PS₅).

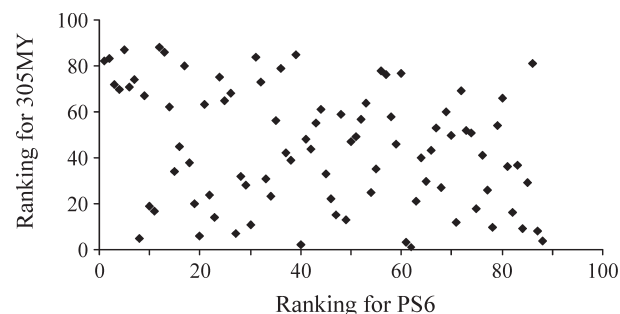


Figure 3 - Dispersion in ranking of sires with more than 25 daughters for 305-day milk yield (305MY) and persistency of lactation (PS₆).

three years, indicating a positive trend regarding improved 305MY. Average EBVs of sires for persistency of lactation and 305-day milk yield according to the birth year of cows is shown Table 5. Figure 9 clearly demonstrates a positive trend for milk yield, but no significant trend in average EBVs of sires for persistency in the 1993-1999 period.

Overall, these results indicate that an increase in 305MY may not lead to improvement in the level of persistency of lactation unless selection for 305MY also takes

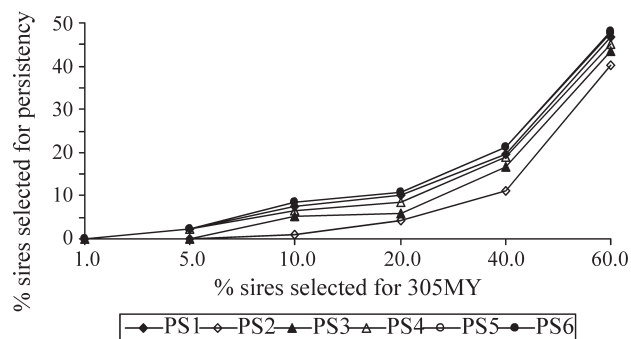


Figure 4 - Percentage of sires selected for persistency of lactation (PS₁-PS₆) when selecting for 305-day milk yield (305MY), at different selection intensities.

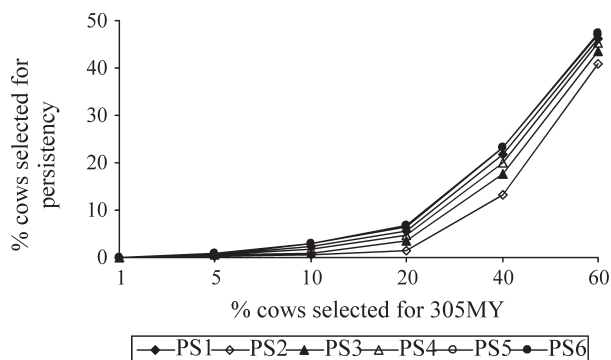


Figure 5 - Percentage of cows selected for persistency of lactation (PS₁-PS₆) when selecting for 305-day milk yield (305MY), at different selection intensities.

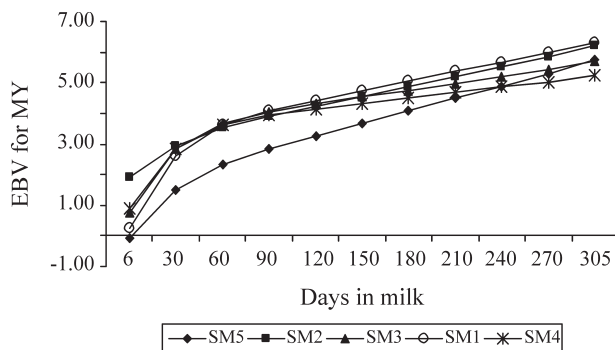


Figure 6 - Estimated breeding values across lactation of the top five sires (SM1-SM5) with more than 25 daughters ranked for 305-day milk yield (305MY).

into account the selection of animals that show higher levels of persistency of lactation. An increase in 305MY might be obtained by the selection of animals that show higher levels of persistency of lactation, which means select cows with a reduced rate of decline in daily milk yield after peak lactation. Previous studies have investigated the effectiveness of different measures of persistency as selection criteria in improvement of persistency of lactation and milk yield simultaneously (Togashi and Lin, 2004) but other studies have introduced doubts regarding whether the

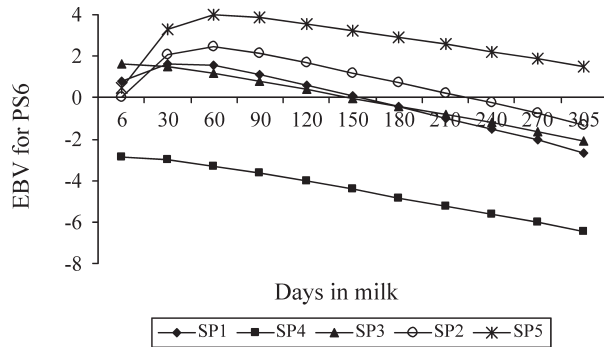


Figure 7 - Estimated breeding values across lactation of the top five sires (SP1-SP5) with more than 25 daughters ranked for persistency of lactation (PS₆).

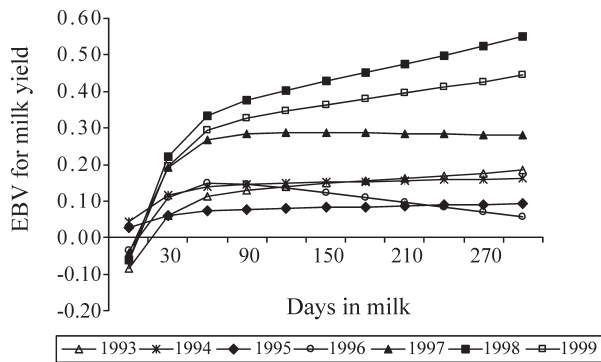


Figure 8 - Average estimated breeding values for milk yield across lactation of cows and sires according to the birth year of cows.

Table 5 - Average estimated breeding values of sires for persistency of lactation (PS₁ to PS₆) and 305-day milk yield (305MY) according to the birth year of cows.

Traits	Year						
	1993	1994	1995	1996	1997	1998	1999
PS ₁	0.03	0.003	0.008	-0.04	0.01	0.15	0.10
PS ₂	3.15	0.91	0.62	0.05	4.33	11.49	9.13
PS ₃	4.58	0.94	0.99	-2.54	4.18	17.53	12.97
PS ₄	4.60	0.65	1.06	-4.58	2.58	18.24	12.80
PS ₅	-3.57	-0.12	-0.91	6.18	0.10	14.96	-9.61
PS ₆	0.03	0.001	0.07	-0.05	-0.00	0.12	0.08
305MY	21.94	20.38	10.48	19.01	52.65	87.09	78.43

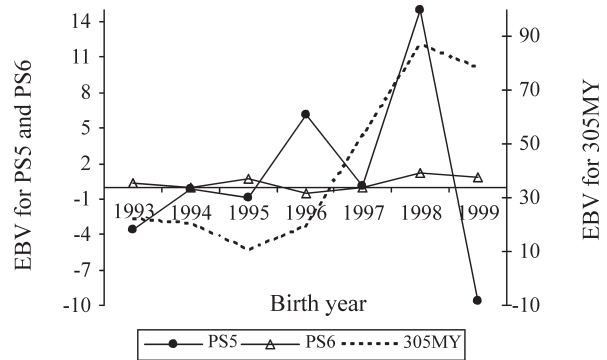


Figure 9 - Average estimated breeding values for 305-day milk yield and persistency of lactation of sires according to the birth year of cows.

days-open effect (Stanton *et al.*, 1992; Dedková and Nemcová, 2003) or does not effect (Van der Linde *et al.*, 2000) the shape of the lactation curve.

Additional research is still needed to identify alternative models to fit test-day data. A Canadian study by Kistemaker (2003) has indicated that test-day models using Legendre polynomials allow for more variability than models using the Wilmink curve. Orthogonal polynomials are most appropriate for the covariates in the random regression model (Schaeffer, 2004), while Jakobsen *et al.* (2002) has reported that a four-order Legendre polynomial best fitted the data for persistency of milk yield.

Our results confirmed the weak association between 305MY and persistency of lactation. From the six measures of persistency evaluated in this study, the performance of PS5 and PS6 were very similar and emerged as the most appropriate when applied to describe persistency or milk yield of the Holstein breed in Minas Gerais State, and are thus potential criteria for use in the genetic evaluation of persistency. However, further studies are needed to evaluate other functions for their ability to model the lactation curve and the effectiveness of measures of persistency as selection criteria for the simultaneous improvement of lactation milk yield and lactation persistency.

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