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Dynamic response of Advanced Placed Ply composites

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Abstract

This work investigates the high strain rate behavior of AP-PLY composites. The large representative volume elements and brittle nature of this material necessitated the use of a bespoke split-Hopkinson bar apparatus. AP-PLY and baseline laminates were subjected to tensile loading at strain rates of 30 s^{-1} . Results were compared with quasi-static data to evaluate whether the laminate architecture introduced any strain rate dependency. In addition, the dynamic experiments were simulated using a multiscale modeling framework, providing further insights into the micromechanisms governing material behavior. The moduli of the AP-PLY composites were found to be strain rate independent, however, strengths were found to be marginally higher than those of their baseline counterparts. At high strain rates, the strain concentrations induced by the geometry of the individual tapes at through thickness undulations and tow boundaries were less significant due to reduced out-of-plane tow straightening and delamination. As a result, no reduction in AP-PLY strength in comparison to the baseline laminates was obtained. These differences in deformation micromechanisms led to an improvement of the damage tolerance when subjected to dynamic loading.

Keywords: Impact behaviour, Automated fiber placement lay-up, 3-Dimensional reinforcement, computational modelling

1. Introduction

Advanced Placed Ply (AP-PLY) is a novel preforming method for Automated Fiber Placement (AFP) that creates through thickness reinforcements by interlacing fiber tows in a pseudo-woven architecture [1, 2, 3, 4, 5]. The three-dimensional reinforcements improve the impact damage tolerance of AP-PLY composites while allowing them to retain the excellent stiffness and strength of conventional angle ply laminates. Previous studies have reported significant improvements in mode I interlaminar fracture toughness and compression after impact (CAI) strength as a result of this novel preforming method [1]. As such, AP-PLY composites are potentially a suitable material choice for aerospace components susceptible to dynamic loads such as engine blades, brackets, nacelles, propellers/rotors, turbine casings, and wings. Previous studies have investigated the low and high velocity impact performance of AP-PLY composites [1, 6, 7, 8]. However, due to the

36 experimental difficulties associated with large representative volume elements (RVEs), the in-plane
37 dynamic material properties of this new family of composite materials has yet to be investigated.

38 The strain rate dependency of composites is typically characterized using Split Hopkinson
39 Bar (SHB) experiments, which provide the stress-strain curves of a material at different strain
40 rates [9]. The high strain rate behavior of conventional carbon fiber epoxy composites has been
41 extensively studied. Fiber dominated material properties are generally strain rate independent,
42 while matrix dominated deformation and failure modes are highly sensitive to changes in the strain
43 rate [10, 11, 12, 13]. The strain rate dependency of composites containing 3D reinforcements is,
44 however, less well understood [10, 14, 15, 16, 17].

45 Reliable data on the dynamic properties of AP-PLY composites are sparse mainly due to exper-
46 imental difficulties [18]. Conventional SHBs are limited to specimens with relatively small dimen-
47 sions, however, the large representative volume elements of AP-PLY composites (approximately
48 40 mm x 40 mm) require the use of more advanced non standard equipment. First, exceptionally
49 large bar diameters and pulse magnitudes are required to generate forces sufficient to break the
50 specimens. Second, a large pulse duration with a progressive rising time is required to avoid the
51 premature failure of the brittle composite [19]. An additional consequence of the brittle nature of
52 carbon fiber composites is that they are more sensitive to mechanical gripping, which may result
53 in measurements of strength that underestimate the actual material strength [20]. Furthermore,
54 since the gauge length and distance between bar ends are much greater in large SHBs, it is more
55 difficult to achieve force equilibrium, requiring more detailed analysis to ascertain the validity
56 of the experimental data [21]. In summary, characterizing the tensile high strain-rate behavior of
57 brittle materials with large RVEs, such as AP-PLY composites, using specimen sizes representative
58 of global material behavior, is highly demanding, both in terms of equipment and data processing
59 expertise.

60 In this context, numerical simulations can be used in tandem with experiments to character-
61 ize the dynamic material properties. This methodology mitigates the uncertainties arising from
62 boundary-conditions [22, 23] and can provide valuable insights into the triggering sequence of fail-
63 ure mechanisms that can not be captured experimentally due to the space and time-resolution
64 limitations of high-speed imaging techniques and post-mortem fractography [12]. In this study,
65 the high strain rate mechanical properties of AP-PLY composites are determined using a hybrid
66 experimental and numerical approach. The response of the AP-PLY laminates is compared with
67 those of conventional angle ply composites to quantify the effect of the through thickness fiber un-
68 dulations. Section 2 summarizes the manufacturing process for these novel composites, and Section
69 3 details the experimental setup, including post-processing of the data from the split-Hopkinson
70 bar apparatus. Section 4 provides a brief overview of the previously validated 3D multiscale nu-
71 merical framework used to model the response of the AP-PLY laminates. Section 5 analyzes the
72 behavior of the AP-PLY laminates at high strain rates, on the basis of the combined numerical
73 and experimental results.

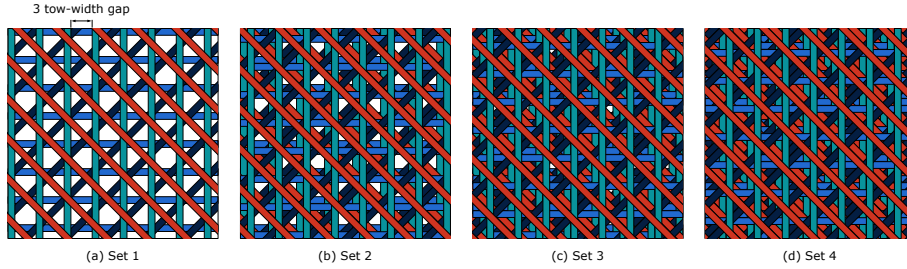


Figure 1: Schematic illustration of the layup process for the quasi-isotropic AP-PLY laminate. Following steps (a) through (d) produces in a 4 ply laminate. To produce the 32-ply thick laminate used in this study, steps (a) through (d) were completed 4 times, and then the process was repeated (4 times) in reverse to produce a symmetric laminate.

74 2. Materials

75 Two AP-PLY laminates were manufactured, one cross-ply $[0/90]_{5s}$ (XP_{AP-PLY}) and one quasi-
76 isotropic $[0/45/90/-45]_{4s}$ (QI_{AP-PLY}). The latter represents the state of the art in terms of the
77 geometrical complexity of its internal architecture [2, 24, 25]. Each AP-PLY laminate was laid up by
78 hand. Tows with a width of 10 mm were first slit from a roll of prepreg (SHD Composites VTC401),
79 then placed into a mould according to a predefined layup sequence. To ensure the correct alignment
80 of each tow, guides were printed. Figure 1 illustrates the layup process for the quasi-isotropic AP-
81 PLY laminate. In both laminates a gap of three tow widths was left between tows placed in the
82 same set. The 300 mm x 300 mm panels were cured in a hot press under 4 bars of pressure at
83 120°C for 120 minutes. In addition, two reference – non AP-PLY – laminates were manufactured
84 for comparison with the AP-PLY panels, (XP_{ref} and QI_{ref}). The AP-PLY preforming process
85 did not alter the thickness of laminates. The average quasi-isotropic specimen thicknesses were
86 6.95 ± 0.15 mm and 6.88 ± 0.04 mm for the AP-PLY and baseline configurations respectively. For
87 the cross-ply configuration, the average AP-PLY specimen thickness was 4.14 ± 0.05 mm, while the
88 average baseline specimen thickness was 4.20 ± 0.16 mm.

89 Specimens were extracted from the laminates using computerized numerical control (CNC)
90 machining according to the design reported in Figure 2. The width of the gauge section varied
91 between 30 mm and 40 mm to ensure the response was representative of the mechanical behavior
92 of the parent laminates [5]. Aluminium end tabs were adhered to the specimens to improve stress
93 transfer between the clamps and the specimen. The end tabs were extracted using a water jet
94 and adhered to the specimens using a two part epoxy adhesive (Permaglue ET5428). Clamps
95 were used to provide a consolidating pressure while the adhesives cured in an oven according to
96 the manufacturer’s recommended cure cycle (60°C for 1 hour). Excess adhesive was removed by
97 machining to achieve the desired dimensional tolerances for testing.

98 3. Experimental Techniques

99 The experimental campaign was carried out at the facilities of the European Laboratory for
100 Structural Assessment: Large Hopkinson Bar Facility (ELSA-HopLab) [26]. The Split Hopkinson

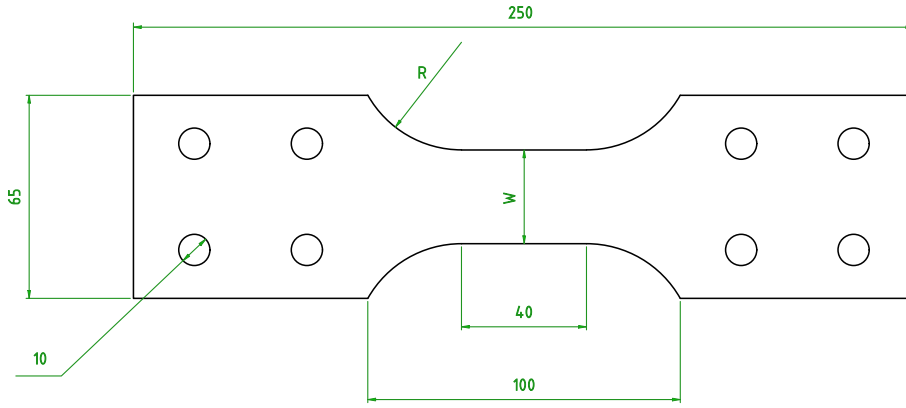


Figure 2: Dynamic tensile testing specimen dimensions (in mm).

101 Bar (SHB) at the HopLab facility consists of incident and transmitter bars made of steel, 72 mm in
 102 diameter and 12 m and 90 m in length respectively, see Fig. 3. It is the world's largest Hopkinson
 103 Bar, specifically designed to test components, sub-assemblies and large material samples. Loading
 104 pulses were generated by first pretensioning a steel cable, then suddenly releasing it using explosive
 105 bolts. This generated a stress pulse with an input velocity of 5 m/s and an approximate effective
 106 strain rate of 30 s^{-1} . The specimens had a gauge length of 40 mm and were threaded into the bars
 107 with custom clamps, see Fig 4(b). Four M10 bolts provided sufficient clamping force to prevent
 108 slippage of the specimens. The friction coefficient between the specimen and the clamps was further
 109 increased by knurling the surface of the grips. Four pins were used to prevent any movement
 110 between the upper and lower clamp plates. A minimum of six specimens per configuration were
 111 tested.

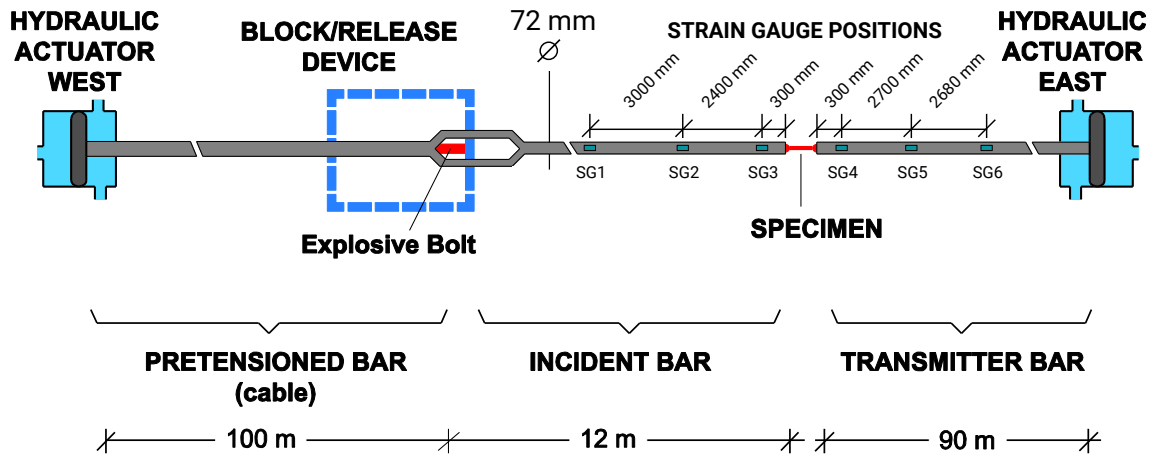


Figure 3: Schematic of the large Split Hopkinson bar for dynamic mechanical testing at the HopLab facility

112 Incident and transmission bars were equipped with six semiconductor strain-gauges connected
 113 in a full-bridge configuration. The positions of the strain gauges are illustrated in Figure 3. The
 114 Wheatstone bridge signal was amplified using a strain-gauge amplifier with a cut-off frequency
 115 of 500 kHz (EFS SGA02 high-speed) and then recorded at a sample-rate of 5 MHz with a fast
 116 transient recorder (National Instruments PXIe-1071 and acquisition boards PXIe-6366). The gain

117 of the ohmic strain-gauges was increased to improve the sensitivity of the strain measurement
118 in the output bar. In addition to measuring strain using gauges, a 2D digital image correlation
119 system was used to capture the strain field in the specimens under loading [27]. A high-speed
120 camera (Photron SA1.1) was used to capture the deformation of the specimens at 50,000 frames
121 per second and at a resolution of 512 x 208 pixels. Cold lights (Veritas Constellation 120) were
122 used to illuminate the specimen surface during the test. Figure 4 illustrates the imaging setup for
123 the SHB tests. The specimens were speckled by hand using a white marker, resulting in an average
124 speckle diameter of 1 mm. Given the resolution of the camera, this resulted in approximately 5
125 pixels per speckle, above the 3 pixel per speckle threshold required to avoid anti-aliasing issues [28].
126 Post-processing of the DIC images was conducted using the MatchID software package. Subset
127 and step size were set to 15 and 17, respectively, and interpolation was conducted using a bi-cubic
128 spline algorithm. Strains were determined using a filter size of 15. The noise floor was estimated to
129 be 50 microstrain, based on the standard deviation of the axial strain in an image of an unstressed
130 specimen. The spatial resolution of the DIC system — estimated on the basis of the subset, step,
131 and strain filter size — was 3 mm.

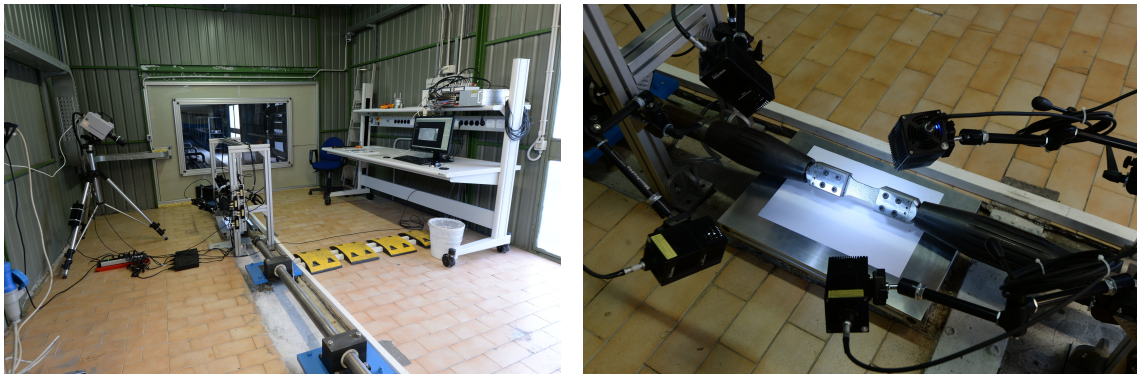


Figure 4: DIC setup for the SHB experiments. The image on the left illustrates the camera positioning orthogonal to the specimen surface. The image on the right illustrates the lighting setup for the experiments and the DIC speckle.

132 Signals from the strain gauges were post-processed in MATLAB. Figure 5(a) illustrates the raw
133 signals from the 6 semiconductor strain gauges adhered to the input and output bars. Note there
134 is a slight offset of the force at time 0 due to the static preload of the bar. The resulting incident,
135 transmitted and reflected waves, illustrated in Figure 5(b), were calculated using a deconvolution
136 algorithm capable of compensating for wave dispersion distortions [29]. Oscillations in the input
137 force history can be attributed to small propagation errors from the deconvolution algorithm and
138 to the interaction of the stress waves with the specimen clamps. The applied strain-rate is plotted
139 in Figure 6(a). The force-time data were combined with the displacement-time data obtained using
140 DIC to generate force-displacement curves. Linear interpolation was used to account for the higher
141 data recording frequency of the strain sensors relative to the high speed cameras. Note that due to
142 the high sensitivity and low signal noise of the semiconductor strain gauges, it was not necessary

143 to filter or smooth the raw signal data to obtain clear force-displacement and stress-strain plots.

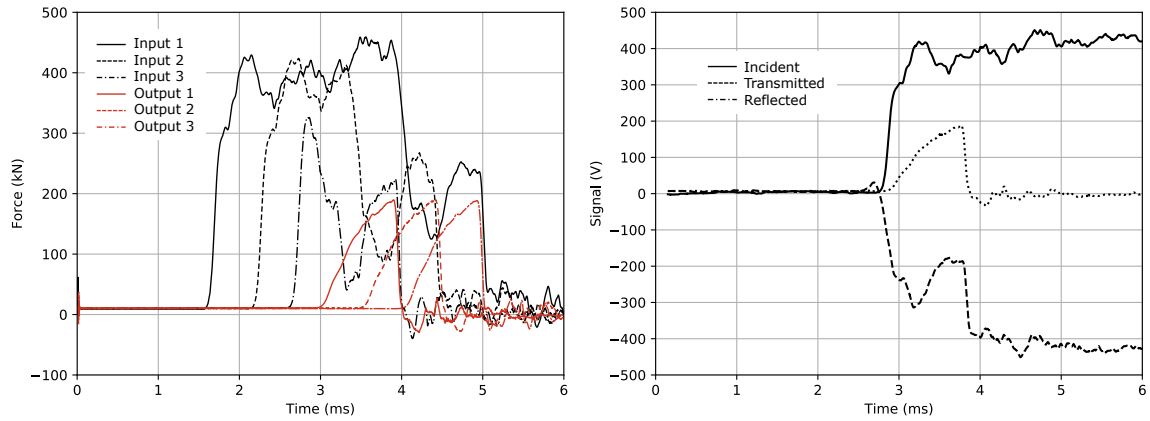


Figure 5: Raw semiconductor strain gauge signals (a) and the resulting waves (b) calculated using a deconvolution algorithm. for QI AP-PLY specimen 2.

144 The dynamic force equilibrium between bars was analyzed to validate the stress-strain curves.
 145 Figure 6(a) plots the force in the input and output bars against time for one of the cross-ply
 146 specimens. Despite the noise of the input bar signal, force equilibrium is reached in the 0.50 ms
 147 to 1.25 ms time interval. Analysis of the strains in the specimen at the input and output ends
 148 using DIC confirms the state of equilibrium in the specimen during the test, see Figure 6(b).

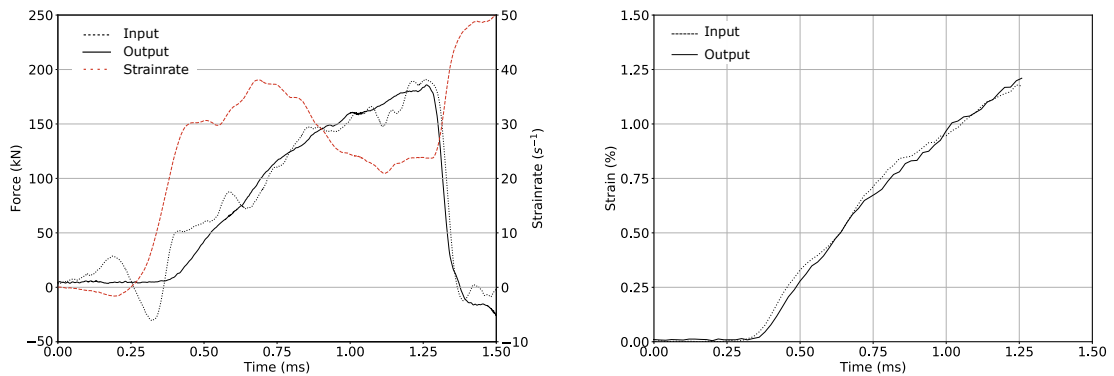


Figure 6: Validation of state of equilibrium for QI AP-PLY specimen 2: (a) input and output bar forces and strain rate as measured using SHB strain gauges, and (b) strain at the input and output ends, determined using DIC.

149 4. Numerical Simulations

150 The SHB experiments of the AP-PLY laminates were simulated using a previously developed
 151 multiscale continuum damage mechanics (CDM) framework [5], able of capturing the effects of the
 152 through thickness tow undulations on the macroscale laminate behavior. The model was previously
 153 validated for quasi-static tensile loading and is briefly recalled here for the sake of completeness.

154 4.1. Multiscale Constitutive Model

155 The approach divides AP-PLY laminates into regions of three different types; straight tow,
 156 resin-rich, and undulation. The region types are illustrated in Figure 7. Straight tow regions

157 behave like conventional unidirectional composite laminae, resin-rich regions represent the edges
 158 of AFP tows where the fiber volume fraction is relatively low, and undulation regions represent
 159 the areas in an AP-PLY laminate where there is through thickness reinforcement. Unit cells
 160 are defined for each region, consisting of different volume fractions of micro constituents (tow or
 161 resin). Using an isostrain assumption, the strains on an element can be applied to each of its
 162 micro constituents. After the strains are rotated to the material coordinate system, a CDM model
 163 is used to determine the resulting stress in each micro-constituent. The stress-strain response of
 164 each element is determined by homogenizing the response of each of its micro-constituents. Using
 165 this approach it is possible to account for the effects of resin pockets and through thickness fiber
 166 undulation without modeling them explicitly geometrically, considerably reducing computational
 167 costs compared with purely micromechanical models [5].

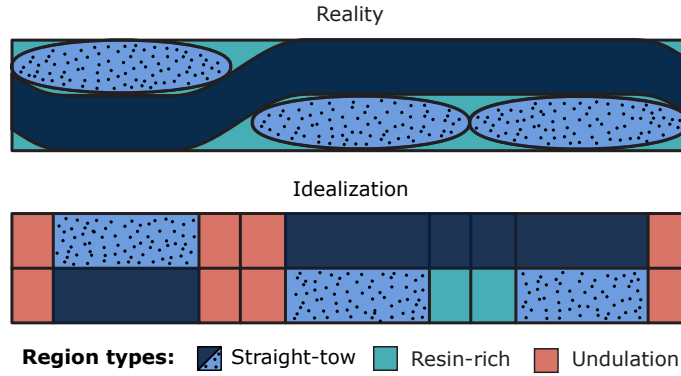


Figure 7: Illustration of the division of the AP-PLY geometry into idealized regions

Two constitutive models are defined; one for the pure resin constituent, and one for the resin impregnated fiber tows. The CDM model for the fiber tows is adapted from the work of Shah *et al.*, Maimi *et al.*, and Tan *et al.* [30, 31, 32, 33]. Prior to damage initiation, material behavior is defined as linear elastic. In the fiber direction, the onset of damage is predicted using maximum strain criteria, while matrix damage initiation is governed by a 3D adaptation of the Hashin failure criteria (Equations 1 - 6).

$$F^{1T} = \frac{\varepsilon_{11}}{\varepsilon_{11}^{0T}} \quad (1)$$

$$F^{1C} = \frac{\varepsilon_{11}}{\varepsilon_{11}^{0C}} \quad (2)$$

$$F^{2T} = \left(\frac{\langle \hat{\sigma}_{22} \rangle}{Y_{is}^T} \right)^2 + \left(\frac{\hat{\tau}_{12}}{S_{is}^L} \right)^2 + \left(\frac{\hat{\tau}_{23}}{S^T} \right)^2 \quad (3)$$

$$F^{2C} = \left(\frac{\langle -\hat{\sigma}_{22} \rangle}{2S^T} \right)^2 + \left[\left(\frac{Y^C}{2S^T} \right)^2 - 1 \right] \frac{\hat{\sigma}_{22}}{Y^C} + \left(\frac{\hat{\tau}_{12}}{S_{is}^L} \right)^2 \quad (4)$$

$$F^{3T} = \left(\frac{\langle \hat{\sigma}_{33} \rangle}{Z_{is}^T} \right)^2 + \left(\frac{\hat{\tau}_{31}}{S_{is}^R} \right)^2 + \left(\frac{\hat{\tau}_{23}}{S^T} \right)^2 \quad (5)$$

$$F^{3C} = \left(\frac{\langle -\hat{\sigma}_{33} \rangle}{2S^T} \right)^2 + \left[\left(\frac{Z^C}{2S^T} \right)^2 - 1 \right] \frac{\hat{\sigma}_{33}}{Z^C} + \left(\frac{\hat{\tau}_{31}}{S_{is}^R} \right)^2 \quad (6)$$

168 where Y_{is}^T , Y^C , Z_{is}^T , and Z^C are the tensile and compressive strengths in the transverse and
 169 through-thickness directions, respectively, and S_{is}^L , S^T , S_{is}^R are the shear strengths in the 12, 23,

170 and 31 directions, respectively. The *is* subscript indicates in-situ strengths [34, 35] and $\hat{\cdot}$ indicates
 171 a trial stress component.

172 After the onset of damage, material stiffness is degraded according to energy based damage
 173 evolution laws. In the fiber direction, damage evolution is exponential. The scalar damage variables
 174 can be expressed in the general form as (adapted from [36]):

$$d_1^k = 1 - \frac{1}{f_1^k(r_1^k)} \exp \{ A_1^k [1 - f_1^k(r_1^k)] \} f(r_H) \quad k = T, C \quad (7)$$

175 where r_1^k represents the elastic domain threshold, and A_1^k is a parameter ensuring the energy
 176 dissipated by the element is equal to the fracture energy of the material in the corresponding
 177 mode. The function $f_1^k(r_1^k)$ is used to force the softening of the constitutive relation, and function
 178 $f(r_N)$ couples the damage laws to the elastic domain thresholds.

179 In the transverse and through thickness directions damage accumulation results in linear soft-
 180 ening of the modulus in the corresponding mode. The damage variables are expressed as functions
 181 of the ultimate failure strain ε^f , the strain at damage onset ε^0 , and the current strain ε :

$$d = \frac{\varepsilon^f (\varepsilon - \varepsilon^0)}{\varepsilon (\varepsilon^f - \varepsilon^0)} \quad (8)$$

182 where the ultimate failure strain is dependent on; the fracture energy of the material \mathcal{G}_c in the
 183 relevant direction, the characteristic length ℓ_c , and the stress at damage initiation σ^0 .

184 The pure resin damage model assumes material behavior is isotropic. As such stiffness is
 185 degraded using a single scalar damage variable d_m . Damage onset is predicted using pressure
 186 dependent loading functions adapted from the work of Liu *et al.* [37].

$$F_m^T = \frac{3J_2 + I_1 (Y^C - Y^T)}{Y^C Y^T} \quad \text{if } I_1 \geq 0 \quad (9)$$

$$F_m^C = -\frac{3J_2 + I_1 (Y^C - Y^T)}{Y^C Y^T} \quad \text{if } I_1 < 0 \quad (10)$$

187 where I_1 represents the trace of the stress tensor and J_2 is the second invariant of the deviatoric
 188 stress tensor. Y^T and Y^C are assumed to be equal to the tensile and compressive transverse
 189 strengths of the unidirectional tows. After failure initiation, moduli are degraded according to an
 190 exponential damage evolution laws similar to those used to express softening in the longitudinal
 191 damage modes of the impregnated fiber tow regions, see Equation 7.

192 4.2. FEA Implementation

193 The multiscale simulation framework presented above was implemented as a VUMAT subrou-
 194 tine in the finite element software Abaqus/Explicit. The geometry creation pre-processing scripts
 195 and the multiscale CDM subroutine are available on GitHub ¹. The quasi-static material properties
 196 of the prepreg fiber tows, shown in Table 1, were obtained experimentally according to the relevant
 197 standards, with the exception of the fracture toughnesses, which were taken from the literature
 198 [38, 39].

¹<https://github.com/rutger-kok>

Table 1: Quasi-static Mechanical properties of SHD Composites VTC401 Prepreg [5].

Elastic Properties	$E_{11} = 124.35$ GPa, $E_{22} = E_{33} = 7.23$ GPa, $G_{12} = G_{31} = 3.268$ GPa, $G_{23} = 2.638$ GPa, $\nu_{12} = \nu_{31} = 0.339$, $\nu_{23} = 0.374$
Strengths	$X^T = 2550$ MPa, $X^C = -1102$ MPa, $Y^T = Z^T = 44$ MPa, $Y^C = Z^C = -184$ MPa, $S^{12} = S^{31} = 55$ MPa, $S^{23} = 83$ MPa
Fracture Energies	$\mathcal{G}_1^T = 134$ N/mm, $\mathcal{G}_1^C = 95.0$ N/mm, $\mathcal{G}_2^C = 0.38$ N/mm, $\mathcal{G}^s = 1.62$ N/mm

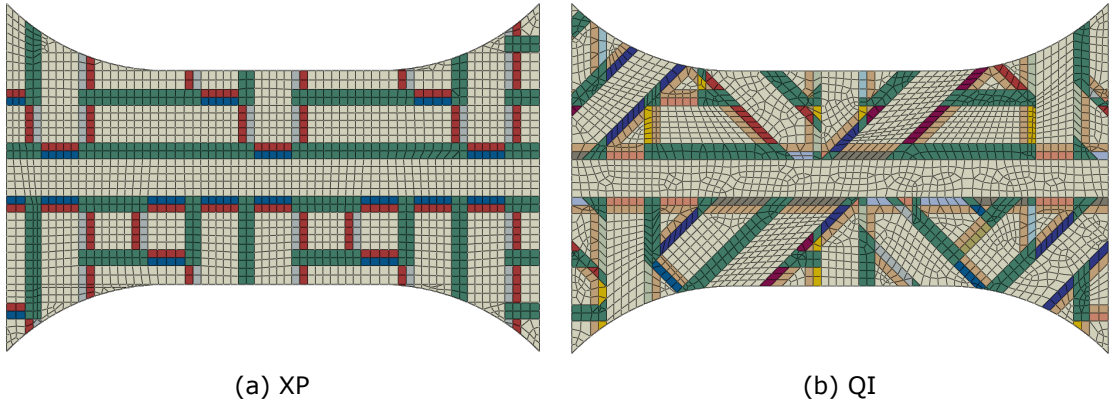


Figure 8: Finite element method meshes for the (a) cross-ply and (b) quasi-isotropic AP-PLY dogbone specimens.

199 Specimens were discretized using 8 node reduced integration linear solid C3D8R elements. Since
200 the stacking sequence in each specimen is repeated and symmetric, an 8-ply sub-laminate was
201 sufficient to represent the response of each 20-32 ply laminate. To further reduce computational
202 cost, only the central (non-clamped) portion of the specimens was modeled. Elements sizes of
203 approximately 1.5 mm were chosen to match the size of the mesoscale unit cells, whose dimensions
204 are a function of the length of the tow undulations. This optimal element size ensured a realistic
205 macro-to-meso strain transformation [30]. Note, however, that due to the automated partitioning
206 of the specimens by the geometry generation scripts, some of the elements were smaller than the
207 mesoscale unit cell. The specimen meshes are illustrated in Figure 8.

208 A zero displacement boundary condition was applied to the left hand side of each of the speci-
209 mens. A relative velocity boundary condition was applied to the other end based on the input and
210 output bar velocities measured experimentally by the strain gauges, see Figure 9. This approach,
211 previously validated in studies of titanium alloys [40] and woven composites [41], is computationally
212 efficient as it does not require the simulation of the entire SHB system. To avoid numerical insta-
213 bility issues at the onset of damage, Abaqus' default bulk viscosity option was used, and enhanced
214 hourglass and distortion control were enabled. The energies in the simulation were monitored to
215 ensure the artificial strain energy resulting from the section controls did not exceed 2% of the

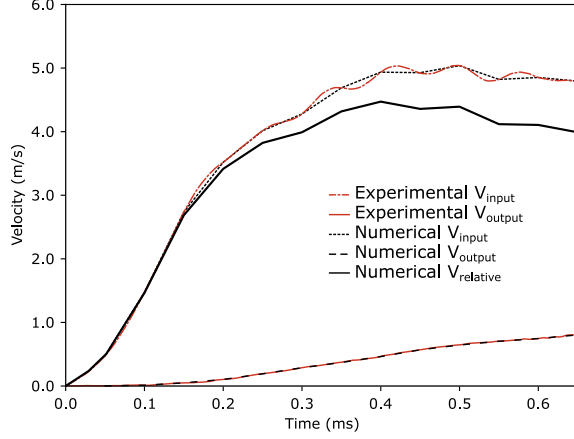


Figure 9: Experimental and numerical input and output bar velocities used to define the boundary conditions in the numerical simulations.

216 total energy in the system. The kinetic energy represented, on average, 0.6% of the total energy
 217 in the model. An element deletion criterion based on the determinant of the deformation gradi-
 218 ent was implemented to prevent unrealistic element distortion resulting from the strain-softening
 219 constitutive behavior [42].

$$\text{Delete element if } \left\{ \begin{array}{l} 0 < \det \mathbf{F} < 0.5 \text{ or } \det \mathbf{F} > 2.5 \end{array} \right. \quad (11)$$

220 5. Results and Discussion

221 5.1. Dynamic response of AP-PLY composites

222 This section analyzes the performance of AP-PLY composites at high strain rates by considering
 223 the results of the experimental and numerical studies together. Figure 10 presents the experimental
 224 and numerical stress-strain response of the AP-PLY specimens subjected to tensile loading at an
 225 average strain rate of 30 s^{-1} . Despite the interaction of secondary waves and the initial noise of
 226 the pulse, the experiments show good repeatability, see Table 2. The moduli of the specimens
 227 were estimated over the strain interval from 0.4% to 0.8%, after dynamic force equilibrium was
 228 established and avoiding the non-linear response outside of this strain range.

229 Numerical models exhibit good agreement with the experimental results. Predictions of the
 230 strengths of the cross-ply and quasi-isotropic specimens are within the experimental error bounds,
 231 differing by -5.2% and 7.0% from the experimental values, respectively. The discrepancy between
 232 the numerical prediction and experimentally determined quasi-isotropic stiffness is similarly small
 233 at only -1.3%. In all specimens, baseline and AP-PLY, the gradient of the stress-strain response
 234 increases incrementally at strains of around 0.2 - 0.4%, a phenomenon not registered at material
 235 level by the numerical model. Rather than reflecting a change in material behavior, the change in
 236 slope, which occurs before dynamic equilibrium is established, is thought to result from localized
 237 stress concentrations in the clamped area. These concentrations resulted in the premature failure
 238 of 4 cross-ply specimens in the bolted joints of the grips instead of in the gauge section. Micro-
 239 inertial effects during dilation of the specimen, as discussed in [43], are hypothesized not to have

240 affected the dynamic stress-strain response over the interval n which moduli were measured, as
 241 the specimens had all attained a state of dynamic force equilibrium at this point, and therefore
 242 accelerations within the specimens were likely to be negligible.

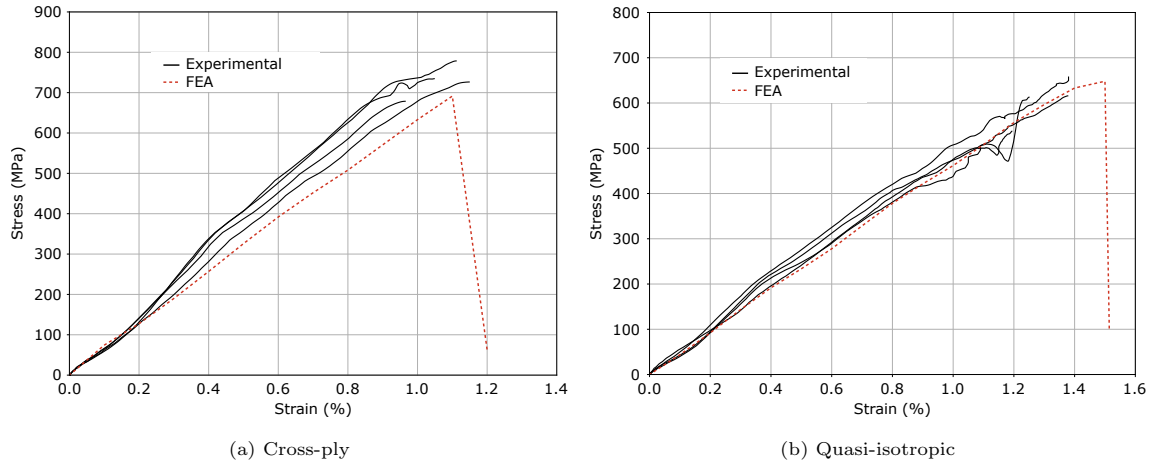


Figure 10: Comparison of experimental and numerically predicted stress-strain dynamic response of AP-PLY (a) cross-ply and (b) quasi-isotropic laminates.

Table 2: Experimental and numerical results of AP-PLY composites at high strain rates.

Conf.	Modulus (GPa)		Strength (MPa)	
	Experimental	Numerical	Experimental	Numerical
XP _{AP-PLY}	69.38 ± 3.29	64.91	729.57 ± 35.48	691.51
QI _{AP-PLY}	47.41 ± 2.63	46.78	605.89 ± 43.19	648.11

243 Fig. 11 and 12 compare the experimental and numerical evolution of the strain fields for AP-
 244 PLY laminates. The symmetry of the strain field measured using DIC, in which similar strain
 245 values are measured at both clamped edges, lends further credence to the assumption of force
 246 equilibrium in the specimen. The strain fields measured on the surface of the specimens depend
 247 on each laminate’s stacking sequence. The cross-ply laminate’s strain field is homogeneous over
 248 the central region, but strain gradients develop at the shoulders of the specimen (Figure 11). In
 249 contrast, the quasi-isotropic strain field is more heterogeneous, with higher strains occurring in an
 250 hourglass shaped region in the center of the specimen (Figure 12).

251 The simulations are able to capture the overall macro-deformation of the specimens, as well as
 252 the location and size of the strain micro-gradients at the tow undulations. These microgradients
 253 have been previously registered experimentally during quasi-static testing [5]. In the present work,
 254 the resolution of the DIC system was insufficient to capture the strain gradients at the tow un-
 255 dulations. As mentioned in section 3 the spatial resolution of the DIC system was approximately
 256 3 mm, in excess of the size of the undulation regions, of approximately 1.5 mm.

257 The damage mechanisms are effectively captured by the numerical models. Matrix cracking
 258 initiates in undulation regions near the specimen shoulders at approximately 0.6% nominal strain.
 259 Localized matrix softening places additional stress on the fiber tows in these areas, inducing fiber

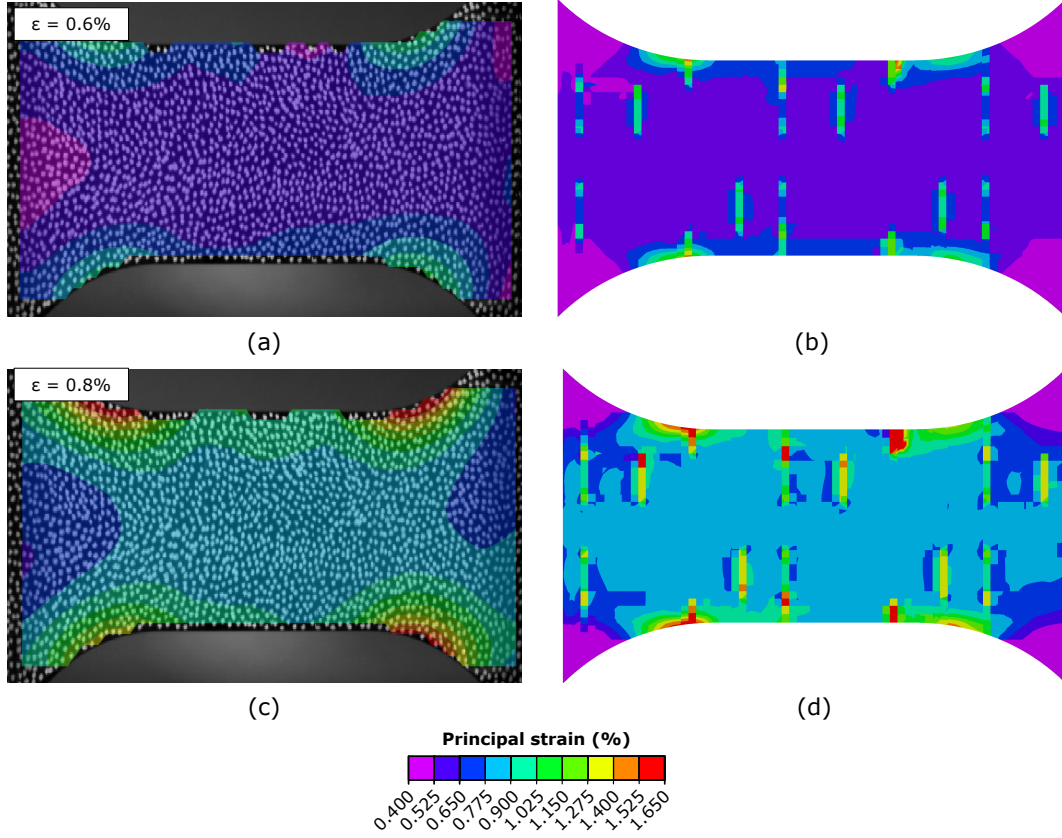


Figure 11: Experimental (a) & (c) and numerical (b) and (d) principal strain contours on cross-ply AP-PLY specimens at 0.6% and 0.8% nominal strain.

260 fracture. In the cross-ply specimens, catastrophic failure through fiber fracture occurs on a plane
 261 orthogonal to the loading direction, near the specimen shoulder, see Figure 13. In the quasi-
 262 isotropic specimens, the failure surface is v-shaped (i.e. at 45° angles to the loading direction), a
 263 phenomenon which is reflected in the experimental results, see Figure 14. Equally well represented
 264 is the extensive matrix damage occurring in the vicinity of the fracture plane.

265 5.2. Influence of undulations at high strain rates

266 Table 3 summarizes the experimental results at quasi-static and dynamic strain rates. It in-
 267 cludes both stacking sequences (cross-ply and quasi-isotropic) and also compares AP-PLY and
 268 baseline laminates. The quasi-static results were obtained from a previous study by the same

Table 3: Quasi-static vs dynamic laminate moduli and strengths.

Configuration	Modulus [GPa]		Strength [MPa]	
	$25 \times 10^{-4} s^{-1}$	$30 s^{-1}$	$25 \times 10^{-4} s^{-1}$	$30 s^{-1}$
XP _{AP-PLY}	65.27 ± 3.53	69.38 ± 3.29	1060.31 ± 47.55	729.57 ± 35.48
XP _{base}	63.59 ± 1.23	62.01 ± 3.63	1273.16 ± 55.61	683.58 ± 68.03
QI _{AP-PLY}	44.96 ± 0.57	47.41 ± 2.63	705.67 ± 28.85	605.89 ± 43.19
QI _{base}	44.56 ± 0.95	43.88 ± 1.51	655.90 ± 29.79	601.23 ± 38.47

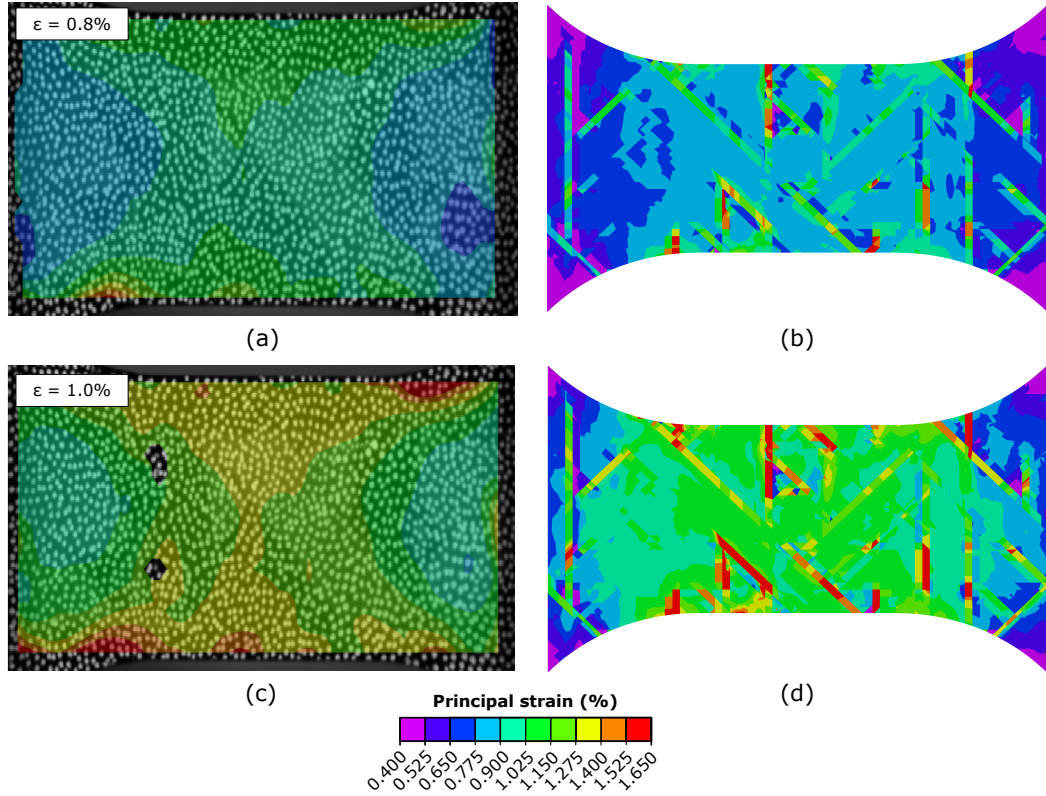


Figure 12: Experimental (a) & (c) and numerical (b) and (d) principal strain contours on quasi-isotropic AP-Ply specimens at 0.8% and 1.0% nominal strain.

269 authors [5]. It should be noted that the dimensions of the specimens studied in the quasi-static
 270 regime differed from those in the dynamic regime. In the former, the specimens were adapted
 271 from the ISO 527 standard, and measured 250 mm in length, 40 mm in width, and approximately
 272 1.6 mm in thickness.

273 Given the overlapping error bounds, we conclude there is no significant difference between the
 274 moduli of the AP-Ply specimens at high and low strain rates. Similarly, there is no appreciable
 275 strain rate dependency in the baseline laminates. Figure 15 presents the quasi-static and dynamic
 276 response of the AP-Ply and baseline laminates. In the dynamic regime, there are marginal im-
 277 provements in laminate stiffness resulting from the AP-Ply preforming process. However, given
 278 the complexity of the dynamic experiments and the intrinsic oscillations in the stress-strain re-
 279 sponse, the discrepancy may be the result of experimental scatter alone. The same conclusion was
 280 drawn at quasi-static strain rates, where the preforming process also had a negligible impact on
 281 the stiffness of the laminates [5]. As previously acknowledged, the dimensions of the specimens
 282 tested in the quasi-static and dynamic regime differed. It is well known that larger specimen sizes
 283 may result in lower strengths, especially for specimens tested in tension [44]. To evaluate whether
 284 this was the case in the present study, a small number of quasi-static tests were conducted using
 285 specimens identical to those used in the high strain rate tests. Failure strengths and moduli for
 286 these specimens were within 10% of the experimental results obtained using the smaller specimens.

287 The strength of all the specimens, both AP-Ply and baseline, is significantly reduced at high

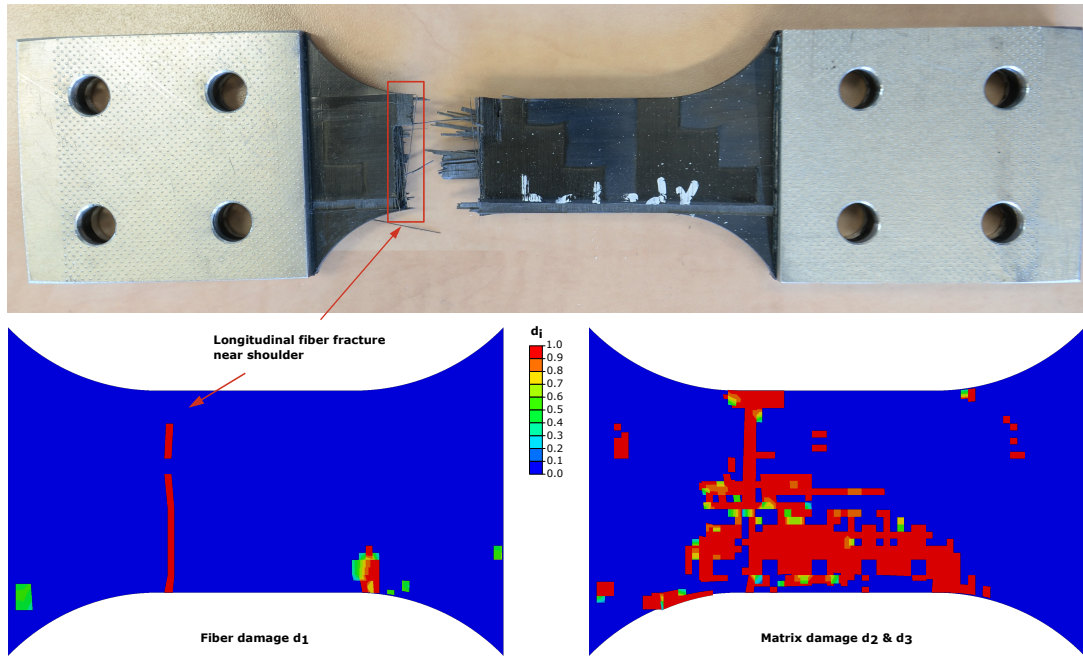


Figure 13: Experimentally observed failure modes and simulated damage envelopes in a cross-ply AP-PLY laminate.

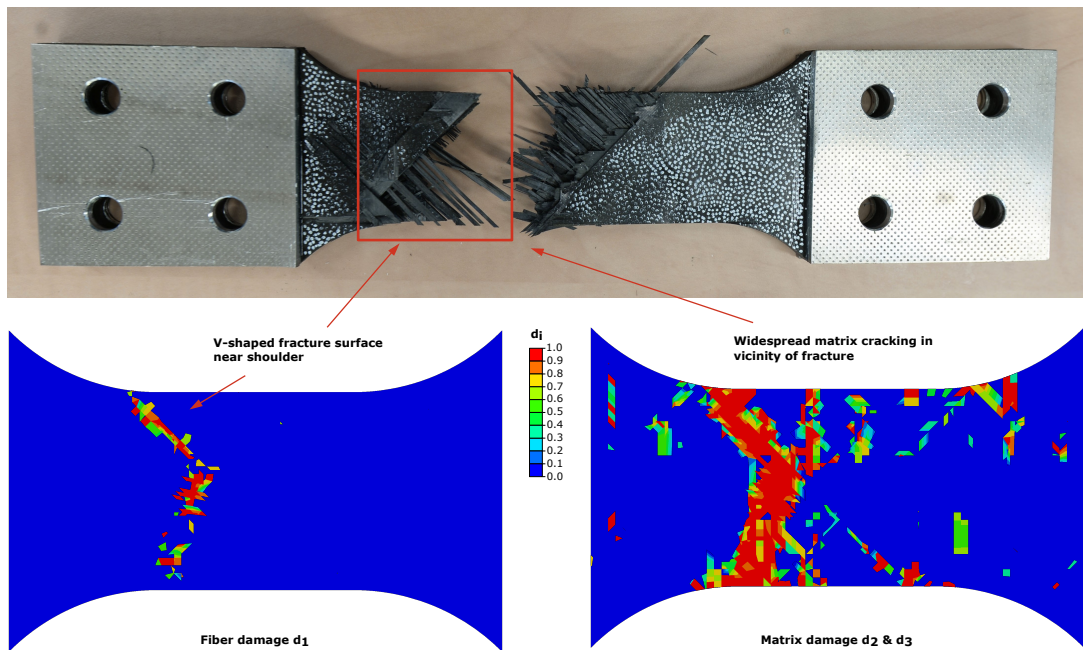


Figure 14: Experimentally observed failure modes and simulated damage envelopes in a quasi-isotropic AP-PLY laminate.

288 strain rates. The proximity of the failure plane to the specimen shoulders, and the strain concentra-
 289 tions measured using DIC, suggest that this lower strength may be a consequence of the geometry
 290 of the specimens, rather than strain rate dependency at the material level. As mentioned pre-
 291 viously, brittle carbon fiber composites are sensitive to mechanical gripping at high strain rates,
 292 potentially reducing their measured strength [20]. Moreover, while stress concentrations arising
 293 from the through-thickness reinforcements in the cross-ply AP-PLY laminates *could* trigger failure

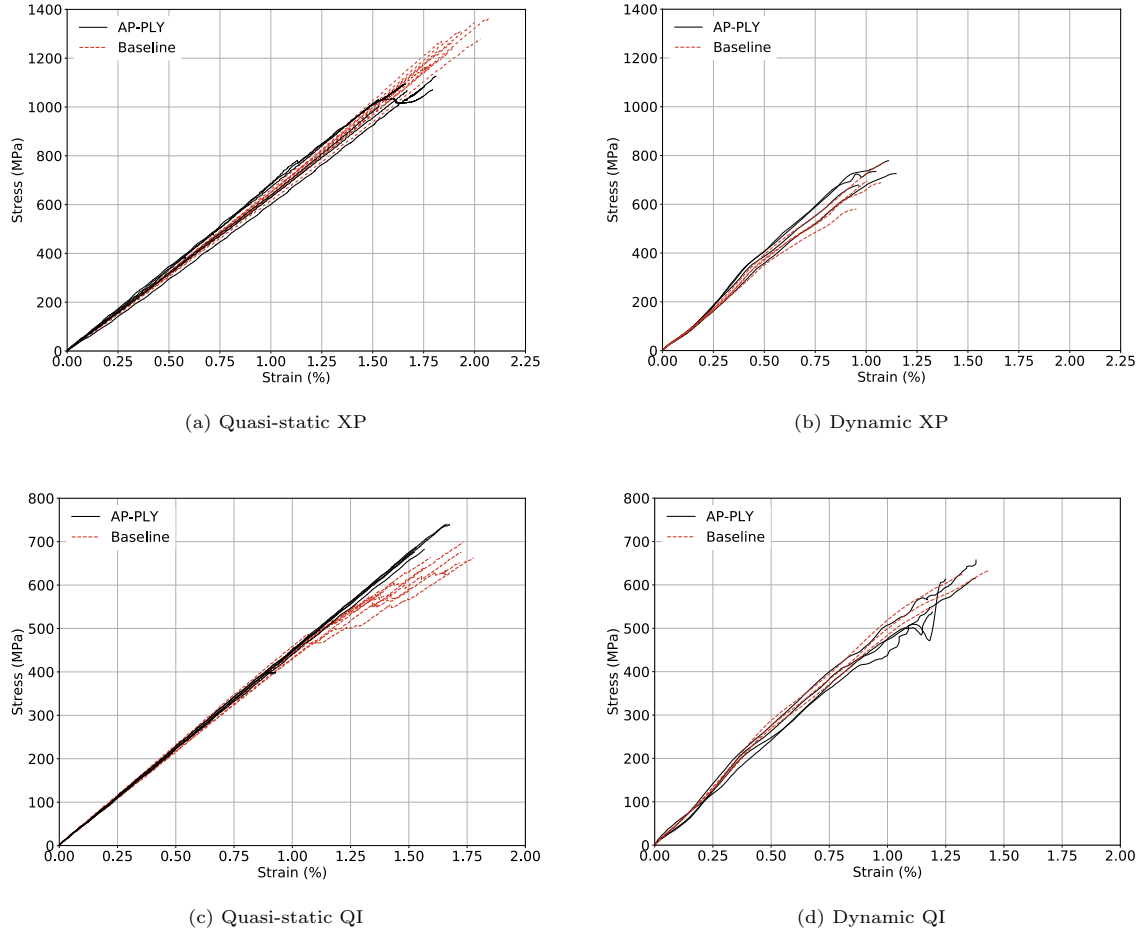


Figure 15: Stress-strain response of (baseline and AP-PLY) cross-ply and quasi-isotropic laminates under quasi-static (a) & (c) and dynamic (b) & (d) loading.

294 in the specimens at relatively low loads, the fact that the strength of the baseline laminates was
 295 reduced to a similar or greater extent suggests that the fiber undulations are not the primary
 296 cause of the low dynamic tensile strength. The reduction in the quasi-isotropic specimen strength
 297 at high strain rates is less substantial compared with the cross-ply specimens. The high strain
 298 rate strengths of the cross-ply baseline and AP-PLY specimens fell by 46% and 32% respectively,
 299 relative to their quasi-static strength, while the reduction in quasi-isotropic baseline and AP-PLY
 300 strengths were only 8% and 14% respectively. This is because, as illustrated in Figure 12, the
 301 strain concentrations at the shoulders of the quasi-isotropic specimen are less pronounced than in
 302 the cross-ply specimens. A possible explanation for the smaller magnitude of these strain concen-
 303 trations is the greater distribution of tow orientations, and as a result the smaller mismatch angles
 304 between tows.

305 At high strain rates, the strengths of the cross ply AP-PLY laminates were found to be insen-
 306 sitive to the internal architecture. This contrasts with data from the quasi-static regime, in which
 307 the strength of cross-ply laminates was negatively affected (-17% loss) by the AP-PLY preform-
 308 ing process [5]. A plausible explanation for this result is that the through thickness undulations
 309 present in an AP-PLY laminate are more effective as crack arrestors in the dynamic than in the

310 quasi-static regime. At low strain rates, undulating tows straighten along the loading direction
311 as the specimens are stressed. This alignment progressively increases the magnitude of the strain
312 gradients at the undulations, resulting in reductions to laminate strength. At high strains rates
313 however, there is insufficient time for tow rotation to occur. As a result, the strain concentration
314 factors at through thickness undulations are smaller, while the reinforcement that these features
315 provide is unaffected. The through thickness connectivity in the laminate mitigates the formation
316 and propagation of matrix cracks, delaying softening and improving the strength of the AP-PLY
317 cross-ply laminates.

318 In contrast to the cross-ply results, the trends in quasi-isotropic laminate strength were sim-
319 ilar for both high and low strain rate loading. In both the quasi-static and dynamic regimes,
320 the discrepancy between the AP-PLY and baseline strengths was within the experimental error
321 bounds, with the former generally exhibiting marginally higher strengths. The tow straighten-
322 ing effects hypothesized to occur in the cross-ply laminates are likely to be less significant in the
323 quasi-isotropic composites, because the former contain a larger proportion of tows oriented with
324 the loading direction, in which the aforementioned dynamic deformation mechanisms will be more
325 significant, and because the mismatch angles between tows in the quasi-isotropic laminates are gen-
326 erally smaller, reducing the magnitude of the strain concentrations. Furthermore, in the AP-PLY
327 laminates, matrix cracks formed predominantly at the boundaries between tows, rarely splitting a
328 tow in the transverse direction. This contrasts with the more widespread matrix cracking observed
329 in the baseline laminates, and may explain the slightly higher average strengths of the AP-PLY
330 laminates in both loading regimes.

331 The numerical model predictions of stiffness and strength at both low and high strain rates are
332 in good agreement with the experimental results, despite using strain rate independent material
333 properties [5]. This suggests that the effect of the strain rate at the material level is minor, and
334 that the realignment of the fibers may play a larger role. Carbon fiber epoxy composites are strain
335 rate insensitive in the fiber direction [10, 45, 46], and at the relatively low dynamic strain rates
336 attained in this study (30 s^{-1}), the transverse properties are likely to be only minimally affected
337 [10, 46]. While microscale numerical modeling and/or in-situ high-speed synchrotron tomography
338 might shed further light on the underlying causes of the discrepancy between the baseline and
339 AP-PLY specimens at high strain rates, they are beyond the scope of this study. Note that at
340 strain rates higher than those studied in the present work (30 s^{-1}), the strain rate sensitivity of the
341 matrix or fibers may have a more significant effect on laminate behavior, and the inclusion of strain
342 rate dependent material models may improve the accuracy of numerical simulation predictions.

343 In summary, these findings prove that the through thickness tow undulations present in an
344 AP-PLY composite do not have a detrimental effect on its dynamic mechanical properties. Fur-
345 thermore, through thickness undulation have the capacity to arrest cracks, delaying the propagation
346 of delamination, and, depending on the laminate configuration, improving the laminate strength.
347 This contrasts with AFP defects e.g. tow overlaps or tow gaps, which have been observed to re-
348 duce a composite's strength [47]. While overlaps and gaps are unpredictable features that occur

349 randomly throughout a laminate, the through thickness undulations introduced by the AP-PLY
350 process occur in a structured pattern and, more importantly, can be strategically distributed to
351 improve the local damage tolerance of composite structures subjected to dynamic loads.

352 **6. Conclusions**

353 The high strain rate tensile behavior of AP-PLY composites was investigated. Due to the large
354 representative volume elements and brittle nature of the laminates, experiments were conducted at
355 the European Laboratory for Structural Assessment, one of the only laboratories worldwide capa-
356 ble of accurately analyzing this family of composite materials. The bespoke SHB equipment and
357 the relatively low impedance design of the clamps ensured dynamic force equilibrium was rapidly
358 established, providing accurate measurements even at low strains. In addition, the SHB experi-
359 ments were simulated using a multiscale numerical modeling framework to gain further insight into
360 the high strain rate deformation mechanisms of the novel pseudo woven composites.

361 Quasi-isotropic and cross-ply AP-PLY specimens were subjected to tensile loading at a strain
362 rate of approximately 30 s^{-1} . The moduli of the AP-PLY composites were found to be independent
363 of the strain rate. While the dynamic experimental AP-PLY laminate strengths were significantly
364 less than the quasi-static strengths, this discrepancy was attributed to the geometry of the speci-
365 mens and the resulting strain concentrations, rather than strain rate dependency in the constituent
366 materials. Numerical model results provided further evidence that the material strength of the
367 AP-PLY composites was not affected by the higher strain rate.

368 The response of the AP-PLY laminates was compared with baseline — non AP-PLY — lami-
369 nates to quantify the effect of the three-dimensional reinforcement. The through thickness undu-
370 lations introduced by the AP-PLY preforming process did not result in a reduction in laminate
371 stiffness in the dynamic regime. While the dynamic AP-PLY laminate moduli were found to be
372 greater than those of the baseline laminates, the discrepancies were small, and could be attributed
373 to the resolution of the SHB equipment. In terms of strength, different trends were obtained de-
374 pending on the predominant failure micromechanism. The failure of the quasi-isotropic AP-PLY
375 laminates was dominated by localized matrix cracking at the tow boundaries regardless of the
376 applied strain rate. This mechanism promoted tow debonding rather than the extensive matrix
377 cracking observed in the baseline laminates, showing the capacity of the AP-PLY architecture
378 to influence laminate deformation. As a result, the quasi-isotropic AP-PLY laminates exhibited
379 slightly higher strengths than their baseline non AP-PLY counterparts at both high and low strain
380 rates. In the cross-ply AP-PLY laminates, strain concentrations at through thickness undulations
381 were found to be the catalysts for failure at low strain rates. In the dynamic regime however, these
382 concentrations had a much smaller impact on the laminate response. This change in behavior was
383 attributed to reduced out-of-plane tow straightening, resulting in smaller strain gradients at tow
384 undulations. As a result, the reduction in cross-ply AP-PLY laminate strength, relative to the
385 baseline, registered in the quasi-static loading regime, was not observed at high strain rates.

386 In summary, at high strain rates, the strain concentrations induced by the geometry of the
387 individual tapes at through thickness undulations and tow boundaries were less significant. As a
388 result, no reduction in AP-PLY stiffness nor strength in comparison to the baseline laminates was
389 obtained. These results prove AP-PLY laminates are effective substitutes for conventional angle-
390 ply laminates in dynamic loading scenarios. They possess the same exceptional specific stiffness as
391 angle-ply laminates, while their improved damage tolerance at high strain rates can result in higher
392 strengths — depending on the stacking sequences. Future studies will investigate the low-velocity
393 impact response of AP-PLY laminates.

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