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1	Evaluating the accuracy of the Distributed Activation Energy Model for
2	biomass devolatilization curves obtained at high heating rates
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11 ABSTRACT

12 The characteristic parameters of devolatilization, the activation energy and the 13 frequency factor, can be obtained following different experimental approaches. In the 14 Distributed Activation Energy Model (DAEM), these parameters are derived from 15 several TGA curves that are typically obtained for constant, low heating rate experiments. Then, the results are used to model high heating rate processes typical 16 17 of industrial combustors. In this work, a wide range of heating rates were employed 18 to obtain different TGA curves of the biomass pyrolysis, in order to analyse the 19 validity of DAEM when extrapolating the kinetic parameters obtained for low heating 20 rate curves used in the laboratory to higher heating rates present in industrial 21 applications. The TGA curves of the biomass pyrolysis employed in DAEM were 22 varied from low heating rates (around 10 K/min, values typically found in the literature on DAEM), to high heating rates (up to 200 K/min). The differences in the activation energy and the frequency factor obtained for different heating rates, were evaluated and the validity of the model was discussed. The results show differences between the activation energy and the frequency factor obtained using low and high heating rates during the TGA tests. Therefore, if an accurate approximation is required when extrapolating the data to high heating rates, the tests should be carried out at high heating rates.

30 KEYWORDS

Distributed Activation Energy Model, devolatilization, pyrolysis, biomass conversion,
 activation energy, heating rate.

33 NOMENCLATURE

- 34 *a* Heating rate [K/s].
- 35 *E_a* Activation energy for a determined devolatilization rate [J/mol].
- 36 k_0 Frequency factor for a determined devolatilization rate [s⁻¹].
- 37 *R* Universal constant [J/mol·K].
- 38 *R*² Determination coefficient of the linear fitting [-].
- 39 *T* Temperature [K].
- 40 V Volatile mass loss [%].
- 41 V^* Volatile content [%].
- 42 V/V^* Devolatilization rate [%].

43 ε Relative error [%].

44 **1. Introduction**

45 Biomass pyrolysis takes place during most of the processes related to biomass thermochemical conversion, such as production of liquid biofuels [1], synthesis gas 46 47 [2], chemicals [3], or charcoal [4], becoming a key factor in most applications. The 48 characteristic parameters that control the kinetics of biomass devolatilization are the 49 activation energy (E_a) and the frequency factor (k_0). Several models are available in 50 literature to describe biomass pyrolysis [5], [6], [7], and between them the Distributed 51 Activation Energy Model (DAEM) proposed by Vand [8] has been widely used due to 52 its simplicity and accuracy. Miura and Maki [9] simplified the model to estimate the activation energy and the corresponding frequency factor from three TGA curves 53 54 obtained for different heating rates. This simplification has been used to describe the 55 kinetics of pyrolysis for different types of biomass [10], [11], [12], [13], [14], coal [15], [16], sewage sludge [17], [18], and waste [19], [20], [21]. 56

57 The heating rates employed using DAEM are usually low, in the range of 3 to 30 K/min, due to the higher accuracy of TGA at reduced heating rates. Miura and Maki 58 59 [9] proposed the use of heating rates of 5, 10 and 20 K/min, but Sonobe et al. [10] 60 employed even lower heating rates 2, 4 and 10 K/min. Shen et al. [11] employed 61 heating rates between 5 and 40 K/min and Soria-Verdugo et al. [18] used heating 62 rates of 10, 15, 20 K/min. Despite of the variety of heating rates found in the literature 63 most of the authors used heating rates below 50 K/min. As an exception, Li et al. [15] used heating rates of 20, 35, 50, 75 and 100 K/min during the devolatilization of coals 64 65 and biomass in a thermogravimetric analyzer, nevertheless there is no available data for heating rates beyond 100 K/min. 66

67 In this work, a wider range of heating rates (3, 5, 10, 15, 20, 30, 50, 80, 100, 150 and 68 200 K/min) were employed to obtain different TGA curves, in order to analyse the 69 validity of the simplified Distributed Activation Energy Model, when extrapolating the 70 kinetic parameters obtained for low heating rate curves to higher heating rates. The simplified DAEM process described by Miura and Maki [9] to obtain the pyrolysis 71 72 parameters was analyzed for the different heating rates, therefore the three TGA 73 curves employed were varied from very low heating rates (3, 5 and 10 K/min) to higher heating rates (100, 150 and 200 K/min). The differences in the activation 74 75 energy and the frequency factor were evaluated and the validity of the model was 76 discussed.

77 2. Experimental procedure

The biomass employed during the tests was obtained from commercial pine pellets. 78 79 The biomass characterization results of a proximate and ultimate analysis are 80 presented in Table 1. The proximate analysis was performed in a TGA Q500 TA 81 Instruments, while the ultimate analysis was carried out in a LECO TruSpec CHN 82 and TruSpec S elemental analyzer. The moisture of the sample was obtained after 83 an isothermal process at 105°C under an inert atmosphere in the TGA, whereas the volatile content was determined heating the sample up to 900°C under an inert 84 85 atmosphere, and maintaining the temperature until no difference in the mass of the 86 sample was observed. The ash content was measured as the constant mass of the sample remaining after an isothermal process at 550°C under and oxidant 87 88 atmosphere. Finally, the fixed carbon of the sample was obtained by difference.

Proximate analysis ^a	l
Moisture [%]	3.3
Volatiles [%]	76.3
Fixed carbon ^b [%]	17

Ash [%]	3.4
Ultimate analysis ^a	
C [%]	46.13
H [%]	6.51
N [%]	0.82
S [%]	0.07
O ^b [%]	46.47

89

90	Table 1. Thermochemical characterization of the biomass employed (^a wet basis, ^b
91	obtained by difference).

92 The devolatilization tests were carried out in the same thermogravimetric analyzer 93 TGA Q500 TA Instruments employed to obtain the biomass proximate analysis. 94 During the experiments, the TGA furnace was flushed with 60 ml/min of nitrogen to 95 maintain an inert atmosphere. The mass of the samples were 10±0.5 mg and they were sieved under 100 µm to avoid heat transfer effects, according to Di Blasi et al. 96 97 [22]. A blank experiment was also run for any case studied to avoid buoyancy effects [11], [12]. Each test was repeated five times to guarantee repeatability, obtaining 98 99 differences always lower than 3%.

100 Once the sample was introduced in the TGA, it was heated up to 105°C from room 101 temperature, and an isothermal process was maintained during 20 minutes to 102 eliminate all the moisture content. Then, the devolatilization process begins, and the 103 temperature increases with a constant heating rate a until 600°C. Fig. 1 shows the 104 weight loss and the temperature versus time for the TGA analysis using heating rates 105 a of 20 and 200 K/min during the devolatilization process. The drying process is the 106 same for both tests so the weight loss curves collapsed during the first part of the 107 analysis, nevertheless the different heating rates employed in the devolatilization 108 process produced significant differences on the sample weight loss curves when the 109 pyrolysis occurred. Depending on the heating rate used during the devolatilization

process, the time needed for the test can be very different, from 68 minutes for the heating rate of 20 K/min to just 45 minutes when using 200 K/min, nonetheless the weight percentage loss at the end of the devolatilization is independent of the heating rate employed. During the experiments several heating rates were employed during the devolatilization process, in a wide range: *3, 5, 10, 15, 20, 30, 50, 80, 100, 150*, and *200 K/min*. In the case of a heating rate of 3 K/min, 210 minutes were needed to perform the test.



Figure 1: Example of a thermogravimetric analysis (*a* = 20 K/min and 200 K/min)

117

119 Finally, since this work is not focused in the drying process but in the devolatilization 120 process, the range of devolatilization can be obtained from the TGA curve (Fig. 1), 121 defining a devolatilization rate of 0% at the end of the isothermal process at 105°C, 122 and 100% when the temperature is 550°C, ensuring a constant heating rate, *a*, for the whole devolatilization process. Fig. 2 shows the devolatilization rate as a function 123 124 of temperature for the same heating rates depicted in Fig. 1. It can be observed that most of the devolatilization process occurs between 300°C and 400°C, obtaining a 125 126 sharp devolatilization rate typical of cellulose.





128 Figure 2: Devolatilization rate against temperature (*a* = 20 K/min, 200 K/min)

129 **3. Simplified DAEM model**

The Distributed Activation Energy Model has been proved to be an accurate method to describe the pyrolysis kinetics of biomass, obtaining a good agreement with the experimental data [10], [23], [24], and [25], when operating at low heating rates. The model assumes the existence of an infinite number of irreversible first order reactions occurring sequentially, with different associated activation energies, E_a . The devolatilization process can be described in the integral form by Eq. 1:

136
$$1 - \frac{V}{V^*} = \int_0^\infty \exp\left(-k_0 \int_0^t e^{-E/RT} dt\right) f(E) dE$$
(1)

where V/V^* is the devolatilization rate, *R* the universal constant, *T* the temperature for each devolatilization and *f*(*E*) the distribution function of the activation energy. This equation was simplified to Eq. 2 by Miura et al. [26]

140
$$V/V^* \cong 1 - \int_{E_a}^{\infty} f(E_a) dE_a = \int_0^{E_a} f(E_a) dE_a$$
 (2)

141 The Arrhenius equation of the simplified DAEM model is:

142
$$\ln\left(\frac{a}{T^2}\right) = \ln\left(\frac{k_0 R}{E_a}\right) + 0.6075 - \frac{E_a}{R} \frac{1}{T}$$
 (3)

The values of the activation energy, E_a , and the corresponding frequency factor, k_0 , present in Eq. 3 can be obtained from three different thermogravimetric curves obtained with different heating rates. Miura and Maki [9] proposed a procedure following the next steps:

- 147 a) Measure and plot the devolatilization rate, V/V*, as a function of the temperature,
 148 *T*, for three different heating rates, *a*.
- b) Plot $\ln(a/T^2)$ versus 1/T for the three different heating rates at each devolatilization

150 rate (Arrhenius plot).

151 c) For each V/V^* in the Arrhenius plot, linearize the data of the different heating rates 152 and obtain E_a and k_0 from the slope and the intercept respectively.

153 **4. Results and discussion**

154 Thermogravimetric tests were carried out for heating rates of 3, 5, 10, 15, 20, 30, 50,

155 80, 100, 150, and 200 K/min, obtaining the devolatilization rates plotted in Fig. 3 for

156 each heating rate. The devolatilization takes place at higher temperatures when

157 increasing the heating rate, a result previously reported in the literature that can be

atributed to non-isothermal pyrolysis processes [27], [28].







Following the procedure proposed by Miura and Maki [9], the temperature at which each devolatilization rate occurs can be obtained from Fig. 3, for each heating rate. With these temperatures, an Arrhenius plot can be built, plotting $\ln(a/T^2)$ versus 1/T, as shown in Fig. 4 for each devolatilization rate, with variations of 5%.



165

166

Figure 4: Arrhenius plot for each devolatilization rate.

The next step in the procedure described by Miura and Maki [9] is the linearization of the results shown in the Arrhenius plot for each devolatilization rate. Analising Fig. 4 for low devolatilization rates ($V/V^* = 5\%$), it can be observed that there is a change in the slope of the linearization curve for heating rates over 50 K/min. For high 171devolatilization rates this is not so evident. In order to quantify the goodness of a172linear fitting of the results considering all the heating rates, the determination173coeficient, R^2 , of the linear fitting is shown in Fig. 5, as a function of the174devolatilization rate. The determination coeficient is found to be lower at low175devolatilization rates informing of a poor linearity of the data in this zone, confirming176the idea that there is a change in slope for low devolatilization rates obtained from177the visual inspection of Fig. 4.



Figure 5: Determination coefficient of the linear fitting for all the heating rates as a
function of the devolatilization rate.

178

181 The linearization of the results shown in the Arrhenius plot (Fig. 4) was carried out 182 regrouping the data for three different heating rates as suggested by Miura and Maki 183 [9]. The experimental data allows to linearize the results for very low heating rates (a = 3, 5, 10 K/min), low heating rates (a = 15, 20, 30 K/min), medium heating rates (a = 184 50, 80, 100 K/min) and high heating rates (a = 100, 150, 200 K/min), in order to 185 quantify the variation of slope stated above. The linearization of the results for each 186 187 group of heating rates provides an slope, *m*, and an intercept, *n*, from which the activation energy, E_a , and the frequency factor, k_0 , can be easily obtained in view of 188 189 Eq. 3, obtaining Eq. 4 and 5.

$$190 E_a = -m \cdot R (4)$$

191
$$k_0 = -m \cdot e^{n - 0.6075}$$
 (5)

192 The values of the activation energy and the frequency factor are presented in Fig. 6 193 a) and b) respectively, as a function of the devolatilization rate for very low, low, 194 medium and high heating rates. There is a clear difference in both the activation 195 energy and the frequency factor when linearizing the results obtained for low and 196 high heating rates. These parameters increase when higher heating rates are 197 employed, confirming the existence of a higher slope in the linearization of the high 198 heating rate TGA curves (a = 100, 150, 200 K/min). The difference is larger at low 199 devolatilization rates, as established in Fig. 5.





The difference in activation energy obtained between each group of heating rates and the higher one can be analyzed by means of a relative error, ε , defined in Eq. 6.

204
$$\varepsilon = 100 \cdot \frac{E_{a_{i,j,k}} - E_{a_{100,150,200}}}{E_{a_{100,150,200}}}$$
 (6)

The results of the relative error in activation energy can be observed in Fig. 7. A relative error around 20% for the medium heating rates (a = 50, 80, 100 K/min) and around 40% for low (a = 15, 20, 30 K/min) and very low heating rates (a = 3, 5, 10K/min) is found for devolatilization rates between 20 and 80%, that is, for most of the devolatilization process. Therefore, an error around 40% is made when determining the activation energy with low heating rate TGA curves typically found in the literature and extrapolating the results to high heating rates.



212

Figure 7: Relative error of the activation energy obtained from low and high heating
rates.

215 Finally, with the activation energy and the pre-exponential factor, the devolatilization 216 curve for a heating rate of 200 K/min can be recuperated and the differences 217 between the experimental curve obtained from the TGA and the curve recuperated using DAEM can be evaluated. The recuperation could be carried out by solving the 218 219 temperature in Eq. 9 or linearizing the Arrhenius plot for each heating rate, as 220 described in [19], with negligible differences. The differences between the TGA curve 221 obtained for a heating rate of 200 K/min and the curve recuperated using the 222 Distributed Activation Energy Model with low (a = 15, 20, 30 K/min) and high heating

rates (*a* = 100, 150, 200 K/min) were analyzed by means of the devolatilization rate error and the temperature error described in Eq. 7 and 8 respectively.

225
$$\varepsilon_{V/V^*} = 100 \cdot \frac{V/V^*_{DAEM} - V/V^*_{TGA}}{V/V^*_{TGA}}$$
 (7)

$$226 \qquad \varepsilon_T = 100 \cdot \frac{T_{DAEM} - T_{TGA}}{T_{TGA}} \tag{8}$$

227 The error obtained for the devolatilization rate is plotted in Fig. 8 a). It can be 228 observed that the DAEM recuperated curve coincided with the experimental curve 229 when using the high heating rates (a = 100, 150, 200 K/min), obtaing and error close 230 to zero. Nevertheless, when recuperating the curve with the activation energy and pre-exponential factor obtained for low heating rates (a = 15, 20, 30 K/min) the error 231 232 in devolatilization rate is not negligible. In this case a higher error is obtained for low 233 temperatures where the devolatilization rate is low, but for temperatures between 234 300°C and 400°C, where most of the devolatilization process occurs, the devolatilization error is between 5 and 10%. In the case of the temperature error, 235 236 show in Fig. 8 b), the value of the error is around 1% for devolatilization rates 237 between 20 and 80%. The higher error obtained for the devolatilization rate, in 238 comparison to that of the temperature, is motivated by the high slope shown in the 239 devolatilization rate curve (Fig. 2) for this type of biomass.





242

241 Figure

Figure 8: Error between the TGA curve for a heating rate of 200 K/min and the curve recuperated using DAEM, a) Devolatilization rate error b) Temperature error.

This result show a certain weakness of the standard process of obtaining the devolatilization parameters, E_a and k_0 , at low heating rates, as defined by Miura and Maki [9]. Even though the error obtained when extrapolating the activation energy obtained for low heating rates to higher rates can be as high as 50%, the final error obtained in the devolatilization curve is around 10% for *V*/*V*^{*} and just 1% for *T*. This error should be considered for and accurate description of the devolatilization process.

250 **5. Conclusions**

251 The Distributed Activation Energy Model (DAEM) was applied to study pine pellets

devolatilization. The model is based on TGA curves obtained for several heating

rates, from low heating rates usually found in literature (3, 5, 10, 15, 20, 30, 50

K/min) to higher heating rates rarely reported (*80, 100, 150, 200 K/min*).

The Miura and Maki procedure was employed to obtain the activation energy and the frequency factor for each devolatilization rate. The procedure was repeated for very low heating rate curves (*3, 5, 10 K/min*), low heating rate curves (*15, 20, 30 K/min*), 258 medium values (*50, 80, 100 K/min*) and high heating rates (*100, 150, 200 K/min*) to 259 analyze the possible differences obtained. Such differences were quantified obtaining 260 a relative error for the activation energy around 40% when extrapolating the results of 261 low heating rates to higher ones. Nonetheless, when comparing the experimental 262 devolatilization curve for a heating rate of *200 K/min* with the curve obtained applying 263 DAEM to low heating rates, the error in the devolatilization rate is under 10% and the 264 error in temperature is just 1%.

Therefore, care should be taken when employing DAEM from low heating rate TGA
curves and extrapolating the results to high heating rates typical of industrial
combustors.

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