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# Analysis and implementation of the Autotransformer Forward-Flyback converter applied to photovoltaic systems 

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#### Abstract

: The Distributed Maximum Power Point Tracking (DMPPT) architecture is employed to overcome the mismatching phenomena in grid-tied photovoltaic (PV) installations. In this kind of architecture, a DC-DC module integrated converter (MIC) manages each PV panel. Thanks to the DC-DC converters, the differences between PV panels do not influence others, maximising the amount of harvested power. The MIC requirements to make this kind of solutions profitable are high efficiency, low cost and the capability of voltage step-up and step-down. This paper analyses the Autotransformer Forward-Flyback (AFF) converter. This converter is considered as a MIC candidate for fulfilling the requirements above. The study of the AFF converter includes the steady-state analysis and the small signal analysis in continuous conduction mode. The AFF converter advantages are its step-up and step-down voltage transfer function; a higher simplicity since it only includes a single controlled switch; the soft switching characteristics in all the diodes; the use of an autotransformer; and good dynamic performances. A step-by-step design procedure focused on a100 kW grid-tied PV installation, with some PV panels affected by shadows, is explained. The theoretical analyses are validated through the experimental results in a 225 W AFF prototype, achieving an efficiency up to $94.5 \%$.


Keywords: DC/DC converter, photovoltaic, efficiency, DMPPT, module integrated converters, autotransformer

## 1. Introduction

Photovoltaic energy is one of the most relevant energy sources. As shown in Figure 1, the PV Cell/Module production is almost exponentially increasing from 2010 to 2018 [1]. This fact, along with the social awareness makes this field worthy and motivates research in the improvement of current PV conversion technologies and the development of new ones.


Figure 1. World PV Cell/Module Production from 2010 to 2018 [1]

Many PV panels are required to generate a high amount of power in PV grid-tied installations. To improve the inverter efficiency, it is a good practice to keep constant the inverter's input voltage. Several PV panels are connected in series in the same string to achieve the desired inverter input voltage. It is well known that PV panels connected to the same string share the same output current.

Therefore, a variation in the electrical characteristic of one of the PV panels connected to the string implies a variation in the rest of the string-connected PV panels, reducing the generated power drastically, even when the irradiation conditions are optimum.
The difference in the PV panels characteristics or the environmental conditions is known as the mismatching phenomena. This issue is considered as one of the most critical issues in PV installations. The mismatching is commonly caused by temperature differences, dirt, shadows, aging, etc., [2] - [3]. The mismatching effect in the PV panel electrical characteristics is deeply studied in the literature [4] - [7]. To overcome the mismatching issue, one of the most standard solutions is the isolation of each PV panel from the rest of the PV panels in the PV installation. A DC-DC Module Integrated Converter (MIC) can be used to achieve the isolation and the maximum harvested power. This kind of PV architecture is known as Distributed Maximum Power Point Tracking (DMPPT) architecture [8] - [14], see Figure 2. The main drawback of DMPPT architectures is the high number of MIC required, that increase the cost of the installation.


Figure 2. PV grid-tied installation with the DMPPT architecture

To make the PV installation profitable, the MIC should have high efficiency, low cost and the capability of voltage step-up and step-down. Several references are focused on the efficiency converters improvement, to fulfil these desired requirements. One of the strategies explored to improve the efficiency of the converter is not to process the full amount of power delivered to the load. This kind of topologies are known as Partial-Power Conversion (PPC), Series Connection, Parallel-Power-Processed (PPP) or Direct Energy Transfer (DET) converters [15] - [23]. In all of them, the efficiency improvement is achieved due to the converter only manages a part of the energy, whereas the rest of the output power is directly delivered to the load. The best efficiency achieved in these converters is up to $98 \%$ in [16]. The main constraint of this kind of topologies is that it can only be used to voltage step-up, reducing the string-configuration
possibilities in the PV installation. Beyond the topologies, that does not process the full power, other authors have also obtained efficiencies around $98 \%$ with full power processing topologies, but these topologies are not capable of both voltage step-down and step-up [24] - [26].

The MIC cost is a variable difficult to estimate because it depends on the manufacturing volumes, and hardly ever is analyzed in the literature. As a rough parameter, the number of components employed in the converters could be used to estimate the cost of the converter, although not all the components cost the same. In any case, this parameter is going to be used in this paper.
Although any DC-DC converter can be employed in PV installations, several authors have demonstrated that the highest flexibility regarding the number of PV panels per string is only achieved with voltage stepup and step-down converters [27] - [30]. Within the voltage step-up and step-down topologies, one of the most promising ones is the classical Non-Inverting Buck-Boost converter [27] and [31]. Although very high efficiencies have been obtained in [27], some drawbacks of this topology are the high current through the inductor and switches, and the needed of four switches and drivers. Therefore, the complexity and the components count increases.
On the other hand, although the achieved efficiency is not as high as the one obtained in [27], in [32] is introduced a topology that fulfils all the desired MIC requirements for being applied to grid-tied PV installations with DMPPT architectures, the Buck-Boost Modified Forward Series (BBMSF) converter.
The topology analysed in this paper is the Autotransformer Forward-Flyback (AFF) converter. This topology can be considered as an evolution of the BBMSF converter, and therefore, it can be considered as a good MIC candidate to be applied in DMPPT architectures. Some advantages of the AFF converter are the voltage step-up and step-down capability, its high efficiency and its simplicity due to it only has one switch, so it only requires one driver. Also, thanks to the autotransformer connection, only a part of the output power is magnetically processed, reducing the autotransformer power losses and reactive energy of the converter.
The paper is organized as follows: in Section 2, a complete analysis of the AFF converter is carried out, including the time domain analysis as well as the frequency domain analysis in continuous conduction mode. In Section 3, the experimental results, obtained with a 225 W AFF prototype, verify the theoretical analysis. The conclusions of the paper are detailed in Section 4.

## 2. Theoretical analysis of the AFF converter

An in-depth analysis of the Autotransformer Forward-Flyback (AFF) converter, which has already been introduced in [33], is carried out in the present paper. The AFF topology is an evolution of the Buck-Boost Modified Series Forward (BBMSF) converter [32]. In Figure 3 it is highlighted the main difference between both topologies which is related to the autotransformer reset.


Figure 3. Comparison between the BBMSF converter topology (a)) and the AFF converter topology (b))

In the BBMSF converter, the autotransformer delivers its previously stored magnetising energy into the input capacitor, however, in the AFF converter, it is delivered to an auxiliary capacitor, $\mathrm{C}_{\text {aux }}$. This different autotransformer reset network connection has important consequences in the converter behaviour and performances. Indeed, due to this connection, the AFF topology can be considered as a combination between the Forward converter and the Flyback converter, see Figure 4.


Figure 4. AFF converter as a Forward and a Flyback converter combination
Figure 4 shows how the Forward-net output and the Flyback-net output delivers energy to the load. This fact can also be appreciated in the output-input voltage transfer function obtained in Section 2.2. Besides, thanks to the voltage fixed into the $\mathrm{C}_{\text {aux }}$ capacitor, the $\mathrm{D}_{2}$ diode blocks a low voltage. Therefore, a highperformance diode is selected, improving the converter efficiency, as shown in Section 3.1.2.

### 2.1 PRINCIPLE OF OPERATION

The AFF converter can be operated in several modes, depending on the conduction mode of each one of their inductors, $L$ and $L_{m}$. Theoretically, the converter offers four possibilities, as summarised in Table I.

Table I. AFF converter operational modes

| Operational Mode | $L$ conduction mode | $L_{m}$ conduction mode |
| :---: | :---: | :---: |
| OM1 | COM | COM |
| OM2 | COM | DCM |
| OM3 | DCM | CWM |
| OM4 | DCM | DCM |

In the operational modes with inductors working in DCM, OM2 to OM4, the RMS currents through the magnetic devices are higher than in CCM, for the same output power. Higher RMS currents tend to imply higher DC losses and higher size magnetic devices. Therefore, all the analyses carried out in this paper refers to the OM1, where both magnetic inductance $L$ and $L_{m}$ work in CCM.
Regarding the principle of operation, two main intervals can be defined depending on the MOSFET state: $t_{0 N}$, while the S MOSFET is switched on; and $t_{\text {OFF }}$, while it is switched off.
Figure 5 to Figure 6 depict the current paths followed by the current in each interval.


Figure 5. AFF current paths during the $t_{\text {ON }}$ interval


Figure 6. AFF current paths during the toff interval

As it can be seen, the current paths are highlighted in blue colour, whereas the rest of the circuit is depicted in grey colour. The direction of the current is denoted with arrows. For the sake of simplicity, the model described in this analysis is ideal, without taking into account the parasitic inductances, capacitances and resistances that are in real converters.

- $t_{\mathrm{ON}}$

As it has been mentioned before, the first interval corresponds to the time while the S MOSFET is switched on. During this interval, both inductances, $L$ and $L_{m}$, are storing energy.
The converter delivers the power from the input to the output filter through the S MOSFET, the autotransformer and the $D_{1}$ diode, see Figure 5. Thanks to the autotransformer connection, only a part of the output power is magnetically processed, increasing the converter's efficiency.

- $t_{\text {OFF }}$

Once the MOSFET is switched off, the reset of both the output inductance $L$ and the magnetising inductance $L_{m}$ begins. As it can be seen in Figure 6, the previously stored energy in $L_{m}$ is delivered to the $C_{\text {aux }}$ capacitor and the output filter, through the diodes $D_{d}$ and $D_{2}$. The $L$ current also flows through the $D_{d}$ and $D_{2}$. Analyzing this operation could seem that both "current sources" are connected in series, but the $\mathrm{C}_{\text {aux }}$ capacitor decouples one from the other. A detail of the currents distribution at this junction point is shown in Figure 7.


Figure 7. Current distribution detail in the Dd, D2 and Caux junction point during the $t_{\text {OFF }}$ interval of the AFF converter. a) Equivalent current sources model b) Electrical scheme; c) Current waveforms

In Figure 7a), the suffix "_d" denotes that the variables are referred to the tertiary winding ( $\mathrm{n}_{\mathrm{d}}$ ), meaning:

$$
\begin{gather*}
Z_{L m_{\_} d}=Z_{L m} \cdot n_{d}^{2}  \tag{1}\\
i_{L m_{\_} d}=\frac{i_{L m}}{n_{d}} \tag{2}
\end{gather*}
$$

It is noteworthy that, during this switching interval, Figure 7c), the average value of the output inductor current is the same as the magnetising inductance current referred to the tertiary winding of the autotransformer, see (3). The difference between both currents is compensated by the $\mathrm{C}_{\text {aux }}$ capacitor.

$$
\begin{equation*}
I_{L m}=I_{L} \cdot n_{d} \tag{3}
\end{equation*}
$$

This interval ends when the S MOSFET switches on again, starting a new cycle.
In Table II are summarised the main events of each switching interval.

Table II. Summary of the principle of operation events for the AFF converter

| Switching interval | Start event | Main considerations | Final event |
| :---: | :---: | :---: | :---: |
| $\mathrm{t}_{\mathrm{ON}}$ | $S$ is turned on | L and $\mathrm{L}_{\mathrm{m}} \rightarrow$ store energy <br> Part of the output power $\rightarrow$ magnetically processed <br> $\mathrm{D}_{1} \rightarrow$ positive biased | $S$ is turned off |
| $\mathrm{t}_{\text {OFF }}$ | $S$ is turned off | $L$ and $L_{m} \rightarrow$ deliver energy <br> Caux $\rightarrow$ decouples $\mathrm{i}_{\mathrm{L}}$ and $\mathrm{i}_{\mathrm{Lm}}$ <br> $D_{2}$ and $D_{d} \rightarrow$ positive biased | $S$ is turned on |

### 2.2 State-stage and time domain analysis in continuous conduction mode

The expression that defines a DC-DC converter used as a voltage source is the output-input voltage transfer function. A voltage-per-second balance in the output filter inductor $L$ is carried out to obtain this expression. In (4), the AFF converter output-input voltage transfer function in OM1, see Table I, is calculated.

$$
\begin{equation*}
\frac{V_{o}}{V_{i}}=\left(1+n+n_{d}\right) \cdot D \tag{4}
\end{equation*}
$$

As it can be seen, the output-input voltage transfer function includes a contribution of both $n$ and $n_{d}$ variables, Forward-net and Flyback-net, see Figure 4.
The AFF converter presents a duty cycle limitation, see (5). The restriction comes from the fact that the Flyback-net output voltage must be lower than the Forward-net one. Otherwise, the $D_{1}$ diode is never directly biased.

$$
\begin{equation*}
d \leq \frac{1+n}{1+n+n_{d}} \tag{5}
\end{equation*}
$$

Next, the current and voltage stresses are analyzed for each one of the AFF converter components. The variables denoted with capital letters indicates average or steady-state values, whereas the variables denoted with lower case letters indicate time dependence.

- Output filter inductance (L)


Figure 8. Output inductor current and voltage waveforms, $\mathrm{i}_{\mathrm{L}}$ and $\mathrm{v}_{\mathrm{L}}$ respectively, during a switching period.

$$
\begin{gather*}
\Delta I_{L}=\frac{V_{i} \cdot D \cdot\left[(1+n) \cdot(1-D)-n_{d} \cdot D\right]}{L \cdot f_{s w}}  \tag{6}\\
I_{L}=I_{\text {string }}=\frac{P}{V_{i} \cdot\left(1+n+n_{d}\right) \cdot D}  \tag{7}\\
v_{L_{-} O N}=v_{i} \cdot\left[(1+n)-d \cdot\left(1+n+n_{d}\right)\right]  \tag{8}\\
v_{L_{-} O F F}=-v_{i} \cdot\left[(1+n)-d \cdot\left(1+n+n_{d}\right)\right] \cdot \frac{d}{1-d} \tag{9}
\end{gather*}
$$

- Autotransformer

The design of the autotransformer is crucial. As it can be seen in (4), the output voltage is highly dependent on the autotransformer turn ratios $n$ and $n_{d}$. Rearranging the equation (5) obtains the maximum tertiary turn ratio $n_{d}$ for a desired maximum duty cycle and a fixed primary turn ratio $n(10)$.

$$
\begin{equation*}
n_{d} \leq \frac{(1+n) \cdot(1-d)}{d} \tag{10}
\end{equation*}
$$

Several currents can be used to define the autotransformer behaviour. However, only the magnetising voltage and current are obtained in this section. The rest of the autotransformer currents can be obtained from other components: the primary current is the same as the S MOSFET current, the secondary current is the same as the $D_{1}$ diode current, and the tertiary current corresponds with the $D_{d}$ diode.


Figure 9. Magnetizing inductor current and voltage waveforms, $i_{\text {Lm }}$ and $\mathrm{v}_{\mathrm{Lm}}$ respectively, during a switching period.

- MOSFET (S)


$$
\begin{equation*}
i_{S_{-} O N}=i_{L} \cdot(1+n)+i_{L m} \tag{15}
\end{equation*}
$$

$$
\begin{equation*}
I_{S}=I_{L} \cdot\left(1+n+n_{d}\right) \cdot D \tag{16}
\end{equation*}
$$

$$
\begin{equation*}
v_{S_{-} O F F}=v_{i} \cdot \frac{1}{1-d} \tag{17}
\end{equation*}
$$

Figure 10. MOSFET current and voltage waveforms, $\mathrm{i}_{\mathrm{DS}}$ and $\mathrm{v}_{\mathrm{DS}}$ respectively, during a switching period.

- $\mathrm{D}_{1}$ diode


$$
\begin{gather*}
i_{D 1 \_0 N}=i_{L}  \tag{18}\\
I_{D 1}=I_{L} \cdot D  \tag{19}\\
v_{D 1 \_O F F}=v_{i} \cdot \frac{\left(1+n+n_{d}\right) \cdot d}{1-d} \tag{20}
\end{gather*}
$$

Figure 11. $\mathrm{D}_{1}$ diode current and voltage waveforms, $\mathrm{i}_{\mathrm{D} 1}$ and $\mathrm{v}_{\mathrm{D} 1}$ respectively, during a switching period.

- $D_{2}$ diode


$$
\begin{equation*}
i_{D 2_{-} O F F}=i_{L} \tag{21}
\end{equation*}
$$

$$
\begin{equation*}
v_{D Z_{-} O N}=v_{i} \cdot \frac{(1+n)-d \cdot\left(1+n+n_{d}\right)}{1-d} \tag{23}
\end{equation*}
$$

Figure 12. $\mathrm{D}_{2}$ diode current and voltage waveforms, $\mathrm{i}_{\mathrm{D} 2}$ and $\mathrm{v}_{\mathrm{D} 2}$ respectively, during a switching period.

- $D_{d}$ diode


$$
\begin{equation*}
i_{D d_{-} O F F}=\frac{i_{L m}}{n_{d}} \tag{24}
\end{equation*}
$$

Figure 13. $\mathrm{D}_{\mathrm{d}}$ diode current and voltage waveforms, $\mathrm{i}_{\mathrm{Dd}}$ and $\mathrm{v}_{\mathrm{Dd}}$ respectively, during a switching period.

## A. Power transfer analysis

The connection of the autotransformer is one of the critical points of the AFF converter. Thanks to this connection, only a part of the delivered power is magnetically processed by the autotransformer. The size of the autotransformer and its power losses are therefore reduced.
In this section, the theoretical expression that defines the power percentage managed by the autotransformer in OM1 is calculated.
Using the equation (4) in the output power expression, (27) is obtained.

$$
\begin{equation*}
P_{o}=V_{o} \cdot I_{o}=\left(1+n+n_{d}\right) \cdot D \cdot V_{i} \cdot I_{o}=D \cdot V_{i} \cdot I_{o}+\left(n+n_{d}\right) \cdot D \cdot V_{i} \cdot I_{o}=P_{\text {not_mag }}+P_{\text {mag }} \tag{27}
\end{equation*}
$$

From the equation (27), the relation between the magnetically processed and not magnetically processed power transference, $P_{\text {mag }}$ and $P_{\text {not_mag }}$ respectively, is calculated:

$$
\begin{equation*}
\frac{P_{\text {mag }}}{P_{\text {not_mag }}}=n+n_{d} \tag{28}
\end{equation*}
$$

The percentages of both $P_{\text {not_mag }}$ and $P_{\text {mag }}$ with respect the output power are described in equations (29) and (30) respectively.

$$
\begin{equation*}
P_{\text {not_mag }}=\frac{1}{1+n+n_{d}} \cdot P_{o} \tag{29}
\end{equation*}
$$

$$
\begin{equation*}
P_{\operatorname{mag}}=\frac{n+n_{d}}{1+n+n_{d}} \cdot P_{o} \tag{30}
\end{equation*}
$$

In Table III, several cases regarding turns ratio parameter are selected to illustrate the equations (29) and (30).

Table III. Magnetically and not magnetically processed power percentage

| $\mathbf{n}+\mathbf{n}_{\boldsymbol{d}}$ | 0.1 | 0.5 | 1 | 1.5 | 2 |
| :---: | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{P}_{\text {not_mag }}(\%)$ | 0.909 | 0.667 | 0.500 | 0.400 | 0.333 |
| $\mathbf{P}_{\text {mag }}(\%)$ | 0.091 | 0.333 | 0.500 | 0.600 | 0.667 |

As it can be seen, the lower the turns ratios $n$ and $n_{d}$, the lower $P_{m a g}$ percentage. Consequently, for a higher efficiency, low turns ratios values are desired. On the other hand, low turn ratios limit the voltage step-up, see (4).
Section 3.1.2 describes the process to select the best turn ratios values for a particular case of study.

### 2.3 Small-signal model. Frequency domain analysis

Classic model techniques based on averaging, linearization and perturbation have been employed to obtain the small signal model of the AFF converter in OM1 [34], see Figure 14.


Figure 14. Small signal model of the AFF converter

In Figure 14 the capital letters refer to DC values for a specific operational point, whereas the disturbed variables are denoted with the superscript " $\wedge$ ".
The injected current method is employed to obtain the small signal transfer functions [34]. In this method, the main small signal transfer functions can be obtained through the current injected into the load. Figure 15 depicts the block diagram that describes the method above.


Figure 15. A small signal block diagram

Therefore, to obtain the small signal transfer functions, the expression that relates the injected current $i_{L}$ in terms of the duty cycle, the input voltage and the output voltage is needed, see (31).

$$
\begin{equation*}
\hat{\imath}_{L}(s)=A(s) \cdot \hat{d}-B(s) \cdot \hat{v}_{o}+C(s) \cdot \hat{v}_{i} \tag{31}
\end{equation*}
$$

Solving the circuit of Figure 14, the terms of the current through the output inductor $i_{L}$, the $A(s), B(s)$ and C(s) terms can be obtained. The specific values for the AFF converter are summarized in Table IV.

Table IV. Expressions of the AFF converter small signal blocks

| Small signal block | Expression |
| :---: | :---: |
| A(s) | $(1+n) \cdot V_{i}-V_{\text {Caux }}+\frac{(1-D)^{2} \cdot N(s) \cdot\left(V_{i}+\frac{V_{\text {Caux }}}{n_{d}}\right)}{n_{d} \cdot Z_{L m}(s)}$ |
|  | $Z_{L}(s)+(1-D)^{2} \cdot N(s)$ |
| $B(s)$ | $\frac{1}{Z_{L}(s)+(1-D)^{2} \cdot N(s)}$ |
| $C(s)$ | $\frac{(1+n) \cdot D+\frac{D \cdot(1-D)^{2} \cdot N(s)}{n_{d} \cdot Z_{L m}(s)}}{Z_{L}(s)+(1-D)^{2} \cdot N(s)}$ |
| $N(s)$ | $\frac{n_{d}^{2} \cdot Z_{L m}(s) \cdot Z_{\text {Caux }}(s)}{n_{d}^{2} \cdot Z_{L m}(s)+Z_{\text {Caux }}(s) \cdot(1-D)^{2}}$ |
| $Z_{\text {caux }}(s)$ | $\frac{1}{s \cdot C_{a u x}}$ |
| $Z_{L}(s)$ | $s \cdot L$ |
| $Z_{L m}(s)$ | $s \cdot L_{m}$ |
| $Z_{p}(s)$ | $\frac{R_{L}}{1+s \cdot C_{o} \cdot R_{L}}$ |

The most common expressions used for defining the dynamic performances of a converter are the output voltage-duty cycle gain $G_{v d}(s)$, the output-input voltage gain (audiosusceptibility) $G_{v v}(s)$ and the output impedance $Z_{o}(s)$. These expressions can be calculated for the AFF converter, replacing in (32) - (34) the $A(s), B(s), C(s)$ and $Z p(s)$ expressions, detailed in Table IV.

$$
\begin{align*}
& G_{v d}(s)=\frac{\hat{v}_{o}}{\hat{d}}=\frac{A(s) \cdot Z_{p}(s)}{1+B(s) \cdot Z_{p}(s)}  \tag{32}\\
& G_{v v}(s)=\frac{\hat{v}_{o}}{\hat{v}_{i}}=\frac{C(s) \cdot Z_{p}(s)}{1+B(s) \cdot Z_{p}(s)}  \tag{33}\\
& Z_{o}(s)=\frac{\hat{v}_{o}}{\hat{\imath}_{o}}=\frac{Z_{p}(s)}{1+B(s) \cdot Z_{p}(s)} \tag{34}
\end{align*}
$$

A four-order polynomic is obtained by expanding the denominator of the expressions (32) - (34). This means that there are four poles in the small signal transfer functions. The four poles are indeed two double poles. The frequency of these pole-pairs is described in (35) and (36):

$$
\begin{equation*}
f_{\text {pole }_{-} F l}=\frac{1}{2 \cdot \pi \cdot \sqrt{L_{m_{-} e q} \cdot C_{a u x}}} \tag{35}
\end{equation*}
$$

$$
\begin{equation*}
f_{\text {pole- } F w}=\frac{1}{2 \cdot \pi \cdot \sqrt{L \cdot C_{o}}} \tag{36}
\end{equation*}
$$

where $L_{m_{-} e q}=\frac{L_{m} \cdot n_{d}^{2}}{(1-D)^{2}}$.

As it is denoted in the suffix of the frequency variables (35) and (36), the lowest frequency is directly dependent on the Flyback-net of the AFF converter, whereas the highest frequency depends on the Forward-net of the AFF converter, see Figure 4. For avoiding the overlapping of the poles-frequencies effects, it is recommended (37):

$$
\begin{equation*}
f_{\text {pole_Fl }}<f_{\text {zeroes }}<f_{\text {pole_Fb }} \tag{37}
\end{equation*}
$$

An overlap between the poles-frequencies, without the zeroes correction, yields in a phase shift of -180 degrees, reducing the chances of obtaining high bandwidth.
Regarding the zeroes of the (32) - (34) small signal transfer functions, the output voltage-duty cycle and the audio-susceptibility have double zeroes whereas the output impedance denominator has a zero in the origin and double zeroes.
Some simulations are carried out in the next section to validate the theoretical analysis.

### 2.3.1 Simulation validation

Each one of the small signal transfer function expressions, obtained in the previous section in (32) - (34), is depicted in Mathcad ${ }^{\oplus}$ and compared with the simulation results obtained with PSIM ${ }^{\oplus}$. The specific values employed for this comparison are summarized in Table V .

Table V. Parameters of the AFF converter for a non-shaded PV panel in Scenario 1

| Parameter | Definition | Value |
| :---: | :--- | :---: |
| $\mathrm{f}_{\mathrm{sw}}$ | Switching frequency | 50 kHz |
| $\mathrm{V}_{\mathrm{i}}$ | Input voltage | 29.3 V |
| D | Duty cycle | 0.689 |
| n | Autotransformer secondary turns ratio | 0.5 |
| $\mathrm{n}_{\mathrm{d}}$ | Autotransformer tertiary turns ratio | 0.5 |
| L | Output filter inductance | $33 \mu \mathrm{H}$ |
| $L_{m}$ | Magnetizing inductance | $185 \mu \mathrm{H}$ |
| $\mathrm{C}_{0}$ | Output filter capacitance | $112 \mu \mathrm{~F}$ |
| $\mathrm{C}_{\mathrm{aux}}$ | Auxiliary capacitance | $100 \mu \mathrm{~F}$ |
| $\mathrm{R}_{\mathrm{L}}$ | Output load | $7.255 \Omega$ |

All the values shown in Table V corresponds to the ones selected in the prototyping step, for a non-shaded PV panel in Scenario 1. The case of study and converter specifications are defined in the converters design Section 3.1.


Figure 16. AFF converter output voltage-duty cycle small signal
transfer function, $\operatorname{Gvd}(\mathrm{s})$


Figure 18. AFF converter output impedance, $\mathrm{Zo}(\mathrm{s})$


Figure 17. AFF converter audio-susceptibility, Gvv(s)

Figure 16 to Figure 18 depict the small signal transfer functions corresponding to expressions (32) - (34) respectively. The theoretical representation is depicted in red colour, whereas the simulated one is depicted in blue colour. By comparing both, the theoretical and simulated graphs, it can be noted that the theoretical results fit the simulated ones up to around 20 kHz , which is almost half of the employed switching frequency. From this frequency on, the simulation results are no longer representative.
As expected, two double poles can be appreciated in the three small signal representations. The frequencies of these poles are the same in all of them. The double zeroes can also be appreciated in both, the gains and phases in Figure 16 - Figure 18. The effect of the zero in origin can be seen in the output impedance small signal transfer function.

Depending on the relation between the poles frequencies and the double zero frequency, the phase step could reach 360 degrees. This fact should be considered when designing the converter regulator.

## 3. Experimental verification

### 3.1 CONVERTER DESIGN

### 3.1.1 The case of study/application environment

A prototype must be designed and tested to verify the previous theoretical analysis. Depending on the application, some decisions should be taken to select the proper components. The field of application, in this case, is a 100 kW grid-tied photovoltaic installation with DMPPT architecture, see Figure 2. In this kind of installations, the central inverter operating voltage is critical, due to it fixes the string voltage. The FREESUN LVT FSO100 inverter is selected for this case of study [35]. This inverter has a 600 V input voltage. Once the central inverter is selected, several PV panels can be chosen. Depending on the type of PV panel, different maximum power point, open circuit and short circuit characteristics must be taken into account. The 225 W SKJ60P6L PV panel, from Siliken, is the one included in this study [36].
The desired 100 kW of the PV installation requires 450 PV panels of 225 W each. The voltage step-up and step-down capability of the AFF converter allows multiple combinations of the number of strings - the number of PV panels per string. In this case, the selected DMPPT configuration is formed by 25 strings with 18 PV panels in series per string.
For taking into account the effect of mismatching, two different scenarios have been defined, depending on the percentage of shaded PV panels. In the Scenario E0, there are no shaded PV panels; whereas a $25 \%$ percentage of the PV panels are affected by shadows in the Scenario E1. As it is described in [2], a shadow in a PV panel can drastically reduce both, the PV panel voltage and the generated power. The power and voltage characteristics of a shaded PV panel, considering the worst-case scenario, are half of the nominal output voltage and a third of the output power [2]. For the sake of simplicity, it is considered that all the PV panels are exactly equaled. Two different voltage and power characteristics are therefore defined, one for the non-shaded PV panels (29.3 V and 225 W ) and the other one for the shaded ones ( 15 V and 67.5 W).

In a DMPPT architecture, the expression (38) is fulfilled by all the MIC connected to the same string.

$$
\begin{equation*}
i_{\text {string }}=\frac{p_{\text {string }}}{v_{\text {string }}} \tag{38}
\end{equation*}
$$

Being $p_{\text {string }}$ and $v_{\text {string }}$ the power generated in the string and the voltage of the string respectively. As aforementioned, the central inverter fixes the string voltage. Considering the ideal case, where the efficiency of the MIC is $100 \%$, the power generated by the PV panel is the same as the power delivered from the converter to the string; i.e. $P_{\text {in }}=P_{\text {out }}$. Therefore, assuming this statement, the output voltage of each converter can be obtained through the whole power generated in the string and the power delivered by the PV panel to the string, see (39).


Figure 19. Detail of the connection between the PV panel and the MIC

$$
\begin{equation*}
V_{o}=\frac{V_{P V} \cdot I_{P V}}{I_{o}}=\frac{V_{P V} \cdot I_{P V}}{p_{\text {string }}} \cdot v_{\text {string }}=\frac{p_{P V}}{p_{\text {string }}} \cdot v_{\text {string }} \tag{39}
\end{equation*}
$$

For Scenario E1, applying the power reduction in the shaded PV panels, the delivered power per string, $p_{\text {string }}$, can be obtained. Finally, with (39), the output voltage of the converters under both scenarios are obtained.

The case-of-study specifications are summarised in Table VI.

Table VI. Case of study parameters summary

| Converter | Parameter | Scenario E0 | Scenario E1 |
| :---: | :---: | :---: | :---: |
|  | Power (W) | 225 | 225 |
| Non-shaded PV panel | $V_{i}(\mathrm{~V})$ | 29.3 | 29.3 |
|  | $V_{o}(\mathrm{~V})$ | 33.3 | 40.404 |
|  | $I_{\text {string }}(\mathrm{A})$ | 6.75 | 5.569 |
|  | Power $(\mathrm{W})$ | $\mathrm{N} / \mathrm{A}$ | 67.5 |
|  | $V_{i}(\mathrm{~V})$ | $\mathrm{N} / \mathrm{A}$ | 15 |
| Shaded PV panel | $V_{o}(\mathrm{~V})$ | $\mathrm{N} / \mathrm{A}$ | 12.121 |
|  | $I_{\text {string }}(\mathrm{A})$ | $\mathrm{N} / \mathrm{A}$ | 5.569 |

It is noteworthy that, in strings with shaded PV panels, the converters attached to the non-shaded PV panels have to step-up their output voltages whereas the ones attached to the shaded PV panels have to step-down its output voltage. This performance can only be achieved with a voltage step-up and stepdown converter.

### 3.1.2 Design procedure: selection of the AFF converter components

In this section, a step-by-step design procedure is applied to the aforementioned case of study.

- Step 1: Stablish the highest voltage step-up for the application of interest. The AFF converter does not present any voltage step-down limitation.
- Step 2: The AFF converter with both the output inductor and the autotransformer operating on CCM (OM1) should fulfil the conditions (4) and (5). In both expressions, there are three independent variables: $n, n_{d}$ and $d$. For solving the system equation, one more condition is added (40)

$$
\begin{equation*}
n=n_{d} \tag{40}
\end{equation*}
$$

The condition (40) is established to make easier the Autotransformer design and to reduce the leakage inductance.

- Step 3: With the three expressions (4), (5) and (40), there is a minimum $n$ and $n_{d}$ value per maximum duty cycle and voltage step-up ratio. The solutions of the system of equations are depicted in Figure 20.


Figure 20. Possible turns ratios values for the AFF converter autotransformer, for different output voltages and maximum duty cycles.
Although the maximum output voltage of the application is $V_{0}=40.404 \mathrm{~V}$, several curves are depicted in order to obtain a maximum duty cycle range for each turns ratio value. Four turns ratios values are highlighted.
As it can be seen, higher turns ratio values yield in lower maximum duty cycle. Therefore, to improve the duty cycle range, low turns ratio values are desired. On the other hand, low turns ratio values increase the voltage stresses that the MOSFET, the $D_{1}$ diode and the $D_{2}$ diode withstand. As a tradeoff, $n=n_{d}=0.5$ is selected as the optimum turns ratio values for the case of study described in Section 3.1.1.

Once these three steps are carried out, the specifications for the AFF converter are obtained, see Table VII.

Table VII. Specifications for the converter design

| Parameter | Specification | Parameter | Specification |
| :---: | :---: | :---: | :---: |
| $V_{i}(V)$ | $[15-29.3]$ | $D_{\max }$ | 0.75 |
| $V_{0}(V)$ | $[12-40.404] \pm 10 \%$ | $P_{\text {omax }}(W)$ | 225 |
| $D_{\text {min }}$ | 0 | $P_{\text {omin }}(W)$ | 60 |

- Step 4: Obtain the electrical stresses in each element of the AFF converter. Section 2.2 details the voltage and current expressions for each component, considering a switching frequency $f_{s}=$ 50 kHz . The maximum values are used for selecting the appropriate devices for the AFF converter prototype. In Table VIII are summarized the main parameters of the selected components.

Table VIII. Maximum electrical stresses in the AFF components.

| Component | Voltages (V) | Currents (A) | Other characteristics | Selected <br> Part-reference |
| :---: | :---: | :---: | :---: | :---: |
| C | $V_{C i}{ }^{(*)}=35.16$ | $I_{\text {ci_rms }}=6.87$ | $C_{i_{\text {I min }}}=178.8 \mu \mathrm{~F}$ | C_50SVPF68M (x4) |
| C | $V_{C o}{ }^{(*)}=48.48$ | $I_{\text {co_rms }}=1.06$ | $C_{o-\min }=26.2 \mu \mathrm{~F}$ | C_EEHZA1J560P <br> (x2) |
| $\mathrm{C}_{\text {aux }}$ | $V_{\text {Caux }}{ }^{(*)}=38.95$ | $\begin{aligned} & I_{\text {Caux_rms }} \\ & =0.93 \end{aligned}$ | $C_{o_{-} \text {min }}=18 \mu \mathrm{~F}$ | C_EEHZA1H101P |
| S | $V_{\text {S_OFF }}=94.36$ | $\begin{gathered} I_{S_{-p e a k}}=17.15 \\ I_{S_{\text {_rms }}}=10.31 \end{gathered}$ | $\begin{gathered} R_{D S \text { _on }}=9.5 \mathrm{~m} \Omega \\ Q_{g}=45 \mathrm{nC} \\ \hline \end{gathered}$ | FDMS86255ET150 |
| $\mathrm{D}_{1}$ | $V_{D 1}=129.82$ | $\begin{gathered} I_{D 1}=3.84 \\ I_{D 1 \text { peak }}=8.58 \end{gathered}$ | $V_{f} \approx 1.2 \mathrm{~V}$ | C3D08065E |
| $\mathrm{D}_{2}$ | $V_{D 2}=24.62$ | $\begin{gathered} I_{D 2}=2.91 \\ I_{D 2 \text { _peak }}=8.58 \end{gathered}$ | $V_{f} \approx 0.09 \mathrm{~V}$ | SPV1002T40 |
| $\mathrm{D}_{\mathrm{d}}$ | $V_{\text {Dd_oN }}=47.18$ | $\begin{gathered} I_{D d}=2.91 \\ I_{D d \_ \text {peak }}=8.55 \end{gathered}$ | $V_{f} \approx 0.33 \mathrm{~V}$ | V40D100C-M3/I |
| L | $\begin{gathered} V_{L_{L O N}}=10.62 \\ V_{L_{-} O F F}=14.01 \end{gathered}$ | $\begin{aligned} \Delta I_{L} & =3.66 \\ I_{L} & =6.75 \\ I_{\text {Lrms }} & =6.832 \end{aligned}$ | $\begin{aligned} L & =33 \mu \mathrm{H} \\ D C R & =13.2 \mathrm{~m} \Omega \end{aligned}$ | 74435583300 |
| Autotransformer $\left(L_{m}\right)$ | $\begin{gathered} V_{\text {Lm_oN }}=29.3 \\ V_{\text {Lm_orF } 1} \\ =65.06 \end{gathered}$ | $\begin{gathered} I_{L m}=2.184 \\ I_{\text {Lm_peak }} \\ =3.375 \\ I_{\text {Lm_rms }} \\ =3.415 \\ \hline \end{gathered}$ | $\begin{gathered} n=0.5 \\ n_{d}=0.5 \\ L_{m}=185 \mu \mathrm{H} \\ L_{\text {leakage }}=190 \mathrm{nH} \end{gathered}$ | Non-standard part <br> RM12-3C90 core. |

${ }^{(*)}$ A $20 \%$ margin is considered in the input and output voltages, see Table VII.

As it can be seen in the characteristics of the selected AFF converter components, the $D_{2}$ diode presents a very low forward voltage drop $V_{f}$. This property is desired for reducing the power losses. The selection of this device is possible thanks to low voltage that withstand, due to the $\mathrm{C}_{\text {aux }}$ placement.

Besides the components summarised in Table VIII, three snubber nets, a driver and a current sensor have been designed and implemented in the AFF prototype, see Figure 21.


Figure 21. AFF prototype. a) TOP view; b) BOTTOM view

Typical R-C dissipative snubber net is added in parallel to the $D_{2}$ and $D_{d}$ diodes. For reducing the voltage spike on the MOSFET, a backward-regenerative and a dissipative snubber nets are used. Both typical electrical schemes are shown in Figure 22.


Figure 22. Snubber nets electrical schemes. a) MOSFET snubber nets; b) $\mathrm{D}_{1}$ diode snubber net

The design of the snubber networks is based in [37]. The components that form the backward-regenerative type snubber are the $D_{S 1}, D_{S 2}$ and $C_{S_{\_} b-r}$, whereas the dissipative snubber type components are denoted with the suffix $d$. The selected capacitors and resistors employed as snubber nets are summarized in Table IX.

Table IX. Parameters of the snubber nets added to the AFF prototype

| Component | Value | Component | Value |
| :---: | :---: | :---: | :---: |
| $\mathrm{R}_{\text {S_d }}$ | $22 \Omega$ | $\mathrm{R}_{\mathrm{D} 2 \text { _d }}$ | $100 \Omega$ |
| $\mathrm{C}_{\text {S_d }}$ | 2.2nF | $\mathrm{C}_{\text {D2_d }}$ | 680pF |
| $\mathrm{C}_{\text {S_b-r }}$ | 1 nF | $\mathrm{R}_{\text {Dd_d }}$ | $22 \Omega$ |
|  |  | $\mathrm{C}_{\text {Dd_d }}$ | 680pF |

Due to the MOSFET position, an isolated driver is required. For this purpose, a pulse transformer is used. The scheme of the driver is detailed in Figure 23.

a)

b)

Figure 23. Driver electrical scheme in a); Driver picture of the prototype in b)

The current sensor is based in a current-sensing transformer, see Figure 24.


Figure 24. Current sensor electrical scheme in a); current sensor picture of the prototype in b)

Where the turn ratio of the current-sensing transformer is $n=100$ and the sensing resistance value is $R_{\text {sens }}=50 \Omega$. Due to these two parameters, the current through the transformer primary side is, in amperes, twice the volts sensed between the sensing resistance terminals (41).

$$
\begin{equation*}
i_{p r i}=2 \cdot v_{s e n s} \tag{41}
\end{equation*}
$$

### 3.2 Time domain measurements

In this section, the most relevant time domain waveforms of the Autotransformer Forward-Flyback converter are shown. The test conditions are the same as described in the Scenario E0, see Table VI. The current waveforms are depicted in green colour whereas the voltage ones are depicted in yellow colour.
Figure 25 shows the S MOSFET current and voltage waveforms.


Figure 25. MOSFET waveforms. $\mathrm{V}_{\mathrm{DS}}$ in yellow colour and $\mathrm{I}_{\mathrm{S}}$ in green colour. a) complete switching period; b) turn-on detail; c) turn-off detail

In Figure 25a) can be seen that the steady state values are the expected ones for the MOSFET waveforms, see Figure 10. Regarding the transitions, it is noteworthy that the MOSFET presents Quasi-ZVS during the turn-on transition, due to the amount of current rising during the voltage falling edge is around a $40 \%$ of the maximum rising current. In the turn-off transition, it presents hard-switching.
In Figure 26, the $D_{1}$ diode waveforms are depicted.

a)

b)

c)

Figure 26. $\mathrm{D}_{1}$ diode waveforms. $\mathrm{V}_{\mathrm{D} 1}$ in yellow colour and $\mathrm{I}_{\mathrm{D} 1}$ in green colour. a) complete switching period; b) turn-on detail; c) turn-off detail

During the $t_{\text {OFF }}$ interval, the $D_{1}$ diode receives a similar voltage and current waveforms compare to MOSFET, as can be appreciated in Figure 25a) and Figure 26a).
In Figure 26b) can be seen that $D_{1}$ diode has Quasi-ZVS when turn-on. In this case, the maximum current value achieved during the voltage falling edge is around $10 \%$ of the maximum rising current. On the other hand, during the turn-off, see Figure 26c), the AFF converter has Zero Current Switching (ZCS). Therefore, very low switching losses are expected in the $D_{1}$ diode. For the $D_{1}$ diode, the time base is zoomed from 40 ns to 20 ns to better shown the ZCS transition.

The $D_{2}$ diode waveforms are depicted in Figure 27.

a)

b)

c)

Figure 27. $\mathrm{D}_{2}$ diode waveforms. $\mathrm{V}_{\mathrm{D} 2}$ in yellow colour and $\mathrm{I}_{\mathrm{D} 2}$ in green colour. a) complete switching period; b) turn-on detail; c) turn-off detail

Low $D_{2}$ switching losses are expected thanks to the ZCS at the turn-off transition, see Figure 27 c ). Also, thanks to the very low forward voltage drop in this diode, low DC losses are also expected. In the turn-on transition, it presents hard-switching, Figure 27b).

The last oscilloscope measurements refer to the $D_{d}$ diode, see Figure 28.


Figure 28. $\mathrm{D}_{\mathrm{d}}$ diode waveforms. $\mathrm{V}_{\mathrm{Dd}}$ in yellow colour and $\mathrm{I}_{\mathrm{Dd}}$ in green colour. a) complete switching period; b) turn-on detail; c) turn-off detail

Due to the Flyback-net of the AFF converter, the autotransformer reset is similar to the Flyback converter one. It means that the magnetising current flows through the $D_{d}, D_{2}$ diodes as well as through the output filter. A ZCS and a Quasi-ZVS performance are also present in this diode during the turn-on and turn-off intervals respectively. Therefore, low switching losses are expected in the $D_{d}$ diode.
Comparing the current and voltage waveforms shown in Figure 26 - Figure 28, with the theoretical ones, see Figure 10 - Figure 13 respectively, the steady-state theoretical analysis is verified, as well as the proper operation of the AFF converter.

### 3.2.1 Efficiency analysis

The efficiency is measured using the Yokogawa WT3000. The efficiency graphs shown in Figure 29 are obtained for the corresponding input and output voltages detailed in Table VI.


Figure 29. AFF efficiency measurements. A) Efficiencies for the shaded PV panel converter; b) Efficiencies for the non-shaded PV panel converter The measurement shown in Figure 29.a) emulates the performance of the AFF converter while attached to a shaded PV panel. Therefore, the input and output voltages are fixed to 15 V and 12.12 V respectively. The performance while attached to a non-shaded PV panel is shown in Figure 29.b). The voltage ranges employed in Scenario E0 and E1 are detailed in Table VI.
As it can be seen in Figure 29, the higher the output voltage, the higher the efficiency of the AFF converter. Also, the higher the output power, the lower the efficiency. Both conclusions are related to the conduction losses, which are more relevant than the switching losses. The AFF converter efficiency, when it is connected to a PV panel in shaded conditions, Figure 29.a), is the lowest. The maximum measured efficiency is $94.5 \%$, and it is quite constant from half load to full load, varying around $1 \%$.
The Buck-Boost converter, the Cúk converter with a coupled inductor and the Non-Inverting Buck-Boost converter have been considered as the main MIC competitors, due to all of them are non-isolated voltage step-up and step-down converters, commonly applied to photovoltaic systems. Table $X$ includes a comparison between them and the AFF converter.

Table X. Comparison between the AFF converter with the Buck-Boost converter, the Cúk converter with a coupled inductor and the Non-Inverting Buck-Boost converter

| Parameters | AFF | Buck-Boost <br> $[30]$ | Cúk with coupled <br> inductor [30] | Non-Inverting <br> Buck-Boost [27] |
| :--- | :---: | :---: | :---: | :---: |
| Magnetic components | 2 | 1 | 1 | 1 |
| Active switches | 1 | 1 | 1 | 4 |
| Drivers | 1 | 1 | 1 | 4 |
| Passive switches | 3 | 1 | 1 | 0 |
| Dynamic performances | No-RHP zero | RHP zero | RHP zero | RHP zero |
| Efficiency (\%) | 94.5 | 87.2 | 93.1 | 98.5 |

As it can be deduced from the comparison shown in Table $X$, the efficiency of the AFF converter is comparable with the efficiencies obtained with other topologies for this application [30]. Although the Cúk converter's component count is lower than for the AFF converter, their diode, main capacitor and active
switch withstand high electrical stresses. Moreover, its dynamic response is slower due to the RHP zero in the small signal transfer functions. Recent works have reported higher efficiencies with the Non-Inverting Buck-Boost converter, see [14] and [27], but including four controlled switches and drivers. In comparison to them, the AFF semiconductor count is limited to three diodes and one power MOSFET, and therefore only a driver, resulting in potential cost reductions. This fact simplifies the converter and improves the reliability of the overall system. Besides, the size of the output filter capacitors in the AFF converter is lower due to its output filter inductor. It is notable that all the competitors suffer from RHP zero in their small signal transfer functions, limiting their dynamic performance.

## 4. Conclusions

The theoretical analysis of the Autotransformer Forward-Flyback (AFF) converter is carried out in this paper, including the steady-state and time domain analysis as well as the small-signal analysis with both the output inductor and the autotransformer operating in continuous conduction mode.
Regarding the steady-state analysis, the main points analysed in the paper are the principle of operation of the AFF converter, the voltage and current expressions of each component and the output-input voltage transfer function.

The frequency domain analysis includes the obtaining of the main small signal transfer functions, meaning the output voltage - duty cycle $\left(G_{v d}(s)\right)$, the audiosusceptibility $\left(G_{v v}(s)\right)$ and the output impedance $\left(Z_{o}(s)\right)$ small signal transfer functions. The analytical results are validated through simulation. Two poles-pairs appear in all the transfer functions, corresponding each poles-pair to the Forward-net and Flyback-net of the AFF converter.
A step-by-step procedure describes how to design the AFF converter for any field of application. A case of study with two different shading conditions is described and used for the design of the 225 W prototype. The measured results in a 225 W prototype verify the theoretical analysis. It has been highlighted that some MOSFET and diodes switching present ZCS and, in particular, the $D_{1}$ diode, which has high influence in the converter efficiency, present both ZCS and quasi-ZVS. The effect of some parasitic inductances, not considered in the theoretical analysis, are shown and explained with the measured waveforms.
The efficiency of the AFF converter is described through a set of measurements for the input-and-output voltage conditions of each Scenario. The highest measured efficiency is $94.5 \%$.

Summarizing, the main advantages of the AFF converter are its step-up and step-down voltage transfer function; the ZCS and quasi-ZVS characteristics in the diodes, yielding in efficiencies up to $94.5 \%$; the use of an autotransformer, with better performances than a typical Forward transformer; and the use of a single controlled switch. This last advantage can result in a potential reduction of cost and increase of reliability. On the other hand, the main drawbacks of the introduced converter are the high voltage stresses in the $D_{1}$ diode and MOSFET. Hence, those devices able to withstand higher voltages but with worse performances are selected. Also, snubber networks must be added to mitigate these voltage spikes due to leakage inductance, yielding in an efficiency reduction. Although it is not a requirement for the field of application, the output of the converter is not isolated from the input, due to the use of an autotransformer. Finally, the AFF converter does not present RHP zero in their small signal transfer functions, and therefore a good dynamic performance is achieved.

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