# Extending the FIP bias sample to magnetically active stars Challenging the FIP bias paradigm?

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#### ABSTRACT

*Context.* The different elemental abundances of the photosphere and the corona are striking features of not only the Sun, but other stars as well. This phenomenon is known as the FIP effect (FIP stands for first ionization potential), and its strength can be characterized by the FIP bias, the logarithmic abundance difference between low- and high-FIP elements in the corona, compared to the photosphere. The FIP bias was shown to depend on the surface temperature of the star.

Aims. We aim to extend the  $T_{\text{eff}}$  –FIP bias relationship to a larger stellar sample and analyse the effect of other astrophysical parameters on the relation (e.g., surface gravity, age, activity indicators).

*Methods.* We compiled FIP bias and other parameters for 59 stars for which coronal composition is available, now including evolved stars. Using principal component analysis and linear discriminant analysis, we searched for correlations with other astrophysical parameters within the sample which may influence the stellar FIP bias.

*Results.* Adding stars to the  $T_{\text{eff}}$ -FIP bias diagram unveiled new features in its structure. In addition to the previously known relationship, there appears to be a second branch, a parallel sequence about 0.5 dex above it. While the  $T_{\text{eff}}$  remains the main determinant of the FIP bias, other parameters such as stellar activity indicators also have influence. We find three clusters in the FIP bias determinant parameter space. One distinct group is formed by the evolved stars. Two groups contain main sequence stars in continuation separated roughly by the sign change of the FIP-bias value.

Conclusions. The new branch of the  $T_{\rm eff}$ -FIP bias diagram contains stars with higher activity level, in terms of X-ray flux and rotational velocity. The Rossby number also seems to be important, indicating possible dependence on the type of dynamo operating in these stars influencing their FIP bias. The two main sequence clusters run from the earliest spectral types of A-F with shallow convection zones through G-K-early M stars with gradually deeper convection zones, and end up with the fully convective M dwarf stars, depicting the change of the dynamo type with the internal differences of the main sequence stars in connection with the FIP-bias values.

**Key words.** stars: abundances – stars: activity – stars: atmospheres

### 1. Introduction

Differences in chemical composition between various regions of the solar corona and the photosphere were documented first by Pottasch (1963), who found significantly higher abundances for Si, Mg and Fe in the corona compared with the photospheric abundances. These elements all exhibit first ionization potentials (FIP) lower than 10 eV, and hence called low-FIP elements, while elements with FIP values higher than 10 eV (e.g., O, Ne, He) are called high-FIP elements. It has now become a wellknown phenomenon that low-FIP element abundances are enhanced in the corona with respect to their photospheric values, while high-FIP elements show significantly lower enhancement, or even depletion (see, e.g. Meyer 1985; Feldman & Laming 2000; Feldman & Widing 2003).

After high-energy space-borne observatories became available in the 1990s with the launch of the *Extreme Ultraviolet Ex*- *plorer* (*EUVE*), similar abundance anomalies were discovered for several late-type stars (Laming et al. 1996; Drake et al. 1997; Laming & Drake 1999), and since then, the *XMM-Newton* and the *Chandra* X-ray observatories have further increased the sample of stars with known FIP effect (e.g. Wood & Linsky 2010; Wood & Laming 2013; Wood et al. 2018, etc.).

Recently, Wood et al. (2018) have pointed out that stars with effective temperatures similar to or higher than that of the Sun show similar abundance enhancements, while cooler stars tend to exhibit lower abundance enhancements. At  $T_{\rm eff} \approx 4500$  K, coronal abundances become equal to the photospheric values, and furthermore, even cooler stars seem to exhibit an inverse FIP effect (IFIP) where low-FIP elements are depleted rather than enhanced in the corona compared to the photosphere. Doschek et al. (2015) and Doschek & Warren (2016) have also found signs of the IFIP effect on the Sun in flares, in small patches

near sunspots, while Katsuda et al. (2020) observed IFIP effect in spatially unresolved segments of solar flare plasma.

The (I)FIP effect has been modeled by Laming (2004, 2009, 2012, 2015b, 2017), and lately, by Laming et al. (2019), and it is explained with the effect of the ponderomotive force associated with Alfvén and fast mode waves, which separates ions from neutrals in the chromospheric regions. Most recently, it has been suggested that resonant Alfvén waves propagating along coronal loops can result in FIP effect (Laming 2015b, 2021), while originally upward propagating p-modes or magneto-acoustic waves, which are converted to fast modes and propagate into the  $\beta < 1$  regions can be a plausible explanation for the IFIP effect (Laming 2021; Baker et al. 2019, 2020). The competition between these two effects might be a deciding factor whether a star exhibits an overall FIP or IFIP effect.

To characterize the strength of the (I)FIP effect, the quantity known as the FIP bias is used, which is the mean coronal abundance of four high-FIP elements (C, N, O, Ne) relative to the Fe abundance (the most easily observable low-FIP element), normalized to the photospheric abundance ratios. The abundance ratios (and hence the FIP-bias values) are given in logarithmic units. In the case of solar-like FIP effect, the FIP bias is negative, while it is positive in the case of inverse-FIP effect. To measure the FIP bias, both the coronal abundances from X-ray spectra, and photospheric abundances from optical spectra are needed. While it is hard to acquire high quality X-ray observations even for nearby stars, there is no straightforward way to measure photospheric abundances of certain elements at all (mainly N and Ne). Thus, it is common to use solar photospheric composition or empirical formulae instead.

On the original  $T_{\rm eff}$ -FIP bias diagram of main sequence stars from Laming (2015a), updated from Wood & Linsky (2010), the stars form a tight sequence with  $T_{\rm eff}$ , but lack diversity in other parameters. In this work we extend the diagram in two aspects: with a larger and more diverse stellar sample, and by involving other parameters, e.g., surface gravity, metallicity, age. We compile the parameters from existing literature, prioritizing homogeneity for stellar parameters, and transparency for the calculation of the FIP bias.

The structure of the paper is as follows: in Sect. 2 we describe the sample and the parameters of interest, in Sect. 3 we describe the methods used to search for correlations within the dataset. In Sect. 4 we present the results, while their implications are discussed in Sect. 5.

### 2. Data

In order to extend the  $T_{\rm eff}$ -FIP bias diagram, we collected all active stars regardless of spectral type and evolutionary stage for which coronal abundance values are available in the literature, thus where it is possible to calculate the FIP bias. In our final sample we selected a total of 59 stars, summarized in Table 1. From the 59 stars, only 18 (31%) are single. 41 are members of binaries or multiple systems, although 25 of them are effectively single, i.e. gravitationally bound wide binaries or long period binaries which were formed together but do not interact, and the components evolve separately. Quite a few binaries are members of hierarchical multiple systems but no interaction between the system members is observed.

The group of solar type stars with 15 members contains six single stars, two close and seven wide binaries. Among the nine flare stars there are two close binaries: YY Gem (M1Ve+M1Ve) and AT Mic (M4Ve+M4Ve) with two equal components, both stars of the binaries are active, the observed signals from the

components are of common origin. We have altogether 13 K dwarfs, three of those are well-known fast rotating, very active and flaring stars. Most of the remaining ten K dwarfs are members of wide binaries as in the case of the solar-type group. The vast majority of the wide binaries are from these groups, as part of the observing strategy (*Chandra* can observe the two components in the same frame, see e.g. Wood & Linsky 2006) beside the importance of having solar-like parameters and activity.

The sample of the evolved stars mostly consists of RS CVn type binaries. These are well-known magnetically active stars, and are bright enough for coronal observations. Most of these 11 binaries are single-lined spectroscopic binaries (SB1), thus most of the observed features can be attributed to the subgiant or giant primary component. Double-lined binaries (SB2) are usually dominated by the primary as well, although the contribution of the secondary is not negligible. Spectral types of the binaries of evolved stars are from Eker et al. (2008).

The sample consists of dwarf stars from the main sequence (MS) and evolved stars from the red giant branch (RGB) of the Hertzsprung-Russell diagram. The MS stars of the sample start with the fully convective M dwarfs through K and G dwarfs to A-F stars, and in this sequence the depths of convective zones are continuously shrinking. Some stars are in an intermediate state: slightly before the MS or just turning off it. The stars on the subgiant and giant branches are inflated. These stars have thick convective envelopes and low surface gravities. All of the sample stars have magnetic activity in common, which is the basis of the observed element fractionation, and through this, the FIP effect. The magnetic fields of the stars are thought to be generated by different types of dynamos. Sun-like stars with  $M \leq M_{\odot}$  and usually showing (quasi-)cyclic magnetic variability, are believed to maintain solar-type  $\alpha \Omega$  dynamos, where differential rotation and large-scale convective flows play a crucial role. However, with vanishing differential rotation, e.g., in less massive stars with a fully convective interior,  $\alpha^2$  dynamos are supposed to operate, driven rather by small-scale turbulent flows. The rotational rates of the stars are from about 0.5 days to over 200 days which have strong impact on the magnetic dynamo. Our sample is heterogeneous, and the task is to investigate how the FIP effect appears on stars of different masses and evolutionary status with different rotational velocities.

For the 59 stars with known coronal composition, we compiled the following parameters from the literature, where available:

- $T_{\rm eff}$ : effective temperature, mostly derived from optical spectra
- log g: surface gravity from optical spectra, in a few cases when no literature data existed it is calculated from mass and radius
- [Fe/H]: metallicity
- log  $R'_{\rm HK}$ : chromospheric contribution of the Ca H&K lines (excluding the photospheric component). It measures the chromospheric activity, but since it varies strongly with activity level (activity cycle, e.g., for the Sun it varies between -4.88 and -5.02, more active stars could exhibit bigger change), rotational modulation of the activity features, and the incidental flares at the time of the observations. Thus it is only a rough index for the strength of activity in a given star (see Ramírez et al. 2014, and their references). This parameter is missing for many objects, particularly for the evolved stars. Only 3 out of the 17 evolved stars have measured log  $R'_{\rm HK}$ .
- R: stellar radius

-  $\log L_X$ : X-ray luminosity

- $\log F_X$ : X-ray flux calculated from  $\log L_X$  and radius
- *t*: age
- $Ro = P_{rot}/\tau_c$ : Rossby number, the ratio of rotational period and the convective turnover time. The latter is not an observable parameter. It was calculated using the empirical relation from Noyes et al. (1984), with B - V values from the Simbad database. In the case of evolved stars, we used a different formula from Gondoin (2007) to calculate *Ro* directly from log  $F_X$  and log g, without the use of  $\tau_c$ . We note that while this empirical formula has a large scatter, *Ro* is itself strongly model dependent through  $\tau_c$ .
- $P_{\text{rot}}$ : photometric rotational period from the rotational modulation of the light curve. It is only used to calculate  $v_{\text{rot}}$  and *Ro*.
- $v_{\rm rot}$ : rotational velocity at the surface, simply  $v_{\rm rot} = 2\pi R/P_{\rm rot}$
- literature FIP bias: FIP-bias values compiled from various sources, and transformed to the same solar photospheric standard from Asplund et al. (2009), and Ne abundance from Drake & Testa (2005) ( $[Ne/O]=log_{10} 0.41$ ). Thus we adopt the following abundance values with the normalization of A(H)=12: A(C)=8.43, A(N)=7.83, A(O)=8.69, A(Ne)=8.30. Where no photospheric abundance was available, solar composition was assumed. The FIP-bias values were corrected by +0.084 according to Wood et al. (2018) to deal with atomic data changes. The individual abundances used for the calculation are listed in Table A.1.
- KNN FIP bias: the same as the previous parameter, but recalculated with homogeneously predicted photospheric abundances with k-nearest neighbour (KNN) algorithm from LAMOST data (Wang et al. 2020), and with the +0.084 correction from Wood et al. (2018) to deal with atomic data changes. See Sect. 3.1 for details and Table A.2 for the individual abundances.
- SME FIP bias: FIP bias calculated using photospheric composition determined by spectral synthesis with the *Spectroscopy Made Easy* code (SME, Piskunov & Valenti 2017), to check the consistency of the previous methods. Only available for a handful of stars, and only from C and O abundances. See Sect. 3.2 for details and Table B.1 for the abundances.

These parameters are summarized in Table 2, with their sources listed in Appendix C. The uncertainty of the FIP bias is taken as the standard deviation of [C/Fe], [N/Fe], [O/Fe] and [Ne/Fe]. We chose this method over propagating the individual error bars of the abundances, as those are not available in some cases, and they are not homogeneous.

We note that in the case of GJ 338 AB the individual coronal abundance fractions are not available from emission measure analysis. Wood et al. (2012) estimated the FIP bias directly from Fexvii/Oviii. Thus we cannot use the same methods to reproduce the results for this binary, and adopt the FIP-bias value from Wood et al. (2018).

#### 3. Methods

#### 3.1. Photospheric abundances from LAMOST

Most of the time when the stellar FIP bias was calculated, there were no stellar photospheric abundances available, so the coronal abundances had to be compared to the solar photosphere. However, different stars can have significantly different chemical composition, which may affect the derived FIP-bias values. To take this into account, individual photospheric abundances are needed. Ideally, one would need a homogeneous survey of high resolution optical/near-infrared spectra with high signal-tonoise ratio, and observable transitions for each of the required elements. Given the absence of such data, to have an independent set of stellar photospheric abundances, as homogeneous as possible, we used the results of Wang et al. (2020), where a large set of abundances were predicted from medium resolution LAM-OST spectra. They used deep learning with a training set compiled from APOGEE results for the common stars in the LAM-OST and APOGEE sample. Instead of using individually measured equivalent widths, the full spectra were used in the prediction. Since the lines of some elements are weak or missing in the optical, the method inherently involves hidden correlations between abundances. Their cited precision is 0.06–0.12 dex for 11 elements, also including C, N and O.

Since the LAMOST survey only extends to the northern hemisphere, roughly half of our sample is not covered by it. To circumvent this problem, we used a k-nearest neighbours regressor (KNN, KNeighborsRegressor from sklearn.neighbors<sup>1</sup>) to predict the abundances of interest from  $T_{\text{eff}}$ , log g and [Fe/H]. This essentially means finding the nearest few stars in this three-dimensional parameter space, and getting their mean abundances as the result. For the prediction, we used k=6 neighbours. The root-mean-square error of the method is 0.05 dex, using 10% of the whole LAMOST sample as test set. The method gives the following abundances for the Sun:  $[C/Fe] = -0.09 \pm 0.03$ ,  $[N/Fe] = 0.06 \pm 0.08$  and  $[O/Fe] = 0.10 \pm 0.03$ . A lower dimensional cut of this parameter space can be seen in Fig. 1. The tempting aspects of this method are the following: it is really accessible (only needs the three most fundamental parameters), it gives even N and O abundances, and since it practically involves interpolation, it cannot give too extreme results (which is a problem with spectral synthesis and NLTE correction, giving occasionally clearly unrealistic O abundances). But since the predictions are quite indirect, we only treat the results as a little better first approximation, after the initial zeroth approximation of solar composition.

#### 3.2. Photospheric abundances from spectral synthesis

To derive homogeneous photospheric abundances for as many stars as possible from the sample, we used spectra from CFHT-ESpaDoNS (Donati 2003) and TBL-NARVAL (Aurière 2003). The high spectral resolution enables the use of spectral synthesis, where the whole line profiles are fitted with model spectra calculated from a model atmosphere with varying physical parameters. The results are used to validate the process described in the previous section.

After acquiring the optical echelle spectra, we begin with a 99% percentile smoothing to locate the continuum, and renormalize it where necessary. We used SME (Piskunov & Valenti 2017) for the spectral synthesis. During the synthesis, MARCS models were used (Gustafsson et al. 2008) with atomic parameters from VALD (Kupka et al. 1999) using a transition list typical for the approximate effective temperature of the star in question. Macroturbulence was computed with the following equation from Valenti & Fischer (2005):

$$v_{\rm mac} = \left(3.98 - \frac{T_{\rm eff} - 5770\,\rm K}{650\,\rm K}\right) \rm km\,s^{-1} \tag{1}$$

Astrophysical parameters were determined by the following procedure:

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<sup>&</sup>lt;sup>1</sup> https://scikit-learn.org

Table 1. The representation of different types of stars in our sample. The numbers of single stars are given in parentheses.

flare stars, M	-type: 9 (3)	solar type:	15 (6)
ADLeo	single M4V	Sun	single G2V
CN Leo	single M6V	$\alpha$ Cen A	wide triple G2V
EQ Peg A	wide binary M3.5V	$\alpha$ Cen B	wide triple K0V
EQ Peg B	wide binary M4.5V	$\pi^1$ UMa	single + debris disk G1.5V
Proxima Cen	wide triple M5.5V	EK Dra	long period binary (45 yr) G5V
EV Lac	single M3.5V	ξBoo A	wide binary G8V
YY Gem	ecl. binary Castor sys. M1Ve+M1Ve SB2	$\chi^1$ Ori	wide binary GOV
AU Mic	triple with AT Mic M0.5V	кCet	single G5V
AT Mic	spectroscopic binary M4Ve+M4Ve SB2	βCom	single GOV
		47 Cas B	wide binary G0-2V
fast rotating l	K dwarfs, flares: 3 (2)	ιHor	single + planet F8V
ABDor	quadruple K0V	11 LMi	long period binary (201 yr) G8V
LO Peg	single K3V	HR 7291	single + planet F8.5V
V471 Tau	binary (triple?) K2V	$\sigma^2 CrB$	spec. binary in a quintuple system F9V+G0V SB2
	• • • •	ξUMa B	spec. binary in a quintuple system G5V SB1
K(-M) dwarfs: 10 (1)		_	
GJ 338 A	wide binary M0V	evolved sta	nrs: 17 (4)
GJ 338 B	wide binary M0V	HR 1099	RS CVn binary K1IV+G5IV SB2
36 Oph A	wide binary K1V	UX Ari	RS CVn binary K0IV+G5V SB2
36 Oph B	wide binary K1V	$\lambda$ And	RS CVn binary G8III-IV SB1
<i>ξ</i> Boo B	wide binary K4V	VY Ari	RS CVn binary K3-4V-IV SB1
61 Cyg A	wide binary K5V	Capella	spec. binary in a quintuple system KOIII
61 Cyg B	wide binary K7V	$\sigma$ Gem	RS CVn binary K1III SB1
70 Oph A	wide binary K0V	31 Com	single GOIII
70 Oph B	wide binary K5V	$\mu$ Vel	long period binary (138 yr) G6III
$\epsilon$ Eri	single with planet K2V	$\beta$ Cet	single G9II-III
		FK Com	single G2III
A-F stars, hot	ter than 6300K: 5 (3)	YY Men	single K1III
$\eta$ Lep	single F2V	EI Eri	RS CVn binary G5IV+G0V SB1
$\pi^3$ Ori	single A3V	V851 Cen	RS CVn binary K3V-IV SB1
$\tau \operatorname{Boo} A$	wide binary	AR Psc	RS CVn binary K1IV-V+G5-6V SB2
Procyon	long period binary (40.8 yr) F5IV-V	AY Cet	RS CVn binary WD+G5III SB1
Altair	single, A type (A7V)	II Peg	RS CVn binary K2IV+M0-3V SB1
		ARIAC	RS CVn binary G2IV+K0IV SB2

- 1. Fitting *v* sin *i* and microturbulence using rough astrophysical parameters and assuming solar abundances.
- 2. Fitting  $T_{\text{eff}}$ .
- 3. Fitting metallicity and microturbulence (microturbulence values can be unreliable sometimes, and can alter the other astrophysical parameters slightly, thus we fit it simultaneously with another parameter).
- 4. Fitting  $\log g$  for the Na doublet and the Mg triplet, or in some cases, for a special line list only containing transitions with  $\log gf > 0$  (stronger lines tend to be more sensitive to changes in  $\log g$ ).
- 5. Refitting  $T_{\rm eff}$  and metallicity.
- 6. Fitting individual abundances (C, O, Ca, Mg, Si, Ti, Fe, Ni).

From the last step, only C, O and Fe are of interest, the others were only added to help with line blends. Determining the Fe abundance is mostly straightforward, thanks to the multitude of Fe lines visible in practically any stellar spectra. The carbon abundance was fitted using several atomic and molecular lines, but most of them are really weak and blended. The oxygen abundance was fitted using only the O triplet at 7774 Å, since the 6300 Å line was not visible in any of the spectra. This is a highly NLTE-sensitive triplet, so we used an NLTE correction from Kovalev et al. (2018) with parameters from Sitnova et al. (2013) that resulted in slightly different values. This correction uses  $T_{\text{eff}}$ , log *g*, [Fe/H] and microturbulence, and outputs separate correction factors for each line in the O triplet, which we averaged. As

there are no N lines in the optical, the N abundance was estimated through proxies (i.e., we assumed the same relative N/O abundance as in the Sun). For Ne we used the empirical relation from Drake & Testa (2005) ([Ne/O]= $\log_{10} 0.41$ ). We note however, that the abundance of 3 out of 4 high-FIP elements depend on the NLTE-sensitive O triplet. Thus we argue that in the case of the high-FIP elements, the photospheric abundances calculated with spectral synthesis are not much more reliable than the values from broader abundance trends or empirical correlations. The results of the spectral synthesis are listed in Table B.1.

#### 3.3. Principal component analysis

In the space of physical parameters of the stars in the sample ( $T_{\text{eff}}$ , log g, [Fe/H], age, radius R,  $v_{\text{rot}}$ , Rossby number Ro, log  $R'_{\text{HK}}$ , log  $L_X$ , log  $F_X$ , literature and KNN FIP bias) there are several clear and not so clear correlations. To find these, we used principal component analysis (PCA, Pearson 1901), with the PCA implementation of sklearn.decomposition. PCA is an algorithm that eliminates linear correlations by selecting directions in the parameter space with the highest variance, and defining new orthonormal basis vectors in those directions, thus creating a basis where a large portion of the variance can be described by only a few components. It is a powerful technique for dimensionality reduction and data compression, and it is often the first step when dealing with clustering problems (for a similar treatment, see e.g. Csörnyei et al. 2021). We use PCA to identify hidden

Table 2. Compiled astrophysical parameters for the sample. See Sect. 2 for the description of each parameter, and Appendix C for the sources.

Stor	FID bios	FID bins	$T_{m}(a)$	log g	[Ee/H]	(b)	P	D	11	P <sub>o</sub>	$\log R'$	log Lu	$\log E_{\rm H}$
Star	literatura		I eff	logg	[1.6/11]	Cum		I rot	Vrot	NO	IOg N <sub>HK</sub>	(c)	(d)
ADI			<b>N</b>	(cgs)	0.00	Gyr	<u>κ</u> <sub>0</sub>	uays	KIII S	0.00	4.10	00.70	()
AD Leo	$0.49 \pm 0.11$	$0.74 \pm 0.10$	$3390 \pm 19$	4.81	0.28	0.16	0.42	2.24	9.53	0.09	-4.19	28.70	0.00
CN Leo	$0.27 \pm 0.17$	$0.46 \pm 0.32$	$3100 \pm 100$	5.21	0.18	0.23	0.14	2./1	2.52	0.08	-	27.01	5.96
EQ Peg A	$0.53 \pm 0.07$	$0.65 \pm 0.25$	$3353 \pm 60$	4.91	0.03	0.10	0.35	1.06	16./1	0.04	-5.16	28.71	6.84
EQ Peg B	$0.49 \pm 0.08$	$0.61 \pm 0.22$	$3152 \pm 2$	4.92	0.03	0.10	0.25	0.40	31.62	0.01		27.89	6.31
Prox Cen	$0.55 \pm 0.30$	$0.67 \pm 0.31$	$2879 \pm 50$	5.23	0.10	5.03	0.13	89.80	0.07	3.00	-5.00	27.22	6.20
EV Lac	$0.55 \pm 0.15$	$0.65 \pm 0.24$	$3291 \pm 51$	5.11	-0.19	0.16	0.34	4.38	3.98	0.16	-3.97	28.99	7.13
YY Gem	$0.69 \pm 0.17$	$0.80 \pm 0.23$	$3775 \pm 110$	4.63	0.00	0.37	0.62	0.81	38.47	0.03	-	29.27	6.90
AU Mic	$0.68 \pm 0.13$	$0.93 \pm 0.09$	$3679 \pm 6$	5.00	0.15	0.02	0.69	4.86	7.18	0.18	-3.99	29.36	6.90
AT Mic	$0.51 \pm 0.07$	$0.70 \pm 0.23$	$3123 \pm 12$	4.67	0.15	0.02	0.60	1.00	30.36	0.04	-	29.47	7.67
AB Dor	$0.60 \pm 0.09$	$0.49 \pm 0.20$	$5081 \pm 50$	4.55	0.18	0.15	0.96	0.51	94.35	0.02	-3.88	30.06	7.31
LO Peg	$0.59 \pm 0.07$	$0.46 \pm 0.31$	$4739 \pm 138$	4.36	0.00	0.15	0.66	0.42	78.79	0.02	-3.91	29.70	7.28
V471 Tau	$0.39 \pm 0.10$	$0.53 \pm 0.17$	$4980 \pm 10$	4.50	0.12	0.75	0.91	0.52	88.33	0.02	-	30.00	7.34
GJ 338 A	$0.39 \pm 0.25$	$0.39 \pm 0.25$	$4024 \pm 51$	4.68	-0.05	0.14	0.58	16.30	1.79	-	-4.65	27.92	5.61
GJ 338 B	$0.39 \pm 0.25$	$0.39 \pm 0.25$	$4005 \pm 51$	4.68	-0.03	0.14	0.58	16.61	1.78	_	-4.42	27.92	5.60
36 Oph A	$-0.14 \pm 0.09$	$-0.18 \pm 0.18$	$5103 \pm 29$	4.64	-0.29	1.39	0.69	20.69	1.69	0.99	-4.57	28.02	5.56
36 Oph B	$-0.27 \pm 0.10$	$-0.28 \pm 0.17$	$5199 \pm 63$	4.62	-0.30	1.44	0.59	21.11	1.41	1.01	-4.56	27.89	5.56
ξ Boo B	$-0.16 \pm 0.15$	$0.16 \pm 0.10$	$4359 \pm 38$	4.69	-0.08	0.27	0.61	11.94	2.58	0.49	-4.42	28.08	5.72
61 Cvg A	$-0.01 \pm 0.04$	$0.08 \pm 0.12$	$4374 \pm 22$	4.63	-0.20	2.12	0.67	35.37	0.96	1.45	-4.76	27.03	4.59
61 Cyg B	$0.33 \pm 0.08$	$0.54 \pm 0.12$	$4044 \pm 32$	4.67	-0.27	1.87	0.60	37.84	0.80	1.46	-4.89	26.97	4.63
70 Oph A	$-0.29 \pm 0.06$	$-0.28 \pm 0.11$	$5320 \pm 40$	4.52	-0.02	1.30	0.83	20.00	2.10	_	-4.55	28.09	5.47
70 Oph B	$0.15 \pm 0.10$	$0.31 \pm 0.04$	4400 + 100	4.47	-0.02	1.30	0.67			_	-3.61	27.97	5.53
e Eri	$0.06 \pm 0.07$	$-0.04 \pm 0.11$	$5050 \pm 100$	4.48	-0.11	0.44	0.74	11.68	3.21	0.54	-4 46	28.31	5.79
Sun	$-0.60 \pm 0.10$	$-0.37 \pm 0.10$	$5777 \pm 10$	4 44	0.00	4 57	1.00	26.09	1 94		-4 94	27 35	4 57
α Cen A	$-0.54 \pm 0.10$	$-0.47 \pm 0.10$	$5829 \pm 6$	4 35	0.23	5.03	1.00	28.80	2.16	1.88	-5.00	26.99	4.03
$\alpha$ Cen B	$-0.38 \pm 0.15$	$-0.33 \pm 0.17$	$5189 \pm 18$	4 30	0.23	5.03	0.87	38 70	1 14	1.00	_4 92	27 32	4.65
$\pi^1$ UMa	$0.30 \pm 0.13$	$0.33 \pm 0.11$	5050 + 70	4.50	0.12	0.10	0.07	4.60	0.82	0.46	4.22	28.00	6.20
π UMa EK Dro	$-0.43 \pm 0.18$	$-0.32 \pm 0.21$	$5930 \pm 70$ 5840 + 100	4.55	-0.12	0.19	0.91	4.09	9.62	0.40	4.56	20.99	7 24
ER Dia	$-0.00 \pm 0.13$	$-0.04 \pm 0.17$	$5550 \pm 100$	4.57	-0.01	0.15	0.95	6.21	6.00	0.24	-4.13	28.00	6.26
$\zeta BOOA$	$-0.29 \pm 0.04$	$-0.19 \pm 0.07$	$5550 \pm 100$	4.00	-0.19	0.19	0.80	5.26	0.90	0.59	-4.30	20.91	0.20
$\chi^{1}$ Ori	$-0.47 \pm 0.33$	$-0.39 \pm 0.31$	$6020 \pm 10$	4.45	-0.06	0.29	0.98	5.30	9.25	0.59	-4.43	28.99	6.22
к Cet	$-0.38 \pm 0.34$	$-0.28 \pm 0.32$	$5/40 \pm 20$	4.46	-0.02	0.52	0.92	9.24	5.04	0.70	-4.42	28.79	6.08
$\beta Com$	$-0.58 \pm 0.25$	$-0.52 \pm 0.23$	$6090 \pm 60$	4.41	-0.03	1.63	1.11	12.35	4.55	1.45	-4.75	28.21	5.33
47 Cas B	$0.19 \pm 0.36$	$0.14 \pm 0.33$	$5780 \pm 100$	4.50	-0.11	0.10	1.00	1.00	50.59	2.50		30.39	7.61
$\iota$ Hor	$0.21 \pm 0.25$	$0.15 \pm 0.19$	$6057 \pm 60$	4.37	0.15	0.75	1.17	8.50	6.96	1.14	-4.56	28.20	5.28
11 LMi	$-0.10 \pm 0.22$	$-0.12 \pm 0.32$	$5376 \pm 43$	4.48	0.33	2.39	1.00	17.88	2.83	0.98	-4.69	28.51	5.73
HR 7291	$-0.51 \pm 0.12$	$-0.53 \pm 0.08$	$6131 \pm 32$	4.34	0.14	2.56	1.19	7.60	7.92	1.34	-4.79	28.57	5.63
$\sigma^2 \mathrm{CrB}$	$0.06 \pm 0.04$	$0.01 \pm 0.03$	$5950 \pm 50$	4.12	-0.06	1.00	1.24	1.16	54.40	0.14	-3.83	30.68	7.80
ξ UMa	$0.35 \pm 0.06$	$0.39 \pm 0.33$	$5796 \pm 100$	4.43	-0.29	-	0.95	3.98	12.07	0.47	–	29.43	6.69
HR 1099	$0.76 \pm 0.12$	$0.76 \pm 0.05$	$4833 \pm 100$	2.84	-0.16	-	3.90	2.84	69.55	0.00	-3.84	31.28	7.31
UX Ari	$1.13 \pm 0.25$	$1.12 \pm 0.21$	$4560 \pm 100$	3.06	0.30	5.60	5.60	6.44	44.01	0.03	-	31.15	6.87
$\lambda$ And	$0.52 \pm 0.07$	$0.48 \pm 0.09$	$4630 \pm 100$	2.57	-0.56	5.62	6.41	53.95	6.01	0.07	-4.48	30.57	6.17
VY Ari	$0.74 \pm 0.09$	$0.75 \pm 0.09$	$4800 \pm 100$	3.10	-0.09	-	2.66	16.20	8.31	0.01	-	31.09	7.46
Capella	$-0.13 \pm 0.20$	$-0.11 \pm 0.18$	$4970 \pm 50$	2.69	-0.04	0.62	11.98	104.00	5.83	0.34	-	30.62	5.68
$\sigma$ Gem	$0.66 \pm 0.26$	$0.60 \pm 0.19$	$4630 \pm 100$	2.79	-0.10	5.00	10.10	19.60	26.07	0.03	_	31.48	6.69
31 Com	$0.07 \pm 0.19$	$0.05 \pm 0.15$	$5660 \pm 42$	3.51	-0.15	0.54	8.74	6.76	65.41	0.40	_	30.90	6.23
$\mu$ Vel	$-0.16 \pm 0.17$	$-0.15 \pm 0.18$	$5030 \pm 40$	2.73	_	0.36	13.00	_	-	0.61	_	30.51	5.50
$\beta$ Cet	$-0.08 \pm 0.14$	$-0.03 \pm 0.21$	$4720 \pm 100$	2.65	-0.15	0.46	16.78	215.00	3.95	1.19	-4.79	30.43	5.20
FK Com	$0.29 \pm 0.07$	$0.30 \pm 0.06$	$5000 \pm 100$	3.50	-0.89	_	6.99	2.40	147.35	0.17	_	31.00	6.53
YY Men	$0.49 \pm 0.31$	$0.47 \pm 0.25$	$4700 \pm 100$	2.40	-0.37	_	12.70	9.55	67.28	0.00	_	32.50	7.51
ELEri	$0.23 \pm 0.08$	$0.32 \pm 0.15$	$5500 \pm 100$	3.73	-0.03	6.15	2.37	1.95	61.58	0.01	_	31.13	7.60
V851 Cen	$0.67 \pm 0.00$	$0.74 \pm 0.12$	$4700 \pm 80$	3.00	-0.13		3 50	12 27	14 43	0.03	_	30.61	674
AR Psc	$0.68 \pm 0.19$	$0.83 \pm 0.27$	$4880 \pm 100$	2.89	-0.91	7.50	2.70	12.25	11 15	0.00	_	31 24	7 59
AY Cet	$0.53 \pm 0.19$	$0.05 \pm 0.27$ 0.59 ± 0.34	5044 + 17	3.05	-0.38	1 32	6.80	75.12	4 58	0.06		31.00	6.55
II Peg	$1.22 \pm 0.14$	$1.22 \pm 0.17$	$4600 \pm 100$	3 20	-0.40	1.52	3 40	672	25.61	0.03		30.78	6.03
$\Delta \mathbf{R} \mathbf{L} \alpha \alpha^{(e)}$	$0.40 \pm 0.17$	$0.40 \pm 0.25$	$1820 \pm 100$	3.69	_0.70	_	2.50	1.09	68.48	0.05	_	31.02	7 87
n Lan	$-0.31 \pm 0.00$	$-0.30 \pm 0.00$	$+620 \pm 100$ $6020 \pm 70$	1 10	-0.70	1 20	2.00	1.90	00.40	0.01	_2 04	28 50	5 22
-3 O	$-0.51 \pm 0.09$	$-0.30 \pm 0.09$	$6720 \pm 70$	4.19	-0.09	1.00	1.50	4 00	16 70	1.00	-3.94	20.00	5.55
$\pi^{-}$ Ori	$-0.41 \pm 0.07$	$-0.31 \pm 0.12$	$0430 \pm 40$	4.25	-0.04	1.55	1.32	4.00	10.70	1.82	-4.65	28.99	5.96
τ B00 A	$-0.21 \pm 0.09$	$-0.21 \pm 0.13$	$03/0 \pm 30$	4.14	0.16	2.30	1.4/	3.31	22.47	0.88	-4.73	28.76	5.64
Procyon	$0.29 \pm 0.17$	$0.25 \pm 0.15$	$6530 \pm 50$	3.96	-0.05	1.87	2.03	23.00	4.47	13.37	-4.63	28.39	4.99
Altair	$-0.56 \pm 0.42$	$-0.25 \pm 0.36$	$/655 \pm 150$	4.29	-0.20	1.20	1.84	0.37	252.28	7.00	-3.97	27.15	3.84

**Notes.** (*a*) Where no error for  $T_{\text{eff}}$  was given in the literature source, we assume ±100 K. (*b*) Estimated age in 10<sup>9</sup> yr. (*c*) Logarithmic values measured in erg s<sup>-1</sup>. (*d*) Logarithmic values measured in erg s<sup>-1</sup>. (*e*) The activity of AR Lac originates from both components, however, the K1V secondary is more luminous and its activity is higher according to Lanza et al. (1998), while the X-ray fluxes of the components and X-ray flares are discussed in Drake et al. (2014); we consider the secondary component as the source of the FIP effect.

correlations between parameters, and to find the parameters that are not really useful. Before running PCA on the full parameter set, we scaled the features to have zero mean and unit variance. In the case of missing parameters, we refilled them using the average value of the given parameter for the 2 nearest neighbours in the 12 dimensional parameter space. For parameters that change orders of magnitude (age, radius,  $v_{rot}$  and Rossby number) we used their base 10 logarithm.



**Fig. 1.** Abundance trends based on data from Wang et al. (2020) for the LAMOST sample, for the three relevant high-FIP elements (there are no available Ne abundances).

#### 3.4. Unsupervised clustering

To separate different groups of stars based on the available parameters, we used unsupervised k-means clustering (Macqueen 1967), with the KMeans implementation of sklearn.cluster. It identifies k different clusters, based on proximity in the parameter space, by minimizing the variance within each cluster. The resulting clusters are basically Voronoi cells around k number of centers (cluster means), where k is defined a priori. Since some of the parameters in the original 12 dimensional dataset are correlated, they do not form an orthogonal basis, which can bias the clustering. Therefore we run the clustering after dimensionality reduction with PCA, only keeping 4 PCs.

#### 3.5. Linear discriminant analysis

To find the main physical difference between the two emerging clusters on the  $T_{\rm eff}$ -FIP bias diagram, we carried out linear discriminant analysis (hereafter LDA, see Fisher 1936 for the original paper, McLachlan 2004 for a review of the method, or Rácz et al. 2018 for an application), using the LinearDiscriminantAnalysis implementation of sklearn.discriminant\_analysis. It finds a linear combination of input features that maximizes the separation between some pre-defined clusters, then uses linear decision boundaries for classification. Interpreting the model given by LDA is relatively straightforward, as it is a simple linear combination of the scaled input parameters. The LDA method assumes that the input features follow a multivariate normal distribution, and are independent with no correlations between them. We note that in our case, none of these assumptions hold strictly. From the 12 input parameters 9 are independent measurements, while log  $F_X$  follows from log  $L_X$  and radius,  $v_{rot}$  contains radius and rotational period, and the Rossby number for giants is derived from  $v_{rot}$  and log g for the evolved sample. Also, there are deviations from normality. For the cluster labels, we used a simple linear boundary on the  $T_{eff}$ -FIP bias diagram. Since the FIP bias was removed from the input features, LDA had to find a combination of the remaining ten parameters that separate the two clusters.

#### 4. Results

Our first step was to plot a new  $T_{\rm eff}$ -FIP bias diagram with all stars in the extended sample using the already published and homogenized FIP-bias values and their error bars (see Sect. 3) in Fig. 2. The figure shows the names of the stars for easier identification, black points mark the stars from the original FIP-bias diagram of Laming (2015a), updated from Wood & Linsky (2010). Our important result, that the relation has now nearly parallel branches separated by about 0.5 in FIP bias, is well seen and will be discussed later. The low mass M dwarf stars ( $T_{\rm eff} < 4000$  K) show a separate blob in the continuation of the original relation. A hint of a bimodal distribution of the FIP-bias values is found in Wood et al. (2018, see their Fig. 7a): all four stars lying above their diagram ( $\tau$  Boo A, EK Dra, AB Dor A and AU Mic) are included now in the parallel, second branch of the relation, see Fig. 2.

# 4.1. Comparison with FIP-bias values derived with different methods

All stars from the sample have both literature and KNN FIP-bias values. No systematic difference is found between them except for the M dwarfs below  $T_{\rm eff}$ ~4200 K, as those stars are at the edge of the LAMOST  $T_{\rm eff}$  – log g–[Fe/H] parameter grid, thus their predicted photospheric abundances are similar. There is generally a good agreement between the FIP-bias values calculated from the original photospheric composition and the newly derived one from spectral synthesis. Fig. 3 shows a comparison between the literature and KNN FIP-bias values. The homogeneously predicted photospheric abundances from LAMOST slightly decrease the scatter, the Spearman correlation coefficient changes from  $-0.67\pm0.07$  for the literature values to  $-0.74\pm0.05$  for LAMOST KNN, with error bars calculated from bootstrap resampling.

The extended  $T_{\rm eff}$ -FIP bias diagram includes 59 stars, which seem to lie on two separate lines, shifted by a FIP-bias value of ~0.5. To show these trends in Fig. 3, we used a RANSAC (RANdom SAmple Consensus)<sup>2</sup> regressor to fit two lines. We use this robust regression method to first identify the most prominent linear correlation (the  $T_{\rm eff}$ -FIP bias diagram of MS stars from Laming (2015a) shown in Fig. 2 with black points), and then fit the outlier points with another RANSAC line. To match visual inspection, the residual threshold parameter was set to 0.2 dex

<sup>&</sup>lt;sup>2</sup> The RANSAC algorithm selects a subset of the original data points, and splits it to inlier and outlier points after fitting them by a model. By iterating these steps a final set of outliers is created where the outliers will have no influence on the final fit. We used RANSACRegressor from sklearn.linear\_model.



**Fig. 2.** Literature FIP bias vs.  $T_{\rm eff}$ . Black dots indicate the stars from the original FIP-bias diagram of Laming (2015a), updated from Wood & Linsky (2010), forming a tight sequence with  $T_{\rm eff}$ .



**Fig. 3.** The  $T_{\rm eff}$ -FIP bias diagram with recalculated FIP-bias values. For the Sun, orange points mark its activity minimum and maximum. Solid and dashed lines show two component linear fits with a RANSAC regressor, with gray and red colours corresponding to literature and KNN FIP bias, respectively.

in FIP bias, it is the maximum residual to be classified as an inlier. The fitted lines seem to be similar for both literature and KNN FIP bias, see the red and gray lines in Fig. 3. For the lower branch, the fitted parameters are as follows:

FIP bias<sub>lit</sub> = 
$$(-0.00038 \pm 0.00002)T_{\text{eff}} + (1.77 \pm 0.08)$$
 (2)

FIP bias<sub>KNN</sub> = 
$$(-0.00041 \pm 0.00002)T_{\text{eff}} + (2.01 \pm 0.09)$$
 (3)

And for the upper branch:

FIP bias<sub>lit</sub> = 
$$(-0.00042 \pm 0.00003)T_{\text{eff}} + (2.61 \pm 0.18)$$
 (4)

FIP bias<sub>KNN</sub> =  $(-0.00040 \pm 0.00003)T_{\text{eff}} + (2.39 \pm 0.16)$  (5)

# 4.2. Contributions of the different stellar parameters to the structure of the $T_{\rm eff}$ -FIP bias diagram

To check the contribution of the different stellar parameters to the structure of the  $T_{\rm eff}$ -FIP bias diagram, we plotted several relations with the data points weighted by a given parameter. In the following we discuss which parameters have strong influence on the FIP-bias values of the sample, thus ultimately shape the diagram, whereas other parameters have seemingly no direct relation to the FIP bias and its bimodal distribution.

In the left panels of Fig. 4 from top to bottom, data points in the  $T_{\rm eff}$ -FIP bias diagram are coloured increasingly dark with increasing values of four stellar parameters: *a*) the log *g* surface gravity, *b*) the log  $L_X$  X-ray luminosity, *c*) the [Fe/H] metallicity, and *d*) the log *t* age. The evolved stars seem to form a separate, steep branch around  $T_{\rm eff} \sim 4500-5000$  K, as seen from the points with light yellow hue accounting for their low log *g* values in



Fig. 4.  $T_{\text{eff}}$ -FIP bias diagrams with data points coloured according to various parameters. Missing parameters are indicated with black crosses. See the text for the details.

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Fig. 4 *a*. The giant stars  $\mu$  Vel, Capella and  $\beta$  Cet, all around  $T_{\text{eff}} \sim 5000 \text{ K}$  with FIP bias slightly below zero, have low gravities and high X-ray luminosities as seen in Fig. 4 *b*.

Metallicity is close to solar for almost all stars; see Fig. 4 c. This parameter is uncertain anyway, and since all stars are close to the Sun in space, we cannot expect great differences. It looks that the observed age does not have an influence on FIP bias at all; see Fig. 4 d. However, we call attention to the uncertainty of the age determinations. The measured stellar parameters which are used for finding the age (like effective temperature or rotation) are modified in different extents by stellar activity originating from magnetic fields of different strengths. Additionally, gyrochronology is valid on the MS only, since off the MS the internal structure of the stars is changing fast (Barnes 2007), therefore it is not possible to use it for the whole sample.

The MS sample consists of mostly young stars with only a few exceptions. Among the solar-type stars, only the two components of the  $\alpha$  Cen system are of similar age than the Sun, and the third component Proxima Cen is among the M-type flare stars. From the 17 evolved stars five are older than 5 Gyr and also five are younger than 1.4 Gyr, the rest do not have derived ages. To find the age of the 10 close RS CVn systems in this group is problematic due to the non-trivial evolution of the close binaries with strong magnetic activity. If there exists any age effect on the FIP-bias values, we cannot explore it on the basis of the available data.

In right panels of Fig. 4 from top top bottom, data points are coloured increasingly dark with increasing values of: e) the  $\log v_{rot}$  stellar rotational velocity, f) the  $\log F_X$  X-ray flux, g) the  $\log R'_{\rm HK}$  chromopheric activity index, and h) the  $\log Ro$  Rossby number. Fast rotating stars (with higher rotational velocity), regardless of spectral type and evolutionary state, have higher FIPbias values by about 0.5 at the same  $T_{\rm eff}$ . The evolved stars with their high rotational velocity make up the majority of the stars on the upper branch of the diagram. Apart from the evolved stars the three fast rotating K dwarfs (AB Dor, LO Peg and V471 Tau), all F-stars except Procyon, and a few fast rotating G dwarfs are situated in the upper branch as well. From the evolved stars Capella and  $\beta$  Cet are the slowest rotators with 104 and 205 days periods, respectively, and for  $\mu$  Vel no rotational period is known; these stars lay on the original lower branch of the  $T_{\rm eff}$ -FIP bias diagram (see the black dots in Fig. 2).

Together with the higher rotational velocities, the X-ray fluxes are also higher in the parallel, upper relation (Fig. 4*f*) as follows from the rotation-activity relation. We note that fast rotating stars did not simply increase the scatter of the relation towards the higher FIP-bias values, but appear on the new branch with a clear separation from the original one, which was implicitly suggested by Wood et al. (2018, see their Fig. 7a), depicting the Vaughan-Preston gap (Vaughan & Preston 1980). For the fast rotating M dwarf stars the X-ray activity saturates (see, e.g. Magaudda et al. 2020).  $\mu$  Vel, Capella and  $\beta$  Cet have large radii, these are three stars out of the four having larger that  $10 R_{\odot}$ . The high X-ray luminosity of  $\mu$  Vel, Capella and  $\beta$  Cet (Fig. 4*b*) combined with their large radii result in lower X-ray fluxes which fit well in the lower, original branch of the relation.

The important chromospheric activity parameter  $\log R'_{HK}$  is missing for many stars, especially for the evolved stars. However, as a direct activity index,  $\log R'_{HK}$  affects the FIP bias at least to some extent; see Fig. 4 g, and see the lower panel of Fig. 7 for more details. The Rossby numbers for the sample were calculated separately for MS (Noyes et al. 1984) and evolved stars (Gondoin 2007) with different empirical methods, see Sect. 2. From Fig. 4 h it seems that stars with lower Rossby numbers have higher FIP-bias values (M-type MS and evolved stars). However, due to the non-uniform calculation of the Rossby number this should be taken with caution. The visible trends would be the same with the dynamo number  $N_D$ , if we assume a power law  $N_D(Ro) \sim Ro^{\alpha}$  with constant exponent. The role of the Rossby number in interpreting the magnetic dynamo inside the stars of the sample is further discussed in Sect. 5.

As a further insight on the importance of each parameter in the formation of the bimodality, the result of the LDA can be used. The upper panel of Fig. 5 shows the linear boundary we used to a priori separate the two parallel sequences. The FIP bias was removed from the input parameters, so the LDA only used ten scaled features to predict the membership to the lower or upper sequence. The absolute values of the LDA coefficients are plotted in the lower panel of Fig. 5. Since the input parameters were scaled to have zero mean and unit variance, these coefficients can be treated as a sort of feature importance. The thin lines show the result of bootstrap analysis, where all the input points were resampled with replacement, in order to quantify the uncertainty of the method. It appears that the most important parameters separating the two sequences are the stellar radius and  $\log L_X$ . Naturally, these are correlated with  $\log g$ ,  $\log F_X$  and  $\log v_{rot}$ . An interesting result is that the ratio of the coefficients corresponding to  $\log R$  and  $\log g$  is ~2, indicating that  $2 \log R + \log g \sim \log M$  is a variable that separates the two branches, where M is the stellar mass. The dependence on metallicity, Rossby number and age is negligible. The small contribution of  $\log R'_{HK}$  is due to the numerous missing values.

# 4.3. Correlations between the parameters of the stars in the $T_{\rm eff}$ -FIP bias diagram

As a start, we plotted the correlation matrix between the stellar parameters with Spearman correlation coefficients in Fig. 6, showing the most direct linear correlations. One can see for example that  $\log L_X$  is correlated with  $\log v_{\text{rot}}$ . The FIP bias shows the strongest correlation with  $T_{\text{eff}}$ , but  $\log F_X$  also seems to be important.

Using all 12 parameters, we run PCA to represent the sample in a lower dimensional space, making it easier to look for emerging clusters. To find the optimal number of principal components (PCs) to keep, several heuristic methods can be used. Figure 7 shows the explained variance ratio for different number of PCs, i.e. the fraction of the sample variance that a given component can explain. An elbow point (abrupt change in the slope) appears around three or four components, hinting that the optimal number should be no greater, as adding more parameters does not cause such a steep increase in information content. Indeed, using the first four PCs can explain  $\sim 80\%$  of the sample variance. It is interesting (although not surprising) that the elbow point is clearly at N=3 for the MS stars, since there are parameters that do not change much if one excludes giants (e.g.  $\log g$ ). The Kaiser criterion (Kaiser 1960) states that one has to retain at least the PCs with eigenvalues larger than 1, which carry more information than an average single parameter from the original dataset (see the dashed line in Fig. 7). In our case the eigenvalues drops below 1 after PC3. In the lower panel of Fig. 7, one can see how each of the PCs are made up. The following rough trends can be observed:

- PC1 contains parameters related to the corona, namely the FIP bias,  $\log L_X$ ,  $\log F_X$  and the Rossby number;
- PC2 contains  $T_{\text{eff}}$  and parameters related to the "size" of the star, log g and radius;



Fig. 5. Results of the linear discriminant analysis (LDA). Upper panel: the pre-defined boundary between the two clusters (red and blue points) is shown with dashed lines on the  $T_{\rm eff}$ -FIP bias diagram. The larger circles indicate the clusters assigned by the LDA. The three misclassified stars are t Hor, HR 7291 and AY Cet. Lower panel: the absolute value of the LD components corresponding to the given parameters. Thin lines come from bootstrap resampling, error bars indicate the region between the 16th and 84th percentiles.



Fig. 6. Correlation matrix using Spearman correlation coefficients.



Fig. 7. Upper panel: Explained variance ratio of each principal component (PC). The dashed line denotes the Kaiser criterion (Kaiser 1960), and the red points show the elbow points. Lower panel: The importance of each parameter to a given principal component, with darker colours indicating stronger contribution (in absolute values).

- PC3 contains  $T_{\rm eff}$  and activity-related parameters  $v_{\rm rot}$  and log  $R'_{HK}$ ; - PC4 contains the otherwise unimportant metallicity

Figure 8 shows two-dimensional projections in PC space. It is clearly seen from the colour gradient that the FIP bias plays an important role (red colour indicates positive, blue negative FIP bias).

#### 5. Discussion

### 5.1. On the bimodality of the $T_{\rm eff}$ -FIP bias diagram

The  $T_{\rm eff}$ -FIP bias plots (see Fig. 2 with the names of the stars indicated) show at least two distinct features, i) the blob of data points splits into two linear correlations, and *ii*) the part where M dwarfs are located seems to be separated. A question arises immediately, namely, is there a connection between the bimodal distribution of the FIP-bias values and the fact that as rotation increases, magnetic field increases and saturation can occur in the filling factor? Concerning the results of Saar (1996) and Reiners et al. (2009), it is possible that magnetic saturation occurs in the filling factor at higher rotation rates. According to Baker et al. (2019) and Laming (2021), higher filling factor leads to less volume for expansion with increasing altitude for the magnetic field, and IFIP is more likely to occur in conditions with minimal field expansion. A higher photospheric filling factor may also lead to an increase in subsurface magnetic reconnection, which appears to be linked to transient solar IFIP coronal abundances (Baker et al. 2019, 2020). Figure 4e shows that stars with higher



**Fig. 8.** The first four PCs, coloured with the FIP bias (see Fig. 9 for the colour scale). The clear colour gradient shows the importance of the FIP bias parameter.

FIP bias exhibit higher rotational velocities. However, this feature alone cannot explain the separation of the two branches in the diagrams.

The bimodality of the FIP diagram probably depicts the Vaughan–Preston gap, originally defined as a discontinuity in the activity index 'S' for FGK main sequence stars (Vaughan & Preston 1980), i.e., medium activity stars are missing. The origin of this discontinuity is still actively debated.

Stellar rotation periods show bimodality in open clusters: the speed of the evolution for stars of similar age depends only on the mass of the stars; this is addressed by Barnes (2010) depicting the rotational evolution of a star with age. The model finds a high speed transition from fast to slow rotation, thereby creating a void at medium rotational periods depending on the colour (temperature) and mass of the stars. As a consequence of the discontinuity of rotational periods and concerning the existing activity–rotation relations (faster rotation results in higher activity level), the bimodality occurs in the activity levels of open cluster members regarding their age, and the transition is not continuous, as observed by Pace et al. (2009). However, this simple relation can be applied only to members of open clusters whose ages are known.

Unfortunately, we cannot use age as a parameter in finding the cause of the bimodality on the FIP bias diagrams. To derive the age of active field stars is complicated, if at all possible. The existing age estimates are usually quite uncertain due to the effect of strong and variable magnetism which is not taken into account in the stellar evolution models (for the evolved stars see more discussion below). Thus, only the stellar rotation remains as the parameter when characterizing the activity level through the known rotation–activity relations. In this work we apply the rotational velocities as a parameter, and for this we need to know the stellar radii as well. We use X-ray flux (surface units) as coronal activity measure. The bimodal distribution of the FIP-bias values is clear between the high and low rotational velocities, in line with the X-ray flux which is representative of the strength of magnetic activity; see Figs. 4*e*-*f*.

Brooks et al. (2017) have shown that the FIP-bias value of the Sun as a star changes with the solar cycle as much as 0.2. The magnetically active stars in the sample may have been at any point in their activity cycle at the time of measurement of their coronal abundances, which may increase the scatter in the  $T_{\rm eff}$ -FIP bias relation, and may narrow the gap between the two branches.

Our sample contains 17 evolved stars, most of them are members of close binaries, only four stars are single (see Table 1). From the evolved stars' sample 11 stars are active RS CVn binaries which have more complicated rotational evolution due to the gravitational and magnetic effects, making it impossible to get reliable age estimates. The active binaries with subgiant or giant primaries maintain fast rotation due to their binarity, and these stars make up the majority of the upper branch in the diagrams with fast rotating stars. The interested reader can find details about the theory of rotational evolution of low mass stars in close binaries, taking into account magnetic braking as well, by Fleming et al. (2019) and references therein.

In Fig. 9 we present the result of a k-means clustering in the 4 dimensional parameter space (keeping only 4 PCs), projected into two dimensions. Based on the elbow method and the average silhouette score (for an overview, see e.g. Nanjundan et al. 2019), the optimal number of k-means clusters is k = 3, which resulted in physically interpretable groups. PC1 reflects mostly the contribution of the effects of the coronal parameters (FIP bias and X-ray flux), while PC2 depends mostly on the stellar parameters of radius and  $\log g$ , as displayed in Fig. 7. Figure 9 shows that the first cluster is formed by flare stars from late K to M type (light red background), the second one by MS stars from A to early K type (light blue background), and the third cluster by evolved stars (light brown background). The upper branch on the  $T_{\rm eff}$ -FIP bias diagram consists mainly of the stars from the third cluster, along with the fast rotating three K dwarfs and the fastest rotating solar-type stars (cf. Tables 1 and 2), all of which situate close to the evolved stars in Fig. 9. The three slowly rotating evolved stars ( $\mu$  Vel, Capella and  $\beta$  Cet) show up in the second cluster and lay in the lower branch in all of the  $T_{\rm eff}$ -FIP bias diagrams. To illustrate the three clusters, Fig. 10 shows the sample on the Gaia colour-magnitude diagram. We note that the same conclusion is reached with clustering in the original 12 dimensional parameter space.

#### 5.2. Clustering by different dynamo types?

The three clusters found in our heterogeneous active star sample shown in Fig. 9 may reflect the differences of the dynamo working inside these stars. Magnetic activity signatures can manifest in different ways on different parts of the Hertzsprung-Russell diagram. On the Sun, active regions are mostly concentrated to a  $\pm 30^{\circ}$  latitude strip around the equator. On fast rotating solarlike stars, stellar spots tend to concentrate around the pole (e.g., V1358 Ori, Kriskovics et al. 2019). Using surface flux transport models, Işık et al. (2018) found that this can indeed happen on faster rotating solar-like stars, due to the surface transport of emerging magnetic structures, which can be attributed to large scale surface flows (e.g., a strengthened meridional circulation) and the Coriolis-force, which can deflect the rising flux towards the poles. On the other hand, fully convective M dwarfs can exhibit spot structures stable for a few thousand rotations (e.g., V374 Peg, Vida et al. 2016). Stars on the red giant branch can also have very different spot configurations, e.g., from time to



Fig. 9. The first two principal components, coloured (in the symbols' centre) with FIP bias. Special stars (evolved, M dwarfs and A–F stars) are indicated separately with different symbols. The clusters found with k-means are shown with red, blue and brown polygons.

time, polar spot structures of varying contrast were observed on  $\zeta$  And (Kővári et al. 2007, 2012; Roettenbacher et al. 2016). A similar RS CVn system,  $\sigma$  Gem also exhibits intermittent polar structures (cf. Kővári et al. 2015; Korhonen et al. 2021). Since spots are the most easily observed proxies of dynamo action, this may also mean that on different types of stars, we observe the manifestations of different types of dynamos.

The depths of the convection zones on the MS vary from the total stellar interior (full convection, low-mass M dwarfs) through different sizes of convection zone decreasing from fully convective to a very thin layer going from M, K, and G dwarfs to F-type stars, all with log g values of around 4.5–5. Both the depth of the convective region and speed of rotation have a bearing on differential rotation, which is crucial for the  $\Omega$ -effect, thus, this might point towards a more  $\alpha$ -effect dominated dynamo as the convective zone deepens. In case of evolved stars the convection zones are deep, but the surface gravity is much lower.

At first glance, one would expect the separation to be dependent on the Rossby number through activity, since it is connected to rotation, especially in light of the fact that  $\log L_X$  and  $\log F_X$ seem to play an important role here. However, it seems that the Rossby number does not. There could be a few reasons for that: the Rossby number was derived using different methods for MS and evolved stars using empirical relationships, and both rotation and the convective turnover time (e.g., through the depth of

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the convective envelope) can be drastically different on different parts of the Hertzsprung-Russell diagram.

For young and evolved stars a common dynamo scaling has been proposed recently by Lehtinen et al. (2020). Following their approach, using the chromospheric activity index  $\log R'_{HK}$  we plotted the coronal activity index  $\log F_X$  of the sample versus stellar rotation+radius and Rossby number in Fig. 11. The result is very similar to that of Lehtinen et al. (2020): while there is a clear separation of  $\log F_X$  between MS and evolved stars in the function of rotation combined with radius (free from  $\tau_c$ ), the use of Rossby number results in one relation regardless of evolutionary state of the stars. This result shows that the strength of coronal activity depends on the underlying dynamo.

The clustering of the stars in our sample points towards the possibility to further check the dynamos at work in the stars within the clusters. We note however, that the origin and working of the stellar dynamos are not well established theoretically to date, and has a lot of unknown effects due to various physical parameters. A thorough and detailed review of dynamos in active stars (including the Sun) is given by Brun & Browning (2017) both from observational and theoretical points of view, and we direct the interested reader to consult this paper.

While the stars in the sample differ by dynamo type, the ways their coronae are heated could also be different (e.g., by waves, turbulence, braiding (nanoflares) and helicity conservation, see Cranmer & Winebarger 2019), which could have implications



**Fig. 10.** Gaia EDR3 colour–magnitude diagram (within 100 pc), showing the clusters from the k-means analysis from Fig. 9, using the same colour coding for the three clusters. Gaia magnitudes for stars brighter than  $G = 3^{\text{m}}$  (e.g. the Sun) were estimated from V and  $I_C$  magnitudes, according to Riello et al. (2021). The nearly equal mass M dwarf binaries YY Gem and AU Mic lie above the main sequence due to their binary nature. In case of AU Mic its youth also plays a role, the third star AT Mic is a PMS object, this triple is a member of the  $\beta$  Pic moving group.

for the FIP effect. Inverse FIP fractionation arises from upward propagating fast modes that are reflected/refracted back downwards (see e.g., Laming 2017). As this happens in the chromosphere, the fractionation itself does not tell anything about how the corona is heated. Figure 12 shows that as the Rossby number decreases, the coronal X-ray flux (depending on the strength of the magnetic field) increases, similar to the results of Testa et al. (2015). Stars with increasing magnetic strength/X-ray flux show FIP effect, which gradually turns to inverse FIP effect. The magnetic field eventually saturates. Although the stellar rotation/dynamo generates magnetic field, it is destroyed by reconnection before it can rise to the corona, and the waves produced by this reconnection give the inverse FIP fractionation.

## 6. Summary and conclusions

We present FIP-bias values for 59 stars extending the sample with active MS and evolved stars for which no FIP-bias values were available to date. The literature FIP-bias values are recalculated, and as a second set, new FIP-bias values are presented for all stars in the sample using homogeneously derived photospheric abundances based on LAMOST data. For a few stars we derived new photospheric abundances via spectral synthesis with SME. The main results can be summarized as follows:

- We did not find systematic difference among the FIP-bias values using the recalculated literature, KNN or SME photospheric abundances, except for the KNN values of the coolest stars due to the lack of such stars in the LAMOST training set.
- We find that the  $T_{\rm eff}$ -FIP bias diagram is not a simple relation, but it now has two branches separated by ~0.5 in FIP bias. The new (upper) branch consists of mostly evolved stars and additionally stars with high rotational velocity. The low-mass, flaring M dwarfs form a small blob in the continuation of the lower branch of the relation.



**Fig. 11.** Upper panel:  $\log F_X$  versus combined rotation period and stellar radius *Lower panel*:  $\log F_X$  versus Rossby number as in Figures 3b and 2a in Lehtinen et al. (2020) but with  $\log F_X$  instead of  $\log R'_{HK}$ . The colour bars in both panels indicate surface gravity.



Fig. 12. X-ray flux versus Rossby number, coloured with the FIP bias.

- We suggest that the well-defined separation of the two branches in the  $T_{\rm eff}$ -FIP bias relation may be related to the bimodality in activity levels (the Vaughan-Preston gap), which in turn may be linked to a bimodality in rotation rates (periods) of stars of the same age but in different evolutionary stages due to different masses and/or binary evolution.

- The separation of the two branches is observable through activity indicators like  $v_{rot}$ , log  $F_X$ , Ro and log  $R'_{HK}$  showing the importance of these parameters in the FIP bias of the stellar sample.
- Statistical analysis of 12 stellar parameters reveals three clusters of stars in the sample. The evolved stars are well separated from the MS stars which are roughly divided by the sign of the FIP-bias values. The distribution of stars in the diagrams showing the clusters by means of distances between the stellar parameters and the linear discriminant analysis suggest that the FIP bias relates to the depths and structures of the convection zones of the stars indicated by their measured parameters. The properties (or the lack) of the convection zones have direct effect on the magnetic activity of the stars, and through this, on the FIP-bias values.

The results presented in this paper through investigating the effects of different stellar parameters widen our knowledge about the existing  $T_{\text{eff}}$ -FIP bias relation. The extension of the sample to evolved stars may help to generalize this relation for different kinds of magnetically active stars in different evolutionary stages.

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# Appendix A: Tabulation of abundances for the FIP bias calculation

Table A.1. Data for the calculation of the literature FIP bias.

Star		Co	rona			Photo	osphere		FIP bias	Corona	Solar photosphere
	[C/Fe]	[N/Fe]	[O/Fe]	[Ne/Fe]	[C/Fe]	[N/Fe]	[O/Fe]	[Ne/Fe]		source	source
AD Leo	1.45	0.96	1.64	1.18	0.93	0.33	1.19	0.80	$0.49 \pm 0.11$	(1)	(30)
CN Leo	1.25	0.64	1.33	0.76	0.93	0.33	1.19	0.80	$0.27 \pm 0.17$	(2) Table 2 DEM1	(24)
EQ Peg A	-	0.80	1.68	1.17	-	0.33	1.19	0.80	$0.53 \pm 0.07$	(3) Table 7 Q	(25)
EQ Peg B	-	0.82	1.61	1.13	-	0.33	1.19	0.80	$0.49 \pm 0.08$	(3) Table 7 Q	(25)
Prox Cen	-	1.13	1.54	1.04	-	0.33	1.19	0.80	$0.55 \pm 0.30$	(3) Table 10 Q	(25)
EV Lac	-	0.93	1.69	1.10	-	0.33	1.19	0.80	$0.55 \pm 0.15$	(3)Table 10 Q	(25)
YY Gem	-	1.12	1.75	1.26	-	0.33	1.19	0.80	$0.69 \pm 0.17$	(3) Table 10 Q	(25)
AU Mic	1.63	1.19	1.77	1.39	0.93	0.33	1.19	0.80	$0.68 \pm 0.13$	(1)	(30)
AT Mic	1.42	0.82	1.55	1.16	0.93	0.33	1.19	0.80	$0.51 \pm 0.07$	(4) Table 4 3T model	(24), O, Fe (26)
ABDor	1.50	1.06	1.75	1.35	0.93	0.33	1.19	0.80	$0.60 \pm 0.09$		(30)
LO Peg	1.50	0.84	1.61	1.35	0.93	0.33	1.19	0.80	$0.59 \pm 0.07$	(5) Table 1 Q	(26)
V471 Tau			1.57	1.04			1.19	0.80	$0.39 \pm 0.10$	(6) Table 4	(26), O (27)
36 Oph A	0.57	0.44	1.19	0.88	0.83	0.49	1.35	0.96	$-0.14 \pm 0.09$	(1)	(30), ph. a. (33)
36 Opn B	0.44	0.33	1.10	0.67	0.83	0.49	1.35	0.96	$-0.2/\pm 0.10$		(30), ph. a. (33)
ξ B00 B	0.78	0.24	1.19	0.97	1.09	0.22	1.30	0.97	$-0.16 \pm 0.15$		(30), pn. a. (33)
61 Cyg A	0.95	0.34	1.12	0.79	0.93	0.33	1.19	0.80	$-0.01 \pm 0.04$		(30), pn. a. (35)
70 Oph A	1.20	0.18	1.60	1.06	0.93	0.41	1.19	0.80	$0.33 \pm 0.08$		(30), pn. a. $(35)$
70 Oph A	0.04	0.18	0.92	1.01	0.88	0.41	1.27	0.88	$-0.29 \pm 0.00$		(30), pli. a. $(33)$
ло Орп Б	0.98	0.70	1.55	0.84	0.88	0.41	1.27	0.88	$0.13 \pm 0.10$ 0.06 ± 0.07		(30), pli. a. $(33)$
a Cen A	0.90	0.42	0.35	0.04	0.75	0.55	1.21	0.02	$-0.54 \pm 0.30$	(1) low activity	(30), pli. a. $(33)$
$\alpha \operatorname{Cen} B$	0.72	0.00	0.33	0.41	0.99	0.40	1.32	0.95	$-0.34 \pm 0.30$ $-0.38 \pm 0.15$	(1) low activity	(30), pl. a. $(33)$
$\pi^1$ LIMo	0.70	0.14	0.87	0.33	1.07	0.43	1.29	1.01	$-0.38 \pm 0.13$	(1) Iow activity	(30), pli. a. $(33)$
FK Dro	0.34	0.30	0.84	0.46	0.02	0.34	1.40	0.80	$-0.43 \pm 0.18$	(1)	(30), pli. a. (33)
ć Boo A	0.98	0.19	1.12	0.90	1.00	0.55	1.19	0.80	$-0.00 \pm 0.13$ $-0.20 \pm 0.04$	(1)	$(30)$ ph $_{2}$ $(33)$
ζ DOOA	0.75	0.20	0.64	0.09	0.00	0.30	1.30	0.57	$-0.29 \pm 0.04$	(1)	(30), pli. a. $(33)$
χ On «Cot	0.33	-0.33	0.67	0.49	1.03	0.48	1.34	0.56	$-0.47 \pm 0.33$	(7)	(24), Fe (28), pli. a. (29) (24) Eq (28), ph. a. (20)
B Com	0.42	-0.12	0.07	0.01	0.96	0.46	1.34	0.50	$-0.38 \pm 0.34$ $-0.58 \pm 0.25$	(7)	(24), Fe $(26)$ , pli. a. $(29)(24)$ Fe $(28)$ ph a $(20)$
47 Cas B	0.49	0.39	1.03	1.03	0.90	0.40	1.52	0.34	$-0.38 \pm 0.23$ 0.19 ± 0.36	(7)	(24), 10(20), pll. a. (29) (24) Ee (28)
/ Hor	0.05	0.33	1.05	0.79	0.95	0.30	1.15	0.38	$0.19 \pm 0.30$ $0.21 \pm 0.25$	(7)	(30)
11 LMi	0.75	0.45	1.09	0.33	0.93	0.33	1 19	0.50	$-0.10 \pm 0.23$	(9) Table 3	(30)
HR 7291	_	_	0.68	0.13	-	_	1 19	0.80	$-0.51 \pm 0.12$	(9) Table 4	(30)
$\sigma^2 CrB$	_	0.35	1.17	0.74	_	0.33	1 19	0.80	$0.06 \pm 0.04$	(10) Table 5.0	(26)
E UMa	_	-	1.42	1 11	_	-	1 19	0.80	$0.00 \pm 0.01$ $0.35 \pm 0.05$	(11) Table 3	(26)
HR 1099	1.50	1.16	1.87	1.41	0.93	0.33	1.19	0.80	$0.35 \pm 0.05$ $0.76 \pm 0.12$	(12) Table 4 APEC	(24), Fe $(28)$
UX Ari	1.95	1.72	2.03	1.72	0.93	0.33	1.19	0.80	$1.13 \pm 0.25$	(12) Table 4 APEC	(24). Fe (28)
$\lambda$ And	1.28	0.74	1.67	1.31	0.93	0.33	1.19	0.80	$0.52 \pm 0.07$	(12) Table 4 APEC	(24), Fe (28)
VY Ari	1.57	1.11	1.78	1.44	0.93	0.33	1.19	0.80	$0.74 \pm 0.09$	(12) Table 4 APEC	(24), Fe (28)
Capella	0.66	0.40	0.93	0.40	0.93	0.33	1.19	0.80	$-0.13 \pm 0.20$	(12) Table 4 APEC	(24), Fe (28)
$\sigma$ Gem	-	1.21	1.61	1.24	-	0.33	1.19	0.80	$0.66 \pm 0.26$	(13) Table 4	rel. to same solar
31 Com	-	_	1.31	0.66	-	-	1.19	0.80	$0.07 \pm 0.19$	(14) Table 5	(25)
$\mu$ Vel	-	-	1.06	0.44	-	-	1.19	0.80	$-0.16 \pm 0.16$	(14) Table 5, ObsID 3410	(25)
$\beta$ Cet	-	-	1.13	0.54	-	-	1.19	0.80	$-0.08 \pm 0.14$	(14) Table 5	(25)
FK Com	-	-	1.35	1.06	-	-	1.19	0.80	$0.29 \pm 0.07$	(15) Table 7	(24)
YY Men	1.14	1.19	1.41	1.13	0.93	0.33	1.19	0.80	$0.49 \pm 0.31$	(16) Table 2 XMM Method 1	(26)
EI Eri	0.10	0.25	0.15	0.08	0.00	0.00	0.00	0.00	$0.23 \pm 0.08$	(17) Figure 5	(30)
V851 Cen	1.19	1.05	1.84	1.50	0.93	0.33	1.19	0.80	$0.67 \pm 0.22$	(18) Table 2	(24)
AR Psc	1.74	1.00	1.70	1.18	0.93	0.33	1.19	0.80	$0.68 \pm 0.19$	(19) Table 5	(25)
AY Cet	1.70	1.01	1.37	0.96	0.93	0.33	1.19	0.80	$0.53 \pm 0.32$	(19) Table 5	(25)
II Peg	-	1.33	2.47	1.93	-	0.33	1.19	0.80	$1.22 \pm 0.14$	(20) Table 4 Q	(24)
ARLac	0.70	0.93	1.51	1.10	1.02	0.33	1.19	0.80	$0.49 \pm 0.17$	(21) Table 3	(24)
$\eta$ Lep	0.78		1.09	0.55	1.03	-	1.55	0.96	$-0.31 \pm 0.09$	(1)	(30), pn. a. (32)
$\pi^{2}$ Ori	0.79	0.11	0.92	0.46	1.12	0.49	1.35	0.96	$-0.41 \pm 0.07$	(1)	(30), ph. a. (33)
$\tau$ Boo A	0.83	-	0.91	0.50	0.93	0.22	1.16	0.77	$-0.21 \pm 0.09$		(30), ph. a. (34)
Procyon	1.20	0.68	1.43	0.77	0.93	0.33	1.19	0.80	$0.29 \pm 0.17$	(22) Table 4	(24), Fe=7.51
Altair	0.95	0.32	0.96	0.26	1 1 0 6	0.89	175	136	$-0.56 \pm 0.42$	1 (23) Table 2 MOS/RGS	(26) ph a (31)

**Notes.** Coronal abundances are taken in quiescent (Q) or low activity state, where available. The original assumed solar photospheric values are indicated in the last column, which were all converted to Asplund et al. (2009) and Ne from Drake & Testa (2005). If there were available stellar photospheric abundance (ph. a.) measurements for a star, the source is also given in the last column. The FIP bias and its uncertainty are calculated as the mean and standard deviation of  $[X/Fe]_{cor}-[X/Fe]_{phot}$ , where X can be C, N, O and Ne. The FIP bias column is corrected by +0.084 according to Wood et al. (2018), except for the stars listing (1) as source. As discussed in Sect. 2, GJ 338 AB is omitted.

**References.** (1) Wood et al. (2018), (2) Fuhrmeister et al. (2007), (3) Liefke et al. (2008), (4) Robrade & Schmitt (2005), (5) Lalitha et al. (2017), (6) García-Alvarez et al. (2005), (7) Telleschi et al. (2005), (8) Sanz-Forcada et al. (2019), (9) Peretz et al. (2015), (10) Osten et al. (2003), (11) Ball et al. (2005), (12) Audard et al. (2003), (13) Huenemoerder et al. (2013a), (14) García-Alvarez et al. (2006a), (15) Gondoin et al. (2002), (16) Audard et al. (2004), (17) Nordon et al. (2013), (18) Sanz-Forcada et al. (2004), (19) Sanz-Forcada et al. (2009), (20) Huenemoerder et al. (2001), (21) Huenemoerder et al. (2002), (23) Robrade & Schmitt (2009), (24) Anders & Grevesse (1989), (25) Asplund et al. (2005), (26) Grevesse & Sauval (1998), (27) Allende Prieto et al. (2001), (28) Grevesse & Sauval (1999), (29) Allende Prieto et al. (2006), (30) Asplund et al. (2009), (31) Erspamer & North (2003), (32) Yüce et al. (2011), (33) Allende Prieto et al. (2004), (34) Gonzalez & Laws (2007), (35) Jofré et al. (2015)

Table A.2. Data for the calculation of the KNN FIP bias.

Star		Со	rona		Photosphere		FIP bias	Corona		
	[C/Fe]	[N/Fe]	[O/Fe]	[Ne/Fe]	[C/Fe]	[N/Fe]	[O/Fe]	[Ne/Fe]		source
AD Leo	1.45	0.96	1.64	1.18	0.58	0.33	0.87	0.48	$0.74 \pm 0.10$	(1)
CNLeo	1.25	0.64	1.33	0.76	0.53	0.32	0.84	0.80	$0.46 \pm 0.32$	(2) Table 2 DEM1
EO Peg A	_	0.80	1.68	1.17	_	0.32	0.84	0.80	$0.65 \pm 0.25$	(3) Table 7 O
EQ Peg B	_	0.82	1.61	1 13	_	0.32	0.84	0.80	$0.60 \pm 0.20$ $0.61 \pm 0.22$	(3) Table 7 Q
Prox Cen	_	1 13	1.54	1.04	_	0.32	0.84	0.80	$0.67 \pm 0.22$	(3) Table 10 O
FV Lac	_	0.03	1.54	1.04	_	0.32	0.04	0.80	$0.67 \pm 0.31$ 0.65 ± 0.24	(3) Table 10 Q
LV Lac	_	1.12	1.09	1.10	_	0.32	0.91	0.80	$0.05 \pm 0.24$	(3) Table 10 Q
	1.62	1.12	1.75	1.20	0.57	0.32	0.80	0.80	$0.80 \pm 0.23$	(3) Table 10 Q
AU MIC	1.05	1.19	1.//	1.39	0.57	0.52	0.00	0.49	$0.95 \pm 0.08$	(1) (4) Tabla 4 2T model
	1.42	0.82	1.55	1.10	0.32	0.52	0.64	0.80	$0.70 \pm 0.24$	(4) Table 4 51 model
AB Dor	1.50	1.00	1./5	1.55	0.89	0.30	1.43	1.04	$0.49 \pm 0.20$	(1)
LOPeg	1.50	0.84	1.61	1.35	1.07	0.23	1.69	0.80	$0.46 \pm 0.31$	(5) Table I Q
V4/I Tau	-	_	1.5/	1.43	-	-	1.25	0.86	$0.53 \pm 0.17$	(6) Table 4
36 Oph A	0.57	0.44	1.19	0.88	0.90	0.37	1.47	1.08	$-0.18 \pm 0.18$	(1)
36 Oph B	0.44	0.33	1.10	0.67	0.87	0.37	1.41	1.02	$-0.28 \pm 0.17$	(1)
<i>ξ</i> Βοο Β	0.78	-	1.19	0.97	0.68	0.31	1.08	0.70	$0.16 \pm 0.10$	(1)
61 Cyg A	0.95	0.34	1.12	0.79	0.70	0.29	1.14	0.76	$0.08 \pm 0.12$	(1)
61 Cyg B	1.26	-	1.60	1.06	0.61	0.33	1.04	0.66	$0.54 \pm 0.12$	(1)
70 Oph A	0.64	0.18	0.92	0.56	0.80	0.41	1.30	0.92	$-0.28 \pm 0.11$	(1)
70 Oph B	0.98	0.70	1.35	1.01	0.69	0.35	1.08	0.70	$0.31 \pm 0.04$	(1)
ε Ēri	0.90	0.42	1.20	0.84	0.83	0.39	1.34	0.96	$-0.04 \pm 0.11$	(1)
$\alpha$ Cen A	0.72	0.06	0.35	0.41	0.83	0.52	1.22	0.84	$-0.47 \pm 0.31$	(1) low activity
$\alpha$ Cen B	0.70	0.14	0.87	0.33	0.79	0.54	1.21	0.83	$-0.33 \pm 0.17$	(1) low activity
$\pi^1$ UMa	0.54	0.36	0.84	0.48	0.91	0.37	1.30	0.91	$-0.32 \pm 0.21$	
EK Dra	0.98	0.19	1.12	0.96	0.84	0.39	1.29	0.90	$-0.04 \pm 0.17$	
É Boo A	0.75	0.12	1 11	0.69	0.85	0.38	1 34	0.95	$-0.19 \pm 0.07$	(1)
$v^1$ Ori	0.75	-0.33	0.64	0.09	0.05	0.36	1.24	0.95	$-0.30 \pm 0.31$	(1)
$\chi$ Off	0.33	-0.55	0.04	1.00	0.91	0.30	1.20	0.09	$-0.39 \pm 0.31$	(7)
R Cel	0.42	-0.12	0.07	0.46	0.04	0.39	1.29	0.91	$-0.28 \pm 0.32$	(7)
p Com	0.49	-0.55	1.02	0.40	0.92	0.50	1.27	0.88	$-0.32 \pm 0.23$	(7)
4/Cas B	0.85	0.39	1.05	1.42	0.80	0.39	1.29	0.90	$0.14 \pm 0.33$	(7)
$\iota$ Hor	0.75	0.43	1.31	1.18	0.88	0.44	1.25	0.86	$0.15 \pm 0.19$	(8)
11 LM1	0.97	0.11	1.09	0.33	0.78	0.58	1.18	0.80	$-0.12 \pm 0.32$	(9) Table 3
HR 7291	-	_	0.68	0.13	-	-	1.25	0.80	$-0.53 \pm 0.08$	(9) Table 4
$\sigma^2 \text{ CrB}$	-	0.35	1.17	0.74	-	0.40	1.28	0.80	$0.01 \pm 0.03$	(10) Table 5 Q
ξ UMa	-	-	1.42	1.50	0.94	0.34	1.34	0.96	$0.39 \pm 0.33$	(11) Table 3
HR 1099	1.50	1.16	1.87	1.41	0.78	0.45	1.19	0.80	$0.76 \pm 0.05$	(12) Table 4 APEC
UX Ari	1.95	1.72	2.03	1.72	0.80	0.45	1.21	0.80	$1.12 \pm 0.21$	(12) Table 4 APEC
$\lambda$ And	1.28	0.74	1.67	1.31	0.87	0.37	1.38	0.80	$0.48 \pm 0.09$	(12) Table 4 APEC
VY Ari	1.57	1.11	1.78	1.44	0.80	0.43	1.22	0.80	$0.75 \pm 0.09$	(12) Table 4 APEC
Capella	0.66	0.40	0.93	0.40	0.62	0.64	1.09	0.80	$-0.11 \pm 0.19$	(12) Table 4 APEC
$\sigma$ Gem	-	1.21	1.61	1.24	-	0.48	1.22	0.80	$0.60 \pm 0.19$	(13) Table 4
31 Com	-	-	1.31	0.66	-	_	1.24	0.80	$0.05 \pm 0.15$	(14) Table 5
$\mu$ Vel	-	-	1.06	0.44	-	_	1.16	0.80	$-0.15 \pm 0.18$	(14) Table 5, ObsID 3410
$\beta$ Cet	-	_	1.13	0.54	_	_	1.10	0.80	$-0.03 \pm 0.21$	(14) Table 5
, FK Com	_	_	1.35	1.06	_	_	1.17	0.80	$0.30 \pm 0.06$	(15) Table 7
YY Men	1.14	1.19	1.41	1.13	0.81	0.45	1.26	0.80	$0.47 \pm 0.25$	(16) Table 2 XMM Method 1
ELEri	1.03	0.58	1.34	1.27	0.77	0.46	1.21	0.82	$0.32 \pm 0.15$	(17) Figure 5
V851 Cen	1.19	1.05	1.84	1.89	0.80	0.44	1.24	0.85	$0.74 \pm 0.27$	(18) Table 2
ARPsc	1 74	1.00	1 70	1.57	0.67	0.54	1.09	0.70	$0.83 \pm 0.27$	(19) Table 5
AY Cet	1.70	1.00	1.70	1.35	0.76	0.51	1.09	0.88	$0.09 \pm 0.27$ 0.59 ± 0.34	(19) Table 5
II Peg	1.70	1 33	2 17	2 32	0.88	0.31	1 38	0.00	$1.22 \pm 0.17$	(20) Table 4 O
ADLee	_	0.02	1.51	1.12	0.00	0.34	1.30	1.00	$1.22 \pm 0.17$ 0.40 ± 0.25	(20) Table 4 Q (21) Table 3
n Lac	0.78	0.95	1.01	0.55	1.02	0.34	1.30	0.06	$0.49 \pm 0.23$	(21) Table 5
$\eta$ Lep	0.70	0.11	1.09	0.33	1.05	0.33	1.33	0.90	$-0.50 \pm 0.09$	
$\pi^{-}$ Ori	0.79	0.11	0.92	0.46	0.99	0.33	1.30	0.91	$-0.31 \pm 0.12$	(1)
τ B00 A	0.83	-	0.91	0.50	0.95	0.41	1.24	0.85	$-0.27 \pm 0.13$	
Procyon	1.20	0.68	1.43	0.77	0.98	0.35	1.29	0.80	$0.25 \pm 0.15$	(22) Table 4
Altaır	0.95	0.32	0.96	0.64	1.07	0.30	1.42	1.42	$-0.25 \pm 0.36$	(23) Table 2 MOS/RGS

**Notes.** Coronal abundances are taken in quiescent (Q) or low activity state, where available. The photospheric abundances are predicted with the KNN method using data from Wang et al. (2020), and are relative to Asplund et al. (2009) solar composition and Ne from Drake & Testa (2005). As there were no Ne abundances in the LAMOST dataset, the photospheric [Ne/Fe] column was calculated as  $[Ne/Fe]_{phot} = [O/Fe]_{phot} + \log_{10} 0.41$ . The FIP bias and its uncertainty are calculated as the mean and standard deviation of  $[X/Fe]_{cor} - [X/Fe]_{phot}$ , where X can be C, N, O and Ne. The FIP bias column is corrected by +0.084 according to Wood et al. (2018), except for the stars listing (1) as source. As discussed in Sect. 2, GJ 338 AB is omitted.

**References.** (1) Wood et al. (2018), (2) Fuhrmeister et al. (2007), (3) Liefke et al. (2008), (4) Robrade & Schmitt (2005), (5) Lalitha et al. (2017), (6) García-Alvarez et al. (2005), (7) Telleschi et al. (2005), (8) Sanz-Forcada et al. (2019), (9) Peretz et al. (2015), (10) Osten et al. (2003), (11) Ball et al. (2005), (12) Audard et al. (2003), (13) Huenemoerder et al. (2013a), (14) García-Alvarez et al. (2006a), (15) Gondoin et al. (2002), (16) Audard et al. (2004), (17) Nordon et al. (2013), (18) Sanz-Forcada et al. (2004), (19) Sanz-Forcada et al. (2009), (20) Huenemoerder et al. (2001), (21) Huenemoerder et al. (2002), (23) Robrade & Schmitt (2009)

# Appendix B: Results of the spectral synthesis

star	T <sub>eff</sub>	$\log g$	[Fe/H]	v <sub>mic</sub>	v sin i	A(C)	A(O) <sub>NLTE</sub>	A(Fe)	FIP bias
	[K]	[cgs]		[km s <sup>-1</sup> ]	[km s <sup>-1</sup> ]				
70 Oph A	$5320 \pm 40$	$4.52 \pm 0.06$	$-0.02 \pm 0.07$	$1.12 \pm 0.02$	$3.7 \pm 0.05$	8.49	8.90	7.42	$-0.49 \pm 0.07^{a}$
70 Oph B	4400	4.47	-0.02	1.85	6.4	8.79	8.81	7.60	$0.12 \pm 0.23^{a}$
$\beta$ Com	$6090 \pm 60$	$4.41 \pm 0.05$	$-0.03 \pm 0.05$	$1.28 \pm 0.1$	$5.1 \pm 0.05$	8.35	8.61	7.45	$-0.54 \pm 0.30^{b}$
EK Dra	$5840 \pm 100$	$4.57 \pm 0.20$	$-0.01 \pm 0.10$	$1.6 \pm 0.05$	$18.3 \pm 0.1$	8.50	8.87	7.53	$-0.13 \pm 0.15^{a,b}$
$\epsilon \operatorname{Eri}$	$5050 \pm 10$	$4.48 \pm 0.05$	$-0.11 \pm 0.01$	$0.99 \pm 0.01$	$3.7 \pm 0.2$	8.53	8.97	7.49	$-0.22 \pm 0.06^{a}$
ηLep	$6920 \pm 70$	$4.19 \pm 0.02$	$-0.09 \pm 0.05$	$1.83 \pm 0.2$	$19 \pm 0.2$	8.27	9.40	7.45	$-0.63 \pm 0.5^{a}$
кCet	$5740 \pm 20$	$4.48 \pm 0.01$	$-0.02 \pm 0.06$	$1.25 \pm 0.03$	$5.7 \pm 0.1$	8.45	8.80	7.45	$-0.46 \pm 0.07^{b}$
$\chi^1$ Ori	$6020 \pm 10$	$4.45 \pm 0.03$	$-0.06 \pm 0.05$	$1.21 \pm 0.05$	$9.7 \pm 0.1$	8.35	8.62	7.47	$-0.38 \pm 0.09^{b}$
<i>ξ</i> Boo A	$5550 \pm 100$	$4.66 \pm 0.20$	$-0.19 \pm 0.10$	$1.29 \pm 0.1$	$5.5 \pm 0.2$	8.50	8.90	7.48	$-0.29 \pm 0.03^{a}$
Sun (Moon)	$5840 \pm 60$	$4.44 \pm 0.10$	$-0.06 \pm 0.10$	$1.13 \pm 0.05$	$2.7 \pm 0.1$	8.44	8.65	7.44	_
$\pi^1$ UMa	$5950 \pm 70$	$4.53 \pm 0.10$	$-0.12 \pm 0.10$	$1.4 \pm 0.05$	$10 \pm 0.1$	8.36	8.69	7.47	$-0.27 \pm 0.18^{a,b}$
$\pi^3$ Ori	$6430 \pm 40$	$4.25 \pm 0.01$	$-0.05 \pm 0.01$	$1.37 \pm 0.1$	$17.8 \pm 0.2$	8.18	8.67	7.43	$-0.23 \pm 0.19^{a}$
$\tau$ Boo A	$6370 \pm 30$	$4.14 \pm 0.04$	$0.16 \pm 0.10$	$1.34 \pm 0.2$	$16.2 \pm 0.2$	8.20	8.64	7.45	$-0.17 \pm 0.20^{a}$
$\lambda$ And	4510	2.57	-0.56	1.26	9.2	8.42	10.19	7.33	$-1.02 \pm 0.69^{\circ}$
$\beta$ Cet	4720	2.65	-0.15	1.58	6.3	8.22	9.16	7.35	$-0.79 \pm 0.46^{d}$
$\sigma$ Gem	4630	2.79	-0.10	1.62	27.4	8.37	9.69	7.34	$-0.58 \pm 0.26^{e}$

Table B.1. Results from the SME fit of CFHT-ESpaDoNS and TBL-NARVAL spectra.

**Notes.** Error bars (except for the FIP bias) are calculated as the standard deviation of the results from multiple spectra, and are omitted when only a single spectrum was available. This represents the internal precision of the method, not the true accuracy. The oxygen abundances already include the NLTE correction from Kovalev et al. (2018).

Sources of coronal abundances. <sup>*a*</sup> Wood et al. (2018), <sup>*b*</sup> Telleschi et al. (2005), <sup>*c*</sup> Audard et al. (2003), <sup>*d*</sup> García-Alvarez et al. (2006b), <sup>*e*</sup> Huenemoerder et al. (2013b)

# Appendix C: References for the individual stars listed in Table 2

#### *M-type flare stars*

**AD Leo**  $T_{\text{eff}}$ , [Fe/H]: Rojas-Ayala et al. (2012), log *g*, *R*: Stassun et al. (2019),  $P_{\text{rot}}$ : Morin et al. (2008), log  $R'_{\text{HK}}$ : Astudillo-Defru et al. (2017), log  $L_X$ : Wood et al. (2018, their Table 1), age (mean): Shkolnik et al. (2009)

**CN Leo**  $T_{\text{eff}}$ : Shulyak et al. (2014), log *g*, *R*: Stassun et al. (2019), [Fe/H]: Rojas-Ayala et al. (2012),  $P_{\text{rot}}$ : Newton et al. (2018), log  $L_X$ : Schmitt & Liefke (2004), age (mean): Pavlenko et al. (2006)

**EQ Peg A**  $T_{\text{eff}}$ : Yee et al. (2017), log g: calculated from mass, [Fe/H]: Yee et al. (2017),  $P_{\text{rot}}$ : Morin et al. (2008), log  $R'_{\text{HK}}$ : Gagné et al. (2016), R, log  $L_X$ : Wood et al. (2018, their Table 6), mass:  $0.36M_{\odot}$  from the Multiple Star Catalog (http://www.ctio.noao.edu/~atokovin/stars/stars.php), age: Zuckerman et al. (2013)

**EQ Peg B**  $T_{\text{eff}}$ : Houdebine et al. (2019),  $\log g$ : calculated from mass, [Fe/H] (as EQ Peg A): Yee et al. (2017),  $P_{\text{rot}}$ : Morin et al. (2008), R,  $\log L_X$ : Wood et al. (2018, their Table 1), mass:  $0.19M_{\odot}$  from the Multiple Star Catalog (http://www.ctio.noao.edu/~atokovin/stars/stars.php), age: Zuckerman et al. (2013)

**Proxima Cen**  $T_{\text{eff}}$ , log g: Zhao et al. (2018), [Fe/H] (as  $\alpha$  Cen A, B): Zhao et al. (2018),  $P_{\text{rot}}$ : Klein et al. (2021), R: Zhao et al. (2018), log  $R'_{\text{HK}}$ : Astudillo-Defru et al. (2017), log  $L_X$ : Wood et al. (2018, their Table 6), age (as  $\alpha$  Cen A, B): Zhao et al. (2018)

**EV Lac**  $T_{\text{eff}}$ , log g, [Fe/H]: Schweitzer et al. (2019),  $P_{\text{rot}}$ : Contadakis (1995), R: Schweitzer et al. (2019), log  $R'_{\text{HK}}$ : Gagné et al. (2016), log  $L_X$ : Wood et al. (2018, their Table 6), age (mean): Shkolnik et al. (2009)

**YY Gem**  $T_{\text{eff}}$ , log g (calculated from mass), R, mass: MacDonald & Mullan (2017),  $P_{\text{rot}}$ : Kochukhov & Shulyak (2019), [Fe/H], log  $L_X$ , age: MacDonald & Mullan (2014)

AU Mic  $T_{\text{eff}}$ : Houdebine et al. (2019), log g: Cifuentes et al. (2020), [Fe/H]: Houdebine (2009),  $P_{\text{rot}}$ : Messina et al. (2017), log  $R'_{\text{HK}}$ : Ibañez Bustos et al. (2019), R, log  $L_X$ : Wood et al. (2018, their Table 1), age: Gagné et al. (2018),

**AT Mic**  $T_{\text{eff}}$ : Malo et al. (2014), log g: calculated from mass, [Fe/H]: Houdebine (2009),  $P_{\text{rot}}$ , R: Messina et al. (2017), log  $L_X$ : Pye et al. (2015), mass:  $0.61M_{\odot}$  from the Multiple Star Catalog (http://www.ctio.noao.edu/~atokovin/stars/stars.php), age: Gagné et al. (2018),

### Fast rotating K dwarfs with flares

**AB Dor**  $T_{\text{eff}}$ : Close et al. (2007), log *g*: calculated from mass, [Fe/H]: Cayrel de Strobel et al. (1997),  $P_{\text{rot}}$ : Strassmeier (2009), *R*: Guirado et al. (2011), log  $R'_{\text{HK}}$ : Boro Saikia et al. (2018), log  $L_X$ : Wood et al. (2018, their Table 1), mass:  $0.86M_{\odot}$  from Guirado et al. (2011), age: Gagné et al. (2018),

**LO Peg**  $T_{\text{eff}}$ , log g: Folsom et al. (2016), [Fe/H]: Jeffries et al. (1994),  $P_{\text{rot}}$ : Dal & Tas (2003), R: Folsom et al. (2016), log  $R'_{\text{HK}}$ : Plavchan et al. (2009), log  $L_X$ : Lalitha et al. (2017), age: Gagné et al. (2018),

V471 Tau  $T_{\text{eff}}$ , log g, [Fe/H],  $P_{\text{rot}}$ , R, log  $L_X$ , log  $F_X$ : Kővári et al. (2021), age: Gagné et al. (2018)

K dwarfs

GJ 338 A  $T_{\text{eff}}$ , log g [Fe/H], R: Schweitzer et al. (2019),  $P_{\text{rot}}$ : González-Álvarez et al. (2020), log  $R'_{\text{HK}}$ : Gagné et al. (2016),  $\log L_X$ : Wood et al. (2018, their Table 6), age (upper limit,  $(B - V)_{SIMBAD} = 1^{m}41$ ): Barnes (2007),

GJ 338 B  $T_{\text{eff}}$ , log g [Fe/H], R: Schweitzer et al. (2019),  $P_{\text{rot}}$ : González-Álvarez et al. (2020) log  $R'_{\text{HK}}$ : Gagné et al. (2016), log  $L_X$ : Wood et al. (2018, their Table 6), age (upper limit,  $(B - V)_{SIMBAD} = 1^{m}.42$ ): Barnes (2007),

**36 Oph A**  $T_{\text{eff}}$ , log g: Luck (2017), [Fe/H]: Cayrel de Strobel et al. (1989),  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1)

**36 Oph B**  $T_{\text{eff}}$ , log g: Luck (2017), [Fe/H]: Cayrel de Strobel et al. (1989),  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1)

 $\boldsymbol{\xi}$  Boo B  $T_{\text{eff}}$ , log g, [Fe/H]: Aleo et al. (2017),  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1) 61 Cyg A  $T_{\text{eff}}$ , log g: Heiter et al. (2015), [Fe/H]: Luck & Heiter (2005),  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1)

61 Cyg B T<sub>eff</sub>, log g: Heiter et al. (2015), [Fe/H]: Luck & Heiter (2005), P<sub>rot</sub>, log R'<sub>HK</sub>, age: Barnes (2007), R, log L<sub>X</sub>: Wood et al. (2018, their Table 1)

**70 Oph A**  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1) **70 Oph B**  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper, log  $R'_{\text{HK}}$  (as 70 Oph A), age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1)

 $\epsilon$  Eri  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1)

Solar type stars

#### Sun

 $\alpha$  Cen A  $T_{\text{eff}}$ , log g, [Fe/H]: Morel (2018),  $P_{\text{rot}}$ : Angus et al. (2015), log  $R'_{\text{HK}}$ : Mamajek & Hillenbrand (2008), R, log  $L_X$ : Wood et al. (2018, their Table 1), age (mean): Zhao et al. (2018)

 $\alpha$  Cen B  $T_{\text{eff}}$ , log g, [Fe/H]: Morel (2018),  $P_{\text{rot}}$ : Angus et al. (2015), log  $R'_{\text{HK}}$ : Mamajek & Hillenbrand (2008), R, log  $L_X$ : Wood et al. (2018, their Table 1), age (mean): Zhao et al. (2018)

 $\pi^1$  UMa  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1) EK Dra  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ : Messina & Guinan (2002), log  $R'_{\text{HK}}$ : Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1), age: Gagné et al. (2018),

 $\xi$  Boo A  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 1)  $\chi^1$  Ori  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 6)  $\kappa$  Cet  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 6)  $\beta$  Com  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 6)  $\beta$  Com  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ , age: Barnes (2007), R, log  $L_X$ : Wood et al. (2018, their Table 6) 47 Cas B  $T_{\text{eff}}$ : Ness et al. (2004), [Fe/H]: Casagrande et al. (2011),  $P_{\text{rot}}$ , log  $L_X$ , age: Telleschi et al. (2005), R: Johnstone & Güdel (2015)

 $\iota$  Hor  $T_{\text{eff}}$ , log g, [Fe/H], R: Fuhrmann et al. (2017),  $P_{\text{rot}}$ : Metcalfe et al. (2010), log  $R'_{\text{HK}}$ : Boro Saikia et al. (2018), log  $L_X$ : Peretz et al. (2015), age: Gagné et al. (2018),

11 LMi  $T_{\text{eff}}$ : Yee et al. (2017), log g, [Fe/H],  $P_{\text{rot}}$ , log  $R'_{\text{HK}}$ : Olspert et al. (2018), R: Boyajian et al. (2013), log  $L_X$ : Peretz et al. (2015), age: Montesinos et al. (2016)

HR 7291  $T_{\text{eff}}$ : Giribaldi et al. (2019, their Table 4),  $\log g$ , [Fe/H],  $P_{\text{rot}}$ , R: Fares et al. (2013), age: Takeda et al. (2007),  $\log R'_{HK}$ : Wright et al. (2004),  $\log L_X$ : Peretz et al. (2015)

 $\sigma^2$  CrB  $T_{\text{eff}}$ , R, [Fe/H], age: Raghavan et al. (2009), log g: Luck (2017),  $P_{\text{rot}}$ : Strassmeier & Rice (2003), log  $R'_{\text{HK}}$ : Gray et al. (2003), log *L<sub>X</sub>*: Pye et al. (2015)

 $\xi$  UMa B  $T_{\text{eff}}$ , log g, [Fe/H]: Zhao et al. (2002),  $P_{\text{rot}}$  (= $P_{\text{orb}}$ ), R: Sanz-Forcada et al. (2003), log  $L_X$ : Dempsey et al. (1993)

## Evolved stars

**HR 1099**  $T_{\text{eff}}$ , log g, log  $R'_{\text{HK}}$ : Sreejith et al. (2020), [Fe/H]: Luck (2017),  $P_{\text{rot}}$ : Lanza et al. (2006), R: Fekel (1983), log  $L_X$ : Huenemoerder et al. (2013b)

UX Ari  $T_{\text{eff}}$ , log g, [Fe/H],  $P_{\text{rot}}$ , R, age: Hummel et al. (2017), log  $L_X$ : Makarov (2003)  $\lambda$  And  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ : Strassmeier et al. (1993), R, age: Montesinos et al. (2016), log  $R'_{\text{HK}}$ : Gray et al. (2003), log *L<sub>X</sub>*: Drake et al. (1992)

**VY Ari**  $T_{\text{eff}}$ , log g, [Fe/H]: Ottmann et al. (1998),  $P_{\text{rot}}$ : Strassmeier et al. (1997), R: Gaia Collaboration et al. (2018), log  $L_X$ : Makarov (2003)

**Capella**  $T_{\text{eff}}$ , log g, [Fe/H],  $P_{\text{rot}}$ , R, age: Torres et al. (2015), log  $L_X$ : Makarov (2003)

 $\sigma$  Gem  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ , R, age: Roettenbacher et al. (2015), log  $L_X$ : Huenemoerder et al. (2013b)

**31** Com  $T_{\text{eff}}$ , log g, [Fe/H],  $P_{\text{rot}}$ , R, age: Strassmeier et al. (2010), log  $L_X$ : García-Alvarez et al. (2006b)

 $\mu$  Vel  $T_{\text{eff}}$ : Ayres et al. (2007), log g: calculated from mass, R: Mullan et al. (2006), log  $L_X$ : Makarov (2003), mass:  $3.3M_{\odot}$ from Mallik et al. (2003)

 $\beta$  Cet  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ : Tsvetkova et al. (2013), R: Berio et al. (2011), log  $R'_{\text{HK}}$ : Rich et al. (2017),  $\log L_X$ : Makarov (2003), age: Stock et al. (2018)

FK Com  $T_{\text{eff}}$ , log g,  $P_{\text{rot}}$ : Korhonen et al. (2004), [Fe/H]: Anders et al. (2019), R: Gaia Collaboration et al. (2018), log  $L_X$ : Ayres et al. (2016)

**YY Men**  $T_{\text{eff}}$ , log g: Randich et al. (1993), [Fe/H],  $P_{\text{rot}}$ , R, log  $L_X$ : Audard et al. (2004)

EI Eri  $T_{\text{eff}}$ , log g, R,  $P_{\text{rot}}$ , age: Washuettl et al. (2009), [Fe/H]: Ottmann et al. (1998), log  $L_X$ : Osten et al. (2002)

**V851 Cen** *T*<sub>eff</sub>, log *g*, [Fe/H]: Katz et al. (2003), *P*<sub>rot</sub>: Kiraga (2012), *R*: Stawikowski & Glebocki (1994b), log *L*<sub>X</sub>: Dempsey et al. (1993)

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**AR Psc**  $T_{\text{eff}}$ , log g, [Fe/H]: Shan et al. (2006),  $P_{\text{rot}}$ : Matranga et al. (2010), R: Stawikowski & Glebocki (1994a), log  $L_X$ : Dempsey et al. (1993), age: Fekel (1996)

AY Cet  $T_{\text{eff}}$ , log g, [Fe/H], age: Deka-Szymankiewicz et al. (2018),  $P_{\text{rot}}$ : Strassmeier et al. (1990), R: Stawikowski & Glebocki (1994a), log  $L_X$ : Sanz-Forcada et al. (2003)

**II Peg**  $T_{\text{eff}}$ , log g, [Fe/H], R: Berdyugina et al. (1998),  $P_{\text{rot}}$ : Strassmeier et al. (1990), log  $L_X$ : Dempsey et al. (1993)

**AR Lac**  $T_{\text{eff}}$ , log g,  $P_{\text{rot}}$  (= $P_{\text{orb}}$ ): Lanza et al. (1998), [Fe/H]: Cayrel de Strobel et al. (1992), R: Zboril et al. (2005), log  $L_X$ : Dempsey et al. (1993)

#### F stars, hotter than 6300 K

 $\eta$  Lep  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper, log  $R'_{\text{HK}}$ : Boro Saikia et al. (2018), R, log  $L_X$ : Wood et al. (2018, their Table 1), age: Casagrande et al. (2011)

 $\pi^3$  Ori  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper, log  $R'_{\text{HK}}$ : Wright et al. (2004), R, log  $L_X$ : Wood et al. (2018, their Table 1), age: Wright et al. (2004)

 $\tau$  Boo A  $T_{\text{eff}}$ , log g, [Fe/H]: from this paper,  $P_{\text{rot}}$ : Fares et al. (2009), log  $R'_{\text{HK}}$ , age: Mamajek & Hillenbrand (2008), R, log  $L_X$ : Wood et al. (2018, their Table 1)

**Procyon**  $T_{\text{eff}}$ , log g, [Fe/H]: Kervella et al. (2004),  $P_{\text{rot}}$ : Ayres (1991), R: Aufdenberg et al. (2005), log  $L_X$ : Ness et al. (2002), age: Liebert et al. (2013)

Altair  $T_{\text{eff}}(\text{mean})$ , [Fe/H], R (mean): Monnier et al. (2007), log g: Malagnini & Morossi (1990),  $P_{\text{rot}}$ : Peterson et al. (2006), log  $L_X$ , age: Robrade & Schmitt (2009)