# The dependence of the gravity effect in elliptic neutron guides on the source size

3	${f D}$ Nekrassov <sup>1,2</sup> , C Zendler <sup>1,2</sup> , K Lieutenant <sup>1,2</sup>
4	<sup>1</sup> Helmholtz-Zentrum Berlin für Materialien und Energie GmbH, Hahn-Meitner-Platz 1, 14109
5	Berlin, Germany
6	$^2$ ESS design update programme, Germany
7	E-mail: daniil.nekrassov@helmholtz-berlin.de
8	Abstract.
9	Elliptic neutron guides are expected to be widely used for construction of long neutron
10	beamlines at the future European Spallation Source and other facilities due to their superiour
11	transmission properties compared to conventional straight guides. At the same time, neutrons
12	traveling long distances are subject to the action of gravity that can significantly modify their
13	flight paths. In this work, the influence of gravity on a neutron beam propagating through elliptic
14	guides is studied for the first time in a systematic way with Monte-Carlo simulations. It is shown
15	that gravity leads to significant distortions of the phase space during propagation through long
16	elliptic guides, but this effect can be recovered by a sufficiently large source size. The results
17	of this analysis should be taken into account during design of long neutron instruments at the
18	ESS and other facilities.

## 19 **1. Introduction**

 $_{\rm 20}$   $\,$  Flight paths of thermalised neutrons at reactor and spallation sources are modified by the action

of gravity. Its influence increases with rising wavelength of the neutrons and longer flight paths.

<sup>22</sup> For example, a 10 Å neutron traveling a distance of d = 100 m is displaced by gravity by

$$\Delta h = 0.5 \times g \times (d/v(\lambda))^2 = 0.5 \times 9.81 \,\mathrm{m/s^2} \times \left(\frac{100 \,\mathrm{m} \times 10 \,\mathrm{\mathring{A}}}{3956 \,\mathrm{m\mathring{A}/s}}\right)^2 \approx 31 \,\mathrm{cm}$$

This effect is significant and needs to be taken into account when designing or operating long
 neutron beamlines.

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The gravity problem has already received some attention in the past. A way to counteract 26 the vertical displacement of long-wavelength neutrons for instruments not comprising neutron 27 guides was found to be a modification of the vertical position of the (virtual) source with respect 28 to the sample and detector position [1], [2]. The influence of gravity on neutrons propagating 29 through a collimation system and a consequential distortion of reflectivity measurements on 30 liquid interfaces was included in an elaborated resolution theory that was confirmed by Monte-31 Carlo (MC) simulations [3]. On the other hand, the treatment of the gravity effect in neutron 32 guide tubes requires a numerical approach due to the occurrence of reflections. At a time when 33 computing power was limited and thus extensive MC simulations were difficult to carry out, an 34

analytical matrix formalism being less demanding in terms of calculation time was developed to
trace phase space during its propagation through straight or curved guides, including the influence of gravity [4]. The calculation of neutron trajectories in and outside guides then became
more accessible since the invention of MC software packages like VITESS [5].

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At the future European Spallation Source (ESS) facility [6], gravity will play a significant 40 role due to the length of planned instruments that often exceed 100 m. Such long beamlines 41 will need to include ballistic neutron guides to efficiently transport the neutrons to the sample 42 position [7]. In particular, elliptically shaped guides have lately received a significant attention 43 regarding their transmission and focusing properties [8], [9]. Currently, it can be expected that 44 several instruments at the ESS will comprise elliptic guides. However, the influence of gravity 45 on the beam properties after transmission through an elliptic guide has not been studied so 46 far in a systematic way, even though it was found that the focusing ability of elliptic guides 47 might be severely disturbed [8]. For a very long instrument of 300 m using a quite narrow 48 waveband of 0.8 Å around 6.66 Å it appears that incorporating the trajectory curvature into the 49 shape of the elliptic guide allows to remove the direct line-of-sight (LoS) without suffering flux 50 losses and preserve the instrument resolution [10]. The latter study, however, was carried out 51 for a potential ESS backscattering instrument, for which the influence of the beam divergence 52 distribution on the measured resolution is significantly reduced. Hence the present work aims 53 at studying the influence of gravity on the phase space structure for a large neutron waveband 54 after propagation in elliptic guides, in particular concerning the shape of the vertical divergence 55 distribution. This is important for instruments where the divergence distribution has a direct 56 impact on the illumination homogeneity of the sample/detector or on the shape of structures in 57 the scattering spectrum (e.g. for diffraction). 58

## <sup>59</sup> 2. Analysis and results

The gravity effect is studied using a simple instrument layout, see Fig 1. A source emitting 60 a constant spectrum as a function of wavelength is followed by an elliptic neutron guide with 61 a square cross section, of which the semi-axes are a = 75 m along the instrument axis and 62 b = 0.15 m in both directions perpendicular to it. The reflectivity of the guide coating  $R(\tilde{m})$ 63 is 0.99 for  $\tilde{m} < 1$  (with  $\tilde{m} = 10 \times \theta [\circ] / \lambda [Å]$ , where  $\theta$  is the reflection angle), decreases linearly 64 to  $R(\tilde{m} = 5.7) = 0.52$  and then drops quickly [11]. The guide is followed by a 1 cm<sup>2</sup> sample. 65 Both the source and the sample are located in the focal points of the ellipse. This study 66 utilises the new elliptic guide module available in the VITESS software from version 3.0, which 67 handles neutron propagation through a perfect ellipse, thus avoiding effects connected with guide 68 segmentation [8], since in such a study the gravity effect should be considered separately from 69 other imperfections. The distance  $D_0$  between the source and the guide entry and between the 70 guide exit and the sample is the same and the total length of the instrument is fixed to 150 71 m.  $D_0$  is varied between 20 cm and 5 m, thus varying the entry/exit width  $W_0$  between 2.2 72 cm and 10.8 cm. The source is a square with the edge length  $X_0$ , which is varied between 73  $1 \times 1$  cm<sup>2</sup> and  $12 \times 12$  cm<sup>2</sup>. All input parameters are summarized in Tab. 1. The coordinate 74 system follows the convention used in VITESS, i.e. the x-axis corresponds to the 75 instrument axis, while the y- and z-axis are completing a right-handed coordinate 76 system in horizontal and vertical directions, respectively. 77

The goal of the performed simulations is to monitor the beam characteristics at the sample position with regard to gravitational effects. Since it can be expected that gravity modifies the vertical divergence distribution (and thus the distribution in real space at the detector), an asymmetry parameter  $\Delta \gamma$  is introduced in order to describe this effect:



Figure 1. A sketch of the instrument layout used in the present study. The distance between the source and the sample is kept constant at 150 m, whereas the distance between the source and the guide entry (the guide exit and the sample) is varied between 20 cm and 500 cm. The source edge length is varied between 1 cm and 12 cm. See text for further details.

Table 1. Summary of input parameters used in the simulations.

Source	Spectrum: $I(\lambda) = const$
	Continuous wavelengths: $1 \text{ \AA} - 12 \text{ \AA}$
	Discrete wavelengths: 2 Å, 6 Å, 10 Å
	Edge length $X_0$ : 1 cm, 2 cm, 4 cm, 6 cm, 8 cm, 10 cm, 12 cm
Guide	Elliptic guide, $a = 75 \text{ m}, b = 15 \text{ cm}, m=6 \text{ coating}$
	Source-to-guide (guide-to-sample) distance $D_0$ :
	0.2  m, 0.5  m, 1  m, 2  m, 5  m
	Guide entry (exit) $W_0$ : 2.2 cm, 3.5 cm, 4.9 cm, 6.9 cm, 10.8 cm
	Source and sample at focal points
Sample	Size: $1 \times 1 \text{ cm}^2$

$$\Delta \gamma = \left| \frac{I(\gamma)_+ - I(\gamma)_-}{I(\gamma)_+ + I(\gamma)_-} \right| = \left| \frac{\int_0^{+\infty} [I(\gamma) - I(-\gamma)] d\gamma}{\int_0^{+\infty} [I(\gamma) - I(-\gamma)] d\gamma} \right|,\tag{1}$$

where  $I(\gamma)$  is the beam intensity as a function of divergence  $\gamma$  either in vertical or horizontal direction. The simulations are carried out for the waveband ranging from 1 Å to 12 Å and for discrete wavelengths 2 Å, 6 Å and 10 Å to illustrate the different behaviour of short- and long-wavelength neutrons.

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The results of the simulations are illustrated in Figs. 2 - 6. A careful consideration of the obtained distributions reveals **the** following major findings:

Gravity can strongly affect the vertical divergence distribution in long elliptic guides, as opposed to propagation through a straight neutron guide of comparable dimensions, see Fig. 2.

• The magnitude of distortion of the divergence distribution due to gravity depends on two parameters:

(i) Wavelength: As it could be expected, the divergence distribution is more distorted with
 increasing wavelength, see Fig. 3. For short wavelengths (and small sources/samples)

[8]), the final divergence distribution is more affected by propagation through an ellipse than by gravity [8].

- (ii) Source and guide entry size: The **asymmetry** decreases with increasing source size 98 (Fig. 2 (b), Fig. 3 (b) and (c)) or with decreasing entry width  $W_0$ /source-to-guide distance  $D_0$  (Fig. 4). 100
  - Despite the asymmetry in the divergence distributions, elliptic guides still provide a reasonable focusing in space, i.e. the flux is the largest at the sample position. At the same time, the focusing is more strongly reduced for larger  $X_0$  distances in vertical than in horizontal direction (if the source size  $W_0$  is kept constant), see Fig. 5.
- To minimize the distortion of the divergence distribution, the source needs to be of the same 105 size or larger than the guide entrance, see Fig. 6 (a). But – not surprisingly – the actual 106 ratio needed of the source size  $X_0$  to the guide entrance size  $W_0$  is wavelength dependent, 107 see Fig. 6 (b) for a (rough) quantification<sup>1</sup>. 108

• When a symmetric and featureless divergence distribution is reached, a further increase of 109 the source size does not increase the flux at the sample, see Fig. 2 (a), (b) and Fig. 3. 110

In particular the last two points are important findings. It can be observed that for a 111 given elliptical guide there is a certain (virtual) source size that completely smears out the 112 gravity distortion and features characteristic for transmission through elliptic guides. At the 113 same time, the source of this size provides the maximum flux on the sample, a fact deserving 114 serious attention when designing a neutron beamline. This is confirmed by an additional set of 115 simulations using an elliptic guide with the semi-axes a = 37.5 m,  $b_1 = 0.15$  m and  $b_2 = 0.075$  m, 116 a fixed distance between the source and the guide of 1 m and varying the size of the source again 117 between  $1 \times 1$  cm<sup>2</sup> and  $12 \times 12$  cm<sup>2</sup>. Here it was again observed that the divergence distribution 118 obtains a symmetric shape around zero every time the source is larger than the guide entry, see 119 Fig. 7. The conclusion is that the recovering of a symmetric divergence distribution happens by 120 mixing the neutron trajectories through multiple reflections, which are by far the most dominant 121 transmission regime in elliptic guides [8], such that all inhomogeneities are smeared out. This 122 process is more efficient if the source injects more phase space into the guide. 123

#### 3. Discussion and conclusions 124

The simulation results described in the last section clearly show that gravity can play an im-125 portant role in neutron transport in long elliptic guides, in particular for small sources and 126 long wavelengths. At the same time, it has been shown that these effects can be removed by 127 increasing the size of the (virtual) source such that it exceeds the guide entry dimensions. Such 128 a source is able to smear out the features in the divergence distribution at the sample position 129 coming both from gravity influence and transmission effects. Hence in principle, elliptic guides 130 are able to transport neutrons over long distances and provide a smooth phase space at the 131 sample position, if provided with an adequate input beam. This should be kept in mind for 132 design of instruments that are in need of a smooth phase space at sample/detector position. 133 134

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> <sup>1</sup> For each wavelength, this ratio was determined by simply averaging the smallest source-toentrance size ratios that still led to an asymmetry smaller than 1% and 5% thresholds, respectively, for all source sizes under study.



(a) Horizontal divergence distribution at sample position for an elliptic guide



(b) Vertical divergence distribution at sample position for an elliptic guide for varying source size  $X_0$ 



(c) Horizontal divergence distribution at sample position for a straight guide



(d) Vertical divergence distribution at sample position for a straight guide

Figure 2. (a) and (b): Divergence distribution at sample position for  $W_0 = 4.9$  cm ( $D_0 = 1$  m) for an elliptically shaped guide, see Tab. 1, using source sizes from  $1 \times 1$  cm<sup>2</sup> to  $12 \times 12$  cm<sup>2</sup> and the full spectrum between 1 Å and 12 Å. (c) and (d): Horizontal and vertical divergence distributions at sample position for a 148 m long guide with a constant  $10 \times 10$  cm<sup>2</sup> cross section having the same source-to-guide and guide-to-sample distance  $D_0 = 1$  m. The y-axis is logarithmic to fit in distributions for small source sizes. The zig-zag structures, which are particularly visible for small source sizes, are a systematic effect and arise due to fractions of the total phase space missing the 1 cm<sup>2</sup> sample, since straight guides lack focusing abilities. Here and in other plots the error bars (mostly too small to be visible) represent the statistical uncertainty due to the number of simulated trajectories.



(a) Vertical divergence distribution at sample position for 2 Å neutrons



(c) Vertical divergence distribution at sample position for 10 Å neutrons



(b) Vertical divergence distribution at sample position for 6 Å neutrons

Figure 3. Vertical divergence distribution at sample position using  $W_0 = 4.9$  cm  $(D_0 = 1 \text{ m})$  for 2 Å, 6 Å and 10 Å neutrons. Gravity leads to a modification and an asymmetry  $\Delta \gamma$  of the vertical divergence distribution in particular for long wavelengths.



Figure 4. Vertical divergence distribution at sample position for an elliptically shaped guide using a source with  $X_0 = 2$  cm and  $W_0$  between 2.2 cm and 10 cm ( $D_0$  between 20 cm and 5 m).



(a) Horizontal position distribution at sample position

(b) Vertical position distribution at sample position

Figure 5. Distribution of neutrons in space for a  $2 \times 2$  cm<sup>2</sup> source. The  $1 \times 1$  cm<sup>2</sup> sample indicated by dotted lines is located at the guide symmetry axis that coincides with the location of the highest flux even for a 5 m distance between guide and sample (corresponding to  $\approx 11$  cm guide exit width).



Figure 6. Vertical divergence distribution at the  $1 \times 1$  cm<sup>2</sup> sample being in the focal point of two different elliptic guides with given parameters. The distance  $D_0$  is 1 m. The guide entry width is 3.44 cm for b = 0.075 m and 6.88 cm for b = 0.15 m, respectively. The divergence distribution saturates for source sizes being larger than the guide entry and the asymmetry parameter  $\Delta \gamma$  becomes negligible.



(a) Vertical divergence asymmetry as a function of  $W_0$  and  $X_0$ 

(b) Size ratio of source to guide entry as a function of  $\lambda$ 

Figure 7. (a) The vertical asymmetry parameter  $\Delta \gamma$  defined in Eq. 1 as a function of the source edge length  $X_0$  and the entry width  $W_0$  of the elliptic guide for all neutrons. The colour plot is saturated at 0.2, with the maximum asymmetry at  $X_0 = 1$  cm and  $W_0 = 10.8$  cm. The white line corresponds to the relation  $X_0 = W_0$ . It is well visible that the gravity effect dominates for  $X_0 < W_0$ , i.e. for sources being smaller than the guide entrance. (b) The ratio of the source edge length  $X_0$  to the entry width  $W_0$  as a function of the neutron wavelength  $\lambda$  that is needed to achieve a vertical divergence distribution at sample position, which exhibits an asymmetry of less than 5% or 1%, respectively. As expected, larger source sizes are needed for larger wavelengths.

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