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RESEARCH ARTICLE

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A Bidirectional Subsurface Remote Sensing Reflectance Model Explicitly Accounting for Particle Backscattering Shapes

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Key Points:

- The bidirectional  $r_{rs}$  was analyzed and parameterized based on a theoretical derivation by Zaneveld (1982, 1995)
- The parameterized model explicitly accounts for particle backscattering shapes

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**Abstract** The subsurface remote sensing reflectance ( $r_{rs}$ ,  $\text{sr}^{-1}$ ), particularly its bidirectional reflectance distribution function (BRDF), depends fundamentally on the angular shape of the volume scattering functions (VSFs,  $\text{m}^{-1} \text{sr}^{-1}$ ). Recent technological advancement has greatly expanded the collection, and the knowledge of natural variability, of the VSFs of oceanic particles. This allows us to test the Zaneveld's theoretical  $r_{rs}$  model that explicitly accounts for particle VSF shapes. We parameterized the  $r_{rs}$  model based on HydroLight simulations using 114 VSFs measured in three coastal waters around the United States and in oceanic waters of North Atlantic Ocean. With the absorption coefficient ( $a$ ), backscattering coefficient ( $b_b$ ), and VSF shape as inputs, the parameterized model is able to predict  $r_{rs}$  with a root mean square relative error of  $\sim 4\%$  for solar zenith angles from 0 to 75°, viewing zenith angles from 0 to 60°, and viewing azimuth angles from 0 to 180°. A test with the field data indicates the performance of our model, when using only  $a$  and  $b_b$  as inputs and selecting the VSF shape using  $b_b$ , is comparable to or slightly better than the currently used models by Morel et al. and Lee et al. Explicitly expressing VSF shapes in  $r_{rs}$  modeling has great potential to further constrain the uncertainty in the ocean color studies as our knowledge on the VSFs of natural particles continues to improve. Our study represents a first effort in this direction.

1. Introduction

A fundamental quantity describing the color of the ocean is the subsurface remote sensing reflectance ( $r_{rs}$ ,  $\text{sr}^{-1}$ ), formed as a ratio of the upwelling radiance,  $L_u(\theta_s, \theta, \phi)$  to the downwelling irradiance,  $E_d(\theta_s)$ , with both defined just below the surface:

$$r_{rs}(\theta_s, \theta, \phi) \equiv \frac{L_u(\theta_s, \theta, \phi)}{E_d(\theta_s)}. \tag{1}$$

Here,  $\theta_s$  represents the in-water solar zenith angle,  $\theta$  the in-water sensor zenith angle, and  $\phi$  the sensor azimuth angle relative to the solar plane. The  $r_{rs}$  is related to the inherent optical properties (IOPs) of absorption and backscattering coefficients ( $a$  and  $b_b$ ) of the water body (Gordon, 1973; Morel & Prieur, 1977):

$$r_{rs}(\theta_s, \theta, \phi) = \frac{f' b_b}{Q a + b_b}. \tag{2}$$

In equation (2), the  $f'/Q$  is called the bidirectional reflectance distribution function (BRDF), describing the angular variation of  $r_{rs}$  with the sun-viewing geometry. Many studies, some of which are cited in the following, used remote sensing reflectance ( $R_{rs}$ ), defined just above the surface to describe the color of the ocean. Since the interface factor  $\mathfrak{R}$ , where  $R_{rs} = \mathfrak{R} \times r_{rs}$ , can be more or less considered as a constant for all practical purposes (Gordon, 2005), we will use  $r_{rs}$ , for simplicity, to represent either case of the definitions.

Both numerical simulations and field measurements showed that the BRDF factor varies with both sun-viewing geometries and the IOPs (Gleason et al., 2012; Gordon, 1989; Lee et al., 2011; Loisel & Morel, 2001; Morel et al., 1995, 2002; Morel & Gentili, 1991, 1993, 1996; Zhai et al., 2015), and it can vary up to 50% with IOPs and up to 100% with sun-viewing geometries as shown in Loisel and Morel (2001) and Morel et al. (2002). It is clear from equation (2) that the BRDF factor needs to be known to estimate  $a$  and  $b_b$  from  $r_{rs}$ , or to predict  $r_{rs}$  from  $a$  and  $b_b$ . Also, correction of the BRDF effect is important for vicarious calibration of an ocean color sensor because the radiance measured in the field and observed in a satellite pixel are often associated with different viewing geometries.

Since the BRDF factor has been scarcely measured in the field, its prediction relies essentially on numerical simulations (Hirata et al., 2009; Hlaing et al., 2012; Lee et al., 2011; Loisel & Morel, 2001; Morel et al., 2002; Morel & Gentili, 1991, 1993, 1996; Park & Ruddick, 2005). Using Monte Carlo simulation, Morel and Gentili (1991, 1993, 1996) parameterized  $f'/Q$  as a function of chlorophyll concentration in case 1 waters. Further improvements were made by accounting for Raman scattering and changes of particle phase function (PF) with chlorophyll concentration (Morel et al., 2002), resulting in a look-up-table (LUT) of  $f'/Q$  with 13 azimuth angles, 17 viewing zenith angles, 6 solar zenith angles, 6 chlorophyll concentrations, and 7 wavelengths. The particle PFs used in the simulation were generated as a linear combination of two PFs, one with backscattering ratio of 1.4% and the other of 0.19%, intended to represent small and large particles, respectively. Currently, this precompiled LUT is widely used for the BRDF correction. However, this method requires the knowledge of chlorophyll concentrations and was designed for Case 1 waters with a maximum chlorophyll concentration of  $10 \text{ mg m}^{-3}$  (Morel et al., 2002).

Park and Ruddick (2005) and Hlaing et al. (2012) developed a fourth-order and a third-order polynomial fittings of  $r_{rs} = \sum_{i=1}^4 g_i \left( \frac{b_b}{a+b_b} \right)^i$  and  $r_{rs} = \sum_{i=1}^3 g_i \left( \frac{b_b}{a+b_b} \right)^i$ , respectively. In both cases, the Fournier–Forand (FF) (Fournier & Forand, 1994) PF was used and the coefficients  $g_i$  were tabulated as a function of sun-viewing geometry. Similarly, Lee et al. (2011) used a second-order polynomial to approximate the BRDF effect:

$$r_{rs} = \left( G_0^w + G_1^w \frac{b_{bw}}{a+b_b} \right) \frac{b_{bw}}{a+b_b} + \left( G_0^p + G_1^p \frac{b_{bp}}{a+b_b} \right) \frac{b_{bp}}{a+b_b}. \quad (3)$$

A fundamental difference between the Lee et al. (2011) model and the models by Park and Ruddick (2005) and Hlaing et al. (2012) is that Lee et al. (2011) separately accounted for the molecular and particle backscattering (Lee et al., 2004). Also, in Lee et al. (2011),  $r_{rs}$  were simulated using a linear mixing of the Petzold average particle PF (Mobley, 1994) representing mineral particles and the FF PF (Fournier & Forand, 1994) with a backscattering ratio of 1% (1% FF) (Mobley et al., 2002) representing phytoplankton particles. A LUT was computed for  $G_0^w$ ,  $G_1^w$ ,  $G_0^p$ , and  $G_1^p$  as a function of 13 azimuth difference angles, 7 viewing zenith angles, and 6 solar zenith angles.

Zaneveld (1982, 1995) derived from the radiative transfer equation (RTE) a theoretical expression for  $r_{rs}$ . This analytical derivation provides a physical basis for evaluating the BRDF effect, which includes four components: the average cosine ( $\bar{\mu}_d$ ) of downwelling radiance field, two shape factors describing backscattered downwelling radiance field ( $f_b$ ) and forward scattered upwelling radiance field ( $f_L$ ), and the diffuse attenuation coefficient of upwelling radiance ( $K_{Lu}$ ). The Zaneveld derivation is not a true solution but a restatement of the RTE with the radiance distribution represented by  $f_b$ ,  $f_L$ , and  $K_{Lu}$  (Zaneveld, 1995). Nevertheless, as pointed out by Zaneveld (1995),  $f_b$  and  $f_L$  vary in a relatively narrow range owing to the unique geometry of the light field and the particle scattering properties in the ocean, therefore it is possible to make approximations by relating them to the IOPs. The Zaneveld derivation has established an analytical basis, different from equation (2), for studying the BRDF effect.

Weidemann et al. (1995) investigated the error in retrieving particle backscattering ( $b_{bp}$ ) from nadir-viewed  $r_{rs}$  due to uncertainties in the two shape factors,  $f_L$  and  $f_b$ . They found the error can vary from  $-20\%$  to  $+40\%$ , primarily due to the uncertainty in  $f_b$ . They concluded that for  $r_{rs}$  inversion to be successful information about  $f_b$  must be included. Hoge et al. (2003) parameterized the Zaneveld (1995) shape factors using the Petzold average particle PF at 5 chlorophyll concentrations from 0.1 to  $10.0 \text{ mg m}^{-3}$ , 6 solar zenith angles from  $0$  to  $60^\circ$ , 1 viewing azimuth angle of  $90^\circ$ , and 10 wavelengths from 412 to 685 nm. Their model was able to predict the shape factors with a relative percentage error of 2–20%, and  $r_{rs}$  within 20%.

Studies have shown that the angular structure of bidirectional  $r_{rs}$  varies with the shape of the actual volume scattering functions (VSFs;  $\beta$ ,  $\text{m}^{-1} \text{ sr}^{-1}$ ) in the ocean (Chami et al., 2006a; Gordon, 1989; Mobley et al., 2002; Morel et al., 2002; Morel & Gentili, 1991; Xiong et al., 2017; Zaneveld, 1982, 1995); however, the current  $r_{rs}$  models are built primarily using one particle phase function (Hoge et al., 2003; Morel & Gentili, 1991, 1993, 1996) or a linear combination of two (Hlaing et al., 2012; Lee et al., 2011; Morel et al., 2002; Park & Ruddick, 2005), because the VSFs had been scarcely measured (Morel et al., 2002). Recent technological advancement (Lee & Lewis, 2003; Sullivan & Twardowski, 2009) has greatly expanded the collection, and the knowledge of natural variability, of the VSFs of oceanic particles (Chami et al., 2005; Sullivan & Twardowski, 2009; Zhang et al., 2002,

2012). These measurements showed that the natural variability of VSFs is much greater than what had been known or assumed previously (Xiong et al., 2017). In this study, we will utilize the new VSF dataset to parameterize  $r_{rs}$  in an attempt to better understand the effect of VSF shapes on the BRDF. In particular, we will use the theoretical derivation of Zaneveld (1995) as an analytical basis to explicitly account for the shape of the VSFs.

## 2. Theoretical Basis

Zaneveld (1982, 1995) derived from the RTE the subsurface bidirectional  $r_{rs}$  for an optically deep ocean,

$$r_{rs}(\theta_s, \theta, \phi) = \frac{1}{2\pi\bar{\mu}_d(\theta_s)} \frac{f_b(\theta_s, \theta, \phi)}{g(\theta_s, \theta, \phi)} \frac{b_b}{a+b_b}, \tag{4}$$

with

$$g(\theta_s, \theta, \phi) = 1 - \frac{K_{Lu}(\theta_s, \theta, \phi)}{a+b_b} \cos \theta - (f_L(\theta_s, \theta, \phi) - 1) \frac{b_f}{a+b_b}, \tag{5}$$

by introducing two shape factors  $f_b$  and  $f_L$ , which were, respectively, defined as

$$f_b(\theta_s, \theta, \phi) \equiv \frac{\int_0^{2\pi} \int_0^{\pi/2} \beta(\gamma) L(\theta_s, \theta', \phi') \sin \theta' d\theta' d\phi'}{\frac{b_b}{2\pi} E_{od}(\theta_s)} \tag{6}$$

and

$$f_L(\theta_s, \theta, \phi) \equiv \frac{\int_0^{2\pi} \int_{\pi/2}^{\pi} \beta(\gamma) L(\theta_s, \theta', \phi') \sin \theta' d\theta' d\phi'}{L_u(\theta_s, \theta, \phi) b_f}. \tag{7}$$

In equations (4)–(7),  $K_{Lu}$  is the diffuse attenuation coefficient for upwelling radiance,  $\bar{\mu}_d$  the downwelling average cosine,  $E_{od}$  the scalar downwelling irradiance,  $L$  the radiance distribution,  $c$  the attenuation coefficient,  $b_f$  the forward scattering coefficient, and  $\beta(\gamma)$  the VSF at the scattering angle  $\gamma$  formed between the incident light traveling in direction  $(\theta, \phi)$  and the scattered light traveling in direction  $(\theta, \phi)$ , and  $\cos \gamma = \cos \theta \cos \theta' - \sin \theta \sin \theta' \cos(\phi - \phi')$ .

Assuming  $\beta$  continuous in  $(\pi/2, \pi)$  and using the second mean value theorem for definite integrals,  $f_b$  in equation (6) can be rewritten as

$$f_b(\theta_s, \theta, \phi) = \frac{\beta(\gamma_m) \int_0^{2\pi} \int_0^{\pi/2} L(\theta_s, \theta', \phi') \sin \theta' d\theta' d\phi'}{\frac{b_b}{2\pi} E_{od}(\theta_s)} = \frac{2\pi\beta(\gamma_m)}{b_b}, \tag{8}$$

where

$$\beta(\gamma_m) = \frac{\int_0^{2\pi} \int_0^{\pi/2} \beta(\gamma) L(\theta_s, \theta', \phi') \sin \theta' d\theta' d\phi'}{\int_0^{2\pi} \int_0^{\pi/2} L(\theta_s, \theta', \phi') \sin \theta' d\theta' d\phi'}, \tag{9}$$

and  $\gamma_m$  represents the mean scattering angle between the downwelling radiance field and the upwelling radiance to be observed. The exact value of  $\gamma_m$  depends on both the shape of VSF and downwelling radiance distribution. As shown in equation (8), the value of  $f_b(\theta_s, \theta, \phi)$  does not depend on the exact geometry of  $(\theta_s, \theta, \phi)$  but is related to the mean scattering angle  $\gamma_m$ ; therefore, for simplicity, we will use  $f_b(\gamma_m)$  to represent  $f_b(\theta_s, \theta, \phi)$  hereafter. Equation (6) that defines  $f_b(\gamma_m)$  can be deduced through equation (8) to a ratio of  $\beta(\gamma_m)$  to  $b_b$ . Ignoring  $\gamma_m$  for a moment, equation (8) shows that the functional form of  $f_b$  is the inverse of the  $\chi$  factor ( $\chi = b_b/2\pi\beta$ ) (Oishi, 1990; Zhang et al., 2014a). However, the exact value of  $\gamma_m$  depends on the light field and the sun-viewing geometry, and so is  $f_b(\gamma_m)$ . Despite this, equation (8) provides a theoretical basis of using the  $\chi$  factor to simulate  $f_b(\gamma_m)$ .

By further separating  $\beta(\gamma_m)$  in equation (8) into molecular,  $\beta_w(\gamma_m)$  and particle,  $\beta_p(\gamma_m)$  components, we have

$$f_b(\gamma_m) = \frac{b_{bw}}{b_b} f_{bw}(\gamma_m) + \frac{b_{bp}}{b_b} f_{bp}(\gamma_m), \quad (10)$$

where

$$f_{bp}(\gamma_m) = \frac{2\pi\beta_p(\gamma_m)}{b_{bp}} \quad (11)$$

and

$$f_{bw}(\gamma_m) = \frac{2\pi\beta_w(\gamma_m)}{b_{bw}}. \quad (12)$$

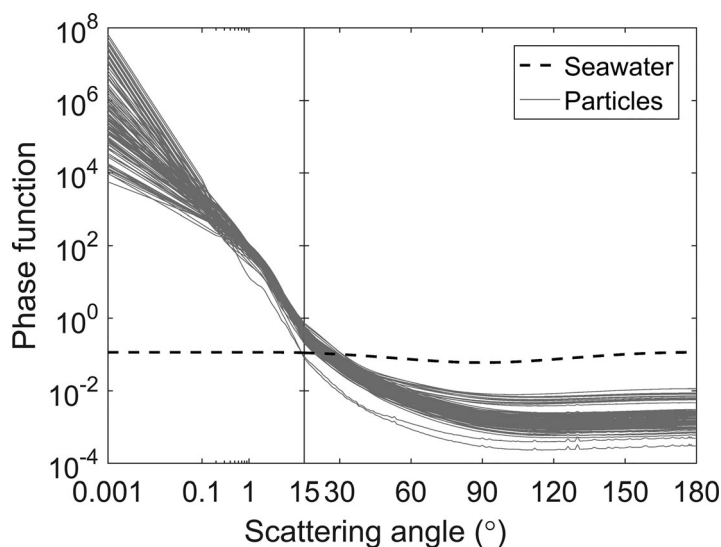
Combining equations (4) and (10), we have the bidirectional  $r_{rs}$  model that we will use for its parameterization in this study:

$$r_{rs}(\theta_s, \theta, \phi) = \frac{1}{2\pi\bar{\mu}_d(\theta_s)g(\theta_s, \theta, \phi)} (f_{bw}(\gamma_m) \frac{b_{bw}}{a+b_b} + f_{bp}(\gamma_m) \frac{b_{bp}}{a+b_b}). \quad (13)$$

In equation (13), the shape of the VSF, while also affects  $g$ , is explicitly represented in the two shape factors,  $f_{bw}$  and  $f_{bp}$ .

### 3. Data and Methods

The VSFs were measured in coastal waters of the US (Chesapeake Bay, Mobile Bay, and Monterey Bay) with chlorophyll concentrations ranging from 1.4 to 40  $\text{mg m}^{-3}$  and in open waters of North Atlantic Ocean with chlorophyll concentrations from 0.07 to 1.40  $\text{mg m}^{-3}$  using a prototype Multispectral Volume Scattering Meter (MVSM) at eight wavelengths and a commercial LISST-100X at 532 nm (Type B; Sequoia Scientific, Inc.). The VSFs by LISST-100X at angles from 0.07 to 9.4° and the VSFs by MVSM at 532 nm from 9.5 to 179° were combined to form a near complete angular resolution of the scattering (Zhang et al., 2012). Altogether, there are 114 measured VSFs. The use of these VSFs and their validations have been reported in several studies (Zhang et al., 2012, 2013, 2014a, 2014b, 2017; Zhang & Gray, 2015). Removing the scattering due to pure seawater (Zhang et al., 2009) from these measured VSFs, we estimated the phase functions due to particles (Figure 1), which exhibit a backscattering ratio varying 0.15–5.4%. For comparison, the backscattering ratios for the particle PFs vary from 0.19 to 1.4% in Morel et al. (2002) and from 1.0 to 1.8% in Lee et al. (2011). The PFs shown in Figure 1 were used in this study to represent the varying angular scattering by oceanic particles.



**Figure 1.** Phase functions at 532 nm computed for pure seawater and estimated for particles from the measured VSFs. The x-axis is in logarithmic scale at angles  $<15^\circ$  and in linear scale at larger angles.

HydroLight (Mobley, 1995) was used to simulate the light field. The IOPs, required as inputs for HydroLight, were generated following the IOCCG Report 5 (IOCCG, 2006). A total of 100 sets of spectral  $a$  and  $b_b$  at 532 nm ( $b_b/(a+b_b) \approx 0.03 - 0.30$ ;  $b_{bp}/(a+b_b) \approx 0.01 - 0.30$ ) were generated using 20 chlorophyll concentrations ( $\text{Chl} = 0.03\text{--}30.0 \text{ mg m}^{-3}$ ) and five phytoplankton specific absorption spectrum. For each set of  $a$  and  $b_b$ , 114 PFs were used to represent different particle assemblages, generating a total of 114,000 ( $=100 \times 114$ ) sets of IOPs ( $a$ ,  $b$ ,  $b_b$ , and PF). The viewing zenith angles in air were set from 0 to 60° at an interval of 10°, the solar zenith angles in air from 0 to 75° at an interval of 15°, and the viewing azimuth angles relative to the sun from 0 to 180° at an interval of 45°. The simulation generated a total of 1,778,400 ( $=5 \times 5 \times 6 \times 100 \times 114 + 1 \times 1 \times 6 \times 100 \times 114$ ) sets of AOPs at 532 nm. The simulated downwelling irradiance, upwelling and downwelling radiance distribution at depths of 0<sup>-</sup> (just below the surface) and 0.01 m were used to estimate the parameters of  $f_b$ ,  $g$ , and  $\bar{\mu}_d$  in equation (13).

$f_L$  was estimated following equation (7) using the input  $\beta$  and HydroLight-simulated upwelling radiance distribution at the depth of  $0^-$ .  $\beta(\gamma_m)$  was estimated following equation (9), and the value of  $\gamma_m$  was found by matching the estimated  $\beta(\gamma_m)$  with the input  $\beta$ . With  $\gamma_m$ ,  $f_{bp}(\gamma_m)$ , and  $f_{bw}(\gamma_m)$  were estimated following equations (11) and (12), respectively.

#### 4. Results

##### 4.1. Comparison of the HydroLight Simulation and the Zaneveld (1995) Model Prediction

Even though both HydroLight and the Zaneveld model are based on the same RTE, it is expected that the detailed numerical implementations would introduce uncertainty. To establish a baseline of uncertainty that is due to numerical implementation, we compare  $r_{rs}$  calculated from equation (13) with the HydroLight simulation (Figure 2).

The two methods agreed with each other within 2.4% (standard deviation (SD) = 0.024  $\text{sr}^{-1}$ , Figure 2b). The Zaneveld model-predicted  $r_{rs}$  seemed to be slightly less than the HydroLight-simulated values for  $r_{rs} > 0.02$  (Figure 2a). Relatively greater differences were also found for both off-nadir viewing geometries and for more peaked phase functions. This is mainly due to the uncertainty introduced in the numerical integration for calculating  $f_L$ , which depends strongly on the shape of phase functions at near forward angles, particularly for off-nadir viewing geometries. Nevertheless, the relative difference in  $r_{rs}$  of 2.4% between the Zaneveld model and the HydroLight simulation is less than half of the 6% uncertainty reported in Mobley et al. (1993), which compared six numerical models in simulating water-leaving radiance.

To eliminate this inherent uncertainty due to performing numerical integration, which is also extremely time consuming, the  $g$  factor, which contains  $f_L$  (equation (5)), was estimated reversely using calculated  $f_b$ ,  $\bar{\mu}_d$ , and  $r_{rs}$ , and inputs of  $a$  and  $b_b$  following equation (4). The similar approach was used in Weidemann et al. (1995).

##### 4.2. Parameterization of $r_{rs}$

###### 4.2.1. Shape Factor $f_b$

Equation (10) shows that the shape factor  $f_b(\gamma_m)$  can be partitioned into backscattering weighted contributions due to pure seawater ( $f_{bw}(\gamma_m)$ ) and particles ( $f_{bp}(\gamma_m)$ ). The exact value of  $f_b(\gamma_m)$  also depends on the mean scattering angle  $\gamma_m$ . The values of  $\gamma_m$ , as shown in Figure 3, are generally greater than  $\pi/2$ , indicating the importance of the backscattering process in regulating  $f_b$ . Because the downwelling radiance field nearly always shows a dominant or maximum radiance at the angle of refracted solar disk just beneath the sea surface, a single-scattering approximation has been used to estimate  $f_b(\gamma_m)$  as  $f_b(\gamma_m) = \frac{2\pi\beta(\gamma_m)}{b_b} \approx \frac{2\pi\beta(\gamma_s)}{b_b}$  (Hoge et al., 2003; Weidemann et al., 1995; Zaneveld, 1995), where  $\gamma_s$  represents the scattering angle formed between the subsurface sun and the viewing vector. While  $\gamma_m$  is closely related to  $\gamma_s$ , which is fixed for a given sun-viewing geometry, they are different in values (Figure 3) as a result of multiple scattering. Therefore, we would also expect  $f_b(\gamma_m) \neq f_b(\gamma_s)$ . As an example, variations of  $f_{bp}(\gamma_m)$  and  $f_{bw}(\gamma_m)$  with  $\gamma_s$  are shown in Figure 4 for two particle PFs ( $b_{bp}/b_p = 0.0045, 0.0312$ ). Clearly,  $f_{bp}(\gamma_m)$  and  $f_{bw}(\gamma_m)$  (colored dots in Figure 4) covary with, but differ from, their respective single scattering counterparts,  $f_{bp}(\gamma_s)$  and  $f_{bw}(\gamma_s)$  (red lines in Figure 4). Over the entire data set, the best fits of  $f_{bp}(\gamma_m)$  and  $f_{bw}(\gamma_m)$  (black lines in Figure 4) are:

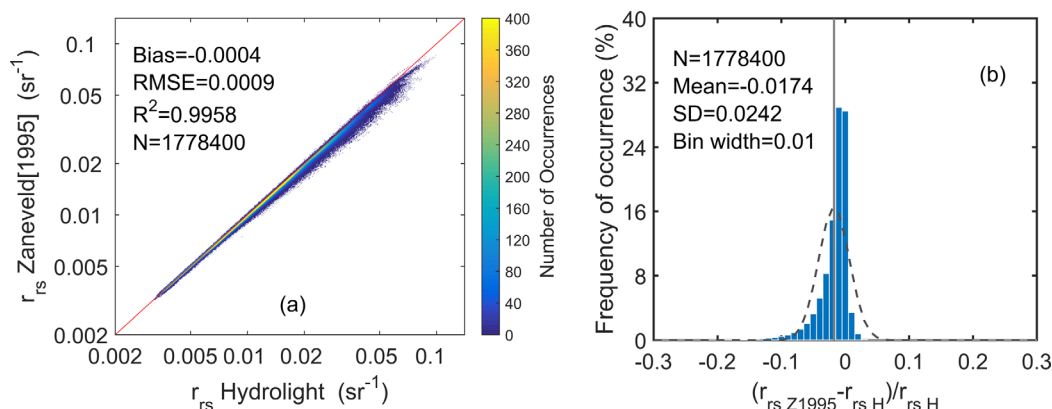
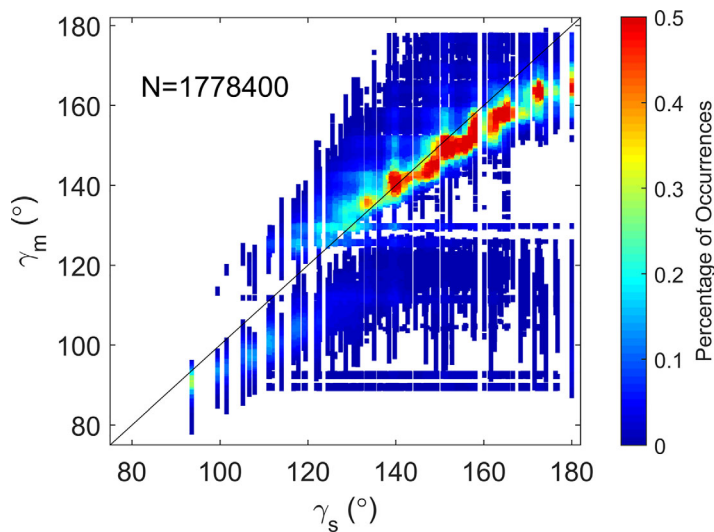


Figure 2. Comparison of  $r_{rs}$  between the Zaneveld (1995) model and the HydroLight simulation.



**Figure 3.** The comparison of single scattering angles ( $\gamma_s$ ) estimated for the sun-viewing geometries used in the simulation and the corresponding mean scattering angles ( $\gamma_m$ ) estimated using equation (9).

$$f_{bw}(\gamma_m) = f_{bw}(\gamma_s) - 0.2811(f_{bw}(\gamma_s) - 0.9407) + 0.0318, \quad (14)$$

$$\begin{aligned} f_{bp}(\gamma_m) &= f_{bp}(\gamma_s) - 0.3919(f_{bp}(\gamma_s) - 0.9314) + 0.0369, & \gamma_s \geq 120^\circ; \\ &= f_{bp}(\gamma_s) + 0.1540(f_{bp}(\gamma_s) - 0.9314) + 0.0369, & \gamma_s < 120^\circ. \end{aligned} \quad (15)$$

In equation (14),  $f_{bw}(\gamma_s)$  was calculated following equation (12) as the inverse of the  $\chi$  factor for pure seawater at angle  $\gamma_s$ , and therefore can be considered as known (Zhang et al., 2009) for a given sun-viewing geometry. Similarly,  $f_{bp}(\gamma_s)$  in equation (15) was calculated following equation (11) as the inverse of the  $\chi$  factor for particles at angle  $\gamma_s$ , which, however, is expected to vary with the size, shape and composition of the particles (Zhang et al., 2014a). Therefore,  $f_{bp}(\gamma_s)$  is generally unknown and needs to be provided.

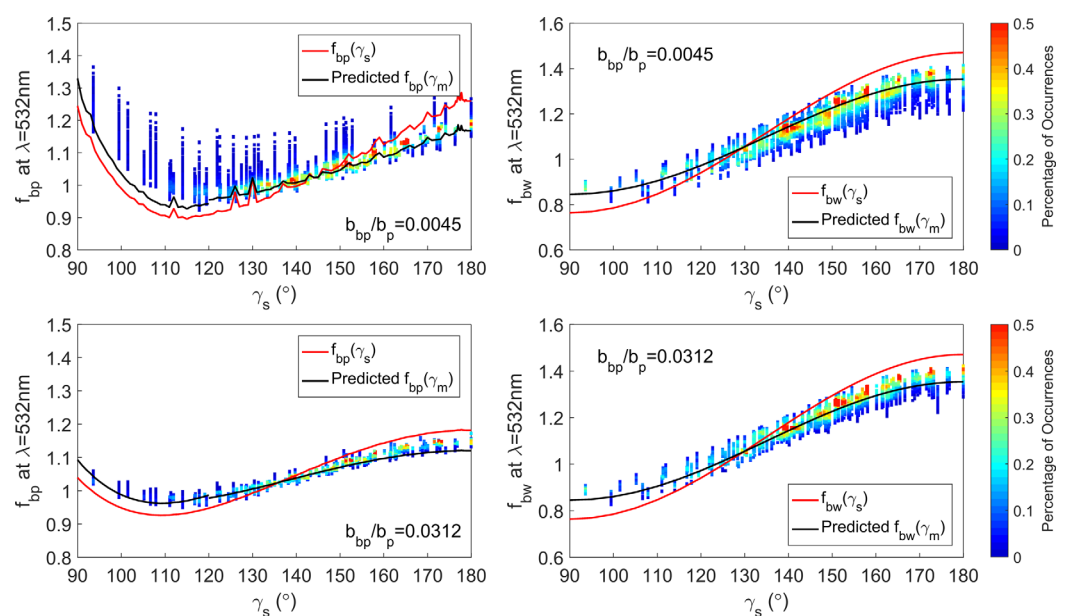
#### 4.2.2. Factor $g$

Factor  $g$  represents a combined effect due to the shape factor  $f_L$ ,  $K_{Lw}$  and the IOPs of  $a$ ,  $b_b$ , and  $b_f$  (equation (5)). Figure 5 shows the variation of  $1/g$  as a function of  $b_{bp}/(a + b_b)$  for different particle PFs (indicated by  $\beta_p(30^\circ)/\beta_p(120^\circ)$  values) and for two viewing geometries. Since  $f_L$  and  $b_f$  are mainly due to forward scattering, which in oceanic waters is expected to be dominated by the particle scattering, the  $g$  values increase with the forward steepness of particle PFs, measured

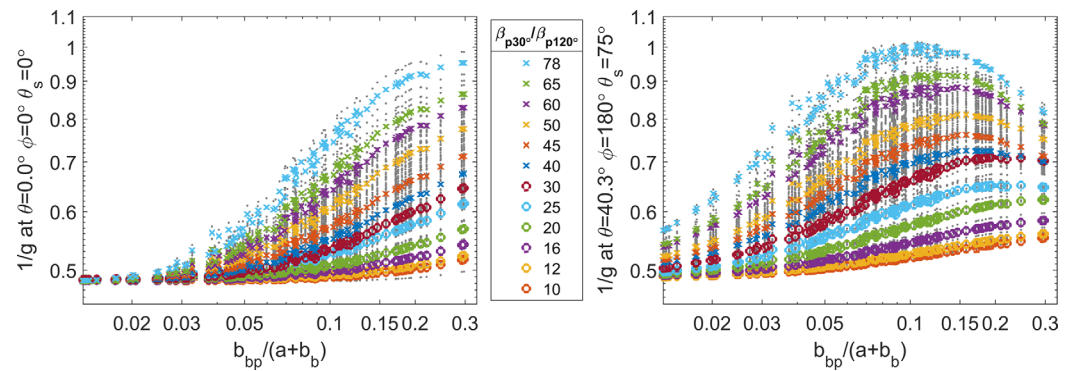
as  $\beta_p(30^\circ)/\beta_p(120^\circ)$ . We used  $\beta_p(30^\circ)/\beta_p(120^\circ)$  to represent the forward shape of particle PFs because both theoretical simulations and field measurements show that  $\beta_p$  exhibits minimal variability at  $120^\circ$  (Boss & Pegau, 2001; Dall'Olmo et al., 2009; Maffione & Dana, 1997; Oishi, 1990; Sullivan & Twardowski, 2009; Zhang et al., 2014a), and the PF shapes at angles  $< 15^\circ$  have a negligible influence on  $r_{rs}$  (Gordon, 1993). The  $g$  factor was parameterized as:

$$g = m_0 + m_1 \left( \frac{b_{bw}}{a + b_b} \right) + m_2 \left( \frac{b_{bp}}{a + b_b} \right) + m_3 \left( \frac{b_{bp}}{a + b_b} \right)^2. \quad (16)$$

A LUT was built for coefficients  $m_{0-3}$  as functions of sun-viewing geometries and values of  $\beta_p(30^\circ)/\beta_p(120^\circ)$ . A sample of the LUT is listed in Table 1.



**Figure 4.** Variations of  $f_{bp}(\gamma_m)$  and  $f_{bw}(\gamma_m)$  at 532 nm with  $\gamma_s$  simulated for two particle PFs with different  $b_{bp}/b_p$  values. Red lines are  $f_{bp}(\gamma_s)$  and  $f_{bw}(\gamma_s)$  and black lines are predicted  $f_{bp}(\gamma_m)$  and  $f_{bw}(\gamma_m)$  using equations (14) and (15), respectively.



**Figure 5.** Variation of  $1/g$  at 532 nm with  $b_{bp}/(a + b_b)$  and  $\beta_p(30^\circ)/\beta_p(120^\circ)$  at two sun-viewing geometries. The gray dots are the estimated  $1/g$  values from HydroLight and the colored symbols are the estimation from equation (16) for the 12  $\beta_p(30^\circ)/\beta_p(120^\circ)$  values shown in the legend.

#### 4.2.3. Downwelling Average Cosine $\bar{\mu}_d$

The average cosine has been used as a simple, but for most purposes, sufficient parameter describing the directional structures of the light field (Kirk, 1981; Mobley, 1994). It has been empirically related to the diffuse attenuation coefficient of downwelling irradiance,  $K_{Ed}$ , and the absorption coefficient (Kirk, 1981; Nahorniak et al., 2001). Figure 6 shows that  $\bar{\mu}_d$  generally increases with cosine of the solar zenith angles. In this study,  $\bar{\mu}_d$  was parameterized as:

$$\bar{\mu}_d = f_1 (1 + f_2 \cos \theta_s + f_3 \cos^2 \theta_s) \left( 1 + f_4 \frac{a}{K_{Ed}} \right), \quad (17)$$

where  $f_1$ ,  $f_2$ ,  $f_3$ , and  $f_4$  are 0.4779,  $-0.0641$ ,  $0.2660$ , and  $0.7164$ . We used the Lee et al. (2005) model for  $K_{Ed}$ :

$$K_{Ed} = (1 + k_1 \theta_s) a + k_2 (1 + k_3 e^{-k_4 a}) b_b, \quad (18)$$

where  $k_1$ ,  $k_2$ ,  $k_3$ , and  $k_4$  are 0.3771, 0.4986, 2.5345, and 0.0852.

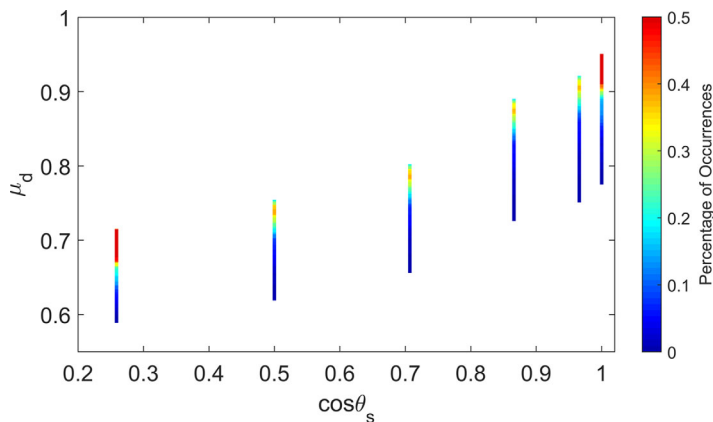
#### 4.3. Performance of Parameterizations for $r_{rs}$

For a given sun-viewing geometry and assuming the IOPs for pure seawater are known, the parameterized  $r_{rs}$  model requires the inputs of  $a$  and  $b_b$  as well as a measure of particle PF. Specifically,  $f_{bp}$  and  $b_{bp}$  are needed to simulate  $f_{br}$ ,  $a$ ,  $b_{bp}$ , and ratio of  $\beta_p(30^\circ)/\beta_p(120^\circ)$  for  $g$ ; and  $a$  and  $b_{bp}$  for  $\bar{\mu}_d$ . Figure 7 evaluates the performance of combined and individual parameterizations of  $f_{br}$ ,  $g$ , and  $\bar{\mu}_d$  for predicting the bidirectional  $r_{rs}$ . Overall, the parameterized model was able to predict  $r_{rs}$  with virtually no bias and an absolute uncertainty (as measured by root mean square error) of  $0.0010 \text{ sr}^{-1}$  (Figure 7a) or a relative uncertainty of 3.5% (as measured by root mean square relative error) (Figure 7b). The uncertainties due to parameterizing  $f_b$  and  $g$  were comparable, of about  $0.0007 \text{ sr}^{-1}$  (Figure 7c) or 2.2% (Figure 7d) and  $0.0007 \text{ sr}^{-1}$  (Figure 7e) or

**Table 1**  
The Values of the Coefficients  $m_{0-3}$  at Five Sun-Viewing Geometries and Two Ratios of  $\beta_p(30^\circ)/\beta_p(120^\circ)$

$\beta_{p30^\circ}/\beta_{p120^\circ}$	$\theta_s$ in air	$\theta$ in air	$\phi$	$m_0$	$m_1$	$m_2$	$m_3$
12	0°	0°	0°	2.0532	-0.1999	0.6349	-1.0137
	30°	40°	90°	1.9708	-0.6163	0.3815	-0.0593
	30°	40°	135°	1.9742	-1.0619	0.4090	0.8819
	60°	40°	90°	2.1515	-1.1224	0.3680	1.0685
	60°	40°	135°	2.1444	-1.6832	0.3510	2.2380
60	0°	0°	0°	2.1110	-6.8176	4.5799	12.8944
	30°	40°	90°	1.8932	-7.3510	6.1285	17.0894
	30°	40°	135°	1.8303	-8.0507	6.9631	19.7766
	60°	40°	90°	2.0265	-7.9635	6.4476	19.6354
	60°	40°	135°	1.8892	-8.6473	7.7785	22.8834





**Figure 6.** Variation of  $\bar{\mu}_d$  with solar zenith angles.

2.7% (Figure 7f), respectively. The smallest source of uncertainty was in modeling  $\bar{\mu}_d$ , which had an uncertainty of about  $0.0003 \text{ sr}^{-1}$  (Figure 7g) or 1.6% (Figure 7h).

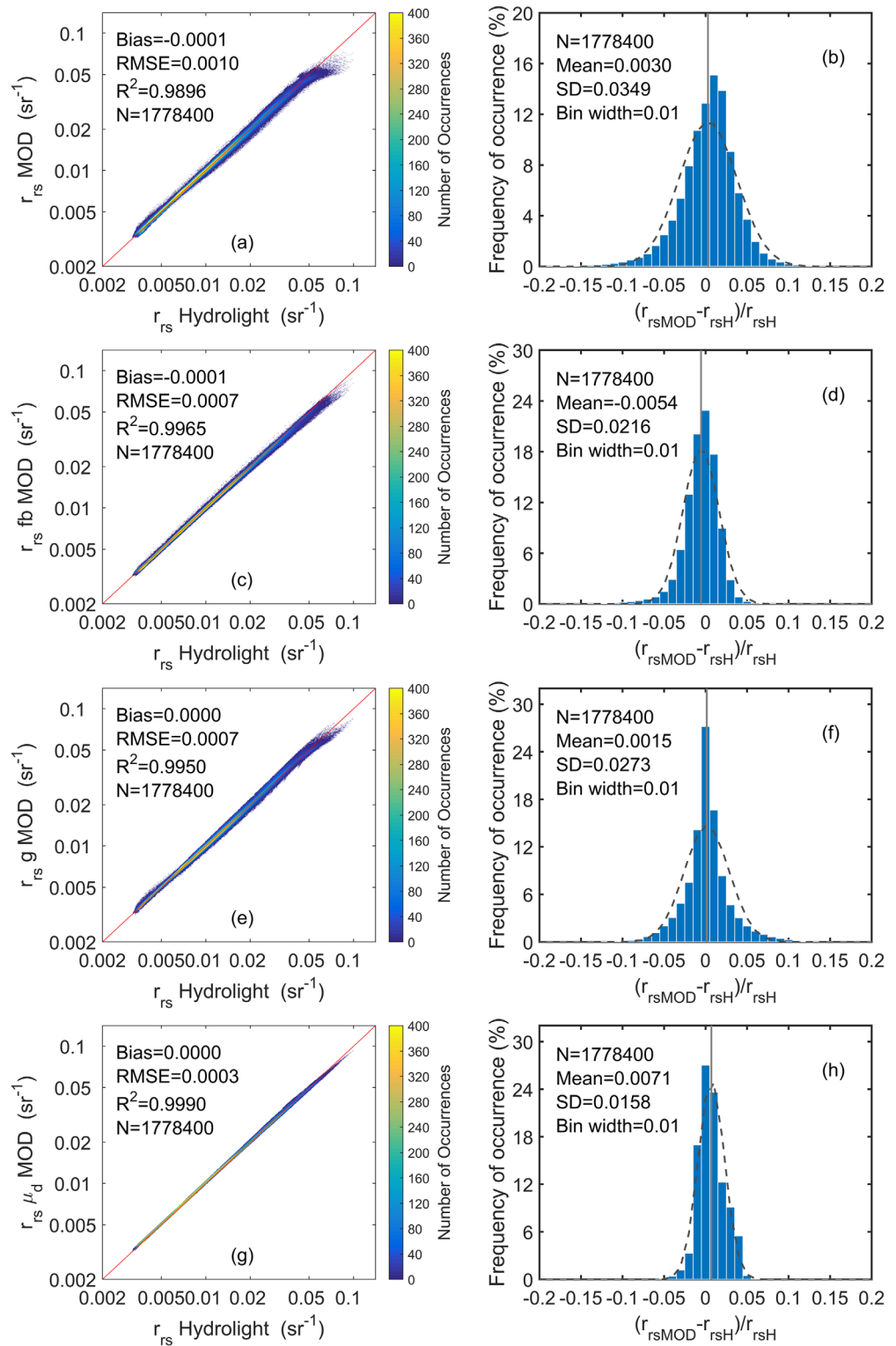
## 5. Discussion and Conclusions

On the basis of a theoretical derivation by Zaneveld (1982, 1995), the bidirectional  $r_{rs}$  was analyzed through equation (4), in which the BRDF is separated into three components of  $f_b$ ,  $g$ , and  $\bar{\mu}_d$ . These three components were parameterized using HydroLight simulations using 114 particle PFs measured in both coastal and oceanic waters. The comparison with simulated data shows that the developed model, with inputs of  $a$ ,  $b_b$ , and the particle PF, is able to predict  $r_{rs}$  at 532 nm with an absolute uncertainty of  $<0.001 \text{ sr}^{-1}$  (Figure 7a) and a relative uncertainty  $<4\%$  (Figure 7b).

As explained in Zaneveld (1995) and derivable from equation (4), if the VSF is isotropic in the backward angles ( $=\frac{b_b}{2\pi}$ ) and isotropic in the forward angles ( $=\frac{b_f}{2\pi}$ ) and the upwelling radiance field is also isotropic ( $=L_u(\theta_s, \theta, \phi)$ ),  $r_{rs} = \frac{1}{2\pi\bar{\mu}_d(1-D\cos\theta)} \frac{b_b}{a+b_b}$ , where  $D = \frac{K_{uw}}{a+b_b}$ . Under single scattering assumption,  $\bar{\mu}_d = \cos\theta_s$  and  $D\cos\theta_s \approx 1$  (varying between 0.8 and 1.2), the above  $r_{rs}$  equation approximates the quasi-single-scattering derivation for  $r_{rs}$ , i.e.,  $r_{rs} \approx \frac{1}{2\pi(\cos\theta_s - \cos\theta)} \frac{b_b}{a+b_b}$  (Gordon, 1973). The multiple scattering, the asymmetric upwelling light field, and the anisotropic scattering by oceanic particles in either forward or backward angles, would cause the deviation of  $r_{rs}$  from this isotropic, single scattering value by a factor  $= \frac{(\cos\theta_s - \cos\theta) f_b(\gamma_m)}{\bar{\mu}_d g}$ . The  $f_b(\gamma_m)$  represents the correction due to the anisotropic VSF shape in the backward angles. The values of  $f_b(\gamma_m)$  vary approximately between 0.9 and 1.5 (Figure 4), depending on the mean scattering angle ( $\gamma_m$ ) and the nature of particle assemblage (Zhang et al., 2017). Since the values of  $f_b$  are mostly  $>1$ , the effect of deviation of the actual shape of the VSF in the backward angles from the isotropic form of  $\frac{b_b}{2\pi}$  is to increase  $r_{rs}$ . Factor  $g$  represents the correction due to the anisotropic VSF shape in the forward angles and the anisotropic upwelling radiance field. The values of  $1/g$  vary approximately between 0.5 and 1.0 over the entire dataset (Figure 5) and between 0.5 and 0.75 for  $b_{bp}/(a+b_b) < 0.05$ , which represents typical oceanic waters. Overall, the values of  $1/g$  are  $<1$ , indicating the combined effect of anisotropic upwelling radiance field as well as the deviation of forward VSF shape from the isotropic form of  $\frac{b_f}{2\pi}$  is to lower  $r_{rs}$ .

Since models by Morel et al. (2002) and Lee et al. (2011) have been frequently used in describing the bidirectional remote sensing reflectance, we compare our model with these two in Table 2. Following equation (4), the BRDF factor in the Morel et al. (2002) model is effectively  $\frac{1}{2\pi\bar{\mu}_d} \frac{f_b(\gamma_m)}{g}$ . The effect of VSF shape was implicitly contained in chlorophyll concentration, which determines the mixing ratio of two PFs with  $b_{bp}/b_p$  ratios of 0.19 and 1.4%, respectively. Equation (10) shows that  $f_b$  is inherently contributed by two components,  $f_{bw}$  due to seawater and  $f_{bp}$  due to particles. Therefore, to more explicitly express the BRDF effect, a logical step is to separate the contributions by seawater and particles. This improvement was achieved by Lee et al. (2011). In their model (equation (3)), the BRDF factors due to seawater and particles are  $G_0^w + G_1^p \frac{b_{bw}}{a+b_b}$  and  $G_0^p + G_1^p \frac{b_{bp}}{a+b_b}$ , which are effectively  $\frac{1}{2\pi} \frac{f_{bw}(\gamma_m)}{\bar{\mu}_d g}$  and  $\frac{1}{2\pi} \frac{f_{bp}(\gamma_m)}{\bar{\mu}_d g}$ , respectively. Even though Lee et al. (2011) used varying VSF shapes in their simulations, their model parameters only have sun-viewing geometries as inputs; therefore their BRDF factor only includes a statistic average of the shape effect. Our approach more or less combined these two methods by (1) separating seawater and particles as in Lee et al. (2011) and (2) treating particle VSF shapes individually as in Morel et al. (2002). A further improvement in our approach is to explicitly express the VSF shape using the Zaneveld's theoretical formula. In addition, the VSF shapes used in our model are all based on field measurements, which exhibit a much greater variability in the VSF shape than the other two models have used (Xiong et al., 2017).

Despite its analytical derivation from the RTE, our model is more complex and requires inputs of the sun-viewing geometry, the IOPs of  $a$  and  $b_b$ , and the VSF shapes. The IOPs of pure seawater, including  $a_w$  and  $\beta_w$  are known quantities (Morel, 1974; Pope & Fry, 1997; Zhang et al., 2009), and particle IOPs of  $a_p$  and  $b_{bp}$  are retrievable from ocean color remote sensing (Lee et al., 2002; Werdell et al., 2013). This leaves out the particle VSF shapes. Zhang et al. (2017) recently showed that oceanic  $f_{bp}(90-180^\circ)$  can be very well



**Figure 7.** Comparison of  $r_{rs}$  between our parameterized Zaneveld model ( $r_{rsMOD}$ ) and the HydroLight simulation ( $r_{rsH}$ ). In (a) and (b), all the three factors in equation (4), i.e.,  $f_b$ ,  $g$ , and  $\bar{\mu}_d$ , were estimated using the parameterized models. In (c) and (d) only  $f_b$  was estimated using the parameterized model; (e) and (f) only  $g$  was estimated using the parameterized model; and (g) and (h) only  $\bar{\mu}_d$  was estimated using the parameterized model.

**Table 2**  
Summary of Three Bidirectional  $r_{rs}$  Models

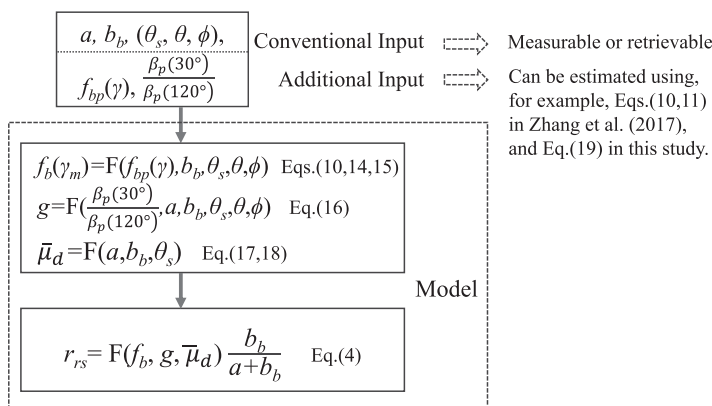
	Morel et al. (2002)	Lee et al. (2011)	This study
Input	Chl, ( $\theta_s, \theta, \phi$ )	$a, b_{bp}, (\theta_s, \theta, \phi)$	$a, b_{bp}, (\theta_s, \theta, \phi), f_{bp}, \beta_p(30^\circ)/\beta_p(120^\circ)$
Model details	$r_{rs} = \frac{f'}{Q} \frac{b_b}{a+b_b}$	$r_{rs} = \left( G_0^w + G_1^w \frac{b_{bw}}{a+b_b} \right) \frac{b_{bw}}{a+b_b} + \left( G_0^p + G_1^p \frac{b_{bp}}{a+b_b} \right) \frac{b_{bp}}{a+b_b}$	$r_{rs} = \frac{1}{2\pi\mu_d} \frac{f_{bw}}{g} \frac{b_{bw}}{a+b_b} + \frac{1}{2\pi\mu_d} \frac{f_{bp}}{g} \frac{b_{bp}}{a+b_b}$
Main features	(1) LUT of $f'$ and $Q$ with $\lambda$ , Chl and sun-viewing geometries; (2) operationally used in ocean color data processing	(1) Separating the effects due to seawater and particles; (2) LUT of spectrally independent $G_i^w$ and $G_i^p$ with sun-viewing geometries	(1) Separating the effects due to seawater and particles; (2) explicitly expressed as a function of backward VSF shapes of seawater, $f_{bw}$ and of particles $f_{bp}$
How are the VSFs treated in the model	(1) The particle VSFs are represented by a combination of two PFs with $b_{bp}/b_p$ of 0.19 and 1.4%; (2) the effect of VSF shapes is implicitly contained as a function of Chl	(1) The particle VSFs are represented by a combination of two PFs, with $b_{bp}/b_p$ of 1.0 and 1.8%; (2) the effect of VSF shapes is statistically averaged	(1) The particle VSFs are based on 114 measurements with $b_{bp}/b_p$ ranging 0.15–5.4%; (2) requires the VSF shapes as additional input

represented by a linear mixing of two end members, one representing the  $f_{bp}$  for particles of sizes much smaller than the wavelength and the other for particles of sizes much greater than the wavelength. Zhang et al. (2017) also showed that the mixing ratio can be predicted by  $b_{bp}$ . In addition, from the measured VSF data used in this study, we found that  $\beta_p(30^\circ)/\beta_p(120^\circ)$  can be related to  $\beta_p(90^\circ)/\beta_p(120^\circ)$ , which is the same as  $f_{bp}(90^\circ)/f_{bp}(120^\circ)$ :

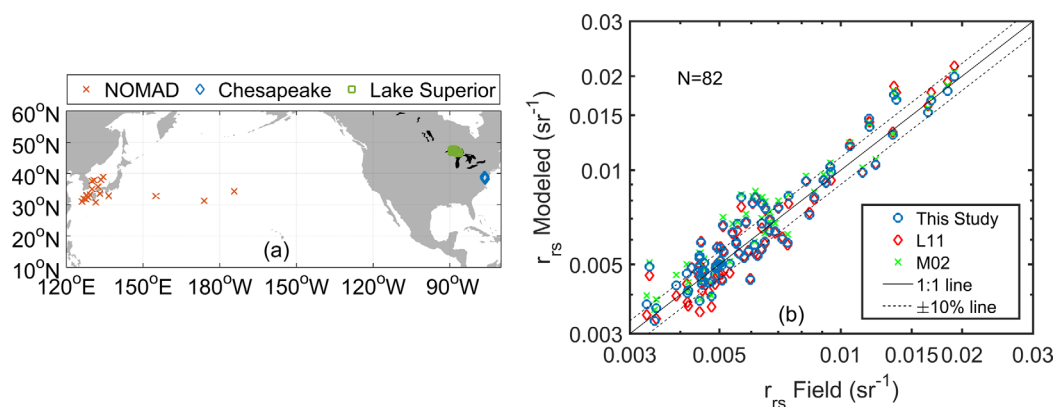
$$\frac{\beta_p(30^\circ)}{\beta_p(120^\circ)} = 63.70 \frac{f_{bp}(90^\circ)}{f_{bp}(120^\circ)} - 56.98. \quad (19)$$

Therefore, both  $f_b$  and  $\beta_p(30^\circ)/\beta_p(120^\circ)$  can be predicted from  $b_{bp}$  using the Zhang et al. (2017) two-component model. Such an implementation (Figure 8) is tested in Figure 9. From the NASA's bio-Optical Marine Algorithm Dataset (NOMAD) (Werdell & Bailey, 2005) and SeaWiFS Bio-optical Archive and Storage System (SeaBASS) (Werdell & Bailey, 2002; Werdell et al., 2003), we found a total of 82 sets of data with concurrent measurements of chlorophyll concentration,  $a$ ,  $b_{bp}$ , and nadir-viewed  $r_{rs}$  collected in three different waters: 25 in the coastal water of Japan and North Pacific Ocean, 30 in Chesapeake Bay, and 27 in Lake Superior (Figure 9a). With only  $a$  and  $b_b$  as inputs, our model (Figure 8) was able to predict  $r_{rs}$  with a root mean square error of  $0.0011 \text{ sr}^{-1}$  and root mean square relative error of 15% (Figure 9b). For comparison,

the absolute and relative errors are  $0.0012 \text{ sr}^{-1}$  and 15% for the Lee et al. (2011) model, and  $0.0013 \text{ sr}^{-1}$  and 19% for the Morel et al. (2002) model. Comparing to measured radiance distribution in various Case I and Case II waters, Gleason et al. (2012) found that both Morel et al. (2002) and Lee et al. (2011) models can simulate the BRDF effect, agreeing generally within  $\pm 20\%$  of the measurements. Relatively, however, they found the Morel et al. (2002) model, which implicitly includes variable particle VSF shapes as a function of chlorophyll concentration (Table 2), performs better in case I waters, indicating the importance of the VSF shapes in modeling the bidirectional  $r_{rs}$ . On the other hand, the Lee et al. (2011) model, which only represents an average shape effect (Table 2), performs better in Case II water at small azimuth angles and for chlorophyll concentration  $> 10 \text{ mg m}^{-3}$ , for which Gleason et al. (2012) found the VSF shape effect is not important. Our results (Figure 9), which are mostly for coastal and inland waters, also show that these two models were generally comparable



**Figure 8.** Flowchart of an example to apply the  $r_{rs}$  model developed in this study.



**Figure 9.** (a) Field data with simultaneous measurements of  $a$ ,  $b_b$ , and  $r_{rs}$ : 25 records from NOMAD in coastal and open North Pacific Ocean, 30 from SeaBASS in Chesapeake Bay, and 27 from SeaBASS in Lake Superior. (b) Measured  $r_{rs}$  are compared with predicted  $r_{rs}$  using our parameterized Zaneveld model, the Lee et al. (2011) model (L11), the Morel et al. (2002) model (M02).

(with Lee et al. slightly better than Morel et al.) in simulating the bidirectional  $r_{rs}$ . In addition, our model performed comparably same as (or marginally better than) these two models. However, since we could not find off-nadir viewed  $r_{rs}$  with simultaneously measured  $a$  and  $b_b$ , we only evaluated the BRDF effect due to the sun elevations.

Even though only the magnitude of the backward  $\beta$  (i.e.,  $b_b$ ) has been used in the current ocean color retrieval algorithms, the Zaneveld theoretical derivation shows that it is  $\beta$ —including both its magnitude and shape—that are actually measured in ocean color remote sensing. In fact, Jerlov (1976) pointed out that the variation of the diffuse reflectance with the sun elevation angle is a direct consequence of the shape of the VSF. Therefore, the shape of the backward  $\beta_p$  is contained in, and hence might be possibly estimated from, the measured  $r_{rs}$  (Gordon, 1989). Here, we demonstrated that a preliminary approach of estimating the backward shape of  $\beta_p$  and  $\beta_p(30^\circ)/\beta_p(120^\circ)$  using  $b_{bp}$  following Zhang et al. (2017) and equation (19). Thus, only two unknowns ( $a$  and  $b_b$ ) exist in the bidirectional  $r_{rs}$  model as sun-viewing geometries are usually known. The entire retrieval algorithm can be executed iteratively initiated by a first guess of  $a$  and  $b_b$  using the current ocean color retrieval algorithm (Figure 8).

We need to point out that the use of the Zhang et al. (2017) model and equation (19) to estimate the VSF shape is only one applicable example and can be improved. For example, we think the model developed in Zhang et al. (2017, equation (11)) for estimating the mixing ratio using  $b_{bp}$  is still preliminary. Nevertheless, we are encouraged by the results shown in Figure 9 that our model, despite its complexity, performed comparable to or slightly better than the currently used models by Morel et al. (2002) and Lee et al. (2011). As our knowledge of the VSFs of natural particles continues to improve, we expect that new and/or better algorithms will be developed to estimate the VSF shapes. This, in combination with our parameterized model based on Zaneveld's derivation, which explicitly accounts for the effect of VSF shapes on  $r_{rs}$ , offers great potential to further constrain the uncertainty in the ocean color studies. For example, a better BRDF correction is needed for the emerging geostationary ocean color remote sensing, which acquires images at a range of sun zenith angles versus the typical sun-synchronous polar orbiting ocean color sensors acquiring images at approximately fixed local sun zenith angle (Ruddick et al., 2014).

Our model is developed for 532 nm at which the VSFs were measured. Our current knowledge on the spectral variation of particle VSFs is limited (Chami et al., 2006b). Assuming the shape of VSFs is spectrally independent, we tested our model at other wavelengths. We found that only the  $g$  parameterization needs modification, whereas the  $f_b$  and  $\bar{\mu}_d$  parameterizations work well at other wavelengths. The reason that  $g$  needs spectral adjustment is because  $g$  depends on the geometrical structure of incident light field, which varies spectrally. This dependence is carried through by  $f_L$  and  $K_{Lu}$  (equation (5)). Downwelling average cosine  $\bar{\mu}_d$  also depends on the incident light field, but the dependence more or less cancels out as a ratio between  $E_{od}$  and  $E_d$ .

The effect of winds was not considered in our study. However, Morel and Gentili (1996) found that the impact of winds ( $0\text{--}10\text{ m s}^{-1}$ ) on the angular  $r_{rs}$  is almost undetectable with solar zenith angles  $<75^\circ$  and

in-air viewing zenith angles  $<42^\circ$ . A maximum variation of 10% can occur at chlorophyll concentration =  $3 \text{ mg m}^{-3}$  with the viewing zenith angle  $>42^\circ$  and sun zenith angle =  $75^\circ$ . For typical sun-viewing geometries applicable to ocean color, they concluded that the BRDF factor can be safely corrected without considering varying wind speeds. Also, only elastic scattering is included in the HydroLight simulations, and inelastic Raman scattering was not considered in this study. Morel et al. (2002) found that the Raman contribution can be neglected in waters with chlorophyll concentration  $>0.3 \text{ mg m}^{-3}$ , but the contribution can be significant in more oligotrophic waters. For example, Gordon (1999) showed that at  $\theta_s = 37^\circ$  Raman scattering could contribute 10–20% of water-leaving radiance at 490–600 nm in a water with chlorophyll concentration  $<0.1 \text{ mg m}^{-3}$ . However, since the angular distribution of Raman scattering is very similar in shape to the molecular scattering (Morel & Mueller, 2002), we expect that accounting for the Raman effect will probably only affect the seawater portion of our model and when particle content is low. A correction of Raman scattering to our  $r_{rs}$  model will be further investigated for oligotrophic waters.

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