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A Modified SIR Model Equivalent to a Generalized Logistic Model, with Standard Logistic Approximations

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A modified SIR model equivalent to a generalized logistic model, with standard logistic approximations

David E. Clark, Gavin Welch, Jordan S. Peck -- MMCRI/CORE/MaineHealth

- Biologically-based epidemic models (for COVID etc) often use systems of differential equations
- Population-based models often fit data to logistic or similar curves, and are more familiar to epidemiologists and engineers
- We intended to show that one modeling approach can be approximated by the other

Classic Susceptible-Infectious-Removed (SIR, Kermack/McKendrick 1927)

$$X'(t) = -\beta XY$$
$$Y'(t) = \beta XY - \gamma Y$$
$$Z'(t) = \gamma Y$$

Modified SIR (note X+Y+Z = 1) $X'(t) = -\beta XY / (X+Y)$ $Y'(t) = \beta XY / (X+Y) - \gamma Y$ $Z'(t) = \gamma Y$ -- Modified SIR solved exactly in terms of Generalized Logistic functions, e.g.,

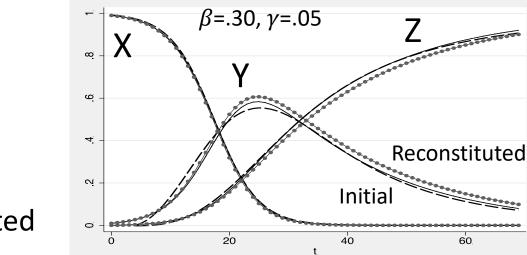
$$\begin{split} \mathsf{X}(\mathsf{t}) &= \lambda \frac{1}{(1 + e^{(t-\mu)/\sigma})^{\beta\sigma}} \quad , \\ &\sigma = 1/(\beta - \gamma), \, \mu = \sigma \log(x_0/y_0), \, \lambda = \left(\frac{x_0 + y_0}{x_0}\right)^{\beta\sigma} \end{split}$$

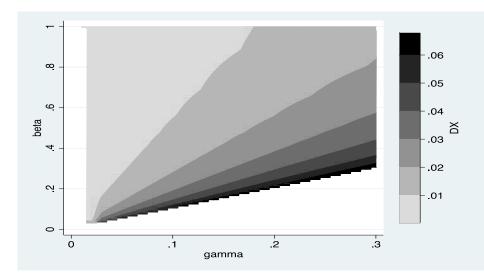
-- Generalized Logistic functions approximated with Standard Logistic (or Log-Logistic) functions by equating quantiles.

-- Evaluated error of approximation (Kolmogorov Distance) for different values of β and γ .

-- Devised algebraic or numeric methods to estimate β and γ from population statistics.

medR**x**iv July 2020, clarkd@mmc.org





Bio-based and pop-based methods interchangeable