# Measurement of prompt $\mathrm{J} / \psi$ and beauty hadron production cross sections at mid-rapidity in pp collisions at $\sqrt{s}=7 \mathrm{TeV}$ 


#### Abstract

The ALICE experiment at the LHC has studied $\mathrm{J} / \psi$ production at midrapidity in pp collisions at $\sqrt{s}=7 \mathrm{TeV}$ through its electron pair decay on a data sample corresponding to an integrated luminosity $L_{\text {int }}=5.6 \mathrm{nb}^{-1}$. The fraction of $\mathrm{J} / \psi$ from the decay of long-lived beauty hadrons was determined for $\mathrm{J} / \psi$ candidates with transverse momentum $p_{\mathrm{t}}>1.3 \mathrm{GeV} / c$ and rapidity $|y|<0.9$. The cross section for prompt $\mathrm{J} / \psi$ mesons, i.e. directly produced $\mathrm{J} / \psi$ and prompt decays of heavier charmonium states such as the $\psi(2 \mathrm{~S})$ and $\chi_{\mathrm{c}}$ resonances, is $\sigma_{\text {prompt J} / \psi}\left(p_{\mathrm{t}}>1.3 \mathrm{GeV} / c,|y|<0.9\right)=8.3 \pm 0.8$ (stat.) $\pm$ 1.1 (syst.) ${ }_{-1.4}^{+1.5}$ (syst. pol.) $\mu \mathrm{b}$. The cross section for the production of b-hadrons decaying to $\mathrm{J} / \psi$ with $p_{\mathrm{t}}>1.3 \mathrm{GeV} / c$ and $|y|<0.9$ is $\sigma_{J / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}\left(p_{\mathrm{t}}>1.3 \mathrm{GeV} / c,|y|<0.9\right)=1.46$ $\pm 0.38$ (stat.) ${ }_{-0.32}^{+0.26}$ (syst.) $\mu \mathrm{b}$. The results are compared to QCD model predictions. The shape of the $p_{\mathrm{t}}$ and $y$ distributions of b-quarks predicted by perturbative QCD model calculations are used to extrapolate the measured cross section to derive the b $\overline{\mathrm{b}}$ pair total cross section and $\mathrm{d} \sigma / \mathrm{d} y$ at mid-rapidity.


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## 1 Introduction

The production of both charmonium mesons and beauty-flavoured hadrons, referred to as b-hadrons or $h_{B}$ in this paper, in hadronic interactions represents a challenging testing ground for models based on Quantum ChromoDynamics (QCD).

The mechanisms of $\mathrm{J} / \psi$ production operate at the boundary of the perturbative and non-perturbative regimes of QCD. At hadron colliders, $\mathrm{J} / \psi$ production was extensively studied at the Tevatron [1-4] and RHIC [5]. Measurements in the new energy domain of the Large Hadron Collider (LHC) can contribute to a deeper understanding of the physics of the hadroproduction processes. The first LHC experimental results on the $\mathrm{J} / \psi$ transverse momentum $\left(p_{\mathrm{t}}\right)$ differential cross sections [6-10] are well described by various theoretical approaches [11-14]. Among those results, the ALICE Collaboration reported the measurement of the rapidity $(y)$ and transverse momentum dependence of inclusive $\mathrm{J} / \psi$ production in proton-proton ( pp ) collisions at $\sqrt{s}=7 \mathrm{TeV}$ [9]. The inclusive $\mathrm{J} / \psi$ yield is composed of three contributions: prompt $\mathrm{J} / \psi$ produced directly in the protonproton collision, prompt $\mathrm{J} / \psi$ produced indirectly (via the decay of heavier charmonium states such as $\chi_{\mathrm{c}}$ and $\psi(2 \mathrm{~S})$ ), and non-prompt $\mathrm{J} / \psi$ from the decay of b-hadrons. Other LHC experiments have separated the prompt and non-prompt $\mathrm{J} / \psi$ component $[6-8,10$. However, at mid-rapidity, only the high- $p_{\mathrm{t}}$ part of the differential $\mathrm{d} \sigma_{\mathrm{J} / \psi} / \mathrm{d} p_{\mathrm{t}}$ distribution was measured $\left(p_{\mathrm{t}}>6.5 \mathrm{GeV} / c\right)$, i.e. a small fraction (few percent) of the $p_{\mathrm{t}}$-integrated cross section.

The measurement of the production of b-hadrons in pp collisions at the LHC provides a way to test, in a new energy domain, calculations of QCD processes based on the factorization approach. In this scheme, the cross sections are computed as a convolution of the
parton distribution functions of the incoming protons, the partonic hard scattering cross sections, and the fragmentation functions. Measurements of cross sections for beauty quark production in high-energy hadronic interactions have been done in the past at p $\overline{\mathrm{p}}$ colliders at center-of-mass energies from $630 \mathrm{GeV}[15,16]$ to $1.96 \mathrm{TeV}[2,17-19]$ and in p-nucleus collisions with beam energies from 800 to 920 GeV [20]. The LHC experiments have reported measurements of b-hadron production in pp collisions at $\sqrt{s}=7 \mathrm{TeV}$ by studying either exclusive decays of B mesons [21-23] or semi-inclusive decays of b-hadrons [6-8, 10, 24, 25]. At mid-rapidity, the measurements are available only for $p_{\mathrm{t}}$ of the b-hadrons larger than $\approx 5 \mathrm{GeV} / c$, whereas the low $p_{\mathrm{t}}$ region of the differential b-hadron cross sections, where the bulk of the b-hadrons is produced, has not been studied.

In this paper, the fraction of $\mathrm{J} / \psi$ from the decay of b -hadrons in pp collisions at $\sqrt{s}=7 \mathrm{TeV}$ for $\mathrm{J} / \psi$ in the ranges $1.3<p_{\mathrm{t}}<10 \mathrm{GeV} / c$ and $|y|<0.9$ is determined. This information is combined with the previous inclusive $\mathrm{J} / \psi$ cross section measurement reported by ALICE [9]. Prompt J/ $\psi$ and b-hadron cross sections are thus determined at mid-rapidity down to the lowest $p_{\mathrm{t}}$ reach at the LHC energy.

## 2 Experiment and data analysis

The ALICE experiment [26] consists of a central barrel, covering the pseudorapidity region $|\eta|<0.9$, and a muon spectrometer with $-4<\eta<-2.5$ coverage. The results presented in this paper were obtained with the central barrel tracking detectors, in particular the Inner Tracking System (ITS) [26, 27] and the Time Projection Chamber (TPC) [28]. The ITS, which consists of two innermost Silicon Pixel Detector (SPD), two Silicon Drift Detector (SDD), and two outer Silicon Strip Detector (SSD) layers, provides up to six space points (hits) for each track. The TPC is a large cylindrical drift detector with an active volume that extends over the ranges $85<r<247 \mathrm{~cm}$ and $-250<z<250 \mathrm{~cm}$ in the radial and longitudinal (beam) directions, respectively. The TPC provides up to 159 space points per track and charged particle identification via specific energy loss ( $\mathrm{d} E / \mathrm{d} x$ ) measurement.

The event sample, corresponding to $3.5 \times 10^{8}$ minimum bias events and an integrated luminosity $L_{\text {int }}=5.6 \mathrm{nb}^{-1}$, event selection and track quality cuts used for the measurement of the inclusive $\mathrm{J} / \psi$ production at mid-rapidity [9] were also adopted in this analysis. In particular, an event with a reconstructed vertex position $z_{\mathrm{v}}$ was accepted if $\left|z_{\mathrm{v}}\right|<10 \mathrm{~cm}$. The tracks were required to have a minimum $p_{\mathrm{t}}$ of $1 \mathrm{GeV} / c$, a minimum number of 70 TPC space points, a $\chi^{2}$ per space point of the momentum fit lower than 4 , and to point back to the interaction vertex within 1 cm in the transverse plane. At least one hit in either of the two layers of the SPD was required. For tracks passing this selection, the average number of hits in the six ITS layers was 4.5-4.7, depending on the data taking period. The electron identification was based on the specific energy loss in the TPC: a $\pm 3 \sigma$ inclusion cut around the Bethe-Bloch fit for electrons and $\pm 3.5 \sigma( \pm 3 \sigma)$ exclusion cut for pions (protons) were employed [9]. Finally, electron or positron candidates compatible, together with an opposite charge candidate, with being products of $\gamma$ conversions (the invariant mass of the pair being smaller than $100 \mathrm{MeV} / c^{2}$ ) were removed, in order to reduce the combinatorial background. It was verified, using a Monte Carlo simulation, that this procedure does
not affect the $\mathrm{J} / \psi$ signal. In this analysis, opposite-sign (OS) electron pairs were divided in three "types": type "first-first" $(F F)$ corresponds to the case when both the electron and the positron have hits in the first pixel layer, type "first-second" $(F S)$ are those pairs where one of them has a hit in the first layer and the other does not, while for the type "second-second" $(S S)$ neither of them has a hit in the first layer. The candidates of type $S S$, which correspond to about $10 \%$ of the total, were discarded due to the worse spatial resolution of the associated decay vertex.

A detailed description of the track and vertex reconstruction procedures can be found in [29]. The primary vertex was determined via an analytic $\chi^{2}$ minimization method in which tracks are approximated as straight lines after propagation to their common point of closest approach. The vertex fit was constrained in the transverse plane using the information on the position and spread of the luminous region. The latter was determined from the distribution of primary vertices reconstructed over the run. Typically, the transverse position of the vertex has a resolution that ranges from $40 \mu \mathrm{~m}$ in low-multiplicity events with less than 10 charged particles per unit of rapidity to about $10 \mu \mathrm{~m}$ in events with a multiplicity of about 40 . For each $\mathrm{J} / \psi$ candidate a specific primary vertex was also calculated by excluding the $\mathrm{J} / \psi$ decay tracks, in order to estimate a systematic uncertainty related to the evaluation of the primary vertex in the case of events with non-prompt $\mathrm{J} / \psi$, as discussed in section 3 . The decay vertex of the $\mathrm{J} / \psi$ candidate was computed with the same analytic $\chi^{2}$ minimization as for the primary vertex, using the two decay tracks only and without the constraint of the luminous region.

The measurement of the fraction of the $\mathrm{J} / \psi$ yield coming from b-hadron decays, $f_{\mathrm{B}}$, relies on the discrimination of $\mathrm{J} / \psi$ mesons produced at a distance from the pp collision vertex. The signed projection of the $\mathrm{J} / \psi$ flight distance onto its transverse momentum vector, $\vec{p}_{\mathrm{t}}^{J / \psi}$, was constructed according to the formula

$$
\begin{equation*}
L_{x y}=\vec{L} \cdot \vec{p}_{\mathrm{t}}^{\mathrm{J} / \psi} / p_{\mathrm{t}}^{\mathrm{J} / \psi}, \tag{2.1}
\end{equation*}
$$

where $\vec{L}$ is the vector from the primary vertex to the $\mathrm{J} / \psi$ decay vertex. The variable $x$, referred to as "pseudoproper decay length" in the following, was introduced to separate prompt $\mathrm{J} / \psi$ from those produced by the decay of b-hadrons, ${ }^{1}$

$$
\begin{equation*}
x=\frac{c \cdot L_{x y} \cdot m_{\mathrm{J} / \psi}}{p_{\mathrm{t}}^{\mathrm{J} / \psi}} \tag{2.2}
\end{equation*}
$$

where $m_{\mathrm{J} / \psi}$ is the (world average) $\mathrm{J} / \psi$ mass [30].
For events with very low $\mathrm{J} / \psi p_{\mathrm{t}}$, the non-negligible amount of $\mathrm{J} / \psi$ with large opening angle between its flight direction and that of the b-hadron impairs the separation ability. Monte Carlo simulation shows that the detector resolution allows the determination of the fraction of $\mathrm{J} / \psi$ from the decay of b -hadrons for events with $\mathrm{J} / \psi p_{\mathrm{t}}$ greater than $1.3 \mathrm{GeV} / c$.

An unbinned 2-dimensional likelihood fit was used to determine the ratio of the nonprompt to inclusive $\mathrm{J} / \psi$ production and the ratio of $\mathrm{J} / \psi$ signal candidates (the sum of

[^0]both prompt and non-prompt components) to the total number of candidates, $f_{\text {Sig }}$, by maximizing the quantity
\[

$$
\begin{equation*}
\ln L=\sum_{i=1}^{N} \ln F\left(x, m_{\mathrm{e}^{+} \mathrm{e}^{-}}\right) \tag{2.3}
\end{equation*}
$$

\]

where $m_{\mathrm{e}^{+} \mathrm{e}^{-}}$is the invariant mass of the electron pair and $N$ is the total number of candidates in the range $2.4<m_{\mathrm{e}^{+} \mathrm{e}^{-}}<4.0 \mathrm{GeV} / c^{2}$. The expression for $F\left(x, m_{\mathrm{e}^{+} \mathrm{e}^{-}}\right)$is

$$
\begin{equation*}
F\left(x, m_{\mathrm{e}^{+} \mathrm{e}^{-}}\right)=f_{\mathrm{Sig}} \cdot F_{\mathrm{Sig}}(x) \cdot M_{\mathrm{Sig}}\left(m_{\mathrm{e}^{+} \mathrm{e}^{-}}\right)+\left(1-f_{\mathrm{Sig}}\right) \cdot F_{\mathrm{Bkg}}(x) \cdot M_{\mathrm{Bkg}}\left(m_{\mathrm{e}^{+} \mathrm{e}^{-}}\right) \tag{2.4}
\end{equation*}
$$

where $F_{\text {Sig }}(x)$ and $F_{\text {Bkg }}(x)$ are Probability Density Functions (PDFs) describing the pseudoproper decay length distribution for signal and background candidates, respectively. $M_{\mathrm{Sig}}\left(m_{\mathrm{e}^{+} \mathrm{e}^{-}}\right)$and $M_{\mathrm{Bkg}}\left(m_{\mathrm{e}^{+} \mathrm{e}^{-}}\right)$are the PDFs describing the dielectron invariant mass distributions for the signal and background, respectively. A Crystal Ball function [31] is used for the former and an exponential function for the latter. The signal PDF is given by

$$
\begin{equation*}
F_{\mathrm{Sig}}(x)=f_{\mathrm{B}}^{\prime} \cdot F_{\mathrm{B}}(x)+\left(1-f_{\mathrm{B}}^{\prime}\right) \cdot F_{\text {prompt }}(x), \tag{2.5}
\end{equation*}
$$

where $F_{\text {prompt }}(x)$ and $F_{\mathrm{B}}(x)$ are the PDFs for prompt and non-prompt $\mathrm{J} / \psi$, respectively, and $f_{\mathrm{B}}^{\prime}$ is the fraction of reconstructed non-prompt $\mathrm{J} / \psi$,

$$
\begin{equation*}
f_{\mathrm{B}}^{\prime}=\frac{N_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}}{N_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}+N_{\text {prompt J } / \psi}} \tag{2.6}
\end{equation*}
$$

which can differ (see below) from $f_{\mathrm{B}}$ due to different acceptance and reconstruction efficiency of prompt and non-prompt $\mathrm{J} / \psi$. The distribution of non-prompt $\mathrm{J} / \psi$ is the convolution of the $x$ distribution of $\mathrm{J} / \psi$ from b-hadron events, $\chi_{\mathrm{B}}(x)$, and the experimental resolution on $x, R_{\text {type }}(x)$, which depends on the type of candidate ( $F F$ or $F S$ ),

$$
\begin{equation*}
F_{\mathrm{B}}(x)=\chi_{\mathrm{B}}\left(x^{\prime}\right) \otimes R_{\mathrm{type}}\left(x^{\prime}-x\right) \tag{2.7}
\end{equation*}
$$

Promptly produced $\mathrm{J} / \psi$ mesons decay at the primary vertex, and their pseudoproper decay length distribution is thus simply described by $R_{\text {type }}(x)$ :

$$
\begin{equation*}
F_{\text {prompt }}(x)=\delta\left(x^{\prime}\right) \otimes R_{\text {type }}\left(x^{\prime}-x\right)=R_{\text {type }}(x) \tag{2.8}
\end{equation*}
$$

The resolution function is described by the sum of two Gaussians and a power law function reflected about $x=0$ and was determined, as a function of the $p_{\mathrm{t}}$ of the $\mathrm{J} / \psi$, with a Monte Carlo simulation study. In this simulation, which utilizes GEANT3 [32] and incorporates a detailed description of the detector material, geometry, and response, prompt $\mathrm{J} / \psi$ were generated with a $p_{\mathrm{t}}$ distribution extrapolated from CDF measurements [1] and a $y$ distribution parameterization taken from Color Evaporation Model (CEM) calculations [33]. These $\mathrm{J} / \psi$ were individually injected into proton-proton collisions simulated using the PYTHIA 6.4.21 event generator [34, 35], and reconstructed as for $\mathrm{J} / \psi$ candidates in data. A data-driven method (discussed in section 3) was also developed and used to estimate the systematic uncertainty related to this procedure. The Monte Carlo $x$ distribution of $\mathrm{J} / \psi$ from the decay of b-hadrons produced in proton-proton collisions simulated
using the PYTHIA 6.4.21 event generator [34, 35] with Perugia-0 tuning [36] was taken as the template for the $x$ distribution of b-hadron events in data, $\chi_{\mathrm{B}}(x)$. A second template, used to estimate the systematic uncertainty, was obtained by decaying the simulated bhadrons using the EvtGen package [37], and describing the final state radiation ("internal" bremsstrahlung) using PHOTOS [38, 39].

For the background $x$ distribution, $F_{\text {Bkg }}(x)$, the functional form employed by CDF [1] was used,

$$
\begin{align*}
F_{\mathrm{Bkg}}(x)= & \left(1-f_{+}-f_{-}-f_{\mathrm{sym}}\right) R_{\mathrm{type}}(x) \\
& +\left[\frac{f_{+}}{\lambda_{+}} e^{-x^{\prime} / \lambda_{+}} \theta\left(x^{\prime}\right)+\frac{f_{-}}{\lambda_{-}} e^{x^{\prime} / \lambda_{-}} \theta\left(-x^{\prime}\right)+\frac{f_{\text {sym }}}{2 \lambda_{\text {sym }}} e^{-\left|x^{\prime}\right| / \lambda_{\text {sym }}}\right] \otimes R_{\mathrm{type}}\left(x^{\prime}-x\right), \tag{2.9}
\end{align*}
$$

where $\theta(x)$ is the step function, $f_{+}, f_{-}$and $f_{\text {sym }}$ are the fractions of three components with positive, negative and symmetric decay length exponential distributions, respectively. The effective parameters $\lambda_{+}, \lambda_{-}$and $\lambda_{\text {sym }}$, and optionally also the corresponding fractions, were determined, prior to the likelihood fit maximization, with a fit to the $x$ distribution in the sidebands of the dielectron invariant mass distribution, defined as the regions 1.8-2.6 and $3.2-5.0 \mathrm{GeV} / c^{2}$. The introduction of these components is needed because the background consists also of random combinations of electrons from semi-leptonic decays of charm and beauty hadrons, which tend to produce positive $x$ values, as well as of other secondary or mis-reconstructed tracks which contribute both to positive and negative $x$ values. The first term in eq. (2.9), proportional to $R_{\text {type }}(x)$, describes the residual combinatorics of primary particles.

In figure 1 the distributions of the invariant mass and the pseudoproper decay length, the latter restricted to candidates with $2.92<m_{\mathrm{e}^{+} \mathrm{e}^{-}}<3.16 \mathrm{GeV} / c^{2}$, for opposite-sign electron pairs with $p_{\mathrm{t}}>1.3 \mathrm{GeV} / c$ are shown with superimposed projections of the maximum likelihood fit result.

The value of the fit parameter $f_{\mathrm{B}}^{\prime}$ provides the fraction of non-prompt $\mathrm{J} / \psi$ which were reconstructed. In principle prompt and non-prompt $\mathrm{J} / \psi$ can have different acceptance times efficiency $(A \times \epsilon)$ values. This can happen because of two effects: (i) the $A \times \epsilon$ depends on the $p_{\mathrm{t}}$ of the $\mathrm{J} / \psi$ and prompt and non-prompt $\mathrm{J} / \psi$ have different $p_{\mathrm{t}}$ distributions within the considered $p_{\mathrm{t}}$ range; (ii) at a given $p_{\mathrm{t}}$, prompt and non-prompt $\mathrm{J} / \psi$ can have different polarization and, therefore, a different acceptance. The fraction of non-prompt $\mathrm{J} / \psi$, corrected for these effects, was obtained as

$$
\begin{equation*}
f_{\mathrm{B}}=\left(1+\frac{1-f_{\mathrm{B}}^{\prime}}{f_{\mathrm{B}}^{\prime}} \cdot \frac{\langle A \times \epsilon\rangle_{\mathrm{B}}}{\langle A \times \epsilon\rangle_{\text {prompt }}}\right)^{-1}, \tag{2.10}
\end{equation*}
$$

where $\langle A \times \epsilon\rangle_{\mathrm{B}}$ and $\langle A \times \epsilon\rangle_{\text {prompt }}$ are the average acceptance times efficiency values, in the considered $p_{\mathrm{t}}$ range and for the assumed polarization state, of non-prompt and prompt $\mathrm{J} / \psi$, respectively. The acceptance times efficiency $(A \times \epsilon)$ varies very smoothly with $p_{\mathrm{t}}$ and, for unpolarized $\mathrm{J} / \psi$ in the $p_{\mathrm{t}}$ range from 1.3 to $10 \mathrm{GeV} / c$, has a minimum of $8 \%$ at $2 \mathrm{GeV} / c$ and a broad maximum of $12 \%$ at $7 \mathrm{GeV} / c[9]$. As a consequence, the $\langle A \times \epsilon\rangle$ values of prompt and non-prompt $\mathrm{J} / \psi$ differ by about $3 \%$ only in this integrated $p_{\mathrm{t}}$ range.


Figure 1. Invariant mass (left panel) and pseudoproper decay length (right panel) distributions of opposite sign electron pairs for $\left|y_{\mathrm{J} / \psi}\right|<0.9$ and $p_{\mathrm{t}}^{\mathrm{J} / \psi}>1.3 \mathrm{GeV} / c$ with superimposed projections of the maximum likelihood fit. The latter distribution is limited to the $\mathrm{J} / \psi$ candidates under the mass peak, i.e. for $2.92<m_{\mathrm{e}^{+} \mathrm{e}^{-}}<3.16 \mathrm{GeV} / c^{2}$, for display purposes only. The $\chi^{2}$ values of these projections are reported for both distributions.

The central values of the resulting cross sections are quoted assuming both prompt and non-prompt $\mathrm{J} / \psi$ to be unpolarized and the variations due to different assumptions are estimated as a separate systematic uncertainty. The polarization of $\mathrm{J} / \psi$ from b-hadron decays is expected to be much smaller than for prompt $\mathrm{J} / \psi$ due to the averaging effect caused by the admixture of various exclusive $\mathrm{B} \rightarrow \mathrm{J} / \psi+\mathrm{X}$ decay channels. In fact, the sizeable polarization, which is observed when the polarization axis refers to the B-meson direction [40], is strongly smeared when calculated with respect to the direction of the daughter $\mathrm{J} / \psi[7]$, as indeed observed by CDF [2]. Therefore, these variations will be calculated in the two cases of prompt $\mathrm{J} / \psi$ with fully transverse $(\lambda=1)$ or longitudinal $(\lambda=-1)$ polarization, in the Collins-Soper (CS) and helicity (HE) reference frames, ${ }^{2}$ the non-prompt component being left unpolarized.

Despite the small $\mathrm{J} / \psi$ candidate yield, amounting to about 400 counts, the data sample could be divided into four $p_{\mathrm{t}}$ bins (1.3-3, 3-5, 5-7 and $7-10 \mathrm{GeV} / c$ ), and the fraction $f_{\mathrm{B}}$ was evaluated in each of them with the same technique. At low $p_{\mathrm{t}}$ the statistics is higher, but the resolution is worse and the signal over background, $S / B$, is smaller (i.e. $f_{\text {Sig }}$ is smaller). At high $p_{\mathrm{t}}$ the statistics is smaller, but the resolution improves and the background becomes negligible. In figure 2 the distributions of the invariant mass and of the pseudoproper decay length are shown in different $p_{\mathrm{t}}$ bins with superimposed results of the fits.

## 3 Systematic uncertainties

The different contributions to the systematic uncertainties affecting the measurement of the fraction of $\mathrm{J} / \psi$ from the decay of b-hadrons are discussed in the following, referring to the integrated $p_{\mathrm{t}}$ range, and summarized in table 1 .

[^1]

Figure 2. Invariant mass (left panels) and pseudoproper decay length (right panels) distributions of opposite sign electron pairs in different $p_{\mathrm{t}}$ bins with superimposed projections of the maximum likelihood fit. The $\chi^{2}$ values of these projections are also reported for all distributions.

- Resolution function. The resolution function was determined from a Monte Carlo simulation, as discussed above. The fits were repeated by artificially modifying the resolution function, according to the formula

$$
R_{\mathrm{type}}^{\prime}(x)=\frac{1}{1+\delta} R_{\mathrm{type}}\left(\frac{x}{1+\delta}\right)
$$

where $\delta$ is a constant representing the desired relative variation of the RMS of the resolution function. Studies on track distance of closest approach to the primary interaction vertex in the bending plane $\left(d_{0}\right)$ show that the $p_{\mathrm{t}}$ dependence of the $d_{0}$ resolution as measured in the data is reproduced within about $10 \%$ by the Monte Carlo simulation [29], but with a systematically worse resolution in data. For the $x$ variable a similar direct comparison to data is not straightforward, however, the residual discrepancy is not expected to be larger than that observed for $d_{0}$.

The variations of $f_{\mathrm{B}}$ obtained in the likelihood fit results by varying $\delta$ from $-5 \%$ to $+10 \%$ are $+8 \%$ and $-15 \%$, respectively, and they were assumed as the systematic uncertainty due to this contribution.
An alternative, data-driven, approach was also considered. The $x$ distribution of the signal, composed of prompt and non-prompt $\mathrm{J} / \psi$, was obtained by subtracting the $x$ distribution of the background, measured in the sidebands of the invariant mass distribution. This distribution is then fitted by fixing the ratio of prompt to nonprompt $\mathrm{J} / \psi$ to that obtained from the likelihood fit and leaving free the parameters of the resolution function. The RMS of the fitted resolution function is found to be $8 \%$ larger than the one determined using the Monte Carlo simulation, hence within the range of variation assumed for $\delta$.

- Pseudoproper decay length distribution of background. The shape of the combinatorial background was determined from a fit to the $x$ distribution of candidates in the sidebands of the invariant mass distribution. By varying the fit parameters within their errors an envelope of distributions was obtained, whose extremes were used in the likelihood fit in place of the most probable distribution. The variations in the result of the fit were determined and adopted as systematic uncertainties. Also, it was verified that the $x$ distribution obtained for like-sign (LS) candidates, with invariant mass in the range from 2.92 to $3.16 \mathrm{GeV} / c^{2}$ complementary to the sidebands, is best fitted by a distribution which falls within the envelope of the OS distributions. Finally, the likelihood fit was repeated by relaxing, one at a time, the parameters of the functional form (eq. (2.9)) and it was found that the values of $f_{\mathrm{B}}$ were within the estimated uncertainties. The estimated systematic uncertainty is $6 \%$.
- Pseudoproper decay length distribution of b-hadrons. The fits were also done using as template for the $x$ distribution of b-hadrons, $\chi_{\mathrm{B}}(x)$, that obtained by the EvtGen package [37], and describing the final state radiation using PHOTOS [38, 39]. The central values of the fits differ by a few percent at most and the resulting systematic uncertainty is $3 \%$.
- Invariant mass distributions. The likelihood method was used in this analysis to fit simultaneously the invariant mass distribution, which is sensitive to the ratio of signal to all candidates $\left(f_{\text {Sig }}\right)$, and the $x$ distribution, which determines the ratio of non-prompt to signal candidates $\left(f_{\mathrm{B}}\right)$. The statistical uncertainties on these quantities were therefore evaluated together, including the effects of correlations. However, the choice of the function describing the invariant mass distribution, as well as the procedure, can introduce systematic uncertainties in the evaluation of $f_{\mathrm{B}}$. Different approaches were therefore considered: (i) the functional form describing the background was changed into an exponential plus a constant and the fit repeated; (ii) the background was described using the LS distribution and the signal was obtained by subtracting the LS from the OS distributions. The signal and the background shapes were determined with $\chi^{2}$ minimizations. Both functional forms, exponential and exponential plus a constant, were considered for the background. The likelihood
fit was then performed again to determine $f_{\mathrm{B}}$ (and $f_{\mathrm{Sig}}$ ); (iii) the same procedure as in (ii) was used, but additionally $f_{\text {Sig }}$ was estimated a priori using a bin counting method [9] instead of the integrals of the best fit functions. The maximum likelihood fit was performed with $f_{\mathrm{Sig}}$ fixed to this new value; (iv) and (v) the same procedures as in (ii) and (iii) were used but with the background described by a track rotation (TR) method [9].
Half of the difference between the maximum and minimum $f_{\mathrm{B}}$ values obtained with the different methods was assumed as systematic uncertainty. It amounts to about $6 \%$.
- Primary vertex. The effect of excluding the decay tracks of the $\mathrm{J} / \psi$ candidate in the computation of the primary vertex was studied with the Monte Carlo simulation: on the one hand, for the prompt $\mathrm{J} / \psi$, the $x$ resolution function is degraded, due to the fact that two prompt tracks are not used in the computation of the vertex, which is thus determined with less accuracy. The effect on the resolution is $p_{\mathrm{t}}$ dependent, with the RMS of the $x$ distribution of prompt $\mathrm{J} / \psi$ increasing by $15 \%$ at low $p_{\mathrm{t}}$ and by $7 \%$ at high $p_{\mathrm{t}}$. On the other hand, for non-prompt $\mathrm{J} / \psi$ a bias on the $x$ determination should be reduced. The bias consists in an average shift of the primary vertex towards the secondary decay vertex of the b-hadrons, which is reflected in a shift of the mean of the $x$ distribution by about $4 \mu \mathrm{~m}$ for the $p_{\mathrm{t}}$-integrated distribution. However, the shift is $p_{\mathrm{t}}$ and "type" dependent. In some cases the bias is observed in the opposite direction and is enhanced by removing the decay tracks of the candidate. This can happen since b-quarks are always produced in pairs. If a charged track from the fragmentation of the second b-quark also enters the acceptance, it can pull the primary vertex position towards the opposite direction. In the end, therefore, the primary vertex was computed without removing the decay tracks of the candidates. To estimate the systematic uncertainty, the analysis was repeated by either (i) removing the decay tracks in the computation of the primary vertex and using the corresponding worse resolution function in the fit or (ii) keeping those tracks and introducing an ad hoc shift in the distribution of the $\chi_{\mathrm{B}}(x)$, equal to that observed in the Monte Carlo simulation for non-prompt $\mathrm{J} / \psi$. The contribution to the systematic uncertainty is about $5 \%$.
- MC $p_{\mathrm{t}}$ spectrum. The ratio $\frac{\langle A \times \epsilon\rangle_{\mathrm{B}}}{\left\langle A \times \epsilon \epsilon_{\text {prompt }}\right.}$ in eq. (2.10) was computed using MC simulations: prompt $\mathrm{J} / \psi$ were generated with the $p_{\mathrm{t}}$ distribution extrapolated from CDF measurements [1] and the $y$ distribution parameterized from CEM [33]; b-hadrons were generated using the PYTHIA 6.4.21 [34, 35] event generator with Perugia-0 tuning [36]. By varying the average $p_{\mathrm{t}}$ of the $\mathrm{J} / \psi$ distributions within a factor 2 , a $1.5 \%$ variation in the acceptance was obtained both for prompt and non-prompt $\mathrm{J} / \psi$. Such a small value is a consequence of the weak $p_{\mathrm{t}}$ dependence of the acceptance. For the measurement integrated over $p_{\mathrm{t}}\left(p_{\mathrm{t}}>1.3 \mathrm{GeV} / c\right)$, the $A \times \epsilon$ values of prompt and non-prompt $\mathrm{J} / \psi$ differ by about $3 \%$ only. The uncertainty due to Monte Carlo $p_{\mathrm{t}}$ distributions is thus estimated to be $1 \%$. When estimating $f_{\mathrm{B}}$ in $p_{\mathrm{t}}$ bins, this uncertainty is negligible.

| Source | Systematic uncertainty (\%) |  |  |
| :--- | :---: | :---: | :---: |
|  | $p_{\mathrm{t}}$ integrated | lowest $p_{\mathrm{t}}$ bin | highest $p_{\mathrm{t}}$ bin |
| Resolution function | $+8,-15$ | $+15,-25$ | $+2,-3$ |
| $x$ distribution of background | $\pm 6$ | $\pm 13$ | $\pm 1$ |
| $x$ distribution of b-hadrons | $\pm 3$ | $\pm 3$ | $\pm 2$ |
| $m_{\mathrm{e}^{+} \mathrm{e}^{-} \text {distributions }}^{\text {Primary vertex }}$ | $\pm 6$ | $\pm 11$ | $\pm 4$ |
| MC $p_{\mathrm{t}}$ spectrum | $+4,-5$ | $\pm 4$ | $+4,-8$ |
| Total | $\pm 1$ | 0 | 0 |
| Polarization (prompt J/ $\psi)$ | $+12,-18$ | $+23,-30$ | $+6,-9$ |
| CS $(\lambda=-1)$ |  |  |  |
| CS $(\lambda=+1)$ | -13 | +22 | +5 |
| HE $(\lambda=-1)$ | +17 | -19 | -3 |
| HE $(\lambda=+1)$ | -14 | +19 | +11 |

Table 1. Systematic uncertainties (in percent) on the measurement of the fraction of $\mathrm{J} / \psi$ from the decay of b-hadrons, $f_{\mathrm{B}}$. The variations of $f_{\mathrm{B}}$ are also reported, with respect to the case of both prompt and non-prompt $\mathrm{J} / \psi$ unpolarized, when assuming the prompt component with given polarization.

- Polarization. The variations of $f_{\mathrm{B}}$ obtained assuming different polarization scenarios for the prompt component only were evaluated, as discussed in section 2 , and are reported in table 1. The maximum variations are quoted as separate errors.

The study of systematic uncertainties was repeated as a function of $p_{\mathrm{t}}$. In table 1 the results are summarized for the integrated $p_{\mathrm{t}}$ range $\left(p_{\mathrm{t}}>1.3 \mathrm{GeV} / c\right)$ and for the lowest $(1.3-3 \mathrm{GeV} / c)$ and highest $(7-10 \mathrm{GeV} / c) p_{\mathrm{t}}$ bins. All systematic uncertainties increase with decreasing $p_{\mathrm{t}}$, except the one related to the primary vertex measurement.

## 4 Results

### 4.1 Fraction of $\mathrm{J} / \psi$ from the decay of b-hadrons

The fraction of $\mathrm{J} / \psi$ from the decay of b-hadrons in the experimentally accessible kinematic range, $p_{\mathrm{t}}>1.3 \mathrm{GeV} / c$ and $|y|<0.9$, which is referred to as "measured region" in the following, is

$$
f_{\mathrm{B}}=0.149 \pm 0.037(\text { stat. })_{-0.027}^{+0.018}(\text { syst. })_{-0.021\left(\lambda_{\mathrm{HE}}=-1\right)}^{+0.025\left(\lambda_{\mathrm{HE}}=1\right)} \text { (syst.pol.). }
$$

The fractions measured in the $p_{\mathrm{t}}$ bins are reported in table 2 and shown in figure 3 . In the figure, the data symbols are placed at the average value of the $p_{\mathrm{t}}$ distribution of each bin. The average was computed using the above mentioned Monte Carlo distributions: the one based on the CDF extrapolation [33] and that using PYTHIA [34, 35] with Perugia-0 tuning [36] for prompt and non-prompt $\mathrm{J} / \psi$, respectively, weighted by the measured $f_{\mathrm{B}}$. In figure 3 the results of the ATLAS [8] and CMS [10] experiments measured at mid-rapidity


Figure 3. The fraction of $\mathrm{J} / \psi$ from the decay of b-hadrons as a function of $p_{\mathrm{t}}$ of $\mathrm{J} / \psi$ compared with results from ATLAS [8] and CMS [10] in pp collisions at $\sqrt{s}=7 \mathrm{TeV}$.
for the same colliding system are also shown. The ALICE results extend the mid-rapidity measurements down to low $p_{\mathrm{t}}$.

### 4.2 Prompt J/ $\psi$ production

By combining the measurement of the inclusive $\mathrm{J} / \psi$ cross section, which was determined as described in [9], and the $f_{\mathrm{B}}$ value, the prompt $\mathrm{J} / \psi$ cross section was obtained:

$$
\begin{equation*}
\sigma_{\text {prompt } \mathrm{J} / \psi}=\left(1-f_{\mathrm{B}}\right) \cdot \sigma_{J / \psi} . \tag{4.1}
\end{equation*}
$$

The numerical values of the inclusive $\mathrm{J} / \psi$ cross section in the $p_{\mathrm{t}}$ ranges used for this analysis are summarized in table 2. In the measured region the integrated cross section is $\sigma_{\text {prompt } \mathrm{J} / \psi}\left(|y|<0.9, p_{\mathrm{t}}>1.3 \mathrm{GeV} / c\right)=8.3 \pm 0.8$ (stat.) $\pm 1.1(\text { syst. })_{-1.4\left(\lambda_{\mathrm{HE}}=-1\right)}^{+1.5\left(\lambda_{\mathrm{HE}}=1\right)} \mu \mathrm{b}$. The systematic uncertainties related to the unknown polarization are quoted for the reference frame where they are the largest.

The differential distribution $\frac{\mathrm{d}^{2} \sigma_{\text {prompt }} / \psi / \psi}{\mathrm{d} p_{\mathrm{t}} d y}$ is shown as a function of $p_{\mathrm{t}}$ in figure 4 and $\frac{\mathrm{d} \sigma_{\text {prompt }} \mathrm{J} / \psi}{\mathrm{d} y}$ is plotted in figure 5. The numerical values are summarized in table 2. In figure 4 the statistical and all systematic errors are added in quadrature for better visibility, while in figure 5 the error bar shows the quadratic sum of statistical and systematic errors, except for the $3.5 \%$ systematic uncertainty on luminosity and the $1 \%$ on the branching ratio $(B R)$, which are added in quadrature and shown as box. The results shown in figures 4 and 5 assume unpolarized J/ $\psi$ production. Systematic uncertainties due to the unknown $\mathrm{J} / \psi$ polarization are not shown. Results by the CMS $[6,10]$, LHCb [7] and ATLAS [8] Collaborations are shown for comparison. Also for these data the uncertainties due to luminosity and to the $B R$ are shown separately (boxes) in figure 5 , while the error

| $\begin{aligned} & p_{\mathrm{t}} \\ & (\mathrm{GeV} / c) \\ & \hline \end{aligned}$ | $\begin{aligned} & \left\langle p_{\mathrm{t}}\right\rangle \\ & (\mathrm{GeV} / c) \\ & \hline \end{aligned}$ | Measured quantity | Systematic uncertainties |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Correl. | Non-correl. | Extrap. | Polariz., CS | Polariz., HE |
| $f_{\mathrm{B}}(\%)$ |  |  |  |  |  |  |  |
| 1.3-3.0 | 2.02 | $9.2 \pm 7.4$ | 0 | +2.1, -2.8 | 0 | +2.0, -1.7 | +1.7, -1.5 |
| 3.0-5.0 | 3.65 | $13.8 \pm 3.8$ | 0 | +1.5, -2.1 | 0 | +1.3, -1.0 | +2.1, -3.0 |
| 5.0-7.0 | 5.75 | $23.2 \pm 7.2$ | 0 | +1.6, -2.1 | 0 | +0.2, -0.2 | +3.5, -2.6 |
| 7.0-10.0 | 8.06 | $30.7 \pm 13.8$ | 0 | +1.8, -2.8 | 0 | +1.5, -0.9 | +3.4, -2.5 |
| $p_{\text {t }}>1.3$ | 2.85 | $14.9 \pm 3.7$ | 0 | +1.8, -2.7 | 0 | +1.9, -1.5 | +2.5, -2.1 |
| $p_{\text {t }}>0$ | 2.41 | $14.3 \pm 3.6$ | 0 | +1.8, -2.6 | +0.2, -0.5 | +2.4, -1.6 | +2.5, -1.9 |
| $\mathrm{d}^{2} \sigma_{\mathrm{J} / \psi} / \mathrm{d} y \mathrm{~d} p_{\mathrm{t}} \quad\left(\frac{\mathrm{nb}}{\mathrm{GeV} / \mathrm{c}}\right)$ |  |  |  |  |  |  |  |
| 1.3-3.0 | 2.02 | $1780 \pm 210$ | $\pm 65$ | $\pm 250$ | 0 | +400, -320 | +330, -280 |
| 3.0-5.0 | 3.65 | $715 \pm 125$ | $\pm 25$ | $\pm 90$ | 0 | +50, -60 | +170, -90 |
| 5.0-7.0 | 5.74 | $405 \pm 70$ | $\pm 15$ | $\pm 45$ | 0 | +1, -3 | +50, -50 |
| 7.0-10.0 | 8.06 | $60 \pm 25$ | $\pm 2$ | $\pm 12$ | 0 | +2, -3 | +5, -6 |
| $\mathrm{d}^{2} \sigma_{\text {prompt } \mathrm{J} / \psi / \mathrm{d} y \mathrm{~d} p_{\mathrm{t}}} \quad\left(\frac{\mathrm{nb}}{\mathrm{GeV} / c}\right)$ |  |  |  |  |  |  |  |
| 1.3-3.0 | 2.02 | $1600 \pm 230$ | $\pm 60$ | $\pm 230$ | 0 | +400, -320 | +330, -280 |
| 3.0-5.0 | 3.65 | $620 \pm 110$ | $\pm 20$ | $\pm 80$ | 0 | +50, -60 | +170, -90 |
| 5.0-7.0 | 5.74 | $310 \pm 60$ | $\pm 10$ | $\pm 35$ | 0 | +1, -3 | +50, -50 |
| 7.0-10.0 | 8.03 | $40 \pm 18$ | $\pm 1$ | $\pm 8$ | 0 | +2, -3 | +5, -6 |
| $\sigma_{\text {prompt J/ } \psi\left(\left\|y_{\mathrm{J} / \psi}\right\|<0.9\right) \quad(\mu \mathrm{b})}$ |  |  |  |  |  |  |  |
| $p_{\mathrm{t}}>1.3$ | 2.81 | $8.3 \pm 0.8$ |  | $\pm 1.1$ | 0 | +1.0, -1.2 | +1.5, -1.4 |
| $p_{\mathrm{t}}>0$ | 2.37 | $10.6 \pm 1.1$ |  | $\pm 1.6$ | +0.06, -0.02 | +1.6, -1.7 | +1.9, -1.8 |
| $\sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}\left(\left\|y_{\mathrm{J} / \psi}\right\|<0.9\right) \quad(\mu \mathrm{b})$ |  |  |  |  |  |  |  |
| $p_{\text {t }}>1.3$ | 3.07 | $1.46 \pm 0.38$ |  | 26, -0.32 | 0 | 0 | 0 |
| $p_{\mathrm{t}}>0$ | 2.62 | $1.77 \pm 0.46$ |  | 32, -0.39 | +0.02, -0.06 | 0 | 0 |
| $\mathrm{d} \sigma_{\mathrm{b} \overline{\mathrm{~b}}} /\left.\mathrm{d} y\right\|_{\|y\|<0.9}(\mu \mathrm{~b})$ |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
| $\sigma_{\mathrm{b} \overline{\mathrm{b}}} \quad(\mu \mathrm{b})$ |  |  |  |  |  |  |  |
|  |  | $282 \pm 74$ |  | 58, -68 | +8, -7 | 0 | 0 |

Table 2. The fraction of $J / \psi$ from the decay of b-hadrons and cross sections. Some of the contributions to the systematic uncertainty do not depend on $p_{\mathrm{t}}$, thus affecting only the overall normalization, and they are separately quoted (correl.). The contributions which depend on $p_{\mathrm{t}}$, even when they are correlated bin by bin, were included among the non-correlated systematic errors. The values of $\left\langle p_{\mathrm{t}}\right\rangle$ were computed using Monte Carlo distributions (see text for details).
bars represent the statistical and the other sources of systematic uncertainties added in quadrature.

The ALICE $\frac{\mathrm{d}^{2} \sigma_{\text {prompt }} / \psi}{\mathrm{d} y \mathrm{~d} p_{\mathrm{t}}}$ measurement at mid-rapidity (left panel of figure 4 ) is complementary to the data of CMS, available for $|y|<0.9$ and $p_{\mathrm{t}}>8 \mathrm{GeV} / c$, and ATLAS, which covers the region $|y|<0.75$ and $p_{\mathrm{t}}>7 \mathrm{GeV} / c$. In the right panel of figure 4 , the ALICE results are compared to next-to-leading order (NLO) non-relativistic QCD (NRQCD) theoretical calculations by M. Butenschön and B.A. Kniehl [12] and Y.-Q. Ma et al. [13]. Both calculations include color-singlet (CS), color-octet (CO), and heavier charmonium feed-down contributions. For one of the two models (M. Butenschön and B.A. Kniehl) the
partial results with only the CS contribution are also shown. The comparison suggests that the CO processes are indispensable to describe the data also at low $p_{\mathrm{t}}$. The results are also compared to the model of V.A. Saleev et al. [14], which includes the contribution of partonic sub-processes involving t-channel parton exchanges and provides a prediction down to $p_{\mathrm{t}}=0$.

The ALICE result for $\frac{\mathrm{d} \sigma_{\text {prompt }} \mathrm{J} / \psi}{\mathrm{d} y}$ (figure 5), which equals

$$
\frac{\mathrm{d} \sigma_{\text {prompt } \mathrm{J} / \psi}}{\mathrm{d} y}=5.89 \pm 0.60(\text { stat. })_{-0.90}^{+0.88}(\text { syst. })_{-0.01}^{+0.03}(\text { extr. })_{-0.99\left(\lambda_{\mathrm{HE}}=-1\right)}^{+1.01\left(\lambda_{\mathrm{HE}}=1\right)} \mu \mathrm{b},
$$

was obtained by subtracting from the inclusive $\mathrm{J} / \psi$ cross section measured for $p_{\mathrm{t}}>0$ that of $\mathrm{J} / \psi$ coming from b-hadron decays. The latter was determined, as discussed in the next section, by extrapolating the cross section from the measured region down to $p_{\mathrm{t}}>0$ using an implementation of pQCD calculations at fixed order with next-to leading$\log$ resummation (FONLL) [41]. The extrapolation uncertainty is negligible with respect to the other systematic uncertainties. In figure 5 the CMS and LHCb results for the rapidity bins where the $p_{\mathrm{t}}$ coverage extends down to zero were selected. For CMS, the value for $1.6<|y|<2.4$ was obtained by integrating the published $\mathrm{d}^{2} \sigma_{\text {prompt } \mathrm{J} / \psi} / \mathrm{d} p_{\mathrm{t}} \mathrm{d} y$ data [6]. The ALICE data point at mid-rapidity complements the other LHC measurements of prompt $\mathrm{J} / \psi$ production cross section as a function of rapidity. It is worth noting that the uncertainties of the data sets of the three experiments are uncorrelated, except for that (negligible) of the $B R$, while within the same experiment most of the systematic uncertainties are correlated. The prediction of the model by V.A. Saleev et al. [14] at mid-rapidity provides $\frac{\mathrm{d} \sigma_{\text {prompt } J / \psi}}{\mathrm{d} y}=7.8_{-4.5}^{+9.7} \mu \mathrm{~b}$, which, within the large band of theoretical uncertainties, is in agreement with our measurement.

### 4.3 Beauty hadron production

The production cross section of $\mathrm{J} / \psi$ from b-hadron decays was obtained as $\sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}=$ $f_{\mathrm{B}} \cdot \sigma_{\mathrm{J} / \psi}$. In the measured region it is

$$
\left.\sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}\left(p_{\mathrm{t}}>1.3 \mathrm{GeV} / c,|y|<0.9\right)=1.46 \pm 0.38 \text { (stat. }\right)_{-0.32}^{+0.26} \text { (syst.) } \mu \mathrm{b} .
$$

This measurement can be compared to theoretical calculations based on the factorization approach. In particular, the prediction of the FONLL [41], which describes well the beauty production at Tevatron energy, provides [42] $1.33_{-0.48}^{+0.59} \mu \mathrm{~b}$, in good agreement with the measurement. For this calculation CTEQ6.6 parton distribution functions [43] were used and the theoretical uncertainty was obtained by varying the factorization and renormalization scales, $\mu_{\mathrm{F}}$ and $\mu_{\mathrm{R}}$, independently in the ranges $0.5<\mu_{\mathrm{F}} / m_{\mathrm{t}}<2,0.5<\mu_{\mathrm{R}} / m_{\mathrm{t}}<2$, with the constraint $0.5<\mu_{\mathrm{F}} / \mu_{\mathrm{R}}<2$, where $m_{\mathrm{t}}=\sqrt{p_{\mathrm{t}}^{2}+m_{\mathrm{b}}^{2}}$. The beauty quark mass was varied within $4.5<m_{\mathrm{b}}<5.0 \mathrm{GeV} / c^{2}$.

The same FONLL calculations were used to extrapolate the cross section of non-prompt $\mathrm{J} / \psi$ down to $p_{\mathrm{t}}$ equal to zero. The extrapolation factor, which is equal to $1.212_{-0.038}^{+0.016}$, was computed as the ratio of the cross section for $p_{\mathrm{t}}^{\mathrm{J} / \psi}>0$ and $\left|y_{\mathrm{J} / \psi}\right|<0.9$ to that in the measured region $\left(p_{\mathrm{t}}^{\mathrm{J} / \psi}>1.3 \mathrm{GeV} / c\right.$ and $\left.\left|y_{\mathrm{J} / \psi}\right|<0.9\right)$. Using the PYTHIA event generator


Figure 4. Double differential production cross section of prompt $J / \psi$ as a function of $p_{\mathrm{t}}$ compared to results from ATLAS [8] and CMS [10] at mid-rapidity (left panel) and to theoretical calculations [12-14] (right panel). The error bars represent the quadratic sum of the statistical and systematic uncertainties.
with Perugia-0 tuning instead of FONLL provides an extrapolation factor of 1.156. The measured cross section corresponds thus to about $80 \%$ of the $p_{\mathrm{t}}$-integrated cross section at mid-rapidity. Dividing by the rapidity range $\Delta y=1.8$ one obtains

$$
\frac{\left.\left.\mathrm{d} \sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}^{\mathrm{d} y}=0.98 \pm 0.26 \text { (stat. }\right)_{-0.22}^{+0.18} \text { (syst. }\right)_{-0.03}^{+0.01} \text { (extr.) } \mu \mathrm{b} \text {. } . \text {. } 10 .}{}
$$

In figure 6 this measurement is plotted together with the LHCb [7] and CMS [6] data at forward rapidity. For CMS the values for $1.2<|y|<1.6$ and $1.6<|y|<2.4$ were obtained by integrating the published $\mathrm{d}^{2} \sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}} / \mathrm{d} p_{\mathrm{t}} \mathrm{d} y$ data [6]; the value for $1.2<|y|<1.6$ was also extrapolated from $p_{\mathrm{t}}^{\min }=2.0 \mathrm{GeV} / c$ to $p_{\mathrm{t}}=0$, with the approach based on the FONLL calculations as previously described. The extrapolation uncertainties are shown in figure 6 as the slashed areas. The central FONLL prediction and its uncertainty band are also shown. A good agreement between data and theory is observed.

A similar procedure was used to derive the b $\overline{\mathrm{b}}$ quark-pair production cross section

$$
\begin{equation*}
\frac{\mathrm{d} \sigma_{\mathrm{b} \overline{\mathrm{~b}}}}{\mathrm{~d} y}=\frac{\mathrm{d} \sigma_{\mathrm{b}}^{\text {theory }}}{\mathrm{d} y} \times \frac{\sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}\left(p_{\mathrm{t}}^{\mathrm{J} / \psi}>1.3 \mathrm{GeV} / c,\left|y_{\mathrm{J} / \psi}\right|<0.9\right)}{\sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}^{\text {the }}\left(p_{\mathrm{t}}^{\mathrm{J} / \psi}>1.3 \mathrm{GeV} / c,\left|y_{\mathrm{J} / \psi}\right|<0.9\right)}, \tag{4.2}
\end{equation*}
$$

where the average branching fraction of inclusive b-hadron decays to $\mathrm{J} / \psi$ measured at LEP [44-46], $B R\left(\mathrm{~h}_{\mathrm{b}} \rightarrow \mathrm{J} / \psi+\mathrm{X}\right)=(1.16 \pm 0.10) \%$, was used in the computation of $\sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}^{\text {theory }}$. The extrapolation with the FONLL calculations provides

$$
\left.\frac{\mathrm{d} \sigma_{\mathrm{b}} \overline{\mathrm{~b}}}{\mathrm{~d} y}=43 \pm 11 \text { (stat. }\right)_{-10}^{+9}(\text { syst. })_{-1.5}^{+0.6}(\text { extr. }) \mu \mathrm{b}
$$



Figure 5. Prompt $\mathrm{J} / \psi$ production cross section as a function of rapidity. The error bars represent the quadratic sum of the statistical and systematic errors, while the systematic uncertainties on luminosity and branching ratio are shown as boxes around the data points. The symbols are plotted at the center of each bin. The CMS value was obtained by integrating the published $\mathrm{d}^{2} \sigma_{\text {prompt } \mathrm{J} / \psi} / \mathrm{d} p_{\mathrm{t}} \mathrm{d} y$ data measured for $1.6<|y|<2.4[6]$. The results obtained by LHCb [7] and CMS are reflected with respect to $y=0$ (open symbols).

Using the PYTHIA event generator with Perugia-0 tuning (with the EvtGen package to describe the particle decays) instead of FONLL results in a central value of 40.4 (40.9) $\mu \mathrm{b}$. A compilation of measurements of $\mathrm{d} \sigma_{\mathrm{b} \overline{\mathrm{b}}} / \mathrm{d} y$ at mid-rapidity is plotted in figure 7 as a function of $\sqrt{s}$, with superimposed FONLL predictions.

Finally, the total $b \bar{b}$ cross section was obtained as

$$
\begin{equation*}
\sigma(\mathrm{pp} \rightarrow \mathrm{~b} \overline{\mathrm{~b}}+X)=\alpha_{4 \pi} \frac{\sigma_{\mathrm{J} / \psi \leftarrow \mathrm{h}_{\mathrm{B}}}\left(p_{\mathrm{t}}^{\mathrm{J} / \psi}>1.3 \mathrm{GeV} / c,\left|y_{\mathrm{J} / \psi}\right|<0.9\right)}{2 \cdot B R\left(\mathrm{~h}_{\mathrm{b}} \rightarrow \mathrm{~J} / \psi+\mathrm{X}\right)} \tag{4.3}
\end{equation*}
$$

where $\alpha_{4 \pi}$ is the ratio between the yield of $\mathrm{J} / \psi$ mesons (from the decay of b-hadrons) in the full phase space and the yield in the measured region $\left|y_{\mathrm{J} / \psi}\right|<0.9$ and $p_{\mathrm{t}}^{\mathrm{J} / \psi}>1.3 \mathrm{GeV} / c$. The FONLL calculations provide $\alpha_{4 \pi}=4.49_{-0.10}^{+0.12}$, which produces $\sigma(\mathrm{pp} \rightarrow \mathrm{b} \overline{\mathrm{b}}+X)=$ $282 \pm 74$ (stat. $)_{-68}^{+58}(\text { syst. })_{-7}^{+8}$ (extr.) $\mu \mathrm{b}$. The extrapolation factor $\alpha_{4 \pi}$ was also estimated using PYTHIA with Perugia-0 tuning and found to be $\alpha_{4 \pi}^{\text {PYTHIA }}=4.20$. This measurement is in good agreement with those of the LHCb experiment, namely $288 \pm 4$ (stat.) $\pm 48$ (syst.) $\mu \mathrm{b}$ and $284 \pm 20$ (stat.) $\pm 49$ (syst.) $\mu$ b, which were based on the measured cross sections determined in the forward rapidity range from b-hadron decays into $\mathrm{J} / \psi X$ and $\mathrm{D}^{0} \mu \nu X$, respectively [7, 24].


Figure 6. Cross section for non-prompt $\mathrm{J} / \psi$ production as a function of rapidity. The error bars represent the quadratic sum of the statistical and systematic errors, while the systematic uncertainties on luminosity and branching ratio are shown as boxes. The systematic uncertainties on the extrapolation to $p_{\mathrm{t}}=0$ are indicated by the slashed areas. The CMS values were obtained by integrating the published $\mathrm{d}^{2} \sigma_{\mathrm{J} / \psi}$ from $\mathrm{B} / \mathrm{d} p_{\mathrm{t}} \mathrm{d} y$ data measured for $1.2<|y|<1.6$ and $1.6<$ $|y|<2.4[6]$. The results obtained in the forward region by LHCb [7] are reflected with respect to $y=0$ (open symbols). The FONLL calculation [41, 42] (and its uncertainty) is represented by solid (dashed) lines.

## 5 Summary

Results on the production cross section of prompt $\mathrm{J} / \psi$ and $\mathrm{J} / \psi$ from the decay of b-hadrons at mid-rapidity in pp collisions at $\sqrt{s}=7 \mathrm{TeV}$ have been presented. The measured cross sections have been compared to theoretical predictions based on QCD and results from other experiments. Prompt $\mathrm{J} / \psi$ production is well described by NLO NRQCD models that include color-octet processes. The cross section of $\mathrm{J} / \psi$ from b-hadron decays is in good agreement with the FONLL prediction, based on perturbative QCD. The ALICE results at mid-rapidity, covering a lower $p_{\mathrm{t}}$ region down to $p_{\mathrm{t}}=1.3 \mathrm{GeV} / c$, are complementary to those of the ATLAS and CMS experiments, which are available for $\mathrm{J} / \psi p_{\mathrm{t}}$ above $6.5 \mathrm{GeV} / c$. Using the shape of the $p_{\mathrm{t}}$ and $y$ distributions of b-quarks predicted by FONLL calculations, the mid-rapidity $\mathrm{d} \sigma / \mathrm{d} y$ and the total production cross section of $\mathrm{b} \overline{\mathrm{b}}$ pairs were determined.

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Figure 7. Beauty production cross section at mid-rapidity as a function of $\sqrt{s}$ in pp (PHENIX [47] and ALICE results) and p $\overline{\mathrm{p}}$ (UA1 [16] and CDF [17] results) collisions. The FONLL calculation [41, 42] (and its uncertainty) is represented by solid (dashed) lines.
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Gupta, ${ }^{d b}$ Hans Gutbrod, ${ }^{d g}$ Oystein Senneset Haaland, ${ }^{a n}$ Cynthia Marie Hadjidakis, ${ }^{b p}$ Maria Haiduc, ${ }^{b x}$ Hideki Hamagaki, ${ }^{e i}$ Gergoe Hamar, ${ }^{c h}$ Byounghee Han, ${ }^{a p}$ Luke David Hanratty, ${ }^{d l}$ Alexander Hansen, ${ }^{c s}$ Zuzana Harmanova, ${ }^{b h}$ John William Harris, ${ }^{e p}$ Matthias Hartig, ${ }^{b z}$ Dumitru Hasegan, ${ }^{b x}$ Despoina Hatzifotiadou, ${ }^{d s}$ Arsen Hayrapetyan, ${ }^{b c, e q}$ Stefan Thomas Heckel, ${ }^{b z}$ Markus Ansgar Heide, ${ }^{c b}$ Haavard Helstrup, ${ }^{b e}$ Andrei Ionut Herghelegiu, ${ }^{c r}$ Gerardo Antonio Herrera Corral, ${ }^{a h}$ Norbert Herrmann, ${ }^{d d}$ Benjamin Andreas Hess, ${ }^{e k}$ Kristin Fanebust Hetland, ${ }^{\text {be }}$ Bernard Hicks, ${ }^{e p}$ Per Thomas Hille, ${ }^{e p}$ Boris Hippolyte, ${ }^{c f}$ Takuma Horaguchi, ${ }^{e j}$ Yasuto Hori, ${ }^{e i}$ Peter Zahariev Hristov, ${ }^{b c}$ Ivana Hrivnacova, ${ }^{b p}$ Meidana Huang, ${ }^{a n}$ Thomas Humanic, ${ }^{a o}$ Dae Sung Hwang, ${ }^{a p}$ Raphaelle Ichou, ${ }^{c k}$ Radiy Ilkaev, ${ }^{d i}$ Iryna Ilkiv, ${ }^{d v}$ Motoi Inaba, ${ }^{e j}$ Elisa Incani, ${ }^{a r}$ Gian Michele Innocenti, ${ }^{a y}$ Pier Giorgio Innocenti, ${ }^{b c}$ Mikhail Ippolitov, ${ }^{d j}$ Muhammad Irfan, ${ }^{a m}$ Cristian George Ivan, ${ }^{d g}$ Vladimir Ivanov, ${ }^{c w}$ Marian Ivanov, ${ }^{d g}$ Andrey Ivanov, ${ }^{e m}$ Oleksii Ivanytskyi, ${ }^{a b}$ Adam Wlodzimierz Jacholkowski, ${ }^{b c}$ Peter Jacobs, ${ }^{c o}$ Haeng Jin Jang, ${ }^{c j}$ Swensy Gwladys Jangal, ${ }^{c f}$ Malgorzata Anna Janik, ${ }^{e n}$ Rudolf Janik, ${ }^{b f}$ Sandun Jayarathna, ef Satyajit Jena, ${ }^{b n}$ Deeptanshu Manu Jha, ${ }^{e o}$ Raul Tonatiuh Jimenez Bustamante, ${ }^{c c}$ Lennart Jirden, ${ }^{b c}$ Peter Graham Jones, ${ }^{d l}$ Hyung Taik Jung, ${ }^{b j}$ Anton Jusko, ${ }^{d l}$ Alexei Kaidalov, ${ }^{b t}$ Vanik Kakoyan, ${ }^{e q}$ Sebastian Kalcher, ${ }^{b i}$ Peter Kalinak, ${ }^{b u}$ Tuomo Esa Aukusti Kalliokoski, ${ }^{\text {bk }}$ Alexander Philipp Kalweit, ${ }^{c a}$ Kalliopi Kanaki, ${ }^{a n}$ Ju Hwan Kang, ${ }^{e s}$ Vladimir Kaplin, ${ }^{c q}$ Ayben Karasu Uysal, ${ }^{b c, e r}$ Oleg Karavichev, ${ }^{b r}$ Tatiana Karavicheva, ${ }^{b r}$ Evgeny Karpechev, ${ }^{b r}$ Andrey Kazantsev, ${ }^{d j}$ Udo Wolfgang Kebschull, ${ }^{b y}$ Ralf Keidel, ${ }^{e t}$ Palash Khan, ${ }^{d k}$ Mohisin Mohammed Khan, ${ }^{a m}$ Shuaib Ahmad Khan, ${ }^{e l}$ Alexei Khanzadeev, ${ }^{c w}$ Yury Kharlov, ${ }^{b q}$ Bjarte Kileng, ${ }^{b e}$ Do Won Kim, ${ }^{b j}$ Mimae Kim, ${ }^{b j}$ Minwoo Kim, ${ }^{e s}$ Seon Hee Kim, ${ }^{b j}$ Dong Jo Kim, ${ }^{b k}$ Se Yong Kim, ${ }^{a p}$ Jonghyun Kim, ${ }^{a p}$ Jin Sook Kim, ${ }^{b j}$ Beomkyu Kim, ${ }^{e s}$ Taesoo Kim, ${ }^{e s}$ Stefan Kirsch, ${ }^{b i}$ Ivan Kisel, ${ }^{b i}$ Sergey Kiselev, ${ }^{b t}$ Adam Ryszard Kisiel, ${ }^{b c, e n}$ Jennifer Lynn Klay, ${ }^{\text {ad }}$ Jochen Klein, ${ }^{d d}$ Christian Klein-Bosing, ${ }^{c b}$ Michael Kliemant, ${ }^{b z}$ Alexander Kluge, ${ }^{b c}$ Michael Linus Knichel, ${ }^{d g}$ Anders Garritt Knospe, ${ }^{e a}$ Kathrin Koch, ${ }^{d d}$ Markus Kohler, ${ }^{d g}$ Anatoly Kolojvari, ${ }^{e m}$ Valery Kondratiev, ${ }^{e m}$ Natalia Kondratyeva, ${ }^{c q}$ Artem Konevskih, ${ }^{\text {br }}$ Andrey Korneev, ${ }^{d i}$ Ravjeet Kour, ${ }^{d l}$ Marek Kowalski, ${ }^{d z}$ Serge Kox, ${ }^{c l}$ Greeshma Koyithatta Meethaleveedu, ${ }^{b n}$ Jiri Kral, ${ }^{b k}$ Ivan Kralik, ${ }^{b u}$ Frederick Kramer, ${ }^{b z}$ Ingrid Christine Kraus, ${ }^{d g}$ Tobias Krawutschke, ${ }^{d d, b d}$ Michal Krelina, ${ }^{b g}$ Matthias Kretz, ${ }^{b i}$ Marian Krivda, ${ }^{d l, b u}$ Filip Krizek, ${ }^{b k}$ Miroslav Krus, ${ }^{b g}$ Evgeny Kryshen, ${ }^{c w}$ Mikolaj Krzewicki, ${ }^{d g}$ Yury Kucheriaev, ${ }^{d j}$ Christian Claude Kuhn, ${ }^{c f}$ Paul Kuijer, ${ }^{c t}$ Igor Kulakov, ${ }^{b z}$ Jitendra Kumar, ${ }^{b n}$ Podist Kurashvili, ${ }^{d v}$ A.B. Kurepin, ${ }^{b r}$ A. Kurepin, ${ }^{b r}$ Alexey Kuryakin, ${ }^{d i}$ Vasily Kushpil, ${ }^{c u}$ Svetlana Kushpil, ${ }^{c u}$ Henning Kvaerno, ${ }^{a q}$ Min Jung Kweon, ${ }^{d d}$ Youngil Kwon, ${ }^{e s}$ Pedro Ladron de Guevara, ${ }^{c c}$ Igor Lakomov, ${ }^{b p}$ Rune Langoy, ${ }^{a n}$ Sarah Louise La Pointe, ${ }^{b s}$ Camilo Ernesto Lara, ${ }^{b y}$ Antoine Xavier Lardeux, ${ }^{d x}$ Paola La Rocca, ${ }^{a w}$ Cristina Lazzeroni, ${ }^{d l}$ Ramona Lea, ${ }^{a t}$ Yves Le Bornec, ${ }^{b p}$ Mateusz Lechman, ${ }^{b c}$ Sung Chul Lee, ${ }^{b j}$ Ki Sang Lee, ${ }^{b j}$ Graham Richard Lee, ${ }^{d l}$ Frederic Lefevre, ${ }^{d x}$ Joerg Walter Lehnert, ${ }^{b z}$ Lars Leistam, ${ }^{b c}$ Matthieu Laurent Lenhardt, ${ }^{d x}$ Vito Lenti, ${ }^{d t}$ Hermes Leon, ${ }^{c d}$ Marco Leoncino, ${ }^{d p}$ Ildefonso Leon Monzon, ${ }^{e b}$ Hermes Leon Vargas, ${ }^{b z}$ Peter Levai, ${ }^{\text {ch }}$ Jorgen Lien, ${ }^{a n}$ Roman Lietava, ${ }^{d l}$ Svein Lindal, ${ }^{a q}$ Volker Lindenstruth, ${ }^{b i}$ Christian Lippmann, ${ }^{d g, b c}$ Michael Annan Lisa, ${ }^{a o}$ Lijiao Liu, ${ }^{a n}$ Per-Ivar Loenne, ${ }^{a n}$ Vera Loggins, ${ }^{e o}$ Vitaly Loginov, ${ }^{c q}$ Stefan Bernhard Lohn, ${ }^{b c}$ Daniel

Lohner, ${ }^{d d}$ Constantinos Loizides, ${ }^{c o}$ Kai Krister Loo, ${ }^{b k}$ Xavier Bernard Lopez, ${ }^{c k}$ Ernesto Lopez Torres, ${ }^{a f}$ Gunnar Lovhoiden, ${ }^{a q}$ Xianguo Lu, ${ }^{d d}$ Philipp Luettig, ${ }^{b z}$ Marcello Lunardon, ${ }^{a s}$ Jiebin Luo, ${ }^{b m}$ Grazia Luparello, ${ }^{b s}$ Lionel Luquin, ${ }^{d x}$ Cinzia Luzzi, ${ }^{b c}$ Rongrong $\mathrm{Ma},{ }^{e p} \mathrm{Ke} \mathrm{Ma}$, ${ }^{b m}$ Dilan Minthaka Madagodahettige-Don, ${ }^{e f}$ Alla Maevskaya, ${ }^{b r}$ Magnus Mager, ${ }^{c a, b c}$ Durga Prasad Mahapatra, ${ }^{b v}$ Antonin Maire, ${ }^{d d}$ Mikhail Malaev, ${ }^{c w}$ Ivonne Alicia Maldonado Cervantes, ${ }^{c c}$ Ludmila Malinina, ${ }^{c g, 1}$ Dmitry Mal'Kevich, ${ }^{\text {b }}$ Peter Malzacher, ${ }^{d g}$ Alexander Mamonov, ${ }^{d i}$ Loic Henri Antoine Manceau, ${ }^{d p}$ Lalit Kumar Mangotra, ${ }^{d b}$ Vladislav Manko, ${ }^{d j}$ Franck Manso, ${ }^{c k}$ Vito Manzari, ${ }^{d t}$ Yaxian Mao, ${ }^{b m}$ Massimiliano Marchisone, ${ }^{c k, a y}$ Jiri Mares, ${ }^{b w}$ Giacomo Vito Margagliotti, ${ }^{a t, d n}$ Anselmo Margotti, ${ }^{d s}$ Ana Maria Marin, ${ }^{d g}$ Cesar Augusto Marin Tobon, ${ }^{b c}$ Christina Markert, ${ }^{e a}$ Irakli Martashvili, ${ }^{\text {eh }}$ Paolo Martinengo, ${ }^{\text {bc }}$ Mario Ivan Martinez, ${ }^{a a}$ Arnulfo Martinez Davalos, ${ }^{c d}$ Gines Martinez Garcia, ${ }^{d x}$ Yevgen Martynov, ${ }^{a b}$ Alexis Jean-Michel Mas, ${ }^{d x}$ Silvia Masciocchi, ${ }^{d g}$ Massimo Masera, ${ }^{a y}$ Alberto Masoni, ${ }^{d r}$ Laure Marie Massacrier, ${ }^{e e, d x}$ Mario Mastromarco, ${ }^{d t}$ Annalisa Mastroserio, ${ }^{\text {ba,bc }}$ Zoe Louise Matthews, ${ }^{d l}$ Adam Tomasz Matyja, ${ }^{d z, d x}$ Daniel Mayani, ${ }^{c c}$ Christoph Mayer, ${ }^{d z}$ Joel Mazer, ${ }^{e h}$ Alessandra Maria Mazzoni, ${ }^{d q}$ Franco Meddi, ${ }^{a v}$ Arturo Alejandro Menchaca-Rocha, ${ }^{c d}$ Jorge Mercado Perez, ${ }^{d d}$ Michal Meres, ${ }^{b f}$ Yasuo Miake, ${ }^{e j}$ Leonardo Milano, ${ }^{a y}$ Jovan Milosevic, ${ }^{a q, 2}$ Andre Mischke, ${ }^{b s}$ Aditya Nath Mishra, ${ }^{d c}$ Dariusz Miskowiec, ${ }^{d g, b c}$ Ciprian Mihai Mitu, ${ }^{b x}$ Jocelyn Mlynarz, ${ }^{e o}$ Bedangadas Mohanty, ${ }^{e l}$ Ajit Kumar Mohanty, ${ }^{\text {bc }}$ Levente Molnar, ${ }^{b c}$ Luis Manuel Montano Zetina, ${ }^{a h}$ Marco Monteno, ${ }^{d p}$ Esther Montes, ${ }^{a g}$ Taebong Moon, ${ }^{e s}$ Maurizio Morando, ${ }^{a s}$ Denise Aparecida Moreira De Godoy, ${ }^{e c}$ Sandra Moretto, ${ }^{a s}$ Andreas Morsch, ${ }^{b c}$ Valeria Muccifora, ${ }^{c m}$ Eugen Mudnic, ${ }^{d y}$ Sanjib Muhuri, ${ }^{e l}$ Maitreyee Mukherjee, ${ }^{e l}$ Hans Muller, ${ }^{b c}$ Marcelo Munhoz, ${ }^{e c}$ Luciano Musa, ${ }^{b c}$ Alfredo Musso, ${ }^{d p}$ Basanta Kumar Nandi, ${ }^{b n}$ Rosario Nania, ${ }^{d s}$ Eugenio Nappi, ${ }^{d t}$ Christine Nattrass, ${ }^{e h}$ Nikolay Naumov, ${ }^{d i}$ Sparsh Navin, ${ }^{\text {dl }}$ Tapan Kumar Nayak, ${ }^{e l}$ Sergey Nazarenko, ${ }^{d i}$ Gleb Nazarov, ${ }^{d i}$ Alexander Nedosekin, ${ }^{b t}$ Maria Nicassio, ${ }^{b a}$ Mihai Niculescu, ${ }^{b x, b c}$ Borge Svane Nielsen, ${ }^{c s}$ Takafumi Niida, ${ }^{e j}$ Sergey Nikolaev, ${ }^{d j}$ Vedran Nikolic, ${ }^{d h}$ Sergey Nikulin, ${ }^{d j}$ Vladimir Nikulin, ${ }^{c w}$ Bjorn Steven Nilsen, ${ }^{c x}$ Mads Stormo Nilsson, ${ }^{a q}$ Francesco Noferini, ${ }^{d s, a i}$ Petr Nomokonov, ${ }^{c g}$ Gerardus Nooren, ${ }^{b s}$ Norbert Novitzky, ${ }^{b k}$ Alexandre Nyanin, ${ }^{d j}$ Anitha Nyatha, ${ }^{b n}$ Casper Nygaard, ${ }^{c s}$ Joakim Ingemar Nystrand, ${ }^{\text {an }}$ Alexander Ochirov, ${ }^{e m}$ Helmut Oskar Oeschler, ${ }^{c a, b c}$ Saehanseul Oh, ${ }^{e p}$ Sun Kun Oh, ${ }^{b j}$ Janusz Oleniacz, ${ }^{e n}$ Chiara Oppedisano, ${ }^{d p}$ Antonio Ortiz Velasquez, ${ }^{b b, c c}$ Giacomo Ortona, ${ }^{a y}$ Anders Nils Erik Oskarsson, ${ }^{b b}$ Piotr Krystian Ostrowski, ${ }^{e n}$ Jacek Tomasz Otwinowski, ${ }^{d g}$ Ken Oyama, ${ }^{d d}$ Kyoichiro Ozawa, ${ }^{e i}$ Yvonne Chiara Pachmayer, ${ }^{d d}$ Milos Pachr, ${ }^{\text {bg }}$ Fatima Padilla, ${ }^{a y}$ Paola Pagano, ${ }^{a x}$ Guy Paic, ${ }^{c c}$ Florian Painke, ${ }^{b i}$ Carlos Pajares, ${ }^{a l}$ S. Pal, ${ }^{a k}$ Susanta Kumar Pal,,${ }^{e l}$ Arvinder Singh Palaha, ${ }^{d l}$ Armando Palmeri, ${ }^{d u}$ Vardanush Papikyan, ${ }^{e q}$ Giuseppe Pappalardo, ${ }^{d u}$ Woo Jin Park, ${ }^{d g}$ Annika Passfeld, ${ }^{c b}$ Blahoslav Pastircak, ${ }^{b u}$ Dmitri Ivanovich Patalakha, ${ }^{b q}$ Vincenzo Paticchio, ${ }^{d t}$ Alexei Pavlinov, ${ }^{e o}$ Tomasz Jan Pawlak, ${ }^{e n}$ Thomas Peitzmann, ${ }^{b s}$ Hugo Denis Antonio Pereira Da Costa, ${ }^{a k}$ Elienos Pereira De Oliveira Filho, ${ }^{e c}$ Dmitri Peresunko, ${ }^{d j}$

[^2]Carlos Eugenio Perez Lara, ${ }^{c t}$ Edgar Perez Lezama, ${ }^{c c}$ Diego Perini, ${ }^{b c}$ Davide Perrino, ${ }^{b a}$ Wiktor Stanislaw Peryt, ${ }^{e n}$ Alessandro Pesci, ${ }^{d s}$ Vladimir Peskov, ${ }^{b c, c c}$ Yury Pestov, ${ }^{a c}$ Vojtech Petracek, ${ }^{b g}$ Michal Petran, ${ }^{b g}$ Mariana Petris, ${ }^{c r}$ Plamen Rumenov Petrov, ${ }^{d l}$ Mihai Petrovici, ${ }^{c r}$ Catia Petta, ${ }^{a w}$ Stefano Piano, ${ }^{d n}$ Anna Piccotti, ${ }^{d p}$ Miroslav Pikna, ${ }^{b f}$ Philippe Pillot, ${ }^{d x}$ Ombretta Pinazza, ${ }^{b c}$ Lawrence Pinsky, ${ }^{e f}$ Nora Pitz, ${ }^{b z}$ Danthasinghe Piyarathna,,${ }^{e f}$ Mateusz Andrzej Ploskon, ${ }^{c o}$ Jan Marian Pluta, ${ }^{e n}$ Timur Pocheptsov, ${ }^{c g}$ Sona Pochybova, ${ }^{c h}$ Pedro Luis Manuel Podesta Lerma, ${ }^{e b}$ Martin Poghosyan, ${ }^{b c, a y}$ Karel Polak, ${ }^{b w}$ Boris Polichtchouk, ${ }^{b q}$ Amalia Pop, ${ }^{c r}$ Sarah Porteboeuf-Houssais, ${ }^{c k}$ Vladimir Pospisil, ${ }^{b g}$ Baba Potukuchi, ${ }^{d b}$ Sidharth Kumar Prasad, ${ }^{e o}$ Roberto Preghenella, ${ }^{d s, a i}$ Francesco Prino, ${ }^{d p}$ Claude Andre Pruneau, ${ }^{e o}$ Igor Pshenichnov, ${ }^{b r}$ Sergey Puchagin, ${ }^{d i}$ Giovanna Puddu, ${ }^{a r}$ Jordi Pujol Teixido, ${ }^{b y}$ Alberto Pulvirenti, ${ }^{a w, b c}$ Valery Punin, ${ }^{d i}$ Marian Putis, ${ }^{b h}$ Jorn Henning Putschke, ${ }^{e 0, e p}$ Emanuele Quercigh, ${ }^{b c}$ Henrik Qvigstad, ${ }^{a q}$ Alexandre Rachevski, ${ }^{d n}$ Alphonse Rademakers, ${ }^{b c}$ Sylwester Radomski, ${ }^{d d}$ Tomi Samuli Raiha, ${ }^{b k}$ Jan Rak, ${ }^{b k}$ Andry Malala Rakotozafindrabe, ${ }^{a k}$ Luciano Ramello, ${ }^{a z}$ Abdiel Ramirez Reyes, ${ }^{a h}$ Sudhir Raniwala, ${ }^{d c}$ Rashmi Raniwala, ${ }^{d c}$ Sami Sakari Rasanen, ${ }^{b k}$ Bogdan Theodor Rascanu, ${ }^{b z}$ Deepika Rathee, ${ }^{c y}$ Kenneth Francis Read, ${ }^{\text {eh }}$ Jean-Sebastien Real, ${ }^{c l}$ Krzysztof Redlich, ${ }^{d v, c e}$ Patrick Reichelt, ${ }^{b z}$ Martijn Reicher, ${ }^{b s}$ Rainer Arno Ernst Renfordt, ${ }^{b z}$ Anna Rita Reolon, ${ }^{c m}$ Andrey Reshetin, ${ }^{b r}$ Felix Vincenz Rettig, ${ }^{b i}$ Jean-Pierre Revol, ${ }^{b c}$ Klaus Johannes Reygers, ${ }^{d d}$ Lodovico Riccati, ${ }^{d p}$ Renato Angelo Ricci, ${ }^{c n}$ Tuva Richert, ${ }^{b b}$ Matthias Rudolph Richter, ${ }^{a q}$ Petra Riedler, ${ }^{b c}$ Werner Riegler, ${ }^{b c}$ Francesco Riggi, ${ }^{a w, d u}$ Bartolomeu Rodrigues Fernandes Rabacal, ${ }^{b c}$ Mario Rodriguez Cahuantzi, ${ }^{a a}$ Alis Rodriguez Manso, ${ }^{\text {ct }}$ Ketil Roed, ${ }^{a n}$ David Rohr, ${ }^{b i}$ Dieter Rohrich, ${ }^{a n}$ Rosa Romita, ${ }^{d g}$ Federico Ronchetti, ${ }^{c m}$ Philippe Rosnet, ${ }^{c k}$ Stefan Rossegger, ${ }^{b c}$ Andrea Rossi, ${ }^{\text {bc,as }}$ Christelle Sophie Roy, ${ }^{c f}$ Pradip Kumar Roy, ${ }^{d k}$ Antonio Juan Rubio Montero, ${ }^{a g}$ Rinaldo Rui, ${ }^{a t}$ Evgeny Ryabinkin, ${ }^{d j}$ Andrzej Rybicki, ${ }^{d z}$ Sergey Sadovsky, ${ }^{\text {bq }}$ Karel Safarik, ${ }^{b c}$ Raghunath Sahoo, ${ }^{b o}$ Pradip Kumar Sahu, ${ }^{b v}$ Jogender Saini, ${ }^{e l}$ Hiroaki Sakaguchi, ${ }^{b l}$ Shingo Sakai, ${ }^{c o}$ Dosatsu Sakata, ${ }^{e j}$ Carlos Albert Salgado, ${ }^{a l}$ Jai Salzwedel, ${ }^{a o}$ Sanjeev Singh Sambyal, ${ }^{\text {db }}$ Vladimir Samsonov, ${ }^{c w}$ Xitzel Sanchez Castro, ${ }^{c f}$ Ladislav Sandor, ${ }^{b u}$ Andres Sandoval, ${ }^{c d}$ Satoshi Sano, ${ }^{e i}$ Masato Sano, ${ }^{e j}$ Rainer Santo, ${ }^{c b}$ Romualdo Santoro, ${ }^{d t, b c, a i}$ Juho Jaako Sarkamo, ${ }^{b k}$ Eugenio Scapparone, ${ }^{d s}$ Fernando Scarlassara, ${ }^{a s}$ Rolf Paul Scharenberg, ${ }^{d e}$ Claudiu Cornel Schiaua, ${ }^{c r}$ Rainer Martin Schicker, ${ }^{d d}$ Christian Joachim Schmidt, ${ }^{d g}$ Hans Rudolf Schmidt, ${ }^{e k}$ Steffen Schreiner, ${ }^{b c}$ Simone Schuchmann, ${ }^{b z}$ Jurgen Schukraft, ${ }^{b c}$ Yves Roland Schutz, ${ }^{b c, d x}$ Kilian Eberhard Schwarz, ${ }^{d g}$ Kai Oliver Schweda, ${ }^{d g, d d}$ Gilda Scioli, ${ }^{a u}$ Enrico Scomparin, ${ }^{d p}$ Rebecca Scott, ${ }^{e h}$ Patrick Aaron Scott, ${ }^{d l}$ Gianfranco Segato, ${ }^{a s}$ Ilya Selioujenkov, ${ }^{d g}$ Serhiy Senyukov, ${ }^{a z, c f}$ Jeewon Seo, ${ }^{d f}$ Sergio Serci, ${ }^{a r}$ Eulogio Serradilla, ${ }^{a g, c d}$ Adrian Sevcenco, ${ }^{b x}$ Alexandre Shabetai, ${ }^{d x}$ Galina Shabratova, ${ }^{c g}$ Ruben Shahoyan, ${ }^{b c}$ Natasha Sharma, ${ }^{c y}$ Satish Sharma, ${ }^{d b}$ Rohini Sharma, ${ }^{d b}$ Kenta Shigaki, ${ }^{b l}$ Maya Shimomura, ${ }^{e j}$ Katherin Shtejer, ${ }^{a f}$ Yury Sibiriak, ${ }^{d j}$ Melinda Siciliano, ${ }^{a y}$ Eva Sicking, ${ }^{b c}$ Sabyasachi Siddhanta, ${ }^{d r}$ Teodor Siemiarczuk, ${ }^{d v}$ David Olle Rickard Silvermyr, ${ }^{c v}$ Catherine Silvestre, ${ }^{c l}$ Goran Simatovic, ${ }^{c c, d h}$ Giuseppe Simonetti, ${ }^{b c}$ Rama Narayana Singaraju, ${ }^{e l}$ Ranbir Singh, ${ }^{d b}$ Subhash Singha, ${ }^{e l}$ Vikas Singhal, ${ }^{e l}$ Tinku Sinha, ${ }^{d k}$ Bikash Sinha, ${ }^{e l}$ Branislav Sitar, ${ }^{\text {bf }}$ Mario Sitta, ${ }^{a z}$ Bernhard Skaali, ${ }^{a q}$ Kyrre Skjerdal, ${ }^{a n}$ Radek Smakal,,${ }^{b g}$ Nikolai Smirnov, ${ }^{e p}$ Raimond Snellings, ${ }^{b s}$ Carsten Sogaard, ${ }^{c s}$ Ron Ariel Soltz, ${ }^{c p}$

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[^0]:    ${ }^{1}$ The variable $x$, which was introduced in [1], mimics a similar variable used for b-hadron lifetime measurements where b-hadrons are reconstructed exclusively and therefore the mass and $p_{\mathrm{t}}$ of the b-hadron can be used in place of those of the $\mathrm{J} / \psi$, to get $c \tau=\frac{L}{\beta \gamma}=\frac{c \cdot L_{x y} \cdot M_{\mathrm{b}} \text {-hadron }}{p_{\mathrm{t}}^{\mathrm{b}-\text { hadron }}}$.

[^1]:    ${ }^{2}$ The polar angle distribution of the $\mathrm{J} / \psi$ decay leptons is given by $\mathrm{d} N / \mathrm{d} \cos \theta=1+\lambda \cos ^{2} \theta$.

[^2]:    ${ }^{3}$ Also at M.V.Lomonosov Moscow State University, D.V.Skobeltsyn Institute of Nuclear Physics, Moscow, Russia.
    ${ }^{4}$ Also at University of Belgrade, Faculty of Physics and "Vinča" Institute of Nuclear Sciences, Belgrade, Serbia.

