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# STUDY ON EVALUATION ERROR CHARACTER OF HYDRAULIC RADIUS IN HYDRAULIC CALCULATION ${ }^{1}$ 

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#### Abstract

Hydraulic radius is an important parameter in hydraulic calculation. But it is often deemed that hydraulic radius can be replaced by the cross-sectional average water depth when the width to depth ratio $(\mathrm{B} / \mathrm{H})$ is greater than a certain value in traditional. Based on the various artificial cross-section and natural ones, value-taking errors of hydraulic radius are studied in this paper. The results show that it's feasible to adopt the average water depth as the hydraulic radius when $\mathrm{B} / \mathrm{H}$ of rectangular section is larger than 40 or $\mathrm{B} / \mathrm{H}$ of isosceles triangular section is larger than 12 . But for natural river, $\mathrm{B} / \mathrm{H}$ is different when water level changes and there is no single-valued corresponding relationship between relative error and $\mathrm{B} / \mathrm{H}$. Therefore we advise that hydraulic radius could not be replaced by other variables in hydraulic calculation of natural rivers.


KEY WORDS: hydraulic radius; cross-sectional average water depth; width to depth ratio (B/H); error character

## 1. INTRODUCTION

As a very important parameter of a cross section, hydraulic radius, which is often used in water dynamics calculations, is defined as the ratio of the cross section area to the corresponding wetted perimeter. For example, it can be used to estimate discharge by the Manning formula ${ }^{[1]}$ and to calculate water level by the Saint-Venant equations and so on ${ }^{[2]}{ }^{[3]}{ }^{[4]}$. Since the cross-sectional shape of natural river is complicated, it's difficult to measure the wetted perimeter, which causes much trouble in hydraulic radius calculation. It is said that when the ratio of water surface width to depth of a certain cross section is greater than 25 , the hydraulic radius could be replaced approximately by average depth of the cross section ${ }^{[5]}$. This view point has a great influence till now. TANG Hongwu suppose that it is reasonable to adopt the $\mathrm{R}=\mathrm{H}$ in shallow water without vegetation. When analyzing the resistance in the Yellow River estuary Hou Zhijun ${ }^{[7]}$ still replaced the hydraulic radius by depth. Even more, the restrictions of the width to depth ratio is often be neglected and error be inevitably brought in practical application. Recently, with the development of the compute, it is possible to use the hydraulic radius directly in calculation and some researchers start to pay attention to the error of replacing the hydraulic radius by depth, some primary analysis of to the error characteristic have been done ${ }^{[8-11]}$ and some academician take hydraulic radius directly without replacing in their calculation ${ }^{[12]}$. Therefore, it is necessary to research on value-taking errors of hydraulic radius, which may give directions to practical application.

## 2. HYDRAULIC RADIUS AND ITS CHARACTER

Hydraulic radius R and average depth H of a certain cross section can be expressed as:

$$
\begin{equation*}
R=\frac{A}{\chi} \tag{1}
\end{equation*}
$$

[^0]\[

$$
\begin{equation*}
H=\frac{A}{B} \tag{2}
\end{equation*}
$$

\]

There, A is the cross-sectional area; B is the width of water surface; $\chi$ is the wetted perimeter. Generically, B is smaller than $\chi$, so H is bigger than R . The relative error between H and R is:

$$
\begin{equation*}
\varepsilon=\frac{H-R}{R}=\frac{\chi}{B}-1 \tag{3}
\end{equation*}
$$

Obviously, the relative error is concerned with the shape of cross section. The hydraulic radius value-taking error of cross sections that have different shapes will be analyzed in the following.

### 2.1 Regular cross section

(1) Rectangular section

As shown in Fig.1, it will result in $A=B H_{\max }$ and $A=B H$, while B expresses water surface width, $H_{\max }$ expresses the biggest depth in section and H is cross-sectional average water depth.

The wetted perimeter of the rectangular section can be expressed as

$$
\chi=B+2 H_{\max }=B+2 H
$$

Assuming that the width to depth ratio $\mu=B / H$, then

$$
\begin{equation*}
\frac{\chi}{B}=\frac{B+2 H}{B}=1+\frac{2}{\mu} \tag{4}
\end{equation*}
$$

Introducing Eq.(4) into Eq.(3), the relative error between H and R will be expressed as following:

$$
\begin{equation*}
\varepsilon=\frac{\chi}{B}-1=\frac{2}{\mu} \tag{5}
\end{equation*}
$$

The relationship between $\mathrm{B} / \mathrm{H}$ and $\varepsilon$ in rectangular section is shown in Tab.1.

Tab. 1 Relationship between $\mathbf{B} / \mathbf{H}$ and $\varepsilon$ in rectangular section

| $B / H$ | 10 | 15 | 20 | 40 | 60 | 100 | 150 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\varepsilon(\%)$ | 20.00 | 13.33 | 10.00 | 5.00 | 3.33 | 2.00 | 1.33 |

According to Tab.1, the bigger the width to depth ratio $(\mathrm{B} / \mathrm{H})$ in a rectangular section is, the smaller the relative error $(\varepsilon)$ is. If $\varepsilon$ couldn't surpass $5 \%, \mathrm{~B} / \mathrm{H}$ should be bigger than 40 .
(2) Isosceles triangular section

As it is shown in Fig. 2, in isosceles triangular, its area is $A=B H_{\text {max }} / 2$, what is more, $A=B H$, therefore $H_{\max }=2 H$. The wetted perimeter of a isosceles triangle cross section is given by

$$
\begin{equation*}
\chi=2 \sqrt{\left(\frac{B}{2}\right)^{2}+\left(H_{\max }\right)^{2}}=2 \sqrt{4 H^{2}+\frac{B^{2}}{4}} \tag{6}
\end{equation*}
$$

Assuming that $\mu=B / H$

$$
\begin{equation*}
\frac{\chi}{B}=2 \sqrt{\frac{4}{\mu^{2}}+\frac{1}{4}} \tag{7}
\end{equation*}
$$

Introducing Eq.(7) into Eq.(3) , the relative error between H and R will be got as following:

$$
\begin{equation*}
\varepsilon=\frac{\chi}{B}-1=2 \sqrt{\frac{4}{\mu^{2}}+\frac{1}{4}}-1 \tag{8}
\end{equation*}
$$

The relationship between $\mathrm{B} / \mathrm{H}$ and $\varepsilon$ in isosceles triangular section is shown in Tab.2. According to Tab.2, the bigger $\mathrm{B} / \mathrm{H}$ in a triangular section is, the smaller $\varepsilon$ is. If $\varepsilon$ couldn't surpass $5 \%, \mathrm{~B} / \mathrm{H}$ should be more than 12 .

| Table 2 Relationship between width to depth ratio and relative error of an isosceles triangular section |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B / H$ | 10 | 15 | 20 | 40 | 60 | 100 | 150 |
| $\varepsilon(\%)$ | 7.70 | 3.49 | 1.98 | 0.50 | 0.22 | 0.08 | 0.04 |

(3) Isosceles trapezoid section

As it is shown in Fig. 3, assuming that the width at the bottom of an isosceles trapezoidal cross section is $b$, its area can be expressed as

$$
\begin{equation*}
A=(b+B) H_{\text {max }} / 2 \tag{9}
\end{equation*}
$$

Assuming that $\lambda=b / B, \quad$ Eq.(9) can be expressed as


Fig. 1 Rectangular section


Fig. 2 Isosceles triangular section

$$
A=(1+\lambda) B H_{\max } / 2
$$

And

$$
A=B H
$$

So

$$
H_{\max }=\frac{2 H}{1+\lambda}
$$

Then the wetted perimeter of this section may be written as

$$
\chi=2 \sqrt{H_{\max }^{2}+(B-b)^{2} / 4}+b=2 \sqrt{\left(\frac{2}{1+\lambda}\right)^{2} H^{2}+\left(\frac{1-\lambda}{2}\right)^{2} B^{2}}+\lambda B
$$

Supposing that $\mu=B / H$, then

$$
\begin{equation*}
\frac{\chi}{B}=2 \sqrt{\frac{4}{(1+\lambda)^{2} \mu^{2}}+\frac{(1-\lambda)^{2}}{4}}+\lambda \tag{10}
\end{equation*}
$$

Introducing Eq.(10) into Eq.(3) , the relative error between H and R will be got as following:

$$
\begin{equation*}
\varepsilon=\frac{\chi}{B}-1=2 \sqrt{\frac{4}{(1+\lambda)^{2} \mu^{2}}+\frac{(1-\lambda)^{2}}{4}}+\lambda-1 \tag{11}
\end{equation*}
$$

It's obvious that the relative error $\varepsilon$ is concerned with not only $B / H$ but also $b / B$ in Eq.(11). In fact, a rectangular section and an isosceles triangular section can be considered as two special ones of isosceles trapezoidal cross sections. When the width at the bottom $b$ equals to $B$, namely $\lambda=1$, an isosceles trapezoid section is a rectangular section. When the width at the bottom $b$ equals to 0 , namely $\lambda=0$, an isosceles trapezoidal section is an isosceles triangular section.

The relationship among $\mathrm{B} / \mathrm{H}, \lambda$ and $\varepsilon$ is shown in Tab. 3. If $\lambda$ is invariable, $\varepsilon$ will reduce as
$\mathrm{B} / \mathrm{H}$ increases. If $\mathrm{B} / \mathrm{H}$ is invariable, as $\lambda$ increases, $\varepsilon$ will decrease at first and increase afterward and $\varepsilon$ will touch bottom when $\lambda$ is approximately 0.3 .

Tab. 3 Relationship among $B / H, \lambda$ and $\varepsilon$

| Tab. 3 Relationship among $B / H, \lambda$ and $\mathcal{E}$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (\%) | 10 | 15 | 20 | 40 | 60 | 100 | 150 |
| 0.1 | 7.07 | 3.21 | 1.82 | 0.46 | 0.20 | 0.07 | 0.03 |
| 0.3 | 6.46 | 2.94 | 1.67 | 0.42 | 0.19 | 0.07 | 0.03 |
| 0.5 | 6.67 | 3.07 | 1.75 | 0.44 | 0.20 | 0.07 | 0.03 |
| 0.7 | 8.13 | 3.85 | 2.22 | 0.57 | 0.26 | 0.09 | 0.04 |
| 0.9 | 13.31 | 7.23 | 4.52 | 1.30 | 0.60 | 0.22 | 0.10 |

### 2.2 Natural river section

Above sections are regular, so we can use the mathematical expression to describe the relative error $\varepsilon$. But for complicated and diversified natural river section, it is difficult to infer $\varepsilon$. In natural river, when we want to calculate hydraulic radius and cross-sectional average water depth, a certain cross section is usually be divided into many sub-cross sections and area, width, wetted perimeter of each sub-cross section be calculated separately. So area, width, and wetted perimeter of the whole cross section can be obtained by addition. And we can use Eq.(1) and Eq.(2) to calculate hydraulic radius and cross-sectional average water depth of the cross section.

Fig. 4 shows the configuration of a natural cross-section. Fig. 5 shows the relations between different water level and $\mathrm{B} / \mathrm{H}$ in it. B/H varies greatly at different water level. Such as, B/H changes between 18 and 106 when the water level varies in the range of 26 m to 27 m . The relationship between $\mathrm{B} / \mathrm{H}$ and $\varepsilon$ is shown in Fig.6. Fig. 7 shows the relationships among $\varepsilon, \mathrm{B} / \mathrm{H}$ and water level. $\varepsilon$ has a tendency to reduce along with the $\mathrm{B} / \mathrm{H}$ enlarging. But they don't have a single-valued relationship. The corresponding error is not always small when $\mathrm{B} / \mathrm{H}$ is big, vice versa. $\varepsilon$ may differ widely from each other when $\mathrm{B} / \mathrm{H}$ is nearly the same. For example, when the water level is 36 m , the corresponding $\mathrm{B} / \mathrm{H}$ is $60, \varepsilon$ might still be $6 \%$. When water level is 26 m and 35 m respectively, the corresponding $\mathrm{B} / \mathrm{H}$ is about 40 , but $\varepsilon$ actually has great difference, $0.6 \%$ and $7 \%$ respectively.

Therefore, identical natural cross section couldn't be described generally by a fixed $\mathrm{B} / \mathrm{H}$. We should compute $\mathrm{B} / \mathrm{H}$ under each grade of water level and $\mathrm{B} / \mathrm{H}$ doesn't have sole corresponding relationships with $\varepsilon$. The view isn't advisable that it's possible to control the error into a certain scope when $B / H$ is bigger than a certain value.


Fig. 4 Sketch map of a natural section


Fig. 5 Relation between water level and $B / H$


Fig. 6 Relation between B/H and $\mathcal{E}$


Fig. 7 Relation among $\mathcal{E}, \mathbf{B} / \mathbf{H}$ and water level

## 3. CASES

Nansha Hydro-junction on Honghe River and Baihe Hydro-junction Hanjiang River are taken as examples. The errors will be analyzed which come from substitution cross-sectional average water depth for hydraulic radius in the water-level computation.

The continuity equation and the motion equation of 1D Saint-Venant equations may be given by

$$
\begin{align*}
& \frac{\partial Q}{\partial x}=q_{1}  \tag{12}\\
& \frac{\partial}{\partial x}\left(\frac{Q^{2}}{A}\right)+g A \frac{\partial Z}{\partial x}+g \frac{Q^{2} n^{2}}{A^{2} R^{4 / 3}}=0 \tag{13}
\end{align*}
$$

Where $Q$ is discharge, $Z$ is water level, $n$ is the roughness coefficient and $q_{1}$ is the lateral inflow discharge per unit of the width.

The discretization of Eq. (12) and (13) can be obtained by using the forward difference:

$$
\begin{align*}
& Q_{j+1}=Q_{j}+q_{1} \Delta x  \tag{14}\\
& Z_{j}=Z_{j+1}+\frac{1}{2 g}\left(\frac{Q_{j+1}^{2}}{A_{j+1}^{2}}-\frac{Q_{j}^{2}}{A_{j}^{2}}\right)+\frac{n^{2} \bar{Q}^{2}}{\bar{A}^{2} \bar{R}^{4 / 3}} \Delta x \tag{15}
\end{align*}
$$

In Eq. (15) $\bar{Q}=\left(Q_{j}+Q_{j+1}\right) / 2, \bar{A}=\left(A_{j}+A_{j+1}\right) / 2, \bar{R}=\left(R_{j}+R_{j+1}\right) / 2$. Suffixes $j$ and $j+1$ are the tabs of upriver and downriver cross sections. The values of $\mathrm{Q}_{\mathrm{j}}$ and $\mathrm{Z}_{\mathrm{j}}$ of each cross section can be obtained by Equations (14) and (15).

Replacing hydraulic radius with cross-sectional average water depth, then Eq.(15) will be changed as

$$
\begin{equation*}
Z_{j}=Z_{j+1}+\frac{1}{2 g}\left(\frac{Q_{j+1}^{2}}{A_{j+1}^{2}}-\frac{Q_{j}^{2}}{A_{j}^{2}}\right)+\frac{n^{2} \bar{Q}^{2}}{\bar{A}^{2} \bar{H}^{4 / 3}} \Delta x \tag{16}
\end{equation*}
$$

In the following the differences of water level will be inquired into further by two computation examples.

### 3.1 Computation of water level in natural river

The Nansha hydroelectric power station is located at the middle reaches of Honghe River, in Yuanxian county, Yunnan province. It's a canyon-reservoir and the river valley is narrow. Its width is mainly in the range of 80 m to 100 m . There are many rapids along the river, but there is no concentrated fall. The mean gradient of the river course is $1.17 \%$.In the natural situation, the
roughness coefficient is between 0.03 and 0.05 .
$\mathrm{B} / \mathrm{H}$ and mean errors of calculating water-level by Eq.(16) under three different discharge of $\mathrm{Q}=1000 \mathrm{~m}^{3} / \mathrm{s}, \mathrm{Q}=2870 \mathrm{~m}^{3} / \mathrm{s}, \mathrm{Q}=5470 \mathrm{~m}^{3} / \mathrm{s}$ are shown in Tab. 4 and Fig. 8.

As it is shown, $\mathrm{B} / \mathrm{H}$ differs from each other greatly, and the bigger the discharge is, the smaller $\mathrm{B} / \mathrm{H}$ is. According to Fig. 8, the water level calculated by Eq.(15) is lower than the one by Eq.(16). In addition, the larger the discharge is, the bigger the error is. When the discharge is $2870 \mathrm{~m}^{3} / \mathrm{s}$, $\mathrm{B} / \mathrm{H}$ varies from $24 \sim 36$ and the water-level error is in the range of 0.06 m to 0.25 m . This can't be ignored in the water-level computation. In one word, it needs treating cautiously that taking place of hydraulic radius with cross-sectional average water depth.

Tab. 4 The error of water-level computed by Eq. (16)

| Discharge $/ \mathrm{m}^{3} . \mathrm{s}^{-1}$ | 1000 | 2870 | 5470 |
| :--- | :--- | :--- | :--- |
| B/H | $28 \sim 45$ | $24 \sim 36$ | $16 \sim 22$ |
| The mean error of <br> water-level $/ \mathrm{m}$ | -0.04 | -0.11 | -0.23 |



Fig. 8 water-level calculating errors

### 3.2 Computation of backwater in reservoir

The Baihe hydroelectric power station is located at the trunk reach of Hanjiang River, between Mahu Town Baihe county of Shanxi province and Jiahe Town Yunxi county of Hubei province. Baihe Reservoir is a channel-type reservoir, whoes width is mainly in the range of 250 m to 400 m . The mean gradient of natural river is $0.6 \%$ and the roughness coefficient is between 0.03 and 0.038 .

The normal water level of Baihe Reservoir is 194.23 m . The backwater caused by reservoir will affect 7 towns along Hanjiang River upstream of station. In order to confirm the scale of immigrants, ground expropriation and the protecting projects, the backwater must be caculated. And the losses of submergence will be obtained by the backwater level curve ${ }^{[9]}$. The calculating results of flood water level in Baihe Reservoir are shown in Tab.5.

Tab. 5 Contrast of results by Eq. (15) and Eq. (16)

|  | Distance from the |  |  | 229 | $\mathrm{m}^{3} / \mathrm{s}$ |  | $\mathrm{m}^{3} / \mathrm{s}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | dam/km | Eq.(14) | Eq.(15) | Eq.(14) | Eq.(15) | Eq.(14) | Eq.(15) |
| Shuhekou (T1) | 39.77 | 207.82 | 207.55 | 211.54 | 211.25 | 213.91 | 213.56 |
| Xianhekou (T13) | 33.72 | 206.02 | 205.79 | 209.79 | 209.52 | 212.14 | 211.83 |
| Latna railway station (T24) | 28.03 | 203.64 | 203.43 | 207.19 | 206.93 | 209.46 | 209.17 |
| Yueritan (T59) | 9.11 | 197.47 | 197.39 | 200.05 | 199.94 | 202.17 | 202.06 |
| Shibaogoukou (T70) | 3.54 | 195.54 | 195.5 | 197.53 | 197.49 | 199.57 | 199.52 |
| Location of Baihe dam (T78) | 0.00 | 194.23 | 194.23 | 195.78 | 195.78 | 197.88 | 197.88 |
| Water-level mean error in whole reservoir/ m |  | -0.14 |  | -0.17 |  | -0.19 |  |
| Mean B/H in whole reservoir |  | 17~28 |  | 14~25 |  | 13~23 |  |

According to Tab. 5, the water level obtained by Eq. (16) is lower than the one by Eq.(15) under the same discharge. Apart from this, the larger the discharge is, the bigger the difference is. For example, the differences at Shuhekou (T1) are $0.27 \mathrm{~m}, 0.29 \mathrm{~m}$ and 0.35 m under three different discharges of $\mathrm{Q}=16900 \mathrm{~m}^{3} / \mathrm{s}, \mathrm{Q}=22900 \mathrm{~m}^{3} / \mathrm{s}, \mathrm{Q}=26400 \mathrm{~m}^{3} / \mathrm{s}$. The mean water level errors of the whole reservoir section are: $-0.14 \mathrm{~m},-0.17 \mathrm{~m}$ and -0.19 m 。

It can be seen from above that using Eq.(16) in water-level computation can cause great error. Say it in another way, substitution cross-sectional average water depth $(\mathrm{B} / \mathrm{H})$ for hydraulic radius(R) will cause water level lower than reality, the site of the pinch-out point will nearer to the dam. As a result, it will make submerging area and losses smaller, which is not able to give right directions to immigrants and protecting projects.

## 4. CONCLUSIONS AND DISCUSSION

As all know, hydraulic radius is usually replaced by cross-sectional average water depth in a certain cross section when $\mathrm{B} / \mathrm{H}$ is bigger than a certain value in hydraulic calculations. Sometimes we even don't care about the limitation of B/H. In fact, the simplification will bring error. Based on different cross sections, value-taking errors of hydraulic radius are studied in this paper. And the errors in water level calculating have been analyzed by two practical examples. As a result, some conclusions and suggestions are obtained as follows:
(1) As for a regular cross section, if the error isn't big than $5 \%$, it will be feasible to adopt $\mathrm{B} / \mathrm{H}$ as hydraulic radius when $\mathrm{B} / \mathrm{H}$ is bigger than 40 in rectangular section, or $\mathrm{B} / \mathrm{H}$ is bigger than 12 in an isosceles triangular one. In addition, the error is related with not only $B / H$ but also $b / B$ in an isosceles trapezoid section.
(2) In natural river, cross section couldn't be described generally by a fixed $B / H$, and $B / H$ may differ from each other greatly under different water levels for the same cross section. So there is no certain relationship between $\mathrm{B} / \mathrm{H}$ and relative error. The view is deserved to be suspected that it's possible to control the error into a certain range when $\mathrm{B} / \mathrm{H}$ is bigger than a certain value. Of course, it's necessary for roles of the relative error investigation to extend to different cross sections in different river.
(3) In practice, not only in natural river but also in reservoir, the error caused by replacing hydraulic radius with cross-sectional average water depth can't be ignored. It will get a set of lower water surface than reality. The larger the discharge is, the bigger the error is. As a result, this make the estimation of the flooded area and the losses is less than it is in reality, which is not able to give right directions to work about immigrants in reservoir.
(4) As a result, it needs treating cautiously to take place of hydraulic radius with $\mathrm{B} / \mathrm{H}$. In order to improve the accuracy of computations, it's advised to use hydraulic radius directly when it's necessary.

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