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Multicarrier Microgrid Operation Model Using Stochastic Mixed Integer Linear Programming

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Abstract—The microgrid operation is addressed in this article based on a multicarrier energy hub. Natural gas, electricity, heating, cooling, hydrogen, carbon dioxide, and renewable energies are considered as the energy carriers. The designed microgrid optimizes and utilizes a wide range of resources at the same time including renewables, electrical storage, hybrid storage, heating-cooling storage, electric vehicles (EVs) charging station, power to gas unit, combined cooling-heating-power, and carbon capture-storage. The purpose is to reduce the environmental pollutions and operating costs. The resilience and flexibility of the energy hub is also improved. Vehicle to grid and fully-partial charge models are incorporated for EVs to improve the system resilience and supplying the critical loads following events. Different events are modeled to evaluate the system resilience. The model is expressed as a stochastic mixed integer linear programming problem. Both active and reactive powers are modeled. The microgrid is simulated under four different cases. The results show that the multitype energy storages reduce the annual cost of energy while the integrated charging station can decrease the load shedding.

Index Terms—CO₂ trading, electric vehicle charging station, multitype energy storage, power-to-gas (P2G), resilience.

NOMENCLATURE

Indices and sets

ac, ec, bo, sw, we, cap Index of absorption and electric chillers, boiler, solar water

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es, cs, hs, gs, CO₂s
 f, F
 kl, KL
 k, K
 s, S
 se, SE
 t, T
 vn, VN
Parameters
 α, β^{-1}
 BM
 Cap_{vn}
 $COP_{cs}, COP_{ac}, COP_{ec}$
 DS_{se}^f
 DRP_{up}, DRP_{down}
 $E^{ini}, E^{max}, E^{min}$
 FR^{max}, FR^{min}
 H_{bo}^{max}
 I_t, I_{STC}
 $L_{ea}, L_c, L_h, L_{com}$
 L_{er}
 $M^{ini}, M^{max}, M^{min}$
 pr_{drp}
 P_{sell}
 $P_{pin}^{se,t}, P_{gin}^{se,t}$
 P_{CO_2}
 $P_{se,t}^{se,t}$
 P_{qin}
 heater, water electrolyzer, and supercapacitor.
 Index of energy, cooling, heating, gas, and CO₂ storages.
 Index of faults, set of faults.
 Index of loads, set of loads.
 Index of polygon lines, set of polygon lines.
 Index of scenarios, set of scenarios.
 Index of seasons, set of seasons.
 Index of time intervals, set of time intervals.
 Index of vehicle, set of vehicles.
 Conversion factor of CO₂ and natural gas (kg/MWh).
 Big-M coefficient.
 Electric vehicle capacity (MWh).
 Coefficient of performance of cooling storage, absorption and electric chiller.
 Number of fault days in each season.
 Added or deducted active demand for shiftable loads (MW).
 Initial, max and min energy of storage (MWh).
 Maximum and minimum flow rate (kg/h).
 Maximum heating power of boiler (MW).
 Solar radiation intensity, irradiance intensity at standard condition.
 Electrical, cooling, heating, combi-national loads (MW).
 Electrical reactive load (MVar).
 Initial, maximum and minimum stored mass (kg).
 Cost coefficient of active shifted power.
 Price of selling CO₂ (\$/kg).
 Price of purchased active power, natural gas (\$/MWh).
 Price of CO₂ emission (\$/kg).
 Price of purchased reactive power, (\$/MVarh).

P_{pv}, P_w	Power of photovoltaic and wind units (MW).	$C_{se}^{se,f,s,t}, C_{ac}^{se,f,s,t}$	Generated cooling power by electric and absorption chillers (MW).
$P_{ch}^{max}, P_{dis}^{max}$	Maximum active power for charging and discharging of battery, heating and cooling storage (MW).	$C_{cs,ch}^{se,f,t}, C_{cs,dis}^{se,f,t}$	Charging and discharging cooling power of cooling storage tank (MW).
P_{STC}	Rated power of PV panel (MW).	$E_{vn}^{se,f,t}, E_{vn}^{se,f,leave}$	Stored energy in time slot t and leaving time from station (MWh).
Pro	Scenario probability.	$E_{es}^{se,f,t}, E_{cap}^{se,f,s,t}$	Stored energy in battery and supercapacitor (MWh).
P_r	Rated output power (MW).	FR_{CO_2s}, FR_{gS}	Flow rate of CO ₂ and natural gas storage tanks (kg/h).
P_{st}, P_{sh}	Start-up and shut-down price of CHP (\$).	$FR_{sell}^{se,f,s,t}, G_{P2G}^{se,f,s,t}$	CO ₂ selling (kg/h).
$P_{vn}^{max}, Q_{es}^{max}$	Maximum power of EV (MW). Maximum reactive power for battery (MVar).	$H_{chp}^{se,f,t}, H_{bo}^{se,f,s,t}$	Flow rate of H ₂ and natural gas regeneration (kg/h).
S_{chp}^A	Apparent power of CHP (MVA).	$H_{ac}^{se,f,s,t}, H_{sw}^{se,f,s,t}$	Heating power of CHP and boiler (MW).
T_t	Ambient temperature (°C).	$H_{com}^{se,f,s,t}$	Generated heating by absorption chiller and solar water heater (MW).
$v_t, v_{in}, v_{out}, v_r$	Wind speed, cut in and cut out speeds, rated speed (m/s).	$H_{hs,ch}^{se,f,t}, H_{hs,dis}^{se,f,t}$	Heating power of combinational load (MW).
ξ_p	Penalty coefficient.	$M_{CO_2s}^{se,f,t}, M_{gs}^{se,f,t}$	Charging and discharging heating power of heating storage tank (MW).
δ_{es}^{self}	Self-discharge of battery (%).	$P_{in}^{se,f,s,t}, Q_{in}^{se,f,s,t}$	Stored CO ₂ and natural gas in storage tanks (kg).
$\eta_{es}^{ch}, \eta_{es}^{dis}$	Charging and discharging efficiency of battery (%).	$P_{chp}^{se,f,t}, H_{chp}^{se,f,t}$	Input active (MW) and reactive (MVar) power.
$\eta_p^{chp}, \eta_h^{chp}, \eta_h^{bo}$	Electrical and heating efficiency of CHP and boiler (%).	$P_{cs}^{se,f,t}$	Active power and heating generated by CHP (MW).
η_{in}	Conversion efficiency of PV inverter.	$P_{cs,ch}^{se,f,t}, P_{cs,dis}^{se,f,t}$	The electrical power consumed by cooling storage (MW).
γ	Shiftable load factor.	$H_{bo}^{se,f,s,t}$	The electrical power for ice making ad melting by cooling storage (MW).
Δt	Duration of time interval (hour).	$P_{es,ch}^{se,f,t}, P_{es,dis}^{se,f,t}$	Heating power produced by CHP (MW).
Binary variables		$P_{cap}^{se,f,s,t}, P_{vn}^{se,f,t}$	Active power exchange of battery storage (MW).
u, x, y	Auxiliary variable for modeling the storages, CHP, supercapacitor.	$P_{com}^{se,f,s,t}, P_{ec}^{se,f,s,t}$	Active power of supercapacitor and electric vehicle (MW).
z	Auxiliary variable for modeling EV charging station.	$P_{we}^{se,f,s,t}, P_{cs}^{se,f,t}$	Input power of combinational load and electric chiller (MW).
Continuous variables		P_{DR}	Input power of water electrolyzer and cooling storage tank (MW).
C_{Pin}, C_{Qin}	Cost of purchased active and reactive powers (\$/year).	$Q_{in}^{se,f,s,t}, Q_{chp}^{se,f,t}$	New active loads after DRP (MW).
C_{Gin}, C_{CO_2}	Cost of purchased natural gas, CO ₂ emission (\$/year).	$Q_{es}^{se,f,t}$	Reactive power of electrical network, CHP (MVar).
$C_{chp}^{st \& sh}$	Start-up and shut-down annual cost of CHP (\$/year).	$\Omega_{kl}^{se,f,s,t}, \psi_{vn}^{se,f,t}$	Reactive power of battery storage (MVar).
C_{shed}^P, C_{EV}^P	Penalty cost of load shedding and EV partial charge (\$/year).		Amount of supplied load and EV charge (%).
$C_{shed}^{kl,se,f,s,t}$	Penalty cost of load shedding (\$).		
$C_{vn}^{se,f,t}$	Penalty cost to EV partial charge (\$).		
C_{sell}	Revenue of selling CO ₂ (\$).		
$C_{st}^{se,f,t}, C_{sh}^{se,f,t}$	Start-up and shut down cost of CHP in season se , fault f , and time slot t (\$).		
C_{DR}	Incentive cost for shiftable loads in DRP (\$/year).		
$CO_2^{se,f,s,t}, G_{in}^{se,f,t}$	CO ₂ emission and input natural gas (kg/h).		
$CO_2^{se,f,s,t}_{chp \& bo}$	CO ₂ produced by CHP and boiler (kg/h).		
$CO_2^{se,f,s,t}_{cap}$	Captured CO ₂ from CHP and boiler (kg/h).		
$CO_2^{se,f,s,t}_{P2G}$	Input flow rate of CO ₂ into P2G unit (kg/h).		

I. INTRODUCTION

A. Motivations of This Article

NOWADAYS, growing concerns about environmental and energy issues are encouraging efficient energy production and consumption systems. With respect to the energy efficiency and resilience, the integrated energy systems composed of

electrical, gas, and heating networks are attracting more attention. The multicarrier energy (MCE) systems directly influence the security and economic operation aspects of power systems. For example, the combined cooling, heating, and power (CCHP) enables the users to utilize multiple energies with about 60%–80% efficiency. The CCHP can reduce the pollutants produced by the conventional fossil fuel power plants [1]. The plug-in electric vehicles (PEVs) can also play a significant role in reducing the petrol consumption and operating costs, improving reliability, and supplying the loads following outages in order to improving the resilience [2]. The resilience shows the capability of the network to operate under extreme conditions caused by weather and natural disasters [3]. The above-mentioned items have motivated the authors to consider a multi-carried energy hub for microgrid resilience and operation.

B. Literature Survey and Contributions

The MCE systems have been investigated from different viewpoints such as topology of energy hubs, types of energy storages, combined effects of component, environmental impacts, carbon emission reduction strategies, and robust-resilience operation. In MCE, the energy hub is an interface between different energy systems playing the role of energy production, conversion and storage [4]. Moreover, energy hub is a multi-input/output unit and has the capability of assisting the energy management and optimization by combining and coupling multiple energy carriers [5].

The electricity, heating, cooling, and combinational hubs are the main energy hubs in such systems [4]. As well, some key components and sectors used in MCE systems are: thermal devices, multitype energy storages, combined heat and power, renewable resources, boilers, PEVs, and the charging stations. The heat energy storage is attracting interest due to its high efficiency, large capacity, and low cost [6]. The hybrid energy storage and PEV can return the stored energy to the hub in order to supplying the electrical appliances whenever needed. This can effectively improve the efficiency of renewables [7], [8].

The MCE systems have been extensively recognized as an efficient way of reducing carbon emission by promoting the integration of renewable energies [9]. The carbon tax policy [9], carbon emission caps [10], carbon emission trading [11], carbon capture and storage [12], methanation reaction and power-to-gas (P2G) technology [13] are the most popular methods in the reduction of carbon emission. The rapid development of P2G technology in recent years has enabled on-site capture and recycling of CO₂ using surplus of renewable energies [14], [15]. One of the best advantages of the combined MCE-P2G system is the onsite recycling of CO₂ and reducing the carbon emission without long-distance transportation of CO₂. The other important issue that can be dealt with the MCE hubs is the resilience. The MCE systems are proper facilities to improve the system resilience. The extreme weather events have increasingly affected power systems worldwide. The global attention to catastrophic consequences of such high impact rare events has promoted the concept of power system resilience [16]. With

respect to the above discussed items, it is concluded that various studies have been published about application of different energy carriers (electricity, gas, hydrogen, etc.) and various technologies (renewable, EV, storage, etc.) in the MCE hub. Moreover, various concepts such as resilience, CO₂ reduction, and robust operation have already been discussed. But none of them considered all of these subjects together in one model. This point is addressed in [Table I](#).

In order to address such research gaps, this article presents a resilient comprehensive model for microgrid operation based on multicarrier energy hub including electricity, gas, heating, cooling, hydrogen, methane, and CO₂. In actual, each of loads is supplied through different parallel paths that increase the system resilience. As well, the model utilizes various technologies including hybrid electrical storage, thermal storage, renewables, EV charging station, P2G, CCHP, and carbon capture-storage (CCS). The model enhances the system resilience by supplying the loads through various paths, minimizes CO₂ emission by capturing/ selling, and using carbon and reduces the operating cost.

The main contributions of the given model are summarized as follows:

- 1) The model includes various energy carriers including electricity, natural gas, heating, cooling, hydrogen, and CO₂; thus, all of the loads are supplied multidirectionally.
- 2) The model utilizes many equipment comprising hybrid storage, thermal storage, renewables, EV charging station, P2G, CCHP, carbon capture and storage, boiler, absorption chiller, and electrical chiller. Each equipment deals with one or more energy carrier.
- 3) The partial charge capability is carried out for electric vehicles in order to supply the critical loads under faulty condition.
- 4) The CO₂ generated by CHP and boiler is captured and used for selling, monetization, and natural gas regeneration in the P2G unit.
- 5) The optimal operation pattern is scheduled for all equipment and both active/reactive powers are incorporated.
- 6) Uncertainty of loads and renewables (e.g., solar PV, wind, solar water heater) are modeled.
- 7) The model aims to enhance the system resilience, minimize CO₂ emissions and reduce the operating costs.

The main contributions of current research against the previous ones are listed in [Table I](#).

II. PROPOSED FRAMEWORK DESCRIPTION

A. Multicarrier Energy Systems

MCE system can be modeled with the energy hub concept, which is considered as a unit where multiple energy carriers can be converted, stored, and distributed. The MCE system can have multiple input and output ports, the input ports are usually connected to electricity, natural gas, district heat, or other types of energy, while the output ports can provide power, heat, cool, natural gas, and multienergy services, simultaneously.

The management strategy in a typical MCE system is shown by [Fig. 1](#). The input energies of this system are supplied by

TABLE I
COMPARING THE CURRENT ARTICLE WITH THE LITERATURE

Ref. No	Year	Demand type	Storage type	CHP modelling	EV charging station	CO ₂ reduction	The other items
		Electrical+ Heat+ cooling+ combinational (E&H)	ES+HS+CS +GS+CO ₂ S	YES	YES	P2G system + emission cost	Resilience analysis under natural gas interruption, islanding mode and hurricane landfall events+ Penalty cost of load shedding
[17]	2018	Electrical+ Heat	ES+GS+HS	NO	NO	NO	NO
[18]	2019	Electrical+ Heat+ cooling	ES	NO	NO	NO	NO
[3]	2018	Electrical+ Gas	GS	NO	NO	NO	load shedding cost to enhancement of resilience
[4]	2018	Electrical+ Heat	ES+HS	NO	NO	NO	NO
[5]	2018	Electrical+ Heat	ES+HS	NO	NO	NO	NO
[19]	2018	Electrical+ Heat+ cooling	ES+HS	NO	NO	Emission cost	NO
[20]	2019	Electrical+ Heat+ combinational (E&H)	ES+HS	YES	NO	NO	Resilience analysis under islanding mode + optimization of load shedding cost
[9]	2019	Electrical+ Heat+ cooling	CS+HS	NO	NO	Carbon tax	NO
[21]	2018	Electrical+ Heat+ cooling	ES+HS+CS+ GS	NO	NO	P2G system + carbon tax	NO
[15]	2017	Electrical+ Heat+ Gas	ES+HS+GS	NO	NO	P2G system + emission cost	NO
[22]	2018	Electrical+ Heat	CO ₂ S+GS	NO	NO	P2G system	NO
[23]	2018	Electrical+ Heat	Electrical+ Heat	NO	NO	NO	Resilience analysis under natural gas interruption, islanding mode and hurricane landfall event
Current paper	-----	Electrical+ Heat+ cooling+ combinational (E&H)	ES+HS+CS +GS+CO ₂ S	YES	YES	P2G system + emission cost	Resilience analysis under natural gas interruption, islanding mode and hurricane landfall events+ Penalty cost of load shedding

The models given by literature (ES = battery energy storage, GS = natural gas storage, HS = heating storage, CS = cooling storage, CO₂S = CO₂ storage)



Fig. 1. Management strategy in a typical MCE system.

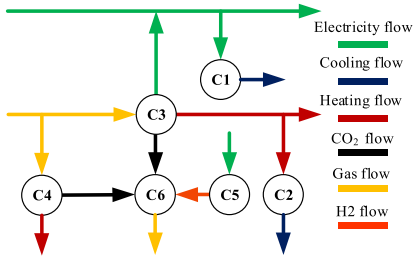


Fig. 2. Interactions between different energy carriers through energy converters.

electrical and gas networks and the outputs are electrical, cooling, heating, and combinational loads. The interaction between different energy carriers through the main energy converters (C1 to C6) is shown by Fig. 2. The converters C1 and C2 consume the electricity and heating, respectively, and produce cooling energy. The generated cooling is appropriate with their coefficient of performance. These converters are known as electrical and absorption chillers. The converters C3 and C4 (i.e., CHP and boiler) consume natural gas in order to generate electricity and heating simultaneously. The C5 is a water electrolyzer that consumes electricity and produces hydrogen. In C6, the released CO₂ by CHP and boiler is combined with hydrogen to produce the natural gas. This converter is the methanation unit. Combination of C5 and C6 is named P2G unit.

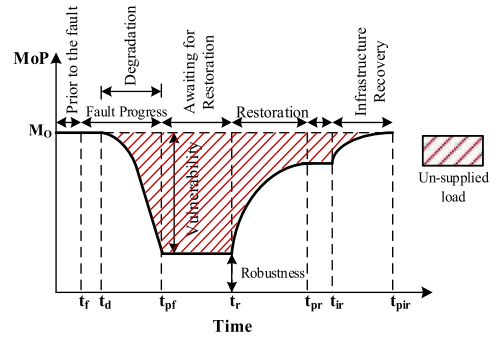


Fig. 3. Typical resilience curve [16].

B. Carbon Capture Storage and Natural Gas Recycle

Carbon capture and storage is one of the important methods for environmental pollution reduction. This technology consists of three units including capture unit, compression unit, and storage tank. In order to generating the natural gas, carbon capture unit delivers CO₂ to P2G unit. The P2G unit consists of two units including water electrolyze and methanation units. The P2G uses CO₂ and hydrogen to produce methane (natural gas).

C. Resilience and System Faults

A typical resilience curve for a given measure of performance (MoP) associated with an extreme event is shown by Fig. 3. All of the processes from prefault, recovery, and postfault are expressed in the figure. Once the fault occurs (t_f) in the network, the system performance starts to degrade and its intensity depends on the fault type and location. The ability of network to supply the critical loads under events is assumed as network robustness. In this article, multiple and different types of faults are imposed on the network to evaluate the resilience and robustness of the model. The electrical network outage, natural gas network outage, earthquake event, and destruction of solar and wind

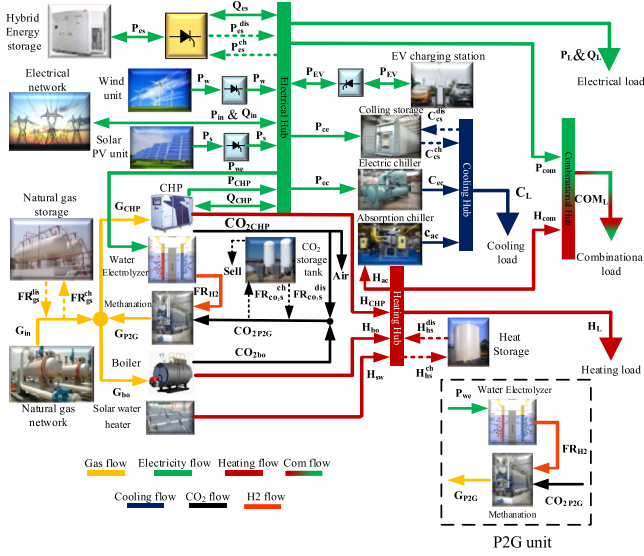


Fig. 4. Proposed microgrid based on MCE.

units, outage of CHP, and outage of boiler are considered for network resilience assessment.

D. Proposed Microgrid Based on MCE

Fig. 4 shows the proposed microgrid based on MCE system. This model is very complex, which increases the costs on the one hand and improves the resilience and reliability on the other hand. The model may also be simplified to have the grids with less cost as well as less resilience and reliability. It often depends on the importance and priority of the loads to select the topology of the grid. The electricity and natural gas are main inputs to the microgrid and the electrical, combinational, and cooling-heating loads are the outputs. The microgrid can sell active power to the network. The reactive power of microgrid is supplied by the electrical network, hybrid battery-capacitor storage, and CHP. The renewables are solar PV, solar water heater, and wind units. Multitype energy storages are considered to enhance the flexibility and reliability. These storages are hybrid battery-capacitor, heating-cooling, CO₂, and natural gas storage. The performance of these energy storages is on different energy carriers, for this reason, the operation of them under small load variations is independent of each other. As a result, it is not efficient to replace all of these small storage units with one large-scale storage system which is installed on one of the energy carriers.

The hybrid energy storage can absorb the stochastic behavior of renewable energies. The natural gas storage has an important role for supplying gas when the input gas pipeline is not available.

The CHP and boiler are the heating resources and the electrical and absorption chillers are the cooling resources. The cooling storage works based on ice making and melting mechanism. The generated CO₂ by CHP and boiler can be released into the air, sold, stored or it may be used for natural gas regeneration in P2G unit. The P2G comprises the water electrolyzer for H₂ generation and Methanation units for producing Methane gas (CH₄). The

EVs charging station is also considered with capability of fully-partial charge operation.

III. PROBLEM FORMULATION

A. Objective Function

The objective function of the problem is the annual operating cost that is shown by (1) that is summation of purchased active and reactive power costs, purchased gas cost, CO₂ emission cost, load shedding cost, penalty cost of EV partial charge, and cost of CHP start up-shut down minus the revenue achieved from CO₂ selling. These items are listed through (2) to (11), respectively. Start-up and shut down cost of CHP in season is linearized by (12) [20] and details of (7) and (8) are expressed by (13) and (14)

$$OF = C_{P_{in}} + C_{Q_{in}} + C_{G_{in}} + C_{CO_2} + C_{CHP}^{st\&sh} + C_{shed}^p + C_{EV}^p - C_{sell}^{CO_2} \quad (1)$$

$$C_{P_{in}} = \sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{s=1}^S \left[\sum_{t=1}^T P_{in}^{se,f,s,t} \cdot \Delta t \cdot p_{pin}^{se,t} \right] \Pr o^s \right) \right) \quad (2)$$

$$C_{Q_{in}} = \sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{s=1}^S \left[\sum_{t=1}^T Q_{in}^{se,f,s,t} \cdot \Delta t \cdot p_{qin}^{se,t} \right] \Pr o^s \right) \right) \quad (3)$$

$$C_{G_{in}} = \sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{s=1}^S \left[\sum_{t=1}^T G_{in}^{se,f,s,t} \cdot \beta \cdot \Delta t \cdot p_{gin}^{se,t} \right] \Pr o^s \right) \right) \quad (4)$$

$$C_{CO_2} = \sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{s=1}^S \left[\sum_{t=1}^T CO_2^{se,f,s,t} \cdot \Delta t \cdot p_{CO_2} \right] \Pr o^s \right) \right) \quad (5)$$

$$C_{CHP}^{st\&sh} = \sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{t=1}^T C_{st}^{se,f,t} + C_{sh}^{se,f,t} \right) \right) \quad (6)$$

$$C_{shed}^p = \sum_{kl}^{KL} \left(\sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{s=1}^S \left[\sum_{t=1}^T C_{shed}^{kl,se,f,s,t} \cdot \Pr o^s \right] \right) \right) \right) \quad (7)$$

$$C_{EV}^p = \sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{t=1}^T \left(\sum_{vn=1}^{VN} C_{vn}^{se,f,t} \right) \right) \right) \quad (8)$$

$$C_{sell} = \sum_{se=1}^{SE} \left(\sum_{f=1}^F D_{se}^f \left(\sum_{s=1}^S \left[\sum_{t=1}^T FR_{sell}^{se,f,s,t} \cdot \Delta t \cdot p_{sell} \right] Pr o^s \right) \right) \quad (9)$$

$$CO_2^{se,f,s,t} = CO_{2chp\&bo}^{se,f,s,t} - \left(CO_{2P2G}^{se,f,s,t} + FR_{CO_2s}^{se,f,s,t} \right) \quad (10)$$

$$CO_{2chp\&bo}^{se,f,s,t} = \left(P_{chp}^{se,f,t} / \eta_P^{chp} + H_{chp}^{se,f,t} / \eta_H^{chp} + H_{bo}^{se,f,s,t} / \eta_H^{bo} \right) \cdot \alpha \quad (11)$$

$$\begin{cases} C_{sh}^{se,f,t} \geq P_{sh} \cdot (x^{se,f,t-1} - x^{se,f,t}) & \forall t \neq 1 \\ C_{st}^{se,f,t} \geq P_{st} \cdot (x^{se,f,t} - x^{se,f,t-1}) & \forall t \neq 1 \\ C_{sh}^{se,f,t} \geq P_{sh} \cdot (x^{se,f,T} - x^{se,f,t}) & \forall t = 1 \\ C_{st}^{se,f,t} \geq P_{st} \cdot (x^{se,f,t} - x^{se,f,T}) & \forall t = 1 \end{cases} \quad (12)$$

$$C_{shed}^{kl,se,f,s,t} = (1 - \Omega_{kl}^{se,f,s,t}) \cdot L_{kl}^{se,s,t} \cdot \Delta t \cdot \xi_p \cdot p_{pin}^{se,t} \quad (13)$$

$$C_{vn}^{se,f,t} = (1 - \psi_{vn}^{se,f,t}) \cdot cap_{vn} \cdot \xi_p \cdot p_{pin}^{se,t} \quad (14)$$

B. Power Balance Constraints in Energy Hubs

The power balance constraints related to electrical, heating, cooling and combinational hubs for faulty time periods ($f \neq 1$) and the other time intervals (healthy periods) ($f = 1$) is expressed through (15) to (20). It is noteworthy that the supplying the load must always be greater than the critical load, where $(1-\Omega)$ is expressed as percentage of unsupplied load. The electrical hub is modeled by (15) and (16)

$$\begin{cases} P_{in}^{se,f,s,t} + P_{pv}^{se,f,s,t} + P_w^{se,f,s,t} + P_{chp}^{se,f,t} + P_{cap}^{se,f,s,t} + P_{es,dis}^{se,f,t} - P_{es,ch}^{se,f,t} \\ - \sum_{vn=1}^{VN} P_{vn}^{se,f,t} - P_{com}^{se,f,s,t} - P_{ec}^{se,f,s,t} - P_{we}^{se,f,s,t} - P_{cs}^{se,f,t} \\ \begin{cases} \geq \Omega_a^{se,f,s,t} \cdot L_{ea}^{se,s,t} & \forall f \neq 1 \\ = L_{ea}^{se,s,t} & \forall f = 1 \end{cases} \end{cases} \quad (15)$$

$$Q_{in}^{se,f,s,t} - Q_{chp}^{se,f,t} - Q_{es}^{se,f,t} \begin{cases} \geq \Omega_{ea}^{se,f,s,t} \cdot L_{er}^{se,s,t} & \forall f \neq 1 \\ = L_{er}^{se,s,t} & \forall f = 1 \end{cases} \quad (16)$$

The heating hub is modeled by (17) and cooling is specified in (18)

$$H_{chp}^{se,f,t} + H_{bo}^{se,f,s,t} + H_{sw}^{se,f,s,t} + H_{hs,dis}^{se,f,t} - H_{hs,ch}^{se,f,t} - H_{ac}^{se,f,s,t} - H_{com}^{se,f,s,t} \begin{cases} \geq \Omega_h^{se,f,s,t} \cdot L_h^{se,s,t} & \forall f \neq 1 \\ = L_h^{se,s,t} & \forall f = 1 \end{cases} \quad (17)$$

$$C_{ec}^{se,f,s,t} + C_{ac}^{se,f,s,t} + C_{cs,dis}^{se,f,t}$$

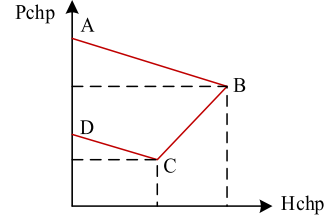


Fig. 5. Typical feasible operation region of a CHP unit.

$$- C_{cs,ch}^{se,f,t} \begin{cases} \geq \Omega_c^{se,f,s,t} \cdot L_c^{se,s,t} & \forall f \neq 1 \\ = L_c^{se,s,t} & \forall f = 1 \end{cases} \quad (18)$$

The combinational hub is defined in (19)

$$P_{com}^{se,f,s,t} + H_{com}^{se,f,s,t} \begin{cases} \geq \Omega_{com}^{se,f,s,t} \cdot L_{com}^{se,s,t} & \forall f \neq 1 \\ = L_{com}^{se,s,t} & \forall f = 1 \end{cases} \quad (19)$$

C. CHP Modeling

The typical feasible operation region of CHP unit is shown by Fig. 5 that can be formulated by the set of linear equations (20) to (25) [20], when $x = 0$, the output apparent electrical power and heat of the CHP unit are zero. Meanwhile, the apparent power of CHP is limited by (26). In order to linearizing this constraint, the hexagon approximations of a circle used and expressed by (27) [24]

$$P_{chp}^{se,f,t} - P_{chp}^A - \frac{P_{chp}^A - P_{chp}^B}{H_{chp}^A - H_{chp}^B} \left(H_{chp}^{se,f,t} - H_{chp}^A \right) \leq 0 \quad (20)$$

$$P_{chp}^{se,f,t} - P_{chp}^B - \frac{P_{chp}^B - P_{chp}^C}{H_{chp}^B - H_{chp}^C} \left(H_{chp}^{se,f,t} - H_{chp}^B \right) \geq - (1 - x^{se,f,t}) \cdot BM \quad (21)$$

$$P_{chp}^{se,f,t} - P_{chp}^C - \frac{P_{chp}^C - P_{chp}^D}{H_{chp}^C - H_{chp}^D} \left(H_{chp}^{se,f,t} - H_{chp}^C \right) \geq - (1 - x^{se,f,t}) \cdot BM \quad (22)$$

$$0 \leq H_{chp}^{se,f,t} \leq H_{chp}^B \cdot x^{se,f,t} \quad (23)$$

$$0 \leq P_{chp}^{se,f,t} \leq P_{chp}^A \cdot x^{se,f,t} \quad (24)$$

$$0 \leq S_{chp}^{se,f,t} \leq S_{chp}^A \cdot x^{se,f,t} \quad (25)$$

$$(P_{chp}^{se,f,t})^2 + (Q_{chp}^{se,f,t})^2 \leq (S_{chp}^A)^2 \quad (26)$$

$$P_{chp}^{se,f,t} \cdot \cos \frac{(2k-1)\pi}{K} + Q_{chp}^{se,f,t} \cdot \sin \frac{(2k-1)\pi}{K} - S_{chp}^A \cdot \cos \frac{\pi}{K} \leq 0 \quad (27)$$

D. Chiller and Boiler Constraints

The electric and absorption chillers consume electricity and heat and produce cooling power. The relationship between input and output powers of these components are indicated by (28), (29) [25]. The output heating power of boiler is limited by (30)

$$C_{ec}^{se,f,s,t} = P_{ec}^{se,f,s,t} \cdot COP_{ec} \quad (28)$$

$$C_{ac}^{se,f,s,t} = H_{ac}^{se,f,s,t} \cdot COP_{ac} \quad (29)$$

$$0 \leq H_{bo}^{se,f,s,t} \leq H_{bo}^{max} \quad (30)$$

E. Energy Storages Devices Constraints

1) *Hybrid, Heating, and Cooling Energy Storages:* The hybrid energy storage can therefore absorb the stochastic behavior of renewable energies. The supercapacitor operation is modeled by (31)–(35). The battery energy storage behavior is modeled by (36)–(42), where (42) shows the reactive power absorption or injection by battery [25]. The cooling and heating storage constraints are similar to (36)–(41) and the similar operation is modeled for them. The electrical power to ice making or melting (charging and discharging) is expressed by (43), and (44) and (45) represent the output cooling power of ice storage [25]

$$P_{cap}^{se,f,s,t} = y_c^{se,f,s,t} \cdot ((P_{pv}^{se,f,s,t} + P_w^{se,f,s,t}) - (P_{pv}^{se,f,s,t} + P_w^{se,f,s,t})) \quad (31)$$

$$E_{cap}^{se,f,s,t} = E_{cap}^{ini} + P_{cap}^{se,f,s,t} \cdot \Delta t \quad \forall t = 1 \quad (32)$$

$$E_{cap}^{se,f,s,t} = E_{cap}^{se,f,s,t-1} + P_{cap}^{se,f,s,t} \cdot \Delta t \quad \forall t \neq 1 \quad (33)$$

$$E_{cap}^{se,f,s,T} = E_{cap}^{ini} \quad (34)$$

$$E_{cap}^{min} \leq E_{cap}^{se,f,s,t} \leq E_{cap}^{max} \quad (35)$$

$$E_{es}^{se,f,t} = E_{es}^{ini} (1 - \delta_{es}^{self}) + (P_{es,ch}^{se,f,t} \cdot \eta_{es}^{ch} - P_{es,dis}^{se,f,t} / \eta_{es}^{dis}) \Delta t \quad \forall t = 1 \quad (36)$$

$$E_{es}^{se,f,t} = E_{es}^{se,f,t-1} (1 - \delta_{es}^{self}) + (P_{es,ch}^{se,f,t} \cdot \eta_{es}^{ch} - P_{es,dis}^{se,f,t} / \eta_{es}^{dis}) \Delta t \quad \forall t \neq 1 \quad (37)$$

$$E_{es}^{se,f,T} = E_{es}^{ini} \quad (38)$$

$$E_{es}^{min} \leq E_{es}^{se,f,t} \leq E_{es}^{max} \quad (39)$$

$$0 \leq P_{es,ch}^{se,f,t} \leq P_{es,ch}^{max} \cdot u_{es}^{se,f,t} \quad (40)$$

$$0 \leq P_{es,dis}^{se,f,t} \leq P_{es,dis}^{max} \cdot (1 - u_{es}^{se,f,t}) - Q_{es}^{max} \cdot u_{es}^{se,f,t} \leq Q_{es}^{se,f,t} \leq Q_{es}^{max} \cdot u_{es}^{se,f,t} \quad (42)$$

$$P_{cs}^{se,f,t} = P_{cs,ch}^{se,f,t} + P_{cs,dis}^{se,f,t} \quad (43)$$

$$C_{cs,ch}^{se,f,t} = P_{cs,ch}^{se,f,t} \cdot COP_{cs} \quad (44)$$

$$C_{cs,dis}^{se,f,t} = P_{cs,dis}^{se,f,t} \cdot COP_{cs} \quad (45)$$

2) *CO₂ Storage Constraints:* The produced CO₂ by CHP and boiler can be stored in CO₂ storage tank and it can be used by P2G unit in order to recycling the natural gas. Behavior of this storage is modeled by (46)–(50)

$$M_{CO_2s}^{se,f,s,t} = M_{CO_2s}^{ini} + (FR_{CO_2}^{se,f,s,t} - FR_{sell}^{se,f,s,t}) \cdot \Delta t \quad \forall t = 1 \quad (46)$$

$$M_{CO_2s}^{se,f,s,t} = M_{CO_2s}^{se,f,s,t-1} + (FR_{CO_2s}^{se,f,s,t} - FR_{sell}^{se,f,s,t}) \cdot \Delta t \quad \forall t \neq 1 \quad (47)$$

$$M_{CO_2s}^{se,f,s,T} = M_{CO_2s}^{ini} \quad (48)$$

$$-M \cdot FR_{CO_2s}^{max} \leq FR_{CO_2s}^{se,f,s,t} \cdot \Delta t \leq FR_{CO_2s}^{max} \cdot BM \quad (49)$$

$$M_{CO_2s}^{min} \leq M_{CO_2s}^{se,f,s,t} \leq M_{CO_2s}^{max} \quad (50)$$

3) *Natural Gas Storage Constraints:* The natural gas storage tank has an important role to system gas supply when the input natural gas from natural gas network is cut off. Equations (51)–(54) show natural gas storage tank constraints

$$M_{gs}^{se,f,t} = M_{gs}^{ini} + FR_{gs}^{se,f,t} \cdot \Delta t \quad \forall t = 1 \quad (51)$$

$$M_{gs}^{se,f,t} = M_{gs}^{se,f,t-1} + FR_{gs}^{se,f,t} \cdot \Delta t \quad \forall t \neq 1 \quad (52)$$

$$M_{gs}^{se,f,T} = M_{gs}^{ini} \quad (53)$$

$$-BM \cdot FR_{gs}^{max} \leq FR_{gs}^{se,f,t} \leq FR_{gs}^{max} \cdot BM \quad (54)$$

$$M_{gs}^{min} \leq M_{gs}^{se,f,t} \leq M_{gs}^{max} \quad (55)$$

F. P2G Modeling

The CO₂ balance constraint is expressed by (56). The captured CO₂ is smaller or equal to produced CO₂ by CHP and boiler as shown by (57), (58) [25]. In order to having a proper performance of P2G, each 2.7 kg of CO₂ is combined with 0.5 kg of H₂ to make 1 kg of CH₄. Thus, CO₂ to hydrogen ratio is 5.3. The water electrolyzer unit consumes 0.05 MWh to produce 1 kg of hydrogen [13]. These constraints are modeled by (59)–(62)

$$CO_{2P2G}^{se,f,s,t} = CO_{2cap}^{se,f,s,t} - FR_{CO_2s}^{se,f,t} - FR_{sell}^{se,f,s,t} \quad (56)$$

$$CO_{2cap}^{se,f,s,t} \leq CO_{2chp\&bo}^{se,f,s,t} \quad (57)$$

$$CO_{2chp\&bo}^{se,f,s,t} = \left(P_{chp}^{se,f,t} / \eta_P^{chp} + H_{chp}^{se,f,t} / \eta_H^{chp} + H_{bo}^{se,f,s,t} / \eta_H^{bo} \right) \cdot \alpha \quad (58)$$

$$CO_{2P2G}^{se,f,s,t} = 5.4 FR_{H_2}^{se,f,s,t} \quad (59)$$

$$CO_{2P2G}^{se,f,s,t} = 2.7 G_{P2G}^{se,f,s,t} \quad (60)$$

$$P_{we}^{se,f,s,t} = 0.05 FR_{H_2}^{se,f,s,t} \quad (61)$$

$$G_{in}^{se,f,s,t} + G_{P2G}^{se,f,s,t} - FR_{gs}^{se,f,t} = (P_{chp}^{se,f,t} / \eta_P^{chp} + H_{chp}^{se,f,t} / \eta_H^{chp} + H_{bo}^{se,f,s,t} / \eta_H^{bo}) \cdot \beta^{-1} \quad (62)$$

G. EV Charging Station Modeling

The vehicle entrance pattern to the charging stations is usually achieved from the historical data. In this article, it is assumed that each EV can stay in the station from 15 min to 1 h and station operator can charge or discharge the EV at each time interval (15 min). Finally, the EV leaves the station fully or partially charged. The vehicle owner may receive an incentive in case of leaving with partial charge (this is the penalty cost for station operator). The station decision variables such as stopping time

TABLE II
FAULTS SPECIFICATIONS

Fault No	Fault occurrence time periods				Fault modeling
	Spring	Summer	Autumn	Winter	
1	Without fault				Safe operation
2	68-85	48-65	70-96	1-31	$P_{in}^{se,f,t} = Q_{in}^{se,f,t} = 0$
3	24h	24h	24h	24h	
4	39-64	25-40	63-79	17-33	$P_{pv}^{se,f,t} = P_w^{se,f,t} = 0$
5	24h	24h	24h	24h	
6	70-89	77-96	3-18	74-96	$P_{chp}^{se,f,t} = Q_{chp}^{se,f,t} = H_{chp}^{se,f,t} = 0$
7	24h	24h	24h	24h	
8	1-30	1-10	1-8, 81-96	1-25, 74-96	$H_{bo}^{se,f,t} = 0$
9	24h	24h	24h	24h	
10	83-96	13-23, 63-82	16-24, 66-96	18-29, 63-91	$G_{in}^{se,f,t} = 0$

TABLE III
MICROGRID DEVICES CHARACTERISTICS

Hybrid battery- capacitor storage	Heating storage	Cooling storage	CO ₂ and natural gas storages
$E_{cs}^{min} = 0$	$E_{hs}^{min} = 0$	$E_{cs}^{min} = 0$	$M_{CO_2}^{min} = 0$
$E_{cs}^{max} = 3.8$	$E_{hs}^{max} = 2.8$	$E_{cs}^{max} = 1.8$	$M_{CO_2}^{max} = 5000$
$E_{cs}^{min} = 0$	$E_{hs}^{min} = 0$	$E_{cs}^{min} = 0$	$M_{CO_2}^{min} = 0$
$P_{cs,dis}^{max} = 0.8$	$H_{hs,ch}^{max} = 0.8$	$C_{cs,ch}^{max} = 0.7$	$FR_{CO_2}^{max} = 800$
$P_{cs,dis}^{max} = 0.9$	$H_{hs,dis}^{max} = 0.8$	$C_{cs,dis}^{max} = 0.8$	$M_{gs}^{min} = 0$
$Q_{cs}^{max} = 0.3$	$\eta_{hs,ch}^{ch} = 0.98$	$\eta_{cs,ch}^{ch} = 0.97$	$M_{gs}^{max} = 3000$
$\eta_{cs}^{ch} = 0.96$	$\eta_{hs,dis}^{dis} = 0.98$	$\eta_{cs,dis}^{dis} = 0.95$	$M_{gs}^{min} = 0$
$\eta_{cs}^{dis} = 0.96$	$\delta_{hs}^{self} = 0.02$	$\delta_{cs}^{self} = 0$	$FR_{gs}^{max} = 500$
$\delta_{cs}^{self} = 0.01$	$\eta_{cs}^{ch} = 0.97$	$COP_{cs} = 3.5$	
Chillers	CHP	Boiler	EV
$COP_{ac} = 1.2$	$\eta_{chp}^{chp} = 0.45$	$H_{bo}^{max} = 2.1$	$P_{vn}^{max} = 0.362$
$COP_{ec} = 4$	$\eta_{h}^{chp} = 0.5$	$\eta_{h}^{bo} = 0.9$	$cap_{vn} = 0.1$

in station, charging time and rate, discharging time, and rate and amount of stored energy in EV battery are optimized. The vehicle available in the charging station is expressed by (63). Equation (64) expresses charging and discharging power rate. The stored energy in EV is presented by (65) and (66). The vehicle energy is limited by (67) and amount of energy stored at leaving time is expressed by (68). The details of EV charging station modeling can be found in [26]

$$z_{vn}^{se,f,t+1} \leq z_{vn}^{se,f,t} \quad (63)$$

$$-P_{vn}^{max} \cdot z_{vn}^{se,f,t} \leq P_{vn}^{se,f,t} \leq P_{vn}^{max} \cdot z_{vn}^{se,f,t} \quad (64)$$

$$E_{vn}^{se,f,t} = P_{vn}^{se,f,t} \cdot \Delta t \quad (65)$$

$$E_{vn}^{se,f,t+1} = E_{vn}^{se,f,t} + P_{vn}^{se,f,t+1} \cdot \Delta t \quad (66)$$

$$E_{vn}^{se,f,t} \leq cap_{vn} \quad (67)$$

$$E_{vn}^{se,f,t_{leave}} = \psi_{vn}^{se,f,t} \cdot cap_{vn} \quad (68)$$

H. Fault Modeling

For resilience assessment, nine various faults are considered in each season. The faults are listed in Table II. In each season, there are nine faulty days and rest of the days are healthy days (Fault1). Faults 2 and 3 occur due to electrical network outage. The applied faults (i.e., events or outages) are typical and the system operation is not a function of fault type, time, or location.

Disconnection of solar PV and wind units from network due to natural disasters are expressed by faults 4 and 5. CHP shutting down because of periodic maintenance is modeled by faults 6 and 7, boiler shutting down due to boiler repair is defined by faults 8 and 9 as well as fault 10 expresses natural gas network outage. In the proposed model, all the equations are important and some equations may not be regarded as the main ones. The

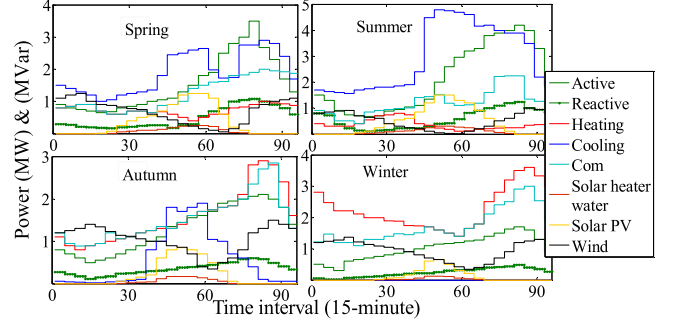


Fig. 6. Daily energy demands by loads and generated energy by renewables.

TABLE IV
CONVERSION COEFFICIENTS AND ECONOMIC PARAMETERS

α (kg/MWh)	β (MWh/kg)	ζ_p	P_{CO_2} (\$/kg)	P_{gr} (\$)	P_{sh} (\$)	P_{sell} (\$/kg)
230	0.015	1.2	0.003	10	10	0.025

proposed framework is modeled by combination of all formulas. The final optimization model is expressed as follows:

Minimizing (1)

Subject to

(2) to (68).

IV. CASE STUDY

The proposed microgrid is shown in Fig. 4. The nominal power of solar water heater 0.03 MW. The output power of solar PV panels can be expressed by (69) [27]

$$P_{PV}^t = \eta_{in} \cdot N_k \cdot P_{STC} \cdot \frac{I_t}{I_{STC}} \cdot (1 + 0.005 \cdot (T_t - 25)) \quad (69)$$

The set of PV array is composed by six pieces of solar panels. The rated power and area of one solar panel is about 250 W and 1.6 m², respectively. The rated power and area of PV array is 1.5 MW and 9.6 m². The other renewable resource is horizontal axis wind turbine. The output power of wind unit can be formulated as a function of wind speed shown by (70) [28]

$$P_w^t = \begin{cases} 0 & v_t \leq v_{in}, v_t \geq v_{out} \\ \frac{v_t - v_{in}}{v_r - v_{in}} \cdot P_r & v_{in} \leq v_t \leq v_r \\ P_r & v_r \leq v_t \leq v_{out} \end{cases} \quad (70)$$

Based on the wind speed and structure of turbine, it is assumed that the nominal power of wind turbine is equal to 1.5 MW. The energy generation profile of renewable resources and loads in each season is shown by Fig. 6. The hourly price of active and reactive power and natural gas [19] is depicted in Fig. 7. The efficiency of battery converter is 96% and the efficiency of other ac/dc converters is equal to 100%. The microgrid devices characteristics and conversion coefficients and economic parameters are given in Tables III and IV, respectively [12], [13], [20], [25], [26]. Some data are directly taken from the mentioned references but some other data are taken and then normalized according to range and scale of current test network. The numbers of seasons

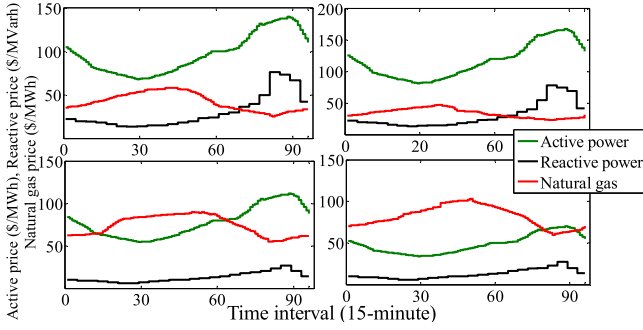


Fig. 7. Hourly price of active-reactive powers and natural gas for four seasons.

TABLE V
CLASSIFICATIONS OF CASES

Case studies	Primary system	Natural gas storage	Heating, cooling and hybrid storages	V2G and Partial charge for EV	CO ₂ storage	P2G and CO ₂ selling
Case 1	✓	✓	×	×	×	×
Case 2	✓	✓	✓	×	×	×
Case 3	✓	✓	✓	✓	×	×
Case 4	✓	✓	✓	✓	✓	✓

days equal 90, 93, 90, and 92 [19]. The daily time is modeled by 96 time-intervals each one 15 min.

Every uncertain parameter follows a PDF with known mean and standard deviation. The standard deviation of uncertain parameters is considered by 10% and mean of these parameters is shown by Fig. 6. The PDF related to each uncertain parameter is approximated by three steps as discrete Gaussian PDF that are denoted as α , β , and δ with probability equal to 0.06, 0.9, and 0.04, respectively. Amount of β is equal to mean and amount of α and δ are equal to 0.5β and 1.5β , respectively. The stochastic programming based on the scenario generation and scenario reduction techniques is used to handle the scenarios and uncertainty [29].

V. SIMULATION RESULTS

The problem is solved by a personal computer with processor core i7, CPU@ 4GHz, and RAM 8GB. The numerical results are given using GAMS software. In order to demonstrating the capability of the proposed model, the simulation is performed under four cases. The classifications of the cases are listed in Table V and case 4 is the final desired case. The primary network defined in Table V consists of electrical and natural gas networks, loads, CHP, boiler, wind, solar PV, solar water heater, electrical-absorption chillers, and EV charging station.

A. Analysis of Different Cases

The annual costs of different cases are shown by Table VI. The active power cost in case 4 is increased due to P2G operation and H₂ generation. Case 2 shows that the multitype energy storage reduces the cost of purchased reactive power by 69.5%. The V2G operation and partial charge capability of EVs in the charging station reduce the load shedding cost by 6.5% in case 3. In case 4, application of CCS and P2G reduces CO₂ emission and cost of natural gas by 75% and 6.1%, respectively.

TABLE VI
ANNUAL OPERATION COST OF NETWORK UNDER DIFFERENT CASES

Various costs (\$/year)	Case 1	Case 2	Case 3	Case 4
Active cost	893368	886500	885516	966107
Reactive cost	76889	23483	23489	23478
Natural gas cost	1949473	1944768	1938149	1818667
Emission cost	34296	34288	34221	8496
CHP cost	7180	7360	7360	5720
Load shedding cost	36881	32837	30718	29754
EV partial charge cost	0	0	5565	4881
selling CO ₂	0	0	0	106281
Full Cost	2998090	2929239	2925021	2750822

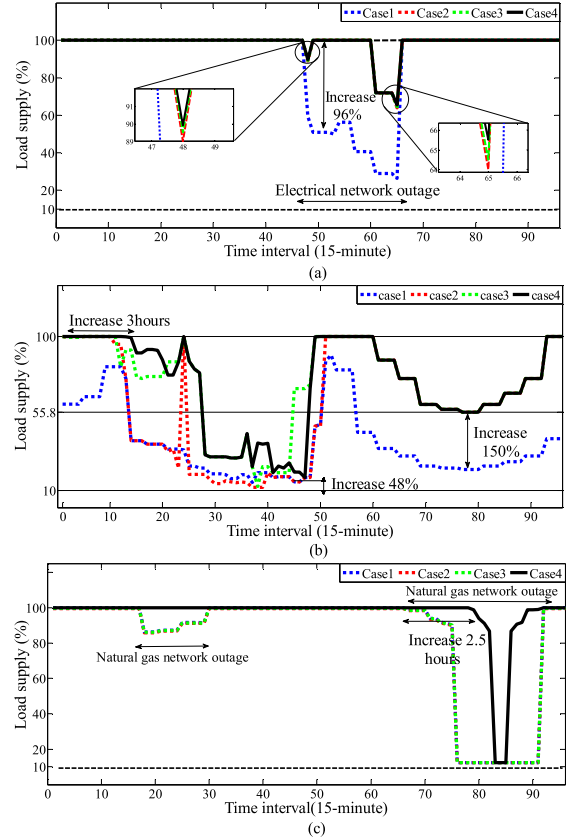


Fig. 8. Hourly supplied electrical load in (a) fault 2 and (b) fault 3 in summer and heating load in (c) fault 10 in winter under different cases.

B. Resilience Analysis

The supplied load over the fault duration is the resilience index of current work that must be maximized. This index is integral of system performance function over the fault duration that is modeled by a nonlinear parameter in [30] and [31]. For resilience analysis of the cases, the supplied load under fault condition is shown in the Fig. 8. In Fig. 8(a), the fault occurs at time interval 48 to 65 and it is clear that not only the supplied electrical load by case 4 is improved by 96% but also 100% of load is supplied at time period between 50 to 60. Among all cases, case 4 has the best operation. Fig. 8(b) demonstrates the supplied electrical load under fault 3 for different cases. Case 4 postpones the network deterioration for 3 h, increases the electrical load supply by 150% at time intervals between 60 to 96, and improves the minimum load supply by 48%. The supplied heating load under fault 10 is shown in the Fig. 8(c). According to this figure, case 4 can supply 100% of heating load

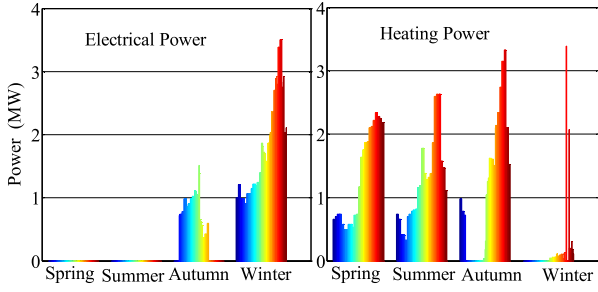


Fig. 9. Combinational load supply in four seasons.

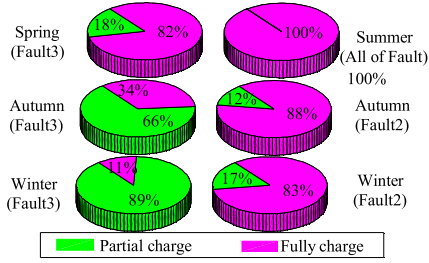


Fig. 10. EV with partial or full charge in four seasons under faults 2 and 3.

under first outage and the network degradation is postponed for 2.5 h under second outage.

C. Analysis of Microgrid Behavior Under Proposed Case

Comparing cases 1 and 4 shows that in case 4, the full cost is decreased by 8.2%, the emission, load shedding, and purchased natural gas costs are decreased by 75%, 19.3%, and 6.7%. In case 4, the adequacy, robustness and resilience of network are increased by 150%, 48%, and 3 h. Therefore, case 4 is considered as final case to be evaluated.

1) *Combinational Load Supply*: The price of electrical energy is high in spring-summer and the price of natural gas is high in autumn-winter. It is therefore expected that the combinational load be supplied by electrical power in autumn-winter and by heating power in other seasons. This point is confirmed in Fig. 9.

2) *Analysis of EV Charging Station Under Fault Condition*: In proposed approach, the charging station is able to charging the EVs partially rather than fully and then it pays the penalty cost to EVs owners.

It is expected that such operation be utilized only when the grid electricity is in short supply. According to Table II, the system under faults 2 and 3 has electrical power shortage, it is therefore expected that the charging station accept the penalty cost and use the partial charge option. The numbers of EVs with partial and fully charges are depicted in Fig. 10. According to this figure, the partial charge occurs only under faults 2 and 3 and the EVs are fully charged under other faults. The penalty cost is a coefficient of electricity price and it is high in summer. As a result, 100% of the EVs are fully charged in summer under all faults but in the autumn and winter, 34% and 11% of EVs are fully charged.

Fig. 11 indicates the number of vehicles available in the charging station under fault 2 and without fault. The fault occurs

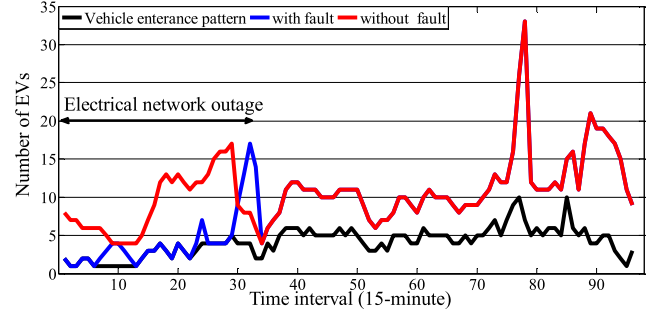


Fig. 11. Vehicle entrance pattern to charging station and hourly number of EV inside station with-without fault in winter.

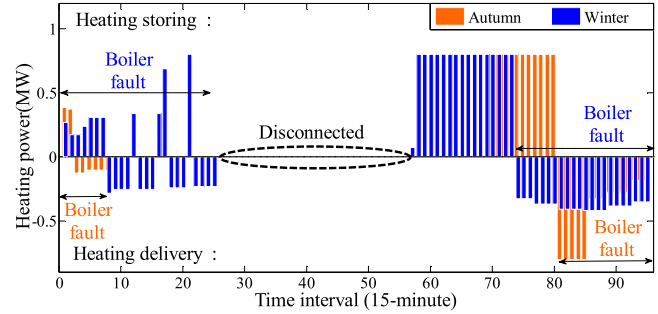


Fig. 12. Heat exchange of heating storage tank under fault 8 in autumn-winter.

from 0 to 31 time-periods. Under the fault, the station charges the vehicles rapidly and sends them out and do not operate the vehicles in V2G mode because the network is under fault and the power of the grid is required to supply the loads (the critical loads are in priority to be supplied). As a result, the vehicles are charged partially and leave the station. After fault, both the curves (with and without fault) fit each other and the station utilizes the vehicles in V2G mode. The duration of stay of vehicles in the station is increased to take part in energy management and peak load shaving.

3) *Heating and Battery Storages*: The heating demand is very high in autumn-winter and the network operation will be expensive under boiler outage; because not only the CHP generation is limited to the operation region but also price of natural gas to supply CHP in winter is high. The heating storage can fix this issue. The heat exchange of heating storage tank under fault 8 in autumn-winter is shown in the Fig. 12. Under the fault condition, the heat storage tank supplies the heating demand and reduces the network cost and CO₂ emission.

The battery storage with charging at low demand and discharging in peak demand shaves the peak load and reduces the cost. As seen in the Fig. 13, the battery not only is charged and discharged under low and peak demands but also is discharged under fault period and significantly reduces the unsupplied loads and penalty costs.

4) *Analysis of CO₂ Capture, Storage, and Trading*: Hourly generated CO₂ by CHP and boiler and captured CO₂ for CO₂ storage and P2G unit in winter under fault 10 (worst scenario) is shown in the Fig. 14(a). As seen in this figure, only 91 kg of CO₂ is released into the air at time interval 1 and at other time

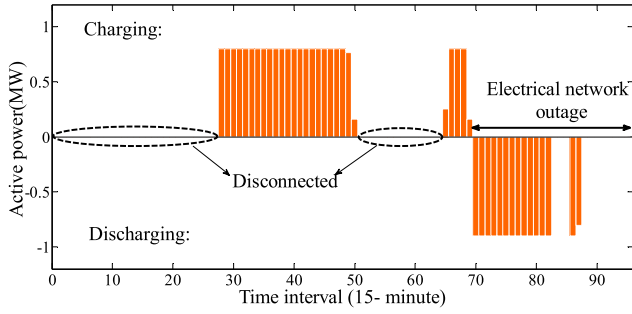


Fig. 13. Active power exchange of battery under fault 2 in autumn.

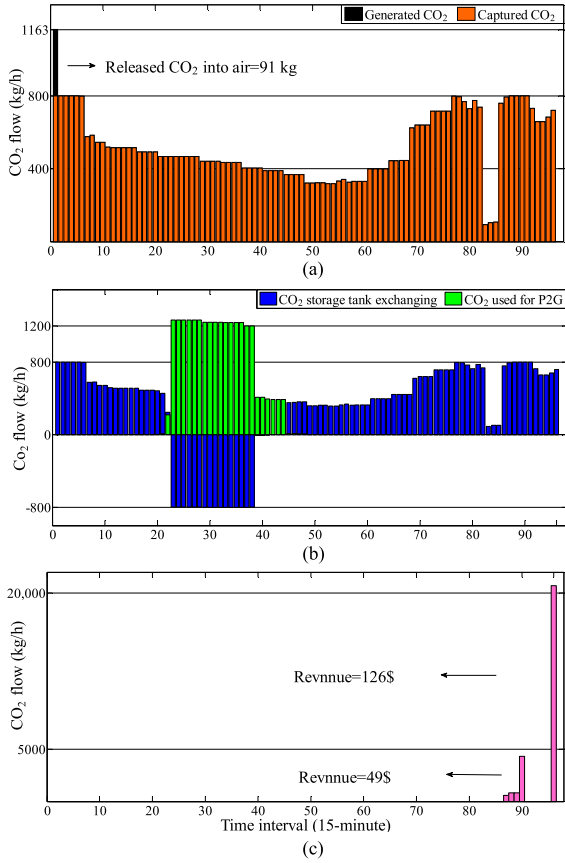


Fig. 14. (a) Hourly generated and captured CO₂, (b) CO₂ storage tank exchanging and CO₂ used for P2G, (c) CO₂ selling in winter under fault 10.

intervals all of the generated CO₂ is captured. Under other time periods, all of the generated CO₂ is captured in order to storing or supplying the P2G unit or selling CO₂. At time intervals 1 to 20 and 45 to 96, all captured CO₂ is stored in CO₂ storage tank. The P2G unit is turned ON at time intervals 22 to 44 for natural gas regeneration. The CO₂ needed for P2G at time intervals 23 to 41 is summation of captured CO₂ and released CO₂ from storage tank as shown in the Fig. 14(b). The stored CO₂ is sold to \$175 in time intervals 87 to 90 and 96, and CO₂ storage tank becomes empty for next day. Fig. 14(c) shows the CO₂ flow rate in order to selling CO₂ in 24 h.

5) *Natural Gas Analysis*: In winter, the heating demand and price of natural gas are high, thus the natural gas network outage

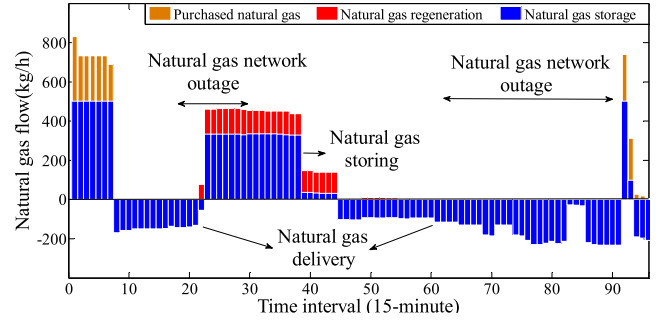


Fig. 15. Hourly purchased natural gas, natural gas regeneration and natural gas storage in winter under fault 10.

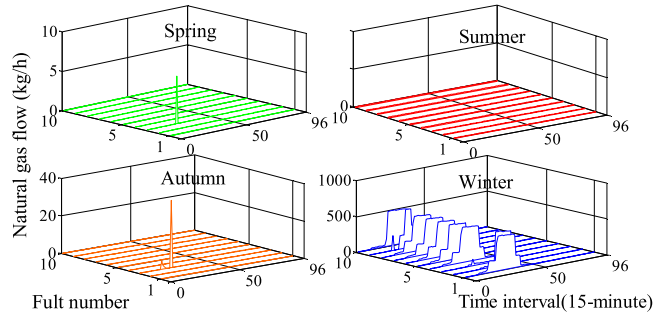


Fig. 16. P2G generation in four seasons under all of the faults.

can be very risky and expensive for network management. The purchased natural gas from the gas network, stored gas, and delivered gas, and the regeneration of natural gas in winter under fault 10 is depicted in Fig. 15.

As seen in the figure, under first outage (time intervals 18 to 29), the natural gas needed by network is supplied by natural gas storage tank and P2G unit. Under second outage (time intervals 63 to 91), the natural gas needed by the network is supplied by natural gas storage tank. Therefore, not only lower cost is used to purchase the natural gas but also the network resilience is increased and CO₂ emission is decreased. The generated natural gas by P2G unit in four seasons under all faults is shown in the Fig. 16. As seen in this figure, in spring and autumn the P2G is turned ON only under fault 3 because the electricity price is low and the network is facing electricity shortage.

The CHP therefore produces electricity and the required natural gas of CHP is supplied by P2G. In summer, the electricity price for water electrolyzer is high and the heating demand is low and P2G has no generation because the system does not need extra gas. In winter, the electricity price for water electrolyzer is low and the heating demand is high. As seen in the figure, under all faults except fault 3, P2G produces natural gas for boiler and CHP. Under fault 3, the CHP is not required to produce electricity and P2G operation is negligible. Because of P2G operation, the emission cost, the natural gas cost and the unsupplied load penalty cost are decreased by 75%, 6.1%, and 3.1%, respectively.

6) *Analysis of CHP Behavior*: The CHP operating points under all four seasons and the CHP operation region are depicted in Fig. 17. As seen in this figure, due to high price of electricity

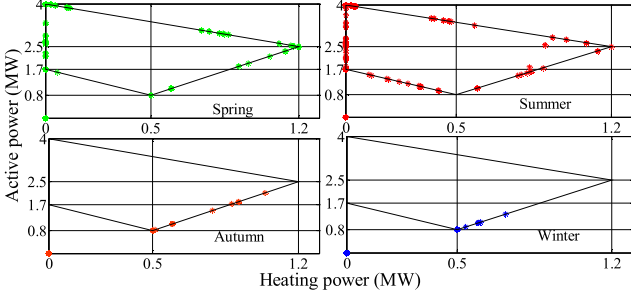


Fig. 17. CHP operating points under all four seasons and the CHP operation region.

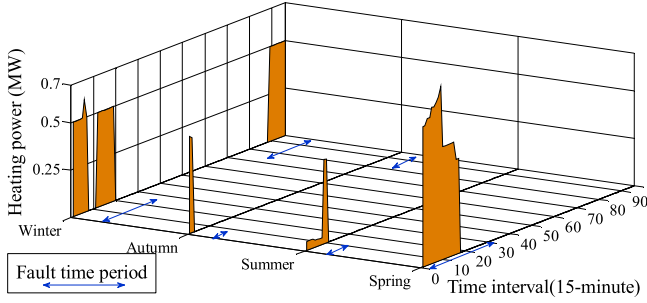


Fig. 18. CHP heating power in four seasons under fault 8.

TABLE VII
PERCENTAGE OF LOAD SUPPLY UNDER DIFFERENT CASES

Case	Deterministic	Stochastic
A	66%	82%
B	55%	78%
C	47%	69%
D	39%	58%

and low price of natural gas in spring-summer, the CHP generates more electrical and thermal powers in the spring-summer compared to the other seasons. The CHP heating generation is utilized in the spring-summer in order to supply the cooling demand. The CHP heating power in four seasons under fault 8 is shown by Fig. 18. As seen in the figure, the CHP generates heating power in order to compensating the heating shortage almost under all fault periods. Thus, the un-supplied heating load is decreased as well as network resilience is increased.

D. Uncertainty Analysis

The stochastic model is more resilient under load or generation variations compared to the deterministic plan. In order to show this point, the percentage of supplied load under different cases is calculated for both the deterministic and stochastic plans as listed in Table VII.

Case A: Generation of wind and solar PV is decreased by 60%.

Case B: Load increasing by 20%.

Case C: Generation of wind and solar PV equal to zero.

Case D: Load increasing by 20% and wind/solar generation equal to zero.

The load supply under stochastic model is more than the deterministic plan in all cases. The annual cost of deterministic

TABLE VIII
ANNUAL COST UNDER DIFFERENT UNCERTAINTY CASES

Various costs (\$/year)	Case 4	Case 5	Case 6
Active cost	966107	971221	971236
Reactive cost	23478	23478	23478
Natural gas cost	1818667	1818667	1818667
Emission cost	8496	8499	8499
CHP cost	5720	5728	5729
Load shedding cost	29754	29758	29758
EV partial charge cost	4881	4956	4958
Selling CO ₂	106281	106283	106285
Full Cost	2750822	2756024	2756040

model is lower than the stochastic plan, but the resilience of network with stochastic plan is better. This point is the most important positive topic of uncertainty modeling especially for supplying the critical loads.

E. Uncertainty of EV Charging Behavior

The uncertainty of EV charging behavior is considered as vehicle entrance pattern and initial energy of EVs. The standard deviation of these parameters is considered by 10% (case 5) and 30% (case 6). Mean of vehicle entrance pattern is shown by Fig. 11 (black curve) and mean of initial EV energy is assumed equal to 25%. The results are listed in Table VIII.

Some costs such as active cost and CHP cost are changed, because the initial of EV in case 4 is constant but in cases 5 and 6 it is uncertain and needs more power from grid. As well, due to increasing CHP operation, the CO₂ emission (emission cost) is increased. The full cost in cases 5 and 6 is increased by 0.18% and 0.19%, respectively. Due to consideration of many uncertain parameters in the model such as behavior of renewables and loads, the EVs uncertainty has trivial effect on the system.

F. Demand Response Program

An incentive-based demand response program is modeled by shifting the electrical load to the other times. The range of shiftable load at each time is expressed by (71). The shifted load is added at next times as shown by (72). The final amount of demand is defined by (73). The demand response cost is calculated by (74) that should be added to the objective function

$$\text{DRP}_{\text{up}}^{\text{se},f,s,t} \leq \gamma \cdot I_{\text{ea}}^{\text{se},f,s,t}, \quad \text{DRP}_{\text{down}}^{\text{se},f,s,t} \leq \gamma \cdot I_{\text{ea}}^{\text{se},f,s,t} \quad (71)$$

$$\sum_{t \in T} \text{DRP}_{\text{up}}^{\text{se},f,s,t} = \sum_{t \in T} \text{DRP}_{\text{down}}^{\text{se},f,s,t} \quad (72)$$

$$\text{PD}_{\text{DR}}^{\text{se},f,s,t} = I_{\text{ea}}^{\text{se},f,s,t} + \text{DRP}_{\text{up}}^{\text{se},f,s,t} - \text{DRP}_{\text{down}}^{\text{se},f,s,t} \quad (73)$$

$$\begin{aligned} C_{\text{DR}} &= \sum_{\text{se} \in \text{SE}} \left(\sum_{f \in F} D_{\text{se}}^f \left(\sum_{s \in \text{SC}} \left(\sum_{t \in T} \left(\text{DRP}_{\text{up}}^{\text{se},f,s,t} + \text{DRP}_{\text{down}}^{\text{se},f,s,t} \right) \cdot \text{pro}_s \right) \right) \right) \end{aligned} \quad (74)$$

TABLE IX
ANNUAL OPERATION COST WITH AND WITHOUT DRP

Various costs (\$/year)	Without DRP	With DRP
Active cost	966107	952181
Reactive cost	23478	23480
Natural gas cost	1818667	1818658
Emission cost	8496	8492
CHP cost	5720	5716
Load shedding cost	29754	2953
EV partial charge cost	4881	4881
Selling CO ₂	106281	106088
DRP cost	0	23785
Full operation cost	2750822	2734058

TABLE X
ANNUAL OPERATION COST OF NETWORK UNDER CONSTANT AND VARIABLE NATURAL GAS PRICE

Costs (\$/year)	Variable price	Constant price
Active power	966107	966212
Reactive power	23478	23463
Natural gas	1818667	1819921
Emission	8496	8500
CHP	5720	5723
Load shedding	29754	29755
EV partial charge	4881	4881
selling CO ₂	106281	106288
Final Cost	2750822	2752167

The results including demand responsive loads are shown in Table IX. The purchased cost of active power is reduced significantly, because the load supply cost under on-peak is reduced. Therefore, the annual operational cost is reduced by 0.6%.

G. Natural Gas Price Analysis

In this article, the gas price is considered different under off-peak and on-peak time-periods, but the gas price may be constant due to natural gas inertia. In order to show the impacts on gas price on the model, the system is simulated under two cases including constant (39\$/MWh) and variable (the proposed cost) natural gas price. The results are listed in Table X. The final cost with content gas price is increased by 0.05%. As a result, the natural gas inertia has a small effect on the results.

H. Battery, Electrolyzer, and Methanation Operational Cost

The operational cost of electrolyzer, methanation, and battery are often high and the fast action reduces their lifetime. In order to show the effects of such costs on the system, the operational costs of battery, electrolyzer, and methanation are considered as 100 \$/MWh, 80 \$/Kg, 140 \$/Kg, respectively [32] with life time equal to 5 years. Such costs increase the annual cost of system to 2874129 \$ which shows 4.5% increment. Therefore, considering the operational cost for the devices with fast operation like battery, electrolyzer and methanation increases the accuracy of the outputs.

VI. CONCLUSION

This article modeled a multicarrier energy hub in the microgrid. The natural gas, electricity, heating, cooling, H₂, CO₂,

and renewables were included in the model. The microgrid utilized multiple resources and capacities. A hybrid electrical storage, thermal storage, EV charging station, P2G system, CCHP, and CCS were coordinated in the given model. Different faults and events were modeled in all seasons to evaluate the energy resilience. Various cases were implemented, simulated, and studied. The results confirmed that the multitype energy storages decreased the cost by 69.5%. The EV charging station can reduce the load shedding cost by 6.5%. The CCS captured about 75% of CO₂ emission. The P2G reduced the natural gas cost by 6.1%. The proposed case including all resources at the same time (case 4) decreased the total system cost by 8.2%. The proposed model reduced the emission, load shedding, and gas cost by 75%, 19.3%, and 6.7%, respectively. In the proposed case, CO₂ trading was considered and the annual revenue from CO₂ selling was 126986 \$. The optimal coordination of multi type storages, CHP, boiler and P2G made positive economic and technical impacts on the system, where the costs were reduced and the resilience, adequacy, and robustness were improved.

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