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OPEN Feasibility and robustness of dynamic ¹⁸F-FET PET based tracer kinetic models applied to patients with recurrent high-grade glioma prior to carbon ion irradiation

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The aim of this study was to analyze the robustness and diagnostic value of different compartment models for dynamic ¹⁸F-FET PET in recurrent high-grade glioma (HGG). Dynamic ¹⁸F-FET PET data of patients with recurrent WHO grade III (n:7) and WHO grade IV (n: 9) tumors undergoing re-irradiation with carbon ions were analyzed by voxelwise fitting of the time-activity curves with a simplified and an extended one-tissue compartment model (1TCM) and a two-tissue compartment model (2TCM), respectively. A simulation study was conducted to assess robustness and precision of the 2TCM. Parameter maps showed enhanced detail on tumor substructure. Neglecting the blood volume V_B in the 1TCM yields insufficient results. Parameter K₁ from both 1TCM and 2TCM showed correlation with overall patient survival after carbon ion irradiation (p = 0.043 and 0.036, respectively). The 2TCM yields realistic estimates for tumor blood volume, which was found to be significantly higher in WHO IV compared to WHO III (p = 0.031). Simulations on the 2TCM showed that K_1 yields good accuracy and robustness while k₂ showed lowest stability of all parameters. The 1TCM provides the best compromise between parameter stability and model accuracy; however application of the 2TCM is still feasible and provides a more accurate representation of tracer-kinetics at the cost of reduced robustness. Detailed tracer kinetic analysis of ¹⁸F-FET PET with compartment models holds valuable information on tumor substructures and provides additional diagnostic and prognostic value.

Despite extensive research, prognosis of patients diagnosed with high-grade glioma (HGG) remains poor¹⁻³. Persistent remissions are rare and local tumor progress still poses a major pattern of therapy failure^{4,5}.

Biological imaging, such as positron emission tomography (PET), can be used to assess tissue metabolism and represents a promising modality to assist in diagnosis and planning of the treatment⁶.

In recent years, ¹⁸F-labeled fluoro-ethyl-tyrosine (FET)⁷ has been increasingly used for imaging HGG⁸⁻¹³. ¹⁸F-FET has been shown to provide high sensitivity and specificity of the tracer for glioma tissue and at the same time low uptake in inflammatory and healthy brain tissue14. The high in-vivo stability of FET and long half-life of ¹⁸F, together with the easy production in sufficient amounts, make the tracer practical for clinical applications.

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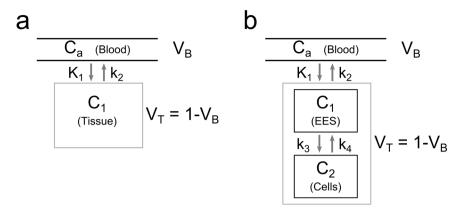


Figure 1. Schematic representation of the used compartment models. C_a is the concentration of tracer in the arterial blood (arterial input function AIF). (a) The one-tissue compartment model (1TCM) describes the exchange of tracer between the arterial blood with the tissue in terms of exchange rates $K_1(1TCM)$ and $k_2(1TCM)$. In an element of tissue the blood compartment in form of the capillaries occupies the volume fraction V_B , whereas the fraction of tissue volume is $V_T = 1 - V_B$. (b) The more complex two-tissue compartment model (2TCM) separates the tracer concentration in tissue into tracer in the extracellular extravascular space (EES) and in the cells. Tracer is transported from the capillaries into the EES over the blood-brain barrier with rates $K_1(2TCM)$, $k_2(2TCM)$, and from the EES it is taken up in the cells with rates $k_3(2TCM)$, $k_4(2TCM)$.

The role of ¹⁸F-FET in both diagnosis as well as therapy monitoring of HGG has been intensively studied^{8,15,16}, proving the value of ¹⁸F-FET for lesion detection in low- and high-grade gliomas as well as the identification of tumor recurrence. Tracer uptake in terms of the standard uptake value (SUV) has further been correlated with tumor cell density¹⁷.

However, it has been shown that the amount of tracer uptake and the subsequent correlation of the SUV with tumor grading depend on the acquisition timing following tracer injection¹⁸. Hence, static PET scan protocols might not reveal the entire metabolic tumor structure, and results can vary for different acquisition schemes.

Advanced pharmacokinetic analysis of time-activity curves (TACs) from dynamic PET scans using compartment models enables for the extraction of direct physiological correlates and helps in the comprehension of the underlying fundamental uptake mechanisms¹⁹. This is of special interest, as it may allow the assessment of tumor physiology and eventual heterogeneity that might not be visible with standard modalities, like magnetic resonance imaging (MRI) or computed tomography (CT).

¹⁸F-FET, unlike other system L- substrates like [¹¹C] methionine and [¹⁸F]FDOPA, is not further metabolized after being taken up by the cells, which simplifies respective compartment models and thus makes it a potentially valuable candidate for tracer kinetic analysis. Several authors have studied the value of dynamic ¹⁸F-FET PET for diagnosis and grading of HGG^{9,20-22}. However, most of them resort to either qualitative analysis of curve shapes or derivation of semi-quantitative parameters such as the initial slope or time to peak. Few authors applied detailed pharmacokinetic analysis using different compartment models^{23,24}, but parameter robustness and reliability were not investigated.

The aim of the present study was to investigate feasibility of tracer kinetic analysis in dynamic ¹⁸F-FET PET of recurrent HGG and to identify the most accurate and reliable model. Therefore, we systematically investigated fits with the 1TCM, the simplified 1TCM and the 2TCM to data from patients with recurrent HGG. Quality of the 2TCM fits was assessed by fitting synthetic TACs, generated with different parameter combinations, and analyzing the resulting parameter estimates in terms of accuracy and robustness.

Methods

All procedures performed in this study were in accordance with the 1964 Helsinki declaration and its later amendments or comparable ethical standards. The study was approved by the institutional ethics committee (ethics committee of the University of Heidelberg, S-421/2015). Owing to the retrospective nature, the need for informed consent was waived.

Compartment models. Different compartment models could be feasible to describe ¹⁸F-FET tracer kinetics. The simplest approach is using a standard one-tissue compartment model (1TCM), which is depicted in Fig. 1a. The exchange of tracer between blood and tissue by means of exchange rate constants $[K_1, k_2]$ can be expressed in a single differential mass balance equation:

$$\frac{dC_t(t)}{dt} = K_1 C_a(t) - k_2 C_t(t) \tag{1}$$

 $C_a(t)$ and $C_t(t)$ represent the tracer concentrations within the arterial blood pool and tissue, respectively. The total measured concentration of tracer in a volume element then yields:

Feature			Grade III	Grade IV
	Gender	Male	6	6
		Female	1	3
	Resection	Complete	1	2
	(surgery)	Partial	2	6
Primary Treatment		Biopsy only	4	1
Filmary freatment	Chemotherapy	TMZ	5	9
	Radiotherapy	Photon	6	9
		Ion	1	0
	Age	<50	1	4
		50-59	4	1
		60-69	1	3
At time of recurrence		≥70	1	1
diagnosis	KPS	100	1	4
		90	5	3
		≤80	1	1
		NA	0	1
	Status at last FU	PD	5	7
After Re-irradiation		SD	2	2
	Death		4	8

Table 1. Patient Characteristics.

$$C_T(t) = (1 - V_B)C_t(t) + V_BC_a(t)$$
 (2)

 V_B represents the relative volume of blood within in a respective volume element (in ml/100 ml tissue, $0 < V_B < 1)^{19}$. In many cases, V_B is assumed to be zero, leading to a simplified model with only two parameters K_1 and k_2^{25} . In the following, this model will be referred to as "simplified 1TCM" (s1TCM). The two transfer constants $[K_1, k_2]$ in the 1TCM include both tracer transport over the blood-brain barrier via blood flow and diffusion and transport of the tracer to the cells. After crossing the blood-brain barrier, ¹⁸F-FET is transported into the cells by the LAT system²⁶. Hence, a more detailed description of the transport processes could be formulated in a two-tissue compartment model (2TCM)¹⁹, which is described by two differential equations with transfer constants $[K_1, k_2, k_3, k_4]$:

$$\frac{dC_1(t)}{dt} = K_1 C_a(t) - (k_2 + k_3) C_1(t) + k_4 C_2(t)$$
(3)

$$\frac{dC_2(t)}{dt} = k_3 C_1(t) - k_4 C_2(t) \tag{4}$$

The interplay of the two tissue compartments is illustrated in Fig. 1b. $C_1(t)$ represents the concentration of tracer in the interstitial space, whereas $C_2(t)$ is the concentration within cells. Transport rates K_1 and k_2 describe blood flow and diffusion of the tracer into the interstitial space, and k_3 and k_4 the transport via the LAT system.

The total tracer concentration $C_T(t)$ in a voxel of tissue corresponds to the time-activity curve (TAC) derived from dynamic PET measurements. The concentration in the arterial blood pool is usually derived from the 4D PET images by extracting the TAC in a feeding artery close to the tissue of interest. This arterial TAC is often referred to as arterial input function (AIF). For tracer-kinetic analysis, the functional representation of $C_T(t)$ from the respective model is fitted to the measured TAC in tissue by means of non-linear least square techniques, using the measured arterial concentration. The fitting routine in terms yields estimates for the models transfer constants

The subsequent bidirectional transport of ¹⁸F-FET into and out of the cells after crossing the BBB can be modeled by application of a 2TCM. However, if data quality is low, e.g. due to low temporal resolution or low signal-to-noise ratio (SNR), a simplified one tissue compartment model (1TCM) could be more suitable as it yields more stable parameter estimates and does not pose the risk of overfitting the data.

Patient data. 16 patients with recurrent HGG were investigated in this institutional review board approved retrospective analysis. Patient characteristics are listed in Table 1. Tumor grade was evaluated at diagnosis of tumor recurrence based on clinical features on MRI.

 $^{18}\text{F-FET}$ years were acquired prior to re-irradiation using a Siemens Biograph 6 PET/CT scanner. Median injected activity was 190 MBq (130 to 235 MBq). Dynamic acquisition was performed over 40 min in 20 frames with temporal sampling of 6 \times 20 s, 8 \times 60 s and 5 \times 300 s. Endpoint static $^{18}\text{F-FET}$ PET images were calculated by averaging the scans of the last 10 minutes. Images featured a resolution of 1.33 mm \times 1.33 mm \times 3 mm, acquired over 80 slices. Static $^{18}\text{F-FET}$ PET raw images were converted to SUV images, and tracer-enhancing tumor lesions

were segmented based on an isocontour of 70% (I_{70}). Various thresholds are in practice for isocontours, ranging from 50% to 90%. 18 F-FET uptake is low compared to other tracers like FDG. Therefore, to our experience in recurrent glioma, I_{90} yields very small volumes of only a few voxels. I_{50} on the other hand can easily result in wide spreading segmentations of half of the brain, as recently shown²⁷. Thus, I_{70} was selected as best compromise between these values.

 SUV_{max} was determined as maximum value within I_{70} . The *standardized uptake ratio* (SUR) was calculated by normalizing SUV_{max} to the mean background uptake (SUV_{bg}), which was derived as average SUV within a region of similar 2D size in a part of the brain contralateral to the tumor.

Patient individual image-derived arterial TACs were extracted from the left/right carotid artery in three image slices. Segmentations of arterial TACs were delineated based on the first and second time frame and chosen to include only the inner part of the artery by selection of voxels with maximum peak activity (visual inspection of voxel-wise TACs) and by co-registering contrast enhanced MRI, in order to minimize partial volume effects. Whole blood to plasma conversion was applied using a factor of 10%.

Voxelwise fitting of TACs with 1TCM, s1TCM and 2TCM was performed within I_{70} , yielding parameter estimates K_1 (s1TCM), k_2 (s1TCM), K_1 (1TCM), k_2 (1TCM), K_1 (1TCM), K_2 (2TCM), k_3 (2TCM), k_4 (2TCM), k_5 (2TCM), k_8 (2TCM), k_8 (2TCM). For all transfer rates a constraint of $0 \, \mathrm{min^{-1}} < k_i < 1 \, \mathrm{min^{-1}}$ was set in order to limit the search space and exclude unreasonable values. The maximum value of respective parameter estimates was defined as the 75th quantile, since the actual maximum value potentially consists of the set parameter constraints. Median and maximum of each of the 6 parameters were correlated with tumor grade. Tumors were irradiated with fractionated carbon ions at a median total dose of 37.5 GyE (range 30 to 42 GyE, 3 GyE per fraction). Median parameter estimates of the 1TCM and 2TCM as well as SUR and grade were correlated with overall survival (OS) and progression free survival (PFS) after re-irradiation using Cox proportional hazards model.

Simulation Data. For assessment of stability and precision of the parameter estimates resulting from fits with the 2TCM, synthetic TACs were generated using various parameter combinations of K_1 , k_2 , k_3 , k_4 and V_B (2TCM). To our knowledge, no detailed reports on tracer kinetic modeling in dynamic ¹⁸F-FET PET in recurrent HGG exist. Thus, representative values of the model parameters, which could be used for data simulation, were not available. Representative sets of parameters for the 2TCM were derived from patient parameter estimates of the current analysis. Histograms of parameter distributions of each patient were investigated and peak values were extracted. From these, ten common parameter combinations were derived (see results). Using the parameter combinations and two different measured patient AIFs, 1000 TACs were generated for each parameter combination using the 2TCM model function.

Acquisition noise was simulated by adding Gaussian random numbers to the synthetic curves, resulting in a signal-to-noise ratio (peak of AIF, divided by standard deviation of the noise) of SNR = 100. Simulated TACs were fitted with the 2TCM, using the same AIF as for data generation.

Evaluation of parameter estimates. Quality of fits was evaluated by means of reduced χ^2_{red} , calculated as the ratio between χ^2 and the number of degrees of freedom f:

$$\chi^2_{red} = \frac{1}{f} \cdot \frac{1}{\Delta y^2} \cdot SSR, \qquad f = n - p, \tag{5}$$

with n being the number of sampling steps, p the number of model parameters, and SSR the sum-of-squared residuals. Δy^2 is the squared error on each measured activity value y. For real patient data, the exact error on the measured activity is usually not known, which complicates calculation of χ^2_{red} . However, apart from systematic errors of the acquisition scanner that are identical for all measurements, the error on the measured activity y is influenced by the statistical nature of the radioactive decay. Therefore, we assumed $\Delta y \approx \sqrt{y}$. For simulated curves, the noise level is known, thus the error on the measured activity can be simply derived as $\Delta y = \sigma_{Noise} = \frac{AlF_{peak}}{CNR}$.

 χ^2_{red} is mainly driven by the SSR, indicating a better fit quality if the model curve lies closer to the measured data points. However, the more parameters a model provides, the better it can approximate the measured data, regardless of validity of these parameters. Hence, the Akaike information criterion (AIC)²⁸ provides a more reliable quantity for fit evaluation, as it penalizes the fit quality of a model with the number of parameters²⁹:

$$AIC = N \cdot \ln\left(\frac{SSR}{n}\right) + 2(p+1) \tag{6}$$

The corrected AIC (cAIC) for small sample sizes is calculated as:

$$cAIC = AIC + \frac{2(p+1)(p+2)}{n-p-2}$$
 (7)

When comparing fits from different models, the model yielding the lowest cAIC is considered to yield the best representation of the measured data. For comparison of the three models used in this study, the cAIC was computed for each fit, and results among models were compared.

Accuracy and stability of parameter estimates from fitting the simulated TACs (P_{fit}) were evaluated in terms of the absolute and relative deviation from the true value (P_{input}), referred to as absolute and relative error:

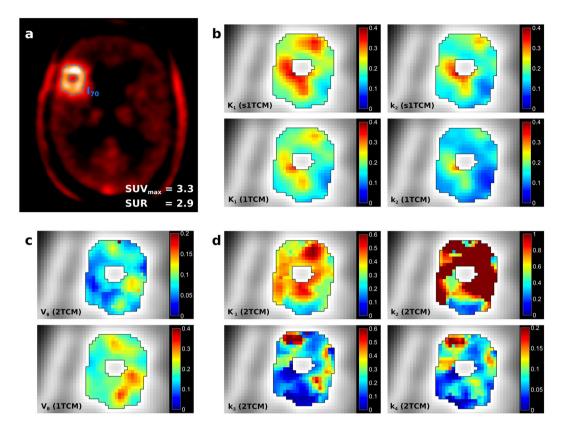


Figure 2. Parameter maps from fits with different compartment models in an exemplary patient with grade IV glioma. Pharmacokinetic analysis was performed within an isocontour of 70%, which was delineated based on the endpoint static summation image, as illustrated in (a). SUV_{max} and SUR were extracted, where SUR is the ratio between SUV_{max} and mean background SUV. Both the standard 1TCM and a simplified 1TCM were fitted voxelwise to the time-activity curves (TACs), yielding estimates for exchange rates K_1 and k_2 (b). Furthermore, TACs were fitted with the more complex 2TCM, which yields metabolic exchange rates K_1 , k_2 , k_3 and k_4 (d). The general definitions of the 1TCM and 2TCM yield estimates on the blood volume V_B , which is displayed in (c). In the simplified 1TCM (s1TCM), the blood volume is assumed to be zero $V_B = 0$. Parameter maps of tracer kinetic analysis show enhanced detail on tumor substructure, however, stability is decreased for the 2TCM. Both 1TCM and 2TCM yield similar distributions of V_B , indicating that the parameter is not negligible.

$$E_{abs} = P_{fit} - P_{input} \tag{8}$$

$$E_{rel} = \frac{P_{fit} - P_{input}}{P_{input}} \cdot 100\% \tag{9}$$

Software. All image analysis was conducted using the Medical Imaging interaction ToolKit (MITK)³⁰. SUV calculations were conducted using the SUV calculation plugin. For segmentation of tumor lesions, the MITK isocontour plugin³¹ was used. Tracer kinetic analysis was performed using an in-house developed software module for pharmacokinetic modeling in MITK³², which allows for voxelwise fitting of the measured time activity curves with various compartment models. The tool is incorporated into MITK and applies a Levenberg-Marquardt algorithm for model fitting.

For statistical analysis and plotting the open-source *R* software package was utilized (version 3.3.2, http://www.R-project.org). Two-sided, unpaired Wilcoxon tests were applied, together with Bonferroni-Holmes multiple testing corrections. Mantel-Cox log-rank test was used to compare differences in Kaplan-Meier survival curves (KM). Cox proportional hazards model was used for univariate analyses using log-transformed median parameter values (survival package, version 2.40-1, https://CRAN.R-project.org/package=survival). The significance level was set to 0.05.

Results

Regions of increased tracer uptake were delineated on basis of endpoint $^{18}\text{F-FET}$ PET images using an isocontour of 70% (I $_{70}$) and SUV $_{\text{max}}$ and SUR were calculated. Within the isocontour, voxelwise tracer kinetic analysis was conducted using the simplified 1TCM (without blood volume V_{B}), the standard 1TCM and 2TCM (both with blood volume).

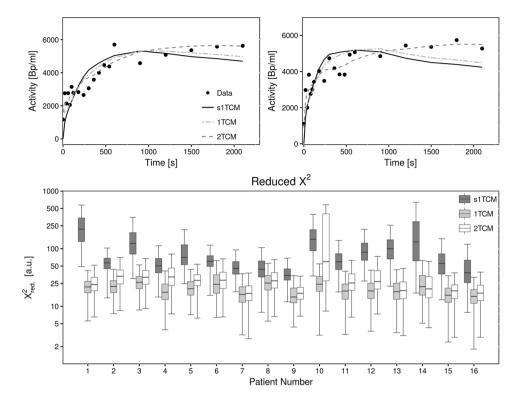


Figure 3. Goodness-of-fit in patient data from fits with different compartment models. The top two plots show the measured time-activity-curve in two exemplary voxels (dots) together with fitted curves from the 1TCM, standard 1TCM and 2TCM (lines). The 2TCM curve visually best describes the measured data points. Differences between s1TCM and 1TCM appear to be small. The bottom plot shows the distribution of the fit-quality measure reduced X² from all three models in every patient. Note that values for χ^2_{red} are shown on a logarithmic scale, since s1TCM yields much higher χ^2_{red} than 1TCM and 2TCM. Lower values of χ^2_{red} indicate better fits, i.e. less deviation between model curve and data points. Fits from s1TCM yield significantly higher χ^2_{red} , thus poorest fits. χ^2_{red} from the 1TCM and 2TCM yield similar values, however 1TCM appears to present with slightly better fits.

Figure 2 shows corresponding parameter maps from fits with the different models in an exemplary patient. K_1 and k_2 from the simplified and standard 1TCM (Fig. 2b) showed tumor substructure in more detail compared to the static SUV image. Parameter maps of K_1 and k_2 are very similar, with hot-spots and cold-spots in the same areas. However, the simplified 1TCM yields higher values in both parameters.

Fits with the 2TCM (Fig. 2d) could resolve the substructure even further; however, the enhanced level of detail of the 2TCM also resulted in less stable parameter estimates. This is visible in k_2 , where dark-red voxels indicate misfits, which approached the parameter constraint boundaries. Parameter maps of k_3 and k_4 present with congruent distributions, however, values of k_3 are higher in hotspots. V_B from the 1TCM and 2TCM show also very similar distributions (Fig. 2c), indicating stability and consistency of the parameter over the models. Estimates for V_B are higher from 1TCM compared to 2TCM. These results indicate that the blood volume V_B is not negligible in tracer kinetic analysis of dynamic ^{18}F -FET PET.

Evaluation of fit quality. Quality of respective fits with the three different models was investigated. Figure 3 shows the measured TAC in two exemplary voxels together with fitted curves from all three models. It can be observed that the 2TCM model function fits the measured time-activity-curves best. The simplified 1TCM provides the least adequate fit, with substantial deviations from the measured curve, especially at later time points. The standard 1TCM describes the time course of tracer activity more appropriately; however, it also shows deviations towards the end of the acquisition. It could be hypothesized that the 2TCM describes the tracer kinetics most accurately, as it visually gives the best fit to the data. In order to further investigate this finding, quantitative analysis of goodness-of-fit was performed by evaluation of χ^2_{red} and cAIC.

Reduced χ^2_{red} from fits to data of each patient with either one of the three utilized models is shown in Fig. 3. The simplified 1TCM yielded much higher χ^2_{red} compared to the standard 1TCM and 2TCM, indicating that it gives only a poor description of the TACs and thus tracer kinetics. χ^2_{red} from the standard 1TCM and 2TCM proved to be very similar. However, in most cases the 1TCM yielded slightly lower χ^2_{red} values. On the other hand it showed more outliers to extremely high values in many patients, showing that in some voxels the model curve did not fit the data at all.

Regardless of the model, χ^2_{red} takes very large values in all patients, even though it should be close to one. A possible explanation for this deviation is an underestimation of the acquisition noise.

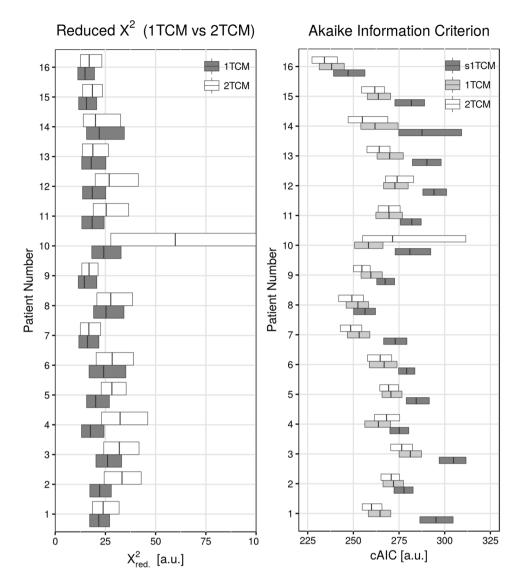


Figure 4. Goodness of fit compared to model stability. The left plot shows χ^2_{red} for the 1TCM and 2TCM on a zoomed scale for better comparison. The right plot shows the values for the corrected Akaike information criterion (cAIC) that accounts for model complexity by panelizing the fit quality (sum of squared residuals) with the number of parameters in the model. Lower cAIC indicates a better representation of the fitted data by the model. cAIC from the 2TCM were lowest, even though χ^2_{red} of this model was slightly higher compared to the 1TCM.

In order to consider fit quality with respect to the number of model parameters, the corrected AIC was calculated (Fig. 4). The results show that the simplified 1TCM yields the poorest results, however, fit quality according to the cAIC is not as bad as suggested by χ^2_{red} . Interestingly, the 2TCM appears to be the best representation of the data (lowest cAIC) in most cases, even though fits showed slightly higher χ^2_{red} compared to the 1TCM.

Parameter estimates from patient data. Table 2 lists median parameter estimates from the three models for all patients, together with the respective SUV_{max} and SUR values. Except for k_2 from the 2TCM, which takes unreasonably high values in many patients (up to the constraint boundary of $1\,\mathrm{min}^{-1}$), parameter estimates from fits with all models present with reasonable values. Figures 5 and 6 show histograms of the total voxel frequency of parameter estimates from the 1TCM (Fig. 5) and 2TCM (Fig. 6) in patients with grade III and grade IV tumors, respectively.

On average, patients with grade IV glioma presented with higher SUV_{max} and SUR (Fig. 7). The difference was not significant (SUV_{max}: 2.3 vs. 3.0, p = 0.2; SUR: 2.2 vs 3.0, p = 0.091). K_1 from fits with the simplified 1TCM showed a tendency towards higher values in patients with grade IV tumors, with mean values of $K_1 = 0.138 \, \text{min}^{-1}$ in grade III, and $K_1 = 0.204 \, \text{min}^{-1}$ in grade IV (p = 0.17). k_2 from s1TCM fits was similar in both groups ($k_2 = 0.189 \, \text{min}^{-1}$ in grade III and $k_2 = 0.194 \, \text{min}^{-1}$ in grade IV). As already discussed, the standard 1TCM yielded lower values for K_1 and k_2 compared to the simplified 1TCM. However, the tendency of lower K_1 in

		s1TCM		1TCM			2TCM					
Grade	SUV _{max}	SUR	K ₁ [10 ⁻² min ⁻¹]	$\begin{bmatrix} k_2 \\ [10^{-2} min^{-1}] \end{bmatrix}$	$K_1 = [10^{-2} min^{-1}]$	$k_2 = [10^{-2} \text{min}^{-1}]$	V _B [ml/100 ml]	$K_1 = [10^{-2} min^{-1}]$	$\begin{bmatrix} k_2 \\ [10^{-2} min^{-1}] \end{bmatrix}$	$k_3 = [10^{-2} min^{-1}]$	$k_4 = [10^{-2} min^{-1}]$	V _B [ml/100 ml]
	1.7	2.1	6.6	10.4	4.9	6.8	4.2	9.3	59.2	18.4	4.1	2.2
	3.9	3.4	12.4	9.2	10.3	6.8	6.7	13.7	33.1	23.0	7.0	5.1
	1.9	1.6	7.3	11.8	4.5	6.2	7.9	7.4	34.4	15.2	3.7	6.6
III	1.1	1.2	15.3	39.2	4.3	7.3	8.6	7.2	45.8	28.8	7.7	7.3
	3.3	2.7	18.9	15.1	14.7	10.7	9.3	22.2	47.2	19.0	8.7	5.9
	3.0	3.1	27.2	26.5	16.4	13.4	10.3	19.4	32.8	28.3	17.2	9.4
	1.2	1.4	8.9	20.5	4.6	9.3	5.7	9.6	100	30.6	6.7	4.8
	1.9	1.7	23.9	43.3	7.2	8.7	12.6	10.1	51.8	35.1	7.5	11.4
	2.9	3.7	42.7	33.8	33.3	22.5	14.7	47.9	100	22.1	13.7	11.5
	4.6	3.2	23.2	15.6	14.8	7.5	15.9	21.8	49.8	44.8	8.4	13.4
	3.3	2.9	22.6	18.0	18.5	13.5	9.8	38.7	100	17.5	6.7	6.9
IV	3.4	4.1	17.1	15.3	12.6	9.6	11.5	20.4	46.7	18.5	7.4	8.8
	2.9	3.0	11.7	7.5	9.0	4.5	11.2	17.5	63.4	26.3	2.2	7.2
	3.4	3.4	13.9	11.0	9.9	6.5	8.7	20.0	97.9	30.6	5.9	5.8
	1.9	2.6	12.7	17.5	5.8	5.0	9.4	8.5	56.2	56.3	6.6	9.1
	2.8	2.6	14.7	14.7	10.4	7.4	10.4	16.2	42.3	23.8	7.5	7.7

Table 2. Median parameter estimates from fits with the three different compartment models in every patient, together with SUV_{max} and SUV-to-background ratio (SUR): K_1 and k_2 from the simplified 1TCM; K_1 , k_2 and V_B from the standard 1TCM; K_1 , k_2 , k_3 , k_4 and V_B from the 2TCM. Note: Median Parameter estimates were used instead of averages, due to several voxels with failed fits, which yielded outliers towards high transfer rates (~100 10^{-2} min⁻¹ was set as upper constraint for all parameters).

grade III tumors and k_2 being alike in both entities remained ($K_1 = 0.085\,\mathrm{min^{-1}}$ vs. $0.135\,\mathrm{min^{-1}}$; $k_2 = 0.087\,\mathrm{min^{-1}}$ vs. $0.095\,\mathrm{min^{-1}}$). This can also be observed in the respective histogram, which presents with a clear shift towards higher values in grade IV tumors. V_B from the 1TCM fits was significantly lower in grade III glioma as shown in Fig. 7, with values of 7.5 ml/100 ml vs. $11.6\,\mathrm{ml/100}\,\mathrm{ml}$ (p = 0.02518, Bonferroni-Holmes corrected). This effect is also partially visible in the total voxel-value frequency histogram. For the 2TCM, similar results were observed with V_B (grade III) = 5.9 ml/100 ml vs. V_B (grade IV) = 9.1 ml/100 ml (p = 0.03112). The result did not remain significant after multiple testing corrections.

Average K_1 in the 2TCM over all patients yielded significantly lower values in grade III compared to grade IV glioma (0.127 min⁻¹ vs. 0.224 min⁻¹, p = 0.0091, Fig. 6 top). Estimates on k_2 presented with a tendency to unrealistically high values in both groups (see Table 2): k_2 (grade III) = 0.503 min⁻¹ and k_2 (grade IV) = 0.676 min⁻¹. Furthermore, estimates on k_2 resulted in several outliers up to the upper parameter constraint of 1 min⁻¹ especially in grade IV tumors. Thus, it is likely, that the fits in these voxels ran into constraint boundaries. Values for k_3 showed a trend to higher values in grade IV tumors (0.233 min⁻¹ vs. 0.305 min⁻¹), whereas mean k_4 was comparable with 0.079 min⁻¹ in grade III and 0.073 min⁻¹ in grade IV.

Parameter estimates from the different models, as well as grade and SUR, were further correlated with patient's overall survival (OS) and progression free survival (PFS). Results are listed in Supplementary Table S1. SUR showed correlation with OS (HR = 2.78, CI = [1.17; 6.64], p = 0.021). Furthermore, median K_1 from both the 1TCM and 2TCM fits showed significant correlation with OS: HR = 2.78, CI = [0.99; 7.84], p = 0.043 (1TCM); HR = 3.02, CI = [1.07; 8.59], p = 0.036 (2TCM). For both models, a cut-off for K_1 was found, that significantly separated patients overall survival, as shown in Supplementary Fig. S2. Patients with lower K_1 showed improved survival, with thresholds of K_1 (1TCM) = 0.074 min⁻¹ (p = 0.0041) and K_1 (2TCM) = 0.104 min⁻¹ (p = 0.0041), respectively. Cut-offs for K_1 from both models also presented with tendencies to separate progression free survival: K_1 (1TCM) = 0.059 min⁻¹, p = 0.082 and K_1 (2TCM) = 0.104 min⁻¹, p = 0.086. A trend towards correlations of these parameters with PFS was found, that was however not significant (p = 0.2006 and p = 0.154, respectively). Furthermore, k_2 from the 1TCM showed tendencies towards correlation with PFS (p = 0.1042). Parameter k_4 separated progression free survival with a threshold of k_4 = 0.067 min⁻¹ (p = 0.066). Cox proportional hazards model revealed however non-significant correlations with p = 0.301.

Evaluation of accuracy and robustness of the 2TCM on simulation data. In order to investigate the validity of 2TCM and test accuracy and robustness of the determined parameter estimates, histogram analysis of the individual patient's parameter maps was performed, as illustrated in Fig. 8 for one patient. Corresponding histograms for K_1 and k_2 from the 1TCM are shown in the supplements (Fig. S3). Peak values of the histograms of each parameter were extracted in order to find common parameter values $[K_1, k_2, k_3, k_4, V_B]$. From these values, 10 combinations were composed for data simulation, which are listed in Table 3. These parameter combinations together with two measured AIFs (Fig. 8 bottom) were used to simulated time-activity curves, which were fitted again with the 2TCM. The resulting parameter estimates were evaluated by means of stability and precision.

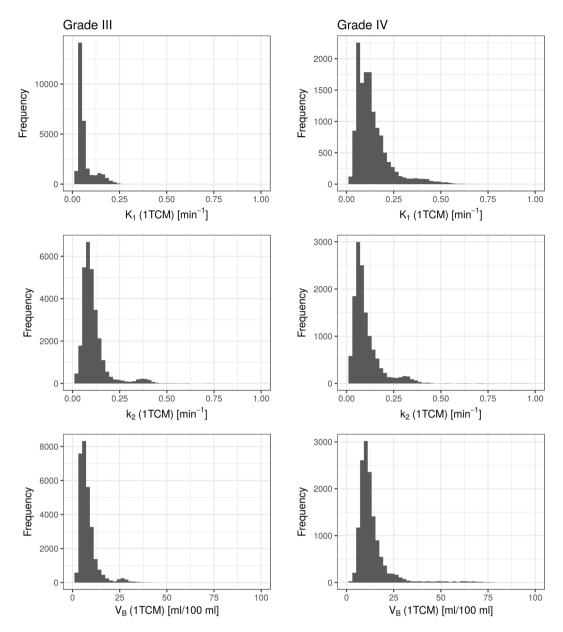


Figure 5. Histogram of total voxel frequency of parameter estimates on K_1 , k_2 and V_B (from top to bottom) from fits with the 1TCM in grade III tumors (left column) and grade IV tumors (right column), respectively. A clear shift towards higher values for grade IV tumors can be seen for K_1 , and to some extend for V_B , whilst distributions for k_2 are relatively similar.

Figure 9a shows the distribution of χ^2_{red} for all 10 combinations, with either one of the AIFs. Fits to data simulated with combination 7 and AIF type I, as well as combination 2 with AIF type II, yielded exceptionally poor fit quality. Apart from these cases, fit quality was good, with χ^2_{red} being close to one. However, in all combinations, some fits completely failed, yielding outliers of very high χ^2_{red} . This suggests decreased stability of the fits, which could be overcome by averaging signal from multiple voxels and thus, decreasing noise of the TACs (ROI-based analysis).

Figure 9b shows absolute errors on parameter estimates of K_1 , k_2 , k_3 and k_4 . It can be observed, that fits with AIF type II yield overall more stable results, with smaller quantiles of the parameter value distribution. This is counter-intuitive, since AIF type I would be assumed to yield better fit accuracy, because it captures the peak activity better. Interestingly, the distinct difference between the two AIF types was not observed in fit quality.

Overall, both accuracy and stability varied greatly over the different parameter combinations, which suggests that the 2TCM accurately describes the kinetics only in some tissue settings. Estimates on K_1 showed the lowest errors of all, with deviations of about $0.01\,\mathrm{min^{-1}}$. k_2 presents with increased errors, which are nonetheless not larger than $0.5\,\mathrm{min^{-1}}$ within the 25^th and 75^th quantile. With regards to stability, k_2 showed the widest distribution of parameters, suggesting that it is the least stable parameter. k_3 shows large errors for combinations 1 and 7 (AIF type I). The errors in combination 7 were already suggested by the poor fit quality and high χ^2_{red} . Interestingly,

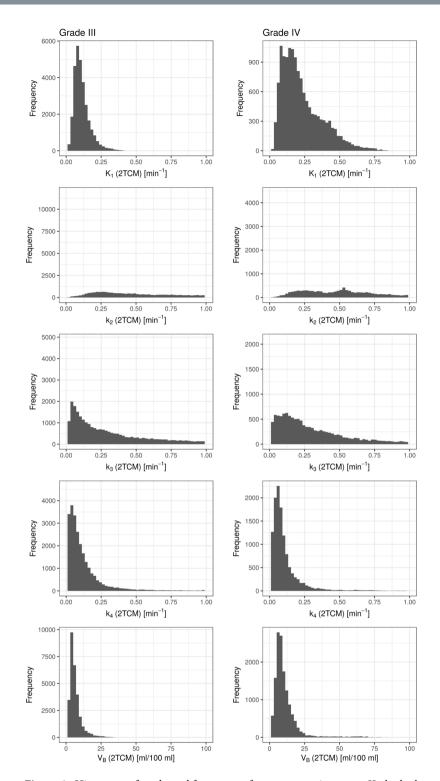


Figure 6. Histogram of total voxel frequency of parameter estimates on K_1 , k_2 , k_3 , k_4 and V_B (from top to bottom) from fits with the 2TCM in grade III tumors (left column) and grade IV tumors (right column), respectively. A clear shift towards higher values for grade IV tumors can be seen for K_1 and k_2 , and to some extend for V_B and k_3 . Distributions for k_4 are relatively similar.

combination 2 (AIF type II) showed low errors on parameter estimates, even though χ^2_{red} predicted the fits to be of poor quality. In all combination k_3 shows many outliers to high values, indicating failed fits. k_4 shows good stability and accuracy, except for one case (combination 9). This combination is the only one with a large true value of $k_4 = 0.2 \, \text{min}^{-1}$, showing that the model loses robustness for high values of this parameter. The inability of the 2TCM do deal with high values of k_4 could also be an explanation for the poorer fit quality in combination 7, where k_4 was set to $0.1 \, \text{min}^{-1}$.

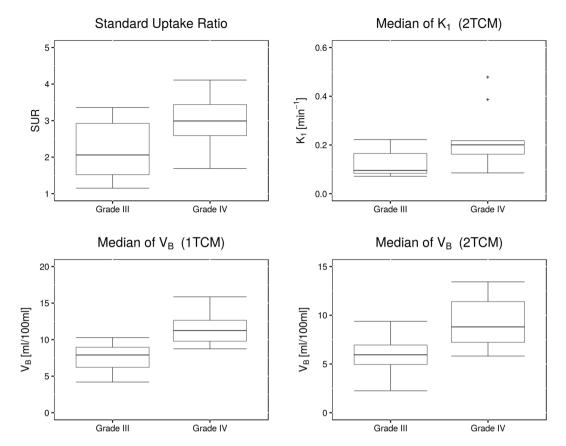


Figure 7. Correlation of parameter estimates with patient's tumor grade. The plots display the differences in median parameter estimates between patients with WHO grade III and WHO grade IV gliomas. Mean values over the entire cohort were 2.2 vs. 3.0 for SUR (p=0.09073), 7.5 ml/100 ml vs. 11.6 ml/100 ml for V_B from 1TCM (p=0.0021), 0.127 min⁻¹ vs. 0.224 min⁻¹ for K₁ from 2TCM (p=0.09073) and 5.9 ml/100 ml vs. 9.1 ml/100 ml for V_B from 2TCM (p=0.03112).

In the majority of cases k_3 and k_4 show positive errors, meaning that they are commonly overestimated by the fit. This is partly due to the fact that they were initial set to very low values for simulation, which also makes it difficult to interpret accuracy of these parameters in terms of absolute errors. Thus, further analysis was done by evaluation of relative errors on parameter estimates, which are displayed in Table 4 for the different parameter and AIF combinations. The high stability and accuracy of estimates on K_1 is confirmed, as the parameter shows low errors, which are mostly under 10% and quantile errors do not exceed \pm 30%. k_2 shows errors that are increased in several cases up to ~50%, but mostly low as well. However, in 4 cases, the deviations from the true value are substantial, because the quantiles do not include the 0% error value. k_3 and k_4 show large deviations from the true values in combinations 1, 7 and 9, with median errors up to several hundred percent with AIF type I. Furthermore, even though median errors are low in most of the other combinations, the parameters present with increased instability, reflected in the large quantiles of the errors.

Discussion

The presented study investigated the feasibility of tracer kinetic analysis in dynamic ¹⁸F-FET PET scans of patients with recurrent high-grade glioma re-irradiated with carbon ions. Up-to-date, controversial reports exits on the value of SUV and SUV-to-background ratio (SUR) for grading of glioma^{17,21,31,33}. These discrepancies might be linked to differences in SUR depending on the time point of PET image acquisition after injection of the tracer, as demonstrated by Weckesser *et al.*¹⁸. In this context, dynamic ¹⁸F-FET PET may provide more detailed information about tracer uptake compared to static image acquisition. However, dynamic scanning protocols are rarely used in clinical routine, due to the time-consuming acquisition and challenging interpretation of the data.

There are only few reports on detailed compartment model analysis in ¹⁸F-FET PET in patients, and the question, which model best describes the kinetics of tracer uptake, metabolism and washout is still unanswered ^{23,24}. However, voxelwise tracer kinetic analysis holds the promise of unraveling tumor sub-volumes of different metabolic activity, which is especially relevant in high-grade glioma due to their infiltrative and heterogeneous nature. Compartment modeling can yield direct physiological correlates on the blood volume and perfusion (i.e. vascularization) and metabolic rate constants.

Retrospective data of 16 patients were analyzed by voxelwise fitting of measured time-activity curves (TAC) with three different compartment models: a standard one-tissue compartment model (1TCM), a simplified 1TCM that assumes the blood volume to be zero (s1TCM) and a two-tissue compartment model (2TCM).

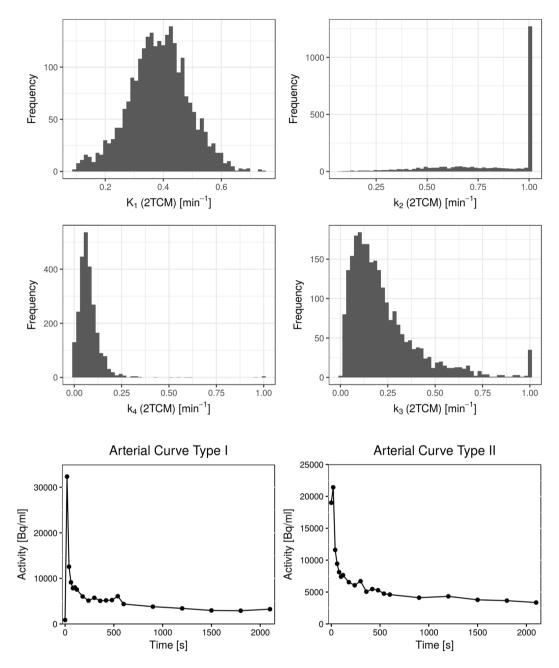


Figure 8. Extraction of parameter values for simulation time-activity curves with the 2TCM. The top plots show representative histograms of the distributions of parameter estimates K_1 , k_2 , k_3 and k_4 from fits with the 2TCM in an exemplary patient. Peak analysis of the histograms of all patients was used to identify the most common value of these parameters that were used as input for data simulation. Two different AIFs, displayed in the bottom two plots, were used for both data simulation and subsequent fitting.

All models could be fitted to the data appropriately within an isocontour of 70%. The applied acquisition protocol was feasible for tracer kinetic analysis with compartment models, providing sufficient data quality in terms of temporal resolution and signal-to-noise ratio. We could find no evidence against application of either of the models on clinical patient data. The standard 1TCM and 2TCM fitted the data very well, with good fit quality and reasonably low χ^2_{red} , however, the 1TCM yielded failed fits with exceptionally high χ^2_{red} in several cases. The simplified 1TCM with $V_B = 0$ presented with poorer fits and the model did not properly represent the curve shapes. Both versions of the 1TCM yielded reasonable estimates on transfer rates K_1 and k_2 . The 2TCM yielded the least stable parameter estimates, especially for k_2 . There were no hints towards overfitting of the data with the 2TCM, as in fact it yielded higher χ^2 , (lower fit quality) than the standard 1TCM.

2TCM, as in fact it yielded higher χ^2_{red} (lower fit quality) than the standard 1TCM. Estimates on the blood volume V_B were reasonable and showed similar patterns of increased and decreased values for the 1TCM and 2TCM, indicating that this parameter is not negligible and the simplified 1TCM might not be an adequate description of uptake kinetics. This is conceivable, as high-grade glioma present with

Combination	K ₁ [10 ⁻² min ⁻¹]	k ₂ [10 ⁻² min ⁻¹]	k ₃ [10 ⁻² min ⁻¹]	k ₄ [10 ⁻² min ⁻¹]	V _B [ml/100 ml]
1	10	20	2.5	5	5
2	10	20	7.5	5	5
3	10	60	12.5	5	5
4	10	45	7.5	5	5
5	10	20	12.5	5	5
6	20	20	2.5	5	5
7	20	20	7.5	10	5
8	20	60	12.5	5	5
9	40	45	2.5	20	5
10	40	60	7.5	5	5

Table 3. Parameter values for K_1 , k_2 , k_3 , k_4 and V_B from the 2TCM used for simulation of time activity curves. Each parameter combination was used with either one of the two AIF types (Fig. 6) to simulated 10000 curves. Gaussian random numbers were added to the simulated curves, in order to simulate noise at the same level as the measured patient TACs. These simulated data were in terms fitted with the 2TCM in order to evaluate precision and robustness of parameter estimates from the 2TCM in data of our quality (temporal resolution, sampling, SNR).

enhanced vascularization and thus, a large blood volume, whereas the fraction of blood vessels is approximately 2 to 4% in normal brain tissue²⁵.

A large source of error in tracer kinetic modeling is the selection of an appropriate arterial input curve³⁴. Ideally, the AIF would be derived from blood sampling during tracer administration; however, this invasive procedure is rarely feasible with patients. Furthermore, in retrospective settings, such an AIF is impossible to acquire. Therefore, image-derived input functions are often chosen, even though they are prone to error due to partial volume effects, motion during acquisition, etc. In this study, image-derived input functions were carefully extracted from carotid arteries, applying several suggested methods³⁴ like co-registration with MRI and visual inspection of TACs in included voxels, in order to minimize distortion of the arterial signal. Nonetheless, no ground truth AIF was available for comparison, and underestimation of arterial tracer concentration, especially in the peak region, can influence parameter estimates of kinetic modeling. No relation was found between the quality of fits and the AIF type, even though it was assumed that fits with AIFs of type III could yield poorer results due to an underestimation of the peak activity.

In many cases, temporal resolution is increased for the initial frames in order to more precisely sample the peak concentration of the AIF and hence, improve parameter estimates. In principle this is possible, as most PET dynamic data is acquired in list mode and afterwards sampled to respective time frames at reconstruction. However, higher temporal resolution always comes at the cost of reduced SNR, which on the other hand decreases quality of the extracted arterial TAC and thus, fit quality³⁵. In contrast to MRI, the signal from the reconstructed PET images is the accumulation of all decays measured between time frames, thus forming an integral signal. This aspect potentially reduces the risk of underestimating the peak activity in the AIF.

It was found that the parameter V_B provides a diagnostic value for tumor grading, especially in the standard 1TCM. Overall V_B from the 1TCM was 7.5 ml/100 ml for grade III tumors and 11.6 ml/100 ml for grade IV tumors (p = 0.02518 after multiple-testing correction). Using the 2TCM yielded lower estimates for V_B of 5.9 ml/100 ml in grade III glioma and 9.1 ml/100 ml in grade IV glioma. These estimates are comparable to values published in the literature, that were derived using dynamic contrast-enhanced MRI (DCE MRI)^{36,37}. Prediction of tumor grade in recurrent glioma via imaging has a clinical impact, as these tumors may derive after long-latency period from lower-grade glioma and are often no more biopsied. Therefore, differentiation of tumor grades based on dynamic ¹⁸F-FET PET scans could provide valuable input in predicting the outcome in recurrent setting.

Parameter estimates were further correlated with tumor grade and OS. Parameter estimates from the 2TCM hinted towards correlation with patients' survival, further indicating the additional value of detailed tracer kinetic analysis in ¹⁸F-FET PET. Additional studies are required to validate potential correlations between 2TCM parameters and OS.

With the 2TCM being more detailed but also less stable compared to the 1TCM, the question arises, which model fit the data more adequately, and thus, better represents the underlying tracer kinetics. Therefore, accuracy and robustness of the more complex 2TCM were investigated by simulating TACs of 10 tissue types and fitting this synthetic data with the 2TCM. Since no complete set of reference values for exchange rates K_1 , k_2 , k_3 , k_4 and V_B was given by the literature, we determined 10 common parameter combinations in our patient data and used these, together with measured patient AIFs, to simulate time-activity curves at the same data quality as the patient PET scans

Fit quality and stability as well as errors on parameter estimates were quantified in order to assess reliability of this model for data at the same quality (SNR, temporal resolution) as patient scans. Results showed sufficient fit quality and precision of parameter estimates. K_1 and V_B are parameters with high stability and accuracy. k_3 and k_4 exhibit large errors at large values (\sim 0.20 min $^{-1}$) but are otherwise robust estimates. k_2 proved to be the least stable and least reliable parameter. Interestingly, AIFs of type II, where the initial frame already includes enhanced activity instead of the zero base line, provided better fit-quality and smaller errors, contrary to the expectations. It was initially hypothesized that a zero-activity first frame is required for a proper description of the peak activity.

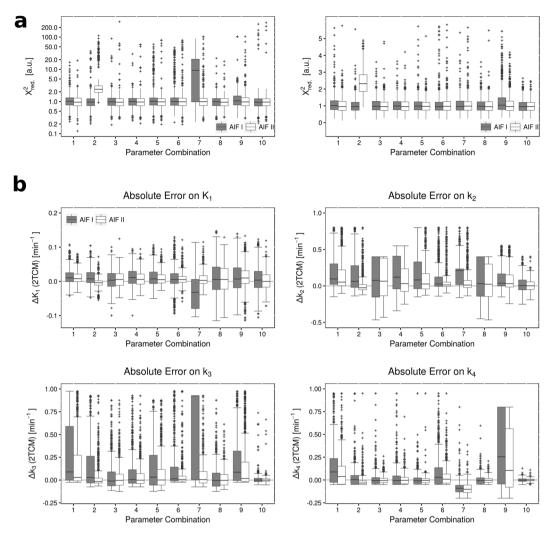


Figure 9. Results from fitting simulated data with the 2TCM. Figure 7 (a) shows goodness-of-fits in terms of reduced X^2 , for each of the 10 different parameter combinations (with both AIFs). Due to outliers at very high values, the y-axis in the left plot is displayed on a logarithmic scale. For more detailed evaluation, the right plot shows the distribution of X^2 at an enlarged linear scale. Apart from two exceptions, both AIF types yielded similar fit quality. Figure 7 (b) shows the distribution of absolute errors in each of the four model parameters K_1 , k_2 , k_3 and k_4 . The absolute error was calculated as the parameter estimate minus the true value used for simulation. While K_1 yields good accuracy and robustness, k_2 showed lowest stability of all parameters. k_3 and k_4 showed tendencies towards positive values for the errors, indicating a systematic overestimation of these two parameters.

Several authors have studied the value of dynamic ¹⁸F-FET PET for grading and prognosis in both low- and high-grade glioma ^{9,10,20,22,38}. Pöpperl *et al.* showed the superior value of dynamic acquisition protocols over static ones for grading in glioma patients²¹. However, for analysis of dynamic scans, most authors rely on qualitative description such as the overall tumor TAC shapes, the determination of semi-quantitative values like SUV at different time points²² or the time-to-peak activity^{9,20}. To our knowledge this study provides the first quantitative report on detailed parameter estimates from these compartment models. Thiele *et al.*, performed tracer kinetic modeling with the 1TCM and 2TCM amongst other analysis techniques of dynamic ¹⁸F-FET PET in grade IV glioma patients²³. However, correlations of parameters from compartmental analysis with clinical outcome were missing due to the low stability of their results. Furthermore, the sinus sagittalis was used for derivation of image-based arterial TACs, which only gives the tracer concentration in venous blood. In addition, neither fit quality nor mentioned instability nor reliability of parameter estimates was further quantified. In contrast, the results of the current analysis provide an estimate on precision and robustness of tracer-kinetic analysis with the 2TCM by evaluating fits to simulated data.

Recently, pharmacokinetic modeling of ¹⁸F-FET tracer kinetics in a syngeneic orthotopic preclinical model was reported by injecting F98 glioblastoma cells into the right hemisphere of Fisher rats³⁹. They found a favorable performance of the 2TCM in terms of model selection criteria AIC, *F* test and residual plots. This finding is in accordance with our study, showing that the 2TCM presents with lowest cAIC and thus appears to be the best representation of the data. However, there are some differences in their study compared to ours. First, F98 is

Combination	AIF	ΔK ₁ [%]	$\Delta k_2 [\%]$	Δk ₃ [%]	$\Delta k_4 [\%]$	ΔV_{B} [%]
	I	10.5	47.9	356.9	176.0	-7.0
1		[-1; 25]	[10; 151]	[-9; 2357]	[-52; 471]	[-23; 11]
	II	7.9	25.9	115.6	76.0	-5.3
		[-1; 21]	[1; 110]	[-34; 1091]	[-95; 302]	[-16; 6]
_	I	7.4	31.5	38.0	6.8	-6.6
		[-4; 26]	[-10; 139]	[-43; 349]	[-87; 100]	[-24; 11]
2	II	-4.0	-12.5	-21.1	-66.9	-8.8
		[-11; 2]	[-26; 9]	[-44; 28]	[-100; -19]	[-19; 5]
	I	3.3	12.7	-8.1	-14.5	-0.5
2		[-15; 23]	[-26; 67]	[-51; 72]	[-81; 53]	[-18; 17]
3	II	5.4	10.8	-2.6	-12.1	-1.5
		[-12; 22]	[-22; 63]	[-46; 52]	[-59; 36]	[-13; 13]
	I	11.0	26.4	6.8	-12.8	-4.1
4		[-6; 29]	[-9; 91]	[-47; 152]	[-100; 90]	[-21; 14]
4	II	5.8	6.9	-2.0	-7.9	-1.9
		[-8; 21]	[-17; 52]	[-50; 94]	[-81; 57]	[-16; 10]
	I	7.1	40.9	25.5	-16.0	-3.4
_		[-6; 27]	[-19; 165]	[-45; 218]	[-81; 46]	[-21; 16]
5	II	5.0	12.9	0.5	-10.8	-5.3
		[-5; 19]	[-21; 85]	[-44; 93]	[-60; 30]	[-18; 8]
	I	2.9	13.0	52.3	56.4	-1.3
		[-3; 11]	[-4; 62]	[-43; 571]	[-85; 271]	[-19; 18]
6	II	2.6	6.7	25.8	16.8	-2.4
		[-1; 7]	[-4; 26]	[-40; 171]	[-69; 131]	[-15; 11]
	I	-16.1	105.7	1233.3	-45.5	191.6
_		[-40; 3]	[9; 117]	[-4; 1233]	[-66; -29]	[-4: 282]
7	II	1.4	5.7	7.4	-51.1	-0.4
		[-3; 8]	[-11; 38]	[-43; 125]	[-69; -28]	[-13; 12]
	I	2.8	5.4	-3.3	-12.0	799.2
_		[-12; 21]	[-24; 67]	[-54; 61]	[-82; 48]	[780; 815]
8	II	2.8	3.8	-2.6	-7.3	798.5
		[-11; 19]	[-24; 50]	[-43; 48]	[-54; 33]	[786; 811]
9	I	1.7	8.3	344.8	127.8	3.1
		[-5; 10]	[0; 37]	[-23; 1272]	[-22; 400]	[-19; 33]
	II	2.5	6.8	69.5	52.4	-2.0
		[-2; 8]	[-4; 33]	[-63; 786]	[-40; 281]	[-16; 14]
	I	0.9	0.8	-1.1	-4.7	-1.4
		[-5; 7]	[-9; 13]	[-24; 26]	[-31; 25]	[-20; 17]
10	II	0.0	0.3	-1.1	-1.0	-0.1
		[-4; 5]	[-8; 9]	[-18; 19]	[-20; 18]	[-13; 12]

Table 4. Median relative errors on parameter estimates from fitting simulated data of 10 different parameter combinations (Table 3) and two different AIFs with the 2TCM, for each of the model parameters K_1 , k_2 , k_3 and k_4 and V_B . The 25^{th} and 75^{th} quantile of the errors are denoted in square brackets under the median value. Normalizing the absolute error to the true parameter value used for simulation, and multiplying by 100 calculated relative errors. Quantiles of k_2 show, that even though errors on this parameter are low in most cases, it presents with high instability. k_3 and k_4 show large relative errors, which is likely to be due to their low original values

carcinogen (nitrosourea-mediated mutagenesis) induced rat glioblastoma model that might differ not only with respect to the molecular characteristics affecting radiosensistivity (e.g., presence of BRCA1 mutation) but also tumor invasion and angiogenesis pattern from the human glioblastoma in patients 40,41 . A second pivotal difference between the two studies is that they do not consider the parameter blood volume ($V_{\rm B}$) in their compartment models. Indeed, we found that neglecting the blood volume in the 1TCM (simplified 1TCM) model yields poor results. However, high-grade glioma are highly vascularized necessitating inclusion of $V_{\rm B}$ in modeling these tumors, at least in patients. Together, our data underscore the importance of considering $V_{\rm B}$ in dynamic modeling. Moreover, we performed simulation analyses to investigate accuracy and robustness of parameter estimates. Results showed that the 2TCM is in principle feasible and accurate, however, at the cost of reduced fit stability.

Overall, the standard 1TCM provided the best results in terms of feasibility and robustness with an appropriate description of the tracer kinetics. This is in concordance with results reported in animal studies²⁴. Additionally, correlation of K_1 with overall patient survival was visible in K_1 from both the 1TCM and 2TCM.

The blood volume V_B appears to be overestimated by the 1TCM compared to values reported previously in the literature³⁶. Precision and robustness of the estimates from the 1TCM should be further investigated, e.g. with a simulation study similar to the one we conducted on the 2TCM in a larger population.

Fitting dynamic 18 F-FET PET data with a 2TCM appears to hold some valuable information on tumor heterogeneity and substructure. The 2TCM provided the best model representation according to the Akaike information criterion 28,29 . Estimated V_B from the 2TCM yielded reliable values with good accuracy and robustness and showed a trend towards prognostic value for grading, as a trend towards higher values for K_1 and V_B was observed in grade IV tumors compared to grade III tumors. k_4 appears to correlate with progression free survival. Larger patient cohorts need to be analyzed to further investigate these findings. Furthermore, the combination of parameters from this more complex model with physiological measures derived from other imaging modalities (e.g. dynamic contrast-enhanced MRI) could provide additional, relevant information on tumor tissue composition.

Conclusion

The presented study provides a first overview on the diagnostic and prognostic value of compartmental analysis for dynamic ¹⁸F-FET PET in recurrent high-grade glioma patients. The models revealed an improved resolution of tumor substructure (e.g. vascularization). Despite the limited size of the cohort, correlation of parameters with tumor grade and overall survival yielded promising results, which warrants further exploration. It is yet to be investigated, whether our findings can be translated to primary, untreated tumors. However, feasibility of the analysis is independent of this, enabling a proper conduction of such a study.

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Author Contributions

C.D., J.D. and A.A. designed the study and conceived the analysis. A.A.O. and U.H. were responsible for data acquisition. R.F. supplied the necessary software support. M.I. supplied the necessary support on tracer-kinetic modeling and model comparison. C.D. analyzed the data. C.D. and A.A. wrote the manuscript. All authors critically revised the manuscript.

Additional Information

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