

University of Groningen

Measurement of the anisotropy power spectrum of the radio synchrotron background

Offringa, A. R.; Singal, J.; Heston, S.; Horiuchi, S.; Lucero, D. M.

Published in:
Monthly Notices of the Royal Astronomical Society

DOI:
[10.1093/mnras/stab2865](https://doi.org/10.1093/mnras/stab2865)

IMPORTANT NOTE: You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

Document Version
Publisher's PDF, also known as Version of record

Publication date:
2021

[Link to publication in University of Groningen/UMCG research database](#)

Citation for published version (APA):

Offringa, A. R., Singal, J., Heston, S., Horiuchi, S., & Lucero, D. M. (2021). Measurement of the anisotropy power spectrum of the radio synchrotron background. *Monthly Notices of the Royal Astronomical Society*, 509(1), 114-121. <https://doi.org/10.1093/mnras/stab2865>

Copyright

Other than for strictly personal use, it is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license (like Creative Commons).

The publication may also be distributed here under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license. More information can be found on the University of Groningen website: <https://www.rug.nl/library/open-access/self-archiving-pure/taverne-amendment>.

Take-down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Downloaded from the University of Groningen/UMCG research database (Pure): <http://www.rug.nl/research/portal>. For technical reasons the number of authors shown on this cover page is limited to 10 maximum.

Measurement of the anisotropy power spectrum of the radio synchrotron background

A. R. Offringa,^{1,2★} J. Singal,³ S. Heston,⁴ S. Horiuchi^{4,5} and D. M. Lucero⁴

¹*Netherlands Institute for Radio Astronomy (ASTRON), Oude Hoogeveensedijk 4, NL-7991 PD Dwingeloo, the Netherlands*

²*Kapteyn Astronomical Institute, P.O. Box 800, NL-9700 AV Groningen, the Netherlands*

³*Physics Department, University of Richmond, 138 UR Drive, Richmond, VA 23173, USA*

⁴*Department of Physics, Virginia Tech University, Blacksburg, VA 24061-0435, USA*

⁵*Kavli IPMU (WPI), UTIAS, The University of Tokyo, Kashiwa, Chiba 277-8583, Japan*

Accepted 2021 September 27. Received 2021 September 10; in original form 2021 June 30

ABSTRACT

We present the first targeted measurement of the power spectrum of anisotropies of the radio synchrotron background, at 140 MHz, where it is the overwhelmingly dominant photon background. This measurement is important for understanding the background level of radio sky brightness, which is dominated by steep-spectrum synchrotron radiation at frequencies below $\nu \sim 0.5$ GHz and has been measured to be significantly higher than that produced by known classes of extragalactic sources and most models of Galactic halo emission. We determine the anisotropy power spectrum on scales ranging from 2° to 0.2 arcmin with Low-Frequency Array observations of two 18-deg^2 fields – one centred on the Northern hemisphere’s coldest patch of radio sky where the Galactic contribution is smallest and the other offset from that location by 15° . We find that the anisotropy power is higher than that attributable to the distribution of point sources above $100 \mu\text{Jy}$ in flux. This level of radio anisotropy power indicates that if it results from point sources, those sources are likely at low fluxes and incredibly numerous, and likely clustered in a specific manner.

Key words: radiation mechanisms: non-thermal – techniques: interferometric – radio continuum: general.

1 INTRODUCTION

A puzzling question to have recently emerged is the origin of the radio background radiation. The background level of radio sky brightness, which is due to some as of now unknown combination of integrated extragalactic sources and a possible large-scale Galactic halo, is dominated by steep-spectrum synchrotron radiation at frequencies below $\nu \sim 0.5$ GHz, and at higher frequencies, it is present along with the otherwise dominant cosmic microwave background (CMB). An apparent bright low-frequency background was reported as early as the 1960s (e.g. Bridle 1967) and 1980s (e.g. Haslam et al. 1982). Interest in this background was renewed by the surprisingly high absolute sky temperature at $\nu \sim 3$ GHz reported by the ARCADE 2 (Singal et al. 2011) stratospheric balloon experiment. Combining the ARCADE 2 measurements from 3 to 90 GHz (Fixsen et al. 2011) with several radio maps at lower frequencies from which an absolute zero level has been inferred (recently summarized in Dowell & Taylor 2018) reveals a synchrotron background brightness spectrum

$$T_{\text{BGND}}(\nu) = 30.4 \pm 2.6\text{K} \left(\frac{\nu}{310 \text{ MHz}} \right)^{-2.66 \pm 0.04} + T_{\text{CMB}} \quad (1)$$

shown in Fig. 1, where T_{CMB} is the frequency-independent contribution of 2.725 K due to the CMB. Following recent works, we refer to this as the radio synchrotron background (RSB).

The reported bright background level is now in extreme tension with estimates of its expected level from the known radio emission

mechanisms in the Universe, as recently summarized in Singal et al. (2018). Several works have considered deep radio source counts and limited the integrated surface brightness from known classes of extragalactic radio sources to only around one-fifth of the radio background brightness level (e.g. Condon et al. 2012; Vernstrom et al. 2014), including recently at 144 MHz (Hardcastle et al. 2020). Thus, to achieve the measured radio background level from point sources would require an entirely new, incredibly numerous, heretofore unobserved population of low-flux radio sources. As an alternative, various types of diffuse extragalactic sources such as cluster mergers (e.g. Fang & Linden 2016) and intergalactic dark matter decays and annihilations in galaxies, clusters, and filaments (e.g. Fornengo et al. 2011; Hooper et al. 2012) have been proposed. Alternatively, a large, bright, roughly spherical synchrotron halo surrounding our Galaxy could explain part of the background (e.g. Subrahmanyan & Cowsik 2013). However, such a large, bright halo would make our Galaxy unique among nearby spiral galaxies (Singal et al. 2015) and would overturn our current understanding of the high-latitude Galactic magnetic field (Singal et al. 2010).

One realm in which the RSB is almost completely unexplored is in its anisotropy. Studies of temperature anisotropy power spectra have helped confirm the source populations responsible for the cosmic infrared (e.g. Ade et al. 2011; George et al. 2015) and gamma-ray (e.g. Broderick et al. 2014) backgrounds, and have been the most important component of CMB science thus far (e.g. Bennett et al. 2013).

The only direct constraints available in the literature on the anisotropy of the RSB at the most relevant angular scales are

★ E-mail: offringa@astron.nl

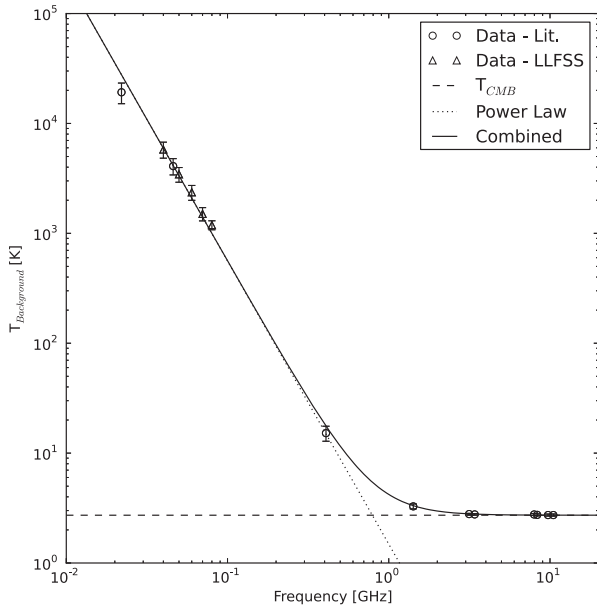


Figure 1. The measured radio background brightness spectrum in radiometric temperature units reproduced from Dowell & Taylor (2018), as measured by the few measurements and maps where an absolute zero-level calibration was either explicit or obtained, including that work. The brightness shows a clear power-law rise at frequencies below ~ 10 GHz, above the otherwise dominant CMB level represented by the dashed line.

from confusion noise limits at a few discrete scales and based on measurements where considerations of the radio background in particular were incidental. These include decades-old measurements in the GHz range overwhelmed by the CMB by an order of magnitude or greater, specifically based on observations made with the Very Large Array at 8.4 GHz (Partridge et al. 1997) and 4.9 GHz (Fomalont et al. 1988), and the Australia Compact Telescope Array at 8.7 GHz (Subrahmanyan et al. 2000). There are also recent measurements of the sky power spectrum at 150 MHz in several fields made with the Giant Metrewave Radio Telescope recently presented in Choudhuri et al. (2020). The results presented there are in a more limited angular scale range, and in fields with higher Galactic diffuse emission structure contribution, than those presented here, and did not directly address specifically the question of the anisotropy power of the RSB. At larger angular scales than those considered here, where the angular power is dominated by the large-scale Galactic diffuse synchrotron structure, there are determinations of the angular power at 408 MHz reported by La Porta et al. (2018).

In this work, we present a power spectrum of measured anisotropies of the RSB over the angular range from 2° to 0.2 arcmin based on dedicated LOW-Frequency ARray (LOFAR; van Haarlem et al. 2013) observations at 140 MHz of two 18-deg² fields. Section 2 describes the observations and data reduction and analysis methods, Section 3 presents the resulting power spectra, Section 4 explores possible point source populations that could produce the measured anisotropy power, and Section 5 presents a discussion. Appendix A provides a reference for considering the conversion factors between different computations and scalings of angular power that are relevant when bridging regimes and methods of determination where different conventions are in use.

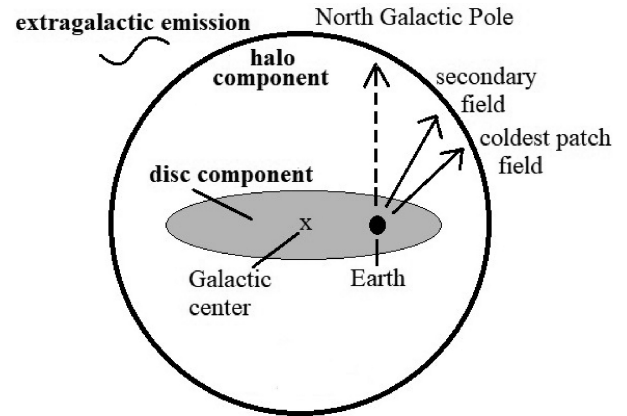


Figure 2. Schematic representation of the coldest patch and secondary target fields observed in this work in the context of a simple model of Galactic diffuse radio emission consisting of an ellipsoidal plane-parallel component due to the Galactic disc and a larger, spherical halo component, each centred on the Galactic Centre. The coldest patch target field is in the direction of minimal integrated line-of-sight total contribution from the two components in the Galactic Northern hemisphere. Such two-component models of large-scale diffuse Galactic radio emission are commonly utilized (e.g. Subrahmanyan & Cowsik 2013; Singal et al. 2015).

2 OBSERVATIONS AND DATA REDUCTION

We use data from 8 h of dedicated observing with LOFAR in high-band antenna dual mode with Dutch stations only (23 core, 14 remote) in the band from 110 to 190 MHz on 2019 November 27. As optimally this measurement should be done on a region with the minimum amount of Galactic diffuse foreground spatial structure, we chose a field centred on the Galactic Northern hemisphere ‘coldest patch’ (Kogut et al. 2011; $9^{\text{h}} 38^{\text{m}} 41^{\text{s}} +30^{\circ} 49' 12''$, $l = 196:0 b = 48:0$), the region of lowest measured diffuse emission absolute temperature and thus where the integrated line-of-sight contribution through the Galactic components is minimal. LOFAR allows a simultaneous observation of an additional field offset by 15° in an adjacent 48-MHz wide band, so we chose a location towards the North Galactic Pole from the coldest patch of $10^{\text{h}} 25^{\text{m}} 00^{\text{s}} +30^{\circ} 00' 00''$ ($l=199:0 b=57:9$), which should have a slightly higher but still nearly minimal total Galactic contribution. Fig. 2 shows a schematic representation of the observed fields relative to a commonly employed simple model of the Galactic diffuse radio emission structure. The data cube consists of 666 baselines (all pairs of correlations) with four linear polarization pairs per visibility in 243 frequency channels with 2-s integrations for a total of 1.4 TB of data per target field. The 243 frequency channels are of equal width of 180 KHz, and the filtering is done with a polyphase filter bank. In addition to the target fields, we observed the flux calibrator 3C 295.

Because we are interested in scales that are much larger than the effect of ionospheric activity, we only perform direction-independent calibration, thereby avoiding the effect of signal suppression that might incur during direction-dependent calibration. We have used two different methods for direction-independent calibration and imaging. The first approach is to use PREFACTOR,¹ the standard automated LOFAR direction-independent calibration pipeline (van Weeren et al. 2016; Williams et al. 2016), which makes use of several software packages, including the Default Pre-Processing Pipeline (DP3; van Diepen, Dijkema & Offringa 2018), LOFAR SolutionTool

¹<https://github.com/lofar-astron/prefactor>

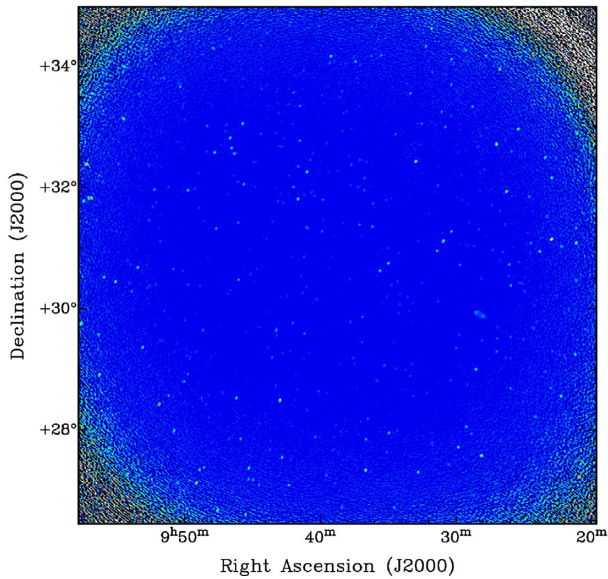


Figure 3. An image of the coldest patch target field resulting from the imaging procedure discussed in Section 2. The synthesized beam measures $1.5 \text{ arcmin} \times 1 \text{ arcmin}$. This field contains 3.6-Jy source 4C 32.30, which can be used for self-flux calibration, and an extended FR II galaxy (visible just to the lower right-hand side of the middle of the field). All sources are removed for power spectrum determination, as point sources manifest power on all angular scales.

(LOSOTO; de Gasperin et al. 2019), and AOFLAGGER (Offringa, van de Gronde & Roerdink 2012). Because this pipeline has not been developed for power spectrum experiments, for verification we also calibrate our data in a manual approach.

Manual calibration is only performed for the coldest patch field. For manual calibration, we start with running AOFLAGGER to flag outlying data points due to radio-frequency interference (RFI) contamination and one outlying station. We perform initial flux and phase calibrations for each sub-band using the flux calibrator observation, which are then applied to the target fields. We image the target fields with WSCLEAN (Offringa et al. 2014) with primary beam correction and standard CLEAN settings to extract an initial point source model for self-calibration. Specifically, we first run the source extractor AEGEAN (Hancock, Trott & Hurley-Walker 2018) with a high flux threshold of 9σ to extract a shallow model, containing about 300 sources. Following this, we run self-calibration using the model on 25 sub-bands and image at a higher resolution of 45 arcsec. We next re-run AEGEAN with a lower flux threshold (7σ), extracting 2396 sources.

Many of these sources are near the edge of the primary beam and so are likely false detections. We cut out all sources that are at a place in the image where the beam has less than 5 per cent gain, reducing the model to 644 sources with almost no false positives. Extended sources, including one prominent Fanaroff–Riley type II (FR II) galaxy, are excluded from calibration. Source 4C 32.30 with flux 3.6 Jy (WalDRAM et al. 1996) is near the middle of the coldest patch target field and is used for flux calibration. Using these full calibration solutions, we re-image the target field with WSCLEAN with 20-arcsec resolution. An image of the coldest patch target field is shown in Fig. 3.

The results of the automated and manual approach are found to be similar on the coldest patch field, so we process the secondary target field only with the automated approach using PREFACTOR. Before

making power spectra, we subtract the foreground sources using a deep WSCLEAN multifrequency deconvolution using automasking (Offringa & Smirnov 2017). The automasking ensures that all sources $\geq 7\sigma$ are subtracted to a 1σ level. To avoid subtracting a diffuse component, we do not use multiscale CLEAN.

3 POWER SPECTRUM

3.1 Full angular power spectrum

Our angular power spectrum pipeline is based on the pipeline described by Offringa, Mertens & Koopmans (2019), which is originally written for the LOFAR Epoch of Reionization project (Mertens et al. 2020). Our angular pipeline produces a power spectrum of fluctuations from the source-removed target field images. We use the central 4.3 deg^2 of each target field image for the determination of the angular power spectra. A quantitative discussion of the procedure for forming a power spectrum from an interferometric image is presented in Appendix A. The steps in making a power spectrum are as follows.

- (i) Make naturally weighted images using multifrequency synthesis from the source-subtracted data. We use WSCLEAN for this with increased accuracy settings (see Offringa et al. 2019).
- (ii) Convert the images of flux density into units of temperature (kelvin) using equation (A17).
- (iii) Take the spatial Fourier transform of the images and point spread functions (PSFs) to create a grid in complex (u, v) space for both.
- (iv) Elementwise divide the complex uv images by the complex value of the uv PSFs.
- (v) Average the power in annuli and normalize these.

This method of determining the power spectrum, where we correct for the (in our case, natural) image weighting function in uv space, alleviates the need to perform a bias correction of the power spectrum. Otherwise, image-based reconstruction of power spectra can give a biased estimate of the true sky signal due to the correlated noise in the image domain (Dutta & Nandakumar 2019).

The resulting power spectrum of fluctuations is shown in Fig. 4, for both the coldest patch and secondary target fields. We also show the spectrum of fluctuations calculated for twelve 4-MHz wide sub-bands separately. The lowest frequency sub-band has approximately 17 times more power in these K^2 units than the highest frequency sub-band because of the spectral dependence of synchrotron radiation (cf. equation 1), which is a bit over four times as bright in radiometric temperature units (and thus around 17 times as bright in K^2 units) at 190 GHz than at 110 GHz. The angular power is lower in the full bandwidth because of more complete uv coverage.

These measurements will have a contribution from the noise of the instrument. To calculate this contribution, we extract Stokes V visibilities and measure the differential variance between consecutive Stokes V visibilities in time, multiply by 2, and assume that this is a representative noise value for all visibilities. We calculate the noise power spectrum by replacing all visibilities by randomly sampled Gaussian values with the calculated variance, produce images, and calculate a power spectrum from the images as described. The result is shown as the dashed line in Fig. 4. Given that the noise power is at least an order of magnitude below the measured power, clearly our measured power is dominated by something other than the system noise. Additionally, while one would expect the power in the full band to be the average of the sub-bands for the case of noise-dominated power, in this case with the noise contribution sub-dominant, the

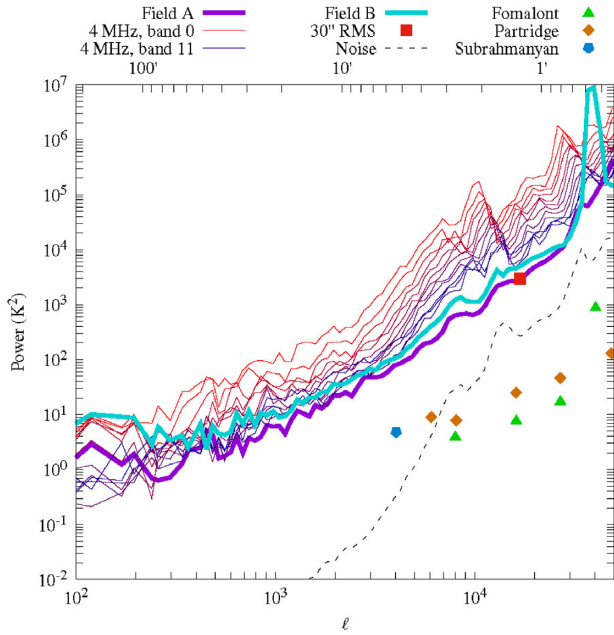


Figure 4. Measured anisotropy power spectrum of the radio sky centred at 140 MHz. Shown are curves for the full bandwidth of the coldest patch field (field A) and the secondary field (field B), as well as for twelve 4-MHz wide sub-bands of field A. The anisotropy in field A deduced by considering the average noise per beam in the image with the synthesized beam tapered to 30-arcsec FWHM is also shown and agrees at the relevant angular scale, given by equation (4). We also show comparison levels inferred by the noise per beam at 8.7, 8.4, and 4.9 GHz in different fields as calculated by Holder (2014) and scaled here to 140 MHz assuming a synchrotron power law of -2.6 in radiometric temperature units. The amount of angular power is ~ 1.4 times higher for field B compared to field A (in K^2 units) across a range of angular scales, as discussed in Section 5. All angular powers are expressed here in the $(\Delta T)_\ell^2$ normalization.

more complete uv coverage of the full band will result in lower angular power.

3.2 Power from rms fluctuations

We can also calculate the power on a specific, discrete angular scale in a completely different, complementary way, following a procedure discussed in Holder (2014).

(i) The noise per beam in the image $\Delta S_{Jy/PSF}$ is measured with the synthesized beam tapered to 30-arcsec full width at half-maximum (FWHM). The noise level of this image is $720 \mu Jy$.

(ii) The beam is fitted to an elliptical Gaussian with major and minor axes w_{maj} and w_{min} to calculate the synthesized beam solid angle in radians,

$$\Omega_{PSF} = \pi(w_{maj} \times w_{min}) \times \left(\frac{1}{60}\right)^2 \times \left(\frac{\pi}{180}\right) \times \left(\frac{1}{4 \log 2}\right). \quad (2)$$

(iii) The resulting temperature fluctuation ΔT is calculated by

$$\Delta T = \Delta S_{Jy/PSF} \frac{10^{-26} c^2}{2k_B \nu^2 \Omega_{PSF}}, \quad (3)$$

to achieve ΔT on the angular scale corresponding to a Gaussian beam of 30-arcsec FWHM.

The fluctuation power calculated in this way is shown in Fig. 4 for the coldest patch target field. The angular scale corresponding

to a 30-arcsec FWHM Gaussian beam does not exactly match a 30-arcsec spherical harmonic due to the beam taper, which is why the rms measurement is not exactly placed at 30 arcsec (see the upper horizontal axis in Fig. 4). To calculate the corresponding angular scale, we have used the formula provided in Holder (2014), which gives the ℓ value corresponding to a particular synthesized beam FWHM expressed in radians:

$$\ell = \frac{2.35}{FWHM}. \quad (4)$$

We see that the fluctuation power calculated directly from the noise per beam matches that determined from a full power spectrum at the particular angular scale. We also show the fluctuation power obtained in this way by Holder (2014) from the measurements of Partridge et al. (1997), Fomalont et al. (1988), and Subrahmanyam et al. (2000), scaling from the relevant GHz frequencies to 140 MHz by a synchrotron power law of -2.6 in radiometric temperature units.

3.3 Power from potentially unremoved point sources

In order to quantify the contribution of potentially unremoved point sources in the images to the measured angular power, we created a Monte Carlo catalogue of simulated sources. We interpolate the simulated sources on to a grid (using sinc interpolation) and simulate visibilities from the resulting sky image to apply the instrumental effects that affect the power spectrum (uv sampling and the primary beam). We use the Image Domain Gridding (IDG; van Tol, Veenboer & Offringa 2018) inside WSCLEAN to apply the time- and frequency-dependent LOFAR primary beam. The resulting visibilities are processed with our imaging and power spectrum generation pipeline.

We distributed the sources in flux (S) according to four models presented in Franzen et al. (2016), based on their measured and extrapolated deep source counts at 150 MHz, of the form

$$\begin{aligned} n(S) = \frac{dn}{dS} &= k_1 \left(\frac{S}{Jy}\right)^{\gamma_1} Jy^{-1} sr^{-1} \text{ for } 0.01 < S < 6.0 \text{ mJy} \\ &= k_2 \left(\frac{S}{Jy}\right)^{\gamma_2} Jy^{-1} sr^{-1} \text{ for } 6.0 < S < 400 \text{ mJy} \end{aligned} \quad (5)$$

and randomly in RA and Dec., with frequency spectral indices distributed normally around -2.6 in radiometric temperature units with a standard deviation of 0.1. The parameters k_1 , k_2 , γ_1 , and γ_2 are given for four models in table 2 of that work for the extrapolated portion. The four models, which are identical in the number of high-flux sources, but differ in the number of low-flux sources, result in roughly the same amount of angular power at all scales, indicating that the contribution to the angular power is dominated by the higher flux sources in this flux range. We then introduce a simple sinusoidal spatial clustering in both RA and Dec. on scales of 1 and 10 arcmin to see whether clustering can have a significant effect on the observed angular power resulting from this model, with results for one of the models (model ‘A’) visualized in Fig. 5.

The clustering on a 1-arcmin scale has very little effect on the measured angular power on any angular scale for this model or any of the four. This is because 1 arcmin is considerably less than the average separation of the higher flux sources, which primarily contribute to the measured angular power. In fact, the clustering added in this way on the 1-arcmin scale slightly reduces the angular power on some angular scales because the angular power involves circular averaging, while the sinusoidal variation has been added to essentially rectangular RA and Dec. coordinates at this scale. The 10-arcmin clustering manifests an appreciable increase in angular power on that particular scale. However, this only propagates to

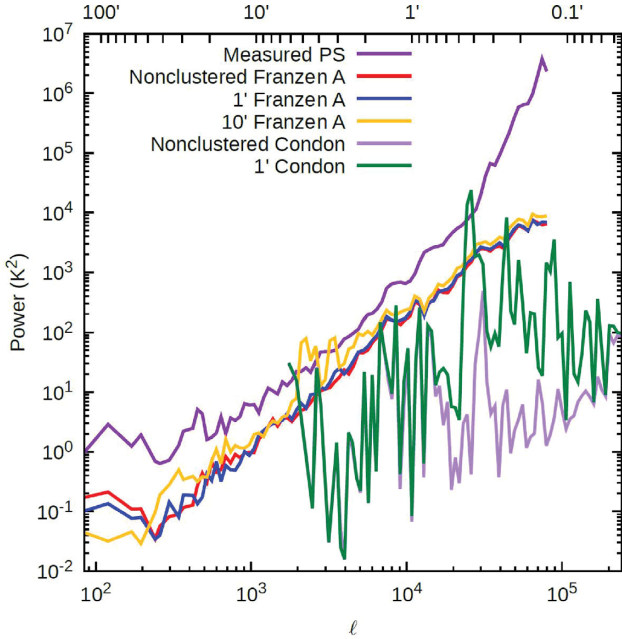


Figure 5. Measured power spectrum (for the coldest patch target field) and the simulated full-pipeline anisotropy power spectrum resulting from (i) the upper limit of potential unremoved point sources down to 100 μ Jy according to a point source model presented in Franzen et al. (2016) discussed in Section 3.3, (ii) the upper limit from the same Franzen et al. (2016) model with sinusoidal clustering added on scales of 1 and 10 arcmin, (iii) potential point sources down to nJy fluxes according to the point source model presented in Condon et al. (2012) discussed in Section 4, which can reproduce the surface brightness level of the RSB, and (iv) the same Condon et al. (2012) model with sinusoidal clustering added on a scale of 1 arcmin.

some smaller angular scales, and we see from the 1-arcmin clustering case that below a certain angular scale (somewhere between 10 and 1 arcmin), clustering in these models cannot add further angular power.

Given that we clean the images to a flux threshold well below 400 mJy with residuals of only around ~ 20 mJy, and that the contribution to the angular power is dominated by the higher flux sources in these models, we emphasize that this modelled observed power resulting from unremoved sources above 100 μ Jy is an upper limit and likely a significant overestimate. This indicates that unsubtracted point sources in the images above the flux detection limit are not a major contributor to the measured angular power, and that sources above 100 μ Jy generally cannot produce the measured angular power on at least some angular scales.

4 POSSIBLE SOURCE POPULATION

With the angular anisotropy power of the radio sky being larger than that can be accounted for by point sources above 100 μ Jy, the question arises as to what flux source count distributions [often denoted by $n(S)$ or $\frac{dn}{dS}$] of faint point sources could give rise to the measured angular power. As discussed in Condon et al. (2012), regarding the surface brightness of the RSB, if it is indeed that given by equation (1), then if originating from point sources, given the measured constraints on the source counts above 10 μ Jy, those sources must be lower flux and incredibly numerous. We will consider here the possibility that the angular power as well is due to a large number of low-flux point sources.

Condon et al. (2012) present three hypothetical low-flux point source population flux distributions, which could provide the mea-

sured surface brightness of the RSB. These distributions are of the approximate form

$$n(S) = \frac{A}{S^2} \exp\left(-4 \ln(2) \frac{[\log(S) - \log(S_{pk})]^2}{\phi^2}\right) \text{Jy}^{-1} \text{sr}^{-1}, \quad (6)$$

with the normalization A , width ϕ , and the flux of the peak contribution to the background per log flux bin S_{pk} given for the three models. All three models feature a large number of low-flux sources with values of S_{pk} of approximately 0.03, 0.02, and 0.003 μ Jy and a density of sources on the sky exceeding that measured in the *Hubble Ultra Deep Field* by at least an order of magnitude.

In a procedure similar to the simulation discussed in Section 3.3, we simulate point source populations distributed in flux according to equation (6) with frequency spectral indices distributed normally around -2.6 in radiometric temperature units with a standard deviation of 0.1 and run the resulting simulated sky through our simulation, imaging, and power spectrum generation pipeline as described there. We adopt the model with the smallest number of sources, which still results in an average around 200 million sources in 1 deg^2 , or 150 sources per pixel. Due to the very large number of sources in this model, computing limitations requires the simulated field of view to be smaller, 0.5 on a side, so the calculation of angular power on angular scales larger than this is not possible. The resulting power can still be calculated for most of the range of angular scales of relevance depicted in, for example, Fig. 4. The result for sources distributed randomly in RA and Dec. is shown in Fig. 5. It is seen that because of the very large average number of sources per pixel, the proportional variation in brightness among pixels is small and therefore the resulting angular power in this isotropic model is low. To preliminarily investigate the effects of clustering for this model, we adopt the same simple sinusoidal clustering on a 1-arcmin scale as discussed in Section 3.3, with results also shown in Fig. 5. In this case, with the very large number of sources, the added clustering increases the simulated observed angular power significantly on all angular scales that are equal to and smaller than that of the clustering scale (corresponding in this case to $\ell \sim 11\,000$). Thus, we conclude that it is a possibility that with the appropriate clustering on many angular scales over a wide range, the Condon et al. (2012) model of many very low flux sources could reproduce the observed angular power.

5 DISCUSSION

We have carried out a dedicated measurement with LOFAR to determine the anisotropy angular power of the radio background at 140 MHz on angular scales ranging from 2° to 0.2 arcmin. As discussed in Section 2, our results stem from 8 h of observing of two fields with a minimal amount of Galactic diffuse foreground structure. As shown in Section 3, both the direct method of imaging, removing sources, and calculating the power spectrum, and the method of considering the noise per beam in the image with the synthesized beam tapered to a specific width yield a measured angular power that is more than that would result from point sources above 100 μ Jy, either distributed randomly spatially or clustered. As shown in Fig. 4, the angular power is also at least an order of magnitude larger than that inferred from measurements at GHz frequencies.

Our measured angular power is around a factor of ~ 3 (in the ΔT normalization) lower than that reported by Choudhuri et al. (2020) in the angular scales of overlap (in the range $10^2 \leq \ell \leq 3 \times 10^3$), applying equation (A12) to convert into the plotted C_ℓ units of their

fig. 1. They observe four fields at a variety of Galactic latitudes and longitudes, with all looking through significantly more Galactic structure than the fields in this work. Their reported angular power differs somewhat at various reported ℓ values over their different fields, but this manifests no apparent correlation with the amount of Galactic structure along a line of sight, indicating that the discrepancy between their fields, and more relevantly with the results here, may be due to instrumental effects and analysis considerations. Interestingly, our measured angular power quite closely matches the *modelled* angular power of unsubtracted point sources below 50 mJy reported in Choudhuri et al. (2020).

The angular power measured here is due to a combination of that due to extragalactic sources, that due to structure in Galactic diffuse emission, and, in principle, that due to possible considerations such as RFI, sidelobe pickup, and residual power from subtracted sources stemming from calibration errors. The lack of artefacts in the visibilities indicates that RFI is not a significant contributor to this measurement, and we do not see evidence of sidelobe pickup in the images, as the sidelobe positions are frequency-dependent and would thus present as shifting patterns in each sub-band. With currently available LOFAR analysis techniques, we cannot absolutely rule out a contribution from the residual power from subtracted sources stemming from calibration errors. In particular, making power spectra at larger scales presents a particular calibration challenge in this regard, as also found by epoch-of-reionization measurements (Barry et al. 2016; Patil et al. 2016; Sadarabadi & Koopmans 2018). Future development of LOFAR analysis techniques may allow a more precise determination of this, but these are beyond the scope of this work.

We can estimate the contribution due to structure in Galactic diffuse emission by noting that the measured angular power in the secondary field is systematically a factor of ~ 1.4 higher in the $(\Delta T)^2$ normalization than that in the coldest patch field, as seen in Fig. 4, and thus a factor of ~ 1.2 higher in the (ΔT) normalization. This is, quite tellingly, the same as the square of ratio of the average absolute brightness in radiometric temperature (K) units for the two regions that we calculate using the Haslam et al. (1982) map averaging over pixels within 4° from the field centres (1.2 ± 0.1). As the differences in absolute brightness are due solely to differences in lines of sight through the Galactic diffuse components (as visualized in Fig. 2), this is a strong indication that the proportion of angular power in (ΔT) units due to Galactic structure tracks the proportion of absolute brightness due to that structure, for lines of sight in this general direction of minimal Galactic structure and likely for general lines of sight far away from the Galactic plane. A number of considerations point to the extragalactic component being overwhelmingly dominant (by at least a factor of 5) in terms of the absolute temperature of the background (e.g. Singal et al. 2015) so we believe that the extragalactic component dominates the measured angular power in the coldest patch field by approximately this factor. Stated another way, the *normalized* angular power ($\frac{\Delta T}{T}$) for both fields is the same, indicating that the contribution to the angular power from Galactic structure is sub-dominant when considering these fields since it is the component that varies spatially between the two fields.

If the angular power measured here is due to low-flux radio point sources, they must be very numerous, paralleling the situation when considering the surface brightness of the radio background. As discussed in Section 4, we simulated the angular power resulting from a source count distribution representing a very large number of sources below $1 \mu\text{Jy}$, which, as shown in Condon et al. (2012),

could potentially provide the level of surface brightness of the RSB. We found that this source distribution when distributed randomly spatially contains low angular power due to the large number of sources per pixel, but could possibly reproduce the angular power of the RSB measured here given the proper detailed clustering on a wide range of angular scales. It is our intention to continue this modelling in a future work in order to determine the precise clustering parameters for very large numbers of low-flux sources, which could, possibly, result in the angular power spectrum observed here, and to explore the implications of such a population.

ACKNOWLEDGEMENTS

We thank the ‘BAM – Anisotropic Universe 2018’ workshop where initial discussions took place. We acknowledge LOFAR award LC12-005. SHE is supported by NSF Grant No. PHY-1914409. SHo is supported by the U.S. DOE Office of Science under the award number DE-SC0020262 and NSF Grants No. AST-1908960 and No. PHY-1914409. This work was supported by World Premier International Research Center Initiative (WPI), MEXT, Japan. This paper is based on data obtained with the International LOFAR Telescope (ILT) under project code LC12-005. LOFAR (van Haarlem et al. 2013) is the Low-Frequency Array designed and constructed by ASTRON. It has observing, data processing, and data storage facilities in several countries, which are owned by various parties (each with their own funding sources) and which are collectively operated by the ILT foundation under a joint scientific policy. The ILT resources have benefitted from the following recent major funding sources: CNRS-INSU, Observatoire de Paris and Université d’Orléans, France; BMBF, MIWF-NRW, MPG, Germany; Science Foundation Ireland (SFI), Department of Business, Enterprise and Innovation (DBEI), Ireland; NWO, the Netherlands; and the Science and Technology Facilities Council, UK.

DATA AVAILABILITY

The data underlying this paper will be shared on reasonable request to the corresponding author.

REFERENCES

- Ade P. et al., 2011, *A&A*, 536, A18
 Ali-Haïmoud Y., Meerburg P., Yuan S., 2014, *Phys. Rev. D*, 89, 083506
 Barry N., Hazelton B., Sullivan I., Morales M., Pober J., 2016, *MNRAS*, 46, 3135
 Bennett C. et al., 2013, *ApJS*, 208, 20
 Bridle A., 1967, *MNRAS*, 136, 219
 Broderick A., Pfrommer C., Puchwein E., Chang P., Smith K., 2014, *ApJ*, 796, 12
 Choudhuri S., Ghosh A., Roy N., Bharadwaj S., Intema H., Ali S., 2020, *MNRAS*, 494, 1936
 Condon J. et al., 2012, *ApJ*, 758, 23
 de Gasperin F. et al., 2019, *A&A*, 622, A5
 Dowell J., Taylor R., 2018, *ApJ*, 858, 9
 Dutta P., Nandakumar M., 2019, *Res. Astron. Astrophys.*, 19, 060
 Fang K., Linden T., 2016, *J. Cosmol. Astropart. Phys.*, 10, 004
 Fixsen D. et al., 2011, *ApJ*, 734, 5
 Fomalont E., Kellermann K. I., Anderson M. C., Weistrop D., Wall J. V., Windhorst R. A., Kristian J. A., 1988, *AJ*, 96, 1187
 Fornengo N., Lineros R., Regis M., Taoso M., 2011, *Phys. Rev. Lett.*, 107, 271302
 Franzen T. et al., 2016, *MNRAS*, 459, 3314
 George E. et al., 2015, *ApJ*, 799, 177

- Hancock P., Trott C., Hurley-Walker N., 2018, *Publ. Astron. Soc. Aust.*, 35, e011
- Hardcastle M. et al., 2021, *A&A*, 648, 10
- Haslam C., Salter C., Stoffel H., Wilson W., 1982, *ApJS*, 47, 1
- Holder G., 2014, *ApJ*, 758, 23
- Hooper D., Belikov A., Jeltema T., Linden T., Porfumo S., Slatyer T., 2012, *Phys. Rev. D*, 863, 003
- Jackson J., US 1998, *Classical Electrodynamics*. Wiley
- Kogut A. et al., 2011, *ApJ*, 734, 4
- La Porta L., Burigana C., Reich W., Reich P., 2018, *A&A*, 479, 641
- Lesgourgues J., 2013, in *Proc. WSPC, TASI Lectures on Cosmological Perturbations Boulder, Colorado*, p. 19
- Mertens F. et al., 2020, *MNRAS*, 493, 1662
- Offringa A., Smirnov O., 2017, *MNRAS*, 471, 301
- Offringa A., van de Gronde J., Roerdink J., 2012, *A&A*, 539, A95
- Offringa A. et al., 2014, *MNRAS*, 444, 606
- Offringa A., Mertens F., Koopmans L., 2019, *MNRAS*, 484, 2866
- Offringa A., Mertens F., van der Tol S., Veenboer B., Gehlot B., Koopmans L., Mevius M., 2019, *A&A*, 631, A12
- Partridge R. B., Richards E. A., Fomalont E. B., Kellerman K. I., Windhorst R. A., 1997, *ApJ*, 483, 38
- Patil A. et al., 2016, *MNRAS*, 463, 4317
- Ryden B., 2006, *Introduction to Cosmology*. Cambridge Univ. Press, Cambridge
- Sadarabadi A., Koopmans L., 2018, *MNRAS*, 483, 5480
- Singal J., Stawarz Ł., Lawrence A., Petrosian V., 2010, *MNRAS*, 409, 1172
- Singal J. et al., 2011, *ApJ*, 730, 138
- Singal J., Kogut A., Jones E., Dunlap H., 2015, *ApJ*, 799, L10
- Singal J. et al., 2018, *Publ. Astron. Soc. Pac.*, 130, 036001
- Subrahmanyan R., Cowsik R., 2013, *ApJ*, 776, 42
- Subrahmanyan R., Kesteven M., Ekers R., Sinclair M., Silk J., 2000, *MNRAS*, 315, 808
- van Diepen G., Dijkema T., Offringa A., 2018, *Astrophysics Source Code Library*, record ascl:1804.003
- van Haarlem M. R. et al., 2013, *A&A*, 556, A2
- van Tol S., Veenboer B., Offringa A., 2018, *A&A*, 616, A27
- van Weeren R. et al., 2016, *ApJS*, 223, 2
- Vernstrom T. et al., 2014, *MNRAS*, 440, 2791
- Waldram E., Yates J., Riley J., Warner P., 1996, *MNRAS*, 282, 779
- Williams W. et al., 2016, *MNRAS*, 460, 2385

APPENDIX A: RELATIONS BETWEEN MEASURES OF ANGULAR POWER OF TEMPERATURE ANISOTROPIES

In this appendix, we present the scaling relationships between two normalizations for the angular power of temperature anisotropies, and derive which arises naturally from power spectra obtained from interferometric observations.

A1 Power spectrum normalizations and multipole moments

Note on notation and dimensions: Square brackets [] will indicate ‘dimensions of’. Here, in order to keep track of factors of the angular scale ℓ and normalization factors of π in quantities, we will follow factors of ℓ and π by a quasi-dimensionality. That is, to encompass both dimensions with physical units and these normalization factors, we will refer in this work to ‘quasi-dimensionality’ to encapsulate both. Definitions of relevant quantities have been obtained from Ryden (2006), Lesgourgues (2013), and Jackson (1998).

The temperature fluctuation, or deviation from the average temperature, at a point on the sky in the direction \hat{n} or, equivalently, at angular coordinates (θ, ϕ) , denoted by δT , can be expressed with the

spherical harmonic functions and their coefficients:

$$\delta T(\theta, \phi) \equiv T(\theta, \phi) - \langle T \rangle = \sum_{\ell, m} a_{\ell, m} Y_{\ell, m}(\theta, \phi). \quad (\text{A1})$$

The ‘angular correlation function’ $C(\theta)$ is an average of the product of $\delta T(\hat{n})$ values in directions separated by the angle θ :

$$C(\theta) = \langle \delta T(\hat{n}) \delta T(\hat{n}') \rangle_{\hat{n} \cdot \hat{n}' = \cos(\theta)}. \quad (\text{A2})$$

Therefore, quasi-dimensionally,

$$[C(\theta)] = [\delta T]^2. \quad (\text{A3})$$

$C(\theta)$ can be expressed as a sum of Legendre polynomials and ‘multipole moment’ coefficients C_ℓ :

$$C(\theta) = \frac{1}{4\pi} \sum_{\ell} (2\ell + 1) C_\ell P_\ell(\cos \theta). \quad (\text{A4})$$

To assess the quasi-dimensionality of the Legendre polynomials, we can use the spherical harmonic addition theorem

$$P_\ell(\cos \theta) = \frac{4\pi}{2\ell + 1} \sum_m Y_{\ell, m}(\theta, \phi) Y_{\ell, m}^*(\theta', \phi'). \quad (\text{A5})$$

Now we must note that any sum over m for a given ℓ runs from $-\ell$ to $+\ell$ and so has $2\ell + 1$ terms and therefore such sums have a quasi-dimensionality of $[2\ell + 1]$. Therefore, quasi-dimensionally,

$$[P_\ell(\cos \theta)] = [4\pi] [Y_{\ell, m}(\theta, \phi)]^2. \quad (\text{A6})$$

To evaluate the quasi-dimensionality of the spherical harmonics $Y_{\ell, m}(\theta, \phi)$, we can note simply that $Y_{0,0} = \frac{1}{\sqrt{4\pi}}$ so that $[Y_{\ell, m}(\theta, \phi)] = [\frac{1}{\sqrt{4\pi}}]^{1/2}$, so $[P_\ell(\cos \theta)] = [1]$; the Legendre polynomials are quasi-dimensionless. Returning to equation (A4), we have

$$[C_\ell] = \left[\frac{4\pi}{2\ell + 1} \right] [C(\theta)] = \left[\frac{4\pi}{2\ell + 1} \right] [\delta T]^2. \quad (\text{A7})$$

The multipole moments C_ℓ are the variance (mean of the squares) of the spherical harmonic coefficients:

$$C_\ell = \langle |a_{\ell, m}|^2 \rangle = \frac{1}{2\ell + 1} \sum_m |a_{\ell, m}|^2, \quad (\text{A8})$$

where again the sum over m for a given ℓ has a quasi-dimensionality of $[2\ell + 1]$. Thus,

$$[C_\ell] = [a_{\ell, m}]^2, \quad (\text{A9})$$

and, utilizing equation (A7), we have

$$[a_{\ell, m}] = [C_\ell]^{1/2} = \left[\frac{4\pi}{2\ell + 1} \right]^{1/2} [\delta T]. \quad (\text{A10})$$

We note that this does not imply that $[\delta T]$ as expressed in equation (A1) is ‘quasi-dimensionless’ with respect to factors of ℓ – i.e. it does not imply that $[\delta T]$ has no natural scaling with ℓ – rather we are just tallying the conversion factors between the quasi-dimensionality of various quantities.

Equation (A10) tells us that in order to express the temperature fluctuation power at a given angular scale ℓ in terms of the multipole moment, we would need

$$(\delta T)_\ell = \sqrt{\frac{2\ell + 1}{4\pi}} \sqrt{C_\ell}. \quad (\text{A11})$$

However, a standard normalization scheme used in the CMB literature (e.g. Ade et al. 2011) is to express the temperature fluctuation angular power multiplied by different factors of the angular scale ℓ , resulting in a measure of the fluctuation power, here denoted by

$(\Delta T)_\ell$, which would be constant across values of ℓ in the case of an invariant spectrum of Gaussian random fluctuations:

$$(\Delta T)_\ell \equiv \sqrt{\frac{\ell(\ell+1)}{2\pi}} \sqrt{C_\ell}. \quad (\text{A12})$$

With equations (A11) and (A12), we see that the relation between the two normalizations of the temperature fluctuation power is

$$(\Delta T)_\ell = \sqrt{\frac{2\ell(\ell+1)}{2\ell+1}} (\delta T)_\ell. \quad (\text{A13})$$

We note that the quantities $(\delta T)_\ell$ and $(\Delta T)_\ell$ can be scaled to be normalized by the average temperature so that they express a fractional deviation from it, and are then denoted by $(\frac{\delta T}{T})_\ell$ and $(\frac{\Delta T}{T})_\ell$, respectively. We will now show that the power spectra produced from interferometric observations most naturally have a normalization of $(\Delta T)_\ell^2$.

A2 Power spectra from interferometric observations

To determine that the power spectra determined from interferometric observations are in the $(\Delta T)_\ell^2$ normalization, we first consider that the power spectrum relates to \tilde{T} , the Fourier transform of the temperature field, as

$$P(\mathbf{k}) \equiv A |\tilde{T}(\mathbf{k})|^2, \quad (\text{A14})$$

where A is the physical area of the field (in Mpc^2). In this equation, the Fourier transform is defined with a ‘ $1/N$ ’ normalization:

$$\tilde{T}(2\pi\mathbf{k}) \equiv \frac{1}{N_x N_y} \sum_{\mathbf{x}} T(\mathbf{x}) e^{-i2\pi\mathbf{k}\cdot\mathbf{x}}. \quad (\text{A15})$$

When a ‘number of image pixels’, $N_x N_y$, is used, this is defined as the *effective* number of pixels. The definition for $N_x N_y$ is

$$N_x N_y = \frac{\Omega_A}{\Omega_{\text{PSF}}}, \quad (\text{A16})$$

where Ω_A is the primary beam solid angle and Ω_{PSF} is the synthesized beam solid angle. For completeness, flux density per beam (Jy/PSF) is converted into temperature (kelvin) as

$$T(\mathbf{x}) \equiv S_{\text{Jy/PSF}}(\mathbf{x}) \frac{10^{-26} c^2}{2k_B \nu^2 \Omega_{\text{PSF}}}, \quad (\text{A17})$$

where S is in Jy/PSF and T in kelvin. If equations (A16) and (A17) are substituted into equation (A15), then Ω_{PSF} cancels out:

$$\tilde{T}(2\pi\mathbf{k}) = \frac{10^{-26} c^2}{2k_B \nu^2 \Omega_A} \sum_{\mathbf{x}} S(\mathbf{x}) e^{-i2\pi\mathbf{k}\cdot\mathbf{x}}. \quad (\text{A18})$$

Therefore, bringing everything together and assuming as input a correctly normalized image in units of temperature $T(\mathbf{x})$, we have

$$P(2\pi\mathbf{k}) = A \left| \frac{1}{N_x N_y} \sum_{\mathbf{x}} T(\mathbf{x}) e^{-i2\pi\mathbf{k}\cdot\mathbf{x}} \right|^2. \quad (\text{A19})$$

The power spectrum is often expressed in so-called dimensionless units (e.g. Ali-Haimoud, Meerburg & Yuan 2014), which, perhaps

confusingly, ends up with physical units of squared temperature (e.g. K^2). The dimensionless power spectrum relates to the two-dimensional power spectrum as follows:

$$\Delta^2(k) = P(k) \frac{k^2}{2\pi}. \quad (\text{A20})$$

Substituting equation (A19) into equation (A20), we have

$$\Delta^2(2\pi\mathbf{k}) = 2\pi k^2 A \left| \frac{1}{N_x N_y} \sum_{\mathbf{x}} T(\mathbf{x}) e^{-i2\pi\mathbf{k}\cdot\mathbf{x}} \right|^2. \quad (\text{A21})$$

The units for the transverse distance are arbitrary in this equation, as they cancel out through $k^2 A$. If we chose p to be the dimensionless counterpart of k such that $A = 1$, then

$$\Delta^2(2\pi\mathbf{p}) = 2\pi |\mathbf{p}|^2 \left| \frac{1}{N_x N_y} \sum_{\mathbf{x}} T(\mathbf{x}) e^{-i2\pi\mathbf{p}\cdot\mathbf{x}} \right|^2. \quad (\text{A22})$$

In a small-angle approximation, the Fourier transform of T can be related to spherical harmonic coefficients using $\tilde{T}(\mathbf{p}) = a(\ell_p, m_p)$:

$$\begin{aligned} \Delta^2(2\pi\mathbf{p}) &= 2\pi |\mathbf{p}|^2 |a(\ell_p, m_p)|^2, \\ \Delta^2(\mathbf{p}) &= \frac{|\mathbf{p}|^2}{2\pi} |a(\ell_p, m_p)|^2, \\ \Delta(\mathbf{p}) &= |\mathbf{p}| \sqrt{\frac{1}{2\pi} |a(\ell_p, m_p)|^2}, \end{aligned} \quad (\text{A23})$$

and thus the power in the spherical harmonic degree corresponding to the normalized wave vector \mathbf{p} can be expressed as

$$\Delta(\ell, m) = \hat{\ell} \sqrt{\frac{1}{2\pi} |a(\ell, m)|^2}, \quad (\text{A24})$$

where $\hat{\ell} = \ell$ in the small-angle approximation. For any appreciable ℓ , $\sqrt{\ell^2} \approx \sqrt{\ell(\ell+1)}$, and so

$$\Delta(\ell, m) \rightarrow \sqrt{\frac{\ell(\ell+1)}{2\pi} |a(\ell, m)|^2}. \quad (\text{A25})$$

From equations (A11) and (A12), we have

$$(\Delta T)_\ell = \sqrt{\frac{\ell(\ell+1)}{2\pi}} [a_{\ell,m}], \quad (\text{A26})$$

and so we see that

$$[\Delta(\ell, m)] = [(\Delta T)_\ell]. \quad (\text{A27})$$

So the power spectra produced in this analysis, and also in analyses typical in 21-cm cosmology, when computed directly with equation (A22), are naturally in the $(\Delta T)_\ell^2$ normalization. Applying equation (A10) to equation (A26), we see that the physical units of Δ^2 will indeed be squared temperature (e.g. K^2).

This paper has been typeset from a $\text{\TeX}/\text{\LaTeX}$ file prepared by the author.