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Introduction to the Special Section on "Numerical and Mathematical Processing"

Daniel Ansari Western University, daniel.ansari@uwo.ca

Bert De Smedt *KU Leuven*

Roland H. Grabner *ETH Zürich*

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Introduction to the Special Section on "Numerical and Mathematical Processing"

Daniel Ansari¹, Bert De Smedt², and Roland H. Grabner³

15 The processing of numerical information is a dominant feature 16 of everyday life. Whether it is in the context of financial 17 transactions, shopping for groceries, or gauging how many 18 people are in a room, we are constantly using numerical 19 information to guide our behavior and make decisions. On the 20 other hand, number and mathematics constitute a crucial part 21 of the curriculum during schooling. There is clear evidence that 22 basic numerical and mathematical skills play a critical role in 23 determining an individual's life success (Reyna, Nelson, Han, 24 & Dieckmann, 2009). Furthermore, there is abundant evidence 25 that low numeracy skills are associated with substantial costs 26 to society at large (Butterworth, Varma, & Laurillard, 2011; 27 Bynner & Parsons, 1997; Duncan et al., 2007).

28 Until recently research on the cognitive and neural 29 foundations of numerical and mathematical skills was a 30 relatively underinvestigated area of research, in particular 31 when compared with the large body of research into the 32 neurocognitive processes underlying the typical and atypical 33 development of literacy and language competencies. However, 34 this state of affairs has changed rapidly in the past 20 years, 35 with much progress being made in understanding the 36 evolutionary origins, ontogenetic foundations, and trajectories 37 as well as neuronal correlates of number processing (for 38 reviews see Ansari, 2008; Nieder & Dehaene, 2009; Piazza & 39 Izard, 2009). The initial years of research into numerical and 40 mathematical processing were characterized by basic research 41 to answer question such as: What numerical competencies do 42 nonhuman animals possess? When do numerical competencies 43 emerge over developmental time? How are numerical symbols 44 learnt? What brain regions are associated with arithmetic 45 problem solving and how do brain activation patterns change 46 over the course of learning and development? Many important 47

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answers to these questions have been provided through basic research that covers multiple levels of description ranging from single cell recordings to cross-cultural research with communities in remote locations. 1

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In recent years, there have been increasing efforts to bridge between, on one hand, basic research on numerical and mathematical processing and, on the other hand, questions that arise from educational context such as: What are the predictors of individual differences in school-relevant measures of arithmetic achievement? What can we learn from empirical research on math skill development about the best way to diagnose and remediate children with mathematical difficulties, such as developmental dyscalculia?

a liftculties, such as developmental dyscalcula?28The present special section in Mind, Brain, and Education29builds on this momentum and includes four empirical research30contributions that illustrate the potential of linking basic31cognitive and neuroscience research with applied questions32that are relevant to mathematics education.33

33 In the domain of reading significant progress toward 34 bridging between the research laboratory and the classroom 35 was made when key foundational factors (such as phonological 36 awareness) that predict typical and atypical reading 37 development were identified, particularly, as this resulted 38 in increased early diagnosis of children at risk of developing 39 reading difficulties, where early interventions are appropriate 40 (for a review see Gabrieli, 2009). In the domain of number 41 processing, such low-level processing factors contributing to 42 the development of higher level mathematical competencies 43 that children are acquiring in the math classroom have 44 recently been the focus of much research. For example, it 45 has been shown that children's ability to indicate which 46 of two Arabic digits or dot arrays is numerically larger 47 correlates with and even predicts their scores on standardized 48 tests of mathematical achievement (De Smedt, Verschaffel, & 49 Ghesquiere, 2009; Halberda, Mazzocco, & Feigenson, 2008; 50 Holloway & Ansari, 2009). Two of the contributions in this 51 special section take this rapidly growing body of research 52 forward in significant ways. Namely, in their article, Sasanguie, 53

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 ¹Numerical Cognition Laboratory, Department of Psychology, University
 of Western Ontario

^{51 &}lt;sup>2</sup>Faculty of Psychology and Educational Sciences, University of Leuven

³Institute for Behavioral Sciences, Swiss Federal Institute of Technology ⁵² (ETH) Zurich Switzerland Research

Van den Bussche, and Reynvoet present a longitudinal study
 to investigate which measures of basic number processing
 are the strongest predictors of later math achievement. Their
 findings show that nonsymbolic number estimation is the
 strongest predictor of math skills 1 year later, with the speed
 of comparing which of two numbers is numerically larger
 also accounting for some of the variance children's subsequent

8 math performance.

9 Vanbinst, Ghesquière, and De Smedt further constrain 10 these findings by investigating how measures of basic 11 number processing are related to one specific school-taught 12 mathematical skill, that is, elementary arithmetic and the 13 strategies used to perform these calculations. Their data reveal 14 that particularly children's symbolic magnitude processing, as 15 measured by tasks that involve the comparison of Arabic 16 digits, is related to their mathematical and arithmetical 17 skills: Children with better access to numerical magnitude 18 representations from symbolic digits retrieve more facts from 19 their memory and are faster in executing various arithmetic 20 strategies. They suggest that educators should particularly 21 focus on connecting Arabic symbols to the quantities they 22 represent. Furthermore, these data provide the first evidence to suggest that arithmetic fact retrieval frequency is related to 23

- 24 basic, symbolic number processing.
- 25 The third contribution of this special section by 26 Gabriel, Coché, Szucs, Carette, Rey, and Content moves 27 on to educational intervention by investigating whether an 28 intervention that focuses on the association between fractions 29 and the magnitudes they represent improves children's 30 understanding of fractions, a major stumbling block for many 31 children in primary school. Their findings reveal that playing 32 games, such as comparing and adding fractions and matching 33 fractions to quantities, all of which foster the connection 34 between fractions and their magnitudes, improved children's 35 ability to estimate and compare fractions-again highlighting 36 the fundamental role played by magnitude processing in the 37 development of mathematical skills.
- 38 The final contribution of this special section bridges 39 to the brain level using functional magnetic resonance 40 imaging to examine basic neurocognitive processes related 41 to mathematics learning in bilinguals. Specifically, Grabner, 42 Saalbach, and Eckstein address the unresolved question of the 43 sources of language-switching costs (i.e., poorer performance) 44 in bilingual mathematics learning that arise when arithmetic 45 problems are solved in a language different from the language of 46 instruction. Two general cognitive mechanisms are discussed 47 in the literature to account for these costs (Dehaene, Spelke, 48 Pinel, Stanescu, & Tsivkin, 1999): they either reflect the 49 need to translate arithmetic knowledge from the language 50
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of instruction into the language of application or they 1 2 derive from additional mathematical information processing 3 (e.g., calculation). The findings by Grabner, Saalbach, and 4 Eckstein provide neurophysiological evidence in favor of the 5 second mechanism and exemplify how neuroscience data 6 can be used to achieve incremental insights into cognitive mechanisms of mathematics learning, whose understanding is 7 8 of high educational relevance.

Taken together, the four contributions contained within9this special section of Mind, Brain, and Education provide a diverse10set of empirical research findings that, in the true spirit of the11rapidly growing field of Mind, Brain, and Education, attempt12to build bridges between basic research on the behavioral and13neuronal mechanisms of numerical as well as mathematical14processing and, on the other hand, educational questions.1516

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