



Near-Chandrasekhar-mass Type Ia Supernovae from the Double-degenerate Channel

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Abstract

Recent observational evidence has demonstrated that white dwarf (WD) mergers are a highly efficient mechanism for mass accretion onto WDs in the galaxy. In this paper, we show that WD mergers naturally produce highly magnetized, uniformly rotating WDs, including a substantial population within a narrow mass range close to the Chandrasekhar mass (M_{Ch}). These near- M_{Ch} WD mergers subsequently undergo rapid spin up and compression on a $\sim 10^2$ yr timescale, either leading to central ignition and a normal SN Ia via the DDT mechanism, or alternatively to a failed detonation and SN Iax through pure deflagration. The resulting SNe Ia and SNe Iax will have spectra, light curves, polarimetry, and nucleosynthetic yields similar to those predicted to arise through the canonical near- M_{Ch} single degenerate (SD) channel, but with a t^{-1} delay time distribution characteristic of the double-degenerate channel. Furthermore, in contrast to the SD channel, WD merger near- M_{Ch} SNe Ia and SNe Iax will not produce observable companion signatures. We discuss a range of implications of these findings, from SNe Ia explosion mechanisms, to galactic nucleosynthesis of iron peak elements including manganese.

Unified Astronomy Thesaurus concepts: Type Ia supernovae (1728); White dwarf stars (1799); Chandrasekhar limit (221); Magnetohydrodynamics (1964); Stellar mergers (2157)

1. Introduction

Type Ia supernovae (SNe Ia) are the radioactively powered thermonuclear explosions of white dwarfs (WDs), and play a crucial role as standardizable candles for cosmology (Pankney 1962; Phillips 1993). The stellar progenitors of SNe Ia have remained a subject of intense investigation for decades. For many years, the single-degenerate (SD) channel, in which a main sequence or red giant star donates material to a CO white dwarf until it reaches a near-Chandrasekhar mass M_{Ch} and subsequently detonates as a SN Ia (Whelan & Iben 1973), was considered canonical. More recent evidence has begun to favor the double-degenerate (DD) SNe Ia channel, resulting from the merger of two white dwarfs (Webbink 1984). However, numerous questions still surround both channels, leaving the nature of the SNe Ia progenitors a largely unsolved problem (Maoz et al. 2014).

A key outstanding puzzle surrounding SNe Ia stems from the nucleosynthesis of iron group elements (IGEs). The fundamental physics of electron degeneracy requires that the central density of WDs increases with increasing WD mass (Chandrasekhar 1935). Consequently, near- M_{Ch} WD progenitors undergo more efficient electron capture in their cores than sub- M_{Ch} progenitors. This efficient electron capture in near- M_{Ch} WD progenitors in turn results in enhanced abundances of neutron-rich isotopes, most notably the radioisotope ^{55}Fe , which decays to the monoisotopic ^{55}Mn (Röpke et al. 2012). Seitenzahl et al. (2013a) compellingly argue that a

substantial fraction of near- M_{Ch} WD events, as much as half of the total SNe Ia rate, is required to produce a solar abundance of ^{55}Mn . Detailed galactic nucleosynthesis models find the fraction of near- M_{Ch} SNe Ia to be as high as 75% in the solar neighborhood, though lower in dwarf galaxies (Kobayashi et al. 2020).

Another puzzle surrounding near- M_{Ch} events is connected to subluminal SNe Iax. SNe Iax are relatively commonplace transients, accounting for 10%–30% of the total SNe Ia rate (Foley et al. 2013). The leading theoretical models for SNe Iax are failed detonations of near- M_{Ch} WDs (Jordan et al. 2012; Fink et al. 2014). Yet, the rates for the production of near- M_{Ch} WDs predicted from binary population synthesis (BPS) models through the canonical SD channel is typically an order of magnitude less than the total SNe Ia rate, and depending on model assumptions, orders of magnitude less (Maoz et al. 2014). Thus, there is also a tension between the requisite SNe Iax rate and that predicted from BPS models, if SNe Iax originate as failed detonations of near- M_{Ch} WDs through the classical SD channel.

Furthermore, numerous observations place tight constraints on the prevalence of near- M_{Ch} SNe Ia events produced through the canonical single-degenerate channel. Observations of the nebular phase spectra of a large sample of 111 SNe Ia including normal, 91T-like, and 91bg-like (but excluding Ia-CSM and Iax) events found no evidence of $\text{H}\alpha$ from the stripped companions expected from the SD channel (Tucker et al. 2020), contrary to theoretical expectations (Botyánszki et al. 2018). Similarly tight limits on single-degenerate SNe Ia are obtained from companion (Li et al. 2011; Shappee et al. 2018), and ex-companion (González Hernández et al. 2012; Schaefer & Pagnotta 2012) searches, the delay-time distribution (DTD) (Strolger et al. 2020), as well as radio (Chomiuk et al. 2016) and X-ray (Margutti et al. 2012, 2014) constraints.

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In this paper, we present a possible solution to the challenges posed by near- M_{Ch} SNe Ia and SNe Iax. We propose that near- M_{Ch} SNe Ia and SNe Iax are produced primarily not through the SD channel, as is widely believed, but instead through the DD channel. Our line of reasoning builds upon recent observational advances, showing that the galactic WD merger rate exceeds the SN Ia rate (Maoz et al. 2018; Cheng et al. 2020), and that at least half of the most massive WDs in the solar neighborhood are merger products (Kilic et al. 2021).

The production of super- M_{Ch} WD mergers through the DD channel exceeds the predicted SD channel rate, provided that only a small fraction of super- M_{Ch} mergers promptly detonate upon merger, as both recent hydrodynamical simulations (Raskin et al. 2012, 2014; Kashyap et al. 2017) and observations (Shen et al. 2018) suggest. Additional theoretical and observational investigations have demonstrated that the product of the merger is a high-field magnetic white dwarf (HFMWD) (Ji et al. 2013; Gvaramadze et al. 2019; Caiazzo et al. 2021). We will show that a substantial population of mergers result in rigidly rotating WDs in a narrow mass range close to M_{Ch} that lose angular momentum through both a propeller-driven phase as well as magnetic dipole radiation. These mergers have been previously shown to undergo central ignition (Becerra et al. 2018, 2019). We will consider both the possibility that these central ignitions lead to SNe Ia as well as failed detonation SNe Iax, and explore an SN Ia model in detail.

The structure of this paper is as follows. In Section 2, we demonstrate how WD mergers are naturally expected to give rise to near- M_{Ch} SNe Ia and SNe Iax progenitors. In Section 3, we describe the methodology used to numerically simulate a near- M_{Ch} DD SNe Ia event, including the calculation of its detailed nucleosynthetic abundances and synthetic spectra. In Section 4, we present the simulation results. In Section 5, we discuss the observational and theoretical implications of WD merger near- M_{Ch} SNe Ia and SNe Iax. Finally, in Section 6, we conclude.

2. Near-Chandrasekhar-mass SNe Ia from DD WD Mergers

2.1. Post-merger HFMWD Production

Decades of theoretical work have elucidated the physical processes at work during WD mergers. WDs in tight binaries formed through previous common envelope phases of evolution (Nelemans & Tout 2005; Di Stefano 2010) are driven together in a final inspiral by gravitational wave radiation (see Figure 1a). As the secondary WD approaches the primary, it is tidally disrupted, producing a hot, flared accretion disk surrounding the primary WD (Benz et al. 1990; Lorén-Aguilar et al. 2009; see Figure 1b). The differential rotation within the disk is unstable to the magnetorotational instability (Balbus & Hawley 1991), such that even a dynamically weak seed field is rapidly amplified over several disk rotational periods (Ji et al. 2013). Consequently, magnetohydrodynamics plays a crucial role both in regulating the accretion and outflow rates, as well as in determining the final thermodynamic structure and spin of the WD merger.

2.2. Accretion onto Magnetically Braked HFMWD

During the merger itself, material accreted from the tidally disrupted accretion disk will initially possess a higher specific

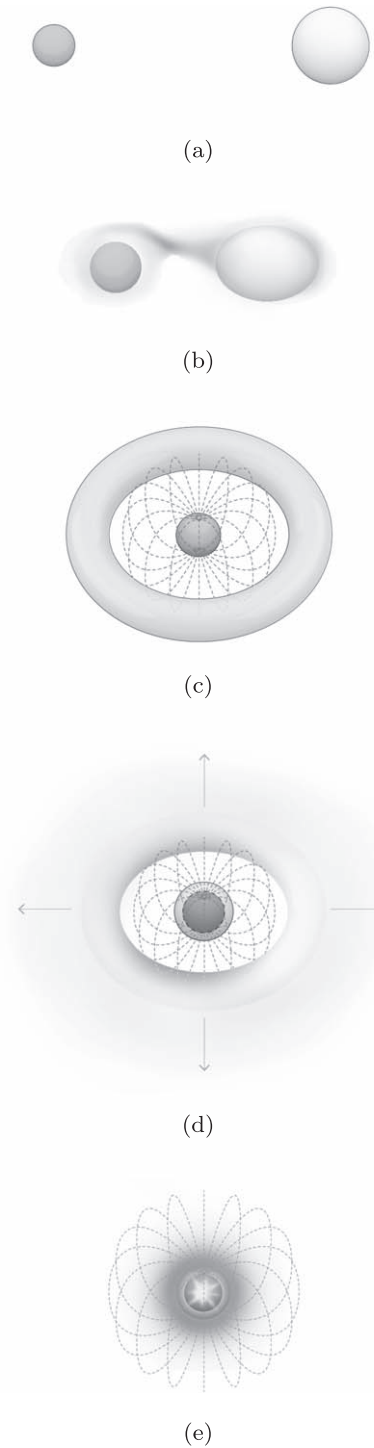


Figure 1. Schematic diagram showing the processes involved in the formation of near- M_{Ch} SNe Ia from a DD WD merger. (a) The inspiral phase of the WD merger lasts $\sim 1\text{--}10$ Gyr. (b) The inspiral phase is followed by the tidal disruption of the secondary on a timescale of $\sim 10^3$ s. (c) The differentially rotating disk gives rise to the magnetorotational instability (MRI), the accretion of which onto the primary produces a rigidly rotating HFMWD. (d) As the primary accretes from the disk, it gains angular momentum and spins up. On a timescale of $\sim 10^6$ s, the system enters the propeller phase. During the propeller phase, the primary ejects the remaining disk from the system and spins down. (e) The misaligned magnetic and rotational axes of the merger cause it to spin up on a timescale of $\sim 10^2$ yr and compress the core, resulting in central ignition, and either an SN Ia or an SN Iax. Image credit: Pedram Karimi.

angular momentum than the primary WD. As a result, the accretion initially generates a differential shear within the WD merger. However, the differential shear within the nascent HFMD results in the propagation of torsional Alfvén waves, which magnetically brake the differential rotation of the HFMD merger rapidly on a timescale of minutes (Shapiro 2000; Piro 2008),

$$t_A = \frac{R}{v_A} \approx 7 \times 10^2 \left(\frac{B_0}{10^{10} \text{ G}} \right)^{-1} \times \left(\frac{R_{\text{WD}}}{2 \times 10^3 \text{ km}} \right)^{-1/2} \left(\frac{M}{1.4 M_\odot} \right)^{1/2} \text{ s.} \quad (1)$$

Here, M and R_{WD} are the radius and mass of the HFMD merger, and B_0 is the surface magnetic field strength. v_A is the Alfvén velocity $B/\sqrt{4\pi\rho}$. The Alfvénic timescale t_A is shorter than the timescale to accrete the tidally disrupted disk,

$$t_{\text{acc}} = \alpha^{-1} t_{\text{dyn}} \approx 3 \times 10^3 \left(\frac{0.01}{\alpha} \right) \times \left(\frac{R_{\text{disk}}}{5 \times 10^4 \text{ km}} \right)^{3/2} \left(\frac{M}{1.4 M_\odot} \right)^{-1/2} \text{ s,} \quad (2)$$

where t_{dyn} is the dynamical timescale corresponding to the outer disk radius R_{disk} . Consequently, the HFMD is rapidly braked, and is in a state of uniform rotation even as it continues to accrete mass from the disk (see Figure 1c). This conclusion is confirmed by multidimensional MHD simulations of post-merger accretion (Ji et al. 2013), where the resulting HFMD is found to be uniformly rotating.

Magnetohydrodynamics is also responsible for converting differential shear into magnetic energy through the magnetorotational (MRI) instability, and in driving jets and outflows. As such, magnetohydrodynamics plays a leading role in establishing the thermodynamic profile of the disk, and consequently key observable properties of the merger, including its final radius and surface temperature. The energy budget of the disk is particularly important because the disk is nondegenerate, and net heating injected into it can result in expanded merger sizes. In particular, if the deposition of differential shear is converted into heat over a viscous timescale through the Shakura-Sunyaev α prescription, the merger expands to $\sim 10^{10}$ – 10^{11} cm (Schwab et al. 2012; Shen et al. 2012). In contrast, magnetohydrodynamics converts shear energy into magnetic energy, and propels a significant amount of energy into jets and winds, producing WD-sized mergers with $\sim 10^5$ cm envelopes (Ji et al. 2013; Becerra et al. 2018).

2.3. Propeller Regime

If the central WD is rotating sufficiently rapidly, then accretion from the disk onto the WD cannot overcome its centrifugal barrier, and the system enters into the propeller regime. Theory and simulations demonstrate that accretion efficiency in the propeller regime is greatly reduced. Instead, in the propeller regime, disk material is efficiently ejected into unbound trajectories through magnetically driven disk winds powered by the rotation of the central star and torquing it down (Illarionov & Sunyaev 1975; Ghosh & Lamb 1979; Lovelace et al. 1999; Romanova et al. 2005).

We now demonstrate that *every double-degenerate white dwarf merger necessarily enters into the propeller regime at some juncture in the accretion process*, provided solely that it does not first detonate promptly as an SN Ia. Ghosh & Lamb (1979) defined the fastness parameter ω_* of the central WD as

$$\omega_* = \frac{\Omega_{\text{WD}}}{\Omega_K(R_{\text{in}})} = \left(\frac{R_{\text{in}}}{R_{\text{co}}} \right)^{3/2}. \quad (3)$$

Here, R_{co} is the corotation radius $R_{\text{CO}} = (GM_1/\omega_{\text{WD}}^2)^{1/3}$. When $\omega_* > 1$, the disk is in the propeller regime. One can estimate the inner disk radius R_{in} as a fraction ξ of the Alfvén radius, where the inflow velocity of spherical accretion equals the Alfvén velocity, such that $R_{\text{in}} = \xi R_A$,

$$R_A = \left(\frac{\mu_*^2}{\sqrt{2GM\dot{M}}} \right)^{2/7}. \quad (4)$$

Here, μ_* is the stellar magnetic dipole moment, and \dot{M} is the mass accretion rate. The propeller regime condition is then simply expressed as $\Omega_{\text{WD}} > \Omega_K(R_{\text{in}})$, or

$$\Omega_{\text{WD}} > \left(\frac{GM_{\text{WD}}}{\xi^3 R_A^3} \right)^{1/2}. \quad (5)$$

Solving for \dot{M} , the propeller regime condition is

$$\begin{aligned} \dot{M} < \dot{M}_{\text{crit}} &= \frac{\xi^{7/2} B_s^2 R_{\text{WD}}^6}{\sqrt{2} G^{5/3} M_{\text{WD}}^{5/3}} \Omega_{\text{WD}}^{7/3} \\ &= \frac{\xi^{7/2} R_{\text{WD}}}{\sqrt{2} \Omega_{\text{max}}} \left(\frac{\Omega_{\text{WD}}}{\Omega_{\text{max}}} \right)^{7/3} \\ B_s^2 &= \frac{\xi^{7/2}}{2^{9/2} \pi^2} \frac{\Phi_s^2}{R_{\text{WD}}^2 v_{\text{max}}} \left(\frac{\Omega_{\text{WD}}}{\Omega_{\text{max}}} \right)^{7/3}, \end{aligned} \quad (6)$$

where $v_{\text{max}} = \Omega_{\text{max}} R_{\text{WD}}$ is the breakup velocity of the WD, $\Omega_{\text{max}} = \sqrt{GM_{\text{WD}}/R_{\text{WD}}^3}$ is the breakup angular velocity of the WD, and $\Phi_s = 4\pi R_{\text{WD}}^2 B_s$ is the mean surface magnetic flux.

The rotation rate Ω_{WD} of a rigidly rotating WD cannot exceed the maximal value, $\Omega_{\text{max}} = \sqrt{GM_{\text{WD}}/R_{\text{WD}}^3}$. Consequently, there is a minimum accretion rate \dot{M}_{crit} crossed when the mass of the accretion disk falls beneath a minimum value, $M_{\text{disk}} \sim \dot{M}_{\text{crit}} t_{\text{acc}}$, below which the system must enter into the propeller regime. The propeller regime has important ramifications for double-degenerate systems. In particular, as a result of the propeller regime, *the entire mass of the donor cannot be efficiently accreted onto the WD merger, and there is a minimum amount of mass, of order $\dot{M}_{\text{crit}} t_{\text{acc}}$, that must be ejected from the system* (see Figure 1d). We note that the propelled mass is in addition to both the tidal tail (Benz et al. 1990; Raskin & Kasen 2013) and magnetically driven jets and outflows (Ji et al. 2013) arising during the earlier phases of the merger; combined, this earlier ejected mass amounts to $\sim \text{few} \times 10^{-3} M_\odot$.

It is important to note that the critical mass accretion rate \dot{M}_{crit} is in turn set by the surface magnetic field of the merger. The propelled mass is clearly a magnetohydrodynamical phenomenon that is absent from a purely hydrodynamical treatment of the merger.

An upper bound estimate of the mass ejected in the propeller phase can be obtained by considering \dot{M}_{crit} and the spin-down

timescale, defined as $t_{\text{sd}} \approx \Omega_{\text{WD}}/|\dot{\Omega}|$. The spin-down of the WD merger in the propeller phase is due to the magnetic torque acting at the interface of magnetosphere and the inner radius of accretion disk; simulations of the MRI show that the Reynolds stress is negligible in comparison to the Maxwell stress (Davis et al. 2010). The spin-down of the WD can then be calculated by integrating the magnetic torque over the inner edge of the disk, assuming that the field at the inner edge of the disk is dominated by a dipolar HFMWD field threading the inner disk during the propeller phase, and the approximate equality of the radial and toroidal components of the magnetic field, $B_r \approx B_\phi$ (Romanova et al. 2003),

$$I \frac{d\Omega}{dt} = -4\pi R_{\text{in}}^2 f \left(R_{\text{in}} \frac{B_{R_{\text{in}}}^2}{8\pi} \right). \quad (7)$$

Then, the spin-down timescale is given by

$$\begin{aligned} t_{\text{sd}} &\approx \frac{\Omega_{\text{WD}}}{|\dot{\Omega}|} \\ &= 2^{4/7} \beta \xi^3 f^{-1} G^{1/14} B_s^{-2/7} \dot{M}^{-6/7} M_{\text{WD}}^{15/14} R_{\text{WD}}^{-5/14} \left(\frac{\Omega_{\text{WD}}}{\Omega_{\text{max}}} \right). \end{aligned} \quad (8)$$

Here, $\beta = I/(MR^2)$, where I is the moment of inertia of the WD and f is the fraction of the full spherical solid angle over which matter is being propelled.

An upper bound estimate for the mass ejected from the system M_{ej} can then be obtained by the product of the critical mass accretion rate \dot{M}_{crit} and spin-down timescale t_{sd} ,

$$\begin{aligned} M_{\text{ej}} &< \dot{M}_{\text{crit}} t_{\text{sd}} = 2^{1/2} \beta \xi^{7/2} f^{-1} M_{\text{WD}} \left(\frac{\Omega_{\text{WD}}}{\Omega_{\text{max}}} \right)^{4/3} \\ &\approx 0.2 M_\odot \left(\frac{\beta}{0.1} \right) \left(\frac{\xi}{1.0} \right)^{7/2} \left(\frac{f}{1.0} \right)^{-1} \\ &\quad \times \left(\frac{M_{\text{WD}}}{1.4 M_\odot} \right) \left(\frac{\Omega_{\text{WD}}}{\Omega_{\text{max}}} \right)^{4/3}. \end{aligned} \quad (9)$$

Physically, this upper-bound estimate on the propelled mass M_{ej} also follows immediately from the conversion of rotational energy of the WD into propelled mass being ejected at the escape speed at the Alfvén radius. Consequently, because the rotational energy of the WD is the ultimate source of energy of the propeller, this upper bound is independent of the magnetic field strength. It is also important to note that the upper bound to the ejected mass M_{ej} is also proportional to the rotational rate of the WD to the 4/3 power; mergers rotating more slowly than breakup will propel less mass.

2.4. Central Ignition

An off-centered ignition burns through the WD envelope to its center on a timescale of order $t_{\text{burn}} \sim 10^4$ yr (Nomoto & Iben 1985; Saio & Nomoto 1985; Schwab et al. 2016). The inwardly propagating carbon-burning flame initiates a convective zone (Schwab et al. 2016), but continues to stably progress inwards; Lecoanet et al. (2016) found the possibility that mixing induced by convective overshoot was unlikely to disrupt the flame. Consequently, in the absence of a strong magnetic field or substantial mass loss, an off-centered ignition invariably results in the formation of a neutron star (Schwab et al. 2016).

However, the magnetic field generated through the action of the turbulent MRI and accreted onto the rigidly rotating HFMWDs will in general be misaligned from its rotational axis. Consequently, the HFMWD will undergo angular momentum loss through the magnetic dipole radiation torque on a characteristic timescale t_B ,

$$\begin{aligned} t_B &\simeq \frac{Ic^3}{B^2 R^6 \Omega^2} \approx 10^2 \text{ yr} \left(\frac{\beta}{0.1} \right)^1 \\ &\quad \left(\frac{M}{1.4 M_\odot} \right) \left(\frac{B}{10^{10} \text{ G}} \right)^{-2} \left(\frac{\Omega_{\text{max}}}{\Omega} \right)^2 \left(\frac{\Omega_{\text{max}}}{5 \text{ s}^{-1}} \right)^{2/3}. \end{aligned} \quad (10)$$

Here, I is the moment of inertia of the WD, $I = \beta MR^2$, where $\beta \simeq 0.1$ (Yoon & Langer 2005), and Ω is the final angular velocity.

The subsequent spin evolution of the WD hinges critically upon its mass. A body of literature, beginning with Finn & Shapiro (1990) and Shapiro et al. (1990), showed that relativistically degenerate stars actually *spin up* and *compress* their cores with angular momentum loss. This seemingly nonintuitive effect is driven fundamentally by the compression induced by angular momentum loss, since the rigidly rotating near- M_{Ch} WD sequence greatly reduces its moment of inertia as it loses angular momentum. Geroyannis & Papatotiriou (2000) expanded on these findings, generating evolutionary sequences of rapidly rotating magnetic WDs, and demonstrating that near- M_{Ch} WDs with masses $\geq 1.32 M_\odot$ continue to spin up, and would compress their cores to extremely high densities $\rho_c = 4 \times 10^{10} \text{ g cm}^{-3}$, in the absence of nuclear reactions.

Becerra et al. (2018) showed that WD mergers with accretion rates set by the viscous timescale initially undergo rapid spin-up due to the torque exerted by the accreting material. When the Alfvén radius becomes larger than the WD radius, the remnant system enters the propeller phase, spinning down and compressing the WD and causing the central density to rapidly rise. Subsequently, Becerra et al. (2018) demonstrated that the timescale of the evolution of the WD is governed by the magnetic dipole radiation torque timescale t_B . In a subsequent paper, Becerra et al. (2019) examined the influence of a strong magnetic field misaligned with the rotational axis of an isolated WD, appropriate for this final phase of evolution of the merger, following the propeller phase. Becerra et al. (2019) demonstrated that the combined effects of neutrino cooling and angular momentum loss due to dipole emission lead to the central nuclear ignition of the merger for magnetic field strengths in excess of 10^7 G. Their detailed models predict timescales of the same order as our simpler estimate for t_B (Becerra et al. 2019). Moreover, Becerra et al. (2018, 2019) noted the sensitivity of the moment of inertia of the relativistically degenerate merger to its mass, with small changes of mass responsible for relatively large compression factors. Consequently, we expect that central ignitions of near- M_{Ch} DD mergers should be robust, and will tend to ignite in a very narrow mass range of progenitors subject to compression-induced angular momentum loss (see Figure 1e).

As a consequence of the relativistically degenerate cores of near- M_{Ch} WDs, uniformly rotating WDs will undergo spin-up and compression until they reach carbon ignition in their cores. The magnetic dipole radiation timescale t_B given by Equation (10) predicts that, for a magnetic field of 10^6 G, a typical field strength for field WDs (Ferrario et al. 2015), t_B exceeds the Hubble time. Thus, we emphasize that the

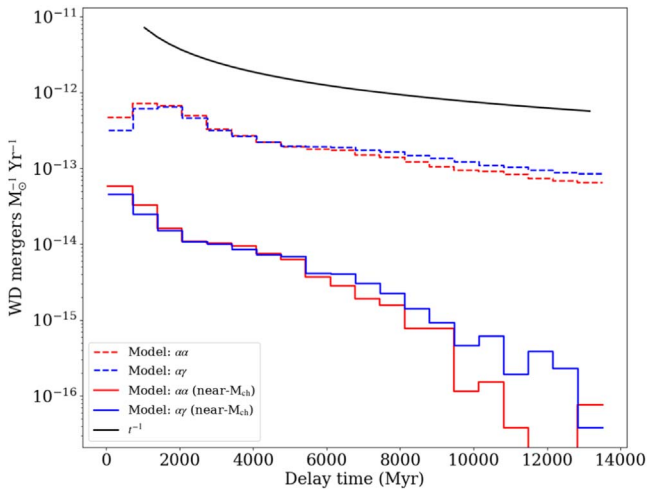


Figure 2. The delay time distribution of double WD mergers, along with the distribution of near- M_{Ch} CO mergers, obtained from the $\alpha\alpha$ and $\alpha\gamma$ BPS models. The near- M_{Ch} WDs have a total mass $M \geq 1.38 M_{\odot}$ and $M \leq 1.48 M_{\odot}$.

production of an HFMWD crucially enables this process of dipole-driven central ignition to be astrophysically relevant.

2.5. WD Merger Rate and Delay Time Distribution

Next, to examine the rate of near- M_{Ch} DD mergers and their associated delay time distribution, we employ two sets of BPS models from Toonen et al. (2012, 2017) using the SeBa code (Portegies Zwart & Verbunt 1996; Toonen et al. 2012). Both models assume a single burst of star formation, with initial periods determined by a flat distribution in the log of the initial semimajor axis. The models differ in the treatment of the common-envelope (CE) phase during the binary merger (Toonen et al. 2017). Model $\alpha\alpha$ assumes conservation of orbital energy for every common envelope phase (Webbink 1984). In contrast, model $\alpha\gamma$ adopts angular momentum conservation (Nelemans et al. 2000), unless a common envelope phase is initiated by a tidal instability, or if the binary contains a WD. Toonen et al. (2012, 2017) provide further details on the BPS models.

Figure 2 shows the delay time distribution (DTD) of all the WD mergers and the subset of near- M_{Ch} CO WD mergers for both common envelope prescriptions, along with a t^{-1} power law, consistent with the observed delay time distribution (Maoz et al. 2014). To create this DTD plot, we first created 20 equally spaced delay time bins. Then, we divided the number of mergers in each bin by the total BPS simulation mass to obtain the specific number of WD mergers per solar mass. Finally, the specific number of WD mergers is divided by the width of each delay time bin, yielding the specific rate of WD mergers per solar mass per year.

We calculate the fraction of WD mergers producing a double CO WD binary under two assumptions regarding mass accretion and ejection during the merger. In the first model, we assume mass accretion is completely conservative during the merger, without any mass lost through any of the possible processes discussed previously in Section 2: tidal tails, magnetized jets and outflows, and propeller-driven outflows. In the second model variation, we assume nonconservative mass accretion, with the maximal propelled mass according to Equation (9). These two model variations span the possible range of mass transfer during the merger. In particular, in order

to produce a near- M_{Ch} mass merger, mass ejection requires even more massive, and consequently rarer, WDs. As a result, fully conservative and maximally nonconservative mass accretion mergers yield upper and lower bounds, respectively, to the fraction of near- M_{Ch} WDs produced. The fraction of near- M_{Ch} CO WD mergers is then estimated by computing the fraction of total post-merger system masses M spanning the range of bounds for rigidly rotating near- M_{Ch} WDs ($1.38M_{\odot} \leq M \leq 1.48M_{\odot}$) from the BPS simulation data sets. The $1.38M_{\odot}$ lower mass bound is adopted from the minimum mass of a rigidly rotating WD that undergoes spin-up upon angular momentum loss in full GR, and the upper bound of $1.48M_{\odot}$ the maximum stable mass of a C-O rigidly rotating WD (Boshkayev et al. 2013).

The maximally nonconservative mass transfer assumption yields 2.7% and 2.0% of near- M_{Ch} CO WD systems for $\alpha\alpha$ and $\alpha\gamma$ models, respectively. Similarly, under the fully conservative mass transfer assumption, these fractions increase to 3.5% and 3.1% for $\alpha\alpha$ and $\alpha\gamma$ models, respectively. Combined, we estimate that near- M_{Ch} CO WD mergers may account for 2%–3.5% of all WD mergers, with the estimates spanning the range of maximally nonconservative to fully conservative mass transfer during the merger, and accounting for both the $\alpha\alpha$ and $\alpha\gamma$ common envelope prescriptions. A radial velocity survey by Maoz et al. (2018) shows that the double WD (DWD) merger rate is approximately six times the specific SN Ia rate in our galaxy. Thus, near- M_{Ch} DWD mergers may account for up to 12%–21% of all SNe Ia events, if all near- M_{Ch} CO DWD mergers result in a SN Ia.

However, because the fundamental physical process of detonation initiation in a turbulent, unconfined medium is an extremely challenging one to address (Poludnenko et al. 2011; Fenn & Plewa 2017; Fisher et al. 2019; Poludnenko et al. 2019), the explosive outcome of a near- M_{Ch} WD remains uncertain from a first-principles standpoint. A central ignition in the core of the near- M_{Ch} WD leads to a deflagration bubble (Nomoto et al. 1984) at a single offset location, according to ab initio numerical simulations (Zingale et al. 2011; Nonaka et al. 2012; Malone et al. 2014). This flame bubble will buoyantly rise and become unstable to the reactive Rayleigh–Taylor and Kelvin–Helmholtz instabilities, driving turbulence that may cause the deflagration to transition to a detonation (Khokhlov 1991), and thereby lead to an SN Ia. Alternatively, the bubble may continue to buoyantly rise until it erupts from the surface of the WD. Under this second possibility, a portion of the buoyant ash will be expelled from the gravitationally bound WD, which is kicked in the opposite direction and enriched from the remaining ash, which falls back onto the surface of the WD. Observational (Jha 2017) and theoretical evidence (Jordan et al. 2012; Fink et al. 2014) point toward the possibility that at least some of these failed detonation events will be visible as SNe Iax (Foley et al. 2013; Stritzinger et al. 2015) and leave behind surviving kicked WDs enriched by ash rich in IGEs resulting from high-density burning, such as LP 40-365 (Raddi et al. 2019).

Therefore, if alternatively a near- M_{Ch} DWD merger ignites but fails to detonate, it will instead produce an SN Iax (Jordan et al. 2012; Fink et al. 2014). This near- M_{Ch} DWD merger rate is close to the 10%–30% of the total SNe Ia rate estimated for SNe Iax by Foley et al. (2013), suggesting that near- M_{Ch} DWD mergers may largely account for the SNe Iax population if the

majority of mergers ignite as pure deflagrations but fail to detonate.

3. Hydrodynamical Simulation and Postprocessing Methodology

We next consider the observable signatures of SNe Ia DD near- M_{Ch} events. In order to capture the detailed nucleosynthetic yields and synthetic spectral signatures of SNe Ia events originating from DD near- M_{Ch} mergers, we turn to hydrodynamical simulations, combined with a nucleosynthetic and radiative transfer post-processing pipeline.

In the following analysis, we will consider the possibility that the DD near- M_{Ch} WD progenitor leads to a successful SNe Ia via the DDT mechanism. We adopt an equilibrium WD progenitor model with a cold degenerate core and a hot, thick isentropic envelope to model the end state of the merger following spin-down and ignition (Yoshida 2019). In particular, as described above, during the final inspiral due to gravitational wave emission, the secondary reaches its Roche limit and is tidally disrupted, forming a massive disk that is then subsequently accreted onto the primary white dwarf. The strong magnetic fields cause nascent HFMWDs to be in a state of uniform rotation. The addition of rigid rotation has only a minimal impact on the density structure of the WD (Ostriker & Bodenheimer 1968; Yoshida 2019), so we utilize a nonrotating WD model for the purpose of computing nucleosynthetic yields and synthetic spectra. We further neglect the influence of the magnetic field upon the WD structure, as the pressure is dominated by the degenerate electron pressure for HFMWDs with surface fields of 10^{10} G and less (Ji et al. 2013), and simulate the evolution in pure hydrodynamics.

More specifically, with this physical picture of the merger remnants in mind, we model the hydrostatic initial condition for our time-dependent simulations as follows. The equation of state (EOS) for the hot envelope is the Helmholtz EOS, which includes contributions from nuclei, electrons, and blackbody radiation, and supports an arbitrary degree of degeneracy and special relativity for the electronic contribution (Timmes & Swesty 2000), and a completely degenerate EOS for the cold core (Shapiro & Teukolsky 1986). The envelope is assumed isentropic. We compute the hydrostatic model using a modified version of Hachisu’s self-consistent field method code (Hachisu 1986), which self-consistently computes both the matter distribution and the gravitational field. The input parameters are the chemical composition of the core and the boundary, the central density, the pressure at which the core-envelope boundary exists, the temperature of the envelope at the core-envelope boundary, and the parameter specifying the rotational deformation of the star, which is set zero here. Further details are given in Yoshida (2019). This hydrostatic model is subsequently mapped into the initial condition for our hydrodynamical simulations, as specified below.

The central density of a near- M_{Ch} SN Ia event plays a primary role in determining the nucleosynthesis of key iron group elements including ^{56}Ni as well as neutronized isotopes such as ^{55}Fe , the parent isotope of ^{55}Mn . For illustrative purposes, we adopt only a single set of representative parameters for the merger for this paper. We select a model with a central density $2 \times 10^9 \text{ g cm}^{-3}$, which has been widely adopted for near- M_{Ch} SNe Ia (Nomoto et al. 1997; Woosley 1997). The total mass of the model is $1.378M_{\odot}$, with a core mass of $0.795M_{\odot}$ and an envelope mass of $0.593M_{\odot}$. If the

merger process conserved mass, the core and envelope masses would equate to the primary and secondary WD masses, respectively. In reality, mass accretion will be nonconservative due to magnetohydrodynamically driven jets and winds and tidal tail ejection, implying the secondary mass will be slightly more massive than the $0.593M_{\odot}$ of the envelope in order to account for mass ejected from the system.

As noted in Section 2.2, the temperature of the envelope is the result of the complex magnetohydrodynamical processes involved during the merger, including the development of MRI turbulence and a magnetized corona, as well as jets and outflows. In our model, this complexity is subsumed into the entropy of the envelope, or equivalently the temperature at the base of the envelope. The primary WD is modeled as isothermal with a temperature of 10^8 K, while the tidally disrupted secondary forms a hot, thick isentropic envelope around the primary with a base temperature 10^9 K, typical of binary WD mergers (Zhu et al. 2013). The composition of the hydrodynamical model is taken to be 50/50 C/O, though we also consider the effect of solar metallicity in nucleosynthetic post-processing.

As noted above, while significant advances have been made in our understanding of turbulent detonation initiation, much work still needs to be done to incorporate these physically realistic detonation mechanisms into first-principles multi-dimensional simulations of SNe Ia. However, the ab initio simulations of the deflagration phase point toward the ignition of a single buoyancy-driven bubble with a mean offset of 40 km (Zingale et al. 2011; Nonaka et al. 2012; Malone et al. 2014). While the process of ignition is inherently a stochastic one, the ab initio simulations indicate the majority of ignitions lead to buoyancy-driven deflagration phases with weak pre-expansion (Fisher & Jumper 2015; Byrohl et al. 2019). Furthermore, recent advances regarding turbulently driven detonation initiation point toward a higher DDT transition density, $\sim 10^8 \text{ g cm}^{-3}$, earlier than the distributed burning density of $\sim 10^7 \text{ g cm}^{-3}$ previously assumed (Poludnenko et al. 2019).

Accordingly, in our DDT model, we adopt a simplified explosion scenario. Incorporating these recent SN IA combustion advances, we neglect the weak pre-expansion of the deflagration phase, and centrally detonate the merger model with a detonation radius of 23 km. The hydrostatic progenitor model is mapped to 2D axisymmetry in the Eulerian adaptive mesh refinement (AMR) code FLASH (Fryxell et al. 2000; Dubey et al. 2009, 2014).⁶ The inviscid Euler equations of hydrodynamics are advanced using an unsplit, higher-order Godunov method. (Lee & Deane 2009) We ran the hydrodynamical simulation on a 2D azimuthally symmetric cylindrical $r-z$ domain, with z axis extending from -1.31072×10^6 km to 1.31072×10^6 km, and r axis extending from 0 to 1.31072×10^6 km. The region surrounding the WD in the domain is filled with a low-density matter with negligible inertia and thermal energy, having an initial density of $10^{-3} \text{ g cm}^{-3}$ and a temperature of 3×10^7 K. FLASH utilizes the Helmholtz EOS (Timmes & Swesty 2000). An advection-diffusion-reaction equation is employed for the detonation front, along with a simplified treatment of the nuclear energy generation (Townsend et al. 2007, 2009). The Poisson equation

⁶ Though the model presented here is essentially spherically symmetric, the 2D axisymmetric setup enables broader sets of initial conditions for comparison against other published runs.

for self-gravity is solved using a multipole moment method (Couch et al. 2013) with isolated boundary conditions, including terms up to $l=6$ in the expansion. In the DDT model, the system is evolved until it reaches free expansion. To follow the nuclear-burning regions with maximal refinement, and to derefine regions with low density, we use several refinement criteria based on Townsley et al. (2007) and Townsley et al. (2009). In our run, refinement and derefinement of the grid is based on a dimensionless gradient parameter of density and burnt fraction, a scalar field that tracks the detonation surfaces, and ranges from 0 for pure fuel to 1 for pure ash (Townsley et al. 2016). The maximum spatial resolution for the hydrodynamical simulations presented here is 4 km.

We also incorporate passively advected Lagrangian tracer particles (Dubey et al. 2012) to record the thermodynamic state along the particle trajectories throughout the simulation. The tracer particles are initialized proportional to the mass in the simulation domain. In the runs presented here, we used 10^4 particles, which provides good precision for near- M_{Ch} WDs in 2D (Seitenzahl et al. 2010). Thermodynamic histories of these particles are restructured into trajectory files that are then post-processed in Torch nuclear network (Timmes 1999), with 489 species, to obtain the detailed nucleosynthetic yields. A convergence test for sample trajectories showed that the maximum final abundance error for integration time step tolerances using abundance normed errors between 10^{-6} and 10^{-8} was $\sim 0.3\%$. Consequently, in the results presented here, an integration time step tolerance of 10^{-6} was used for all tracer particles.

To generate synthetic spectra, we map the nucleosynthetic yields onto a 2D axisymmetric velocity mesh. This homologically expanding mesh is then followed with the LTE radiative transport code SuperNu (Wollaeger et al. 2013; Wollaeger & van Rossum 2014), which employs the implicit Monte Carlo (IMC) and discrete diffusion Monte Carlo (DDMC) methods. We bin photons at every time step into 512 logarithmically spaced wavelength bins within 10^3 – $10^{4.5}$ Å. To classify the synthetic spectra, we use the supernova identification code SNID (Blondin & Tonry 2007), which cross-correlates the input model spectra with templates of previously observed events, and identifies the best-matched supernova type as well as its epoch.

4. Simulation Results

4.1. DD Near-Chandrasekhar-mass DDT

The hydrodynamical simulation of the detonation through free expansion yields a total nuclear energy of 2.13×10^{51} erg. Overall, the energetics and nucleosynthetic yields are comparable to the most energetic deflagration-to-detonation near- M_{Ch} previously published (Seitenzahl et al. 2013b; Ohlmann et al. 2014; Leung & Nomoto 2018), though with the marked difference of less ^{28}Si , owing to the less vigorous pre-expansion resulting from our deflagration and turbulently driven deflagration-to-detonation model assumptions. Table 1 contains stable mean nucleosynthetic yields for isotopes with abundances greater than $10^{-6}M_{\odot}$. Complete mean nucleosynthetic yields, which include both stable and radioisotopes obtained at the onset of free expansion, $t=2.5$ s, with abundances greater than $10^{-6}M_{\odot}$ are given in Table 2.

Table 1
DDT Stable Mean Nucleosynthetic Yields in Solar Masses

Isotope	$Z=0$	$Z=Z_{\odot}$
^4He	9.21×10^{-3}	8.09×10^{-3}
^{12}C	2.85×10^{-6}	3.53×10^{-6}
^{16}O	9.33×10^{-4}	1.04×10^{-3}
^{24}Mg	7.78×10^{-5}	1.55×10^{-5}
^{28}Si	7.76×10^{-3}	7.95×10^{-3}
^{29}Si	1.97×10^{-6}	3.84×10^{-6}
^{30}Si	8.23×10^{-6}	4.68×10^{-6}
^{31}P	1.81×10^{-6}	3.47×10^{-6}
^{32}S	4.93×10^{-3}	4.80×10^{-3}
^{33}S	2.59×10^{-7}	3.62×10^{-6}
^{34}S	3.93×10^{-6}	2.64×10^{-5}
^{35}Cl	1.43×10^{-6}	2.96×10^{-6}
^{36}Ar	1.22×10^{-3}	1.12×10^{-3}
^{38}Ar	5.69×10^{-7}	1.60×10^{-5}
^{39}K	1.70×10^{-6}	4.23×10^{-6}
^{40}Ca	1.32×10^{-3}	1.18×10^{-3}
^{44}Ca	1.10×10^{-5}	8.67×10^{-6}
^{48}Ti	6.29×10^{-5}	5.55×10^{-5}
^{49}Ti	5.09×10^{-7}	2.67×10^{-6}
^{51}V	1.12×10^{-5}	1.59×10^{-5}
^{50}Cr	3.88×10^{-5}	4.74×10^{-5}
^{52}Cr	1.26×10^{-3}	1.19×10^{-3}
^{53}Cr	2.31×10^{-4}	3.07×10^{-4}
^{55}Mn	9.19×10^{-3}	1.02×10^{-2}
^{54}Fe	7.79×10^{-2}	8.52×10^{-2}
^{56}Fe	9.98×10^{-1}	9.60×10^{-1}
^{57}Fe	4.24×10^{-2}	4.72×10^{-2}
^{59}Co	1.45×10^{-3}	1.54×10^{-3}
^{58}Ni	1.98×10^{-1}	2.26×10^{-1}
^{60}Ni	1.78×10^{-2}	1.45×10^{-2}
^{61}Ni	7.18×10^{-4}	7.90×10^{-4}
^{62}Ni	4.61×10^{-3}	6.42×10^{-3}
^{63}Cu	4.75×10^{-5}	6.58×10^{-6}
^{65}Cu	5.22×10^{-6}	5.69×10^{-6}
^{64}Zn	2.77×10^{-4}	8.66×10^{-5}
^{66}Zn	8.67×10^{-5}	1.17×10^{-4}
^{68}Zn	2.04×10^{-6}	1.35×10^{-7}
^{70}Ge	2.31×10^{-6}	2.31×10^{-6}

Notes. Only isotopes in excess of $10^{-6}M_{\odot}$ in either model are shown. Abundances for all isotopes are provided in machine-readable format.

Plots of the frozen-out electron abundance fraction $Y_e = \sum_i X_i Z_i / A_i$, where Z_i is the atomic number, A_i is the atomic mass number, and X_i is the mass abundance of the isotope i , are depicted near the onset of homologous expansion in Figure 3. Consistent with the findings of previous simulations of near- M_{Ch} SNe Ia DDT models (including Meyer et al. 1996; Nomoto et al. 1997; Woosley 1997; Brachwitz et al. 2000; Krueger et al. 2012), we find that the greater electron capture rates in the cores of denser WD progenitors lead to greater abundances of stable IGEs in the n-NSE regime.

Next, in conducting our synthetic spectroscopic classification, we compare not to a single event, but rather to a template library, just as new optical transients are classified observationally. Accordingly, we utilize the supernova identification code SNID, which defines the quality parameter r to quantify the strength of the correlation between the input synthetic spectra and previously observed events (Blondin & Tonry 2007). Tonry & Davis (1979) defined the parameter r in terms of the ratio of the height h to the root mean square of the antisymmetric term of the normalized cross-correlation

Table 2
DDT Frozen-out Mean Nucleosynthetic Yields in Solar Masses

Isotope	$Z = 0$	$Z = Z_{\odot}$
^4He	9.21×10^{-3}	8.09×10^{-3}
^{12}C	2.85×10^{-6}	3.53×10^{-6}
^{16}O	9.33×10^{-4}	1.04×10^{-3}
^{24}Mg	7.78×10^{-5}	1.55×10^{-5}
^{28}Si	7.76×10^{-3}	7.95×10^{-3}
^{29}Si	7.47×10^{-7}	3.84×10^{-6}
^{30}Si	1.55×10^{-7}	4.65×10^{-6}
^{30}P	5.85×10^{-6}	3.38×10^{-8}
^{30}S	2.22×10^{-6}	7.15×10^{-12}
^{31}S	9.57×10^{-7}	5.44×10^{-8}
^{32}S	4.93×10^{-3}	4.80×10^{-3}
^{34}S	1.62×10^{-6}	2.64×10^{-5}
^{34}Cl	1.65×10^{-6}	5.59×10^{-9}
^{35}Cl	1.11×10^{-6}	2.94×10^{-6}
^{36}Ar	1.22×10^{-3}	1.12×10^{-3}
^{38}Ar	1.75×10^{-7}	1.60×10^{-5}
^{39}K	1.61×10^{-6}	4.17×10^{-6}
^{40}Ca	1.32×10^{-3}	1.18×10^{-3}
^{44}Ti	1.10×10^{-5}	8.67×10^{-6}
^{48}Cr	6.29×10^{-5}	5.55×10^{-5}
^{49}Cr	5.08×10^{-7}	2.67×10^{-6}
^{50}Cr	3.88×10^{-5}	4.74×10^{-5}
^{51}Mn	1.11×10^{-5}	1.58×10^{-5}
^{53}Mn	3.25×10^{-6}	4.29×10^{-6}
^{52}Fe	1.26×10^{-3}	1.19×10^{-3}
^{53}Fe	2.28×10^{-4}	3.03×10^{-4}
^{54}Fe	7.79×10^{-2}	8.52×10^{-2}
^{55}Fe	1.55×10^{-4}	1.83×10^{-4}
^{56}Fe	5.38×10^{-5}	7.85×10^{-5}
^{55}Co	9.04×10^{-3}	1.00×10^{-2}
^{56}Co	1.48×10^{-4}	1.60×10^{-4}
^{57}Co	8.77×10^{-5}	1.04×10^{-4}
^{56}Ni	9.98×10^{-1}	9.60×10^{-1}
^{57}Ni	4.24×10^{-2}	4.71×10^{-2}
^{58}Ni	1.98×10^{-1}	2.26×10^{-1}
^{59}Ni	1.98×10^{-4}	2.21×10^{-4}
^{60}Ni	1.35×10^{-4}	1.63×10^{-4}
^{58}Cu	2.80×10^{-4}	2.22×10^{-6}
^{60}Cu	8.22×10^{-5}	6.92×10^{-5}
^{61}Cu	1.18×10^{-5}	1.33×10^{-5}
^{60}Zn	1.76×10^{-2}	1.43×10^{-2}
^{61}Zn	7.07×10^{-4}	7.77×10^{-4}
^{62}Zn	4.61×10^{-3}	6.42×10^{-3}
^{63}Zn	4.38×10^{-6}	3.29×10^{-6}
^{63}Ga	4.26×10^{-5}	3.28×10^{-6}
^{64}Ga	4.65×10^{-6}	1.93×10^{-6}
^{64}Ge	2.72×10^{-4}	8.46×10^{-5}
^{65}Ge	4.69×10^{-6}	5.09×10^{-6}
^{66}Ge	8.66×10^{-5}	1.17×10^{-4}
^{68}Se	1.92×10^{-6}	8.50×10^{-8}
^{70}Se	2.31×10^{-6}	2.84×10^{-6}

Notes. Only isotopes in excess of $10^{-6} M_{\odot}$ in either model are shown. Abundances for all isotopes are provided in machine-readable format.

function between the input and the template spectra, σ_a , so that $r = 2^{-1/2} h \sigma_a^{-1}$. In addition, SNID also uses the overlap of the spectra in log wavelength space to quantify the reliability of the correlation peak. To match with the wavelength range of the input spectrum at the correlation peak redshift, the template spectra are trimmed. Then the overlap parameter, named lap, in log wavelength space is given by $0 \leq \text{lap} \leq \ln(\lambda_1/\lambda_0)$, where $[\lambda_0, \lambda_1]$ is the rest-frame wavelength range of the input

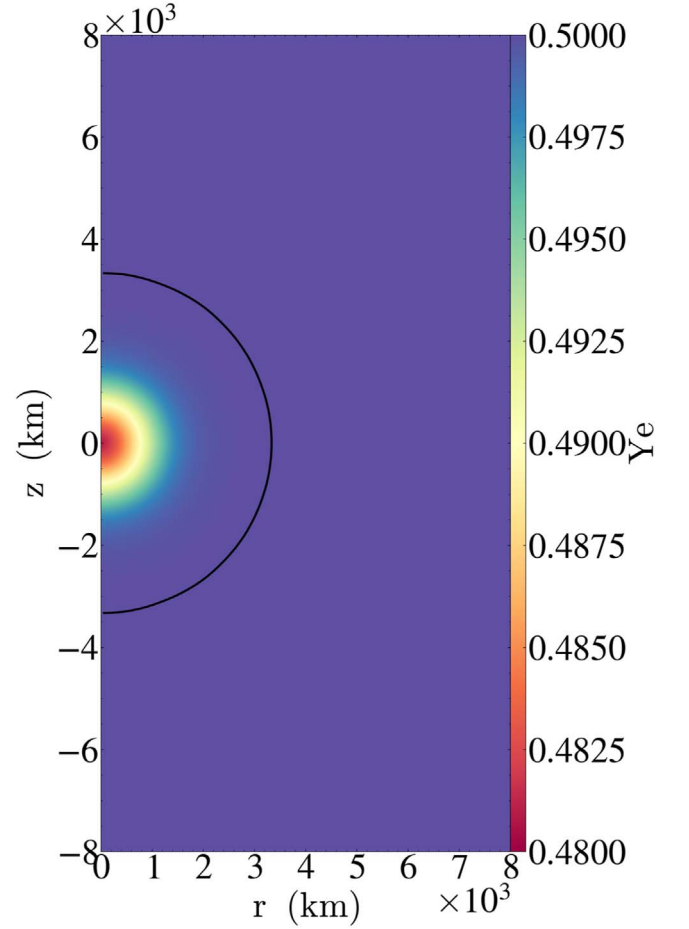


Figure 3. Slice plot of Y_e at $t = 240$ ms, when the nucleosynthetic yields have frozen out, showing the centrally concentrated region of neutronized isotopes produced from electron captures. Note that this plot represents the hydrodynamic model output, which is at zero WD progenitor metallicity. The 10^6 g cm^{-3} density isocontour is represented by a black line.

spectrum. Values of rlap , defined as the product of r and lap , over 5 are considered to be good matches. We constrain our synthetic spectra to the rest frame at redshift $z = 0$.

SNID classifies the best matches to the synthetic spectra at peak brightness for both WD progenitor metallicities $Z = 0$ and $Z = Z_{\odot}$ as SN 1999ee, a type Ia-norm, at an epoch of -9.1 days (Hamuy et al. 2002). These matches have rlap scores 7.5 and 8.6, respectively. Figure 4 shows the synthetic spectrum for $Z = Z_{\odot}$, plotted against its best-match spectrum. *We emphasize that the match is obtained directly from the near- M_{Ch} progenitor without any fine-tuned parameters.* The overall agreement between the two spectra is quite good, with the noted exception of a blueshift in the synthetic spectral Si II absorption feature near 6000 \AA , in comparison to SN 1999ee, as well as in the pre-peak epoch identification. The inclusion of non-LTE in the radiative transfer is expected to shift the Si II feature toward the red, which may partially account for this disagreement (Shen et al. 2021). The blueward shift of the Si II feature caused by the LTE approximation may also partially account for the SNID epoch identification prior to peak brightness, as the Si II feature generally shifts redward at later epochs (Pereira et al. 2013).

We also note that SN 1999ee is a member of a class of SNe Ia with high-velocity Si II and Ca II features (HVF s). The origin of these features in SN 1999ee and other similar SNe Ia HVF

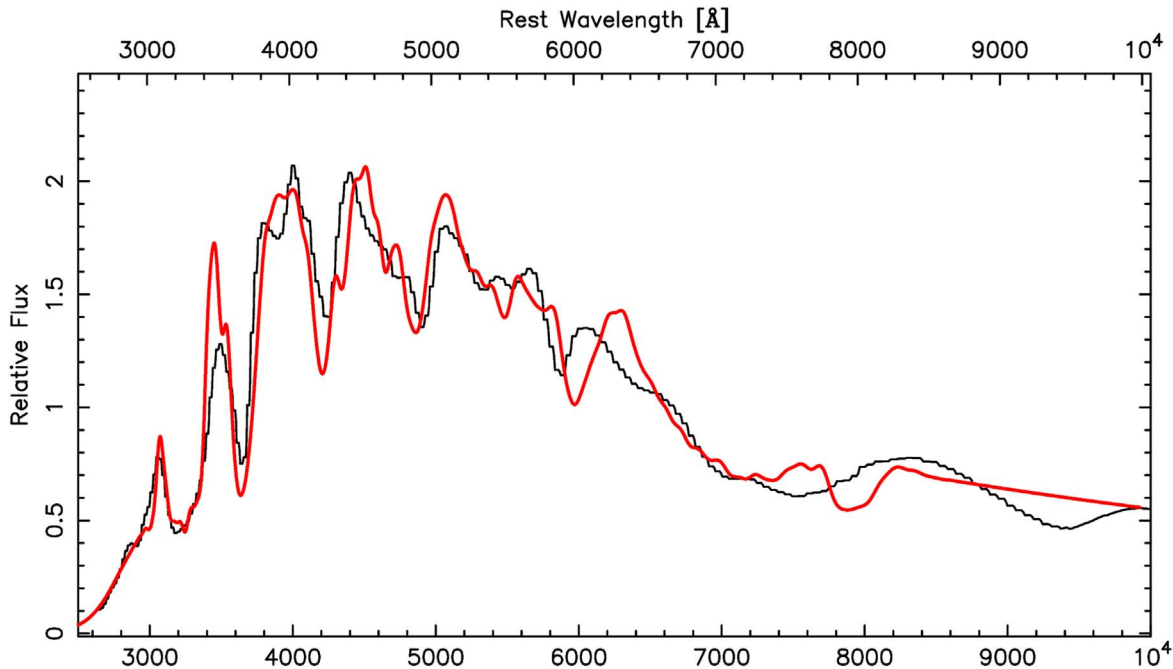


Figure 4. Synthetic peak brightness model spectrum (black) at WD progenitor metallicity $Z = Z_{\odot}$ compared with the best-matching spectral template, SN 1999ee, a normal Ia (red).

events has been discussed in the literature, with possibilities ranging from density and abundance enhancements in the progenitor WD to interactions with circumstellar material (Mazzali et al. 2005). Our models support the viewpoint that the high-velocity Si II HVF in particular may be connected to nuclear burning on massive white dwarfs (Kato et al. 2018).

To compare against observations of supernova remnants, we consider stable isotopic abundances. Because supernova remnants typically have ages of hundreds to thousands of years, in the decay chain $^{53}\text{Fe} \rightarrow 9\text{m } ^{53}\text{Mn} \rightarrow 4\text{ Myr } ^{53}\text{Cr}$, we restrict the ^{53}Fe decay to ^{53}Mn only (Unterwiesing et al. 1992). The decayed IGE abundance ratios relative to solar abundances, with a WD progenitor with solar metallicity $Z_{\odot} = 0.0139$ (Asplund et al. 2021), and C/O ratio of unity yield $[\text{Ni}/\text{Fe}] = 0.62$, $[\text{Cr}/\text{Fe}] = -1.11$ and $[\text{Mn}/\text{Fe}] = 0.02$, all relative to solar. The $[\text{Ni}/\text{Fe}]$ ratio is higher than Tycho or Kepler, but comparable to SNR 3C 397. We emphasize that this comparison is based upon our specific choice of parameters, and is therefore illustrative rather than exhaustive of the range of possibilities of DD near- M_{Ch} SNe Ia.

5. Observational Implications

The classical single-degenerate near- M_{Ch} DDT mechanism requires fine-tuning of the ignition in order to obtain the vigorous pre-expansion necessary for a normal SN Ia. In contrast, DD near- M_{Ch} SNe Ia naturally begin with an extended heated envelope of tidally disrupted material from the secondary. The braking timescale is less than the cooling timescale for the WD merger for an HFMWD, allowing the WD progenitor to retain this extended envelope at the onset of detonation. As a direct result, a DDT within a DD near- M_{Ch} naturally predicts a normal SN Ia with high-velocity Si II features without any fine-tuning of parameters, even though the silicon abundance is significantly subsolar. We expect that a range of central densities at ignition, as well as entropies of the envelopes of DD near- M_{Ch} progenitors, will be produced from

DD near- M_{Ch} SNe Ia and SNe Iax, depending on the masses of the binary WDs. These progenitors will in turn produce a range of nucleosynthesized ^{56}Ni and hence intrinsic luminosities. Since the compression mechanism of DD near- M_{Ch} due to angular momentum loss differs fundamentally from the compression due to accretion from the nondegenerate donor of the SD scenario, further models are required to explore the evolution of highly magnetized WD mergers as they reach ignition conditions, and connect these to SNe Ia and SNe Iax explosion models.

A similar magnetic dipole mechanism for nuclear ignition as discussed here is also envisioned for the core degenerate scenario (Ilkov & Soker 2012). The two scenarios differ in the physical explanation for the DTD. In the core degenerate scenario, the DTD is explained by the magnetic braking timescale, whereas in our scenario the DTD is explained instead by gravitational wave inspiral, as in the standard double-degenerate scenario. Because the core degenerate scenario predicts a long post-merger delay, and our proposed scenario a relatively prompt delay, the two scenarios offer different possibilities for SN ejecta interactions, which can be used in observational tests.

SNe Ia and their remnants are known to have a high degree of spherical symmetry. Spectropolarimetry of normal SNe Ia generally reveal a low degree of polarization, typically 0.5% in the Si II absorption line feature at peak brightness, which is a sensitive probe of the outskirts of the SN (Wang & Wheeler 2008; Cikota et al. 2019). This degree of polarization in SNe Ia is particularly striking in comparison with core-collapse SNe, particularly striped envelope CCSNe, which can exhibit much greater polarizations up to several percent, which translate into intrinsic SN asymmetries of tens of percent (Wang et al. 2001; Wang & Wheeler 2008). Additionally, the line and thermal X-ray emission of SNe Ia remnants also possess a high degree of spherical symmetry (Lopez et al. 2009, 2011). Taken together, these observational findings place

stringent limits on SNe Ia channels that predict large asymmetries, either in the progenitor or the explosion mechanism, or through the SN blast wave interacting with a nondegenerate companion or circumstellar medium. For example, the violent double-degenerate merger predicts Si II polarization of $\sim 1\%$ – 3% , in excess of most observations of normal SNe Ia (Cikota et al. 2019). Additionally, the interaction of the SN blast wave with the nondegenerate stellar companion in the classical single-degenerate near- M_{Ch} scenario leaves a large “shadow” that is present in the young remnant for hundreds of years (Gray et al. 2016).

In contrast, the DD near- M_{Ch} channel predicts the WD merger progenitor will be uniformly and slowly rotating at the time of detonation, and so will be very highly spherical. Furthermore, as emphasized in our discussion of deflagration initiation and the turbulent deflagration-to-detonation mechanism, recent work points toward a mild pre-expansion and relatively prompt detonation. Consequently, DD near- M_{Ch} SNe Ia will have very low Si II polarization near peak brightness.⁷ While the first DDT simulations of DD near- M_{Ch} SNe Ia presented in this paper neglect the initial deflagration phase, we expect that more realistic simulations including the initial deflagration phase through the DDT will produce Si II polarization levels similar to prior near- M_{Ch} SNe Ia DDT models, typically well under 1%, in line with observational constraints (Cikota et al. 2019). Further, DD near- M_{Ch} SNe Ia remnants will also naturally be nearly spherically symmetric, without the shadow predicted to arise from the companion in the classical single-degenerate near- M_{Ch} scenario.

A large body of observational evidence has also placed stringent constraints on SNe Ia nebular H α (Leonard 2007; Tucker et al. 2020), X-ray (Margutti et al. 2014), and radio emission (Chomiuk et al. 2016), and the existence of stellar binary companions (Li et al. 2011) and ex-companions (Schaefer & Pagnotta 2012) pre-explosion and post-explosion, respectively, in the vast majority of normal SNe Ia systems. A natural prediction of the near- M_{Ch} DD scenario is that there is no surviving companion, implying that there can also be no nebular H α emission. The near- M_{Ch} DD scenario further predicts an absence of strong prompt X-ray and radio emission, although there are prospects for delayed interaction with the propelled and ejected material.

Recent work on the ratio of the abundances of Ni II/Fe II, accessible through optical and NIR lines, has elucidated that this line ratio is sensitive to the mass of the progenitor, owing largely to the production of stable Ni isotopes in the cores of near- M_{Ch} events, in particular ^{58}Ni (Flörs et al. 2018, 2020). The use of stable Ni is therefore a promising discriminant between near- M_{Ch} and sub- M_{Ch} events (though also subject to caveats—see Blondin et al. 2021). The nucleosynthetic yields presented here predict a relatively high abundance of $^{58}\text{Ni}/^{56}\text{Fe} = 0.2$ for a DD near- M_{Ch} event, in comparison to other previously computed near- M_{Ch} models (Blondin et al. 2021). While the $^{58}\text{Ni}/^{56}\text{Fe}$ abundance ratio will decrease in a more realistic explosion scenario including the deflagration phase, the stable Ni test may help shed light not only upon the mass of the SN Ia progenitor, but also the physics of its formation and the detonation mechanism.

⁷ The failed detonation of DD near- M_{Ch} progenitors leading to SNe Iax will have a much greater degree of asymmetry originating from the explosion mechanism itself: the pure deflagration within its interior.

While substantial evidence points toward the likelihood that partially burnt near- M_{Ch} WDs lead to SNe Iax (e.g., Jha 2017), there is a relative scarcity of direct observational evidence for helium through the helium-accreting single degenerate channel. Jacobson-Galán et al. (2019) find early-time He I CSM lines in two of a sample of 44 SNe Iax; with a luminosity limit cutoff, they conclude He I CSM features are present in 33% of the remaining sample. They further find no evidence for stripped helium in the late-time nebular spectra of 11 SNe Iax, placing an upper bound limit on the amount of helium to be less than $10^{-2}M_{\odot}$ in these events, with even tighter bounds of $10^{-3}M_{\odot}$ for stripped hydrogen. In the context of the near- M_{Ch} DD scenario, the absence of large amounts of helium in SNe Iax spectra is a natural consequence of the complete merger of the double-degenerate system prior to the SN Iax event. Most of the thin 10^{-3} – $10^{-1}M_{\odot}$ (Lawlor & MacDonald 2006) helium surface layers atop the two white dwarfs will be susceptible to nuclear burning during the final merger. However, the rapid accretion just prior to and during the tidal disruption of the donor may cause a small amount of helium to be ejected through the outer Lagrange point L2 (Livio et al. 1979; MacLeod et al. 2018). Such ejected helium may account for the early-time He I CSM seen in some SNe Iax.

Another strong constraint on SNe Ia channels is the t^{-1} observed delay time distribution (DTD) (Maoz et al. 2010; Maoz & Badenes 2010; Graur et al. 2011; Maoz et al. 2012). DD models generically predict a t^{-1} DTD from gravitational wave inspiral. In contrast, theoretical models of the SD typically produce a sharper decay, owing to the absence of the requisite intermediate mass SD donors over 10 Gyr timescales. While multicomponent SD DTDs invoking both main-sequence and red giant donor channels have found agreement with a t^{-1} DTD (Hachisu et al. 2008), these same models encounter the aforementioned tensions with the observed absence of companion signatures in the majority of SNe Ia events. In contrast, DD near- M_{Ch} SNe Ia originate from the same gravitational wave inspiral mechanism that underlies the overall DD population and do not possess companion signatures. Consequently, as we have demonstrated in Section 2.5, the DTD of DD near- M_{Ch} SNe Ia retains the t^{-1} DTD of the wider DD population. Furthermore, the characteristic t^{-1} DTD shape is not significantly biased by a mass selection effect, even taking into account the maximum possible mass lost through the propeller phase.

Recent models of double detonations on sub- M_{Ch} WDs suggest that carbon-enriched helium surface layers may produce sufficient ^{55}Mn to reduce but not entirely eliminate the need for near- M_{Ch} SNe Ia events (Gronow et al. 2021). Consequently, the classical SD scenario and its corresponding predictions for companion and ex-companion interactions is in tension with the requisite need to produce ^{55}Mn through near- M_{Ch} . The nucleosynthetic yields for the DD near- M_{Ch} event presented here shows an approximately solar abundance of Mn/Fe. Late-time light curves (Seitenzahl et al. 2009) offer a window into the 55 and 57 isobar decay chains terminating in ^{55}Mn and ^{57}Fe , respectively, and may help shed light on both the progenitor as well as the explosion scenario.

There are two primary means of observationally determining the galactic WD merger rate. The first method infers the WD merger rate from observations of WD field binaries (Maoz et al. 2018). The second examines single WDs, and discriminates those produced by mergers from those resulting from isolated

evolution (Cheng et al. 2020). The field WD merger rate obtained in the most recent observations is systematically higher than that inferred from merged single WDs, which may be at least in part be due to unaccounted systematics between these two techniques. Explosive transients, including the near- M_{Ch} DD mergers described here, may account for a key systematic bias between these two sets of observations.

Observational surveys of the abundance ratios of [Ni/Fe] and [Mn/Fe] have yielded a rich picture of the nucleosynthetic histories of different galactic environments. In particular, the dwarf spheroidal Sculptor, which had a single burst of star formation after its formation, has decreasing ratios of [Ni/Fe] and [Mn/Fe] as a function of metallicity [Fe/H], a proxy for age (Kirby et al. 2019; de los Reyes et al. 2020). In contrast, other galactic environments with ongoing star formation histories, including Leo I, Fornax, and the Milky Way, exhibit increasing ratios of [Ni/Fe] and [Mn/Fe] with [Fe/H] (Kirby et al. 2019; de los Reyes et al. 2020). Because near- M_{Ch} events, including the DD channel presented here, generally have higher [Ni/Fe] and [Mn/Fe] in comparison to sub- M_{Ch} events, the nucleosynthetic histories of stellar environments such as Sculptor undergoing a single star formation burst point toward an increasing predominance of sub- M_{Ch} relative to near- M_{Ch} events with time. Other stellar environments with ongoing star formation histories point instead toward an increasing ratio of near- M_{Ch} to sub- M_{Ch} events with time. A possible explanation for these diverse SNe Ia histories stems from considerations of both the sub- M_{Ch} as well as the DD near- M_{Ch} DTDs. The DTD of sub- M_{Ch} double detonations from nondegenerate donors inferred from BPS models exhibit a sharp cutoff at times earlier than ~ 1 Gyr (Ruiter et al. 2014). In contrast, the characteristic t^{-1} shape of the DD near- M_{Ch} DTD is significantly delayed relative to sub- M_{Ch} double detonations fed by nondegenerate donors. Furthermore, the qualitative difference of the DD near- M_{Ch} DTD with the classical SD near- M_{Ch} DTD, which cuts off sharply after a few Gyr (Kobayashi et al. 2020), may offer a potentially observable test of these different scenarios for the production of near- M_{Ch} SNe Ia.

During the final writing of this paper, the discovery of a rapidly rotating, strongly magnetized near- M_{Ch} WD, ZTF J190132.9+145808.7, was reported (Caiazzo et al. 2021). The surface magnetic field was estimated to be 600–800 MG, with an inferred internal O/Ne composition approaching a central density of $\sim \text{several} \times 10^9 \text{ g cm}^{-3}$ and central temperature $\sim 7 \times 10^8 \text{ K}$. This rapidly rotating, strongly magnetized near- M_{Ch} WD is similar to the DD near- M_{Ch} progenitors discussed in this paper. The inferred internal composition and thermodynamic structure, as well as the inferred age of this WD will, however, hinge crucially on magnetohydrodynamical processes that give rise to such a strongly magnetized WD, and further modeling is required in order to better elucidate its formation mechanism and evolution.

6. Conclusion

In this paper, we have presented a model for the production of near- M_{Ch} WDs from the DD channel resulting from the merger and inspiral of two C/O WDs. The magnetic field plays a crucial role in this mechanism, first during the production of a high-field magnetic WD during the merger, and second in compressing the core of the WD to ignition conditions during spin-down. We have also demonstrated the onset of a propeller

phase during the merger, with potentially observable interaction signatures. Finally, we presented an exploratory hydrodynamical simulation of a DD near- M_{Ch} system, computed its nucleosynthetic yields, and matched its synthetic spectrum to that of a normal SN Ia. The initial condition of this hydrodynamical simulation incorporated the effect of tidal heating of the secondary WD during the merger, using a self-consistent equilibrium with an isentropic hot envelope. The hydrodynamical simulation assumes negligible pre-expansion and negligible magnetic pressure and rotational support within the merger.

To summarize the key observable signatures of SNe Ia and SNe Iax produced by DD near- M_{Ch} :

1. A t^{-1} DTD both DD near- M_{Ch} SNe and SNe Iax.
2. The absence of companion and ex-companion signatures in both DD near- M_{Ch} SNe and SNe Iax.
3. Weakly polarized Si II lines in DD near- M_{Ch} SNe Ia.
4. In near- M_{Ch} DD SNe Ia, the production of a bright normal to potentially overluminous (91T-like) event.
5. The absence of strong H and He signatures in both DD near- M_{Ch} SNe and SNe Iax. Trace He abundances may be possible by ejection through the outer Lagrange point L2, and may account for He I CSM in some events.
6. Solar or supersolar abundances of [Mn/Fe] and [Ni/Fe].
7. Highly spherical SNRs, with high [Mn/Fe] and [Ni/Fe] abundance ratios, and without companion shadows.

Further theoretical modeling and simulation is required in order to obtain a clearer picture of the role that magnetohydrodynamics plays in WD mergers, and to help address which circumstances lead to explosive transients, and which lead to stable massive magnetized mergers. While magnetohydrodynamics plays a key role during the WD merger, the process has been long neglected in the majority of models. Massive magnetized WDs like ZTF J190132.9+145808.7 are providing us with a strong clue that the stellar merger, magnetohydrodynamics, and the SN Ia mechanism are all inextricably linked.



New observational instruments, including JWST and the Rubin Observatory, will help discriminate both between sub- M_{Ch} and super- M_{Ch} events and the explosion scenario using a wide range of observational tests, including the radioisotopic decay of SNe Ia late-time light curves, and the presence of stable Ni in the nebular phase of SNe Ia. Detailed surveys of galactic SN Ia SNRs, particularly of the near- M_{Ch} SNR 3C 397, will shed a complementary light on the stellar progenitor and the explosion mechanism.

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Software: SeBa (Toonen et al. 2012), FLASH 4.3 (Fryxell et al. 2000; Dubey et al. 2012), FLASH SN Ia module Townsley et al. (2016) (<http://pages.astronomy.ua.edu/townsley/code>), yt (Turk et al. 2011), Python programming

language (van Rossum & de Boer 1991), Numpy (van der Walt et al. 2011), IPython (Perez & Granger 2007), Matplotlib (Hunter 2007).

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