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Identifying fibre orientations for fracture process zone characterization in scaled centre-notched quasi-isotropic carbon/epoxy laminates with a convolutional neural network

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ABSTRACT

This paper presents a novel X-ray Computed Tomography (CT) image analysis method to characterize the Fracture Process Zone (FPZ) in scaled centre-notched quasi-isotropic carbon/epoxy laminates. A total of 61 CT images of a small specimen were used to fine-tune a pre-trained Convolutional Neural Network (CNN) (i.e., VGG16) to classify fibre orientations. The proposed CNN model achieves a 100% accuracy when tested on the CT images of the same scale as the training set. However, the accuracy drops to a maximum of 84% when tested on unlabelled images of the specimens having larger scales potentially due to their lower resolutions. Another code was developed to automatically measure the size of the FPZ based on the CNN identified 0° plies in the largest specimen which agrees well with the manual measurement (on average within 3.3%). The whole classification and measurement process can be automated without human intervention.

1. Introduction

A size effect describes the change of strength with specimen dimensions [1]. It has significant implications on the strength prediction of full-scale aerospace structures, which were proven to be challenging [2,3]. Previously, in-plane scaled centre-notched quasi-isotropic (QI) carbon/epoxy specimens were tested, and the tensile strength was found to decrease with increasing specimen dimensions [4]. The size effect was associated with a Fracture Process Zone (FPZ) ahead of the centre-notch tips. It is crucial to characterize the FPZ in order to explain the size effect in QI laminates.

FPZ was studied by using a variety of techniques including Digital Image Correlation (DIC) [5–7], and X-ray Computed Tomography (CT) [4,8,9]. DIC can generate surface strain fields automatically, which is then associated with the size of FPZ via some assumptions, e.g., force equilibrium being achieved at the FPZ boundary in [6]. Compared with DIC, CT scanning can objectively quantify internal damage, such as in 0° plies, and accurately determine the size of FPZ. By using CT scans, it was found that the size of the FPZ, which was quantified by the fibre breakage length in the 0° plies, initially scaled with the notch size and then approached a plateau at larger scales, leading to a change of scaling law [4]. However, processing CT data is a time-consuming manual process. Automation of CT analysis for FPZ characterization can potentially further promote the adoption of CT scanning.

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Convolutional Neural Networks (CNN) are an excellent tool for computer vision tasks like image recognition and classification. CNNs are usually built using three types of layers: (i) convolutional layers, (ii) sub-sampling layers, and (iii) fully connected layers. The convolutional layers employ a set of filter masks, also called feature detectors, to capture the relevant patterns (i.e., feature maps) in the dataset images. Once the relevant features of the images are detected, sub-sampling (or pooling) layers are usually utilized to decrease the feature maps' spatial resolution, which in turn reduces the reliance on precise positioning within feature maps produced by the convolutional layers. Disregarding the exact position of features within a feature map while maintaining the relative position of features with respect to each other allows for a better CNN performance on inputs that relatively differ from the training data. The final convolutional or sub-sampling layer is flattened and connected to fully connected layer(s) to perform the classification task.

CNNs have been used to analyse images of advanced materials, such as a bicontinuously nanostructured copolymer [10], and 3D-printed metal [11] to characterize cracks. Trained by finite element simulations, these CNNs derived accurate fracture properties, including crack length and fracture toughness. CNNs have been widely applied to medical CT analysis, such as for intraoperative imaging, to improve surgical precision as reviewed by Alam et al. [12]. However, only a few articles were published on CT analysis of advanced composites using CNNs. For example, Yang et al. [13] adopted a U-net CNN to reconstruct a rubber composite structure from only tens of micro-CT images. Chen et al. [14] also adopted a U-net deep CNN to create digital material twins for woven ceramic-matrix composites from micro-CT images. Tian et al. [15] used a mask and regional CNN to detect local cracks from CT images of concrete. A deep CNN was also used to detect surface or near-surface defects in composites from X-rays [16]. Some work on characterization of individual fibre orientation has been done using dictionary-learning [17] in which a segmentation method could accurately extract individual fibres from low contrast X-ray scans of composites with high fibre volume fraction. However, classification of fibre orientations using CNNs from CT images has not been done. This is extremely useful for the determination of fracture properties of composites, such as the size of FPZ.

This paper presents a novel CT analysis method using a CNN for classification of fibre orientations and then another code to measure FPZs. The proposed workflow is established to automatically measure the FPZ size in centre-notched QI carbon/epoxy laminates in two steps. First, a pre-trained, fine-tuned VGG16 CNN was trained using labelled CT images of the centre-notched specimens from interrupted tests at 95% of average failure load. Then, the CNN was applied to the unlabelled CT images of the other centre-notched specimens having different scales to classify their fibre orientations. A test accuracy of 100% for the former and a maximum prediction accuracy of 84% for the latter were achieved. After the 0° plies were identified, the size of the FPZ in the largest centre-notched specimen was automatically measured to understand the size effect by using an image analysis workflow. To the author's best knowledge, this paper is the first to use a CNN for the classification of fibre orientations in multi-directional composites from CT images. The present method can potentially automate CT analyses for FPZ evolution with notches. In doing so, it can improve accuracy and efficiency and reduce potential human errors.

2. Experiments

A schematic of the in-plane scaled centre-notched QI specimens is shown in Fig. 1(a). The specimens with a notch length of C = 3.2 mm is referred to as the baseline, C = 6.4 mm as Scale 2, C = 12.7 mm as Scale 4 and C = 25.4 mm as Scale 8. The schematic of the largest centre-notched specimens with a notch length of C = 50.8 mm (Scale 16) is shown in Fig. 1(b). Only their width and notch length are doubled from the Scale 8 specimens, while their gauge length remains the same. Scale 16 specimens were not fully scaled due to limitations of the facilities. It was found that the specimens with a halved gauge length of the baseline specimens had a similar tensile strength within 3% [4].

The material used was HexPly[®] (Hexcel, US) IM7/8552 carbon-epoxy unidirectional pre-preg with a cured nominal ply thickness of 0.125 mm. The stacking sequence was $[45/90/-45/0]_{4s}$, for all the sizes. The nominal specimen thickness was 4 mm. The centre notches were cut with a 1 mm end mill on a computer numerical controlled milling machine. Then the notch tips were manually extended by using 0.25 mm-wide piercing saw blades.

250 kN Instron and 500 kN Dartec hydraulic-driven test machines were used. The scaled specimens were tested under tension using displacement control with scaled loading rates for different gauge lengths, e.g., 0.25 mm/min for the baseline, 0.5 mm/min

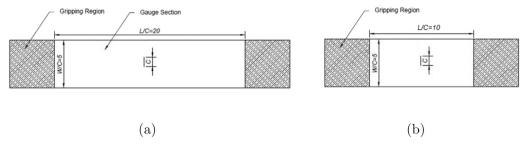


Fig. 1. Schematic of (a) in-plane scaled centre-notched specimens with C = 3.2 to 25.4 mm and (b) largest specimen with C = 50.8 mm.

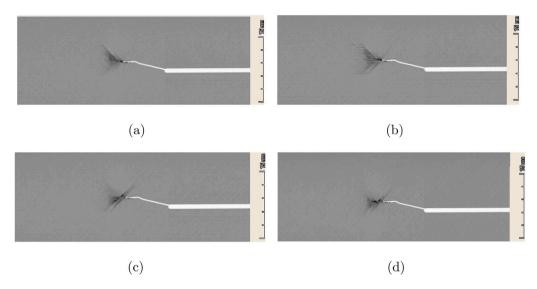


Fig. 2. Typical CT images of Scale 16 specimen (a) 45° (b) 90° (c) -45° (d) 0°.

for Scale 2, 1 mm/min for Scale 4, 2 mm/min for Scale 8 and Scale 16. Interrupted tests in which the tests were stopped at 95% of the average failure load were carried out. The tensile test results were documented in by Xu et al. [4].

A single specimen from each size was examined by CT scanning to measure the FPZ, so a total of five specimens were scanned. The specimens from the interrupted tests were soaked in a bath of zinc iodide penetrant for three days. A Nikon XT H 225 ST CT scanner was used to scan the specimens from interrupted tests. The scanner has a 3 μ m focal spot size, but the spatial resolution varies with the specimen size. For example, the CT images of the scaled centre-notched specimens reported by Xu et al. [4] had a pixel size of 18 μ m for the baseline, 20 μ m for Scale 2, 47 μ m for Scale 4 and 71 μ m for Scale 8. The CT images of the largest Scale 16 specimen were not reported by Xu et al. [4] because the specimen was too large for the CT scanner to generate quality images. In this paper, the largest Scale 16 specimen from the interrupted test for CT scanning was cut down to a narrower strip parallel to the centre notch, so the X-ray source could be placed closer to the notch tips to achieve a pixel size of 106 μ m. The edges of the strip were kept away from the centre notch, so no further damage was introduced to the existing FPZ at the notch tip as shown in Fig. 2. The 3D CT volumes were segmented into 2D CT images for each ply through the specimen thickness in VG Studio Max (Volume Graphics, Germany). The previously labelled CT images from the single CT scan of the Scale 2 specimen were used for training, validation, and testing of the CNN for image classification. Then the CNN was applied to the unlabelled CT images of Scale 4, Scale 8, and Scale 16 specimens to classify their fibre orientations. The details are explained in Section 4.1.

3. CNN methodology

Training a CNN from scratch to obtain a high classifier accuracy requires significantly more training data than is feasible in this case due to the expensive nature and the human resources necessary to run the CT scans. Data augmentation and transfer learning were used in this paper to overcome the relatively limited training set size. Additionally, the CT images were standardized by making the mean of the entire dataset equal to zero and the standard deviation equal to one. Transfer learning allows for good accuracy when dealing with small datasets by taking a pre-trained neural network and re-purposing its learned features and weights to model a different dataset. The ability of several well-known CNN architectures and weights to fit and classify our dataset was investigated (e.g., ResNet50 [18], InceptionV3 [19], and VGG16 [20]). A fine-tuned version of VGG16 yielded the best accuracy in our case, with a 100% ability to provide the correct classification for the considered testing set using labelled CT images.

VGG16 won the first and second places in the ImageNet Large Scale Visual Recognition Competition (ILSVRC) 2014 in the localization and the classification tasks, respectively. The ImageNet dataset used in training VGG16 includes over 14 million images belonging to around 22 thousand categories [20,21]. VGG16 comprises 16 trainable layers interspersed with sub-sampling layers, as shown in Fig. 3, and is considered as one of the excellent vision model architectures. In this paper, the pre-trained weights of the convolutional layers have been maintained while optimizing the weights of the two last fully connected layers to model the dataset. A stochastic gradient descent optimizer was adopted with a learning rate of 10^{-3} , a decay of 10^{-6} , and a 0.9 momentum paired with Nesterov's accelerated gradient [22,23].

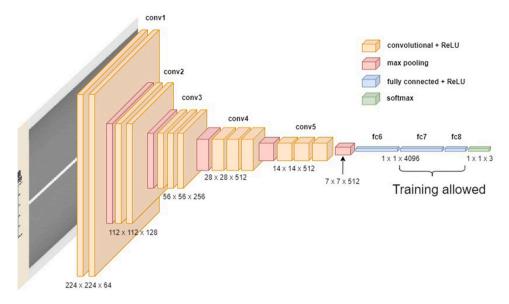


Fig. 3. Proposed CNN architecture based on VGG16 with fine-tuning.

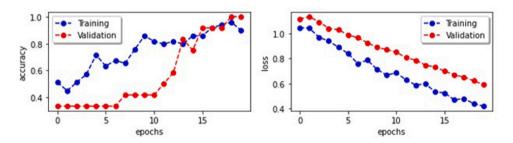


Fig. 4. Proposed CNN model: model accuracy (left) and loss function value (right) over epochs.

4. Results

4.1. Classification of fibre orientations using a CNN

The objective of the proposed CNN is to classify fibre orientations in the in-plane scaled centre-notched specimens into three classes, 0°, 45°, and 90° plies, based on CT images from the interrupted tests according to the flowchart in Fig. 6. A total of 61 labelled CT images from the Scale 2 interrupted test were used for the (i) training, (ii) validation and (iii) testing of the CNN. All above images were augmented by horizontal flipping, rotating, and shifting the original CT images in each set using Keras's image data generator class [22]. The baseline specimen has a different damage pattern in the centre 0° ply compared to other sizes, so it is not used in the CNN. The Scale 2 images have better quality than the even larger scales, so are chosen for training. The Scale 2 images were approximately split into an 80% training set and a 20% validation & testing set. Specifically, the training set comprised 12 CT images of the 0° plies, 25 of the 45° plies, and 12 of the 90° plies. The validation & testing set contained 4 CT images of the 0°, 4 of the 45°, and 4 of the 90° plies. Each ply was sliced once. The CNN reached a 100% model accuracy after 20 epochs, based on a categorical cross-entropy loss function. Fig. 4 contains the accuracy (left) and loss function value (right) of a trained model showing a 100% model accuracy. The corresponding confusion matrix normalized by the numbers of tested images for each considered fibre orientation is shown in Fig. 5. It shows fibre orientation prediction; diagonal-terms all being 1 mean that the trained model identified all fibre orientation correctly. They show that the predicted fibre orientations agree extremely well with the true fibre orientations within the training set. The total run time was 1.7 s and the time per step at the final epoch was 0.27 s, demonstrating the computational efficiency of the current CNN model.

Once training, validation, and testing were completed based on the Scale 2 CT images, the CNN was also applied to Scales 4, 8, and the new Scale 16 CT images to predict their fibre orientations. The prediction accuracy dropped to 83.9% for Scale 4, 62.6% for Scale 8, and 60.1% for Scale 16 as shown in Fig. 7. This means that when the scale of the target CT images is closer to that of the training dataset, the prediction accuracy is higher. However, it was preferred to use the CNN trained by the Scale 2 CT images to identify the 0° plies of the largest Scale 16 specimen for two practical reasons: (i) this proposed bottom-up approach is more

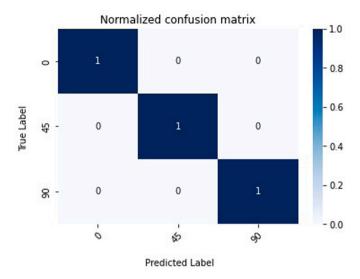


Fig. 5. Normalized confusion matrix showing an excellent agreement between actual and predicted fibre orientations; diagonal terms being 1 means 100% accuracy, using the training dataset.

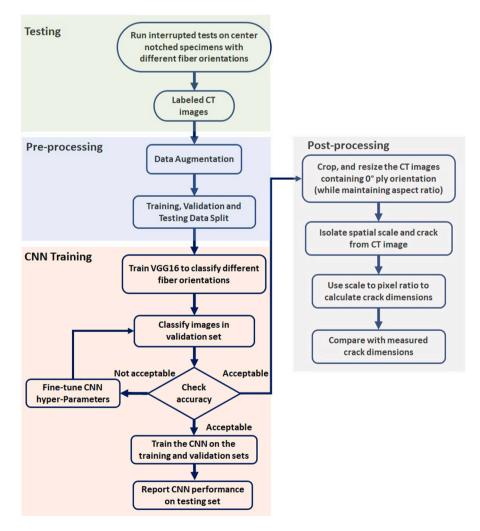


Fig. 6. Two-step FPZ characterization process: CNN for fibre orientation identification and followed by automated post-processing for FPZ characterization.

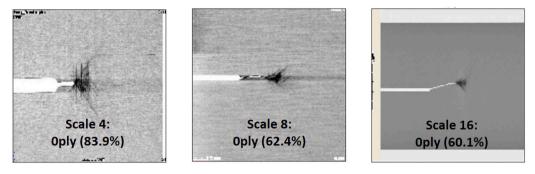


Fig. 7. CNN model prediction accuracy on unlabelled CT images (not to scale).

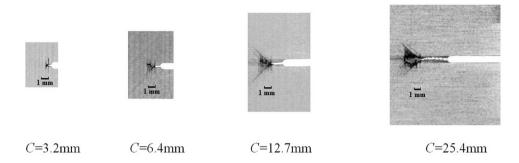


Fig. 8. CT images of typical single 0° plies in scaled centre-notched specimens.

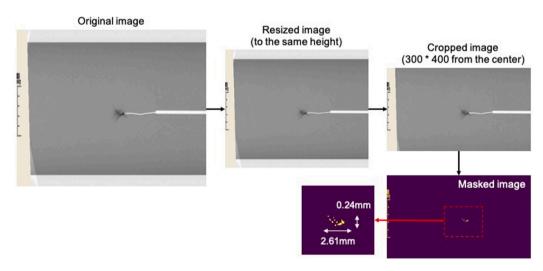


Fig. 9. Automated crack measurements using the CT image of a 0° ply.

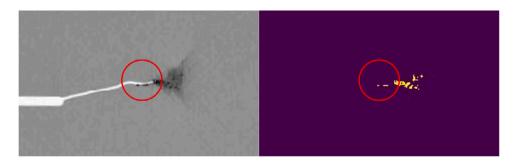


Fig. 10. Over-estimated crack length due to excessive dye penetrant (in red circle).

Table 1 Comparison of FPZ measurements based on the 0° plies of Scale 16 specimen.

Image No.	Manual measurement	Automatic measurement	Error
1	2.85	2.79	-2.11%
2	2.74	2.71	-1.09%
3	2.74	2.81	2.55%
4	2.96	2.92	-1.35%
5	2.74	2.69	-1.85%
6	2.96	2.69	-9.12%
7	3.28	3.16	-3.66%
8	2.74	2.61	-4.74%
9	2.96	2.72	-8.11%
Mean	2.88	2.79	-3.27%
CV ^a	6.23%	5.92%	
10 ^b	2.96	4.99	68.8%
11 ^b	2.85	4.74	66.5%
12 ^b	3.39	5.34	57.3%

^aCoefficient of Variation.

in line with the test pyramid approach for real-world applications and (ii) the new FPZ measurements for Scale 16 specimens are more representative of the material properties since the FPZ from the smaller specimens are not fully developed [4].

4.2. FPZ characterization

The FPZ size is defined as the average horizontal distance between the furthest fibre breakage point to the notch tip in the single 0° plies. The furthest fibre breakage point is often marked by the last 0° split in the specimen, but practically represented the furthest pixel in black in the CT images. Previously, the size of FPZ was measured manually for the baseline, Scale 2, Scale 4, and Scale 8 specimens as shown in Fig. 8 [4]. In the current study, the FPZ measurements were done both manually and automatically based on the new set of CT images from the Scale 16 specimen. A spatial scale was printed on the images during the CT analysis (Fig. 9). After the CNN was trained and used to identify the 0° plies, a workflow was developed to automatically post-process the CT images by isolating the spatial scale and the crack to measure its dimensions as shown in Fig. 6. First, the images were cropped and resized while preserving the original images' aspect ratio. The crack and spatial scale's colour gamut was then isolated from the rest of the image. The scale to pixel ratio was then calculated from the filtered image, which was then used to calculate the size of the FPZ based on the number of pixels occupied by the crack. As a comparison, manual measurements were also done using the software *Image J* (National Institutes of Health, US) by comparing the number of pixels for the FPZ and that for the scale.

The automatic measurements of the FPZ are compared with the manually measured values in Table 1. From the first 9 images out of the total 12 considered, the automatically measured FPZ size is 2.79 mm, with an average relative percentage error of 3.3% from the manual measurement. The last three measurements, however, show a large discrepancy. The reason for this is because some excessive dye penetrant remains in the pre-existing crack tip, which misleads the code to believe that it is part of the FPZ (Fig. 10). These three measurements are an artefact of the image processing analysis, so they are excluded when calculating the size of the FPZ.

5. Discussion

One may argue that this satisfactory result (a 100% model accuracy) emanates from over-interpretation (or over-fitting) of the training dataset. This may be true for a small dataset (\leq 100 data) used for training. In this work, VGG16 was the backbone of the CNN architecture and fine-tuned with optimizing the weights of only last fully connected layers (Fig. 3). As previously stated, data augmentation and transfer learning was applied to try to avoid potential over-fitting of the model. The CNN model is currently being improved with cross-validation, feature selection, and regularization techniques to simplify its architecture, thus overcoming potential over-fitting issue.

It is not surprising that the accuracy dropped, depending on how different the scale of the target CT images is from the training dataset. The CNN generally predicted the fibre orientations from the CT images of the relatively smaller specimens (Scale 4) more accurately than from the larger specimens (Scales 8 and 16). This is potentially due to nosier CT data and poorer CT image quality at the larger scales. More work is needed to improve the proposed CNN prediction accuracy when dealing with the unlabelled CT images of different specimen sizes.

When identifying fibre orientations in the centre-notched QI carbon/epoxy laminates, the CNN initially showed a high accuracy level. However, the code had limitations when measuring the FPZ from the identified 0° plies, such as not recognizing the excessive dye penetrant. This illustrates that the second automated step for FPZ measurement could be further improved, e.g., by creating a mask using a threshold optimized for each CT image.

The new CT images confirmed that the measured FPZ size of the Scale 16 specimens (C = 50.8 mm) does not double when compared to the previously reported 2.28 mm for the Scale 8 specimens (C = 25.4 mm) [4]. Instead, it approaches an approximately constant size while the notched strength approaches a fracture-mechanics scaling asymptote [4].

^bMeasurements influenced by excessive dye penetrant are excluded.

6. Conclusions

A Convolutional Neural Network (CNN) has been successfully implemented for in-plane scaled centre-notched carbon/epoxy quasi-isotropic laminates to classify fibre orientations based on X-ray Computed Tomography (CT) images. It achieved a 100% test accuracy on the labelled Scale 2 CT images (the same scale as the training set) and a maximum prediction accuracy of 84% using the unlabelled CT images of the other sized specimens (Scales 4, 8 and 16). After the 0° plies were identified, the size of the FPZ from the new CT images of the Scale 16 specimen was automatically measured using another newly developed image processing code. The automatically measured FPZ size agrees well with the manually measured average value using *Image J* - an open-source image analysis software platform - with an average relative error of 3.3%. The current method enables the automation of FPZ characterization from CT images, potentially eliminating human interventions while maintaining good accuracy.

CRediT authorship contribution statement

Xiaodong Xu: Writing – review & editing, Writing – original draft, Validation, Resources, Project administration, Methodology, Investigation, Funding acquisition, Data curation, Conceptualization. Aser Abbas: Software, Formal analysis. Juhyeong Lee: Writing – review & editing, Visualization, Validation, Supervision, Software, Methodology, Investigation, Funding acquisition, Formal analysis, Conceptualization.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

The raw/processed data required to reproduce these findings cannot be shared at this time as the data also forms part of an ongoing study.

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