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Mono and Stereoscopic Image Analysis for Detecting the Transverse Profile of Worn-Out Rails

Marco Guerrieri^a*, Giuseppe Parla^b, Dario Ticali^c

^a Faculty of Engineering (CRB), University of Perugia, Strada S. Lucia Canetola s.n.,06125 Perugia, Italy ^bFaculty of Engineering, University of Palermo, Viale delle Scienze, 90144 Palermo, Italy ^cFaculty of Engineering, University of Enna "Kore", Cittadella Universitaria, 94100 Enna, Italy

Abstract

The purpose of this paper is to suggest a new procedure for reconstructing the transverse profile of rails in operation by means of *image-processing technique*. This methodological approach is based on the "information" contained in high-resolution photographic images of tracks and on specific algorithms which allow to obtain the exact geometric profile of the rails and therefore to measure the state of the rail-head extrados wear. The analyses and the results concern rails taken from railway lines under upgrading by means of mono- and stereoscopic methods which are appropriate to be employed in laboratory applications or in high-efficiency surveys in situ.

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1. Introduction

One of the most frequent and dangerous accidents in the railway field is the derailment which can be caused by a lot of factors, some occasional and statistically insignificant, others much more frequent and due to mismanagement of the superstructure which may be below the minimum safety standards established by the rail management authorities. Among these accidents, there is the derailment accident which can be classified according to the determining factors as follows: *i) wheel-flange-climb derailment; ii) slide-up derailment*, generally due to too broad a gauge; *iii) jump-up derailment* caused by a violent collision of the train wheel with

^{*} Corresponding author. Tel.: +39 333.9993614.

E-mail address: marco.guerrieri@tin.it

the rail. The most frequent, and therefore the most interesting, is the wheel-flange-climb derailment, which occurs when the forward motion of the axle is combined with an excessive ratio of Q/P wheel/rail contact forces. This usually occurs under conditions of reduced vertical force and increased lateral force that cause the wheel flange to roll onto the top of the rail head. The climb condition may be temporary, with wheel and rail returning to normal contact, or it may result in the wheel fully climbing over the rail [1]. If we respectively denote the transverse load with Q, the wheel load with P, the flange angle with α and the friction coefficient with *f*, the limit value of the ratio Q/P (see Fig. 1) which avoids the derailment can be obtained from Nadal's well-known equation [2]:

$$\frac{Q}{P} = \frac{\tan \alpha - f}{1 + f \tan \alpha} \tag{1}$$

Nadal's equation allows to lead to two limit situations: the former concerning a high safety level which occurs in presence of heavy axial loads P and low values of the lateral force Q; the latter regarding a low safety level which occurs in opposite conditions (moderate axial load and high lateral force value). From relation (1) it is inferred that, all conditions being equal, the ratio Q/P decreases when the flange angle increases as an effect of the rail wear (see Fig. 1). Apart from the rail head wear, there could be a great number of other damage, cracks or defects (see Fig. 2) on the rail, thus potentially endangering safety conditions.

The rail wear and other imperfections can be both monitored through low-efficiency equipment (e.g. miniprof device) or diagnostic trains which perform track laser scans while monitoring rail travels [3]. More recently the potentialities offered by *real-time image processing techniques* to determine the vertical, horizontal and 45° rail wear have been pointed out [4, 5, 6, 7, 8].

The following paragraphs describe the results got from laboratory analyses performed on worn-out rails taken from railway lines under upgrading, and aimed to determine the transverse profile of the railhead by means of mono- and stereoscopic techniques.



Fig.1. Q/P Ratio (according to Nadal equation)



Fig. 2. Rail wear and damage (examples)

2. Image Processing for Railways Track Profile Measurement (monoscopy)

The primary goal of image processing is to make the information content of a given image explicit with regard to the reference application type. All the segmentation methods are defined to process an image through specific algorithms which divide that image into distinct and uniform regions according to a set feature [9]. This operation is the first step to distinguish the region enclosing the object of interest (ROI, region of interest) from the other parts or the background. Such an image partition process must be able to preserve the valuable information along the object contours which in this paper is the starting point for detecting the distances between the rail transverse profiles in different operational conditions, more specifically worn-out and new rails. After analyzing the image of the rail (e.g. UIC 60), the segmentation procedure detects the image contour or "edge" through Canny's algorithm [10]. Only afterwards this procedure solves the problem to compare the two rail profiles (worn-out and new) and to measure the vertical, horizontal and 45° deviations. The image edge detection phase is necessary in that digital images are definitely realized by high-resolution equipment but some image pixels could be affected by noise (very rough light scatterings located at the rail image contour), thus making the rail edge detection less accurate. More specifically, it is essential to detect the exact position of the image edge even in those parts where it cannot be distinguished, perceptually and/or numerically, from the clear background. Canny's algorithm examines the behavior of the gradient operator applied to a noisy contour. The algorithm establishes that the pixel located at position (i,j) on the generic chromatic plane p^{\dagger} of the image A(i,j,p) is a Canny contour pixel if the intensity value of the pixel examined -A(i,j,p) – appears to be superior to given threshold values as established by Canny [10], based upon hysteresis thresholding and non-maximum suppression algorithms. It has also been observed that on the same image, an edge detection applied separately to the three chromatic planes (RGB) produces, as expected, better results in giving contour details, therefore we preferred to operate separately on the three chromatic image planes and collect the application results in one piece of Boolean information. The rail edge points obtained by Canny algorithm, denoted with $\{C\}$, are illustrated in the binary image of Fig. 4, which is an enlargement of a part of the original image (cf. Fig. 3) For each contour point $\{C\}$ some clearer pixels which do not belong to rail microwrinkles can be detected near its edge. For every chromatic plane of the analyzed image, a median filter is applied by following this relation:

(2)

where *template B*, in this specific case, has a definite dimension [3x3] and a coefficient equal to (1/9).

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[†]"p" is plane index: p=1 Red plane, p=2 Green plane, p=3 Blue plane

Relation (2) represents the pixel mean of the neighboring eight values. The implemented procedure iteratively applies the previous filter so as to spread the numerical values of all the pixels which certainly belong to a colorimetrically homogeneous region, located at either the background or rail. Therefore the idea is very simple: the image at time t (iteration step) derives from the initial image convolved with the median filter (2), or:

$$A(i,j,t) = A_0(i,j) \times M(i,j,t) \tag{4}$$

where (i,j) are the pixel position indices within the original matrix A and "x" represents the convolution operator. Moreover, since the expanded mean filter (4) tends to remove the information on the edge details, this effect should be mitigated by applying another operator which, instead, emphasizes the rail edge.

In light of the above, downstream from the previous convolution (4), an edge extraction operator called *range operator* was applied [11, 12]. For each deviation (i,j) from template B, the value of the central pixel can therefore be formalized as follows:

$$R(i,j) = Max (A_{i-1,j-1}; A_{i-1,j}; A_{i-1,j+1}; A_{i,j-1}; A_{i,j}; A_{i,j+1}; ...; A_{i+1,j+1} - Min(A_{i-1,j-1}; A_{i-1,j+1}; A_{i,j-1}; A_{i,j}; A_{i,j+1}; ...; A_{i+1,j+1})$$
(5)

To this end the range values of every [3x3] boundary of all the pixels belonging to the original image A have been sought and highlighted. The following equation (6) formalizes the previous difference operation. Therefore, given a generic iteration step **t**, the suggested algorithm is able to lower the pixel intensities which mark the rail edge of the plane section.

$$Min(A_{i-1,j-1}; A_{i-1,j}; A_{i-1,j+1}; A_{i,j-1}; A_{i,j}; A_{i,j+1}; \dots; A_{i+1,j+1})$$
(6)

It can easily be noticed that, with regard to any direction taken along the rail edge, while relation (4) tends to make numerically uniform the pixel value on the point edge under consideration, relation (5) on the same boundary lowers the values in the darkest regions and therefore colorimetrically near the rail.

Then we detected some uncertainty areas along the point edges where the profile in the eight directions marked a rough variation or, in any case, a skip over a precise threshold level, localized by three constants [Ti, To, Ts]. Such constants are automatically determined by the algorithm in relation to the maximum, minimum and mean deviation values of the two profiles. In these areas, for each iterative step t the pixel values fill in the matrixes $\{Si\}$ and $\{Gi\}$, well distinct from the matrixes $\{S\}$ and $\{G\}$ which instead are almost certainly background and rail. Therefore, at the iterative step t we have:

S(i, j, t) = J(i, j, t, Ti)	(7)
Si(i, j, t) = J(i, j, t, Ti, To)	(8)
Gi(i,j,t) = J(i,j,t,To,Ts)	(9)
G(i, j, t) = J(i, j, t, Ts)	(10)

The suggested algorithm is able to define the matrix CF(i,j) of the final edge, which is formalized by the following relation:

$$CF(i,j,t) = F(S(i,j,t), Si(i,j,t), Gi(i,j,t), G(i,j,t))$$
(11)

where F is the function which formalizes the belonging of the pixel to the rail boundary or to the background. Its superimposition on the original image is illustrated in Figure 7.



Fig. 4. Binary image

Fig. 5. Final result of the algorithm suggested

Fg. 6. Binary encoding of the previous rail part

It should be underlined that, downstream from the previous thresholding operations (cf. eq. (10)), the procedure is also able to extrapolate not only the exact contour position (cf. ef. (11)), but also a first object-based binary encoding which is formalized as follows:

$$G(i,j,t) = J(i,j,t,Ts)$$
⁽¹²⁾

The result which can be obtained by applying the previous relation to the rail part in Fig.1, is illustrated in Fig. 4. This binary encoding is properly refined on the basis of some binary morphology operations. In fact, by carefully examining Figure 4 we note that this binary selection has inside some cavities which do not allow to create a *binary large object* or *blob* constituted by close and connected pixels; therefore it requires the application of some mathematical morphology operations [13] which allow to modify the original information and to obtain the matrix BW illustrated in Fig. 7 with regard to the whole rail image, which clearly shows a complete connectivity between neighboring pixels.



Fig. 7. Morphological Closing Operations for the rail under examination

Fig. 8. Detection of the rail head auxiliary edge

3. Assessment Of Geometric Reference Features

For the purpose of this research, we further measured some geometrical sizes which characterize the binary object shape previously defined. The most widespread method to encode a binary object edge, originally developed by Freeman [14], is commonly known as *chaincode* and consists in storing a list of points (without any color but only position information). Once determined the coordinates of a point in the object border (generally at the highest and the leftmost position), the successive point is detected only by following the direction which

connects pixel barycentres [15]. Therefore, once detected the blob (binary large object) and its contour coordinates, it is simple to calculate the centroid (M) representing the center of mass (center of gravity). We then could determine the centroid position (xoj, yoj) of the worn-out rail and its contour coordinates, by means of Freeman's algorithm developed on the result formalized by relations (11) and (12) after carrying out, as said above, the proper morphological closing operations (cf. Fig.7). These coordinates are properly recorded in the vector WR (worn-out rail) of dimension [n x 2], where n is the Cartesian axis number of the edge. The algorithm then adds the profile coordinates of the unworn rail (in this case UIC 60 rail have been taken into consideration) and carries them to the same image scale previously determined.

These coordinates are properly recorded in a vector *IR* (*intact rail*) of dimension [kx2] where k represents the number of the discrete axes denoting the contour of the intact rail. In order to get the deviation between the profiles of the worn-out and unworn rails, an auxiliary profile has been developed by reducing the previous *IR* by a constant term equal to 1.3 (Rg), thus obtaining a perfectly homothetic boundary to the profile with the coordinates in the vector *IR* (cf. Fig. 7). The distances between the two profiles have been determined by the intercepts of the straight lines from the centroid of the profile *IR*, with regard to this last boundary Rg, whose domain is obviously perfectly parallel to the previous one. The procedure allows to get the deviation between the two compared profiles (worn-out and unworn) with regard to a 360° rotation of the straight line coming out of the rail centroid and, therefore, produces output information on the wear condition of the whole rail profile [5, 6]. Figures 9 and 10 show the final result yielded by the application of the algorithm suggested. The following diagrams illustrates the trend of the deformation of a UIC 60 rail profile properly examined in laboratory, with regard to the part of the rail head located at an angle " θ " between 20° and 160°. Obviously, it is also possible to work out the values of vertical, horizontal and 45° wear, as required, for instance in Italy, by the Italian Railway Network [16].



Fig. 9. Rail wear diagram ($\theta = 20^{\circ}$ - 70°) Fig. 10. Rail wear diagram ($\theta = 110^{\circ}$ - 160°)

4. Image processing for railways track profile measurement (stereoscopy)

Stereoscopy is based on the analysis of images taken by two cameras located at a certain distance from each other [17, 18, 19, 20]: so, the same scene produces two slightly different images, in which the same objects can show light relevant deviations, as schematized in Figure 11 (the cameras are separated by a horizontal base, the so-called *baseline*).

In order to simplify the elaborations, it is certainly advisable to endow both the cameras with lens having the same focal length, and sensors having equally sized pixels.

Moreover, since the image employed in this application does not contain objects in motion, it is not required to synchronize the capture of the pair of cameras, which is vice versa necessary in stereo *real-time* applications where objects in motion should be tracked in the scene.

A crucial parameter is the *baseline*, i.e. the distance between the cameras, which can be fixed or variable. This value influences the field of application; for instance, larger *baselines* allow a better distance resolution. As a matter of fact, since the distance resolution is equal to the minimum distance which can be distinguished by the stereo system, the stereo algorithm is nothing but a triangulation procedure; so this resolution is worsened by the distance between the cameras. Therefore, a better resolution allows to highlight position differences more clearly when the objects are far from the cameras.

The images acquired by the stereo vision system have slightly different viewpoints; the depth can be obtained by using the different position of the objects in the two images.

If we consider a point P as belonging to the scene, we clearly see it in two different positions I_1 and I_2 on the two right and left images. If u_1 and u_2 denote the distances between these positions and the optical axes of the cameras, then the difference $u_1 - u_2$ represents the disparity (see Fig. 12 and 13).



Fig. 11. Rail image taken from the two cameras (red and blue images)

If we make each pixel of the left image correspond to one of the image on the right, we obtain the disparity image [21, 22] including the depth information extracted. Since the cameras cover different areas of the scene, the disparity image will include only the information in the area which gathers the data derived from both the cameras.

Therefore, apart from the areas uncovered by either image, the disparity could not be determined in other parts of the scene. In general, therefore, the disparity image determined in real contexts does not include data on all the points which can be seen by the two cameras.

For this application the object, whose third dimension should be investigated, needs to be reproduced, so that the superimposition area is larger where the depth is to be extracted.



Fig. 12. The projections I_1 and I_2 of a point P on the two images



Fig. 13. Rail "disparity" image



Fig. 14. References to the 3D space and images

4.1. The Correspondences

In producing the disparity image [21, 22] the first problem to solve is the correspondence, that is the search for the projection of the same physical point in the two images (*matching-point technique*). This problem is dealt with global or local methods. By means of local methods one image is analyzed to find the correspondence with a small region coming from the other image. This analysis is carried out by employing such features as angles or rectilinear line segments (in *feature-based methods*), or by means of correlation operators (in *area-based methods*). Global methods complete local methods with such general information as the continuity of the surfaces or the presence of particular *textures* on the scene. Each methods, for instance, are more suitable for interiors of buildings, where the space has lots of rectilinear surfaces, while *area-based* techniques are applicable to a broader range of situations. The fast evaluation of disparities is a hard task. The major problems which can lead to the incorrect relationship between two non-corresponding points are caused by:

- occlusions: cameras are located in different positions, therefore it is possible for some objects to be partially visible or to be seen only in either image;
- distortion: owing to the perspective projection, the same object can be differently projected onto the two images;
- *different parameters of the two cameras:* if either camera is out of focus at the same distance as the other, or if it has a different opening of the diaphragm, the corresponding points have different characteristics in the two images;
- specular reflections;
- sensor noise.

In the present paper we have implemented an algorithm which takes into account both the continuity and colorimetrically uniform texture of the rail surface and searches, by mutual correlation, for the correspondences between the left and right images through a window of constant dimensions equal to 11 rows and 11 columns.

4.2. The Calibration

In an ideal space the cameras of a stereo head answer the *pinhole* model, have exactly the same focal length and parallel optical axes. In the real world, unfortunately, lenses introduce some distortions, can have different focal lengths and misaligned optical axes. Calibration [18, 19, 23] aims at establishing two sets of intrinsic and extrinsic parameters, which are able to compensate for the imperfection of the stereo head. Intrinsic parameters adjust lens distortions and the difference in focal length, while the extrinsic ones determine the spatial offset of the two cameras, including the distance between them and the deviation from the parallelism of optical axes. By means of these parameters it is possible to convert the acquired images into *ideal* images, just as those seen by *pinhole* cameras with parallel optical axes.

4.3. Projection And Reprojection

If calibration parameters are known, it is possible to carry out a more detailed analysis of the operations which allow to move from a three-dimensional scene to right and left images and from a disparity image to a 3D reconstruction [24]. The projection matrix P converts 3D coordinates into ideal image coordinates. The reference systems are chosen so as to make the calculations simpler; they are illustrated in Figure 15 (in general, reference systems for 3D space and images are selected so as to have the X-axis parallel to the u-axis and the Y-axis parallel to the v axis. (The Z-axis is perpendicular to the images). There is a projection matrix for the left camera and one for the right one. If they are known, it is possible to project a point of coordinates $[X Y Z 1]^T$, represented in homogeneous coordinates $[X Y Z 1]^T$, into coordinates $[u v]^T$ of the image through the following matrix multiplication:

$$\begin{bmatrix} u \\ v \\ w \end{bmatrix} = P \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$
(13)

$$P = \begin{bmatrix} F_x & 0 & C_x & -F_x T_x \\ 0 & F_y & C_y & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$
(14)

In matrix P there are the values obtained by calibration procedures, especially the focal length ($F_x e F_y$, in pixel), the coordinates of the optical centre ($C_x e C_y$, in pixel), the translation with regard to the left camera (T_x , in mm, is equal to 0 for the left image matrix); the coordinates of the point in the ideal image are $[u/w v/w]^T$. Vice versa, the reprojection matrix Q allows to obtain the spatial coordinates of a point, provided that the disparity is known:

$$\begin{bmatrix} X \\ Y \\ Z \\ W \end{bmatrix} = \begin{bmatrix} u \\ v \\ d \\ 1 \end{bmatrix}$$
 (15)

$$Q = \begin{bmatrix} 1 & 0 & 0 & -C_x \\ 0 & 1 & 0 & -C_y \\ 0 & 0 & 0 & F_x \\ 0 & 0 & \frac{1}{-T_x} & \frac{C_x - C'_x}{T_x} \end{bmatrix}$$
(16)

The values in matrix Q reflect those present in matrix P for the left image, except C_x' , which is extracted by the right image matrix. The coordinates of the reprojected point are therefore equal to $[X/W Y/W Z/W]^T$. The following figures show 3D reconstruction of the UIC 60 rail under examination, which can lead to its wear measurement and to develop pictures very similar to those shown in Figures 15 and 16.



Fig. 15. 3D image



5. Conclusions

The control of the state of the rail wear is one of the key aspects to guarantee an adequate safety level of the railway system. This research has examined a new procedure based on the *image processing technique*, not for determining the rail wear. This method, based on the analyses of high resolution photo images, has required the design and implementation of specific mathematical algorithms suitable to provide the cross section geometry of a generic worn-out rail and the measurements of its relevant deviations in comparison with new rails of the same type. The study has carried out two different modes of analysis: the monoscopic (based on the use of images originated from a single camera) which can be employed only for the laboratory analyses, in that it requires photos from the rail cross section and the stereoscopic (obtained by combining two cameras) which, unlike the former, could be also used in monitoring track operations by means of diagnostic trains. The results have shown that both the procedures are marked by a reliable and rapid analytical approach as well as high precision in wear measurements.

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