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# On the Near-Field Shaping and Focusing Capability of a Radial Line Slot Array

Mauro Ettore, *Member, IEEE*, Massimiliano Casaletti, *Member, IEEE*, Guido Valerio, *Member, IEEE*, Ronan Sauleau, *Senior Member, IEEE*, Laurent Le Coq, Santi C. Pavone, *Student Member, IEEE*, and Matteo Albani, *Senior Member, IEEE*

**Abstract**—We describe the design of a radial line slot array antenna with a shaped and focused near field. The antenna is designed in such a way to control the side lobe level and beamwidth of the normal component of the electric field with respect to the radiating aperture. The design procedure consists of two steps. In the first step the requirements on the near-field pattern are provided over a focusing plane at a given distance from the radiating aperture. A set theoretic approach is then used to derive the aperture field distribution fitting the requirements over the near field. In the second step, the aperture field distribution is synthesized by accurately placing and sizing the slots of the antenna. The spillover efficiency is maximized during the design process. The antenna is centrally fed by a simple coaxial probe. The antenna design is validated by a prototype and measurements at 12.5 GHz.

**Index Terms**—Near field, focusing, radial line slot array, RLSA, near-field shaping.

## I. INTRODUCTION

**R**ADIAL line slot array (RLSA) antennas have been widely investigated in literature for far-field applications [1]-[4]. RLSAs are attractive antenna solutions thanks to their compactness, planarity and high efficiency. Such features are also extremely appealing for several near-field applications such as near-field probing, radiometry, non-invasive medical imaging, etc. [5]-[11]. The design techniques used for focusing and shaping the electromagnetic field in the near-field or Fresnel zone of an antenna stem from the seminal works in [12]-[14]. In these works, large (in terms of wavelength) and linearly-polarized apertures are considered and an equivalence between their near and far fields is derived. The considered near fields are either transversal or longitudinal to the axis of a defined focal plane parallel to the focusing aperture. In brief, it is shown that the fields in the Fresnel and far-field zones present the same properties if a quadratic phase taper

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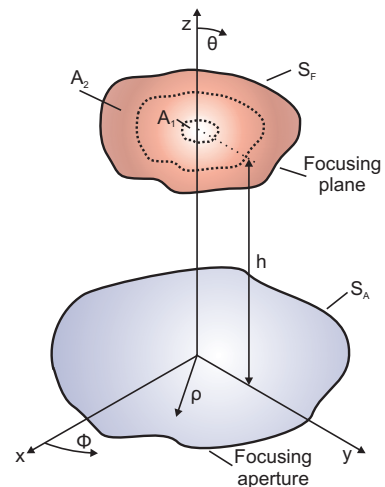


Fig. 1. Geometry of the problem with two generic surfaces defined on two parallel planes orthogonal to the  $z$ -axis. The focusing aperture  $S_A$  is located at  $z = 0$ . The focusing plane  $S_F$  is at  $z = h$ . On the focusing plane the surfaces  $A_1$  and  $A_2$  are used in the first step of the design procedure for defining the field constraints.

is imposed to the tangential field distribution of the focusing aperture. Therefore, the optimization/shaping of the fields in the Fresnel zone is generally done by using classical far-field techniques. This is strictly valid as long as the focal plane is placed at distance larger than one aperture size and generally beyond the near-field or reactive zone of an antenna. In addition, there is no control or design flexibility on the aperture and spillover efficiency, polarization and size of the system. Besides, complicated and lossy beam forming networks are used to practically implement the required aperture field distribution introducing inevitable distortions [5]-[7].

In this paper the design of a RLSA antenna focusing its main beam in the near field is proposed. A novel design procedure is adopted for shaping the electromagnetic field radiated by the antenna without any limitation on the location of the focusing plane and polarization as in previous works [5]-[11]. In particular the possibility to control and shape the normal component of the electric field radiated by the antenna is considered as in [15]-[20]. In addition, the antenna is centrally fed by a coaxial probe avoiding lossy and cumbersome feeding networks [6], [7], [17]. The design methodology is divided in two main steps: (1) derivation of the aperture field generating the required focal pattern; (2) automatic design of the RLSA with the required aperture field distribution.

In the first step, the required pattern or field distribution is provided based on the particular application or needs. Here, we consider the possibility to control the side lobe level and beamwidth of the normal component of the electric field of the focused beam within the near field of the structure. A set theoretic approach and alternate projection method [21] is used to derive the aperture field distribution generating the required pattern.

In the second step and in contrast to previous works [5]-[11], the optimization tool is linked to an in-house Method of Moment (MoM) [22]-[27] for deriving the RLSA structure having the required aperture profile. The automatic design and optimization scheme proposed in [4] is generalized for near-field applications. The required aperture field is achieved by properly designing the slot dimensions and locations across the radiating aperture. Finally, a prototype has been manufactured and tested at the operating frequency of  $f_0 = 12.5$  GHz

The paper is organized as follows. Sec. II introduces the first step of the design procedure where the required aperture field distribution of the near-field focusing antenna is derived. In Sec. III, the second step of the design procedure is presented together with the RLSA geometry. The complete tool is used in Sec. IV for designing a prototype able to focus its main beam at a distance equal to half the antenna size. Details on the convergence, accuracy of the design and coaxial feeding transition are also provided. The prototype is validated by near-field measurements of the normal component of the electric field at different frequencies and at various planes parallel to the antenna aperture. Finally, conclusions are drawn in Sec. V.

## II. DERIVATION OF THE APERTURE FIELD DISTRIBUTION

The geometry of the problem is shown in Fig. 1. An aperture of size  $S_A$  is located at  $z = 0$  and is radiating in free space. The required pattern is defined over a focusing plane ( $S_F$ ) located at a distance  $z = h$  and parallel to the radiating aperture. In the following discussion, transverse magnetic (TM) modes with respect to the  $z$ -direction will only be considered [15], [16]. However, the proposed procedure can be extended to transverse electric (TE) modes or any combination of modes.

The goal of any synthesis procedure is to derive the aperture field distribution that generates the required pattern. A priori, such a pattern may also not be a physical solution of the problem at hand. The technique adopted here is based on a set theoretic approach and alternate projection method [21]. In these approaches, each requirement or relevant information (fabrication tolerances, synthesis error, etc.) is expressed as a set of constraints for the possible solution. The solution of the problem will belong to the intersection of all these sets of constraints or will be the closest one, according to a provided measure criterion. Circularly- and linearly-polarized fields can be considered as well as single components of the field. In the present case we will focus our attention on the possibility to control the beamwidth and sidelobe level of the  $z$ -component of electric field ( $E_z$ ) in the focusing plane (see Fig. 1). In addition  $\phi$  invariance is assumed for the radiated field. The requirements define a mask for the near field in the focusing

plane as:

$$\text{Mask} = \begin{cases} \frac{|E_z(x,y,h)|}{\max(|E_z(x,y,h)|)} > c_1 & \text{in } A_1, \\ \frac{|E_z(x,y,h)|}{\max(|E_z(x,y,h)|)} < c_2 & \text{in } A_2, \end{cases} \quad (1)$$

where  $0 < c_2 < c_1 < 1$  are fixed limits for the normalized module of  $E_z$  in some space domains  $A_1$  and  $A_2$  over the focusing plane, respectively (see Fig. 1). The function  $\max(|E_z|)$  indicates the maximum value of the  $z$ -component of the electric field in the focusing plane. For clarity, in the following the normalized  $E_z$  component of the electric field in the focusing plane is indicated as:

$$\overline{E}_z(x, y, h) = \frac{E_z(x, y, h)}{\max(|E_z(x, y, h)|)}. \quad (2)$$

Note that the mask also defines a reference solution Ref equal to  $c_1$  and  $c_2$  in the two domains  $A_1$  and  $A_2$ , respectively. The size of the focusing aperture ( $S_A$ ) is another constraint of the optimization procedure.

Once the constraints of the problem are defined, an iterative procedure based on an alternative projection method is used to derive the aperture field distribution [21]. To this end an arbitrary complex field distribution  $E_z$  is defined at beginning over the focusing aperture:  $E_z^{(n)}(x, y, 0)$ . The apex  $n$  indicates the iteration step of the procedure. The field is defined only over the surface  $S_A$  and it is assumed zero outside this region. A uniform field distribution may be assumed as guess distribution (step  $n = 1$ ). The Fourier transform (FT) of the aperture field distribution is then derived:

$$\widetilde{E}_z^{(n)}(k_x, k_y, 0) = \iint_{S_A} E_z^{(n)}(x, y, 0) e^{j(k_x x + k_y y)} dx dy, \quad (3)$$

with  $k_x$  and  $k_y$  the spectral frequencies extending over the entire frequency spectrum ( $-\infty < k_x, k_y < +\infty$ ). The electric field  $E_z(x, y, h)$  over the focusing plane can be calculated as [28]:

$$E_z^{(n)}(x, y, h) = \frac{1}{4\pi^2} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \widetilde{E}_z^{(n)}(k_x, k_y, 0) e^{-jk_z h} \times e^{-j(k_x x + k_y y)} dk_x dk_y, \quad (4)$$

with  $k_z = \sqrt{k^2 - k_x^2 - k_y^2}$  and  $k$  the propagation constant in free space. Therefore, for the next step ( $n + 1$ ), the module of the derived electric field is modified accordingly to the defined mask as:

$$|E_z^{(n+1)}(x, y, h)| = \begin{cases} c_1 \max(|E_z^{(n)}|) & \text{if } |\overline{E}_z^{(n)}| < c_1 \text{ in } A_1, \\ c_2 \max(|E_z^{(n)}|) & \text{if } |\overline{E}_z^{(n)}| > c_2 \text{ in } A_2. \end{cases} \quad (5)$$

Note that the phase of the electric field is not modified. In addition, at each iteration  $n$  the squared error of the field distribution is derived over the focusing plane  $S_F$  as:

$$\Delta_F^{(n)} = \iint_{S_F} \left| \frac{|E_z^{(n)}(x, y, h)|}{\max(|E_z^{(n)}(x, y, h)|)} - \text{Ref} \right|^2. \quad (6)$$

The FT of the electric field over the focusing plane  $S_F$  is then evaluated as in Eq.(3) and indicated as  $\widetilde{E}_z^{(n+1)}(k_x, k_y, h)$ . The

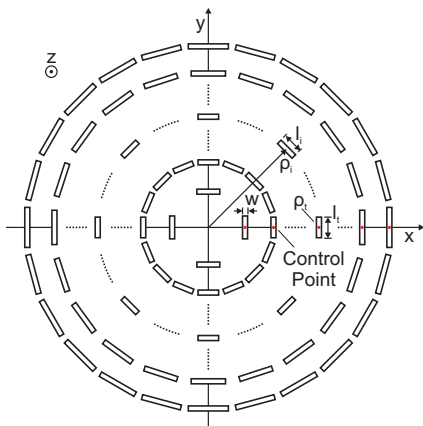


Fig. 2. Geometry of the RLSA (top view). The slots on each ring have the same length ( $l_s$ ). The width of the slots ( $w$ ) is constant. The slots are uniformly distributed over the rings along  $\phi$ . The generic control point (red dot) of the optimization procedure is indicated by the index  $t$ .

integration is limited to the physical size of the focusing plane  $S_F$ . The novel aperture field is obtained:

$$E_z^{(n+1)}(x, y, 0) = \frac{1}{4\pi^2} \iint_{k_x^2 + k_y^2 \leq k^2} \widetilde{E}_z^{(n+1)}(k_x, k_y, h) e^{jk_z h} \times e^{-j(k_x x + k_y y)} dk_x dk_y, \quad (7)$$

where the integral has been limited to the visible spectrum avoiding super-oscillating aperture distributions [29]. The procedure is repeated until  $E_z$  lays within the imposed requirements in the focusing plane or the squared error  $\Delta_F$  is lower than a certain threshold. It is worth saying that the FTs in Eqs. (4), (7) have been evaluated with a Fast Fourier Transform (FFT) algorithm speeding up their computation and the overall time convergence of the design procedure.

The present procedure provides the  $z$ -component of electric field  $E_z$  over the focusing aperture [15]-[16]. However, in the next step the tangential electric field distribution is required for designing the RLSA. Thanks to the  $\phi$  invariance of the radiated field, the  $\rho$ -component of the tangential electric field is given by:

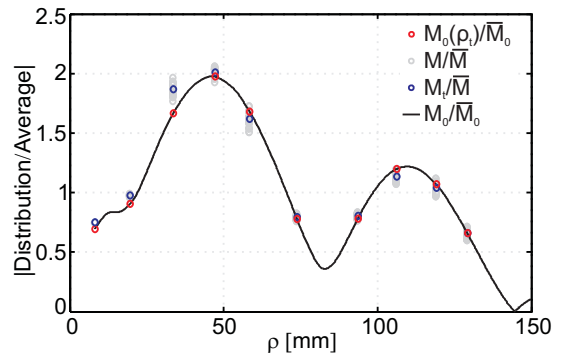
$$E_\rho(x, y, 0) = \frac{1}{4\pi^2} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \frac{k_z}{k_\rho} \widetilde{E}_z(k_x, k_y, 0) \times e^{-j(k_x x + k_y y)} dk_x dk_y, \quad (8)$$

with  $k_\rho = \sqrt{k_x^2 + k_y^2}$ .

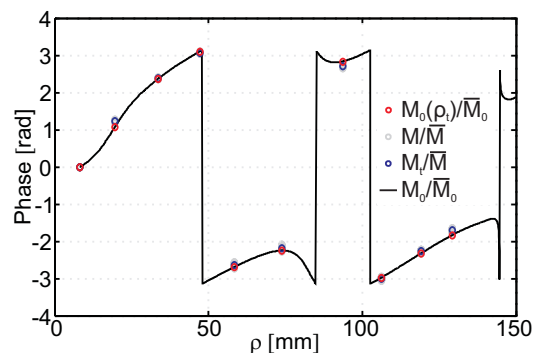
Finally, the scalar procedure presented here can be easily extended to a more general vector approach. In addition, the procedure can be directly applied to the tangential components of the electric field in place of the vertical one.

### III. SYNTHESIS OF THE APERTURE FIELD DISTRIBUTION

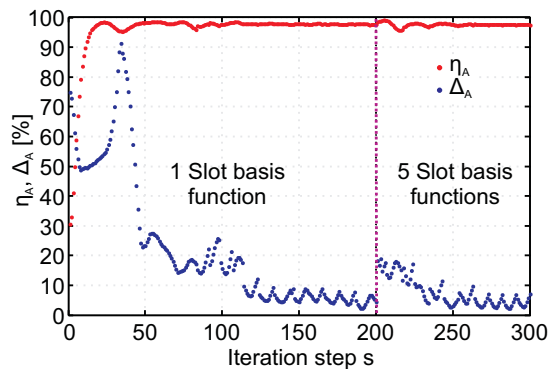
The design of the RLSA structure follows the same steps outlined in [4]. The derived aperture field distribution in Eq.(8) corresponds to an equivalent aperture magnetic current distribution:  $\mathbf{M}_0(\rho) = M_0(\rho)\hat{\phi} = -E_\rho(\rho)\hat{\phi}$ . Note that the current distribution is oriented along  $\phi$  and is a function only of  $\rho$  due to the  $\phi$ -invariance of the assumed TM modes in



(a)



(b)



(c)

Fig. 3. (color) Ideal and synthesized magnetic dipole moment distribution provided by the two steps of the design procedure for the final RLSA antenna: (a) magnitude; (b) phase. (c) Spillover efficiency ( $\eta_A$ ) and average aperture distribution error ( $\Delta_A$ ) vs. iteration step ( $s$ ) with a different number of entire domain basis functions for the analysis of the RLSA with the MoM code.

the first step of the design process. The current distribution is synthesized by using the slots of the RLSA.

Each slot is equivalent to a magnetic dipole oriented along the slot length. The dipole moment is proportional to the feeding mode (outwards cylindrical wave) within the parallel plate waveguide (PPW) of the RLSA antenna and function of the position and size of the corresponding slot. The slots, and

TABLE I  
POSITION AND DIMENSIONS (in mm) OF THE SLOTS IN EACH RING OF THE RLSA

Ring number	1	2	3	4	5	6	7	8	9	10
Length	5.23	5.9	8.08	7.35	8.3	7.89	7.28	8.33	8.68	10.19
$\rho_t$	8.15	19.54	33.61	47.13	58.38	73.80	93.57	106.16	119.05	129.20

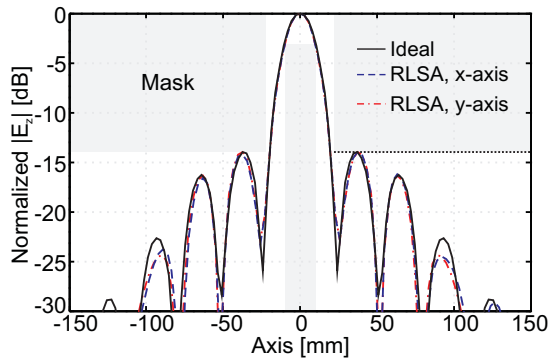


Fig. 4. (color) Normalized  $E_z$  component of the electric field in the focusing plane ( $z = 150$  mm) radiated by: ideal aperture field distribution (solid line); synthesised RLSA (blue dashed line along the  $x$ -axis, red dash-dotted line along the  $y$ -axis). The reference mask is also provided for comparison.

as a consequence their equivalent magnetic dipoles, must be oriented in the same direction as the current distribution ( $\mathbf{M}_0$ ) for its synthesis [4].

The resulting geometry of the RLSA antenna is shown in Fig. 2 (top view). The slots are placed in the upper plate of a PPW structure filled by a dielectric with permittivity  $\epsilon_r$  [1], [2]. Slots of same length ( $l_i$ ) are uniformly spaced in each ring and oriented along  $\phi$  thanks to  $\phi$ -invariance of the assumed current distribution. It is worth saying that the mutual coupling between each slot of any ring and the surrounding slots may be different and may induce small asymmetries in the radiated field. The width of the slots is constant.

For each slot of the RLSA the equivalent magnetic dipole moment  $\mathbf{M}(\rho_i) = M(\rho_i)\hat{\phi}$  is derived with an in-house MoM [22], [23]. The position ( $\rho_t$ ) and length ( $l_t$ ) of one representative slot per ring (control point in Fig. 2) is adjusted for synthesising the derived aperture magnetic current distribution  $\mathbf{M}_0$ . This is possible thanks to the assumption of equal slots in each ring of the RLSA. In other words the magnetic dipole moment is averaged over each ring, yielding:

$$M_t(\rho_t) = \frac{1}{N_t} \sum_{i=1}^{N_t} M(\rho_i), \quad (9)$$

where  $N_t$  is the number of slot on ring  $t$ . For each slot or control point (see Fig. 2) a complex fitness function is defined:

$$F_t = \frac{M_t(\rho_t) \overline{M_0}}{M_0(\rho_t) \overline{M}}, \quad (10)$$

where  $\overline{M} = \sum_{t=1}^{N_{ring}} |M_t(\rho_t)| N_t / N_{slot}$  and  $\overline{M_0} = \sum_{t=1}^{N_{ring}} |M_0(\rho_t)| N_t / N_{slot}$  are the realized and target average magnetic dipole moment amplitude, with  $N_{slot}$  and  $N_{ring}$  the total number of slots and rings. The phase ( $\angle F_t$ ) and amplitude ( $|F_t|$ ) of the fitness function represent the error between the target and actual magnetic dipole moment distribution over the

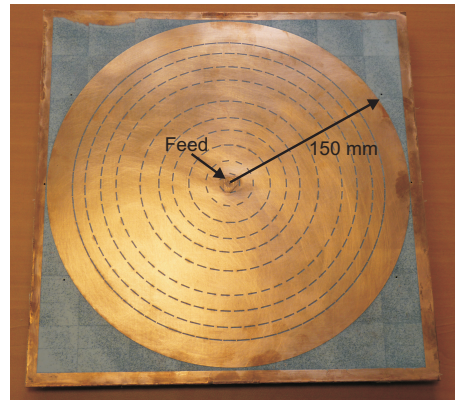


Fig. 5. Final prototype. The slots have been etched by laser ablation.

TABLE II  
GEOMETRICAL DIMENSIONS (in mm) FOR THE COAXIAL TRANSITION OF THE PROTOTYPE

$D_1$	$D_2$	$D_3$	$h_1$	$h_d$
1.28	2.34	7.68	1.58	3.175

aperture. The fitness function is used to modify the position ( $\rho_t$ ) and length of the slots ( $l_s$ ) within an optimization loop. At each iteration ( $s$ ) of the optimization process, the in-house MoM is used to evaluate the slots' magnetic dipole moment distribution. The fitting function  $F_t^{(s)}$  is then derived. In addition, the spillover efficiency of the antenna is also calculated:

$$\eta_A^{(s)} = \frac{P_{acc} - P_{res}}{P_{acc}}, \quad (11)$$

with  $P_{acc}$  and  $P_{res}$  the power accepted by the antenna and the residual power trapped in the PPW, respectively. The spillover efficiency is maximized during the optimization. The position and length of the slots are updated accordingly as:

$$\rho_t^{(s+1)} = \rho_t^{(s)} + \xi_p \angle F_t^{(s)} / k_d, \quad (12)$$

$$l_t^{(s+1)} = l_t^{(s)} + \xi_q (1 - |F_t^{(s)}| \sqrt{\eta_A^{(s)}}) l_t^{(s)}, \quad (13)$$

where  $k_d = k \sqrt{\epsilon_r}$  is the wavenumber in the dielectric filling the PPW, and  $0 < \xi_p, \xi_q < 1$  are damping factors used in the optimization loop [4]. Note that the number of slots in each ring ( $N_t$ ) is calculated as:

$$N_t^{(s+1)} = \left\lfloor \frac{2\pi \rho_t^{(s+1)}}{l_{max}} \right\rfloor, \quad (14)$$

where  $l_{max}$  is the upper limit for the slot length which is set to the resonant slot length [4]. The notation  $\lfloor \cdot \rfloor$  indicates the floor function. The convergence criteria of the optimization loop are based on the spillover efficiency, and the average

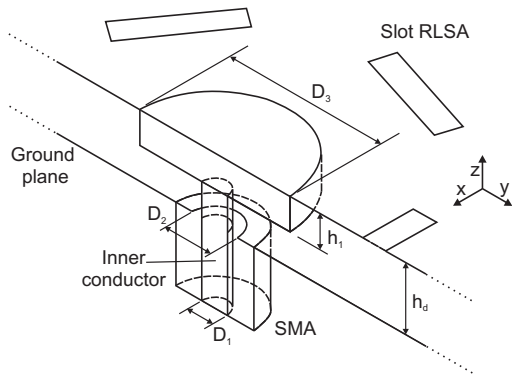


Fig. 6. Coaxial transition. The metallic disc of diameter  $D_3$  and thickness  $h_1$  is inserted in the substrate of the RLSA structure and attached to the inner conductor of the SMA connector. The SMA connector is placed on the back side of the antenna.

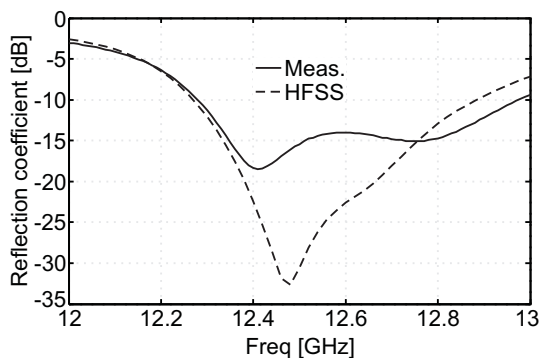


Fig. 7. Simulated and measured input reflection coefficient. The simulation results have been obtained by the general purpose software HFSS [30].

aperture distribution error given by:

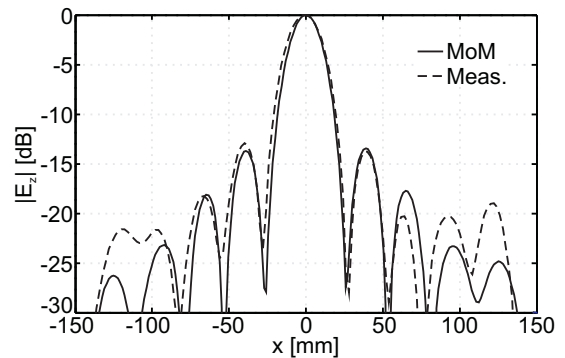
$$\Delta_A = \frac{1}{N_{slot}} \sum_{t=1}^{N_{ring}} \left| \frac{M_t(\rho_t)}{M} - \frac{M_0(\rho_t)}{M_0} \right| N_t. \quad (15)$$

Note that the proposed optimization loop adopts a projection method as in the first step of the design procedure [21]. In addition, the procedure proposed in this section can be extended to more general configurations with different slot patterns for the RLSA structure, as shown in [4] for far-field applications using RLSA antennas as those in [1]-[3].

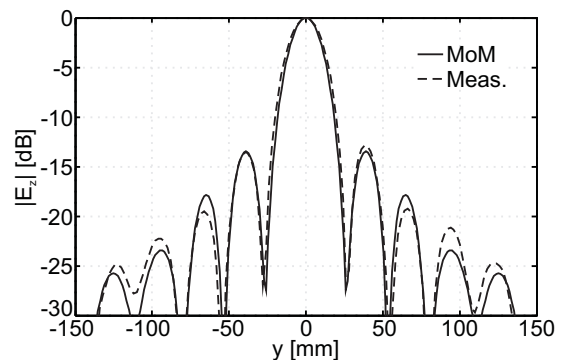
#### IV. PROTOTYPE AND EXPERIMENTAL RESULTS

The procedure presented in the previous sections is used to design a RLSA with a shaped  $z$ -component of the electric field ( $E_z$ ) (see Fig. 1). The operating frequency is chosen equal to  $f_0 = 12.5$  GHz. The physical constraints for the first step of the design procedure in Sec. II are:  $S_A < 300$  mm<sup>2</sup>;  $h = 150$  mm. The antenna focuses  $E_z$  at a distance equal to half the antenna size. In addition the following mask is imposed on the normalized  $E_z$  profile over the focusing plane in terms of side lobe level (SLL) and beamwidth:

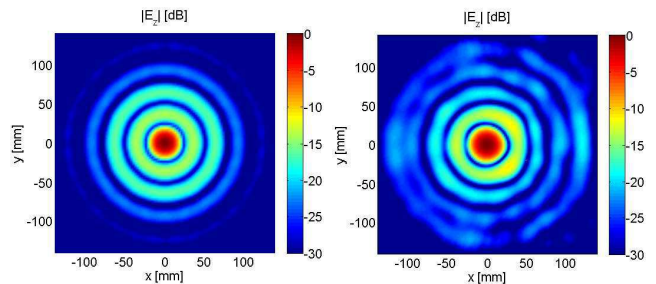
$$\text{Mask} = \begin{cases} \frac{|E_z|}{\max(|E_z|)} > -3 \text{ dB} & \text{for } \rho < 10 \text{ mm,} \\ \frac{|E_z|}{\max(|E_z|)} < -14 \text{ dB} & \text{for } \rho > 20 \text{ mm.} \end{cases} \quad (16)$$



(a)



(b)



(c)

(d)

Fig. 8. (color) Normalized  $E_z$  component of the electric field at  $f_0$  on the focusing plane. (a) Comparison between measured and MoM results along the  $x$ -axis. (b) Comparison between measured and MoM results along the  $y$ -axis. (c) 2D MoM electric field plot. (d) 2D measured electric field plot.

Note that this mask is chosen as an example. However, other requirements may be defined based on the considered target application.

For the second step (Sec. III), the convergence criteria are the followings:  $\eta_A > 95\%$ ;  $\Delta_A < 3\%$ . The RLSA antenna is made by a PPW of height  $h_d = 3.175$  mm and filled by a dielectric with permittivity  $\epsilon_r = 2.17$ . The final positions and lengths of the slots are given in Table I. The diameter of the antenna is smaller than 300 mm. The final RLSA structure has a spillover efficiency and average aperture distribution error

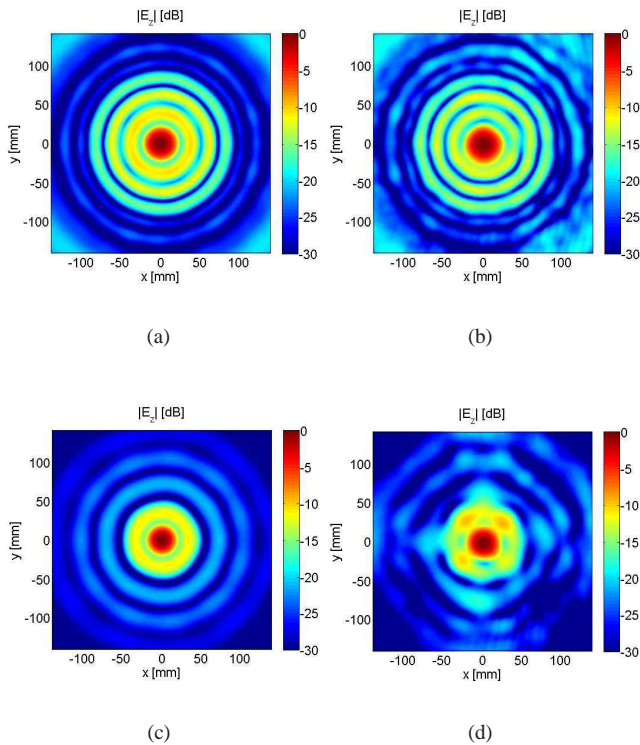


Fig. 9. (color) Normalized  $E_z$  component of the electric field at  $f_0$  on two different planes parallel to the RLSA aperture. (a) 2D MoM electric field plot at  $z = 100$  mm. (b) 2D measured electric field plot at  $z = 100$  mm. (c) 2D MoM electric field plot at  $z = 200$  mm. (d) 2D measured electric field plot at  $z = 200$  mm.

of 97.8% and 2.2%, respectively. The ideal and synthesized magnetic dipole moment distribution are shown and compared in Fig. 3 in amplitude and phase. The blue and grey circles indicate the averaged magnetic dipole moment at the control point ( $M_t/\overline{M}$ ) and at each slot in the rings of the RLSA ( $M/\overline{M}$ ), respectively. The black line is the ideal averaged magnetic current distribution over the aperture provided by Eq.(8) ( $M_0/\overline{M}_0$ ). The red circles are the samples of this distribution at the location of the control point  $\rho_t$  in each ring ( $M_0(\rho_t)/\overline{M}_0$ ). A good agreement can be appreciated between the ideal profile (black curve and red circles) and the real one (blue circles) of the RLSA antenna. In some cases, a small variation in absolute value can be noticed between the slots' magnetic dipole moment of a particular ring (grey circles in Fig. 3 (a)) and their average distribution (blue circles in Fig. 3 (a)). This is due to the different mutual coupling between each slot of each ring and the surrounding slots of the RLSA structure.

The variation of the spillover efficiency ( $\eta_A$ ) and average aperture distribution error ( $\Delta_A$ ) with respect to the iteration step ( $s$ ) is shown in Fig. 3. It can be noticed that  $\eta_A$  converges faster than  $\Delta_A$  to acceptable values. Fig. 3 also shows the effect of using a different number of entire domain basis functions in the MoM code for the analysis of the RLSA. In particular, 1 basis function is used at the beginning of Step 2 of the design procedure to speed up the optimization process. Once a solution is reached, the number of basis functions is

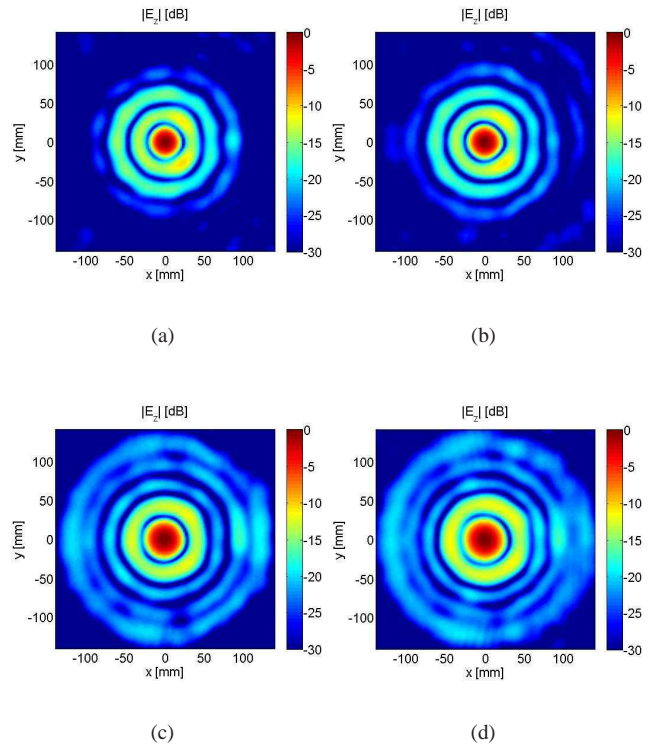


Fig. 10. (color) Normalized 2D measured  $E_z$  component of the electric field on the focusing plane at various frequencies. (a)  $f = 12.3$  GHz. (b)  $f = 12.4$  GHz. (c)  $f = 12.6$  GHz. (d)  $f = 12.7$  GHz.

increased to 5 for a higher accuracy of the MoM analysis and final results. This approach is possible thanks to the extreme efficiency in computational time of the in-house MoM [22], [23]. Note that the final RLSA has 400 slots.

The normalized  $E_z$  component of the electric field radiated by the RLSA along the  $x$ - and  $y$ -axis on the focusing plane is shown in Fig. 4. The field radiated by the derived ideal aperture field distribution in Eq.(8) is also shown for comparison. A small difference can be noticed in the lobes lower than  $-20$  dB but in all cases the patterns are within the imposed mask. Besides, the field radiated by the RLSA antenna have a good  $\phi$  invariance.

A prototype of the RLSA has been manufactured and tested at IETR. The prototype is shown in Fig. 5. The slots of the RLSA are etched by laser ablation on the upper face of a double grounded Neltec NY9217 substrate with permittivity  $\epsilon_r = 2.17$  and thickness  $h_d = 3.175$  mm. The prototype is centrally fed by a coaxial probe attached on the back side of the prototype to a SMA connector. The coaxial transition shown in Fig. 6 is used to match the antenna to the 50 Ohm SMA connector. The transition is made by a metallic disc of diameter  $D_3$  and thickness  $h_1$  connected to the inner conductor of the SMA connector. The final dimensions for the coaxial transition are provided in Table II. The symbols refer to Fig. 6. The simulated and measured reflection coefficients are plotted in Fig. 7, and show good agreement.

The  $E_z$  component of the electric field was measured above the prototype using a short electric probe attached to

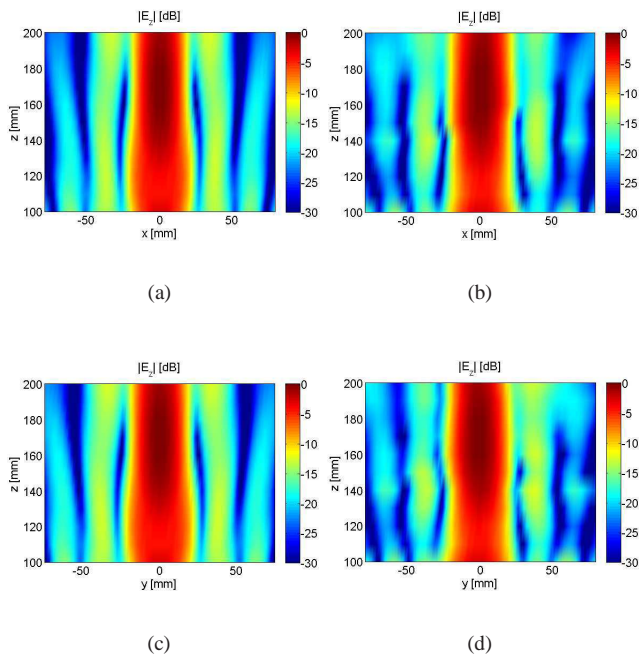


Fig. 11. (color) Normalized  $E_z$  component of the electric field at the operating frequency. (a) 2D MoM electric field plot along the  $xz$ -plane. (b) 2D measured electric field plot along the  $xz$ -plane. (c) 2D MoM electric field plot along the  $yz$ -plane. (d) 2D measured electric field plot along the  $yz$ -plane.

an automatically controlled 2D translation stage. The short electric probe is made out of a semi-rigid coaxial cable (UT-85) by removing the external conductor and dielectric insulator. The inner conductor extends for a length of 2.5 mm (about  $\lambda/10$  with  $\lambda$  the free space wavelength at the operating frequency) beyond the outer conducting shield. The near field was measured over an area of  $150 \times 150 \text{ mm}^2$  with a step of 2 mm at different distances from the RLSA structure. The normalized  $E_z$  component at the operating frequency  $f_0$  along the  $x$ - and  $y$ -axis is shown in Fig. 8 (a) and (b), respectively. Good agreement is achieved between the measured and simulated results. This is also evident in the 2D plots of the fields in Fig. 8 (c) and (d). A good circular symmetry of the pattern can be appreciated. However small discrepancies between measured and simulated results can be noticed for side lobes lower than  $-15 \text{ dB}$  at the edge of the measured space. Such discrepancies may be attributed to the fabrication tolerances related to the etching process used for the slots of the RLSA structure.

To further validated the design, 2D plots of the normalized electric field are provided in Fig. 9 at difference distances from the RLSA:  $z = 100 \text{ mm}$ ;  $z = 200 \text{ mm}$ . Once again, a close agreement is observed between the simulated and measured results even outside the focusing plane. The variation of the measured field within the band 12.3-12.7 GHz is shown in Fig. 10. It can be noticed that the field pattern is preserved within the considered band. For brevity, only the measurement results are provided. However also for these cases there was a good agreement with the simulated ones.

Finally, Fig. 11 provides the 2D plot of the normalized  $E_z$  along the  $xz$ - and  $yz$ -plane. The field was measured with a step of 10 mm in  $z$ . At the time of the measurements the near-field scanner did not have a translation stage for the  $z$ -axis. Therefore, the probe was manually adjusted along  $z$ . For this reason, the measured fields are normalized along  $z$  using the MoM results to prevent any artefact or misleading information due to the measurement limitations. In other words, the maximum along the  $z$ -axis is the same for both the measured and MoM results. The focusing behaviour and good accuracy of the measured near field along  $z$  can be appreciated.

## V. CONCLUSION

In this paper, the design and measurement results of a radial line slot array antenna focusing in its near field have been presented. The possibility to control the side lobe level and beamwidth of the vertical component of the electric field has been considered. The RLSA structure is automatically generated by a novel design procedure. The input information of the design procedure are the size of the antenna and the requirements on the near-field pattern. The procedure is divided in two main steps. In the first step the aperture field distribution generating the required near field is derived. In the second step, the position and size of the slots of the RLSA are adjusted for synthesizing the derived aperture field and maximizing the spillover efficiency. An in-house fast MoM is used in the second step of the design procedure and for the analysis of the structure. General purpose software can not be used during this step due to their prohibitive computational time. In addition, the antenna can not be designed with classical near-field methodologies based on an equivalence between the near and far field of an antenna. Exhaustive 2D measurements validated the proposed approach and realized prototype. The proposed structure and design technique may find application in areas such as near-field probing and radiometry, wireless power transfer, medical imaging, and non-diffractive radiation.

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