# Finding binaries from phase modulation of pulsating stars with Kepler VI. Orbits for 10 new binaries with mischaracterized primaries 

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#### Abstract

Measuring phase modulation in pulsating stars has proven to be a highly successful way of finding binary systems. The class of pulsating main-sequence A and F variables, known as $\delta$ Scuti stars consists of particularly good targets for this, and the Kepler sample of these has been almost fully exploited. However, some Kepler $\delta$ Scuti stars have incorrect temperatures in stellar properties catalogues, and were missed in previous analyses. We used an automated pulsation classification algorithm to find 93 new $\delta$ Scuti pulsators among tens of thousands of F-type stars, which we then searched for phase modulation attributable to binarity. We discovered 10 new binary systems and calculated their orbital parameters, which we compared with those of binaries previously discovered in the same way. The results suggest that some of the new companions may be white dwarfs.


Key words: binaries: general-stars: oscillations - stars: variables: $\delta$ Scuti-stars: variables: general.

## 1 INTRODUCTION

The utility of Kepler data has expanded far beyond the primary purpose of exoplanet transit detection (Borucki et al. 2011) and the asteroseismology programme (Gilliland et al. 2010). An unexpectedly successful use of the data has been to infer companions to stars via their influence on the stellar pulsations (Shibahashi \& Kurtz 2012; Murphy et al. 2014). In this endeavour, the pulsations are used as clocks whose ticks arrive early or late according to the position of the star in its orbit, similar to $\mathrm{O}-\mathrm{C}$ analyses. The time derivative of the time delays gives the radial velocity curve, and analysis of these time delays allows the orbit to be determined. Faster clocks (shorter period pulsations) and more stable clocks allow the orbit to be determined more precisely. So far, the class of intermediate-mass stars on the main sequence, known as $\delta$ Scuti ( $\delta \mathrm{Sct}$ ) stars has proven to be the most valuable for pulsation-timing studies (Compton et al. 2016; Murphy 2018).
The largest sample of pulsation-timing binaries are the 341 systems with $\delta$ Sct primaries presented in the previous (fifth) paper of this series (Murphy et al. 2018, hereafter Paper V). That study used $\sim 12600$ stars in or near the $\delta$ Sct instability strip, spanning the $T_{\text {eff }}$ range $6600-10000 \mathrm{~K}$, of which 2200 were pulsators. This relatively small number of pulsators results from the fact that, even in the middle of the instability strip, no more than 70 per cent of stars actually pulsate (Murphy et al. 2019). This pulsator fraction

[^0]drops precipitously at the red edge of the instability strip, while the number of stars increases greatly due to the stellar initial mass function. In other words, expanding the search for $\delta$ Sct stars to cooler temperatures is an exercise in diminishing returns.

A small number of Kepler $\delta$ Sct stars appear to lie outside of the instability strip. Generally, these have incorrect temperatures in the Kepler Input Catalogue (KIC; Brown et al. 2011 and its subsequent revisions by Huber et al. 2014; Mathur et al. 2017; Berger et al. 2018). Having incorrect KIC temperatures is even more likely for binary stars, since we observe the blend of light of the two stars. The photometric colours used to determine the effective temperatures will not be representative of typical $\delta$ Sct stars, but will instead be biased by the companions, which are typically less massive main-sequence stars (Paper V) with lower temperatures and redder colours. Finding these $\delta$ Sct stars with mischaracterized temperatures by searching for pulsations in stellar light curves is a time-consuming task that is amenable to automation. In this paper, we use machine learning on 56860 stars with KIC temperatures cooler than those studied in Paper V (i.e. cooler than 6600 K ) to find 93 new $\delta$ Sct stars and search for binaries among them.
We also investigate 362 stars hotter than the upper limit of 10000 K used in Paper V. This sample consists of stars from other classes useful for pulsation timing, such as $\beta$ Cephei ( $\beta$ Cep) stars (B stars pulsating in p modes), subdwarf B stars (pulsating in p and/or g modes), white dwarfs (pulsating in g modes), but also the less useful slowly pulsating B stars (g modes), whose long pulsation periods are less precise clocks, and a large number (295) of nonpulsators or stars with amplitudes too low to be useful for pulsation
timing. It is also possible that $\delta$ Sct stars exist as the secondaries in these systems and that their pulsations will be detectable in the Kepler light curves, despite the significant dilution.

We describe our target-selection procedure and pulsation-timing method in more detail in Section 2. The results are shown in Section 3.

## 2 METHODOLOGY

### 2.1 Sample definition

Our goal was to ensure that all pulsators with coherent (not stochastic) oscillations had been analysed with the phase-modulation method to search for binarity. We defined our sample to have $T_{\text {eff }}>$ 6000 K in the Mathur et al. (2017) stellar properties catalogue. This extends the sample in the Paper V catalogue to stars between 6000 and 6600 K (the 'cool stars' subsample) and to stars hotter than 10000 K (the 'hot stars' subsample). We excluded stars already analysed in Paper V.

### 2.2 Classifying cool stars by variability

For the 56860 stars with temperatures between 6000 and 6600 K , we used a machine-learning algorithm to isolate potential $\delta$ Sct candidates for manual (visual) inspection. Our approach leverages existing work (Barbara et al., in preparation), which constructed a feature space and classification algorithm for distinguishing seven classes of light curves: six common classes of variable stars detached eclipsing binaries, contact binaries, $\delta$ Sct stars, $\gamma$ Dor stars, rotational variables, and RR Lyrae stars - as well as an additional class containing non-variable stars. The training set contained 1341 Quarter 9 (Q9) Kepler light curves of stars with $T_{\text {eff }}$ between 6500 and 10000 K . The light curves were obtained from KASOC ${ }^{1}$ and were processed with the multiscale MSMAP pipeline (Stumpe et al. 2014). Here, we used the feature space and classification algorithm, specifically trained to accurately distinguish Kepler light curves, to identify new $\delta$ Sct candidates. Detailed methods are described in Barbara et al. (in preparation) and are summarized below.

First, in identifying appropriate time-series features to represent Q9 light-curves, we used a forward-feature selection algorithm (Fulcher \& Jones 2014) on a library of over 7000 time-series features from across the scientific literature, implemented in the HCTSA package (Fulcher, Little \& Jones 2013; Fulcher \& Jones 2017). The seven-class classification performance of each feature (or set of features) was assessed according to its balanced classification accuracy using a linear support vector machine (SVM) using 10fold cross-validation. This procedure yielded a set of five time-series features that are well suited to distinguishing the seven classes of light curves. Briefly, these features measure the following:
(i) non-linear autocorrelation (feature name AC_nl_012 in HCTSA);
(ii) the probability of two magnitude increases in two successive time points (SB_MotifTwo_diff_uu);
(iii) relative power contained in peaks of the Fourier transform (SP_Summaries_fft_peakPower_prom2);
(iv) autocorrelation at time-lag 8 (AC_8); and
(v) entropy of the distribution of values in the time-series (EN_DistributionEntropy_hist_fd_0).

[^1]Representing each star in the training set in this five-dimensional feature space, we trained a Gaussian mixture model (GMM) to accurately classify light curves between the seven classes.

To identify new $\delta$ Sct candidates, we converted Kepler light curves from Q9 for the much larger number of stars in the wider $T_{\text {eff }}$ range of $6000-10000 \mathrm{~K}$ into five-dimensional feature vectors. We then used the trained GMM to calculate posterior probabilities for each of the seven classes and focussed on the 56860 stars in the 'cool stars' subsample. We generated an automated shortlist of 1203 candidates whose most likely variable class was $\delta$ Sct, which included $960 \delta$ Sct stars already known from Murphy et al. (2019). By manually inspecting all stars on this list, we identified 93 new $\delta$ Sct stars. The false-positive rate during shortlisting was $\sim 9$ per cent, with the primary sources of false positives being, in order of occurrence, harmonics of g-mode pulsations, Kepler data artefacts, apparent non-pulsators with noise spikes, and very low amplitude pulsators of borderline significance. Stars in the latter category could be considered $\delta$ Sct stars, depending on the chosen significance threshold (see Murphy et al. 2019 for a discussion), but the amplitudes would be too low to detect any phase modulation.

Since the new $\delta$ Sct stars have temperatures much cooler than the red edge of the $\delta$ Sct instability strip (Dupret et al. 2005; Murphy et al. 2019), their temperatures must be mischaracterized. Of the 93 $\delta$ Sct stars, 91 had pulsation amplitudes high enough for a phasemodulation analysis.

### 2.3 Classifying hot stars by variability

The hot stars subsample contained only 362 stars. The machine learning classifier was not applied to these stars because of the greater variety of variable stars and the small number of stars available for use as a training set. These stars were therefore classified manually into pulsators and non-pulsators using the full 4yr Kepler light curves. Of the 362 stars, only 51 stars had pulsations suitable for measuring phase modulation (after excluding seven eclipsing binaries).

### 2.4 Detecting and modelling binary orbits

To search for binary stars among the 142 newly identified pulsators, we followed the method used in Paper V, which can be summarized as follows. We calculated the Fourier transform of the $4-\mathrm{yr}$ Kepler light curves and used the frequencies of the strongest Fourier peaks as 'clocks'. We used a non-linear least-squares algorithm to find the best-fitting frequencies, amplitudes and phases for these peaks. The resulting pulsation frequencies for each star are listed in Table 1 for each of the 10 systems that were ultimately found to be binaries.

We subdivided the light curves into $10-\mathrm{d}$ subdivisions and, keeping the pulsation frequencies fixed, looked for periodic changes in the pulsation phases that could be attributed to binarity. Each pulsation frequency should generally respond in the same way to the orbit, though minor intrinsic phase modulation occasionally occurs, as in KIC 11340713 and KIC 6804957 (Figs 1 and 2). Frequencies with close neighbours in the Fourier transform are strongly affected by beating and were excluded from the analysis (see Murphy et al. 2014 for further discussion). After identifying binary candidates, we considered different subdivision sizes that might better sample the orbit, using shorter subdivisions for short-period binaries and longer subdivisions for pulsators with modes that were poorly resolved. The subdivision sizes used for Figs 1 and 2 are also given in Table 1.

We calculated the weighted-average time delay in each subdivision, weighting by the phase uncertainties for each pulsation mode.

Table 1. Pulsation frequencies extracted from the Kepler light curves of the detected binaries. Frequencies excluded from the time-delay averaging are indicated in square brackets. The frequency labels correspond to the ones used in Figs 1 and 2. The final column gives the length of subdivisions used to calculate time delays.

| KIC number | $f_{1}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | $f_{2}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | $f_{3}$ <br> $\left(\mathrm{~d}^{-1)}\right.$ | $f_{4}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | $f_{5}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | $f_{6}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | $f_{7}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | $f_{8}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | $f_{9}$ <br> $\left(\mathrm{~d}^{-1}\right)$ | Subdivision <br> $(\mathrm{d})$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11340713 | 10.15 | 9.50 | 10.55 | 9.84 | 11.91 | 13.06 | - | - | - | 10 |
| 3969803 | 7.45 | 15.66 | $[16.95]$ | 19.23 | $[19.13]$ | 8.55 | 16.35 | 15.40 | 9.28 | 10 |
| 4756171 | 10.68 | 9.98 | 11.79 | 10.38 | 9.66 | $[17.49]$ | 20.41 | 15.86 | $[18.25]$ | 8 |
| 5305553 | 16.56 | $[32.15]$ | $[5.13]$ | 19.00 | $[5.23]$ | 17.33 | 17.41 | $[5.79]$ | $[4.44]$ | 10 |
| 5480040 | 8.26 | 9.43 | 11.51 | 7.18 | $[9.20]$ | 8.41 | 8.47 | $[10.45]$ | 6.19 | 10 |
| 6804957 | 8.24 | 7.15 | 12.72 | $[11.06]$ | 11.66 | 7.22 | 7.92 | 5.19 | 14.11 | 18 |
| 6887854 | 28.36 | 29.70 | 36.87 | 27.16 | 29.91 | 35.36 | 36.49 | 36.70 | 29.40 | 8 |
| 8647777 | 11.31 | $[10.68]$ | 12.06 | 10.82 | 10.15 | $[11.63]$ | 9.15 | 9.23 | $[12.26]$ | 10 |
| 8842025 | $[11.47]$ | 12.72 | 15.13 | $[6.25]$ | 11.11 | 18.92 | 14.63 | 10.37 | 14.17 | 10 |
| 9306893 | 16.62 | $[29.81]$ | 16.47 | 15.77 | 31.59 | 25.25 | $[17.43]$ | 19.42 | 19.58 | 10 |












Figure 1. Time delays for different pulsation modes in five binary stars (left-hand panels) and orbital solutions for the weighted-average time delay (righthand panels), with 25 random steps from the MCMC (Markov chain Monte Carlo) chain plotted. Targets are (top to bottom): KIC 11340713, KIC 3969803, KIC 4756171, KIC 5305553, and KIC 5480040.

These phase uncertainties are the formal least-squares uncertainties for each pulsation mode for each subdivision of the light curve, which also depend on the remaining variance in the light curve (modelled or otherwise). That is, any variance not attributable
to the up to nine fitted pulsation frequencies will lead to larger uncertainties. For this reason, and because lower frequency (unused) g-mode pulsations often occur in these stars, we used the Gaussian_filter function from scipy.ndimage to apply


Figure 2. As Fig. 1, for five more binaries (top to bottom): KIC 6804957, KIC 6887854, KIC 8647777, KIC 8842025, and KIC 9306893.
a high-pass Gaussian filter to the data to remove this variance. For all but one of the 10 discovered binary systems, this led to appropriate uncertainties on the weighted-average time delay, but for KIC 5305553 the uncertainties remained too large - almost every time-delay data point was within $1 \sigma$ of the fit (described in the next paragraph). We divided the uncertainties by 4 for this target, so that the reduced chi-squared ( $\chi^{2} / N$ ) was close to unity.

To find the best-fitting orbital parameters and their uncertainties, we used an MCMC method (Murphy, Shibahashi \& Bedding 2016) that implements a random walk Metropolis-Hastings algorithm (Metropolis et al. 1953; Hastings 1970). The orbits were initialized at values near the expected solution using the semi-analytic method described by Murphy \& Shibahashi (2015). All orbital solutions were visually inspected to check the quality of the fit and to confirm that $\chi^{2} / N$ was of the order of unity.

## 3 RESULTS

A total of 10 new binary systems were discovered (Figs 1 and 2), all of which were from the subsample of 91 cool stars. Thus, 11 per cent of those targets turned out to be binary systems. Among
the hot stars, no new binaries were found, though two targets deserve further mention. Some phase modulation was detected for KIC 11558725 , a known 10-d binary consisting of a white dwarf and a pulsating subdwarf (Telting et al. 2012). Our search used only long-cadence data and used 10-d sampling by default, so the $10-\mathrm{d}$ modulation was not detected. Instead, some modulation was detected at longer periods using the g modes near $25 \mathrm{~d}^{-1}$, but there was little mutual consistency between different modes. The second target is KIC 7108883, for which different pulsation modes were also not in good agreement (Fig.3). This target will have to be followed up with radial velocities. If genuine, the binary period is at least as long as the Kepler observations.

Given that B stars are known to have a high rate of multiplicity (Abt, Gomez \& Levy 1990; Sana et al. 2013; Moe \& Di Stefano 2017), it is noteworthy that we find so few in binary systems here. This is presumably due to the fact that B-type stars, like most classes of variable star, are not well suited to a phase-modulation analysis (Murphy 2018). Generally, high-frequency oscillators are more useful clocks, but the B stars that do oscillate at high frequencies - the sdB stars and white dwarfs - often show intrinsic phase modulation, which makes them poor clocks (Østensen et al.


Figure 3. The hot star KIC 7108883, which shows some phase modulation, but the different oscillation modes do not agree well. The pulsation frequencies are $f_{1}=6.18, f_{2}=8.01$, and $f_{3}=12.35 \mathrm{~d}^{-1}$.

2014; Silvotti et al. 2018; Zong et al. 2018). If a large sample of $\beta$ Cep stars with long time-series can be collected with TESS or future missions, these would be the best future B-type targets for phase-modulation studies.

For the 10 new binaries, we determine the orbital parameters as the medians of the marginalized posterior distributions from the MCMC chains, which we give in Table 2. The uncertainties are given as the upper and lower bounds that encompass the central 68.2 per cent of the marginalized posteriors.

All 10 of the systems were detected as single-pulsator binaries (PB1s), meaning that the pulsation frequencies arise in the same star. One system (KIC 8647777) is a possible triple. The orbit in Table 2 is the short-period one, but there is also a long- period variation in the time delays (Fig. 2, left-hand panels). Even the full 4-yr Kepler light curve is not long enough to determine the parameters of the longer orbit. The parameters for the short-period orbit were determined after fitting and subtracting a sinusoid to the long-period variation (Fig. 2, right-hand panels).

Fig. 4 shows how the 10 new systems fit within the full sample of Kepler pulsating binaries. Four of the new systems have relatively large binary mass functions $\left(f_{\mathrm{M}}>0.1\right)$ and three have relatively small mass functions $\left(f_{\mathrm{M}} \sim 10^{-3}\right)$. All are consistent with being stellar-mass companions, as opposed to brown dwarf or planetary companions.

The new binaries include two at rather short periods (31 and 40 d ), where the search for binaries with the phase-modulation method has so far proven incomplete (Paper V). It is noteworthy that these two binaries (KIC 4756161 and 8647777 , respectively) also have relatively large mass functions, which made their detection easier. The short-period binaries in Paper V include some systems with low mass functions, so there is no clear implication that


Figure 4. Orbital periods and semimajor axes $\left(a_{1} \sin i / c\right)$ of the new systems (cyan crosses) and the binaries from Paper V (black circles). The background shading shows the binary mass function. Adapted from fig. 1 of Hey et al. (2020).
the mass-ratio distribution at these shorter periods $(P \lesssim 100 \mathrm{~d})$ is necessarily different from the distribution at longer periods $(P \gtrsim 100 \mathrm{~d})$. To check the accuracy of these two solutions, we also used the MAELSTROM code (Hey et al., in press) to determine orbits by forward modelling the time delays on to the light curve. This approach is more sensitive for shorter period and eccentric systems. A comparison of results is given in Table 3. We find that the values agree within the uncertainties: however, the eccentricities are still poorly constrained, as indicated by the posterior distribution for one of the stars in Fig. 5. Radial velocities would help to constrain the eccentricities of these systems.

The largest eccentricity of the 10 new binaries is 0.31 , and Fig. 6 shows that six of the 10 are located in the long-period, low-eccentricity 'post-mass-transfer triangle' (Paper V), where it is possible that the systems have experienced mass transfer. In systems where the original primary has already ascended the asymptotic giant branch (AGB), the AGB star can transfer mass by stable Roche-lobe overflow, causing the binary to circularize and the period to shorten (Jorissen et al. 1998; Karakas, Tout \& Lattanzio 2000; van Winckel 2003; Geller \& Mathieu 2011). Any post-AGB

Table 2. Orbital parameters for the PB1 systems. The time of periastron, $t_{\mathrm{p}}$, is specified in Barycentric Julian Date. $K_{1}$ is calculated from the other quantities and is convolved with $\sin i$. The full machine-readable table is available online.

| KIC number | P <br> (d) | $a_{1} \sin i / c$ <br> (s) | $e$ | $\begin{gathered} \varpi \\ (\mathrm{rad}) \end{gathered}$ | $\begin{gathered} t_{\mathrm{p}} \\ (\mathrm{BJD}) \end{gathered}$ | $\begin{gathered} f_{\mathrm{M}} \\ \left(\mathrm{M}_{\odot}\right) \end{gathered}$ | $\begin{gathered} K_{1} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11340713 | $984.8{ }_{-4.3}^{+5.0}$ | $107.35_{-0.98}^{+0.98}$ | $0.102_{-0.019}^{+0.018}$ | $6.100_{-0.042}^{+0.058}$ | $2455248.0_{-9.3}^{+10.0}$ | $0.00137_{-0.00004}^{+0.00004}$ | $2.389_{-0.025}^{+0.027}$ |
| 3969803 | $737-20$ | $95.6{ }_{-7.8}^{+8.6}$ | $0.101_{-0.068}^{+0.120}$ | $4.666_{-0.51}^{+0.63}$ | $2455661_{-71}^{+80}$ | $0.00174_{-0.00039}^{+0.00051}$ | $2.87{ }_{-0.24}^{+0.27}$ |
| 4756171 | $31.123_{-0.034}^{+0.033}$ | $66.3_{-6.6}^{+8.3}$ | $0.27_{-0.18}^{+0.25}$ | $4.22_{-0.62}^{+0.98}$ | $2454984.0_{-3.4}^{+4.6}$ | $0.324_{-0.087}^{+0.140}$ | $48.5_{-5.5}^{+11.0}$ |
| 5305553 | $186.73_{-0.22}^{+0.20}$ | $78.7_{-1.3}^{+1.4}$ | $0.200_{-0.030}^{+0.034}$ | $3.215_{-0.120}^{+0.076}$ | $2455042.2_{-3.7}^{+2.6}$ | $0.01499_{-0.00073}^{+0.00080}$ | $9.37{ }_{-0.18}^{+0.21}$ |
| 5480040 | $1358{ }_{-34}^{+46}$ | $440_{-14}^{+18}$ | $0.170_{-0.026}^{+0.020}$ | $2.771_{-0.049}^{+0.025}$ | $2455484_{-43}^{+43}$ | $0.0493_{-0.0023}^{+0.0030}$ | $7.161_{-0.088}^{+0.097}$ |
| 6804957 | $1073.2_{-3.3}^{+3.2}$ | $826.6_{-5.0}^{+5.1}$ | $0.3128_{-0.0100}^{+0.0097}$ | $3.574_{-0.038}^{+0.035}$ | $2455479.7_{-5.9}^{+6.3}$ | $0.527_{-0.010}^{+0.011}$ | $17.68_{-0.16}^{+0.17}$ |
| 6887854 | $183.82_{-0.12}^{+0.11}$ | $167.0_{-1.7}^{+1.6}$ | $0.170_{-0.018}^{+0.019}$ | $4.595_{-0.071}^{+0.070}$ | $2455061.6_{-2.2}^{+2.1}$ | $0.1481_{-0.0045}^{+0.0042}$ | $20.11_{-0.24}^{+0.22}$ |
| 8647777 | $39.813_{-0.044}^{+0.041}$ | $63.9{ }_{-4.6}^{+5.3}$ | $0.20_{-0.12}^{+0.18}$ | $0.57_{-0.65}^{+1.30}$ | $2454973.4_{-4.4}^{+7.4}$ | $0.177_{-0.035}^{+0.047}$ | $35.8{ }_{-2.8}^{+4.2}$ |
| 8842025 | $1133_{-13}^{+15}$ | $307.7_{-7.5}^{+7.4}$ | $0.201_{-0.043}^{+0.042}$ | $2.71{ }_{-0.11}^{+0.16}$ | $2455977_{-29}^{+37}$ | $0.0243_{-0.0018}^{+0.0019}$ | $6.04{ }_{-0.19}^{+0.19}$ |
| 9306893 | $605.9_{-4.3}^{+4.3}$ | $82.0_{-2.6}^{+2.7}$ | $0.079_{-0.046}^{+0.055}$ | $2.41_{-0.28}^{+0.31}$ | $2455543_{-28}^{+30}$ | $0.00161_{-0.00015}^{+0.00016}$ | $2.96_{-0.10}^{+0.10}$ |

Table 3. Orbital parameter comparison for the short period ( $P<100 \mathrm{~d}$ ) binaries found in this work, using the phase-modulation method (Murphy et al. 2014, 2016) and MAELSTROM (Hey et al. 2020).

| KIC number | $P$ <br> $(\mathrm{~d})$ |  | $a_{1} \sin i / c$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $(\mathrm{~s})$ |  |  |  |  |



Figure 5. Corner plot for the posterior distribution of parameters for KIC 8647777 using MaElstrom. The eccentricity is not well constrained in this short-period system.
system originally located above or to the left of this triangle would rapidly become a common-envelope binary instead. Hence, systems above or to the left of this triangle are almost certainly mainsequence pairs, but systems inside the triangle may be post-masstransfer binaries. If these systems have indeed experienced mass transfer, then the system currently consists of a $\delta$ Sct primary with a white-dwarf secondary whose mass should be around $0.5 \mathrm{M}_{\odot}$ (Jorissen et al. 1998; van Winckel 2003; Geller \& Mathieu 2011). Such a system is shaded green in Fig. 6.

With a reasonable estimate of the masses of the $\delta$ Sct primaries, we can estimate the nature of their companions. Given that the systems have been photometrically (mis)classified with temperatures just cooler than the $\delta$ Sct red edge, we assume that the primaries are low-mass $\delta$ Sct stars near the instability strip's red edge, which suggests that they have masses of $\sim 1.5 \mathrm{M}_{\odot}$ (Dupret et al. 2004; Murphy et al. 2019). Alternatively, these $\delta$ Sct stars could have low metallicities and lower masses $\left(\sim 1.2 \mathrm{M}_{\odot}\right)$, but that does not greatly affect the following calculations.

We first consider the three systems with very low mass functions (KIC 11340713, KIC 3969803, and KIC 9306893). Only for orbital inclinations below $\sim 20^{\circ}$ would the current secondaries have masses consistent with ordinary white dwarfs. At statistically more likely inclinations near $60^{\circ}$, they would have masses closer to $0.2 \mathrm{M}_{\odot}$, consistent with being extremely low mass white dwarfs (ELMs).


Figure 6. The 10 new binaries (large squares) compared with the population of binaries from Paper V (small circles) in the period-eccentricity diagram. Systems are colour coded by their binary mass function, fM . The light-grey triangle is the 'post-mass-transfer triangle' defined in fig. 9 of Paper V , and the dark-grey region contains the system whose orbits cannot be uniquely determined because the period is longer than the Kepler data set.

However, the formation model for ELMs predicts that they must have orbital periods in the range 2-20h (Sun \& Arras 2018), as supported by observations (Boffin 2015; Brown et al. 2016). None the less, it is noteworthy that ELMs have been found at longer periods (Masuda et al. 2019), despite there being no valid formation model for them yet. Determination of the true nature of these three new systems awaits astrometric data from Gaia DR3 to infer the orbital inclinations and hence component masses. They could also be low-mass M dwarfs; distinguishing between these two scenarios observationally is almost impossible.

Of the three other systems in the post-mass-transfer triangle, KIC 6804957 has a large mass function so it is probably a mainsequence pair occupying this same parameter space; KIC 8842025 has a mass function consistent with a white-dwarf companion; and KIC 5480040 could have a massive white-dwarf companion or be a main-sequence pair. These could be confirmed with high-signal-to-noise-ratio spectra, in which case main-sequence companions would be found as double-lined (SB2) systems and white-dwarf companions would be single-lined (SB1).

## 4 CONCLUSIONS

We used a machine-learning algorithm to find $\delta$ Sct stars with mischaracterized temperatures, manually verifying the machineautomated shortlist of 1203 candidates to recover 960 known and 93 new $\delta$ Sct stars. We searched these systems for binarity using
the phase-modulation method and found 10 new binaries. We also searched for binaries among Kepler B stars with the same method, but no new binaries could be confirmed. Since B stars are usually found in binary or multiple systems, the low detection rate is probably because B-type variable stars are generally not well suited to phase-modulation analysis.
The new binaries range in orbital period from 31 to 1073 d. One of the systems may be triple, with an outer period longer than the Kepler data set. The binary mass functions and positions in the period-eccentricity diagram suggest the companions to these $\delta$ Sct stars are diverse in nature, spanning a wide range of main-sequence masses and possibly also including white dwarfs.

Stars with spectral types between late A and early F are typically rapid rotators, making radial velocity follow-up difficult. Nevertheless, such studies would shed more light on the nature of the companions if the spectra turn out to be double lined. Otherwise, the orbital parameters correspond (in most cases) to small radial velocity semi-amplitudes, which along with the typically rapid rotation, suggests that these binaries would not be detectable by conventional methods.
The temperature range that was searched extended down to 6000 K , considerably cooler than the red edge of the $\delta$ Sct instability strip. It is unlikely that $\delta$ Sct stars with main-sequence companions would have effective temperatures much more mischaracterized than this. However, some $\delta$ Sct stars have red-giant companions that dominate the flux, and such systems would contain a wealth of asteroseismic information. These are promising future targets on which to apply the phase-modulation method.

Our application of automated variable-star classification suggests that there is great potential for machine learning in asteroseismology, particularly with wide-field surveys like TESS and PLATO, where the number of observed asteroseismic targets is increasing by orders of magnitude. While manual classification by human experts can be subjective and can contain implicit bias, automated classification methods are objective and can encourage clear, interpretable definitions of the characteristics of a given asteroseismic target. Although classification algorithms for this application are yet to reach the accuracy of a human expert, even relatively simple algorithms can drastically reduce the manual input required and guide human experts. This is demonstrated here, where our classification pipeline generated a shortlist of candidate targets for expert inspection, dramatically reducing the time burden of scouring the full catalogue manually. As pattern-detection algorithms for asteroseismology continue to mature, their ability to guide human expertise is likely to become increasingly valuable in generating new scientific understanding from large and growing asteroseismic data sets.

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## SUPPORTING INFORMATION

Supplementary data are available at $M N R A S$ online.
Table 2. Orbital parameters for the PB1 systems. The time of periastron, $t_{\mathrm{p}}$, is specified in Barycentric Julian Date. $K_{1}$ is calculated from the other quantities and is convolved with $\sin i$.
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