

The vibrational properties of benzene on an ordered water ice surface

Victoria H. J. Clark ¹★ and David M. Benoit ²★

¹Department of Physics and Astronomy, University College London, London WC1E 6BT, UK

²E.A. Milne Centre for Astrophysics, University of Hull, Hull HU6 7RX, UK

Accepted 2021 September 10. Received 2021 July 16; in original form 2021 July 16

ABSTRACT

We present a hybrid CCSD(T) + PBE-D3 approach to calculating the vibrational signatures for gas-phase benzene and benzene adsorbed on an ordered water ice surface. We compare the results of our method against experimentally recorded spectra and calculations performed using PBE-D3-only approaches (harmonic and anharmonic). Calculations use a proton ordered XIh water ice surface consisting of 288 water molecules, and results are compared against experimental spectra recorded for an ASW ice surface. We show the importance of including a water ice surface into spectroscopic calculations, owing to the resulting differences in vibrational modes, frequencies, and intensities of transitions seen in the IR spectrum. The overall intensity pattern shifts from a dominating ν_{11} band in the gas-phase to several high-intensity carriers for an IR spectrum of adsorbed benzene. When used for adsorbed benzene, the hybrid approach presented here achieves an RMSD for IR active modes of 21 cm^{-1} , compared to 72 cm^{-1} and 49 cm^{-1} for the anharmonic and harmonic PBE-D3 approaches, respectively. Our hybrid model for gaseous benzene also achieves the best results when compared to experiment, with an RMSD for IR active modes of 24 cm^{-1} , compared to 55 cm^{-1} and 31 cm^{-1} for the anharmonic and harmonic PBE-D3 approaches, respectively. To facilitate assignment, we generate and provide a correspondence graph between the normal modes of the gaseous and adsorbed benzene molecules. Finally, we calculate the frequency shifts, $\Delta\nu$, of adsorbed benzene relative to its gas-phase to highlight the effects of surface interactions on vibrational bands and evaluate the suitability of our chosen dispersion-corrected density functional theory.

Key words: astrochemistry – molecular data – dust, extinction – ISM: molecules – infrared: ISM.

1 INTRODUCTION

Benzene, C_6H_6 , is an aromatic hydrocarbon that was first isolated and identified on Earth in 1825 by Michael Faraday (Faraday 1825). Comprising of six carbon atoms bonded into a ring with a single hydrogen attached to each, benzene was first detected in the interstellar medium (ISM) by Cernicharo et al. (2001). It is thought to be one of the most basic building block of polycyclic aromatic hydrocarbon (PAH) molecules and is a key ingredient for the synthesis of PAH molecules, if formed via a bottom-up approach (Salama 2008; Kaiser, Parker & Mebel 2015). Along with its detection in the ISM, benzene has been detected and identified in a number of astronomical environments such as the planetary nebula of CRL618 (Cernicharo et al. 2001), the comae of comets and asteroids (Schuhmann et al. 2019) and meteoritic chondrites (Delsemme 1975), to name a few. Benzene is also thought to be a key ingredient of Titan’s atmosphere (Waite et al. 2007) and it has been recently detected in the atmosphere of Saturn (Koskinen et al. 2016). Due to its importance, benzene is often included as a component of kinetic reaction models when investigating interstellar dust grains, as Jones et al. (2011) showed it could be formed through a barrierless reaction. Protoplanetary and protostellar discs are another important area in which benzene is being searched for (Woods & Willacy 2007), a logical next step as hydrocarbon molecules including PAHs have

already been observed in these and similar environments (Cernicharo et al. 2001; Acke & van den Ancker 2004; Matsuura et al. 2004; Geers et al. 2006; Visser et al. 2007; Walsh et al. 2014). Complex organic molecules such as benzene are difficult to locate in protoplanetary disc due to their low abundance and complicated spectra (Walsh et al. 2014), therefore accurate binding energies and spectroscopic peak positioning are vital for this type of work.

There have been many studies investigating the vibrational frequencies of gaseous benzene (e.g. Szczepaniak & Person 1972; Hagen, Tielens & Greenberg 1983; Stephenson, Radloff & Rice 1984; Christiansen, Stanton & Gauss 1998). However, spectroscopic investigations of benzene on (water-)ice in the ISM have often focused on the vibrational frequency shifts of the OH bands of water (Michoulier et al. 2020) owing to the many known phases of water ice (Salzmann 2019), or the reactions of benzene (Sivaraman et al. 2014; Noble et al. 2020) rather than the vibrations of the molecules on the surface.

Currently, there are few studies investigating the vibrational frequencies of benzene on a water ice surface (Hagen et al. 1983; Dawes et al. 2018) with many authors using ice ‘nanocrystals’, containing up to eight water molecules as models (e.g. Augspurger, Dykstra & Zwier 1992; Tabor et al. 2015; Miliordos, Aprá & Xantheas 2016). However, it has been shown that results for both vibrational and binding/desorption energy calculations vary depending on the nature of the surface model (cluster or actual surface) (Silva & Devlin 1994; Thrower et al. 2009) and using large surfaces is likely needed to accurately reproduce experiment (Ma & Ma 2012). For this reason,

* E-mail: v.clark.17@ucl.ac.uk (VHJC); d.benoit@hull.ac.uk (DMB)

and to further aid the detection and identification, benzene has recently been included in an experimental work investigating the desorption and infrared spectrum of small aromatic molecules in water-containing astrophysical ices (Salter et al. 2021).

It is known experimentally that the binding of benzene to water ice is likely to occur through the π -hydrogen bonding of benzene with the dangling H–O bonds of the ice surface (see e.g. Silva & Devlin 1994). This binding mode (i.e. benzene acting as a hydrogen-bond acceptor) has also been confirmed by experimental and computational studies on benzene–water clusters (Engdahl & Nelander 1985; Gotch & Zwier 1992; Suzuki et al. 1992; Benoit, Chavagnac & Clary 1998) and this study builds on our previous publication which showed the feasibility of this type of molecular arrangement (Clark & Benoit 2019). Hence, adsorption of benzene on the surface of interstellar ice is a strong possibility and this paper presents a study of the expected infrared spectra that would be detected upon adsorption.

Here, we explore from first principles the vibrational signature of benzene on an ideal high-dipole ice surface to generate a suitable reference theoretical spectrum that could guide observations. We use the basal plane surface of ferroelectric water ice XIh (henceforth referred to as ‘ice’) as an ordered model for crystalline interstellar ice. The proton-ordered phase of crystalline ice Ih, ice XI or XII (see ‘Proton ordering and reactivity of ice’, Raza 2012, PhD thesis), has been suggested to exist on Kuiper belt objects in the Solar system (McKinnon & Hofmeister 2005) although it remains difficult to detect with certainty, but progress in this direction is being made (Fukazawa et al. 2006; Arakawa, Kagi & Fukazawa 2009; Wójcik et al. 2014). Nevertheless, this thermodynamically stable phase of water ice below 72 K is computationally simpler to model due to its straightforward proton ordering and has also been used in other studies as a model for crystalline water in the ISM (Kayi, Kaiser & Head 2011).

The paper is organized as follows: in Section 2, we present a fully anharmonic technique to compute the predicted vibrational signature of benzene adsorbed on ice XIh from first principles, with a detailed description of our computational details in Section 3. We evaluate the agreement of our calculations with available experimental infrared laboratory data in Section 4 and present our conclusions in Section 5.

2 THEORY

2.1 Vibrational spectra modelling

The anharmonic calculations are performed using the VCIPSI approach developed in Scribano & Benoit (2008). We represent the potential energy surface (PES), $V(q_1, \dots, q_n)$, as a sum of one-mode terms, V^{diag} , and two-modes terms, V^{coupl} , a pairwise approximation suggested by Jung & Gerber (1996). Thus, for a system composed of N vibrational modes we have:

$$V(\mathbf{q}) = V(q_1, \dots, q_n) = V^{(0)} + \sum_{i=1}^N V^{\text{diag}}(q_i) + \sum_{i=1}^N \sum_{j>i}^N V^{\text{coupl}}(q_i, q_j), \quad (1)$$

where q_i are the normal modes of the system, $V^{(0)}$ is the energy of the minimum. Note that throughout this paper, we use rectilinear normal modes as PES coordinates. The VCIPSI approach represents the vibrational wavefunction as a sum of n -mode vibrational states (configurations), which are in turn described as product of single-mode wave functions (modals), $\varphi_i^{(\mathbf{k})}(q_i)$. Thus:

$$\Psi_{\mathbf{k}}(\mathbf{q}) = \sum_{\mathbf{k}} C_{\mathbf{k}} \left[\prod_{j=1}^n \varphi_j^{(\mathbf{k})}(q_j) \right], \quad (2)$$

where $\mathbf{k} = \{k_1, k_2, \dots, k_n\}$ specifies the excitation quanta of each single-mode wavefunction and $C_{\mathbf{k}}$ are the coefficients of each configuration. The modal product is optimized using a vibrational self-consistent field approach (VCSF) and the configuration coefficients are optimized using a selective vibrational configuration technique detailed in Scribano & Benoit (2008). In this study, we follow closely the approach outlined in Benoit (2015) for water on a Pt(111) surface.

2.2 Infrared intensities calculations and line averaging

The infrared transition intensity from $v_i = 0$ to $v_i = 1$ for each line, I_i , is computed using the diagonal (uncoupled) 1D vibrational wavefunction and a global dipole surface computed at the PBE-D3/MOLOPT-TZV2P level of theory (see Section 3 for details). The strength of the fundamental transition is given by the integral:

$$I_i = \frac{8\pi^3 N_{\text{Av}}}{3hc} v_i \left| \left\langle \varphi_i^{v_i=0}(Q_i) \left| \vec{\mu}_i(Q_i) \right| \varphi_i^{v_i=1}(Q_i) \right\rangle \right|^2, \quad (3)$$

where N_{Av} is Avogadro’s number, h is Planck’s constant, c is the speed of light, and v_i is the uncoupled, diagonal, fundamental frequency for mode i . The diagonal dipole moment surface is computed using:

$$\vec{\mu}(\mathbf{Q}) = \vec{\mu}(0) + \sum_{i=1}^n \vec{\mu}_i(Q_i), \quad (4)$$

where $\vec{\mu}(0)$ is the dipole moment at equilibrium and $\vec{\mu}_i$ is the dipole moment along normal coordinate Q_i . In practice, we compute the dipole moment at each 1D grid point and then interpolate the dipole moment to a finer-meshed representation using a cubic-spline algorithm for each dipole vector component. Note that one limitation of the scheme is that it cannot realistically model intensity borrowing or combination bands, as those inherently rely on coupled dipole surfaces.

The position of degenerate bands that should be equivalent by symmetry (such as E_{1u} -bands, for example) are averaged using an intensity weighted scheme. This is necessary since the VSCF procedure ignores symmetry by constructions (independent modals) and can lead to non-equivalent transition frequencies for E -symmetry modes (although this is partly corrected by the VCIPSI approach). Our averaging scheme for two non-equivalent E -bands v_a and v_b , each having intensity I_a and I_b is given by:

$$v_{\text{avg}} = \frac{I_a v_a + I_b v_b}{I_a + I_b}. \quad (5)$$

This scheme is applied throughout, but for transparency all individual computed mode frequencies are shown in supplementary information (Tables S2 and S3).

2.3 Potential energy surface for benzene on ice vibrational calculations

In order to simplify the vibrational calculation, we use a partial Hessian technique (details in Section 3) where the ice surface is held fixed while the adsorbed benzene molecule is allowed to vibrate. This type of approach has already been validated for adsorbed molecules on metal surfaces (Benoit et al. 2011). However, in the present case, the mass separation between adsorbate and surface is not as large. As this can potentially cause artefacts in our calculations, we checked that normal modes obtained when allowing both benzene and the topmost ice layer to move were sufficiently localized on the benzene fragment. Clearly, a more elaborate treatment of ‘second-order’ phenomena, such as intensity transfer and dissipative surface

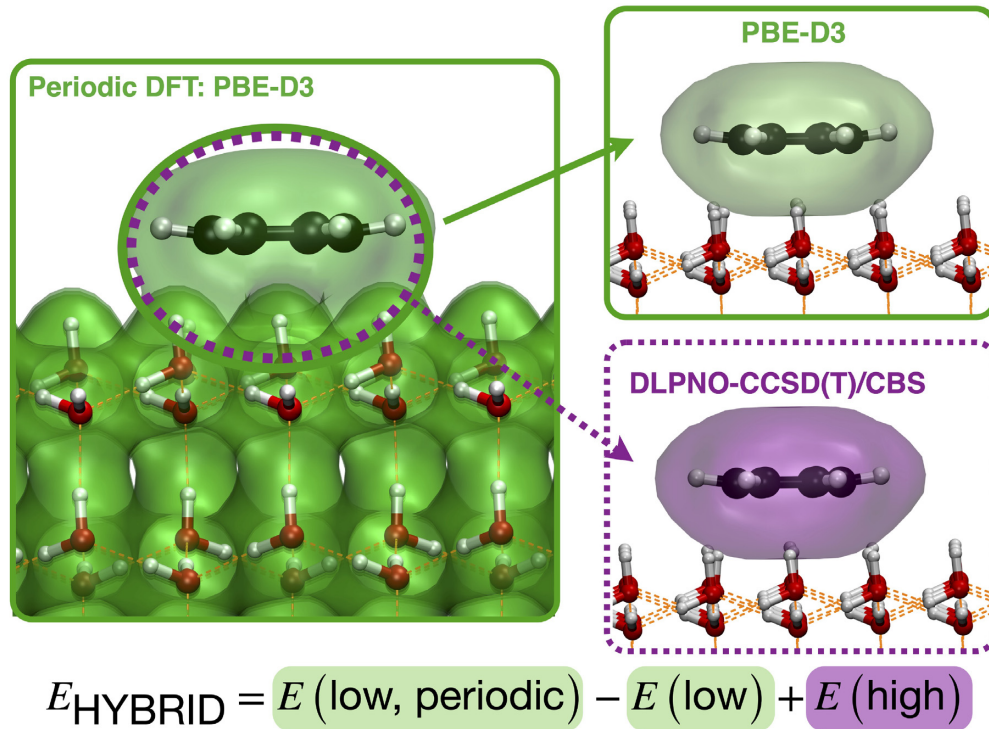


Figure 1. Representation of ONIOM approach used to compute the hybrid potential. The energy is decomposed into three calculations: two periodic DFT calculations (full system and model, full line) and one DLPNO-CCSD(T) calculation (model, dashed line). The parts of the system include in each calculation are indicated using a green colour for PBE-D3 and a purple colour for DLPNO-CCSD(T).

dynamics, should consider those but this is beyond the scope of this study.

The PES used for the anharmonic vibrational calculations is obtained using a hybrid approach that follows our earlier work for water on a Pt(111) surface (Benoit 2015). The diagonal part of the PES in equation (1), $V^{\text{diag}}(q_i)$, is computed using a hybrid approach while the coupling term in equation (1), $V^{\text{coupl.}}(q_i, q_j)$, is computed at the periodic density functional theory (DFT) (‘low’) level of theory. Thus, we have

$$V(\mathbf{q}) = \sum_{i=1}^N V_{\text{HYBRID}}^{\text{diag}}(q_i) + \sum_{i=1}^N \sum_{j>i}^N V_{\text{low}}^{\text{coupl.}}(q_i, q_j), \quad (6)$$

where the $V^{(0)}$ term has been subtracted as it is not relevant for vibrational calculations. In contrast to our previous study (Benoit 2015), where we used an explicitly correlated F12 approach, the size of this system prevents us from using a high-level correlated method for the entire system. Therefore, we use an approach that mixes periodic DFT with coupled-cluster singles and doubles with perturbative triples (CCSD(T)) calculations. The scheme, referred later on as DFT/CCSD(T), is a version of the ‘our own n-layered integrated molecular orbital and molecular mechanics’ (ONIOM) approach developed by Morokuma and collaborators (see Dapprich et al. 1999). This allows us to use a cost-effective yet high-quality approach and define $V_{\text{HYBRID}}^{\text{diag}}(q_i)$ as

$$V_{\text{HYBRID}}^{\text{diag}}(q_i) = V_{\text{low}}^{\text{diag}}(q_i, \{\text{Bz} + \text{Ice}\}) - V_{\text{low}}^{\text{diag}}(q_i, \{\text{Bz}\}) + V_{\text{high}}^{\text{diag}}(q_i, \{\text{Bz}\}), \quad (7)$$

where the notation $\{\text{Bz} + \text{Ice}\}$, $\{\text{Bz}\}$ indicates that the energy calculations are performed for benzene *with* an ice surface or *without*, respectively. The ‘low’ level of theory is PBE-D3/MOLOPT-TZV2P

and the ‘high’ level of theory is DLPNO-CCSD(T)/CBS using non-augmented basis sets ($X = 3$ and $Y = 4$) and EC2 approach to speed up the PES generation. The energy decomposition scheme used is shown graphically in Fig. 1. Further details of the method used are shown in Section 3 below.

3 COMPUTATIONAL DETAILS

3.1 Ice XIh model

Our model uses an ice surface generated from the optimized low-temperature proton-ordered coordinates from Hirsch & Ojamäe (2004), obtained at the PW91/PW(350 Ry cutoff) level of theory (structure 1 in their original paper). In order to create the slab of ice XIh, the original unit cell ($a = 4.49225 \text{ \AA}$, $b = 7.78080 \text{ \AA}$ and $c = 7.33581 \text{ \AA}$, $\alpha = \beta = \gamma = 90^\circ$) was repeated to create a $6 \times 3 \times 2$ supercell. In total, there are 36 unit cells of XIh ice in the slab, totalling 288 H_2O molecules, with four double-layers of water molecules. The surface is chosen along the c direction and thus the lattice constant is increased to $c = 34.6716 \text{ \AA}$ to accommodate the adsorption of a benzene molecule. In order to relax the surface energy, the positions of the surface atoms in the topmost water double-layer (72 H_2O molecules) are optimized, while the coordinates of the bottom three double-layers (216 H_2O molecules) of ice remains fixed. We use surface periodic boundary conditions in the x , y (a , b) directions, while the z (c) direction is treated non-periodically.

3.2 DFT calculations

All PBE-D3 calculations were performed using the Gaussian plane waves method implemented in the QUICKSTEP module (Goedecker,

Teter & Hutter 1996; Perdew, Burke & Ernzerhof 1996; VandeVondele et al. 2005) of CP2K (v4.1 and v6.1) (Naumkin & Knowles 1995; Chergui 1996; Goedecker et al. 1996; Lippert, Hutter & Parrinello 1997; VandeVondele & Hutter 2007). The valence electrons of all atoms are described using a TZV2P-MOLOPT-GTH basis set (Dunning 1971; Krack 2005; VandeVondele & Hutter 2007). The core electrons are represented using Goedecker-Teter-Hutter (GTH) pseudo-potentials (Krack 2005) along with an auxiliary plane-wave cutoff of 300 Ry. XY periodicity was used for all calculations with an analytical Poisson solver for the electrostatic energy. The wavefunction convergence was set to 1.E-7 au for all calculations. During geometry optimizations, the convergence criterion for the maximum force of element was set to 1.E-5 bohr⁻¹ Hartree except for the geometry optimization of gaseous benzene, when a maximum force of 1.E-6 bohr⁻¹ Hartree was required. The exchange-correlation functional is that derived by Perdew, Burke and Ernzerhof (PBE; Perdew et al. 1996) and we account for dispersion interactions using the DFT-D3 correction scheme of Grimme et al. based on a damped atom-pairwise potential and three-body C₉ corrections (Wishnow, Gush & Ozier 1996). While the coordinates of the benzene atoms remained unconstrained in all calculations, the coordinates of all ice molecules were constrained in the vibrational analysis (288 molecules), while the top layer of ice was left unconstrained in the geometry optimizations (only constraining the lower three layers, corresponding to 216 H₂O molecules, as described in Section 3.1). The geometry of the adsorbed benzene and selected structural parameters were reported already in Clark & Benoit (2019), for full transparency we have also included a coordinate file as supplementary information.

3.3 DLPNO-CCSD(T)/EC2-CBS calculations

The complete basis set extrapolation of the domain-based local-pair natural orbital coupled-cluster singles doubles and perturbative triples (DLPNO-CCSD(T)) energy was performed using the ORCA 3.0.3 suite of programs. Note that this particular version of ORCA, the (T) implementation uses a ‘semicanonical’ approximation to compute the perturbative triples correction, also known as T0 correction. The expression used for the EC2-CBS extrapolation, due to Jurečka et al. (2006) is

$$E(\text{DLPNO-CCSD(T)/EC2-CBS}(X,Y)) \approx E(\text{SCF}; Y) + E(\text{DLPNO} - \text{CCSD(T)}; X) + E(\text{MP2}; \infty) - E(\text{MP2}; X). \quad (8)$$

Where X and Y are the cardinal number of each basis set used. Here, we use the ano-pVTZ basis set together with the ano-pVQZ basis set (Neese & Valeev 2011) and thus X = 3 and Y = 4, respectively.

The MP2 energy is extrapolated using

$$E(\text{MP2}; \infty) = \frac{X^\beta \cdot E(\text{MP2}, X) - Y^\beta \cdot E(\text{MP2}, Y)}{X^\beta - Y^\beta}, \quad (9)$$

where $\beta = 2.41$, value optimized by Neese, Hansen & Liakos (2009) and Neese & Valeev (2011).

In order to accelerate the calculations, we used both the RI-JK approximation (Weigend 2008) [with a cc-pVQZ/JK auxiliary basis set (Dunning 1989)] and the RI-MP2 approach (Weigend & Häser 1997) [with an aug-cc-pVQZ/C auxiliary basis set (Kendall, Dunning & Harrison 1992)]. All calculations used the vertyightscf convergence criterion of ORCA (Neese 2012). All DLPNO-CCSD(T) calculations used the default ORCA criteria for the PNO generation (NormalPNO).

3.4 Vibrational calculations

We obtain the harmonic normal modes, q_i , by diagonalizing a mass-weighted partial Hessian matrix computed in CP2K. Note that all surface atoms are kept frozen during the Hessian matrix calculation.

The PES computation is then driven by the PVSCF program (Benoit et al. 2011) that is developed in our laboratory. We use the DFT energy values computed for 16 points along each rectilinear vibrational coordinate to interpolate a finer-meshed representation of the diagonal terms (1D) of the PES using a cubic-spline algorithm. The starting and finishing points of each coordinate scan in q -space are optimized to ensure that the curve supports at least eight bound states. Each mode–mode coupling term is computed for 16×16 regularly spaced grid points and then interpolated on a finer mesh using a bicubic interpolation (Akima 1996). These points form a discretized version of the PES of the system, $V(\mathbf{Q})$, as formulated in equation (1).

In order to provide high-accuracy surfaces the 1D energy points are re-computed using the DLPNO-CCSD(T)/EC2-CBS(ano-3,4) approach described in Section 3.3 for the benzene only and a hybrid ONIOM model for benzene on ice described in Section 2.3. Note that this scheme only contains benzene in the ONIOM layer (i.e. no water molecules are included) and thus does not require diffuse (aug-) functions in the basis.

All the 1D VSCF equations are solved using the FGH method (Marston & Balint-Kurti 1989; Balint-Kurti, Ward & Clay Marston 1991). We compute the correlation corrections using the VCIPSI method and explore a VCI basis made of all one-, two-, three- and four-mode excitations (VCISDTQ) up to seven excitation quanta ($n_{\text{max}} = 7$). In particular, we note that in order to accurately model the C–H stretching bands, it is necessary to include modal excitations of up to 4 modes simultaneously, even with a simple mode–mode coupling. The convergence of these vibrational bands with the excitation level is shown in Table S1 in the supplementary material. The iterative VCI matrices are diagonalized using our own implementation of the Davidson algorithm. Note that the vibrational calculation is only performed for the Γ -point of the Brillouin zone (Keçeli, Hirata & Yagi 2010; Ulusoy et al. 2011).

All anharmonic transition intensities are computed using a diagonal representation of the dipole surface computed at the PBE-D3/MOLOPT-TZV2P level of theory along with the 1D vibrational wave functions (i.e. without including effects from vibrational correlation).

4 RESULTS AND DISCUSSION

As a highly symmetric molecule, benzene is a challenging system due to a number of resonances, high symmetry band groups and vibrational modes that combine both bending and stretching motions. This combination of factors stretches the capabilities of the simple harmonic approximation, likely leading to a poor overall mode description in a rectilinear coordinate system and inaccurate resonance description.

However, symmetry can easily be included in that model and offers a strong guiding principle for attributing vibrational modes to observed bands. When benzene is placed on an ice surface (even one with a symmetry that resembles that of benzene, like the XIh ice surface), most of the symmetry-based guiding principles are weakened (or even absent) thus making mode attribution extremely difficult.

In this context, we compare the performance of the harmonic approximation to that of an accurate method that naturally accounts for

Table 1. Infrared active vibrational frequencies in cm^{-1} of isolated gas-phase benzene. All degenerate computed bands are intensity averaged (see Section 2.2 for details).

Band [\mathcal{D}_{6h} label]	Harmonic		Anharmonic	Exp.	Ref.
	PBE-D3	PBE-D3	CCSD(T) + PBE-D3		
11 [A_{2u}]	663	694	718	673.975	Hollenstein et al. (1990)
18 [E_{1u}]	1034	1026	1051	1038.267	Plíva & Johns (1984)
19 [E_{1u}]	1465	1443	1490	1483.985	Plíva & Johns (1983)
20 [E_{1u}]	3105	2949	3059	3047.908	Plíva & Pine (1982)
RMSD	31	55	24	–	

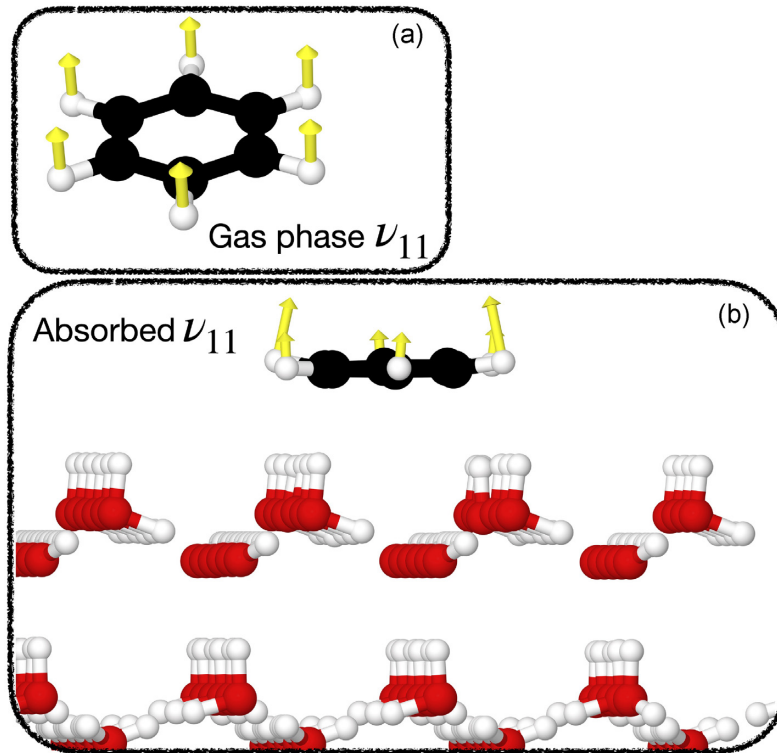


Figure 2. Vibrational mode corresponding to out-of-plane band ν_{11} for benzene in the gas-phase (Box A) and benzene adsorbed on a highly ordered basal plane surface of ferroelectric water ice XIh (Box B). Note the difference between the symmetric appearance of the mode in the gas-phase while the adsorbed version of this mode is noticeably asymmetric.

vibrational resonances, namely the vibrational configuration interaction on a basis of vibrational self-consistent modals (VSCF/VCIPSI). The accuracy of the approach has already been shown for many molecules on surfaces (see e.g. Chulkov & Benoit 2013 or Benoit 2015).

4.1 Gaseous benzene

In this subsection we compute the vibrational spectrum of gaseous benzene as a benchmark to establish the effect of surface interaction on its vibrational signature. We note that gas-phase benzene has already been the subject of many studies both experimental and theoretical [see references in Table S2 for specific experimental lines, and Christiansen et al. (1998), Senent et al. (2002) for examples of theoretical work], but our aim here is simply to correlate our adsorbed spectra (see Section 4.2) with results for a non-adsorbed system, obtained using the same approach.

Our results for the infrared active modes are shown in Table 1. For each band, we report results obtained using a harmonic model (PBE-

D3 surface), our anharmonic model (using two PESs) and the latest experimental results. As is known from group theory, the infrared spectrum of benzene is surprisingly sparse (see Table 1), with the \mathcal{D}_{6h} point group of benzene allowing only four active vibrational bands (one A_{2u} band: ν_{11} , and three E_{1u} bands: ν_{18} , ν_{19} and ν_{20}). We observe that those bands are qualitatively well described by all models, although we note that the harmonic model overestimates ν_{20} by over 50 cm^{-1} . Instead, our anharmonic approach leads to an excessive lowering of this band by $\sim 100 \text{ cm}^{-1}$ relative to experiment for PBE-D3. This functional has already been shown to describe bends better than it does stretches (see Respondek & Benoit 2009 for further details). The hybrid PES leads to a welcome redshifting of ν_{20} to 3059 cm^{-1} in close agreement with the experimental value of Plíva & Pine (1982).

However, the bands corresponding to modes that contain a bending component (ν_{11} , see also Fig. 2, and ν_{18} to some extent) are poorly described by the hybrid approach and overestimate the experimental values (by 44 cm^{-1} and 13 cm^{-1} , respectively). This outcome is not unexpected as the vibrational self-consistent field (VSCF) theory

Table 2. Raman active vibrational frequencies in cm^{-1} of isolated gas-phase benzene. All degenerate computed bands are intensity averaged (see Section 2.2 for details).

Band [\mathcal{D}_{6h} label]	Harmonic		Anharmonic		Exp.	Ref.
	PBE-D3	PBE-D3	CCSD(T) + PBE-D3	PBE-D3		
6 [E_{1g}]	603	601	609		608.13	Hollinger & Welsh (1978)
10 [E_{1g}]	834	846	879		847.1062	Plíva, Johns & Lu (1996)
1 [A_{1g}]	991	984	1000		993.071	Jensen & Brodersen (1979)
9 [E_{1g}]	1162	1154	1184		1177.776	Hollinger & Welsh (1978)
8 [E_{1g}]	1591	1566	1620		1600.976	Plíva, Esherrick & Owyong (1987)
7 [E_{1g}]	3091	2936	3041		3056.6	Hollinger & Welsh (1978)
2 [A_{1g}]	3115	2982	3081		3073.942	Jensen & Brodersen (1979)
RMSD	22	60	16		–	

ignores symmetry relations and uses a rectilinear coordinate system that typically disadvantages bends over stretches.¹ Indeed, bends involve angular motions that require a curvilinear coordinate system and cannot be described adequately with (recti)linear vectors. This has already been explored for methanol, for example, and clearly showed some of the shortcomings of the rectilinear approach for torsional modes, e.g. Scribano, Lauvergnat & Benoit (2010). For benzene, the limitations of this coordinate system mean that some of the complex bend-stretch bands (e.g. ν_{11} and ν_{18}) are disadvantaged by our present approach and likely appear in the incorrect order.

Another consequence of the shortcomings of the rectilinear approach, combined with a limited 2-mode interactions PES, is shown for ν_{20} , where our approach predicts a doublet instead of the single band of E_{1u} symmetry seen experimentally (see Table S2). Indeed, the splitting between the two modes (28 and 29) that make up ν_{20} is only 3 cm^{-1} at the harmonic level but further increases for the anharmonic calculation on both PBE-D3 and hybrid surfaces (16 cm^{-1} and 24 cm^{-1} , respectively). By de-coupling the C–H stretches from the rest of the modes, we can estimate that the exaggerated rectilinear stretching–bending coupling terms contribute as much as $10\text{--}15 \text{ cm}^{-1}$ and that the remaining differences are likely down to lack of a symmetrical exploration of the PES for those two equivalent modes.

Nevertheless, the root-mean-square deviation (RMSD) of the anharmonic approach on our hybrid surface is small (24 cm^{-1}) and improves on both harmonic and anharmonic approaches for PBE-D3 (31 cm^{-1} and 55 cm^{-1} , respectively).

The Raman-active bands provide further comparison points with experiment and our results for those modes are shown in Table 2. Here again, we provide results obtained for the harmonic model (PBE-D3 surface), our anharmonic model (using two PESs) and the latest experimental results. The \mathcal{D}_{6h} point group of benzene allows more bands for this type of spectroscopy, leading to seven active vibrational bands (two A_{1g} bands: ν_1 and ν_2 , one E_{1g} band: ν_{10} , and four E_{1g} bands: ν_6 , ν_9 , ν_8 , and ν_7).

We see, here too, that all Raman bands are qualitatively well reproduced by all models. The harmonic approach overestimates the high-frequency modes (ν_7 by 34 cm^{-1} and ν_2 by 41 cm^{-1}), while the anharmonic PBE-D3 results strongly underestimate the two same bands (ν_7 by 121 cm^{-1} and ν_2 by 92 cm^{-1}). The prediction of most Raman active bands is dramatically improved by the hybrid PES, which corrects both ν_7 and ν_2 to within 15 cm^{-1} and 7 cm^{-1} of the experimental data, respectively. One notable exception is the

E_{1g} band (ν_{10}), which was fortuitously well described by both the harmonic and anharmonic treatment at the PBE-D3 level of theory but is overestimated by nearly 32 cm^{-1} in the hybrid model. Here, rectilinear coordinates likely couple C–H stretching modes into this out-of-plane bending band and fortuitously favour the PBE-D3 anharmonic calculation, leading to an apparent good agreement for this band.

Nevertheless, our hybrid approach leads to a very good overall agreement with experimental data (RMSD of 16 cm^{-1}), compared to the PBE-D3 surface (22 cm^{-1} for the harmonic model and 60 cm^{-1} for the anharmonic model). This agreement is in line with the expected performance of our model (see Scribano et al. 2010 for a more detailed discussion) and further accuracy increase would require a more elaborate mode–mode interaction potential (3-modes or more) and/or a non-rectilinear coordinate system.

4.2 Benzene on an ice surface

Upon adsorption of benzene on our proton-ordered ice surface model, the high symmetry of benzene is perturbed and most vibrational modes are now able to contribute to the infrared spectrum (and thus possibly indicating a C_1 symmetry instead). Yet, in order to examine the correspondence between gas-phase and adsorbed modes, we analyse the vibrational modes in the \mathcal{D}_{6h} point group when possible.

To facilitate the cross-assignment between vibrational modes of \mathcal{D}_{6h} gas-phase benzene and benzene adsorbed on the ice surface, we have analysed the overlap between each set of normal modes and generated the correspondence graph shown in Fig. 3. This figure shows the normal modes in gaseous benzene (right) mapped to the corresponding normal modes for adsorbed benzene on to an ordered ice surface (left). We see that while 10 modes retain their character upon adsorption (modes 5, 6, 12, 15, 19, 20, 25, 26, 27, and 30), most of the other modes are either swapped within their symmetry band (modes 1&2, 3&4, 7&8, 13&14, and 28&29) or undergo a noticeable re-organization. This is an indication of the influence of the ice surface on the vibrational structure of benzene, and is also important when comparing frequency shifts at a vibrational mode level (see below).

Our results for the observed infrared bands are shown in Table 3. For each band, we report results obtained using a harmonic model (PBE-D3 surface), our anharmonic model (using two PESs) and the latest experimental results (a complete list of all frequencies is also shown in Table S3).

At first glance, the two sets of experimental frequencies (Hagen et al. 1983; Dawes et al. 2018) seem in very good agreement with each other. There are some discrepancies; however, when we consider the weaker lines observed by Hagen et al. (1983) (indicated in brackets

¹Other coordinate systems are available in PVSCF but are untested for molecules on surfaces, see <https://pvscf.org> for further information.

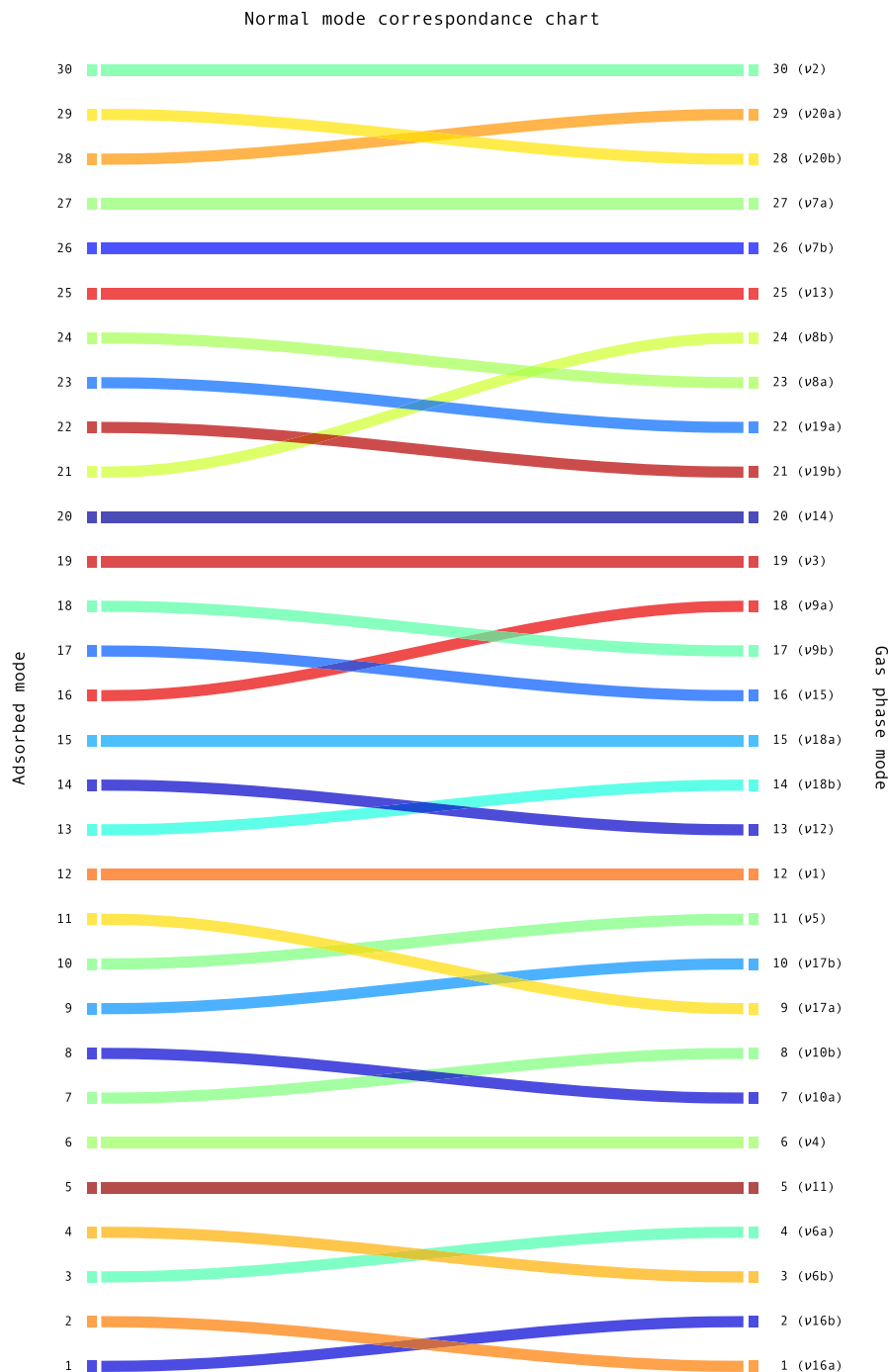


Figure 3. The normal mode correspondence between benzene adsorbed on to ice surface (left) and gaseous benzene (right). The band labelling follows the convention adopted for gas-phase benzene in D_{6h} symmetry.

in Table 3) which are shifted by up to 12 cm^{-1} (ν_{17}) compared to the measurements of Dawes et al. (2018). On closer inspection of the original papers, we noticed a large deviation for ν_2 , which Hagen et al. (1983) attribute to their peak at 3069 cm^{-1} , while Dawes et al. (2018) attribute this band to a peak at 3089 cm^{-1} in their spectrum. This assignment would lead to a large disagreement of 20 cm^{-1} for this strong band – unlike all other strong bands observed. It is worth noting that Hagen et al. (1983) do record a peak at 3090 cm^{-1} (see also the spectra shown in Fig. 4) but attribute this to a combination band ($\nu_8 + \nu_{19}$) of significant intensity. Given the overall excellent

agreement between the two studies for the strong intensity modes, we are inclined to think that Dawes et al. (2018) band ν_7 is more likely to correspond to band ν_2 and that ν_7 (a band described as weak by Hagen et al. 1983) is not present in their spectra. Another issue stems from the ambiguous assignment of ν_2 and ν_{13} in Hagen et al. (1983) (see also Table S3). In their paper, the peak at 3069 cm^{-1} discussed above is attributed to either band ν_{13} or ν_2 (table V in Hagen et al. 1983 listing it as ‘13 or 2’). This assignment probably originates from a comparison with the comprehensive work of Szczepaniak & Person (1972) on benzene in a solid HCl matrix where they list a ν_{13} band

Table 3. Benzene on ice IR vibrational frequencies in cm^{-1} . All degenerate computed bands are intensity averaged (see Section 2.2 for details). Weak bands observed by Hagen et al. (1983) are indicated in brackets. $\star = (\nu_{20}$ in original reference), $\dagger = (\nu_{18}$ in original reference), \ddagger corresponds to a band that we have re-attributed based on Hagen et al. (1983)'s observations. RMSD (IR) only includes the modes that are originally infrared active for a \mathcal{D}_{6h} symmetry (bold modes), while RMSD (all) includes all bands.

Mode [\mathcal{D}_{6h} label]	Harmonic		Anharmonic	Hagen et al. (1983)	Dawes et al. (2018)
	PBE-D3	PBE-D3	CCSD(T) + PBE-D3		
11 [A_{2u}]	619	657	677	681	–
10 [E_{1g}]	737	747	786	860	858
17 [E_{2u}]	848	798	843	(977)	989
12 [B_{1u}]	991	975	1005	(1012)	1011
18 [E_{1u}]	994	978	1002	1035 \star	1035
15 [B_{2u}]	1133	1123	1144	1148	1148
9 [E_{1g}]	1106	1121	1149	1176	1177
14 [B_{2u}]	1353	1329	1328	(1305)	1312
19 [E_{1u}]	1439	1413	1457	1478	1478
8 [E_{1g}]	1483	1419	1472	(1585)	1586
20 [E_{1u}]	3084	2922	3020	3034 \dagger	3034
7 [E_{1g}]	3069	2943	3023	(3050)	–
2 [A_{1g}]	3096	2925	3031	3069	3070 \ddagger
RMSD (IR)	49	72	21	–	–
RMSD (all)	68	100	56	–	–

Table 4. Vibrational frequency shift, $\Delta\nu$, for benzene adsorbed on ice compared to gas-phase in cm^{-1} . We define $\Delta\nu_i = \nu_i^{\text{gas}} - \nu_i^{\text{ice}}$. All degenerate computed bands have been intensity averaged (see Section 2.2 for details). Modes that are originally infrared active for a \mathcal{D}_{6h} symmetry are shown in bold. Experimental shifts are computed using the experimental values reported for the gas-phase in Table S2 and the theoretical values are computed similarly using the gas-phase values obtained for the corresponding level of theory.

Mode [\mathcal{D}_{6h} label]	Harmonic		Anharmonic	Hagen et al. (1983)	Dawes et al. (2018)
	PBE-D3	PBE-D3	CCSD(T) + PBE-D3		
11 [A_{2u}]	+44	+37	+41	–7	–
10 [E_{1g}]	+97	+99	+93	–13	–11
17 [E_{2u}]	+100	+155	+151	–10	–22
12 [B_{1u}]	+4	+9	+11	–2	–1
18 [E_{1u}]	+40	+48	+49	+3	+3
15 [B_{2u}]	+10	+19	+24	0	0
9 [E_{1g}]	+56	+33	+35	+2	+1
14 [B_{2u}]	–6	–3	–13	+4	–3
19 [E_{1u}]	+26	+30	+33	+6	+6
8 [E_{1g}]	+108	+147	+148	+16	+15
20 [E_{1u}]	+21	+27	+39	+14	+14
7 [E_{1g}]	+22	–7	+18	+7	–
2 [A_{1g}]	+19	+57	+50	+5	+4
Average, ($\Delta\nu$)	+42	+50	+52	+2	+1
RMSD	+55	+71	+71	+8	+10

at 3063 cm^{-1} and indicate the ν_2 band as a possible shoulder around 3051 cm^{-1} . Based on the later work of Dawes et al. (2018) and our own calculations, it seems more likely that the peak at 3069 cm^{-1} in Hagen et al. (1983) corresponds to ν_2 as it is a stronger intensity carrier than ν_{13} .

Analysing the computational results from Table 3, we see that the strong bands are qualitatively well described by all models. The harmonic approximation underestimates slightly the bands below about 1200 cm^{-1} (ν_{11} , ν_{10} , ν_{17} , ν_{12} , ν_{18} , ν_{15} , and ν_9) and overestimates the C–H stretching bands (ν_{20} , ν_7 , and ν_2). This indicates that a global scaling of the harmonic frequencies (often used to account for anharmonicity in an empirical fashion, see also Kesharwani, Brauer & Martin 2015) is unlikely to lead to a satisfactory agreement here. The largest deviations from the experimental data of Hagen

et al. (1983) are seen for bands ν_{10} (123 cm^{-1}), ν_{17} (129 cm^{-1}), and ν_8 (102 cm^{-1}), with slightly larger deviations compared to Dawes et al. (2018). Overall, the harmonic approximation has an RMSD of 49 cm^{-1} for the original gas-phase IR active modes (ν_{11} , ν_{18} , ν_{19} , and ν_{20} , shown in bold in Table 3) and 68 cm^{-1} for all observed bands, compared to the data of Hagen et al. (1983).

The anharmonic approach underestimates all bands apart from ν_{14} . This is more pronounced for the PBE-D3 surface, with the largest deviation for ν_{10} (113 cm^{-1}), ν_{17} (179 cm^{-1}), ν_8 (166 cm^{-1}), ν_{20} (112 cm^{-1}), ν_7 (107 cm^{-1}), and ν_2 (144 cm^{-1}). Note that all C–H stretches are underestimated by over 100 cm^{-1} for this surface, similarly to the PBE-D3 results for gas-phase benzene. We see the RMSD increase for this PES to 72 cm^{-1} for the original IR active bands and 100 cm^{-1} for all observed bands.

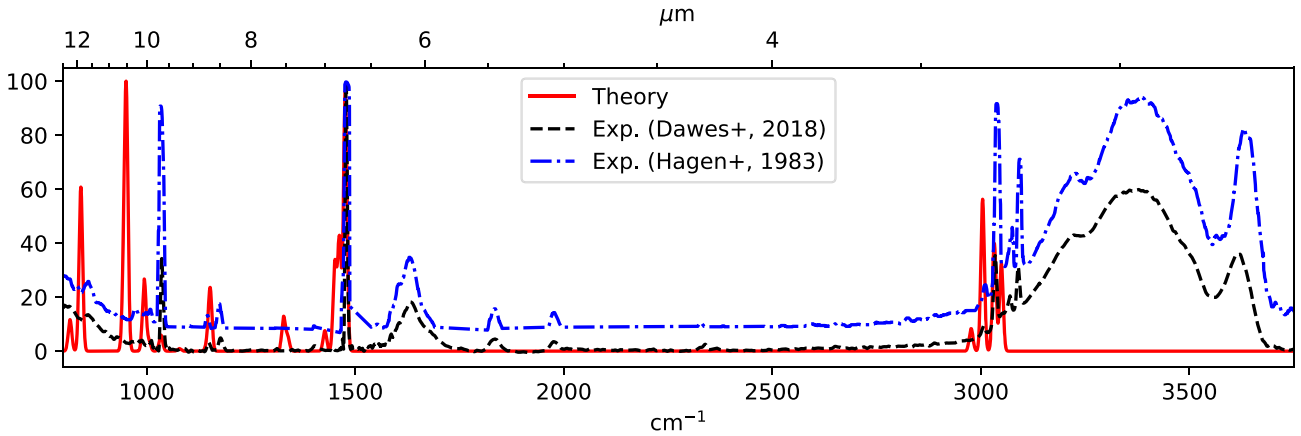


Figure 4. Comparison between simulated the IR spectrum for benzene on ferroelectric proton-ordered hexagonal crystalline water ice (XIh) surface model of this work (plain red trace); the experimental data from Dawes et al. (2018) (dashed black trace); and a digitized version of Hagen et al. (1983) (dot-dashed blue trace). See Section 4.2 for computational details. All spectra are normalized so that their largest intensity peak corresponds to 100 per cent. The digitized trace was obtained from Hagen et al. (1983) using WebPlotDigitizer on their fig. 4 and, to compensate for artefacts in the digitization, shifted by $+23 \text{ cm}^{-1}$ to match the reported values for benzene on ice in their table V. Our shifted version of the digitized spectrum from Hagen et al. (1983) is available as a CSV file in supplementary material.

Our hybrid PES improves the situation significantly by providing a ‘steeper’ PES that closes some of the gaps between theory and experiment. The overall agreement is now much improved, with an RMSD of 21 cm^{-1} for the original IR active bands and 56 cm^{-1} for all observed bands, outperforming both the PBE-D3 surface and the harmonic approximation. The largest deviations are seen for bands ν_{17} (134 cm^{-1}) and ν_8 (113 cm^{-1}). All C–H stretching bands are improved by an order of magnitude compared to the PBE-D3 PES data.

We compare our best first-principle model spectrum with that of Hagen et al. (1983) and Dawes et al. (2018) in Fig. 4. The simulated spectrum is obtained from the hybrid vibrational frequencies and PBE-D3 intensities shown in Table S3 convolved with a Gaussian lineshape with 5 cm^{-1} half-width at half-maximum, which mimics the linewidth of Hagen et al. (1983). We see that our predicted spectrum agrees qualitatively very well with experiment, displaying a structure for the C–H stretching bands similar to that observed experimentally. The strong band just below 1500 cm^{-1} (ν_8 and ν_{19}) is well reproduced along with other low-frequency peaks. The overall spectrum is red shifted in parts for reasons discussed later, but overall it provides a suitable guide to explore the nature of the bands observed for benzene on an ice surface.

Fig. 5 shows the intensity and position of all computed IR visible peaks for benzene on ice (top) and gaseous benzene (bottom), using data from both Tables S2 and S3. This qualitative figure emphasizes how the number, position, and relative intensities of the peaks change when the benzene is adsorbed on a water ice surface compared to when it is its gaseous form. Our anharmonic model captures correctly the overall shape and spectral changes going from gas-phase benzene, with only four active infrared bands, to adsorbed benzene on ice that displays approximately 13 bands in the infrared. Moreover, we see the overall intensity pattern shifts from a dominating ν_{11} band in gas-phase benzene (used as identification fingerprint in CRL618 by Cernicharo et al. 2001, for example) to several high-intensity carriers for adsorbed benzene (ν_8 and ν_{19} , for example).

The near-global underestimation of the vibrational bands for the anharmonic calculations are likely an indication of the strength of the interaction between benzene and the ice surface. Indeed, the stronger the interaction, the more affected the vibrational modes are and, consequently, the more red shifted (lower frequency) they will

be. As the benzene–ice interaction is computed at the same level of theory for all models (using PBE-D3), we expect the trends observed to have a common source. The PBE-D3 approach has been shown to overestimate the binding energy of molecules on surfaces (Reckien, Eggers & Bredow 2014 for benzene adsorption on metal surfaces, for example) which could explain the excessive red shift seen in our theoretical values.

In order to gain further insights into the influence of surface adsorption on the vibrational spectrum of benzene, we computed the frequency shift, $\Delta\nu$ resulting from adsorption. We define this frequency shift as

$$\Delta\nu_i = \nu_i^{\text{gas}} - \nu_i^{\text{ice}}, \quad (10)$$

where ν_i^{gas} is the frequency of band ν_i for benzene in the gas-phase and ν_i^{ice} that for adsorbed benzene. The experimental shifts are computed using the values of Hagen et al. (1983) and Dawes et al. (2018), along with the corresponding experimental frequencies for gas-phase benzene (see Table S2). Our results are shown in Table 4. We observe a slight blue shift (adsorbed benzene bands occurring at higher frequencies) for out-of-plane bands (ν_{11} , ν_{10} , and ν_{17}), while most other bands are either weakly affected (ν_{12} , ν_{18} , ν_{15} , ν_9 , and ν_{14}) or red shifted by up to $+16 \text{ cm}^{-1}$ (ν_{19} , ν_8 , ν_{20} , ν_7 , and ν_2). Blue shifting is consistent with a stiffening of out-of-plane modes for an adsorbed molecule that vibrates against a fixed (slightly repulsive) surface (e.g. normal mode corresponding to ν_{11} shown in Fig. 2 B, and also Zamirri et al. 2018 for a similar observation for CO on water ice). Red shifting, on the other hand, is indicative of an attractive interaction between benzene and the water molecules, typically through hydrogen bonding (see e.g. Mukhopadhyay, Cole & Saykally 2015 for similar observations for the water dimer).

Our theoretical shift values are computed similarly using the gas-phase values obtained for the each corresponding level of theory. The vibrational shift provides an information that is typically more reliable than absolute frequency values. Indeed, taking the frequency difference can cancel systematic method issues, as long as both gas-phase and adsorbed frequencies are computed using the same method (see also Michoulier et al. 2020 where a similar approach is used to explore water ice OH-stretch shifts). Here, we see that all

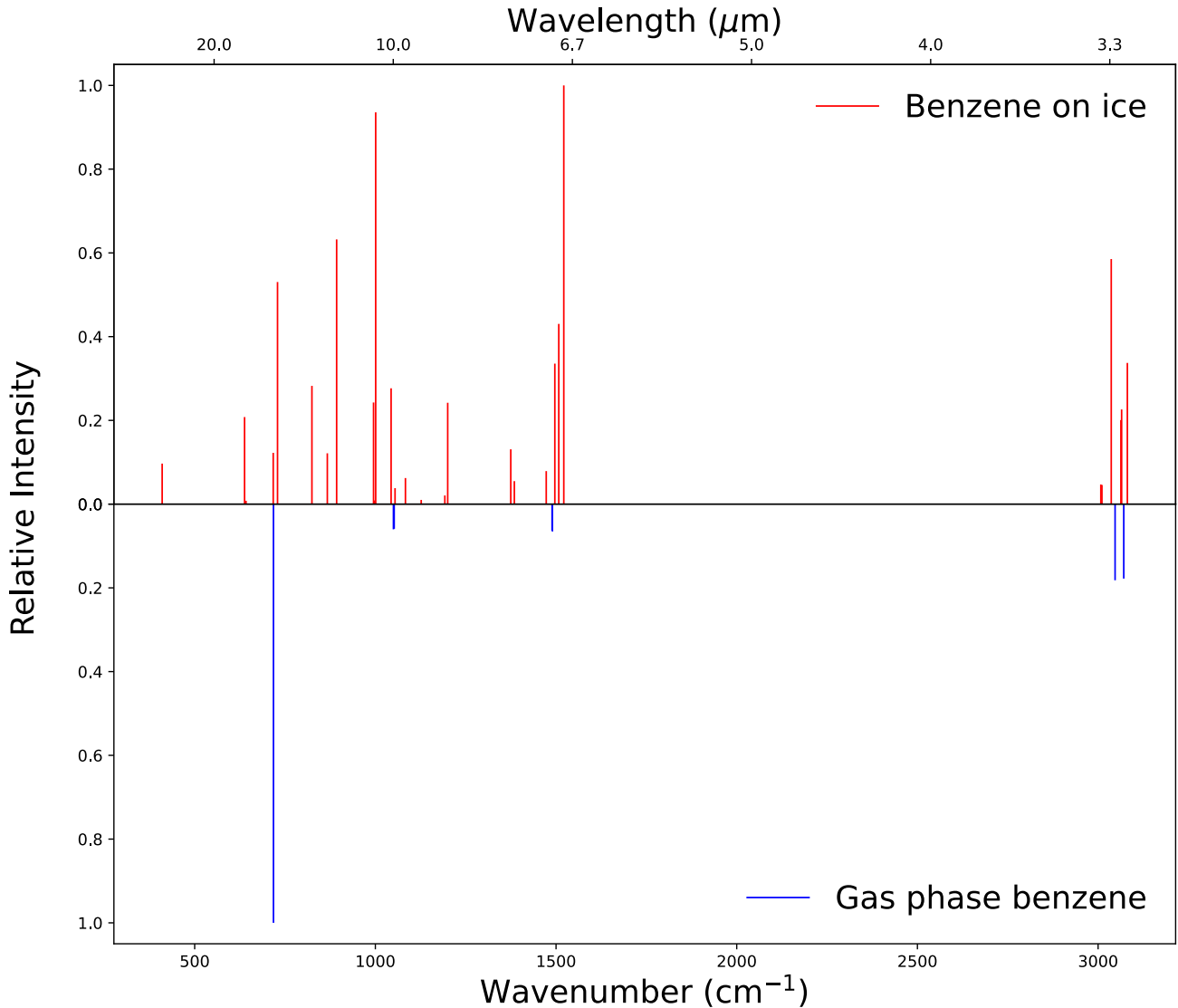


Figure 5. Relative intensities and frequencies of the IR visible transitions for benzene adsorbed on to ice surface (top, red) and gaseous benzene (bottom, blue). The stick spectra are generated using data from both Tables S2 and S3. It is clear that the number, position, and relative intensities of the IR peaks change drastically when the benzene is adsorbed on to a model ice surface.

three theoretical approaches show a much larger shift than the two experimental studies.

Interestingly, we notice that all three models follow a similar pattern with mostly positive shifts [i.e. frequencies are lower (red shifted) for adsorbed benzene compared to the gas-phase] apart from $\Delta\nu_{14}$ which is slightly negative. The anharmonic PBE-D3 results also display a negative shift for ν_7 , likely due to the issues mentioned earlier regarding the description of stretching modes in pure DFT. One particular qualitative feature is that the low-frequency out-of-plane blue shifts observed experimentally are not reproduced by any of the approaches. The remaining modes, however, mirror roughly the experimental trend albeit with a much larger magnitude.

To investigate the overall magnitude of the deviations, we explore the average shift, $\langle\Delta\nu\rangle$, and RMSD for all reported vibrational shifts in Table 4. The harmonic model has an average shift of $+42\text{ cm}^{-1}$ and corresponding RMSD of $+55\text{ cm}^{-1}$. Similarly, the anharmonic model provides an average of $+50\text{ cm}^{-1}$ with the PBE-D3 surface ($+71\text{ cm}^{-1}$ RMSD) and a $+52\text{ cm}^{-1}$ for the hybrid

surface ($+71\text{ cm}^{-1}$ RMSD). Those average shifts are to be compared with much lower $\langle\Delta\nu\rangle$ for the experimental data ($+2\text{ cm}^{-1}$ for Hagen et al. 1983 and $+1$ for Dawes et al. 2018) and RMSD values ($+8\text{ cm}^{-1}$ and $+10\text{ cm}^{-1}$, respectively). Here again, we see that either measure (average or RMSD) of the shift magnitude is much larger for the models than what is computed for the experimental data. This is another indication that the interaction of benzene with the ice surface is likely overestimated by the PBE-D3 approach. Another possible explanation is that our model represents the most binding version of an ice surface, while the experiments were performed using low-temperature deposited disordered ice layers (amorphous structured water, ASW) that is likely less strongly interacting with benzene.

5 CONCLUSION

In this paper we have presented a hybrid approach to calculating the vibrational signatures for a system of benzene adsorbed on

to a water ice surface by using a combination of CCST(T) and PBE-D3 in an ONIOM-like procedure. We compare the results of our hybrid method with the latest experimentally recorded spectra and calculations performed using either harmonic or anharmonic methods using a PBE-D3-only PES. When used for gaseous benzene calculations, the hybrid approach achieved an RMSD for IR active modes of 24 cm^{-1} , compared to 55 cm^{-1} and 31 cm^{-1} for the anharmonic and harmonic PBE-D3-only approaches, respectively.

We used a proton-ordered ferroelectric XIh water ice surface model consisting of 288 water molecules arranged in four double-layers of H_2O molecules, and our hybrid calculated spectrum for benzene on ice agrees well with the experimentally measured spectra of Hagen et al. (1983) and Dawes et al. (2018) on ASW, resulting in an RMSD for IR active modes of 21 cm^{-1} , compared to 72 cm^{-1} and 49 cm^{-1} for the anharmonic PBE-D3 approach and the harmonic PBE-D3 approaches, respectively. Our hybrid approach remains relatively ‘low-cost’ compared to a full correlation treatment and thus is suitable for the investigation of larger aromatic species on water ice surfaces.

We have also shown the importance of including a water ice surface into spectroscopic calculations that lead to differences in vibrational modes, vibrational frequencies, intensities and number of transitions seen in the IR spectrum. The overall intensity pattern of the spectrum changed from a being dominating by the ν_{11} band in gas-phase benzene to showing several high-intensity carriers for adsorbed benzene. To facilitate the cross-assignment between vibrational modes of gaseous benzene versus benzene on an ice surface, we have analysed the overlap between each set of normal modes and generated a correspondence graph.

We calculate the frequency shifts, $\Delta\nu$, of adsorbed benzene relative to its gas-phase for both experimental data and our theoretical models. We show that, while there is a reasonable common agreement between harmonic and anharmonic approaches, the underlying description of the benzene–water interactions at the PBE-D3 level is likely too strong and leads to an excessive red shift for all methods.

Finally, both sets of IR measurements were performed on ASW ice but we find here that there is a surprising agreement with our computed highly ordered crystalline ice data. This implies either that the simple ordered model that we developed describes realistically the local environment experienced by benzene on ASW (i.e. on a local scale, the binding mode of benzene in ASW resembles that of ice XIh). We are currently exploring this avenue further and will report our findings in a future publication.

ACKNOWLEDGEMENTS

We thank Dr Anita Dawes (The Open University, UK) for generously providing experimental data used in this work. We acknowledge the Viper High Performance Computing facility of the University of Hull and its support team.

REFERENCES

Acke B., van den Ancker M. E., 2004, *A&A*, 426, 151
 Akima H., 1996, *ACM Trans. Math. Softw.*, 22, 362
 Arakawa M., Kagi H., Fukazawa H., 2009, *ApJS*, 184, 361
 Augspurger J. D., Dykstra C. E., Zwier T. S., 1992, *J. Phys. Chem.*, 96, 7252
 Balint-Kurti G. G., Ward C. L., Clay Marston C., 1991, *Comput. Phys. Commun.*, 67, 285
 Benoit D. M., 2015, *J. Phys. Chem. A*, 119, 11583
 Benoit D. M., Chavagnac A. X., Clary D. C., 1998, *Chem. Phys. Lett.*, 283, 269

Benoit D. M., Madebene B., Ulusoy I., Mancera L., Scribano Y., Chulkov S., 2011, *Beilstein J. Nanotechnology*, 2, 427
 Brodersen S., Langseth A., 1956, *The Infrared Spectra of Benzene, Sym-benzene-d3, and Benzene-d6*. E. Munksgaard, Copenhagen
 Brodersen S., Langseth A., 1959, *Kgl. Dan. Vidensk. Selsk., Mat.-fys. Skr.*, Vol. 1. Univ. of Copenhagen, Copenhagen, p. 7
 Cernicharo J., Heras A. M., Tielens A. G. G. M., Pardo J. R., Herpin F., Guélin M., Waters L. B. F. M., 2001, *ApJ*, 546, L123
 Chergui M., 1996, *Femtochemistry: Ultrafast Chemical and Physical Processes in Molecular Systems*. World Scientific Press, Singapore
 Christiansen O., Stanton J. F., Gauss J., 1998, *J. Chem. Phys.*, 108, 3987
 Chulkov S. K., Benoit D. M., 2013, *J. Chem. Phys.*, 139, 214704
 Clark V. H., Benoit D. M., 2019, in Salama F., Linnartz H., eds, *Proc. IAU Symp. 15, Laboratory Astrophysics: From Observations to Interpretation*. Cambridge Univ. Press, Cambridge, p. 468
 Dapprich S., Komáromi I., Byun K., Morokuma K., Frisch M. J., 1999, *J. Mol. Struct.*, 461–462, 1
 Dawes A., Pascual N., Mason N. J., Gärtner S., Hoffmann S. V., Jones N. C., 2018, *Phys. Chem. Chem. Phys.*, 20, 15273
 Delsemme A., 1975, *Icarus*, 24, 95
 Dunning T. H., 1971, *J. Chem. Phys.*, 55, 716
 Dunning T. H., 1989, *J. Chem. Phys.*, 90, 1007
 Engdahl A., Nelander B., 1985, *J. Phys. Chem.*, 89, 2860
 Erlekam U., Frankowski M., Meijer G., von Helden G., 2006, *J. Chem. Phys.*, 124, 171101
 Faraday M., 1825, *Phil. Trans. R. Soc.*, 1, 440
 Fukazawa H., Hoshikawa A., Ishii Y., Chakoumakos B. C., Fernandez-Baca J. A., 2006, *ApJ*, 652, L57
 Geers V. et al., 2006, *A&A*, 459, 545
 Goedecker S., Teter M., Hutter J., 1996, *Phys. Rev. B*, 54, 1703
 Goodman L., Berman J. M., Ozkabak A. G., 1989, *J. Chem. Phys.*, 90, 2544
 Gotch A. J., Zwier T. S., 1992, *J. Chem. Phys.*, 96, 3388
 Hagen W., Tielens A. G. G. M., Greenberg J. M., 1983, *A&AS*, 51, 389
 Hirsch T. K., Ojamäe L., 2004, *J. Phys. Chem. B*, 108, 15856
 Hollenstein H., Piccirillo S., Quack M., Snels M., 1990, *Mol. Phys.*, 71, 759
 Hollinger A. B., Welsh H. L., 1978, *Can. J. Phys.*, 56, 1513
 Jensen H. B., Brodersen S., 1979, *J. Raman Spectrosc.*, 8, 103
 Jones B. M., Zhang F., Kaiser R. I., Jamal A., Mebel A. M., Cordiner M. A., Charnley S. B., 2011, *Proc. Natl. Acad. Sci.*, 108, 452
 Jung J. O., Gerber R. B., 1996, *J. Chem. Phys.*, 105, 10332
 Jurečka P., Šponer J., Černý J., Hobza P., 2006, *Phys. Chem. Chem. Phys.*, 8, 1985
 Kaiser R. I., Parker D. S., Mebel A. M., 2015, *Ann. Rev. Phys. Chem.*, 66, 43
 Kayi H., Kaiser R. I., Head J. D., 2011, *Phys. Chem. Chem. Phys.*, 13, 15774
 Kendall R. A., Dunning T. H., Harrison R. J., 1992, *J. Chem. Phys.*, 96, 6796
 Kesharwani M. K., Brauer B., Martin J. M. L., 2015, *J. Phys. Chem. A*, 119, 1701
 Keçeli M., Hirata S., Yagi K., 2010, *J. Chem. Phys.*, 133, 034110
 Koskinen T. T., Moses J. I., West R. A., Guerlet S., Jouchoux A., 2016, *Geophys. Res. Lett.*, 43, 7895
 Krack M., 2005, *Theor. Chem. Acc.*, 114, 145
 Lippert G., Hutter J., Parrinello M., 1997, *Mol. Phys.*, 92, 477
 Ma H., Ma Y., 2012, *J. Chem. Phys.*, 137, 214504
 McKinnon W. B., Hofmeister A. M., 2005, *Bull. Am. Astron. Soc.*, 37, 49
 Marston C. C., Balint-Kurti G. G., 1989, *J. Chem. Phys.*, 91, 3571
 Matsuura M. et al., 2004, *ApJ*, 604, 791
 Michoulier E., Toubin C., Simon A., Mascetti J., Aupetit C., Noble J. A., 2020, *J. Phys. Chem. C*, 124, 2994
 Miliordos E., Apré E., Xantheas S. S., 2016, *J. Chem. Theory Comput.*, 12, 4004
 Mukhopadhyay A., Cole W. T., Saykally R. J., 2015, *Chem. Phys. Lett.*, 633, 13

- Naumkin F. Y., Knowles P. J., 1995, *J. Chem. Phys.*, 103, 3392
- Neese F., 2012, *WIREs Comput. Mol. Sci.*, 2, 73
- Neese F., Valeev E. F., 2011, *J. Chem. Theory Comput.*, 7, 33
- Neese F., Hansen A., Liakos D. G., 2009, *J. Chem. Phys.*, 131, 064103
- Noble J., Michoulier E., Aupetit C., Mascetti J., 2020, *A&A*, 644, A22
- Perdew J. P., Burke K., Ernzerhof M., 1996, *Phys. Rev. Lett.*, 77, 3865
- Plíva J., Johns J. W. C., 1983, *Can. J. Phys.*, 61, 269
- Plíva J., Johns J., 1984, *J. Mol. Spectrosc.*, 107, 318
- Plíva J., Pine A., 1982, *J. Mol. Spectrosc.*, 93, 209
- Plíva J., Esherick P., Owyong A., 1987, *J. Mol. Spectrosc.*, 125, 393
- Plíva J., Johns J., Lu Z., 1996, *Mol. Phys.*, 87, 859
- Raza Z., 2012, Proton Ordering and Reactivity of Ice, Available at: <https://discovery.ucl.ac.uk/id/eprint/1369753/>
- Reckien W., Eggers M., Bredow T., 2014, *Beilstein J. Org. Chem.*, 10, 1775
- Respondek I., Benoit D. M., 2009, *J. Chem. Phys.*, 131, 054109
- Salama F., 2008, *Organic Matter in Space, Vol. 4*. Cambridge University Press, Cambridge, p. 357
- Salter T. L., Stubbing J. W., Brigham L., Brown W. A., 2021, *Frontiers Astron. Space Sci.*, 8, 28
- Salzmann C. G., 2019, *J. Chem. Phys.*, 150, 060901
- Schuhmann M. et al., 2019, *A&A*, 630, A31
- Scribano Y., Benoit D. M., 2008, *Chem. Phys. Lett.*, 458, 384
- Scribano Y., Lauvergnat D. M., Benoit D. M., 2010, *J. Chem. Phys.*, 133, 094103
- Senent M.-L., Palmieri P., Carter S., Handy N. C., 2002, *Chem. Phys. Lett.*, 354, 1
- Silva S. C., Devlin J. P., 1994, *J. Phys. Chem.*, 98, 10847
- Sivaraman B., Mukherjee R., Subramanian K., Banerjee S., 2014, *ApJ*, 798, 72
- Stephenson T. A., Radloff P. L., Rice S. A., 1984, *J. Chem. Phys.*, 81, 1060
- Suzuki S., Green P. G., Bumgarner R. E., Dasgupta S., Goddard W. A., Blake G. A., 1992, *Science*, 257, 942
- Szczepaniak K., Person W. B., 1972, *Spectrochim. Acta A*, 28, 15
- Tabor D. P., Kusaka R., Walsh P. S., Zwier T. S., Sibert III E. L., 2015, *J. Phys. Chem. A*, 119, 9917
- Thrower J., Collings M., Ruppen F., McCoustra M., 2009, *J. Chem. Phys.*, 131, 244711
- Ulusoy I. S., Scribano Y., Benoit D. M., Tschetschetkin A., Maurer N., Koslowski B., Ziemann P., 2011, *Phys. Chem. Chem. Phys.*, 13, 612
- VandeVondele J., Hutter J., 2007, *J. Chem. Phys.*, 127, 114105
- VandeVondele J., Krack M., Mohamed F., Parrinello M., Chassaing T., Hutter J., 2005, *Comput. Phys. Commun.*, 167, 103
- Visser R., Geers V., Dullemond C., Augereau J.-C., Pontoppidan K., van Dishoeck E., 2007, *A&A*, 466, 229
- Waite J. H., Young D. T., Cravens T. E., Coates A. J., Cray F. J., Magee B., Westlake J., 2007, *Science*, 316, 870
- Walsh C., Millar T. J., Nomura H., Herbst E., Weaver S. W., Aikawa Y., Laas J. C., Vasyunin A. I., 2014, *A&A*, 563, A33
- Weigend F., 2008, *J. Comput. Chem.*, 29, 167
- Weigend F., Häser M., 1997, *Theor. Chem. Acc. (Theoretica Chimica Acta)*, 97, 331
- Wishnow E. H., Gush H. P., Ozier I., 1996, *J. Chem. Phys.*, 104, 3511
- Wójcik M. J., Gług M., Boczar M., Boda Ł., 2014, *Chem. Phys. Lett.*, 612, 162
- Woods P. M., Willacy K., 2007, *ApJ*, 655, L49
- Zamirri L., Casassa S., Rimola A., Segado-Centellas M., Ceccarelli C., Ugliengo P., 2018, *MNRAS*, 480, 1427

SUPPLEMENTARY INFORMATION

Supplementary data are available at *MNRAS* online.

Table S1. Gas-phase C–H stretching bands convergence with increasing number of allowed mode excitations (2-modes: SD, 3-modes: SDT, and 4- modes: SDTQ).

Table S2. Vibrational frequencies of isolated benzene.

Table S3. Vibrational frequencies of benzene on ice.

Please note: Oxford University Press is not responsible for the content or functionality of any supporting materials supplied by the authors. Any queries (other than missing material) should be directed to the corresponding author for the article.

This paper has been typeset from a $\text{\TeX}/\text{\LaTeX}$ file prepared by the author.